

MICROFILMED - 1983



# A NEW SYSTEME OF THE MATHEMATICKS:

CONTAINING

- ARITHMETICK, as well NATURAL and DECIMAL, as in *Species*, or the *Principles* of *Arithmetic*.
- II. Practical GEOMETRY, together with the first Six Books of *Euclid's ELEMENTS*, as also the *Eleventh* and *Twelfth*, symbolically demonstrated.
- III. TRIGONOMETRY PLAIN and SPHERICAL.
- IV. COSMOGRAPHY, or a DESCRIPTION of the HEAVENS.
- V. NAVIGATION, or SAILING by a *Plain* or *Mercator's Chart*; as also by the *Arch* of a *Great Circle*, &c.
- VI. The DOCTRINE of the SPHERE, grounded on the *Motion* of the *Earth*, according to the *Old Pythagorean* and *Copernican Systeme*.
- VII. *Astronomical TABLES*, with *Tables* of *Logarithms*, *Natural* and *Artificial Sines* and *Tangents*, and *versed Sines*.
- VIII. A NEW GEOGRAPHY, or a *Description* of the most *Eminent Countries* and *Coasts* of the *WORLD*, with *Maps* of them, and *Tables* of their *Latitude* and *Longitude*.

Composed by Sir JONAS MOORE Knight,  
Late Surveyor General of His MAJESTY's Ordnance, and  
Fellow of the ROYAL SOCIETY:

And designed for the Use of the Royal Foundation of the Mathematical  
SCHOOL in CHRIST-HOSPITAL.

By His MAJESTY's special Command.

LONDON,

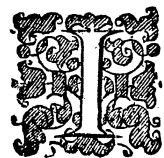
Printed by A. GALE and J. HODGKIN for ROBERT SCOTT,  
Bookseller in Little Britain, M. DC. LXXXI.

Royal  
Astronomical  
Society.



# TO THE KING.

*May it please Your Majesty,*



*T*is not from any forgetfulness of the  
Reverence due to Your Sacred  
NAME, that the Publishers of  
this Treatise have presum'd to  
give it this Dedication; they well  
knowing, how much better it had suited with their  
humble state, could it as well have stood with  
their Duties, to have sought for Patronage  
from any lower, or (indeed) other Hand than Your  
MAJESTY'S, to a Work, not only undertaken by  
Your immediate Command, and by a Person, who  
held it his highest Honour, and no less Happiness,  
to have the most valuable part of his Life exer-  
cis'd and finish'd in Your Majesty's Service; but  
destin'd also to the particular use of that part of  
Your Royal Care, the Children of Your Own

a

Mathe-



## The Epistle Dedicatory.

Mathematical Foundation in CHRIST'S-Hospital: Which, by the Munificent Provision Your Majesty has made for the Improvement of Naval Knowledge, and the necessary Advantages of Maritime Dominion and Commerce, depending thereon, will let Posterity see how much more it owes on that Subject to Your single Name, than to the united Performances of all Your Royal Ancestors.

In contemplation whereof, and of our Duties therein paid to Your MAJESTY, as well as Respect to the Memory of Your Servant, our late honoured Father-in-law, Sir JONAS MOORE, its Author: We do in all humility lay this our Collection of his Labours therein at Your Sacred Feet, being,

(May it please Your Majesty)

Your Majesty's most loyal and  
obedient Subjects and Servants,

WILLIAM HANWAY,  
JOHN POTENGER.



## THE PREFACE.

**S**IR JONAS MOORE, the Author of the ensuing WORK, was a Person, who, by his eminent and known skill in the Mathematics, had attain'd to very considerable Employments in his MAJESTIES Service. Some Years before his Death, he was chosen one of the Governours of Christ's-Hospital, LONDON, whereupon considering with himself the Advantage and Benefit, which the Nation might reap from a Mathematical School, if duly managed, he made it his earnest business to promote the improvement of it. His MAJESTY had of his own Bounty, and by the Mediation of His Royal Highness, then Lord High Admiral of England, been pleas'd to Order a liberal Allowance, for the Maintenance of a Select number of the ablest and

a 2                      fittest



## THE PREFACE.

finest Youths of the said *Hospital*, to be Annually chosen, as also for that of a Master, to instruct them, in such Parts of the *Mathematics* as are requisite in a Skilful *Sea-man*.

The *School* was settled; but there still wanted a Methodical *Institution*, from which the Youths might receive such necessary helps as their Studies required. A laborious Work! from which the great and assiduous Employments of Sir *Jonas* might justly have exempted him, had he not made this reflection, That he could not have better bestow'd the spare Hours of his declining Age, or done a thing more acceptable to His MAJESTY (to whose Service he had Dedicated his All) than by contributing what lay in his power to the improvement of so hopeful a Seminary of Sea-men.

Having thus engag'd himself in the prosecution of this generous design, the first thing to be determin'd was his *Method*. The whole ensuing Work he resolv'd to divide into *Four Parts*. The first of those should comprehend the *Rules and Principles of Arithmetic, Vulgar, Decimal, and Logarithmical; Practical Geometry, Trigonometry Plain, and Spherical; Cosmography, and Navigation*: And that the other Three Parts should consist of a Volume of *Astronomical Tables*; a concise *Geography*, something of *Astronomy, Algebra*, and the most useful Books of *Euclid's Elements*. But in what Order these Three last were to succeed each other, appears not otherwise, than that the *Algebra*, and *Euclid*, were to Compose the last Part; whence it may be collected, that the *Tables of Geography and Astronomy*, were to make up the two middle Parts.

The

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The *Arithmetic, Practical Geometry, Trigonometry, and Cosmography* were writ by Sir *Jonas* himself, and Printed during his Life time. In which, if the *Style and Method* shall, by some, be thought not so exact, as might have been expected from a Person of his great repute; Or if the occasional *Repetitions* of his Principal Rules, and Applications to the Youths of the *Mathematical School*, shall be censur'd as a blemish to his Work, it may be answer'd for him, That intending them chiefly for the Instruction of the said Youths, he concluded nothing would more engage their diligence, than such familiar Addresses to them, and that accordingly, such *Repetitions* may be of good use. For tho' Persons of riper Years, and more mature Judgments may, upon the first perusal, understand what they Read; yet when such green wits are to be Taught, there is a necessity of repeating and reinculcating the Ground-work Rules, and Principles, upon every occasion.

Whilst the forementioned Part was passing through the Press, Sir *Jonas* had procured the *Algebra*, with the first Six Books of *Euclid's Elements*, as also the Eleventh and Twelfth, to be done by Mr. *Perkins*, the then Master of the *Mathematical School*. The *Figures*, which he appointed to be us'd, were those of *Melder*, and, where he ended, those of Dr. *Barrow*, whose Method he required to be every where follow'd. The Volumes of *Tables* were Printed off; the *Tables* for the *Geography* all Collected by himself; the *Maps* were Engraved; as also the *Plates with Prospects* for Part of the Work. But the *Tables and Directions*, for Calculating the Place of the *Luminaries*, and *Eclipses*, were communicated by Mr. *Flamsted*.

Sir



## THE PREFACE.

Sir *Jonas* was ready to enter upon the Chapter of *Navigation*, and conceiv'd himself within view of the much desired Conclusion of his Work, when it pleas'd the Divine Providence, by Death, to put a Period to his Labours; which happen'd answerably to his own desire, to wit, that of ending his days in his MAJESTY'S Service.

The Author's known Abilities had rais'd a great expectation of the coming forth of this Work. Many Persons, but more especially the Learned Sir *Charles Scarborough*, and *Samuel Pepys* Esq; with others, the Governours of the *Hospital*, were very Sollicitous to have it Published. But upon Sir *Jonas's* Decease; all was at a stand, for many Months; till such time as his Son-in-law, Mr. *Hanway*, came over from *Ireland*, and vigorously concern'd himself in hastening the Publication of this useful and much-desired Work. His Endeavours therein were seconded by those of Mr. *Potenger*, another Son-in-law of Sir *Jonas's*; they being resolv'd, what ever pains or Charges they were at, to see it perfected. Some Part of the *Geographical* Plates had been, by the mutual consent of the Parties concern'd therein, deliver'd into the Hands of the *Hospital*. But when the Workmanship thereof came to be examin'd, it was found, that great faults were committed in them by the Engraver. The *Tables* and *Discourse* belonging thereto were imperfect. Nothing of the intended *Navigation* (of Sir *Jonas's*) could be met withall. Whereupon it was agreed, that Mr. *Edmund Halley* should be intreated to peruse the *Geography*, and to add what was wanting in it; which he willingly undertook. An Explication of the *Copernican Hypothesis* was

## THE PREFACE.

was promis'd by Mr. *Flamsted*; and Mr. *Perkins*, who was like to be most concern'd with it, undertook the *Navigation*: Mr. *Hanway* and Mr. *Potenger*, making it their Province to have the Plates necessary for each Part, Engraved, as they were Transmitted to them, defraying the Charges thereof, and urging all convenient Expedition both from the Press, and the Undertakers.

The Work being thus carry'd on with great vigour, the *Doctrine of the Sphere* was first finished, and Printed off; then the *Geography*; and Mr. *Perkins* had but just compleated the *Navigation*, when it pleas'd God, to conclude his Life with his Work, and to deprive the School of an able and diligent Master. Of the said Chapter of *Navigation*, it may reasonably be affirm'd, That it has the advantage of any other Treatise Published upon that Subject. Within the Compass of some few Pages, he hath, with great perspicuity, Taught the three several sorts of *Sailing*, viz. by the *Plain Chart*, *Wright's*, or *Mercators*, and the Arch of a great Circle. He hath shewn, how the usual Propositions in each may be wrought either *Arithmetically*, *Geometrically*, or by the *Gunter's-Line*. To which he hath added a new and a very easy Method of keeping the true reckoning of a Ship's way; the Description of such Instruments as are most approv'd, for Observations at Sea; together with the ways of Observing therewith. And in the use of the *Azimuth-Compass*; he hath been very express, and more copious than usual; for this reason, that our Seamen account the finding of the *Variation* one of the most difficult things in their practice. His Method seems every where the same which



## THE PREFACE.

which he used in his *School*; and it is not to be doubted, but that his Successors will find it both most instructive to their Disciples, and easy to themselves.

After this short account of the Work, and the accidents which retarded its coming abroad at the time it was at first design'd, this may be further added, That whereas the Author makes Mention of a Preface of his own Writing, wherein he had advertis'd the Youths of the necessity of *Arithmetic*, and other Parts of the *Mathematics* in their Studies, there was not any thing of that kind found after his Decease. So that, for what is done by way of Preface, the Public is oblig'd to the present Editors of this Work, Mr. *Hanway* and Mr. *Potenger*, his Sons-in-law. But with a more particular Acknowledgment to the *former*, for his great Care, Pains, and expence in promoting it, not without extreme detriment to his Affairs elsewhere.

THE

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ERRATA.



Page.	ERRATA.	Page.	ERRATA.
210	FOR <i>Dwillions</i> , read <i>Millions</i> .	124	For <i>Phenomena</i> , read <i>Hypotheses</i> .
3	For out of the, read under the.	13	For to consider, read <i>supposes</i> .
24	For one, read the one.	15	For to conceive, read <i>conceives</i> .
24	From the bottom of the Page, for only that, read only note that.	21	For but 2 <i>Degr.</i> read near 3 <i>Degrees</i> .
50	For be both a Right-Angle, read taken both together be equal to one Right-Angle.	125	Blot out <i>Phenomena</i> or.
53	For by a Right-Angled Triangle, read by turning a Right-Lined Triangle about its Axis.	135	For 29 Days and some odd Minutes, read 29 Days 12 Hours and some odd Minutes.
11	For comprised of, read comprehended by.	45	For 12 Minutes, read 49 Minutes.
56	For 335, read 355.	137	For <i>Yess</i> , read <i>Years</i> .
11	For 335, read 355.	141	For C D, read C B.
39	For p l, read p d.	15	For C A C, read C A B.
69	For C D E and H B E, read C B D, and F B G.	142	For 30 Minutes, read 25 Minutes.
19	For B G E, read B G F.	143	For <i>Refractiō</i> , read <i>Refractiō</i> .
70	For Figures 6, and 10, read Figure 7, and 10.	21	For <i>Ecliptick</i> , read <i>Equator</i> .
31	After B C D add Figure 14.	149	In the Margin put Fig. 2, page 103.
71	After as if, put in (Figure 15).	150	For of <i>Middleaven</i> , r. of the <i>Middleaven</i> .
71	From the bottom, for D E B read C E B, and for B C D, read B D C.	158	For <i>Artib Sine</i> , read every where and <i>Arith Compl. of the Sine</i> .
73	For C I B, read C F H.	159	For <i>Fibration</i> , read <i>Libration</i> .
74	For C a, read c a.	172	For $\frac{1}{2}$ , read $\frac{1}{3}$ .
79	For ascribed, read inscribed.	174	For 30 36 read 30 56.
81	For C A, read B A.	21	For 53 16 read 53 26.
85	For b, read d.	177	For A and C the, read A and C the.
91	After, from x to s, add 105°.	158	For lay 70 from A to B, read lay 51 from A to B.
86	For all the second and third Terms, read add the Logarithms of the second and third Terms.	186	For 43 34 read 36 05.
89	For D A, read B A.	8	For 74.4 read 86.4
99	For a b i, read a b f.	196	In the Figure through B draw a Line Parallel to A C, and mark it F G.
34	For from t to i, read from f to i.	2	From the bottom for 7 read 8, and in the last for 5, read 6.
104	From the bottom, for B A, r. C A.	197	For in b and l, read in e, and after from e to n, add, draw n l Parallel to C c.
106	Rule 5, Line 29. read Co-f. B. R. ∴ Co-t. B C. Co-t. B A.	209	After <i>Tangent</i> whereof is, add omitting the Characteristick.
116	For As Radius, Co-t. B A ∴ Co-f. B. Tang. B A, read it As Co-f. B. Radius ∴ Co-t. B C. Co-t. B A.	17	In the Figure, through E draw E F Parallel to E C.
110	For Sines, read Signs.		

Note, that in the Figure Page 283. all the small Letters *f, g, h, i, m, p, r, s, d, y, λ*. mentioned in the following page, are wanting, whose places may be found, and themselves inserted by the Method prescribed and used in the Figure next preceding it.



# CHAP. I. Of ARITHMETICK.

## PREFACE.

Y On (the Children of the Royal Foundation) have been told in the Epistle, that the Method intended for this work requires, first, to lay down some short Introduction for Arithmetick, to the end you may have wherewith to mind you for the Practice thereof, if it happens you forget any of the Rules. I shall not need to enforce any Arguments, to perswade you to be ready and dextrous therein, for that the universal use thereof, whether you be at Sea or Land, requires it; and if you should be but excellent herein, with fair Writing, it is enough to prefer you, if you had no other Art besides. It is the great Difference that distinguishes us from Brutes and brutish Men, it changes our Natures, sharpens our Understandings, and prepares us for Business. I divide all into Sections and Propositions, as followeth.

## SECTION I. Of the Common Parts of Arithmetick.

### § 1. Of Simple Numeration.

S Imple Numeration consists in the Distinction, in the Estimation, and Pronunciation of Numbers. Every Place towards the left hand being ten times more than the Place on the right, or in decuplo proportion, therefore if any Number of Figures be given, to declare or pronounce what Number it is, first distinguish the whole into Periods, beginning



ginning with Unity, and taking three Places to each *Period*, as you may see by the Example following.

The Characters are 9, 8, 7, 6, 5, 4, 3, 2, 1, 0, whereof the last is Nullity, or Nothing, ora Cypher, the rest, 1 for Unity, 2 for Duality or Two, &c. Secondly, for the value ordinarily estimated, from the right hand as the first place for Units, the second for Tens, the third for Hundreds, Thousands, Tens of Thousands, Hundreds of Thousands, Millions, &c. The Estimation will be best by the Periods, the first being of Units, the second of Thousands, the third of Millions, the fourth Thousands of Millions, the fifth Millions of Millions or Dwillions, &c. and in every Period there being three Places, that to the right hand being Units, the middle Tens, and the third Hundreds; as 764, is Seven Hundred Sixty Four in the first Period; but in the second Period, it would be Seven Hundred Sixty Four Thousand; if in the third, Seven Hundred Sixty Four Millions, &c. So that, lastly, if this Number 7.345.596.712.345.082 were to be pronounced, having distinguished all into Periods, it would signifie Seven Thousand of Millions of Millions, Three Hundred and Forty Millions of Millions, Five Hundred Ninety and Six Thousand of Millions, Seven Hundred and Twelve Millions, Three Hundred Forty Five Thousands, and Eighty Two Units, of whatsoever be assigned.

### §. 2. Of Compound Numeration.

Numeration  
compound.

**N**umeration compounded contains the Rules of *Addition*, *Subtraction*, *Multiplication*, and *Division*, under which last may be comprehended *Extraction* of the *Square* and *Cube Roots*. The Rules shall follow briefly and in order, for Whole Numbers.

#### Rule I.

Addition.

**A**DDITION is the Invention of the Sum of two or more Numbers, and requires the Ordering of the Places so, as Units may stand under Units, Tens under Tens, &c. and then the Collecting every Column by it self, and if it fall out to be under Ten, to set it down; if above Ten, set down the odd Units, if there be any, and carry to the next Column so many Tens as the Number shall come to; as in these Examples.

16	34	756	5789	93256
72	68	382	3452	12700
88	102	568	7898	78250
		1706	3257	97662
			20396	15628
				297496

So

So if it be required to give the Sum of any Number of Goods, delivered at several times, viz. 50 at one time, 7 at another, 168 at another, and 72 at another, setting them down as before directed, you will find the Sum to be Two Hundred Ninety and Seven.

50  
7  
168  
72  
---  
297

#### Rule II.

**S**UBTRACTION is the Invention of the Difference of two Numbers, which are found by subscribing the lesser Number out of the greater, setting Units under Units, Tens under Tens, &c. then beginning with the last Figures towards the right hand, take the lesser from the greater, and set down the Remainder under that Figure. If the Figures be equal, set down a Cypher; if the higher be lesser than the lower, add Ten, or call it Ten more than it is, and be sure the next below be made One more, that is, if it be 2, make it 3; if 6, make it 7, &c. The Examples will make all easily.

18	756	8254	56748
15	431	6332	358784
Rem. 3	325	1922	208654

The Number to be subtracted, together with the Difference or Remainder, are equal to the Number from which the Subtraction was made, which is a good Proof for Subtraction; as in the third Example, 6332 and the Remainder 1922 makes 8254, the first Number.

The Proof of Addition is to divide the Parcels, and if the Sum of the Parts be equal to the Whole, all is right.

#### Rule III.

**M**ULTIPLICATION is but a Compendium of Addition, for the *Multiplicand* (which is the Number to be multiplied) is so often added to it self, as an Unit is contained in the *Multiplier* (which is the Number multiplying;) and so the *Product* is gotten (which is the Result of the Work.)

For the Multiplication of the smaller Figures, under 5, it is so easie, that any Child may do it, as 2 times 2 is 4, 3 times 4 is 12, &c. But for those higher, by the Table adjoining; they must be perfectly got by heart, so that forward, backward, or any ways they may be remembered.

B 2

This



5	5	25	7	7	49
	6	30		8	56
	7	35		9	63
	8	40		8	64
	9	45		9	72
6	6	36	9	9	81
	7	42			
	8	48			
	9	54			

This Table may be perfectly learn'd in six hours time, and left: Then for multiplying two or more Figures by one Figure, set down the Multiplicand, and by that one Figure (being the Multiplier) multiply all the Figures of the Multiplicand, remembering to carry in your mind for every Ten, One to the next place.

2123	Multiplier.	31567	38976
3	Multiplier.	7	9
6369	Product.	220969	350784

But if you multiply by more Figures than one, work as before, but set each several Product one place forward towards the left hand, and set the Unit-place exactly under the Figure you multiply, as in these Examples.

3576	32569	35000
263	527	7000
10728	227983	24500000
21456	65138	
7152	162845	
940488	17163863	

If there be Cyphers at the end either of Multiplicand or Multiplier, make the Multiplication in the Whole Numbers, and at last add so many Cyphers as there are Places of them in one or both, as in the last Example.

I should desire that the Boys should learn by heart all the Products of 12, as in the following Table, for they will have great use thereof.

2 times

2	times 12 is	24
3		36
4		48
5		60
6		72
7		84
8		96
9		108
10		120
11		132
12		144

## Rule IV.

**DIVISION** is a Compendium of Subtraction, for the Divisor is so many times contained in the Dividend, as there are Units in the Quotient; so that subtracting continually the Divisor from the Dividend, accounting an Unit for each time, the Sum of those Units is the Quotient.

The Dividend stands in the middle, betwixt the Divisor on the left hand, and the Quotient on the right, as in this Example.

In this Example, as in all others of this kind, I consider how many times 3 can be in 6, and find it 2 times, I set 2 in the Quotient, and multiply that 2 by 3 the Divisor, which makes 6, which I set under the first Figure 6, and subtracting one from the other the Remainder is 0. Then I put down 7, the next Figure of the Dividend, making a Point under it, and set it after 0; I demand how many times 3 can be in 7? and set 2 in the Quotient, then multiplying 2 by 3 makes 6, which I take from 7, and there remains 1; after which I add 5, the next Figure, making a Prick under it, and proceed as in the Example, finding the whole Quotient to be 2253, without any Remainder.

But if you be to divide two Figures, then the matter will be a little more difficult, and more care will be required to find fit Quotients: Wherefore I advise the young Scholar, that he may the better understand the Method of chusing due Quotients, to make a Table of all the several Multiplications of the Divisor to 9, by which he will perceive where the difficulty lyes, and after he has made his Quotient by the Table and without it, he will be perfect therein, and perceive his Work the better. Let the Dividend be 940488, the Divisor 263, whereof I make a Tariff or Table by doubling or Ad-

1	263
2	526
3	789
4	1052
5	1315
6	1578
7	1841
8	2104
9	2367

dition,



dition, as for 2 I double 263 and it makes 526, for 3 adding the first and second makes 789, for 4 I double the second, for 5 I add the second and third, for 6 I double the third, for 7 I add the third and fourth, for 8 I double the fourth, and for 9 adding the fourth and fifth makes 2367, which is 9 times 263.

First I find how far the Divisor will reach into the first Places of the Dividend, which will be to three Places, which is 940: Then I seek how many times 263 will be in 940, and by the Table, seeking for that Number or the next less to it, I find it 3 times, viz. 789, which I set under 940 of the Dividend, making a Point as before, and subtract, and it leaves 151; after which I add the next Figure of the Dividend 4, and make a Point under it; then I enquire how many times can 263 be in 1514, and the Table tells me no more than 5 times, viz. 1315, which I set down, subtract, and so proceed, till I have brought all the Figures of the Dividend down, and find the Quotient 3576, and no Remainder.

Thus by making such a Table *Division* is easily performed, but this is too tedious, and my Boys must not spare labour, but perform it by their memory and practice, after this manner: Let the same Example be set down.

Seek how many Figures the Divisor will require in the Dividend to be bigger than it self, viz. 940, there make a Point, and estimate how many times 2 can be in 9, having respect to the 6 that follows in the Divisor, for though you can have 2 four times in 9, yet four times 26, which is 104, is bigger than 94, therefore it can be but three times; set 3 in the Quotient, and multiply the Divisor 263 by it, and set it (viz. 789) to the first Prick, subtract it from 940, and after the Remainder set the next Figure in the Dividend, viz. 4; and so proceed till you have finished your Division.

After Division be finished, if any thing remain, it is set over the Divisor in form of a Fraction. If the Divisor hath Cyphers at the right hand, they may be omitted, and so many of the last Figures of the Dividend cut off, and so the Division to be made with the rest of the Figures.

## Rule V.

Bipartion.

**BIPARTION** or Halving, or dividing by 2, is perfectly to be practised, thus: Suppose 782358 be required to be halved; I begin, and say, the half of 7 is 3, and because 7 is odd, I say, the half of 18

is

is 9, the half of 2 is 1, the half of 3 is 1, the half of 15 is 7, and the half of 18 is 9, which is 391179. And it will be requisite, to learn to divide by 12 at once, as was done in *Multiplication* for that part.

The *Proofs of Multiplication and Division* are mutually tried by each other, for the Product being divided by the Multiplier gives the Multiplicand, and by the Multiplicand gives the Multiplier: So likewise if you multiply the Divisor by the Quotient (adding the Remainder of the Dividend, if any such were) the Product will be the Dividend.

Lastly note, That if the Quotient be equal to the Divisor, and that nothing remain, then is the Dividend a Square Number, and the Divisor is the Root. To Extract which, is the next Rule.

## Rule VI.

**A SQUARE NUMBER**, as before was said, has a Side or Root, *Extraction of the Square Root.* which multiplied by it self produceth that Square Number, as 49 is a Square Number whose Side is 7, for 7 times 7 is 49; and in the Table annexed all the Squares of the Digits to 9 are set down. But if the Number exceed, then the Rule is, *Make a Point over the last Figure, or Unit-place, and so of each other, the Number of those Points shews how many Places of Figures are to be the Quotient or Root:* As in the Example.

Go to the first Point on the left hand, which is 10; seek in the Table the next less Square, which is 9, and the Root set in the Quotient, which is 3; set 9 under 10, and subtract, rests 1, after which adding the two next Figures makes it 160: Now double the Quotient 3, and it makes 6, which set before 160 for a Divisor, and work as in Division; only note, that the Divisor when multiplied must not reach by one place so far as the Remainder; so 6 will be in 16 twice, I set 2 in the Quotient, and multiply it by 6, and it makes 12, which set under 16; then take the Square of 2, the last Figure in the Quotient, which is 4, and setting it under 0, makes in all 124, which subtracting leaves 36. Double the Quotient 32, and it makes 64 for the new Divisor, (which is every time to be repeated) which will be found five times in 361: Work as before, and as in Division, and the Root will be found 3256.

Roots.	Squares.	Cubes.
1	1	1
2	4	8
3	9	27
4	16	64
5	25	125
6	36	216
7	49	343
8	64	512
9	81	729

16661536	( 3256
9	
6	160
	124
64	3615
	320
	25
650	39036
	3900
	36
	000

Rule



## Rule VII.

Extraction of  
the Cube Root.

**A** CUBE NUMBER is such, whose Root multiplied by it self, and again the Product multiplied by the Root, produceth the Cube; as 343 is a Cube Number, whole Root is 7, for 7 times 7 is 49, and 7 times 49 is 343, and those Numbers in the former Table, under *Cubes*, are the Cubes of all the Digits to 9, and will be of use, as followeth. When any Number is given to extract the Cube Root, do thus: First point the last Figure, and every third, as in this Example; then I seek in the Table of Cubes for 146, and find 125 next less, whose Root 5 I set in the Quotient, and subtract 125 from 146 and there rests 21; after which I add 363 to the next Point: Now for a new Divisor, which must be found at each several Operation, square the Quotient, and triple that Number, as 5 times 5 is 25, and 3 times 25 is 75, which I set for a new Divisor; (and whereas in the searching for the Square Root I set all one short from the right hand, here I allow two Places;) then I enquire how many times 75 can be in 213? and finding it twice, I set 2 in the Quotient, and multiplying it by 75 find it 150, which I set (as in the Example) two Places

$$\begin{array}{r}
 146363183 \text{ (527)} \\
 \underline{125} \\
 21363 \\
 \underline{150} \\
 60. \\
 \underline{8} \\
 15608 \\
 8112 \text{ ) } 5755183 \\
 \underline{56784} \\
 7644. \\
 \underline{343} \\
 5755183 \\
 \underline{\quad\quad\quad} \\
 0
 \end{array}$$

short of the last Figure. Next, I square 2 the last Figure in the Quotient, which makes 4, and multiply that by the Triple of the former Figure, that is, 3 times 5 makes 15, and 4 times 15 is 60, which I set one Place further on to the right hand, as in the Example. Lastly, I cube 2, which is 8, as you may see in the little Table, and set it still one Place further, under the Figure 3: Then I add those three Sums, and find the Product 15608, which I subtract from 21363, and there rests 5755, to which I annex the next three Figures, and make it 5755183. And this Work must be repeated for each several Figure in the Quotient. The next Divisor will be found to be 8112; by squaring 52, or multiplying 52 by 52, it makes 2704, which tripled is 8112, and the Work will stand (by repeating the same operation) as in the Example, where 7 times 8112, which is 56784, is set two Places short; then square 7, which is 49, and multiply that by 156, which is the Triple of 52, it makes 7644, which I set one Place further; and lastly I cube 7, which is 343, and set it to the last, and adding them together they make 5755183, which taken from the last Remainder leaves nothing. So the Root is 527. If after all these there remain any Figures, what to do in that case shall be shewed hereafter.

These

These Rules thus perfectly gotten, the rest of the Work, through all the Parts of *Arithmetick*, will be pleasant and easie to the Learner; wherefore if this be had, which but a little pains may obtain, we may proceed to the rest.

## SECTION II.

## Of Weights, Measures, Coin, and Time.

## §. 1. Long Measures.

**M**EASURES are of Application or Reception; those of Application or Length are taken from the Parts of the Body; *Long Measures* but in *England* they are taken from the Standard of a Yard kept in *Guildhall, London*, the third part whereof is a Foot, and the Thirty sixth part an Inch, expressed in the following Table, from One Inch to a Mile.

This Section of Measures, Weights, &c. will be of great use to be understood and known.

Inch.									
3	Pa'm.								
9	3	Span.							
12	4	1 $\frac{1}{3}$ Foot.							
18	6	2	1 $\frac{1}{2}$ Cubit.						
36	12	4	3	2 Yard.					
45	15	5	3 $\frac{1}{2}$	2 $\frac{1}{2}$	1 $\frac{1}{2}$	Ell.			
60	20	6 $\frac{2}{3}$	5	3 $\frac{2}{3}$	1 $\frac{2}{3}$	1 $\frac{1}{4}$	Pace.		
72	24	8	6	4	2	1 $\frac{1}{4}$	1 $\frac{1}{4}$	Fathom.	
198	66	22	16 $\frac{1}{2}$	11	5 $\frac{1}{2}$	4 $\frac{3}{4}$	3 $\frac{1}{8}$	2 $\frac{1}{4}$	Pole.
7920	2640	880	660	440	220	176	132	110	40 Furlong.
63360	21120	7040	5280	3520	1760	1408	1056	880	320 8 Mile.

This Table of *Long Measures* (as all the rest after) may be considered as to the Columns from top to bottom, or by and betwixt the Lines from left hand to right: Each Column has its Name at the top, as in the first of Inches, all the Numbers, *viz.* 3, 9, 12, 18, 36, &c. are to be accounted Inches; but the Numbers between the Lines have respect to the Name at

C

the



the end against which they stand, as 36 Inches, 12 Palms, 4 Spans, 3 Feet, and 2 Cubits, make severally a Yard; and so at the bottom you have the Inches, Palms, Spans, Feet, Cubits, Yards, Ells, Paces, Fathoms, Poles, and Furlongs in a Mile.

In this Table it is said, that a Pole or Perch for measuring Land is 16  $\frac{1}{2}$  Feet, which is according to the Statute, but there are other Customary Poles or Perches, as 18 Feet for Fens and Wood-land, 21 Feet for Forests, *Lincolnshire*, and *Ireland*, and 18  $\frac{1}{4}$  for *Scotch* Measure.

The Measure for the Height of Houses is by Handfuls, viz. 4 Inches.

The Ell by the Table is  $\frac{5}{8}$  Quarters of a Yard, and contains 20 Nails, as a Yard does 16; therefore the fifth part of an Ell is a Quarter of a Yard. A *Dutch* or *Flemish* Ell or Stick is three Quarters of a Yard, by which Tapiftry is measured.

### § 2. Square Measure.

Square Measure.

**SQUARE MEASURES**, or *Superficial*, are contained in this small Table.

Inches square.						
144	Feet sq.					
1296	9	Yard sq.				
3600	25	2.77	Paces sq.			
39204	272.25	30.25	10.89	Poles sq.		
1568160	10890	1210	435.6	40	Roods sq.	
	43560	4840	1742.4	160	4	Acres sq.
		3097600	1115136	102400	2560	640 Miles sq.

By reading of which Table, the Columns are Square Inches, Feet, Yards, &c. and the Lines, suppose against Acres, are read thus: 43560 square Feet, 4840 square Yards, 1742.4 square Paces, 160 Pole, and 4 Roods, or any of them, make one Acre.

### § 3. Solid Measure.

Solid Measure.

**SOLID MEASURE**, or a Cubick Foot, contains 1728 Cubick Inches. A Cubick Yard is 27 Cubick Feet, and 46656 Cubick Inches. A Statute-Brick is 9 Inches long, 4  $\frac{1}{2}$  Inches broad, and 2  $\frac{1}{2}$  Inches thick.

A Cord of Wood is 4 Feet over, 4 Feet deep, and 8 Feet long, which makes 128 Cubick Feet.

A Stack of Wood is 3 Feet over, 3 Feet deep, and 12 Feet long, which makes 108 Solid Feet.

Great Log-Wood is sold by the Cord, and Small-Wood by the Stack.

Fifty

Fifty Feet of Timber make a Load, 40 Feet a Tun; 18 Feet square and one Foot deep, or 324 Feet solid, is a Floor of Earth; as 27 solid Feet is a Yard.

300 Feet of 2 Inch Plank, 200 Feet of 3 Inch Plank, 150 Feet of 4 Inch Plank, 400 Feet of 1  $\frac{1}{2}$  Inch, and 600 Feet of Inch Plank, make a Load of Plank.

Now I should acquaint you with *Hollow Measures*, or of *Capacity*; but because most of them depend upon *Troy* or *Averdupois* Weights, I will explain them first, and then the other.

### § 4. Troy weight.

**TROY WEIGHT** weigheth Gold, Silver, Jewels, Amber, Ele. *Troy weight.* Quaries, Bread Corn, Liquors, &c. and from this Weight all Measures of Wet and Dry Commodities are taken.

The Pound *Troy* is divided into 12 Ounces, the Ounce into 20 Pennyweight, and that into 24 Grains, as by the first Table appears.

Grains.	Troy Weight.	
24	Penny-weight.	
480	20	Ounces.
5760	240	12 Pounds.

Grains.	Apothecaries Weight.			
20	3	Scruple.		
60	3	3 Drams.		
480	24	8	3 Ounces.	
5700	288	96	12	1 lb Pound.

Apothecaries make up their Medicines by the last Table of *Troy* Weight, but buy and sell Drugs by the *Averdupois*.

### § 5. Averdupois Weight.

**BY AVERDUPOIS WEIGHT** are weighed all Physical Drugs, *Averdupois weight.* Grocery, Rosin, Wax, Pitch, Tar, Tallow, Soap, Hemp, and all things that have waste, all base Metals and Minerals, as Iron, Steel, Lead, Tin, Copper, Alom, Copperas, &c.

The Pound *Averdupois* is divided into 16 Ounces, an Ounce into 8 Drams, a Dram into 3 Scruples, and a Scruple into 20 Grains.

Scruples.	Averdupois Weight.			
3	Drams.			
24	8	Ounces.		
384	128	16	Pounds.	
43008	14336	1792	112	Hundreds.
860160	286720	35840	2240	20 Tuns.

C 2

Now



Great Hundred.

Now 112 lb. make a C. or Hundred-weight, or the great Hundred, and 20 C. make a Tun, which is shewed in the last Table.

Eighty Ounces *Averdupois* make near to 73 Ounces *Troy*: But Dr. *Winbird* makes 14 Pound *Averdupois* equal to 17 Pound *Troy*; therefore let *Troy* Pound to *Averdupois* be as 17 to 14, *Troy* Ounces to *Averdupois* as 51 to 56.

The Hundred-weight being 112 lb. is divided into Quarters, each 28 lb. and Stones, each 14 lb. By which are weighed Iron, Guns, Shot, &c.

#### Variation of the Tun and Hundred.

Tun and Hundred's Variation.

Nineteen Hundred and an half is a Tun, or Fodder of Lead. Alom, Cinnamon, Nutmegs, Pepper, and Sugar, have 13  $\frac{1}{2}$  Pound to the Stone, and 108 Pound to the Hundred. *Essex* Cheefe and Butter has 8 Pound to the Clove, the *Wey* 32 Cloves, or 256 Pound. In *Stafford* the Clove is 8 Pound, the *Wey* 42 Cloves, or 336 Pound; 56 Pound of Butter, 60 Pound of Soap make a Firkin, and 4 Firkins a Barrel of each.

Hay has 18 Hundred, 36 Trusses, or 2016 Pound, to the Load or Tun.

Wool is sold by the Clove of half Stone 7 Pound, 14 Pound the Stone, and 28 Pound the Tod; the *Wey* 182 Pound, and the Sack 364 Pound; the Laft 4:68 Pound.

A Faggot of Steel is 120 Pound. A Burthen of Gad Steel is 9 Score or 180 Pound. Butchers account 8 Pound to the Stone. A Laft of Powder is 24 Barrels.

To weigh much with a few Weights, note, That 1 Pound, 3 Pound, and 9 Pound, will weigh all from 1 to 13 Pound; and 1, 3, 9, 27 Pound, will weigh all to 40 Pound; and 1, 3, 9, 27, and 81 Pound, will weigh all to 121 Pound.

And note, it will be useful to observe, That a Vessel which is 12 Inches square, and 12 Inches deep, that is, a *Cubick Foot*, will hold 76 lb. *Troy*, and 62.488 lb. *Averdupois*; and therefore 1 lb. *Troy* will fill 22.757 Solid Inches, and 1 lb. *Averdupois* 27.609 Solid Inches.

Having thus stated the businets for Weights, I come now to Measures of Capacity, which are either Dry Measures or Wet.

#### §. 6. Dry Measures.

Dry Measures.

**D**RY MEASURES of Capacity, are raised from the Gallon, containing 8 Pints, which should be contained in 272  $\frac{1}{2}$  Cubick Inches, and should hold of pure Running or Rain Water 9 Pound, 13 Ounces, 12 Drams and  $\frac{1}{2}$ , *Averdupois* Weight. Therefore to obtain a true Gallon for Dry Measure, if you make a Vessel Cubick, that shall have all the Sides 6 Inches and 48 hundred Parts of an Inch square, and just so deep; or if you weigh with *Averdupois* Weights 9 Pound, 13 Ounces, and 12 Drams and  $\frac{1}{2}$ , of clean Rain or Running Water; either of these will find out the Gallon for Dry Measure.

The

The Table following shews 8 Pints to be a Gallon, 2 Gallons a Peck, 4 Pecks to a Bushel, 2 Bushels to a Strike, 2 Strikes or 4 Bushels to a Coom or Canock, 2 Coom to a Quarter, Seam or Rofer, 6 Quarter to a Wey.

This Table is for measuring Corn, and the two last Lines contain the estimated Weights, the first *Troy*, the last *Averdupois*, that each several Quantity contains.

Pints.		Gallons.		Pecks.		Bushels.		Strikes.		Canock or Coom.		Seam or Quarter.		Wey.		Laft.	
8																	
16	2																
64	8	4															
128	16	8	2														
256	32	16	4	2													
512	64	32	8	4	2												
3072	384	102	48	24	12	6											
5120	640	320	80	40	20	10	12										
A	1 lb.	8 lb.	16	64	128	256	512	3072	5120								
B	14 $\frac{2}{3}$	7 lb.	14	56	1 C.	2 C.	4 C.	24 C.	40 C.								

Some make 6 Quarters of Meal a Wey, and 1 Wey and  $\frac{1}{4}$  to a Laft.

Meal is weighed as Corn, but the common repute is, that a Gallon of Wheat Meal weighs 7 Pound *Averdupois*, and 8 Pound, 6 Ounces, 4 Penny-weight, *Troy*; and so a Bushel 56 Pound *Averdupois*, and 68 Pound, 1 Ounce, 12 Penny-weight, *Troy*. All other Grain, Salt, Lime, Coals, &c. follow the *Winchester* Measure; though Sea Coal and Salt be measured by this Bushel, yet it is heap'd, or else 5 stricken Pecks are allowed to the Bushel called *Water-Measure*; 36 Bushels are a Chaldron of Coals, and on Ship-board 21 go to the Score; 3 Bushels make a Sack, 4  $\frac{1}{2}$  such Bushels a Fat or Flat, 12 Sacks make 4 Fats. Of Salt 40 Bushels make a Wey.

#### §. 7. Liquid Measures.

**L**IQUID MEASURE is either of Wine, Ale, or Beer. The *Liquid Measure* Wine Gallon contains 231 Cubical Inches, and should hold of pure *Wines*. Rain or Running Water 8 Pound, 1 Ounce, 11 Drams, *Averdupois*; or 9 Pound, 10 Ounces, 1  $\frac{1}{4}$  Penny-weight, *Troy*; or a Cubick Vessel of 6 inches and 13 hundred Parts every way: Either of these will find out this Gallon. A Tun of Wine weighs 17 Hundred Weight *Averdupois*.

A Table



Wine, Honey,  
Oyl, &c. Meas-  
ure.

A Table for Wine Measure, Honey, Oyl, &c.									
Pints.	Gallons.								
8	18	Runnlets.							
144	31 ½	1 ½	Barrels.						
252	42	2 ½	1 ½	Tervces.					
336	63	3 ½	2	1 ½	Hogheads.				
504	84	4 ½	2 ½	2	1 ½	Pumbecons.			
672	126	7	4	3	2	1 ½	But or Pipe.		
1008	2016	252	14	8	6	4	3	2	Tun.

The Gallon for Ale and Beer holds 282 Solid Inches, and weighs of pure Water 10 Pound, 3 Ounces, .426 hundred Parts, *Averdupois*; therefore the Cubick Vessel ought to be 6 Inches, and 55 hundred Parts of an Inch each way, to find this Gallon. In a Solid Foot are 1728 Solid Inches, which make 6.128 Gallons; and in a Hoghead are 10 Feet Solid, and 287 Parts, and taking the round Sum 10 Feet to be in a Hoghead, there will be 20 Feet in a But or Pipe, and 40 Feet in a Tun.

Beer and Ale  
Measure.

Beer Measure.					Ale Measure				
Pints.	Gallons.				Pints.	Gallons.			
8	9	Firkins.			8	9	Firkins.		
72	144	18	2	Kilderkins.	64	128	18	2	Kilderkins.
288	336	36	4	Barrels.	256	336	36	4	Barrels.
576	72	8	4	Hoghead.	512	72	8	4	Hoghead.

Note, That Vessels for Butter, Fish, Soap, follow the Ale Measure of a Gallon, and that 12 Ale Barrels make a Laft. The Tare for the Cask of Butter, Soap, is 6 ½ Pound for a Firkin, 13 Pound for the Kilderkin, and 26 Pound for the Barrel.

#### ¶ 8. Tale of several Goods.

Tale of several  
Goods.

THE *TALES* of several Goods will be worth knowing, either at home or abroad.

120 Ells of Canvas Cloth make an Hundred, 14 Ells of Fustian make a Chefc, and 10 Ells of fine Linnen, Silk, and Sindon, the same.

Cod Fish, Haberdine, Ling, &c. have 124 to the Hundred, and 1240 to the Thouland. Eels, 25 to the Stick, and 10 Sticks to the Bind. Of Herrings and Stock Fish, 120 to the Hundred, 1200 to the Thouland laid in a Barrel, and 12 Barrels to the Laft.

Deals

Deals and Nails are for the most part sold 120 to the Hundred. Of Furs; Filches, Grays, Jennets, Martins, Sables, Minks, 40 Skins make a Timber; other Skins, 5 Score to the Hundred.

A Seam of Glafs is 24 Stone, or 120 Pound.

A Bale of Paper is 10 Ream, a Ream 20 Quire, a Quire 25 Sheets of some, and 24 of others.

A Roll of Parchment is 5 Dozen, a Dozen is 12 Skins.

Twelve Dozen make a Gros.

Ten Hides are a Dicker, 20 Dickers a Laft.

Ten Pair of Gloves make a Dicker, and 10 do 10 Horse-shoes.

Great Skins are numbred by the Kip, of 50 Skins to the Kip.

Laths 5 Foot long have 5 Score to the Hundred, 4 Foot long 120 to the Hundred. All Laths ought to be 1 ½ Inch broad, and ½ Inch thick.

Five Hundred Bricks make a Load, and 10 do 100 Plain Tiles.

Of Bread, 13 goes to the Dozen, and 21 Dozen to the Score.

Five Foot of *Newcastle* Glafs make a Table, and 45 Tables make a Cafe; but of *Normandy* Glafs, 25 Tables make a Cafe.

In the City, Lime is sold by the Bag, each Bag holds a Bushel, and 25 such Bags make an Hundred. Some Places have 40 Bushels to the Load.

70 Pipe Hoops, 90 Hoghead Hoops, 120 Barrel or Kilderkin Hoops, or 180 Firkin Hoops, make a Bundle or Hundred.

#### ¶ 9. Money.

THE ACCOMPT of *MONET* is very necessary to be known. *Money.*

##### English Money.

4 Farthings	} make 1	} Penny.		} A Mark is	s.	d.	
12 Pence					} Shilling.	13	04.
20 Shillings						} Pound	A Noble

##### Spanish Money.

6 Carnadoes	} make 1	} Marveid.		} 40 Res		
54 Marveids					} Ryal. 6d. Eng.	
11 Ryals						} Ducat.
8 Ryals						
	} 4 s. Engl.					
		} Royal.				
4 Quartiles						10 Ryals
					2 ½ Ducats	

##### Portugal Money.

40	Res	}	make 1	}	Ryal. 6d Eng
2 $\frac{1}{2}$	Ryals				Testoon.
4	Testoons or				Ducat.
	10 Ryals				
2 $\frac{1}{2}$	Ducats				Milt of gold

##### French Money.

12 Deniers	} make 1	} Soulz.		} 1 Small Peece		
20 Soulz					} Frank or Liver.	
16 Soulz						} Cardecu.
4 Cardecues						
		} Frank or Liver.		} 3 Small Peecces		
		} Cardecu.				
		} Crown.		} 2 Nobles		
				3 Nobles		

##### Scotch Money.

1 Small Peece	} make 1	} 2 $\frac{1}{4}$ d. English.		
3 Small Peeeces			} Noble, 6 $\frac{1}{4}$ d. Eng.	
2 Nobles				} Mark, 13 $\frac{1}{2}$ d. Eng.
3 Nobles				

Irish



## Irish Coin.

Two  $4\frac{1}{2}d.$  is one Harper, or 9 *d. English*; and 20 Harpers is 1 *l. Irish*, or 15 *s. English*.

## Flemish Coin.

8 Pence	} is	1 Groat.
2 Groats		1 Single Stiver.
2 Single Stivers		1 Double Stiver, or $3\frac{1}{4}d.$ <i>English</i> .
20 Single Stivers, or 10 Double		1 Gilder.
6 Gilders		1 Pound.

## §. 10. Time.

Time.

IN a Common-Year are 365 Days and 6 Hours, but in a Leap-Year 366. In a Day Natural are 24 Hours, in an Hour 60 Minutes, and in a Minute 60 Seconds, &c. In a Year are 52 Weeks, 13 equal Months of 28 Days to a Month and 1 Day, or 12 unequal Months.

The Characters used to express the former Moneys, Weights, &c. are they that follow.

A Pound *l.* a Shilling *s.* a Penny *d.* an Half-penny *ob.* or  $\frac{1}{2}$ ,  $\frac{2}{3}$ ,  $\frac{1}{4}$ , for 3 Farthings, an Half-penny, or Farthing. A Pound Weight *lb.* an Ounce  $\mathfrak{z}$ , a Grain *gr.* a Scruple  $\mathfrak{z}$ , a Dram  $\mathfrak{z}$ , a Quarter *qr.* a Crown  $\Delta$ , an Hundred Weight *C.*

I shall now come to shew you the Practice of *Addition* and *Subtraction* in these Parts of Money, Weight, and Time, where the Denominators are omitted, which will bring to use the aforelaid Rules, and will caule you to seek for as much as you shall have need for amongst the Tables.

## SECTION III.

## Of the Addition, Subtraction, and Reduction of Numbers of several Denominations.

## §. 1. Addition of several Denominations.

Addition of several Denominations.

THE Rule for *ADDITION* will be, To sum up each Denomination, and to see how many of them will make one of the next Denomination, and to bear so many Units forwards, as those will come to.

In

In this Example I begin with Pence, and say, 9 and 2 is 11, and 8 is 19, which I find to exceed 12 Pence, the Pence in a Shilling, and contain it once, and 7, which 7 I set down under Pence, and carry 1 to Shillings, saying, 1 and 5 is 6, and 1 is 7, and 7 is 14, I set down 4, and account how many 10 *s.* I have, which are 3, which make 1 *l.* 10 *s.* the 10 *s.* I set by the 4, and carry 1 to the Pounds, and adding them as in whole Numbers, I find the Sum to be 23 *l.* 14 *s.* 7 *d.*

<i>l.</i>	<i>s.</i>	<i>d.</i>	<i>Troy Weight.</i>			<i>Averdupois Weight.</i>			
175	15	02 $\frac{3}{4}$	<i>lb.</i>	$\frac{5}{8}$	<i>lwr.</i>	<i>Gr.</i>	<i>lwr.</i>	<i>C.</i>	<i>Gr.</i>
75	11	09	13	09	13	15	0	2	3
30	00	00	221	11	10	01	0	16	2
71	11	11 $\frac{3}{4}$	15	10	11	02	0	34	1
131	10	10	251	07	14	18	0	17	0
484	09	09					3	10	3

These three Examples will be sufficient. The first of Pounds, Shillings, and Pence, as before. The second Example of *Troy Weight*, where for every 24 Grains I carry 1 to the Penny-weight, for every 20 Penny-weight I carry 1 to the Ounces, and for every 12 Ounces 1 to the Pound, and the Sum will be 251 Pound, 7 Ounces, 14 Penny-weight, and 18 Grains. And so for *Averdupois Weight*, for every 16 Ounces I carry 1 to the Pound, for every 28 Pound I carry 1 to the Quarters, and for every 4 Quarters 1 to the Hundred, and 20 Hundred for a Tun.

All the trouble lyes in carrying to many of former Denominations as are contained in that Row you add up.

## §. 2. Subtraction of several Denominations.

**SUBTRACTION** in these Numbers, is no more, than to take the lower Denomination from the higher; which if it be lesser, and you cannot take it, then you must borrow one of the former Denominations and subtract, remembering to add 1 to the next Denomination below.

<i>l.</i>	<i>s.</i>	<i>d.</i>	<i>Troy Weight.</i>		
375	11	05	<i>lb.</i>	$\frac{5}{8}$	<i>Pwr.</i>
132	09	04	1754	11	02 $\frac{3}{4}$
			982	13	05 $\frac{1}{2}$
Rem.	243	02 01	771	17	09 $\frac{1}{4}$

The first Example has no difficulty, being the lower is in each Denomination less than the higher. In the second Example, because 5 *d.* will not come out of 2 *d.* I borrow 12 *d.* and make it 14 *d.* and then 5 out of 14

D

refts



refts 9; now I remember to make 13, 14, restoring the 12 d. I borrowed (which must be carefully done) and say, 14 out of 31 (borrowing 20) refts 17. Then, as in the Whole Numbers, 3 out of 4, refts 1, &c.

Note, It is an easier way, to take the lower from what you borrowed, and add the Remainder to that above, than to work the ordinary way; as in the said Example, say 5 out of 12 I borrowed refts 7, and 7 and 2 is 9. Again, in Shillings, it is better to say, 14 out of 20 refts 6, and 6 and 11 makes 17. In the third Example of *Troy Weight*, in the second Denomination of *Peny-weight*, I say, 19 out of 20 refts 1, and 1 and 13 makes 14. Then, 12 Ounces from 12 I borrow refts 0, and 0 and 9 is 9.

Here the young Scholar will receive some encouragement; for if I demand of him this present year 1678, what Age I was, being born 1617? let him subtract the lesser Number 1617 from the greater 1678, and there refts 61 Years.

	<i>l.</i>	<i>s.</i>	<i>d.</i>	
Received	30	00	00	
More	50	00	00	
More	62	11	06	
Sum of Receipts	142	11	06	
Disburs'd	7	15	07 $\frac{1}{2}$	
More	34	18	09	
More	18	17	05	
More	23	11	08 $\frac{1}{2}$	
More	32	09	08 $\frac{1}{2}$	
Sums disburs'd	117	13	02 $\frac{1}{2}$	
Remains	24	18	03 $\frac{1}{2}$	
Proof	142	11	06	

### §. 3. Reduction.

The next is, to shew how any of these Numbers, whether of Money, Weight, Measure, &c. may be brought from the highest or higher Term to the lowest or lower; which to do, you must consider how many of the next lesser Denomination is contained in the next greater before, and by that Number multiply the greater; as Pounds are brought into Shillings by multiplying by 20, Shillings into Pence by 12, and Pence into Farthings by 4; as in the following Examples, where 27 *l.* 19 *s.* 5 *d.* make 6713 *d.* and 13 *l.* 15 *s.* 6  $\frac{1}{4}$  *d.* make 13227 *f.* And here I multiply by 12 at once.

<i>l.</i>	<i>s.</i>	<i>d.</i>
27	19	5
20	540	6713
	559	12

<i>l.</i>	<i>s.</i>	<i>d.</i>	<i>f.</i>
13	15	6 $\frac{1}{4}$	
20	200	3306	
	275	12	13227

*Troy Weight* may be reduced into Grains, by multiplying by 12, 20, and 24: And *Averdupois Great Weight* into Ounces, by 4, 28, and 16. 352 Pound *Troy Weight* makes 2027520 Grains.

<i>Lib.</i>	$\bar{s}$ .	<i>Pwt.</i>	<i>Lib.</i>	$\bar{s}$ .	<i>Pwt.</i>	<i>Grains.</i>
352	4224	84480	37	10	16	11
12	20	24	12	444	9080	36384
4224	84480	337920		454	9096	18192
		168960		20	24	218315
		2027520				

And so of any higher to a lower by Multiplication; but if it be to bring the lower to a higher, then divide the least by so many of its Denominations as are contained in the next greater. Example, to bring 42720 Pence into Pounds, Shillings, and Pence; the Answer is 178 Pound: And if any had remained in either Division, they had been the odd Pence and Shillings; as in the second Example, in 6713 *d.* there is 27 *l.* 19 *s.* 5 *d.*

Note, That to reduce Shillings into Pounds, is to cut off the last Figure, and take half of the rest, as the half of 5 is 2, of 15 is 7, and there remains 19 *s.* and 5 *d.*

<i>d.</i>	<i>s.</i>	<i>l.</i>
12 ) 42720	( 3560	( 178
36		
67	2)	
60		
72		
72		
0		

<i>l.</i>	<i>s.</i>	<i>d.</i>
12 ) 6713	( 559	( 27:19:05
60		
71	2)	
60		
72		
113		
108		
5	<i>d.</i>	

After the same manner may *Troy Weight*, *Averdupois*, or any other Weight or Measure, be reduced.

Likewise Foreign Coin may be reduced into *English*, by turning the Value into



into English Coin of any part: As, What is the Value of 223 Scotch Mark, equal to  $13 \frac{1}{2} d.$  English? which is 54 Farthings, and 223 by 54 makes 12042 Farthings, which reduced backwards to Pounds, Shillings, Pence, makes 12  $l.$  10  $s.$  10  $\frac{1}{2} d.$

## SECTION IV.

Of FRACTIONS, whose Species and Rules shall be brought into as short a Form as may be.

Of Fractions.

A Broken Number, called a FRACTION, denotes or signifies one or more Parts proportionably of any thing divided: It consists of two Numbers, the higher and lower, with a Line betwixt them. The higher is the Remainder after Division, the lower is the Divisor; the higher numbers the Parts of the Thing divided remaining after Division, and is called the Numerator; the lower denominates the Parts, and is called the Denominator.

This Knowledge consists in the Reading of a Fraction, in the Abbreviation, Estimation, and Reduction; and lastly, in the performing the ordinary Rules of Addition, Subtraction, Multiplication, Division, and in Extracting the Roots. Every one of which shall follow in order.

## §. 1. Pronunciation.

Reading of a Fraction.

THE READING pronounceth the higher first, then the lower, as  $\frac{3}{4}$ , called three fourths; to  $\frac{1}{2}$ ,  $\frac{2}{3}$ ,  $\frac{3}{4}$ ,  $\frac{1}{5}$ , are called, the half, the third part, the five seven parts, the 32 parts of 150.

## §. 2. Abbreviation of a Fraction.

Abbreviation of a Fraction.

THE ABBREVIATION is, when both the Numerator and Denominator, divided by some Common Measure, are express'd in lower Terms, as  $\frac{4}{8}$  being divided by 4, the greatest Common Measure, gives  $\frac{1}{2}$ , the same in value; for as 4 is the half of 8 (supposing of an Inch divided into 8) so is 1 of 2, &c.

How to find this Greatest Common Measure, the Rule is, Divide the Numerator by the Numerator, or the greater by the less, and the Divisor by the Remainder, and the first of the Divisors, that divideth the Dividend without a Remainder, is the Greatest Common Measure. Thus in  $\frac{4}{8}$ , 2 is found the Greatest Measure, and will bring  $\frac{4}{8}$  to  $\frac{1}{2}$  by dividing by 2.

$$\begin{array}{r} 14) 38(1 \quad 14) 24(1 \quad 10) 14(1 \quad 4) 10(2 \quad 2) 4(2 \\ \underline{14} \quad \underline{14} \quad \underline{10} \quad \underline{8} \quad \underline{4} \\ 24 \quad 10 \quad 4 \quad 2 \quad 0 \end{array}$$

Thus

Thus all Fractions ought to be abbreviated before you work them, as  $\frac{14}{28}$  by 14 becomes  $\frac{1}{2}$ , to  $\frac{24}{120}$  by 24 becomes  $\frac{1}{5}$ , being of the same value as before. But if the last Remain in finding the Common Measure be 1, then those Numbers are incommensurable, and are in their least Terms already. If both the Terms have Cyphers to the right hand, cut them off, to  $\frac{20}{40}$  becomes  $\frac{1}{2}$ . Even Numbers may be brought down by halving, or dividing them by some commonly known Measure.

## §. 3. The Value of a Fraction.

THE ESTIMATION or VALUE of a Fraction is known thus: Value of a Fraction. If the Numerator be equal to the Denominator, then is the Fraction equal to Unity, or one Whole. But if the Numerator be less, then the Fraction is less than 1; if greater, greater:  $\frac{2}{3}$  is equal to  $1 \frac{1}{3}$  is less than 1, but  $\frac{4}{3}$  is 1 and  $\frac{1}{3}$ . If you desire to know the Value of a Fraction in some other Denomination than his own, as, What is the 5 Twelfths of a Crown? Here  $\frac{5}{12}$ , which has 12 for the Denominator, is to be changed into a Denominator that has 60, for 10 many Pence are in a Crown. Multiply the Numerator in the new Denominator, and divide by the old Denominator, and you have the Value. So 60 into 5 is 300, which divided by 12 gives 25, which signifies that 25 Pence is the  $\frac{5}{12}$  of a Crown. And to the  $\frac{5}{12}$  of a Day will be found 18 Hours. And so of any other.

## §. 4. Reduction of Fractions.

FIRST to reduce two Fractions of divers Denominations to one and the same, (having brought them first to their least Terms) multiply the Denominators together for a new Denominator, and multiply cross, the Denominator of one by the Numerator of the other, for new Numerators. Reduction of Fractions.

Example.

$\frac{3}{5}$  and  $\frac{2}{3}$  reduced to the same Denomination becomes  $\frac{6}{15}$  and  $\frac{10}{15}$ .

$$\begin{array}{r} 21 \quad 20 \\ \frac{3}{5} \quad \frac{2}{3} \\ \hline 35 \end{array}$$

And if there be more Fractions than two, to be reduced to one and the same Denomination, multiply all the Denominators for a new one, and each Numerator into all the Denominators but his own.

Thus  $\frac{1}{2}$ ,  $\frac{2}{3}$ ,  $\frac{1}{4}$ , and  $\frac{3}{5}$ , if reduced to one Denomination, becomes  $\frac{15}{60}$ ,  $\frac{20}{60}$ ,  $\frac{15}{60}$ , and reduced by halving will be  $\frac{3}{12}$ ,  $\frac{4}{12}$ ,  $\frac{3}{12}$ ,  $\frac{5}{12}$ .

$$\begin{array}{r} 60 \quad 80 \quad 90 \quad 96 \\ \frac{1}{2} \quad \frac{2}{3} \quad \frac{1}{4} \quad \frac{3}{5} \\ \hline 120 \end{array}$$

To reduce a Whole Number into an improper Fraction of a Denomination given, multiply that Number by the Denominator given, and set it over



over it Fraction-wise, as to reduce 7 to a Denominator of 4, it will be  $\frac{28}{4}$ ; and to reduce 5 into  $\frac{1}{4}$ , it will be  $\frac{5}{4}$ : And thus any Whole Number and Parts are to be handled; as  $3\frac{3}{4}$  makes  $\frac{15}{4}$ : So likewise an improper Fraction, where the Numerator is equal or greater than the Denominator, is to be brought into Whole Numbers, by dividing the Numerator by the Denominator. Thus  $\frac{15}{4}$  will be 3, and  $\frac{3}{4}$  will be  $3\frac{3}{4}$ , and  $\frac{15}{3}$  will be  $5$ .

#### §. 5. Fractions of Fractions.

Fractions of Fractions.

Thus far has concerned Fractions pure, that are only Parts of the Whole; there are yet such as are called *Fractions of Fractions*, or *Particulars*, which are Parts of a Fraction, as  $\frac{1}{2}$  of  $\frac{1}{2}$ , or  $\frac{1}{4}$  of  $\frac{1}{2}$ ; or, what is the  $\frac{1}{2}$  of the  $\frac{1}{2}$  of a Shilling? Here the half of a Shilling, which is 6 d. is supposed to be divided into 2, and so the  $\frac{1}{2}$  will be 3 d.

To know these Fractions from other, it is usual to make a Comma after them; and to reduce them to one Denomination, so as they may be wrought with other Fractions, is to multiply all the Denominators together for a new Denominator, and all the Numerators together for a new Numerator.

Thus  $\frac{1}{2}$  of  $\frac{1}{2}$  will make  $\frac{1}{4}$ , abbreviated will be  $\frac{1}{4}$ , by dividing all by 2 the Common Measure.

#### §. 6. Addition and Subtraction of Fractions.

Addition and Subtraction of Fractions.

Addition and Subtraction of Fractions (after they be abbreviated and reduced as is before shewed) consists in the adding and subtracting the Numerators to or from one another. And this falls out either to be Fractions with Fractions, Whole Numbers with Fractions, or Mixt with Fractions, or Mixt with Mixt.

##### Addition.

Fractions.  $\frac{1}{2}$  and  $\frac{1}{2}$  make  $\frac{2}{2}$ , or 1.

Numbers & Fractions.  $5$  and  $\frac{1}{2}$  to be added is  $5\frac{1}{2}$ .

Whole Numbers and Mixt.  $7$  and  $4\frac{1}{2}$  added would be  $11\frac{1}{2}$ . Subtracted will be  $2\frac{1}{2} - \frac{1}{2} = 2$ .

Mixt with Mixt.  $5\frac{1}{2}$  added to  $4\frac{1}{2}$  makes 9 and  $\frac{1}{2}$ . Subtracted is  $1\frac{1}{2}$ .

Unlike Denomination.  $3\frac{1}{2}$  and  $2\frac{1}{2}$  added makes  $6\frac{1}{2}$ . Subtracted is  $1\frac{1}{2}$ .

##### Subtraction.

$\frac{1}{2}$  less by  $\frac{1}{2}$  make  $\frac{0}{2}$ .

$5$  less by  $\frac{1}{2}$  make  $4\frac{1}{2}$ .

$7$  less by  $4\frac{1}{2}$  make  $2\frac{1}{2}$ .

$5\frac{1}{2}$  less by  $4\frac{1}{2}$  make  $1$ .

$3\frac{1}{2}$  less by  $2\frac{1}{2}$  make  $1$ .

The

The Work for Addition,  $\frac{8}{12} + \frac{9}{12} = \frac{17}{12}$ . For Subtr.  $3\frac{2}{3}$  less by  $2\frac{2}{3}$  make  $1\frac{1}{3}$ .

So to add  $6\frac{1}{2}$  to  $10\frac{1}{2}$ , and to  $14\frac{1}{2}$ , I reduce the Fractions as before, then it will be  $6\frac{1}{2}$ ,  $10\frac{1}{2}$ ,  $14\frac{1}{2}$ , which will make, if added together,  $30\frac{3}{2}$ , or  $32\frac{1}{2}$ , or  $32\frac{1}{2}$ .

So to subtract  $\frac{1}{4}$  from  $6\frac{3}{4}$ , that is reduced  $5\frac{2}{2}$ , less by  $\frac{1}{2}$ , rests  $5\frac{1}{2}$ .

#### §. 7. Multiplication of Fractions.

Make Mixt Numbers improper Fractions (first having brought them down by Abbreviation) and make Whole Numbers like Fractions, by placing an Unit under them. Then the Rule for Multiplication is, Multiply the Numerators together for a new Numerator, and the Denominators for a new Denominator.

$\frac{1}{2}$  by  $\frac{1}{2}$  make  $\frac{1}{4}$  or  $\frac{1}{4}$ .  $2\frac{1}{2}$  by  $3\frac{1}{2}$ , or  $\frac{5}{2}$  by  $\frac{7}{2}$ , make  $\frac{35}{4}$  or  $8\frac{3}{4}$ .  
6 by  $3\frac{1}{2}$ , or  $\frac{12}{2}$  by  $\frac{7}{2}$ , make  $\frac{84}{4}$ , or  $21$ .

If the cross Terms can be abbreviated, do it, as in this Example.

$\frac{1}{2}$  by  $\frac{1}{2}$  abbreviated cross will be  $\frac{1}{2}$  by  $\frac{1}{2}$  makes  $\frac{1}{4}$ .

#### §. 8. Division of Fractions.

For Division the Rule is, Multiply alternately the Numerator of the Dividend by the Denominator of the Divisor for a new Numerator, and the other Numerator and Denominator for a new Denominator.

$\frac{1}{2}$   $\frac{1}{2}$   $\frac{1}{2}$  (  $\frac{1}{2}$  )  $\frac{1}{2}$  ( or  $\frac{1}{2}$  )  $\frac{1}{2}$  (  $\frac{1}{2}$  )  $\frac{1}{2}$  (  $\frac{1}{2}$  )

If one Fraction be divided by another, the Quotient shews the Proportion which one bears to another, by which you may know the greater. Thus,  $\frac{1}{2}$   $\frac{1}{2}$  (  $\frac{1}{2}$  ) is equal to  $\frac{1}{2}$ , but  $\frac{1}{2}$  is greater than  $\frac{1}{2}$ , for  $\frac{1}{2}$  (  $\frac{1}{2}$  ) and  $\frac{1}{2}$  is less than  $\frac{1}{2}$ , because  $\frac{1}{2}$  (  $\frac{1}{2}$  )

Here note, That to multiply any of the Parts of Money, Weight, &c. by reducing all into the least Terms will be erroneous, as 2 l. 19 s. 11  $\frac{1}{2}$  d. multiplied by it self, reduced to 2879 Farthings, will be 8633 l. 1 s. 8  $\frac{1}{2}$  d. because the Denominator 960 is omitted, which ought in this case to be restored to it as a Fraction.



## SECTION V.

## Of Decimal Arithmetick.

Decimal Arithmetick.

**I** Come now to that Part called *DECIMAL ARITHMETICK*, which is no other, but a more easie kind of *Fractions*; and if all the Account of Money, Weight, Measure, &c. were divided and subdivided into Tens, then all the former Rules of *Fractions* might be saved: As in some sort of Coin at *Rome*, consisting in Ducats, Julio's, and Baiocca's; a Ducat is the Integer, and is divided into Ten Julio's, and each Julio into Ten Baiocca's; so that to express 35 Ducats, 8 Julio's, and 7 Baiocca's, you may write them thus, 35.87, which is 35 Ducats,  $\frac{8}{10}$  and  $\frac{7}{100}$  of a Ducat or  $\frac{87}{100}$  of a Julio. Therefore in every Decimal Fraction a Point or other Mark must follow Unity. Then, as in Integers Figures of the same kind increase in a Decimal Proportion towards the left hand, so here it is Ten times less towards the right.

## §. 1. Addition and Subtraction in Decimals.

Addition and Subtraction in Decimals.

**A**ddition and Subtraction in *Decimals* is the same with Whole Numbers: Regarding and absolutely requiring, that Units be set under Units, and the respective Figures under the same estimation with those above them; for Cyphers before Integers or after Decimals signify nothing, but after Integers and before Decimals retain their Value.

Addition.

$$\begin{array}{r}
 35.5 \\
 342.61 \\
 2376.723 \\
 111.15 \\
 \hline
 2865.983
 \end{array}$$

Subtraction.

$$\begin{array}{r}
 37.82 \\
 572.119 \\
 327.9 \\
 \hline
 15.826
 \end{array}$$
  

$$\begin{array}{r}
 32. \\
 0.38 \\
 \hline
 31.62
 \end{array}$$
  

$$\begin{array}{r}
 58.72 \\
 19.37 \\
 \hline
 39.35
 \end{array}$$
  

$$\begin{array}{r}
 157.1 \\
 32.578 \\
 \hline
 124.522
 \end{array}$$

## §. 2. Multiplication in Decimals.

Multiplication in Decimals.

**V**Hether the Number be a Whole Number, Decimal, or Mixt with Mixt, or otherwise, the *Multiplication* is performed as in Whole Numbers; only that after the Product is found, to know how many of them are Whole, and how many are Decimals, you must separate the one from the other by a Point, telling how many Places of Decimals there are in Multiplicand and Multiplier, for so many there must be in the Product.

0.005

$$\begin{array}{r}
 0.005 \\
 0.03 \\
 \hline
 0.00015
 \end{array}$$
  

$$\begin{array}{r}
 0.15 \\
 3.21 \\
 \hline
 0.4815
 \end{array}$$
  

$$\begin{array}{r}
 12.301 \\
 .0021 \\
 \hline
 0.0258321
 \end{array}$$
  

$$\begin{array}{r}
 0.0057 \\
 0.0008 \\
 \hline
 0.0000456
 \end{array}$$

## §. 3. Division in Decimals.

**D**ivision in *Decimals* will give the same Rule as before, if you conceive the Dividend to be the Product, and the Divisor and Quotient to be Multiplicand and Multiplier, for then it will follow from the former, That there must be as many Places of Decimals in the Divisor and Quotient as there are in the Dividend, and that being certain how many there are in the Dividend, and how many in the Divisor, you must take so many Places of Decimals in the Quotient, as with those Places in the Divisor (which are known) will make up the Number in the Dividend. So that if there be five Places of Decimals in the Dividend, and three in the Divisor, there will be two in the Quotient.

Division in Decimals.

Divisor. Dividend. Quotient.

$$28.64 \quad 77443692 \quad (27.040$$

$$2864 \quad 77443692 \quad (.27040$$

If there be Places of Decimals in the Divisor, and none in the Dividend, add as many Cyphers to the Dividend, making them Decimals, and work as before.

$$5.71 \quad 1713.00 \quad (30$$

$$.72 \quad 3816.00 \quad (53$$

And if all the Places in the Divisor and Quotient will not amount to the Quantity of Places in the Dividend, then place as many Cyphers before the significant Figures of the Quotient, as will make up the Number.

$$72 \quad 3.816 \quad (.053$$

$$72 \quad 0.3816 \quad (.0053$$

Lastly, If after Division of any Number, there remain after all, some part, add a Cypher or Cyphers to the Dividend, and that part of the Quotient arising from these Cyphers will be Decimals.

Also if any thing remain after the Square Root, add two Cyphers; after the Cube Root, three; and the Quotient will give the Decimal Fraction.

## §. 4. Reduction of Fractions into Decimals, and contrarily, viz.

**A**N Ordinary Fraction will be reduced into a Decimal of one Place, by multiplying the Numerator by 10; of two Places, by 100; of three, by 1000, &c. and dividing the Product by the Denominator. So  $\frac{1}{4}$  will be

Reduction of Fractions into Decimals.



be  $\frac{7}{10}$ , or .75, by multiplying 3 by 100, which is 300, and dividing 300 by 4. So  $\frac{1}{2}$ , or 19 s. will be found .95

Fractions of Fractions must be reduced into one Ordinary Fraction, and then put into Decimals. So 2 l. 19 s. 11  $\frac{1}{2}$  d. will be found in Decimals 2.9993; and multiplied (as before was shewed in Fractions) by it self, will produce 8.9956, which is 8 l. 19 s. 11 d. 3 f.

The Decimals for Shillings may be found by taking the half of the Number of Shillings, as of 16 s. is .8; of 10 s. .5; of 2 s. .1; of 1 s. .75; of 0 s. .45; of 1 s. .05

But it being tedious to convert the Ordinary Fractions this way, it is best to have Tables prepared and made ready for Use, of the most notable known Parts of Money, Weights, and Measures, as follow in the next Page.

The making of these Tables, or any other the like, is done by making the Integer 1, and adding Cyphers to it, and then taking Halves, Quarters, and Parts, 'till you come to the least Denomination, whereby the whole Table may be completed. As 1 l. I make 1.0000; then is the  $\frac{1}{2}$  or 10 s. .5; the  $\frac{1}{4}$  or 5 s. .25; and the  $\frac{1}{8}$  of that, or 1 s. .05: So having 1 s. 2 s. will be .1; 3 s. .15; 4 s. .2; and so the Table of Shillings is made: And because 12 d. is equal to .05, 6 d. will be .025; 3 d. .0125; and 1 d. .00417; which will make the Table of Pence. And after this manner all the rest are made.

The Uses of these Decimal Tables, First, are to turn any Number of Shillings, Pence, or Farthings, into Decimals: As 3 l. 15 s. 6  $\frac{1}{2}$  d. would be in Decimals 3.7771

$$\begin{array}{rcl} 15 \text{ Shillings} & = & .75 \\ 6 \text{ Pence} & = & .025 \\ 2 \text{ Farthings} & = & .0021 \\ & & \hline & & .7771 \end{array}$$

I seek 15 s. against which is .75, then 6 d. .025, then 2 f. is .0021, which added is .7771

So for *Averdupois* Little Weight, 6 Pound, 12  $\frac{1}{2}$  Ounces, will be 6.78125: So 3 Months and 6 Days will be .2664, &c.

The second Use is to turn any Number of Decimals into the known Parts of what they represent, whether Money, &c.

Example, 3.7771 signifies 3 l. 15 s. 6  $\frac{1}{2}$  d. By first seeking the greatest Number next to .77, which is .75, for 15 s. then taking that out of .7771, leaves .0271, which amongst Pence is 6 d. and leaves .0021, which amongst Farthings is 2 f.

So in *Averdupois* Small Weight, 32.5786 would be 32 Pound, 9 Ounces, and 4 Drams, thus: The next less to .5786 is .5625 for 9 Ounces, and there remains .0261, which will be found 4 Drams.

## DECIMAL TABLES.

Table I. English Coin, 1 l. Integer.	Table III. Averdupois Great Weight, Int. 1 C.	Table IV. Averdupois Little Weight, Int. 1 lib.	Table VI. Bakers in Decimals, Integer 1 Foot.
Penc. Dec. Parts.	Lib. Dec. Parts.	Oun. Dec. Parts.	Inch. Dec. Parts.
11 .045833	27 .34171	15 .0375	11 .916666
10 .041666	26 .32142	14 .0375	10 .833333
9 .0375	25 .223214	13 .8125	9 .75
8 .033333	24 .214285	12 .75	8 .666666
7 .029166	23 .25337	11 .6875	7 .583333
6 .025	22 .196428	10 .65	6 .5
5 .020833	21 .1875	9 .5625	5 .416666
4 .016666	20 .178571	8 .5	4 .333333
3 .0125	19 .169042	7 .4375	3 .25
2 .008333	18 .160714	6 .375	2 .166666
1 .004166	17 .157857	5 .3125	1 .083333
Farth.	16 .14857	4 .25	Quar.
3 .00312	15 .137857	3 .1875	5 .019531
2 .002833	14 .125	2 .125	4 .015625
1 .001041	13 .11671	1 .0625	3 .011718
Table II.	12 .107142	Dra.	2 .007812
Troy Weight, Integer 1 Ounce.	11 .098214	15 .058593	1 .003906
Penny-weight the same with still.	10 .89285	14 .054087	Quar.
Grain. Dec. Parts.	9 .88337	13 .050781	3 .002939
23 .047916	8 .871428	12 .046875	2 .001953
22 .045833	7 .8635	11 .42968	1 .000976
21 .04375	6 .85571	10 .40625	Table V.
20 .041666	5 .84857	9 .38281	Liquid Measure.
19 .039583	4 .84142	8 .35937	Int. a Gallon 2.
18 .0375	3 .83428	7 .33593	Pints. Dec. Parts.
17 .035416	2 .82714	6 .3125	3 .002939
16 .033333	1 .82000	5 .28906	2 .001953
15 .03125	12 .025	4 .26562	1 .000976
14 .029166	11 .022916	3 .24218	Table V.
13 .027083	10 .020833	2 .21875	Liquid Measure.
12 .025	9 .01875	1 .19531	Int. a Gallon 2.
11 .022916	8 .016666	1 .17187	Pints. Dec. Parts.
10 .020833	7 .014583	1 .14843	3 .002939
9 .01875	6 .0125	1 .12500	2 .001953
8 .016666	5 .010416	1 .10156	1 .000976
7 .014583	4 .008333	1 .07812	Table V.
6 .0125	3 .00625	1 .05468	Liquid Measure.
5 .010416	2 .004166	1 .03125	Int. a Gallon 2.
4 .008333	1 .002083	1 .00781	Pints. Dec. Parts.
3 .00625	0 .99991	1 .00390	3 .002939
2 .004166	0 .99782	1 .00195	2 .001953
1 .002083	0 .99573	1 .00097	1 .000976



## SECTION VI.

Of Logarithms, which are Numbers, that differ Arithmetically, as the Numbers answering them differ Geometrically, and serve to ease Multiplication, Division, and Extracting the Roots, with many other Uses.

## §. 1. To find a Logarithm.

To find a Logarithm.

**I**N the first Page of the Table of Logarithms, Printed in the Second Part, the Logarithms answering to all Numbers under 100 are easily found, viz. the Logarithm of 38 is 1,579783, of 72 is 1,857332, &c. If the Number consist of three Places, that is, a Number under 1000, look for the Number in the Table under N, and the Logarithm is found against it in the Column under 0; so the Logarithm of 349 is 542825, of 893 is 950851. If the Number be of four Places, and under 10000, seek the three first Figures under N as aforesaid, and the last Figure on the top, under which in that Column, lineally against the first three Figures, you have the Logarithm; as for Example, the Logarithm of 3583 is 554247; finding 358 under N, against it in the Column under 3 is the Logarithm aforesaid: So the Logarithm of 4268 is 630224, of 9546 is 970821. But if the Number be above 10000, and under 100000, you will find it by the Difference, and the Table of Parts Proportional, Printed at the End of the Tables of Logarithms: Thus, if the Logarithm of 35786 be required, first seek the Logarithm of 3578, which will be 553649, and the Common Difference under D. 121; with this Difference enter the Table of Parts Proportional, and find 121 in the first Column under D. and then lineally against that Number, and under 6, the last Figure of the last Place of the Number 35786, found at the Head of the seventh Column, you will find 72, which added to the Logarithm of 3578, viz. 553649, makes 553721, the Logarithm of 35786.

## §. 2. Of the Indices.

Indices

**B**UT before I proceed to find Numbers answering to Logarithms, I will shew what is meant by the first Figure prefixed or to be prefixed to a Logarithm; for in the first 100 Logarithms there is a Place more than in the rest, which is by Mr. Briggs called the *Characteristick*, by me the *Index*, for it shews of what nature, or how far from Unity the first Figure of any Number stands. The Index of Unity is 0, of Tens is 1, of Hundreds is 2, of Thousands is 3, &c. as in the following Example, the Index of 7 is 0,

of

of 3 is 2, of 5 is 4, of 7 is 5, and according to this Rule, an Index must be placed to all the Logarithms in the Table.

Indices	543210
Numbers	754327

But if you deal with Fractions turn them into Decimals, and then for the Indices, according as their Places stand from Unity, take their Complements to 10; as if it stand next Unity take 9, if two Places from it take 8, if three 7, &c. setting a Tittle over the heads of them, so those Indices will stand quite contrary, as you will see by Examples.

$$10.9\bar{8}876 \\ 21.5782$$

Whence the Index of the Logarithm of 0.037 will be 8. Thus the Logarithm of 5784 in the Table will be found to be 762228, and the Index of the first Figure 5 being 3 as before, the Logarithm will be 3,762228.

5784	3,762228
578.4	2,762228
57.84	1,762228
.5784	9,762228
.005784	7,762228

In these five Examples, the Logarithm is the same, but the Index alters according to the Distance of the first significant Figure from Unity; as in the second Example, the Index of 5 is 2, but in the fourth Example, the Index of 5 is 9 with a Tittle, and of the last is 7, because the third from Unity is a Decimal.

## §. 3. To find the Number to a Logarithm.

**T**O find the Number answering to a Logarithm given, omitting the Index, seek in the Table for the Logarithm equal or next less to the Logarithm given, the Number in the Column under N. with that on the top over the Logarithm, is the Number desired, which must be ordered according to the Index. Example. The Logarithm 3,544821; omitting the Index 3, I find 544821 to answer 3506, which the Index 3 shews to be all Integers; but if the Index had been 1, then the Number would have been 35.06, that is, 35 whole and .06 hundred Parts; and if 2, then 3506, all Decimals; if 3, then .03506, &c.

But if the Logarithm be not exactly to be found, and five Places be required, find the Number to four Places as before, noting the Common Difference under D, then take the Difference betwixt the Logarithm given,

and



and the Logarithm found in the Table less than it; seek the Common Difference in the Table of Proportional Parts under D. and in that Line find out the Difference of the Logarithms, and at the top just above it you have the fifth Figure. Example of the Logarithm 2,543612, the Logarithm next less is 543571, answering to 3496; the Common Difference is 124, the Difference of the Logarithms is 41, which in the Table of Proportional Parts against 124 gives 3; so that the absolute Number is 34963, and because the Index is 2, the Number will be 349 whole and  $\frac{3}{10}$  Parts, or 349.63

§. 4. Addition of two or more Logarithms.

Addition in Logarithms.

**F**irst, If the Indices be both (or all) Integers or of whole Parts, add them as usually. But, Secondly, If the Indices be unlike, that is, some of Integers, some of Parts, and if the Sum of the Indices be 10, or above, cast away 10, the Remainder is the Index of Integers; if under 10, Decimal Parts. Lastly, If the Indices be both of Decimal Parts, and when added be under 10, add 10 to them; if just 10, then Unity; if above 10, cast 10 away; the Index thus gotten is always Decimal Parts.

Examples.

2,057821	2,257242	9,397941	9,875061
7,583210	9,875062	9,875062	8,698972
9,641031	8,698971	9,273003	8,574033
	0,811275		

§. 5. Subtraction in Logarithms.

Subtraction in Logarithms.

**I**f the Indices be of Integers, then as usually. If the Indices be either or both of Decimals, observe whether the Index of the higher be a smaller Figure than the lower, if it be add 10 to it; and if the higher be of greater value than the lower, (that is, a bigger Index by Place) then the Remainder will be Integers; if not, Decimal Parts.

Examples.

2,033421	9,875062	9,875062	1,235781
9,875062	2,033421	8,574031	3,572141
2,153359	8,41641	1,301031	7,663640

The Logarithm of a Fraction is found, by subtracting the Logarithm of the Denominator from the Logarithm of the Numerator; as  $\frac{1}{2}$ ; the Logarithm of 4 is 0,602060, out of the Logarithm of 3, 0,477121, leaves the Difference 9,875061, the Logarithm of .75

The

The most of the admirable Uses of the Logarithms are comprehended in the following Rules.

§. 6. Multiplication by Logarithms.

**T**O multiply one Number by another, is nothing but to add their Logarithms, the Sum is the Logarithm of the Product.

Multiplication by Logarithms.

Multiplicand	32	1,505150	5.12	0,709265
Multiplier	52	1,716003	1.55	0,190332
Product	1664	3,221153	7.936	0,899497

§. 7. Division by Logarithms.

**T**O divide one Number by another, is to subtract the Logarithm of the Divisor from the Logarithm of the Dividend.

Division by Logarithms.

Dividend	7286	3,862489	4.512	9,654369
Divisor	32	1,505150	0.315	8,498311
Quotient	227.8	2,357339	14.32	1,156058

§. 8. Extraction of the Square and Cube Roots.

**T**O square a Number is to multiply its Logarithm by 2, to cube it by 3, to square-square it by 4, &c. To Extract the Square Root is to halve the Logarithm, or divide it by 2. To Extract the Cube Root is to divide the Logarithm by 3, the Square-square by 4.

Extraction of the Square and Cube Roots.

Examples.

Number	5832	Logarithm	4,879852
Square Root	275.37	2)	2,439926 for the Square Root.
Number	75832	Logarithm	4,879852
Cube Root	42.327	3)	1,626614 for the Cube Root.

Thus far all the several and Prime Parts of Arithmetick have been handled, hereafter the Comparative Part shall be shewed, which useth all the former Rules, and no other, and will by Practice easily be attained.

To end this Section, I shall insert the Characters of some Letters used by the Romans, and by People under their Subjection, and continued often in these days, and are these; I for 1, V for 5, X for 10, L for 50, C for 100, D for 500, and M for 1000; and sometimes thus I 500, C 1000; and note, that I before V or X, and X before L or C, takes away one or ten, as IX 9, IV 4, XL 40, XC 90, &c.

SECT.



## SECTION VII.

## Of the Comparative Part of Arithmetick.

## §. 1. The Golden Rule or Rule of Three.

The Golden  
Rule or Rule  
of Three.

**T**he Golden Rule, Rule of Three, or of Proportion, is that by which most of the Questions of use in all manner of Traffick, or Business of this Life, are answered. I divide this Rule into four Parts: 1. *Direct*, 2. *Indirect* or *Backward*, 3. *Double Rule Direct*, 4. *Double Rule Indirect*.

## The Single Rule of Three Direct.

Golden Rule  
Direct.

**F**irst, The *Single Rule Direct* finds a fourth Number, in such Proportion to the third, as the second is to the first; or, As the first is to the second, so is the third to the fourth. Let the Terms stand thus;

$$1 . 2 :: 3 . 4$$

And note, That the first and third Terms, and the second and fourth, are of the same Denominations; as if the first be of Moneys, Weights, Measures, &c. so shall the third; and so as the second, the fourth.

This Rule requires (and is to be known thus) that if the second Term be greater or less than the first, the fourth Term shall be likewise greater or lesser than the third: Or in the Question, if more require more, or less less, then use this Rule *Direct*, and multiply the second and third Terms together, and divide the Product by the first Term, and it gives the fourth Term or Answer. Example. If 4 Yards cost 8 s. what will 8 Yards cost? Answer 16 s.

$$4 . 8 :: 8 . 16$$

This Rule bids you multiply 8 by 8, which makes 64, and divide by 4, and it gives 16 the Term required. Let that Term therefore of the three, which makes the Question, whether it be of Value or Price, be set in the third Place, and that which is of the like Name or Denomination set in the first Place, and the Number remaining set in the second, of which nature the Number sought must ever be. As for Example, if the Question be thus put, What will 9 Yards cost, if 2 Yards be bought for 3 s? Answer 22 s. 6 d.

$$2 . 3 :: 9 . 22\frac{1}{2}$$

Again, If 12 Yards of Damask will line 16 Yards of Velvet, how much Damask will line 24 Yards of Velvet? Answer 18. To be placed thus:

$$16 . 12 :: 24 . 18$$

The Rule requiring the multiplication of the second and third Terms, viz. 12 by 24 makes 288, which divided by 16, gives the Answer 18.

Therefore if an Unit or 1, as 1 Yard, 1 Pound, be in the first Term, then the Rule is wrought by Multiplication only. Example; If 1 Yard cost 16 shillings, what will 32 Yards cost? Answer (by multiplying 32 by 16) 512 shillings, or 25 l. 12 s. by dividing by 20.

## Rules of Practice.

**H**ence come those Rules called *Rules of Practice*, which shew the true Price or Value of any Parcel of Goods, sold by the Pound, Ell, Yard, Dozen, Gros, or any other Thing, whereof the first Term is one.

The first and plain ordinary way is by *Reduction*, or bringing the Price of the Pound, Yard, Ell, &c. into the lowest Denomination of usual Moneys, as hath been taught in *Reduction*. Example; At 1 s. 2 d. the Pound, what comes 152 Pounds to? Answer 8 l. 17 s. 4 d. That bring all into Pence, and say,

$$1 . 14 :: 152 . 9$$

152 by 14 gives 2128 Pence, which reduced by dividing by 12 gives 177 s. 4 d. that is 8 l. 17 s. 4 d. by halving of 17.

Example 2. If 1 Pound cost 3 s. 6 d. what shall the great Hundred and 5 Pound cost? First reduce the 3 s. 6 d. into Six-pences, that is 7 Six-pences, and because the great Hundred is 112 lb. the Pounds will be 117. Then the Question will stand thus:

$$1 . 7 :: 117 . \text{Answer } 819$$

117 by 7 is 819 Six-pences, which is 409 s. 6 d., that is 20 l. 9 s. 6 d.

But if the Price fall out to be the *Aliquot* or Even Parts of a Pound, or of a Shilling, then the Work may be shortned much; as for Example: *Parts*. The Even Parts of a Shilling are these, 6 d. the half, 4 d. the third part, 3 d. the fourth part, 2 d. the sixth part, 1 d. the eighth part, and 1 d. the twelfth part: Therefore if any Question, wherein 1 is in the first place, be proposed, and if any of these Parts be in the second, you may find the fourth Term by taking the Part of the third, as is here required.

At 6 d. the Yard, what comes 352 Yards to? Answer 176 s. by taking the half of 352, which is 176 s. or 8 l. 16 s.

At 3 d. the Yard, or Pound, or Ounce, what comes 74 to? Answer 18 s. 6 d. by dividing 74 by 4, as before, which is 18 s. 6 d.

But if the Question fall not right upon any of these Aliquot Parts, then

It signifies the  
fourth Term  
sought.



you must work oftner, as, *At 10 d. the Pound, what will 133 Pound give?* Answer *5 l. 10 s. 10 d.* by dividing 133 by 2 for 6 d. which will be 66 s. 6 d. and then by 3 for 4 d. which makes 44 s. 4 d. in all 110 s. 10 d. or 5 l. 10 s. 10 d. So for 8 d. take 4 d. twice; for 9 d. take 3 d. thrice; for 11 d. take 6 d. 3 d. and 2 d.

The Aliquot Parts of a Pound are, 10 s. the half, 5 s. the fourth part, 4 s. the fifth part, 2 s. the tenth part, and 1 s. the twentieth part: So 6 s. 8 d. is the third part, and 3 s. 4 d. the sixth part. Then to answer such Questions as fall upon these Even Parts, divide by these Even Parts, the Answer is Pounds, and the Remain shall be so many of those Parts as that part requires. Examples.

If 1 Pound cost 10 s. what will 135 l. cost? Answer 67 l. 10 s. Take the half of 135, which is 67 l. and 1 remains, which is 10 s.

*At 4 s. the Yard, what comes 89 Yards to?* Answer 17 l. 16 s. I divide 89 by 5 s. which gives 17 l. and 4 remains, which is 16 s.

But if it chance that the Question fall not upon those Parts, but upon others, as 8 s. take 4 s. twice, if upon 14 s. take 10 s. and 4 s. Example. *At 9 s. the Grofs, what comes 36 Grofs to?* I take 5 s. and 4 s. which is the fourth and fifth parts, and take those parts of 36, viz. the fourth part is 9 l. and the fifth part is 7 l. 4 s. in all 16 l. 4 s.

Even Parts of a Pound.	Parts.	Uneven of a l.	Divided into even Parts.	Parts.	Even Parts of an Hundred-weight.
s. d.		s.	s.		
10 00	$\frac{1}{2}$	19	10 5 4	2 4 5	56 $\frac{1}{2}$
6 08	3	18	10 4 4	2 5 5	28 4
5 00	4	17	10 5 2	2 4 10	16 7
4 00	5	16	10 4 2	2 5 10	14 8
3 04	6	15	10 5	2 4	8 14
2 06	8	14	10 4	2 5	7 16
2 00	10	13	4 4 5	5 5 4	4 28
1 08	12	12	10 2	2 10	2 56
1 03	16	11	5 4 2	4 5 10	1 112
1 00	20	9	5 4	4 5	
0 10	24	8	4 4	5 5	Fractions of an Hundred-weight.
0 08	30	7	5 2	4 10	98 7.8
0 05	40	6	4 2	5 10	96 6.7
Even Parts of a Shilling.		3	2 1	10 20	84 3.4
	Of a s.	d.			80 5.7
6 d.	$\frac{1}{2}$	11 d.	6 3 2	2 4 6	70 5.8
4	3	10	6 4	2 3	64 4.7
3	4	9	3 3 3	4 4 4	48 3.2
2	6	8	4 4	3 3	32 2.7
1	12	7	4 3	3 4	
1 ob.	8	5	3 2	4 6	

But

But because all this may the better be made plain and easie, I have added yet a more compleat Division of the Even Parts of a Pound, and the Uneven; the like of Pence, and the Even Parts of an Hundred Weight, and the Fractions of it. The Even Parts of Pounds and Shillings were before declared, the Uneven Parts are thus explained; as, for 11 s. the Table bids take 5 s. 4 s. 2 s. which are the fourth, fifth, and tenth parts; for 11 d. take 6 d. 3 d. and 2 d. which are the half, fourth, and sixth part.

The Uses are gathered easily from what hath been before taught; so that if this Question was proposed, *What comes 3 Peeces of Broad Cloth to, at 1 l. 12 s. 8 d. the Yard, every Peece being 27 Yards long?* First find the Yards, that is 3 times 27, which is 81, then multiply 81 by the Pounds, which here being but 1 makes 81; then for 12 s. take the tenth part and half of 81, which is 48 l. 12 s.; then for 8 d. take the third part twice, which is 54 s. in all 132 l. 6 s.

#### Examples in Practice for Navigation

1. About the Building of a Vessel, *At 11 l. 15 s. the Tun, what will a Ship of 342 Tun cost?* First multiply 342 by 11, and it makes 3762 l. then for 15 s. take the fourth part three times, which comes to 256 l. 10 s. in all 4018 l. 10 s.

2. About the Parts, *What will the Sixteenth Part of a Ship that cost 2432 l. 8 s. come to?* Turn the Pounds into Shillings, which are 68648 s., which divided by 16 gives 4290  $\frac{1}{2}$  s. that is 214 l. 10 s. 6 d.

3. About the Freight, *What comes 342 Tun to, at 3 l. 10 s. the Tun?* Multiply 342 by 3, and it gives 1026 l. take half of 342 for 10 s. and it gives 171 l. in all 1197 l.

4. About Wages, *At 23 s. 4 d. per Month for a Seaman, what is due after 2 Years and 3 Months?* The Months are 27; therefore the whole Pounds are 27, and for the 3 s. 4 d. the sixth part of 27, which is 4 l. 10 s. in all 31 l. 10 s.

5. For Averidge, or Loss by inevitable Accident, *The Loss comes to 943 l. the Value of the Goods aboard the Ship is 18000 l. what shall that Person pay that had Goods aboard worth 3246 l?*

18000 . 943 :: 3246 . Answer 170 l. 1 s. 1 d.

By multiplying the second and third, and dividing the Product by 18000, you have 170.0544, which by the Decimal Table comes to 170 l. 1 s. 1 d.

I will give one Question more in the *Rule Direct*, and work it at large four several ways, viz. 1. By the ordinary way of *Reduction*: 2. By *Fractions*: 3. By *Decimal Arithmetick*: And 4. By *Logarithms*. Which being rightly known, I will not further work any Question at large, because I desire to be short. Let this Question therefore be understood.

F

W



What shall  $\frac{1}{4}$  of a Yard of Velvet cost, when the Piece of 21  $\frac{1}{2}$  Yards cost 24 l. 6 s. 8 d?

*By Reduction.* First, By *Reduction*. The Rule stands thus:

$$21 \frac{1}{2} : 24 \text{ l. } 6 \text{ s. } 8 \text{ d.} :: \frac{1}{4} : q$$

Because the first and third Terms must be of one Name, I bring 21  $\frac{1}{2}$  Yards into Quarters, and they will be 86 Quarters; ther. I bring 24 l. 6 s. 8 d. into Pence, by multiplying by 20 and 12, as was taught before, which makes 5840 Pence; and the Rule stands thus:

$$86 : 5840 :: 3 : \text{Answer } 203 \text{ d. } 3 \text{ f.}$$

$$\begin{array}{r} 86 \overline{) 17520} \quad ( 203 \frac{3}{4} \\ \underline{172} \phantom{00} \\ 320 \\ \underline{258} \phantom{0} \\ 62 \end{array}$$

For to find the Farthings, I multiply 62 by 4, and it makes 248, which divided by 86 gives 3. Now 203 d. being divided by 12 gives 16 s. 11 d. So the Answer is 16 s. 11 d. and  $\frac{3}{4}$  or 3 f.

*By Fractions.* Secondly, By *Fractions*. The Rule will stand thus:

$$21 \frac{1}{2} : 24 \frac{1}{2} :: \frac{1}{4} : q$$

I multiply 24  $\frac{1}{2}$ , or  $\frac{49}{2}$ , by  $\frac{1}{4}$ , and it will give  $\frac{49}{8}$ , because the Byas  $\frac{1}{2}$  may be put out of them both. Then  $\frac{49}{8} \div \frac{1}{4} = \frac{49}{8} \times \frac{4}{1} = \frac{49}{2}$ . Now I seek how many Shillings, Pence, and Farthings, are in  $\frac{49}{2}$ , that is, I multiply 73 by 20, and it makes 1460, which divided by 86 gives 16 s. and there remains  $\frac{3}{4}$ . I multiply 84 by 12, and it gives 1008, which divided by 86 gives 11 d. and there rests  $\frac{3}{4}$ ; which multiplied by 4, and divided by 86, gives 3 f. in all 16 s. 11  $\frac{1}{4}$  d. for three Quarters of Velvet.

*By Decimals.* Thirdly, By *Decimals*. By the Table I put the Question into Decimal Fractions, and the Rule will stand thus:

$$21.5 : 24.3333 :: .75 : q$$

I multiply the two middle Terms together, which gives 18.249999, this I divide by the first Term 21.5, and it gives in the Quotient .8488, which in the Decimal Table gives 16 s. 11  $\frac{1}{4}$  d.

Fourthly,

Fourthly, By *Logarithms*. Set the first, second, and third Terms, in Decimals, as in the following Example, and find their respective Logarithms.

$$\begin{array}{r} 21.5 \quad 1.332438 \\ 24.3333 \quad 1.386195 \\ .75 \quad \underline{9.875061} \\ 1.261256 \\ .8488 \quad \underline{9.928818} \end{array}$$

I add the Logarithms of the second and third together, which makes the Logarithm 1.261256, from which I take the first Logarithm 1.332438, and there rests the Logarithm 9.928818, which being sought in the Canon gives the Number 8488, and because of the Index 9 they are all Decimals, and being sought for in the Table, as before, gives 16 s. 11  $\frac{1}{4}$  d.

*Note*, That in this Rule, if you multiply the second and third Terms together, the Product shall be equal to the Product of the first Term multiplied by the fourth, which may very well prove it, if required.

#### The Backward or Indirect Rule of Three.

Secondly, The *Backward or Indirect Rule of Three*, which is known by being contrary to the *Direct*; for whereas the former required, that more shall have more, and less, less; as, if 4 Yards cost 2 s. 8 Yards will cost more than 2 s. because it is double to 4 Yards, and so must the Answer be double to 2 s. viz. 4 s. But in this Rule more will require less, and less more; as, if 4 Horses in 6 Days eat 10 Bushels of Oats, 8 Horses will eat 10 Bushels in a fewer quantity of Days, viz. in 3. Here 10 Bushels being common is omitted, and the Question will stand thus:

$$4 : 6 :: 8 : 3$$

And the Rule bids you multiply the first and second Terms for a Dividend, which divide by the third, and the Quotient gives the Answer or fourth Term; as in the last Question, multiply 4 by 6, and it gives 24; which divided by 8 gives 3.

Example 1. If 20 Pioneers can finish a Work in 2 Months and 10 Days, how many Pioneers will finish that Work in 20 Days? Answer 66 Days.

Example 2. If for the Masting of a Room there needs 100 Yards of a Yard broad, how many Yards will be needful of  $\frac{1}{4}$  broad? In Decimals thus:

$$1 : 100 :: .75 : 133.33$$

Having put  $\frac{1}{4}$  into .75 divide 100 by it, and the Quotient will be the Answer, viz. 133.33 or 133  $\frac{1}{3}$ .

Example



Example 3. If a 2 d. Loaf of Bread weighed 6 lb.  $3\frac{2}{3}$ . when a Bowl of Rye cost 6 s. 6 d. what is a Bowl of Rye worth when a 2 d. Loaf of Bread weighs 2 lb.  $4\frac{2}{3}$ ? Answer 17 s.  $10\frac{1}{2}$  d.

### The Double Rule of Three.

Double Golden Rule.

Thirdly and Lastly, The Double Rule, both Direct and Indirect, or Forward and Backward, I comprise into one Rule, with two Operations only, which is usually wrought by two Positions of the Golden Rule.

Observe, That the given Terms are always five, whereof three are conditional and antecedent, or suppositious, the other two demand the Question, and are Consequents, matching or answering some of the former Antecedents; in so much, that with the Answer there will be as many Consequents as Antecedents, which must match one another in the same Denomination exactly.

Now for the right placing of the Question and Terms, first, the three Terms of the conditional Part are duly to be regarded: Let that which is the Principal Cause of Loss or Gain, Increase or Decrease, Action or Passion, be put in the first Place; that which betokeneth the Space of Time, Distance of Place, &c. be put in the second Place; and the remaining Part in the third. The conditional Part thus stated, the other two Terms wherein the Demand lies, must be placed so under the former Terms, that they may correspond one with another.

Rule I. Then, If the Blank, or Place sought, fall under the third Term, multiply the three last Terms for a Dividend, and the two first for a Divisor, and the Quotient gives the sixth Term desired.

Rule II. But, If the Blank fall under the first or second Terms, multiply the first, second, and fifth Terms for a Dividend, and the third and fourth for a Divisor; the Quotient gives the Answer. Examples will make all plain.

Example 1. If 12 Rods of Ditching be done by 2 Men in 6 Days, how many Rods shall be wrought by 8 Men in 24 Days? Answer 192.

Men.	Days.	Rods.
2	6	12
8	24	

Here Men, the Cause, is in the first Place, Days in the second, Rods in the third; the Match-Terms, 8 and 24, being placed as in the Example; the Blank is under third; wherefore 12 in 8 in 24 makes 2304 for the Dividend, and 2 in 6 makes 12 for the Divisor; the Quotient gives 192 Rods of Ditching to be done by 8 Men.

$$12 \times 24 \times 8 = 2304$$

Example 2. If 2 Men work 12 Rod in 6 Days, how many Men will work 192 Rods in 24 Days?

Set

Set the Rule as before is taught, and the Blank will fall under the first Term, which by the second way will give 8 Men.

Men.	Days.	Rods.
2	6	12
	24	192

Here I multiply the first, second, and last for the Dividend, viz. 2 in 6 in 192 makes 2304, and the third and fourth for the Divisor, viz. 12 in 24 makes 288.

$$288 \times 8 = 2304$$

### Simple Interest.

Questions of Simple Interest belong to this Rule, of which take this Simple Interest. Example: If 100 l. in 12 Months give 6 l. what shall 40 l. in 6 Months give?

l.	Months.	l.
100	12	6
40	6	

6 in 40 in 6 is 1440 for the Dividend, and 100 in 12 is 1200 for the Divisor.

$$1200 \times 1.2 = 1440$$

If there be the same Supposition, and it be required to know the Principal that yielded 1 l. 4 s. in 6 Months, the Answer will be 40 l. by the second way.

100	12	6
	6	1 l. 4 s.

These Rules will work best by Decimals, where the Year is the Integer, Months and Days are Decimals.

### §. 2. Fellowship or Partnership.

The Rule of Fellowship or Partnership is of very great use to Balance Fellowship or Partnership Accounts, and for Accounts amongst Merchants and Owners of Ships; for when any number of Persons put together a general Stock, so that it be required to give to every one his proportional Share of the Loss or Gain, the Golden Rule several ways repeated will fully answer such Questions. For, As the whole Stock, (or general Antecedent) is to the Total thereby gain'd or lost; (which is the general Consequent:) So each Man's particular Share, is to his proper Share of Loss or Gain. Wherefore, let the several Moneys of every Partner be gathered into one Sum, which make the first Term, the common Gain or Loss the second, every Man's particular



ticular Share the third, working the *Golden Rule* for many several times as there are Partners.

There be two Parts of this Rule, *without Time*, and *with Time*.

*Fellowship without Time.*

*Fellowship without Time.* A, B, and C freight a Ship with Wine, viz. A lays out 1342 l. B 1178 l. C 630 l. the whole 212 Tuns of Wine is sold at 32 l. a Tun; what shall each Man receive? First, I find out the Price received, by multiplying 212 by 32, which makes 6784; then I add up the several Stocks, 1342 l. 1178 l. and 630, which make 3150 l. and the work will stand thus:

$$\begin{array}{r} 2150 \cdot 6784 :: \left\{ \begin{array}{l} 1342 \cdot \text{Answer } 2890.199 - \\ 1178 \cdot \text{Answer } 2537.001 - \\ 630 \cdot \text{Answer } 1356.800 \end{array} \right. \\ \text{Proof } 3150 \qquad \qquad 6784 \end{array}$$

If one dye indebted to eight several Persons, viz. to A 100 l. to B 86 l. to C 75 l. to D 60 l. to E 54 l. to F 32 l. to G 24 l. to H 15 l. and all his Goods will but amount to 150 l. the Creditors dividing according to Proportion, their Shares will be in Decimals, A 33.5323, B 28.9238, C 25.2242, D 20.1802, E 18.1514, F 10.7623, G 8.0517, and H 5.4448; all which make up 150 l. their whole Debt being 446 l. which is the Proof of this Rule.

A hath Half a Ship, B a Quarter, C One Sixteenth, and D Three Sixteenths, the Master of the Ship brings an Account, and clears 120 l. how much must each Person have? Accompt the Ship 16, and the Gain 120 l.

$$\begin{array}{r} 16 \cdot 120 :: \left\{ \begin{array}{l} 8 \cdot \text{Answer } 60 \\ 4 \cdot \text{Answer } 30 \\ 1 \cdot \text{Answer } 7.5 \\ 3 \cdot \text{Answer } 22.5 \end{array} \right. \\ \qquad \qquad \qquad 120 \end{array}$$

*Fellowship with Time.*

*Fellowship with Time.* A Ships Company, viz. Officers, Midship-Men, and Sailors take a Prize of 300 l. which is to be divided amongst them, according to their Pay and the Time they have been on Board; the Officers and Midship-Men 5 Months, and the Sailors 3 Months; the Officers one with another 40 s. per Month, the Midship-Men 30 s. per Month, and the Sailors 22 s. per Month; there were 6 Officers, 12 Midship-Men, and 34 Sailors: What must each Party have of the Prize? For a general Stock I begin first with the Officers, which are 6, and that multiplied by the Rate of 40 s. gives 240, which multiplied by the 5 Months makes 1200 s. After the same fashion I find the Midship-Men's Stock 1800 s. and

and the Sailors 5544 s. All added together make 8544 s. for the whole Stock, and the Work will stand thus:

$$8544 \cdot 300 :: \left\{ \begin{array}{l} 1200 \cdot \text{Answer } 42.12327 \text{ l.} \\ 1800 \cdot \text{Answer } 63.2029 \text{ l.} \\ 5544 \cdot \text{Answer } 194.6629 \text{ l.} \end{array} \right\} 299.999 = 300$$

And turning the Decimals into Money by the Table, it will give for

	l.	s.	d.
Officers	42	02	06
Midship-Men	63	04	00 $\frac{1}{4}$
Sailors	194	13	05

A, B, and C, enter into Partnership the first of January for a whole Year, A the same Day disburs'd 100 l. whereof he received back again upon the first of April 20 l. B payeth in the first of March 60 l. and more the first of August 100 l. C payeth in the first of July 140 l. but the first of October with draweth 40 l. at the Years end their clear Gain is 142 l. How much thereof ought every particular Person to have? Answer, A 51 l. B 55 l. C 36 l. which makes the whole Gain 142 l. without consideration of Interest. For A, 100 into 3 is 300 l. and 80 in 9 is 720, in all 1020 l. for A. For B, 60 in 10 makes 600, more 100 in 5 is 500, in all 1100 for B. For C, 140 in 3 is 420, and 100 in 3 is 300, in all 720 for C. Now 1020, more 1100, more 720, makes in all 2840 for the general Antecedent, and the Gain 142 for the general Consequent; then the Rule will stand thus:

$$2840 \cdot 142 :: \left\{ \begin{array}{l} 1020 \cdot \text{Answer } 51 \\ 1100 \cdot \text{Answer } 55 \\ 720 \cdot \text{Answer } 36 \end{array} \right\} \text{which in all is } 142 \text{ l.}$$

## SECTION VIII.

### Of Simple and Compound Interest.

#### §. Simple Interest.

**S**IMPLE INTEREST is of Use amongst Merchants, and to find the Resolution of such Questions, as are commonly propos'd of this kind, which are the Forbearance of Money, or Rebate, which is the present Worth of Money due hereafter, the Time is accounted by Days, which by the following Table is easily found.



334	January	0
306	February	31
275	March	59
245	April	90
214	May	120
184	June	151
153	July	181
122	August	212
92	September	243
61	October	273
31	November	304
0	December	334

This Table contains three Columns, the last shews the Days from the first of *January*, or the beginning of the *Year*, to the beginning of each Month through the whole Year; the middle Column contains the Names of the Months; and the first shews the Days from the last of *December* to the ending of each Month. Now there being in one Year  $365\frac{1}{4}$  Days, in two Years  $730\frac{1}{2}$ , in three Years  $1095\frac{3}{4}$ , and in four Years  $1461$  Days, if the Question be of intermediate Times, it will be from the Beginning of a Year, or in the Middle, or Part of two Years.

*Example 1.* From the Beginning of the Year to the Eleventh of *October* will be found 284 Days; for by the third Column in the Table from the Beginning of the Year unto *October* is 273 Days, which added to the 11 Days in *October* makes 284.

*Example 2.* From the Twelfth of *March* to the Sixteenth of *December* will be found 279 Days; for from the Beginning of the Year to the Twelfth of *March* is 71, found as before, and so to the Sixteenth of *December* 350 Days, now take 71 from 350, and there remains 279.

*Example 3.* From the Tenth of *June*, 1677, to the Fifth of *February* following, will be found 240 Days; for by the first Column to the last of *June* is 184, which added to 20 Days in *June* makes 204, to which adding the 31 Days in *January*, and the 5 in *February*, it makes in all 240.

Having found the Days as before, the next Table will shew the Simple Interest of One Pound for any Number of Days, under 10000, at 6 per Centum.

The first Column of which Table shews the Days, and may be Thousands, Hundreds, Tens, or single Days, and the other Columns shew the Interest of 1 *l.* according to the Number of Days in the first Column.

Days.

	Thousands.			Hundreds.		Tens.	Units.
	<i>l.</i>	<i>s.</i>	<i>d.</i>	<i>s.</i>	<i>d.</i>	<i>d.</i>	<i>Parts.</i>
1	00	03	03.452	00	03.945	00.394	.039
2	00	06	06.904	00	07.890	00.789	.079
3	00	09	10.356	00	11.835	01.183	.118
4	00	13	01.804	01	03.780	01.578	.157
5	00	16	05.260	01	07.726	01.972	.197
6	00	19	08.712	01	11.671	02.367	.236
7	01	03	00.164	02	03.616	02.761	.276
8	01	06	03.616	02	07.561	03.156	.316
9	01	09	07.068	02	11.506	03.550	.355

*Example.*

What is the Use of 1 *l.* for 1732 Days? Answer  $5\text{ s. }8\frac{1}{4}\text{ d.}$

Days.	<i>s.</i>	<i>d.</i>
1000	= 03	= 03.452
700	= 02	= 03.616
30	= 00	= 01.183
2	= 00	= 00.079
1732	= 05	= 08.330

And if you turn the Interest of 1 *l.* found as before, into Decimals, and multiply it by any Sum propounded, it gives the Interest of that Sum for the Days propounded, at 6 per Cent. Simple Interest.

But if you would work the said Questions by Numbers without the Table, you must know that the Interest of 1 *l.* for one day at 6 per Cent. per Ann. is .000164384, at 5 per Cent. .0001369836, both of them found by dividing 6 or 5 by 365, and if it be required to give the Simple Interest of any Sum for a certain Number of Days at 6 per Cent. find the Interest of 1 *l.* for that time, by multiplying .000164384 by the Days, and multiply the Interest found by the Sum propofed, and it gives the Answer. Or easily by the Logarithms, thus: Add the Logarithm 7.215862 for 6 per Cent. or 7.136665 for 5 per Cent. to the Logarithm of the Days, and to the Logarithm of the Sum propofed, the Sum of these three Logarithms is the Logarithm of the Interest. And for the Rule for Rebate, or the Present Worth of a Sum of Money due some Days after, find the Interest of 1 *l.* for that time, and add an Unit to it, by which divide the Sum propounded, and the Quotient gives the Present Worth. Thus much of Simple Interest.

G 2

p. 2. Of



## §. 2. Of Compound Interest.

Compound Interest.

Questions of *Compound Interest*, or *Interest upon Interest*, are most easily answered by *Logarithms*, and being prepared with *Logarithms*, if the Interest be at 6 per Cent. find the *Logarithm* of 1.06, and divide it by 2 for Half-Years, by 4 for Quarters, by 12 for Months, by 52 for Weeks, and by 365 for Days, as in the Table annexed, which will be of special use to answer Questions of this nature.

Logarithm of 1.06	0,025306
Half-Year	0,012653
Quarter	0,006326
A Month	0,002109
A Week	0,000527
A Day	0,000075

The Six Propositions, for resolving Questions of *Compound Interest* and *Annuities*, at 6 per Cent. propofed by Mr. Oughtred, , and performed in as many Resolutions following, noted with these six Letters, *A, B, C, D, E, F*, are:

Prop. I. *P lends to R 1 l. for 3 Years, what must P receive at the End of the Term?* Answer *A* 1 l. 3 s. 10 d.

Prop. II. *R oweth unto P 1 l. to be paid at the End of 3 Years, P desires his Money presently, what is it worth in ready Money?* Answer *B* 16 s. 9  $\frac{1}{2}$  d.

1.06	0,025306
	3
<i>A</i> 1.1910	0,075918
<i>B</i> .8396	9,924081 Arithm. Compl.

By multiplying the *Logarithm* of 1.06 by 3 gives 0,075918, the *Logarithm* of *A*, which is 1 l. 3 s. 10 d. And taking the *Arithmetical Complement* of that *Logarithm*, by subtracting it from 10, it gives the *Logarithm* 9,924081 for *B*, .8396, or 16 s. 9  $\frac{1}{2}$  d.

Prop. III. *P hath an Annuity of 1 l. per Annum to be paid by R, who forbears Payment for 3 Years, what will it then amount unto?* Answer *C* 3 l. 3 s. 8 d.

Prop. IV. *R is to pay unto P 1 l. at the End of 3 Years, but desires to pay an Annuity or Yearly Rent, what must R pay every Year for these 3 Years?* Answer *D* 6 s. 3  $\frac{1}{2}$  d.

A lēfs

<i>A</i> lēfs 1 is .191	Logarithm	9,281033
1.06 lēfs 1 is .06		8,778151
<i>C</i> 3.1833	Difference	0,502882
<i>D</i> 0.3141	Arithm. Compl.	9,497117

*A* by the first Proposition was 1.191, which must be made lēfs by 1, and it leaves .191, and 1.06 lēfs by 1 is .06. The Difference of their *Logarithms* is 0,502882, the Number answering is *C* 3 l. 3 s. 8 d. which resolves the Third Proposition; and the *Arithmetical Complement* of the last *Logarithm* is 9,497117, the Number is 6 s. 3  $\frac{1}{2}$  d. which gives *D* the Answer of the Fourth Proposition.

Prop. V. *P has an Annuity of 1 l. per Annum, for 3 Years, what is the Present Worth in ready Money?* Answer *E* 2 l. 13 s. 5  $\frac{1}{2}$  d.

Prop. VI. *P has 1 l. to bestow upon an Annuity for 3 Years, what will it purchase Yearly?* Answer *F* 7 s. 6 d.

<i>C</i> 3.1833	Logarithm	0,502882
<i>A</i> 1.191	Logarithm	0,075918
<i>E</i> 2.6728	Difference	0,426964
<i>F</i> .3741	Ar. Compl.	9,573036

Subtract the *Logarithm* of *A* 1.191 from the *Logarithm* of *C* 3.1833, it leaves the *Logarithm* of *E*, whose Number is 2.6728, and answers the Fifth Proposition; and the *Arithmetical Complement* is the *Logarithm* of *F*, whose Number is .3741, and answers the Sixth Proposition.

Thus for 1 l. the Answers are fitted to all the Six Propositions, and the like Work must be made, if the Payments were half-yearly, quarterly, &c. taking the *Logarithm* answering in the little Table before expressed, and after the Answer is found for 1 l. by adding its *Logarithm* to the *Logarithm* of any other Sum, it gives the Answer accordingly. Example, if 352 l. 10 s. were due three Years hence, and it is desired to know the Present Worth, after the Rate of 6 per Cent. I add the *Logarithm* of 352.5, which is 2,547159, to the *Logarithm* of *B* 9,924081, found by the Second Proposition, and the Sum is 2,471240, the *Logarithm* of 295.97, or 295 l. 19 s. 6 d.





## CHAP. II.

## Of Practical GEOMETRY.

Practical Geometry.

**I** Now come to show you the Second Step, whereby you may ascend to the admirable Knowledge of the *Mathematicks*; for *Arithmetick* and *Geometry* are the *Foundations* of what we are about; and though I now defer the Teaching you the *Theory*, which you will have in the Last Part, yet the *Practice* you are now beginning, and I am ready to deliver you, will fettle you to the Use of the *Compasses*, and make you ready to measure whatsoever is Quantity, whether it be Distance on the Sea or Land, Heights of Hills, Mountains, Towers, Depths, Superficies, and Bodies; besides the Roundness of the Earth, and the Height or Distance of the Heavenly Bodies. I have not gone the ordinary way, I hope a better, more intelligible, and fitter for Use. I first begin some *Definitions*, mixing *Propositions* along, as the nature of them require, and according to my Ability to make all easie, and so to be retained in the Memory.

## SECTION I.

## Of several Definitions and Problems for Measures.

Definitions and Problems for Measures.

Fig. 1, 2, 3.

**T** Here are but Three *Dimensions*, viz. a *Line*, which is only Length; a *Superficies*, which is Length and Breadth; and a *Solid*, which is Length, Breadth, and Thickness; expressed by the first, second, and third Figures in the first Plate.

## Prop. I. Of a Line.

Line.  
Fig. 4.

**A** Straight Line, as *ab*, is drawn upon Paper commonly with a Ruler *bc*, and by turning the Ruler end for end, as *c* where *b* was, you may try whether it draws a straight Line or not, for if it trace by a Point the same Line again, the Ruler is straight.

To

## Sect. 1.

## Of Practical Geometry.

To draw a straight Line upon the Ground which is level, as between *a* and *b*, set up some Pickets, as *c* and *d*, which shall cover the Mark *b* Fig. 5 standing at *a*, and by them (or as many as need be) with a Line, Chord, or Chain, you may mark out the Line *ab* on the Ground.

But before I proceed any further, I must make known to you the ordinary Measures of our own Country, and repeat again part of the Table of *Long Measures*, before laid down in the *Arithmetick*, Cap. 1. Sect. 2. §. 1. viz. a *Palm* is 3 Inches, a *Foot* is 12 Inches, a *Yard* is 3 Feet or 36 Inches, a *Pace* is 5 Feet or 60 Inches, a *Pole* is 5 Yards and an half, a *Furlong* is 40 Pole, and a *Mile* is 8 Furlongs; the Gage for all these is the *Yard Standard* at *Guild-Hall*. But divers Countries have their divers Measures, as you will find by the Table in the Third Part, called *Foreign Weights and Measures compared with the English*, to which I refer you. Note likewise, that three Miles English or French are called a *League*.

Thus, whatever Line you measure upon the Ground or otherwise, whether by Inch, Foot, Yard, Pole, or Mile, you may make a Scale, by which the same may be represented and laid down in a straight Line, upon Paper or what else you think fit, (which Scales are called *Plane Scales*) after this manner: First, that all Plane Scales may be known, an Inch is commonly taken for the Common Measure to know them by, as in the seventh Figure, where the Scale *ab* is divided into 6 Inches, and the first Inch *bc* is divided into 10 Parts, which being made the Scale for your Measure, every Part is the Tenth of an Inch; in the next Scale every Part is the Twelfth, in the next the Twentieth, and the next the Thirtieth; all which the Boys must be made to understand.

But because these Scales only express the Tenths of Parts, there is another Scale yet more exact of ordinary use, called a *Diagonal or Decimal Scale*, as in the eighth Figure you may see; the Exactness ariseth from the Breadth, as in this Scale one Tenth of an Inch is actually divided into Ten Parts by the Diagonal, as in the Uses of this Scale shall hereafter be shewed you.

## Prop. II. Of a Circle.

**T** He whole Business of Dimension depending upon measuring of Lines and Angles, which last relate to a Circle, I have thought good to treat of a Circle in the second Place.

A Circle is described ordinarily with a Pair of Compasses, one End remaining fixt, the other moving about makes that Line which is called the *Circumference* or *Arch*, the Point fixt is called the *Center*, and the Distance from that Center to the Circumference (which remains always the same whilst you describe it) is called the *Radius* or *Semidiameter*, the Line that passeth from one part of the Circumference by the Center to the other is called the *Diameter*, equal to two *Radii*; as in the ninth Figure, *c* is the Center, *acb* is the Circumference, *ca*, *cb*, *cc*, and *cd* are all Semidiameters or *Radii*, and *ed* or *ab* are *Diameters*.

All



Degrees.

All Circles whether greater or lesser are divided commonly into 360 Parts, called *Degrees*, that Number allowing many Aliquot or Even Parts, as the Half is 180, the Third Part 120, the Fourth 90, the Fifth 72, the Sixth 60, the Eighth 45, the Ninth 40, the Tenth 36, the Twelfth 30, the Fifteenth 24, and the Eighteenth Part is 20.

Division of a Circle.

The Compasses at the same opening will go exactly 6 times about, or will describe each time 60 Parts or Degrees; therefore to divide any Circle into 360 Parts, set off 60 Degrees 6 times, as in *fig. 9*, divide each 60 into Halves, which is 30, and each 30 into 3 Parts, which will be 10 Degrees, each 10 Degrees into Halves for 5 Degrees, and each of those into 5 Parts by 4 Points into Degrees; as you see in the Figure.

Fig. 9.

Every Degree (if the Circle be so large) may be divided into 60 Parts called *Minutes*, and every Minute into 60 Parts called *Seconds*, and so into *Thirds*, *Fourths*, &c. so that all Circles, whether as great as the Heavens, or as little as a Penny, are always accounted to contain 360 Degrees, as you see in the little Circle *m n o p*. So that if you make two or three Circles greater than one another, and divide them as I have taught into 360 Degrees each, (which I advise you to do) they will be of good use.

Fig. 9.

Quadrant.

The *Quarter* of the Circle, or 90 Degrees, is called a *Quadrant*, there being 4 such in every Circle, viz. *b c e*, *c c a*, *a c d*, and *d c b*, which will be sufficient for the whole, if divided into 90 Parts.

Semicircle.

Two Quadrants, or that Part which is divided by a Diameter is called a *Semicircle*, which contains 180 Degrees, as in the same Figure, *a c b c* is a Semicircle.

### Prop. III. Of a Plain Right Lined Angle.

Angle.

**T**his is made by the Concourse of two straight Lines not lying direct, and is of three sorts, viz. a *Right Angle*, an *Acute Angle*, or an *Obtuse Angle*, all which are measured by a Circle, or Part of a Circle, for every one of these Angles contains to many Degrees, Minutes, &c. of a Circle, as are comprised or intercepted betwixt the two Sides of that Angle, (produced if need be) neither doth the Length of those two Sides, or a bigger or lesser Circle, alter the same at all. As in the Tenth Figure, if upon the Point *c* in the Line *g a* you move another Line, suppose *c b*, and beginning at *a* move it towards *d*, 'till it makes an Acute Angle, and contains less Degrees than 90, as the Angle *b c a* is 30 Degrees, but when it comes to *d*, it is then 90 Degrees, and is called a *Right Angle*, or a *Perpendicular*, for *d c* 90 Degrees falls right on *g a*, and makes the Spaces *d c a* and *d c g* equal, viz. both 90 Degrees; but after it be passed *d c*, then it is an *Obtuse* or blunt Angle, and contains more than 90 Degrees, 'till it comes to *g c*, which is 180 Degrees, as the Angle *f c a* is 120 Degrees. All which being perfectly understood, will avail much to the understanding of all the Natures of Angles.

Fig. 10.

Acute Angle.

Right Angle.

Obtuse Angle.

Note, That an Angle is commonly expressed by three Letters, the middle Letter standing at the Angular Point, and the other upon the Sides: And that

that instead of expressing Degrees and Minutes, &c. at large, I use the Character " for Minutes, " for Seconds, &c. as to set down an Angle of 32 Degrees and 42 Minutes, thus,  $32^{\circ} 42'$ .

To measure any Plain Angle is nothing else, but upon the Angular Point to describe a Circle (already divided) or part of it, and see how many Degrees and Minutes it contains, for that is the Measure thereof. As in the Eleventh Figure, suppose the Angle *a b c* was proposed to be measured, or to know how many Degrees and Minutes it contains: Upon the Point *a* I describe Part of one of my divided Circles, and find it  $32^{\circ}$ .

The Measure of an Angle.

Fig. 11.

Likewise if it were required to lay down an Angle of  $45^{\circ}$  upon the Line *a c*, and upon the Point *a*, I describe Part of my divided Circle, and take with my Compasses the Distance from *c* to 45, and place it from *c* to *b*, then is the Angle *b a c*  $45^{\circ}$ .

To lay down an Angle.

Fig. 12.

And to make one Angle equal to another Angle, is only to make that the same Equal Part of the Circle be contained in them both.

To make one Angle equal to another.

Hence it plainly appears, that let there be never so many Angles set upon one Point of a Line, as at *c*, Figure 13, all will be but two Right Angles, or 180 Degrees.

Fig. 13.

Likewise if two Lines cross one another, then they make 4 Angles, all equal to  $360^{\circ}$ , or the whole Circle; and the Cross or Head-Angles are equal, viz. *b c a* to *d c f*, and *d c b* to *f c a*, as in the Fourteenth Figure, they containing the same Number of Degrees; as you may prove in the Circle, the Demonstration follows in the Last Part

Head-Angles equal.

Fig. 14.

### Prop. IV. Of Parallels.

**P**arallel straight Lines in the same Plain are such, as if infinitely continued in the same Plain, would never meet, and 'till we come to the Last Part I shall only illustrate the same with a familiar Example: Imagine that in the Fifteenth Figure, *a b* was parallel to *c d*, then that those two Lines made but one broad Line, then by the last part of the Third Proposition, the Angle *f l b* will be equal to *c h g*, and to *l h d*, and to *a l h*, and so on the other side; so that the altern Angles are equal.

Parallels.

Fig. 15.

Therefore if *a b* and *c d* be parallel, and from the Point *m* in *c d* two Lines be drawn to the other Parallel *a b*, as at *n* and *o*, there will be five Angles marked on the inside, according to the Figures 1, 2, 3, 4, 5, by the last the Angles 1 and 4 and 3 and 5 will be equal, but the Angles 1, 2, 3, are equal to two Right Angles, and therefore the Angles 2, 4, and 5, will be equal to two Right Angles, or to  $180^{\circ}$ .

Fig. 16.

### Prop. V. Of Plain Figures, which are encompassed about with a Line or Lines: As,

I. **T**he Circle, whose Superficies or Area is contained within one regular crooked Line, as has been before laid down, to be described from one Center.

H

II. The



Ellipsis.

Fig. 17.

Triangles.  
Equilateral.

Fig. 18.

Fig. 19.

Fig. 20.

Rectangles.  
Fig. 21Fig. 22.  
Acute-angled  
Triangles.  
Obtuse.

Squares.

Fig. 23.

Oblong.

Fig. 24.

Rhombus.

Fig. 25.

Rhomboides.

Fig. 26.

Trapezes.

Multilateral.

Polygons Regu-  
lar.

Fig. 27.

Base.

Height.

II. The *Ellipsis*, or regular Oval, described on two Centers, as  $a$  and  $b$  in the Seventeenth Figure.

III. *Plain straight-lined Figures*, as of three Sides and three Angles, called *Triangles*, whereof there are six sorts, three in respect of the Sides, and three of the Angles: As, First, an *Equilateral Triangle*, that has three equal Sides, and three equal Angles, each of 60 Degrees, as in the Eighteenth Figure. Secondly, an *Isosceles Triangle*, that hath two equal Sides and one unequal; as in the Nineteenth Figure,  $bc$  is equal to  $ca$ , and  $b$   $a$  left. Thirdly, all the Sides unequal, called a *Scalenum*, as in the Twentieth Figure. Fourthly, in respect of the Angles, as a *Rectangled Triangle*, that has one Right Angle, as Figure 21, where  $a$  is the Right Angle, then must the other two Angles at  $b$  and  $c$  be both a Right Angle, for by the latter Part of the Fourth Proposition, all the Angles of any Plain Right Triangle are equal to  $180^\circ$ , or two Right Angles, therefore  $b$  and  $c$  must be  $90^\circ$ , and from hence the Remainder of the Degrees of any Angle to  $90$  is called the Complement of that Angle, as if  $b$  be  $50^\circ$ ,  $c$  will be  $40^\circ$ , so that  $c$  is the Complement of  $b$  to  $90^\circ$ . This Note must be remembered, because of great use. Fifthly, all the Angles may be Acute, as in Figure 22, called *Oxigonium*, where the third Angle is the Complement of the other two to  $180^\circ$ . Sixthly and Lastly, it may be an Obtuse-angled Figure, having one Obtuse Angle, and the rest Acute, called an *Amblygonium*.

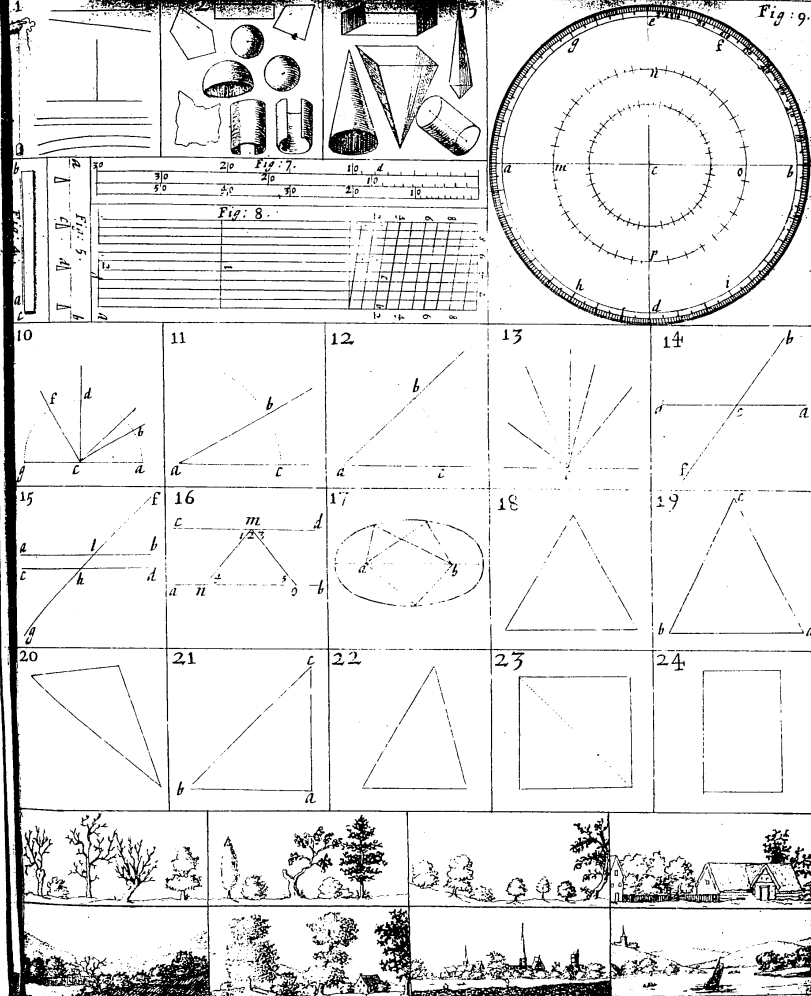
IV. *Right-lined Figures*, or *Superficies*, of four Sides, being *Quadrilateral*, are of five sorts, viz. a *Square*, that has four equal Sides, and four Right Angles, as in Figure 23. Or an *Oblong*, Rectangle, or Long Square, that has four Right Angles, and four Sides, whose opposite Sides are equal, as in Figure 24. Or a *Rhombus*, that has all the Sides equal, but the Angles not Right Angles, as in Figure 25. Or a *Rhomboides*, that hath the opposite Sides and Angles equal, but not Equilateral or Right-angled, as in Figure 26: The Oblong and this are called *Parallelograms*, because two Sides are equal to two Sides, and parallel. Or lastly, all other four-sided Figures are called *Trapezes*; and all *Quadrilateral Figures* may be divided into two *Triangles*, by drawing a Line from one Angle to the opposite Angle, which is called the *Diagonal*.

V. Other Plain straight-lined Figures, of more Sides than four, are called *Multilateral*, and takes the Name from the Number of their Sides or Angles, which if they be equal are called *Regular Polygons*; as of five equal Angles, the *Pentagon*; of six, the *Hexagon*; of seven, the *Heptagon*; of eight, *Oxagon*; &c. Now every Multilateral Figure is divided into *Triangles*, by drawing Lines from corner to corner, and it will have as many *Triangles* as there be Sides less two, as in Figure 27, of an Irregular seven-sided Figure there will be five *Triangles*.

VI. The Line whereon a Triangle, Square, Oblong, &c. stands on, is called the *Base*.

VII. The *Height* of any Triangle or Figure, is the Line drawn perpendicular from the Top to the *Base*, as in the Examples following will appear.

Prop.





Prop. VI. *Here follow the Resolutions of certain Geometrical Problems, fitting to be done for several Uses, and for the Exercising the Hand for the Managing of the Ruler and Compasses.*

I. **T**O raise *Perpendiculars*, either upon Paper or the Ground: As upon the Middle of a Line, Figure 28, at *a*: Take the Compasses, and open them, and set equal Distances from *a* to *b*, and to *c*, then open the Points to a Distance of above *ab* or *ac*, and setting one Foot in *b* make an Arch about *d*, and with that opening, setting a Foot in *c*, cross the former Arch at *d*; then draw *da*, which is a Perpendicular. *To rise a Perpendicular.* Fig. 28.

Upon the End of a Line, or near the End, as in Figure 29, by once opening of the Compasses. On the Point *a*, as a Center, describe part of a Circle, *bcd*, with that opening set off the Radius from *b* to *c*, and from *c* to *d*, upon which Points *c* and *d* cross an Arch at *m*; *ma* is a Perpendicular. Fig. 29.

Another way, where you may not come so far as *d*, as in Figure 30. Describe the Arch *bc*, and set the Compasses unfitted from *b* to *c*, and setting one Foot in *c* make an Arch at *d*, lay a Ruler by *b* and *c* and cross the Arch at *d*; *da* is a Perpendicular. Fig. 30.

Another way, setting the Compasses in *a*, as in Figure 31. Set the other about *c*, and draw the Circle *bcd*, and the Diameter *bcd*; then is *da* a Perpendicular. Fig. 31.

II. To let fall a *Perpendicular* from a Point above a Line, as at *a*, in Figure 32. Open the Compasses, setting one Foot in *a*, with an Arch cross the Line in *b* and *c*; again with that opening upon *b* and upon *c* cross an Arch at *d*; then is *aod* a Perpendicular. *To let fall a Perpendicular.* Fig. 32.

Another way, towards the End of a Line, as at *a* in Figure 33. From *a* draw a Diameter *ab*, which divide in halves at *c*, with the Radius *ca* or *cb* draw the Semicircle *adb*, cutting the Line at *d*; then is *ad* a Perpendicular. Fig. 33.

III. To divide a Line into two, or into many Parts. First, into two Parts; suppose the Line *bc*, in Figure 28. Open the Compasses to above half, and make the cross Arches at *d* and *a*; the Line *da* divides *bc* into halves at *a*. *Division of Lines.* Fig. 28.

Secondly, to divide a Line into five or more Parts: Raise two Perpendiculars on the Ends of the Line at *a* and *b* contrariwise, as in Figure 34, and set off five Parts on those Perpendiculars, as in the Figure, draw the Diagonal Lines, which will divide *ab* into five equal Parts. Fig. 34.

Likewise, by making an Oblong, and dividing of it, as in Figure 35, you may divide all Lines, that will not exceed it, into what Parts you please; which may be done with white Lines that will not deface the Draught, as *ab* to be divided into thirteen Parts, as in the Example. Fig. 35.



Angles.

Fig. 36.

Parallel Lines.  
Fig. 37.

Fig. 38.

Triangles,  
Squares, &c.  
described.  
Fig. 39.

Fig. 40.

Fig. 41.

Fig. 42.

IV. To make Angles equal to one another, and to measure and lay them down, was shewn before plainly. The ordinary way, by describing an Angle equal to another by a little Arch, may be easily understood by Figure 36; for upon the Point  $a$  of the Angle  $c a b$  you make the Arch  $b c$ , Figure 36; for upon the Point  $d$  make an Arch  $e f$ , and not stirring the Compasses upon the Point  $d$  make an Arch  $e f$ , and taking the opening or distance  $b c$ , set the same from  $f$  to  $e$ , and draw  $e f$ ; then is the Angle  $f d e$  equal to the Angle  $c a b$ , having the same Number of Degrees.

V. Of drawing *Parallel Lines* in the same Plain, which can never meet: For Example, To draw a Parallel to  $ab$ , at the Distance  $c d$ ; take  $c d$  in the Compasses, and towards the End of the Line  $ab$ , as at  $m$  and  $n$ , make two Arches, as at  $o$  and  $p$ , and by the top of those Arches draw the Parallel Line  $o p$ .

But if the Line  $ab$  in Figure 38, and the Point  $d$  be set down, whereby to draw a Parallel Line to it, set the Point of the Compasses in  $d$ , and take with the other Point the nearest Distance to  $ab$ , as at  $m$ , and with that opening towards the other end, as at  $n$ , make another Arch at  $p$ , and draw  $d p$  for a Parallel.

VI. To make an Equilateral Triangle upon a Line given, is done, by taking the Line in the Compasses, and from both Ends describe an Arch, as at  $d$ , Figure 39, and draw the Triangle accordingly.

To make a Triangle upon any three Lines given, so that any two may be longer than the third: Lay down any Line of the three, and on the Ends thereof, with those other Lines, make an Arch, as at  $d$ , in Figure 40, and describe the Triangle.

To make a true Square upon any Line given, as upon  $ab$ , in Figure 41: Upon one End, as at  $a$ , raise a Perpendicular, as  $ac$ , take the Length of  $ab$  in the Compasses, and set it from  $a$  to  $b$ , and with that opening, upon the Points  $c$  and  $b$ , cross an Arch at  $d$ ; then draw  $c d d b$  for a true Square.

To describe a Circle, that shall pass by the three Points  $b c d$  of the Triangle  $b c d$ . (Or to draw those three Points into a Circle, which is all one) is to cut any two Sides, as  $c d$  and  $b d$ , into two equal Parts, by the Third Problem of this Proposition of a Line, and draw the Lines 'till they meet, as at  $o$ , that will be the Center, that the Compasses must be pitched in, to describe the Circle, that will pass by those three Points.

Prop. VII. Of *Solid Bodies*, which have three Dimensions, Length, Breadth, and Thickness, and the Extreams are Surfaces. The *Regular Bodies* are,

Solid Bodies.  
Sphere.

I. The *Sphere*, which is comprised of one round Superficies, from whence all Lines drawn to the Center are equal, and may be made by

by a Semicircle turn'd about. These may be round Balls, Globes, &c. Any Diameter may be called the Axis, as  $ab$ . See Figure 43.

II. A *Spheroid*, or long Sphere, is made by the turning the half of an Ellipsis upon his longer Diameter. See Figure 44. The Ends cut off, it makes a Hoghead. Fig. 43.

III. A *Cylinder*, is a Column, or round Pillar, whose Base is a Circle, and is described by a Parallelogram moving upon one of its Sides, as  $a b$ . See Figure 45. cylinder. Fig. 45.

IV. A *Cone*, is a Pyramidal Body that has a Circular Base, and is described by a Right-angled Triangle, as Figure 46. Cone. Fig. 46.

V. A *Cube*, is a Body comprised of six Squares, as a Dice. See Figure 47. Cube. Fig. 47.

VI. A *Parallelepipedon*, is a long Body comprehended of six Plain Quadrangles, and has all its Sides opposite and parallel, and equal one to another, as Figure 48. Parallelepipedon. Fig. 48.

VII. A *Prism*, is a Solid Body comprehended of many Superficies, two whereof are opposites, equal, parallel, and like, but the rest are Parallelograms. Figure 49. A Prism. Fig. 49.

VIII. A *Pyramid*, is a Body comprised of many Planes, meeting in one Point at the Top, and having a Plane for its Base. Figure 50. Pyramid. Fig. 50.

There are other Regular Bodies, the Number of Five, called *Plato's Bodies*, which may be inscribed in a Sphere, and touch the Superficies, viz. Fig. 51.

(1.) The *Cube*, of 6 Sides, before described. (2.) The *Tetrahedron*, of 4 Sides. (3.) *Octohedron*, of 8 Sides. (4.) *Dodecahedron*, of 12 Sides. And (5.) The *Icosahedron*, of 20 Sides. As the Figures represent, where I have added the Forms of each, which being half cut through with a Penknife will fold up, and make the said five Regular Bodies.

Thus far I have gone in Definitions, and some Practical Rules, for the Use of the Scale and Compass; I now come to the necessary Part of Measuring of Lines, Superficies, and Solids.

### Prop. VIII. The Measure of Lines.

OF Measuring Lines, and of the Common Measures, as Inches, Feet, Yards, Ells, Poles or Perches, Furlongs, and Miles, something has been laid already; and now I would have the Boys fully instructed, by Measuring with a Yard or Foot in any Gallery or Room, or elsewhere, what the meaning of a Scale, or of laying down any Measure upon Paper doth signify. As by the Scales before set down, Figure 7, suppose I measure in some High-way 324 Yards, to lay this down upon Paper, I go, for Example, to my Plain Scale of Ten Parts in an Inch, and set my Compasses in 3 whole Inches (marked 30) and extend the other Point into the small Divisions of an Inch, betwixt  $c$  and  $b$ , being 10, to above 2 of them for 20, and almost by Estimation to half the Distance betwixt 2 and 3 of that Scale for 4 at  $d$ . This being laid down, as in Figure 52, represents the Length of 324 Yards. But if this Scale be found too big, then you may chuse a lesser, of 12, 16, 20, &c. Parts in an Inch, set down in Figure 7 as before, and

Fig. 52.



and this will (by a little Practice) be easily attained, how to measure by any Plain Scale whatsoever.

Yet by these Scales I could not find the 4 part of my Number 324, but by guessing at the fourth part as near as I could; but by the *Decimal Diagonal Scales* you may find that Length exactly. The Scale is described Figure 8, and for the better understanding of these kind of Scales, I have in figure 53 taken the Tenth part of an Inch, and drawn a Diagonal to divide it actually into Ten parts, and yet by guess you may very near imagin the Spaces to be again divided into other Ten parts, that is, an Inch into 1000 Parts; for Example, if the former Distance 324 were propoed to be taken from that Diagonal Scale N<sup>o</sup> 8, I go down to 3 on the Scale for 300 at *a*, then upon that Part divided into 10 I seek for 2 on the Scale for 300 at *a*, and extending the Compasses from that Parallel in the Line of 300 at *d* to *c*, that Distance will be equal to 324 Yards, Ells, Feet, or Miles.

If you measure with a Chain or Rod of 10 Foot, or any other Measure, you must be careful to measure in a Right Line, and not to go in or out, which you may do by help of Lines, or small Pins or Pickets, set in the way.

And because several Lines require several Measures, you must know, that in measuring,

1. Timber, Stone, Earth-work, Gardens, Alleys, Board, Glass, and the like, are measured by the Foot.
2. Land, Woods, Brick-work, &c. are measured by the Perch or Pole.
3. Pavings, Plasterings, Wainscottings, are measured by the Yard: And so all Linnen and Woollen Cloth, Stuffs, Silks, &c. by the Yard or Ell.
4. Tapiftry is measured by the Stick of  $\frac{1}{2}$  of a Yard.
5. Carpenters Work, as Flooring, Partitioning, Roofing; and so Tiling, Slating, and sometimes the Ground-Plot of Houfes and whole Buildings, are measured by a Rod of 10 Foot long, and that every way is called a Square, being 100 square Feet.

### Prop. IX. Measuring of Superficies.

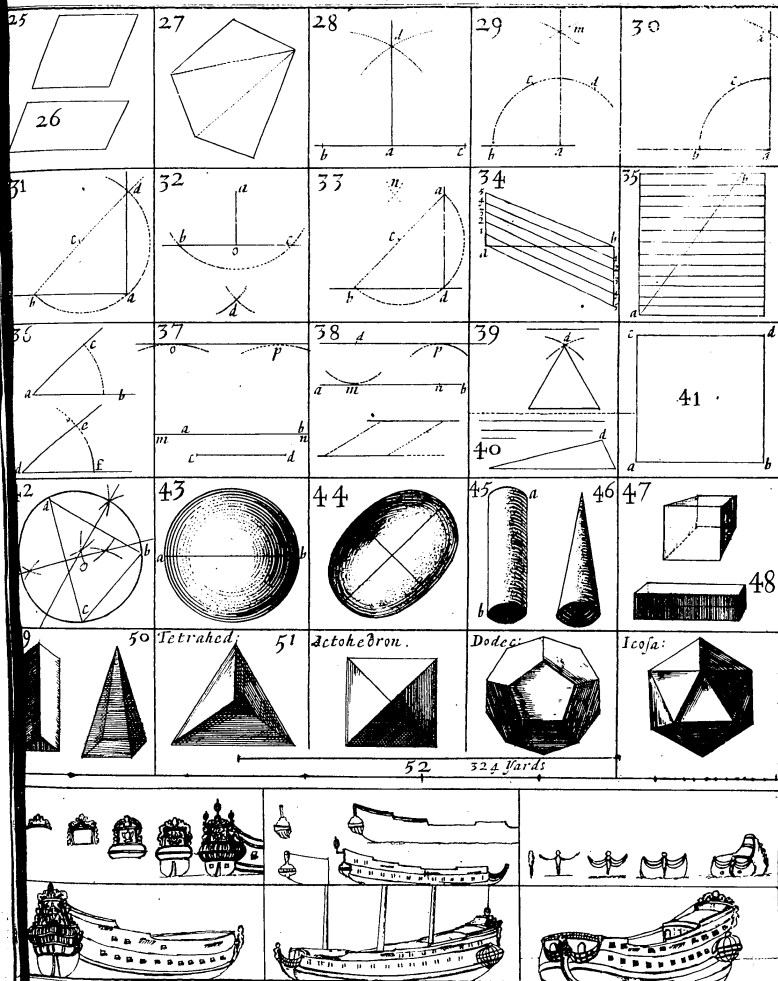
Measuring of Superficies.

TO Measure a Superficies which has two Dimensions, as I said before, is quite otherwife than to measure Lines or Lengths; for as we say, in such a Length there is such a Number of Inches, Feet, Yards, Poles, Miles, &c. so in a Superficies it is said, there is such a Number of Square Inches, Square Feet, Square Yards, Square Perches and Miles; which Squares are the most simple and natural, and so commonly known, and are of two Dimensions, for there being in a Foot 12 Inches, a square Foot is 12 times 12, or 144 square Inches, and there being 3 Foot in a Yard, there are 3 times 3, viz. 9 square Feet in a Yard, and so of the rest; which being the only observable Note of this nature, I shall proceed to give the several Rules for Superficies, and then proceed to Solids.

To measure a Square, as suppose the Side be 13 Feet; Multiply the Side by it self, that is, 13 by 13, and it produces 169 square Feet, as in Figure

Square.  
Fig. 55.

55.





55 But if you should yet desire to know a nearer Measure, as in Inches, then the 13 Feet would be 156 Inches, and that would be in square Inches 24336, which divided by 144, the square Inches in a Foot, gives 169 square Feet; and if any thing remained, it would be square Inches, where 98 would be  $\frac{1}{4}$ , 72 one  $\frac{1}{2}$ , and 36 one  $\frac{3}{4}$ , of a Foot.

To measure an Oblong, or Long Square, is to multiply the Length by *Oblong.* the Breadth, suppose that in Figure 56, one Side to be 171 Feet, and the *Fig. 56.* other 56, 171 times 56 will be 9576 square Feet; and if it be desired to know what square Yards there were, divide 9576 by 9, the square Feet in a Yard, and it makes 1064 Yards.

The Area of a Rhombus, or Rhomboides, is got by multiplying the Perpendicular P, let fall on one of the Sides, by that Side or Base *Rhombus and Rhomboides.* *Fig. 57.* b, as in Figure 57. The Perpendicular is found 82 Yards, and the Side 254 Yards, which multiplied makes 20728 square Yards. But if it be desired to give the Measure in Perches and Acres, because by the Table of *Square Measure*, 30  $\frac{1}{4}$  Yards go to make a Pole or Perch, (which is  $\frac{1}{4}$  multiplied by  $\frac{1}{4}$  Yards) divide 20728 by 30.25 Yards, and it gives 685 Perches, 6 Feet, and  $\frac{1}{4}$  of a Foot; and divide 685 by 160 Perches (for so many are in an Acre) and it gives 4 Acres and 45 Perches, which makes 1 Rood and 5 Perches, which is 4 Acres, 1 Rood, 5 Perches, 6 and  $\frac{1}{4}$  Feet, square.

All other Multangled Figures may be reduced into Triangles, as was before declared.

The Area of any Plain Triangle is gotten, by multiplying the Perpendicular (let fall on the Base) by the Base, and taking half thereof, or by multiplying *Triangle.* the Base by half the Perpendicular; or lastly, the Perpendicular by half the Base; for all are the same in the Product. So in Figure 58, the Triangle is *abc*, the Base *ab* measured to be 264 Perches, and the Perpendicular *cd* 32 Perches, which multiplied make 8448 square Perches, the half whereof is 4224 Perches, and dividing that Sum by 160 (the square Perches in an Acre) it gives 26 Acres, 1 Rood, and 24 Perches. *Fig. 58.*

Note, If you had made any other Side for Base, you should have found the same thing, but then you must have prolonged the Base *ac* towards *f*, and *cb* towards *g*, before you could have found the Length of the Perpendiculars *bf* and *ag*; all which will be plain, when you understand the Demonstration thereof in the Last Part.

To measure the Area of a Close or Field, that hath one Side going in and out, as in Figure 59: First, in stead of the crooked Side *cd*, which may *Area.* be some old River, I draw a straight Line *cd*, which as near as I may judge *Fig. 59.* may take in as much as it leaves out, then I divide this Five-sided Irregular Plot into 3 Triangles, and let fall Perpendiculars from *b* upon the Base *ac*, and from *a* and *d*, upon the Common Base *cc*; then I multiply *ac* by the half of *bf*, and *cc* by the half of *ag* and *bd* added together; those two Products gives the Area in Perches, which divided by 160 gives Acres.

The Area of a Circle, or of any Regular Polygon, is gotten by multiplying half the Circumference by the Radius, or the Perpendicular falling *Circles and Polygons.* from the Center upon any of the Sides. But because there are certain Proportions.



portions, found out by *Archimedes* and others, betwixt the Diameter and Circumference of a Circle, I will let them down, and explain them.

As 7, to 22; so is the Diameter of a Circle, to the Circumference: Therefore, multiply the Diameter given in Length by 22, and divide the Product by 7, the Quotient gives the Circumference. In stead of 7 to 22, if you will go nearer and more exact, you may take *Motius* his Proportion, As 113 to 355; or yet nearer, As 1 to 3.1415926. But for ordinary use, 7 to 22 will be enough.

As 22, to 7; so is the Circumference of a Circle, to the Diameter. Multiply therefore the Circumference by 7, and divide the Product by 22, the Quotient gives the Diameter. So 355 to 113; or, As 3.1415926 to 1, will do the same more exactly.

As 14 to 11; or, As 1 to .785399; so is the Diameter squared, to the Area of a Circle. Contrary, As 11, to 14; so is the Area of a Circle, to the Diameter squared.

As 88 to 7; or, As 1, to .079577; so is the Square of the Periphery, to the Area of the Circle.

As 1, to .707107; so is the Diameter, to the Root of a Square to be inscribed in a Circle.

As 1, to .886227; so is the Diameter, to the Root of a Square equal to the Circles Area, which is the squaring of a Circle.

And note, That in all these, and the like Rules, where the *Golden Rule* is proposed, by Three Terms to find the Fourth, it is meant, that the Second and Third Terms be multiplied together to make a Dividend, which divided by the First Term gives the Demand.

Thus much for the Area's of Whole and Perfect Circles, now I will shew you, how you may get the Area's of Parts of a Circle, whether it be a Sector or a Segment. A Sector is contained betwixt two Radii, or Semidiameters, and the Arch; a Segment, betwixt the Chord and the Arch. Example in Figure 60; *anbc* is a Sector of a Circle, less than a Semicircle, *abbc* is a Sector greater: So is *abn* a lesser Segment, and *abba* a greater Segment than a Semicircle.

To measure a Sector, as *anbc*, multiply the Radius, or Semidiameter, *ac*, by half the Arch *ab* for the Area; and so of the other Sector in the greater.

To measure a Segment is more troublesome, for first you must find the Diameter, thus: Divide the Chord *ab* into Halves in *p*, draw a Perpendicular at *p* to *ab*, that shall pass by the Center: Then say, As *np*, to *pb*; so is *pb*, to *pl*: That is, Square the half Chord, and divide it by the *Sagitta np*, it gives a Number, which added to *up* gives the Diameter, the half is Radius. Then find the Area of the Sector *acbn*, and of the Triangle *abc*, which take from the Sector, and it leaves the Area of the Segment *abn*. The like Work will find the greater Segment, for the half Chord is a Mean Proportional betwixt the Segments of the Diameter.

The Area of a Sphere or Globe, or any other round Ball, is had, by multiplying the Diameter by the Circumference of the great Circle; or, by

Fig. 60.

Sector.

Segment.

Area of the Sphere.

by multiplying the Square of the Diameter by 22, and dividing by 7. For, As 7, to 22; so the Square of the Diameter, to the Area.

And, As 7, to 22; so is the Diameter multiplied by the Axis of a Cylinder, to the Superficies of the Cylinder.

And, As 7, to 22; so is the Radius or Semidiameter into the Side of a Cone, to the Superficies.

Again, As 1, to .564189; so is the Circumference, to the Square Root of a Number equal to the Superficies of a Sphere.

To find the Area of an Ellipsis, multiply the longer Diameter by the shorter, and take the Square Root of that Product, which shall be the Diameter of a Circle equal to that Ellipsis. The Area of that Circle is taught before; for, As 14, to 11; so is the Square of the Diameter, to the Area.

I will here, to finish this Part of Measuring Superficies, add a few Tables, very little, but exceedingly useful, when occasion requires, for turning lower Denominations into higher; as for Example, to save Division of many Perches by 160 to turn them into Acres, Roods, and Perches, you may enter the following Table with your Perches, and take out the Acres, Roods, and Perches, answering to Thousands under M, to Hundreds under C, and Tens under X.

	M.			C.			X.	
	Ac.	R.	Per.	Ac.	R.	Per.	R.	Per.
1	06	1	00	00	2	20	0	10
2	12	2	00	01	1	00	0	20
3	18	3	00	01	3	20	0	30
4	25	0	00	02	2	00	1	00
5	31	1	00	03	0	20	1	10
6	37	2	00	03	3	00	1	20
7	43	3	00	04	1	20	1	30
8	50	0	00	05	0	00	2	00
9	56	1	00	05	2	20	2	10

Example.

Having cast up my Field, I find by computing my Triangles, that I have 7854 Perches, which I set down severally, as follows, and take out of the Table the Parts answering, which make in all 49 Acres, and 14 Perches.

Perch.	Ac.	R.	Per.
7000	=	43	3 00
800	=	05	0 00
50	=	00	1 10
4	=	00	0 04
7854	=	49	0 14

Some.



Sometimes, as in Gardens, Courts, Yards, and other small Places, the Superficies is given in square Feet, which you may turn into Acres, Roods, and Perches, by the adjoining Table, entering it with the Feet, as you did the last with Perches, and adding them together.

	C.M.			X.M.			M.		C.	
	Ac.	R.	Per.	Feet.	Ac.	R.	Per.	Feet.	Per.	Feet.
1	02	1	07	036	00	0	36	119	03	183
2	04	2	14	171	00	1	33	126	07	094
3	06	3	21	257	00	2	30	053	11	005
4	09	0	29	065	00	3	26	252	14	189
5	11	1	36	150	01	0	23	179	18	099
6	13	3	03	240	01	1	20	106	22	011
7	16	0	11	053	01	2	17	033	25	194
8	18	1	18	140	01	3	13	232	29	106
9	20	2	25	215	02	0	10	159	33	017
									03	084

Example.

Suppose 97642 square Feet be to be turned into Acres, Roods, Perches, and Feet, you will find by the Table, that they make 2 Acres, 38 Perches, and 179 Feet; which must be thus set down.

Feet.	Ac.	R.	P.	Feet.
90000	= 2	0	10	159
7000	= 0	0	25	194
600	= 0	0	02	56
42	= 0	0	00	42
97642	= 2	0	38	179

The next Table gives the square Perches, Quarters, and Feet, upon the Face of any Brick Wall measured by a Foot Measure, suppose a Rod of Ten Foot, or otherwise; as for Example: A Wall 68 Foot long and 26 Foot high makes 1768 square Feet, which by the Table gives 6 Perches, 1 Quarter, and 58 Feet. And note, That 272  $\frac{1}{2}$  square Feet make a Perch, 20  $\frac{1}{4}$  three Quarters, 136  $\frac{1}{2}$  half a Perch, and 68 a Quarter. This Measure is for Brick and half, which is 14 Inches, but if the Wall be thicker, account by half Brick, and say, *As* 3, *to* any other Wall in half Bricks; *so* are the Perches and Parts found by Measure, *to* the Perches of that other Wall given in half Bricks.

X M.

	X M.			M.			C.			X.	
	Per.	Q.	F.	P.	Q.	F.	P.	Q.	F.	Q.	F.
1	036	2	63	03	2	41	00	1	31	0	10
2	073	1	58	07	1	26	00	2	62	0	20
3	110	0	53	11	0	05	01	0	26	0	30
4	146	3	55	14	2	52	01	1	57	0	40
5	183	2	40	18	1	31	01	3	20	0	50
6	220	1	35	22	0	10	02	0	54	0	00
7	257	0	43	25	2	57	02	2	17	1	02
8	293	3	41	29	1	36	02	3	47	1	12
9	330	2	25	33	0	15	03	1	14	1	22

The following Table is for Measuring Board, Glaſs, &c. by Inches, which will turn square Inches into Feet, Quarters, and Inches; as 984 square Inches make 68 Feet, 1 Quarter, and 14 Inches.

	M.			C.			X.	
	F.	Q.	In.	F.	Q.	In.	Q.	In.
1	06	3	28	00	2	28	0	10
2	13	3	20	01	1	20	0	20
3	20	3	12	02	0	12	0	30
4	27	3	04	02	3	04	1	04
5	34	2	32	03	1	32	1	14
6	41	2	24	04	0	24	1	24
7	48	2	16	04	3	16	1	34
8	55	2	08	05	2	08	2	08
9	62	2	00	06	1	00	2	18

Thus much for the Plain Measure of Area's and Superficies, which if you understand, will be very useful to you; for Example, I demand how many square Miles are upon the Face of the Terraqueous Globe, or whole Earth and Sea? The greatest Circle being 360°, and supposing 60 *Italian* Miles in a Degree, the Circumference will be 21600 Miles, and the Diameter 6873 Miles in a round Number, omitting Fractions; and being shewed in this Proposition, that the Area of a Sphere is found by multiplying the Diameter by the Circumference, multiply the Diameter 6873 by the Circumference 21600, and it gives the Product 148456800 square Miles, the Area required. Now a Mile square being 640 Acres, (for 320 Perches make a Mile, and 320 by 320 gives 102400 square Perches, which divided

I 2 by



by 160 gives 640 Acres) and allowing 20 Acres for a Family of 6 People, a Mile square will maintain 320; then deducting half of the square Miles of the whole Globe for Sea, there remains 74228400 square Miles of Land, which multiplied by 320 gives 23753088000 People, that possibly may live upon the whole Earth; but this Number is far greater than the People living at once, for by Ricciolus his Account in his *Geography*, they exceed not 1000000000.

### Prop. X. Measuring of Solids.

Measuring of Solids.

**V**VE are come now to three Dimensions for the Measuring of Solids; and as Superficies are measured by Squares of the same kind, so Solids are measured by Cubes, as Cubick Inches, Cubick Feet, Cubick Yards, Perches, and Miles, a Cubick Inch being commonly the least Measure. If the Side of a Cubick Foot be 12 Inches, to find how many Inches there are in the whole, I multiply 12 by 12, and it gives the square Inches upon the Face of the Cubick Foot to be 144, and then multiplying 144 by 12 for the third Dimension, it gives 1728 Cubick Inches in the solid Foot: This will appear perfectly in the Cubick Foot Figure 61. Therefore the measuring of a Cube, is to multiply the Side by it self, and the Product by the Side again. And as in the Plain Parallelogram, you may imagin the motion of one Side parallel to the other, to describe all those several Squares that make up that Superficies; so in the Cube, or Parallelepipedon, if you imagin the Superficies ABCD to move through the Solid, it will give you the several Cubes in that Body by that Dimension.

Fig. 61, 62.  
Cube.

Parallelepipedon.  
Gen.  
Fig. 63.

The Measure of a right Parallelepipedon, improperly called a long Cube, is to multiply one Side by another, producing the Square at the End, and then that Product by the Length (all those Lines measured making one solid Angle) which produceth the Cubick Feet: As in Figure 47, where the Breadth at the Ends are 1 Foot 4 Inches, and 10 Inches, that is, 16 and 120 Inches, which multiplied make 160 square Inches for the End, and that multiplied by the Length 5 Feet 7 Inches, that is, 67 Inches, makes 10720 solid Inches, which divided by 1728, the Cubick Inches in a solid Foot as before said, it gives 6 Feet solid, and 352 Cubick Inches, which is less than the  $\frac{1}{4}$  of a solid Foot, for there being 1728 in a Foot, 1296 solid Inches make  $\frac{1}{4}$  of a Foot, 864 the  $\frac{1}{2}$ , and 432 the  $\frac{3}{4}$ .

But to avoid these Parts by Inches, it is best to measure with a Foot divided into Ten Parts, and those Parts subdivided into Ten again; for then if you measure either Plains or Solids, the Work will give you Feet, and Decimal Parts of a Foot of the same kind, without any Reduction at all; and in case you have no such Foot by you, then by the Sixth Decimal Table in the *Arithmetick* you may put the Inches and Parts into Decimals, as if it were subdivided; as in the last Example, for 1 Foot 4 Inches I set down 1.333, for 4 Inches by the said Sixth Table gives .333, and for 10 Inches I find there .833, and for 5 Feet 7 Inches I find 5.583; now multiplying 1.333 by .833 it gives Decimally 1.11059, and that by 5.583 gives

gives 6.198, which is 6 Feet and almost  $\frac{2}{5}$  of a Foot, which is less than a Quarter.

If you are not minded to work by Decimals, but by solid Inches, then this little Table following will immediately turn the solid Inches into solid Feet, Quarters of a Foot, and solid Inches, by Inspection.

	X M.			M.			C.	
	F.	Q.	In.	F.	Q.	In.	Q.	In.
1	05	3	064	00	2	136	0	100
2	11	2	128	01	0	272	0	200
3	17	1	192	01	2	408	0	300
4	23	0	256	02	1	112	0	400
5	28	3	320	02	3	248	1	068
6	34	2	384	03	1	384	1	168
7	40	3	016	04	0	088	1	268
8	46	1	080	04	2	224	1	368
9	52	0	144	05	0	360	2	036

Suppose 11572 solid Inches be to be turned into Feet, entering the Table as directed in the last Proposition, you will find they make  $6\frac{1}{2}$  solid Feet, and 340 solid Inches; which are less than  $\frac{1}{4}$  of a Foot, as in this Example.

Inch.	F.	Q.	In.
10000	5	3	064
1000	0	2	136
500	0	1	068
72	0	0	072
11572	6	2	340

But if the Parallelepipedon be not right, that one Side be not perpendicular over the other, then must you find the Perpendicular or nearest Distance to the Base, and multiply as before. All Walls, the Dimensions of Rooms, Galleries, &c. are thus measured.

The Measure of Prisms, or the solid Body described before by that Name, is gotten by multiplying the Superficies of the Base into the Height of the Prism; that Superficies of the Base, being to be made of all Plain Figures, is to be gotten as in measuring Superficies; and that Height is to be measured by the nearest Distance of any Part of the Base, continued if need be to the parallel Top.

For Example, Figure 63, let the Base of the Prism be *abcdef* of six Sides, divide the Superficies thereof (measuring it as in Plains) into 4 Triangles, and 2 Diagonals, by the Decimal Foot, which comes to  $7\frac{1}{2}$  Feet, that

Measure of a Prism.

Fig. 63.



that is, 7.5, and let the Height  $bf$  be 3 and .7 Tenths of a Foot, which multiplied by 7.5 makes 27 solid Feet, .75 Hundred Parts, which is just  $\frac{3}{4}$  of a solid Foot.

Measure of a Pyramid.

Fig. 64.

Regular Solids.

To measure the Solidity of a Pyramid, is to multiply the Base (which like that of a Prism may be of many sorts of Superficies) into one third part of the Height, which is taken by letting fall a Perpendicular from the Top of the Pyramid to the Base, produced if need be; for a Pyramid and Prism, upon equal Bases and Heights, are as 1 to 3. See the Figures 64.

To find the Solidity of the Five Regular Bodies before described: 1. For the *Tetrahedron*, that is, a Pyramid, and last measured. 2. The *Hexahedron*, is the Cube before measured. 3. The *Octahedron*, thus measured, Multiply the Square of one of the Sides into  $\frac{2}{3}$  of the Distance of any two Corners, and the Product is the Solidity; for it is but two Pyramids upon a square Base. 4. The *Dodecahedron* is only 12 Pyramids, whose Base is a Pentagon, and Top the Center, therefore multiply the Base into  $\frac{2}{3}$  of the Height to the Center 12 times, which is the Solidity of the whole; And to find that Height, take the Distance of two parallel Faces, the half is the Height. 5. The Solidity of the *Icosahedron* consists in 20 several Pyramids, whose Bases are Triangles, that is, its Faces, the Height is the half Distance of two equidistant Faces; multiply the Triangle, which is the Base, by  $\frac{2}{3}$  of the Height, and that taken 20 times makes the Solidity.

Irregular Solid Bodies of Plain Faces.

Now even as these last Regular Bodies are measured by the Number of Pyramids contained in them, even so all Irregular Plain Solids may be divided into so many Prisms and Pyramids, as Plain Figures into Triangles, and then measured as before.

To measure Cylinders, or Columns.

Fig. 65, 66.

Trunks of Cylinders.

Fig. 67.

Cone.

Fig. 68.

Trunk of a Cone.

Fig. 69.

Sphere.

Multiply the Base (that is, the Area of a Circle, taught before) by the Height of an upright Cylinder, or by the Perpendicular of a sloping one, and the Product gives the solid Content, as in the Figures 65 and 66.

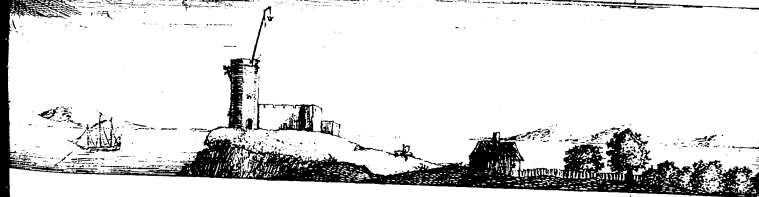
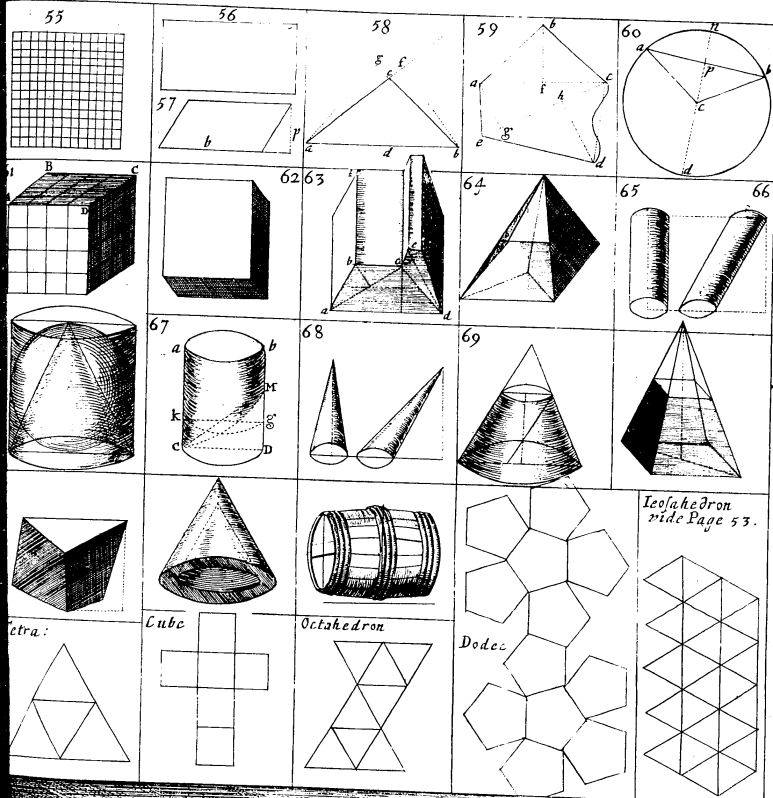
These are round Columns, Trees (commonly measured in the middle) and all other such Figures measured. But if it be a Trunk of a right Cylinder, obliquely cut off, as in Figure 67; to deal with this Trunk, draw by the Point C a parallel Circle to the top, and divide MD into halves, then measure  $abkg$  as a Cylinder by itself.

The Solidity of a Cone is gotten, if you multiply the Base by one third of the Height, the Height is found as you may see by Figure 68.

To measure the Trunk of a Cone, or a Cone cut off, as in Figure 69, first take the Diameters at both Ends of the Trunk, and the Height, then say, As the Difference of Diameters, to the lesser Diameter; so is the Height of the Trunk, to another Number, which is the Height of a Cone that will supply the Trunk; to have you two Cones; and if you take the lesser out of the greater, it leaves the Solid of the Trunk required.

The Solidity of the Sphere is found, by multiplying its Superficies (taught before) into one third part of the Radius or Semidiameter, or one sixth of its Diameter. I will give you some few Proportions, that concern the Solidity of Spheres, Cylinders, Cones, &c. as follows.

As 14, to 11; or, As 1, to .785399; so is the Square of the Diameter multiplied





multiplied by the Side of the Cylinder, *to* the Solidity of the Cylinder: And, *so* is the Diameter squared, multiplied by one third of the Axis, *to* the Solidity of the Cone.

*As* 1, *to* .523599; *so* is the Cube of the Diameter, *to* the Solidity of the Sphere.

*As* 1, *to* .016887; *so* is the Periphery cubed, *to* the Solidity of the Sphere.

*As* 42, *to* 22; or, *As* 1, *to* .5236, *so* is the Diameter cubed, *to* the Solidity of the Sphere.

A *Cone*, a *Sphere*, and a *Cylinder*, that have the same Heights, and Diameters of the greatest Circles equal, are as 1, 2, 3.

#### Measuring of Ships.

For the Measuring of Ships, it will be found a very difficult matter to do it truly, the Body within being so irregular, however it will be requisite to fer down the way that Ship-Masters and Carpenters generally use for the Measuring the Tunnage of a Ship, *viz.* They multiply the Length of the Keel, the Breadth of the Midship-Beam, and the Depth of the Hold, one into another, and divide the Product of those three Numbers by 100, the Quotient gives you the Tuns of that Ship: And this is the Measure His Majesty gives for Merchant-Men for the Wars. But where there is no Allowance for Guns, &c. divide by 95, and the Quotient gives the Tunnage; Example, A Ship is 60 Foot by the Keel, the Breadth is 20 Foot, and 11 Foot deep in the Hold; I multiply 60 Feet by 20, and it gives 1200, which multiplied by 11 gives 13200 solid Feet, I divide that by 100, and it gives 132 Tuns for the Measure of that Ship; but if divided by 95, it will give 138 Tun, and almost an half, for Merchant-Men.

#### Gauging of Vessels.

The Gauging of Vessels (or all manner of Cask) may be required from you, therefore you must know, that the *Gallon* (which is the Common Measure for this Work) is of several Dimensions, for several Measures are now allowed and used: A Gallon for Dry Measure contains 272 Solid Inches, for Wine 231, and for Beer and Ale 282. The three following Tables are made for converting any Number of Solid Inches, whether of Corn, &c. or liquid Substance, into Gallons; the first for Dry Measure, the second for Wine, and the third for Beer and Ale.

There being 272 Solid Inches in a Gallon for Dry Measure, 34 Solid Inches will stand for a Pint; and 29 for a Wine Pint, and 35 for Beer or Ale.

The Use of these Tables is to cast up what quantity of Gallons, Pints, and Inches, are in any Number of Solid Inches, found in the Measure of any Cask or other Vessel, either for Dry Measure by the first, for Wine by the second, or for Ale and Beer by the third. Let one Example serve for all. Suppose 9845 Solid Inches were found to be contained in a Cask of Wine.



Wine, take out of the second Table 9 M. 8 C. 4 X. and to them add the 5, and you will find the Content to be 42 Gallons, 4 Pints, and 26 Inches; and the like Work for the rest.

Inch.	G.	P.	In.
9000	= 38	7	20
800	= 3	3	19
40	= 0	1	11
5	= 0	0	5
9845	= 42	4	26

Table I.

*Solid Inches turned into Dry Measures.*

	X M.			M.			C.			X.		
	G.	P.	In.	G.	P.	In.	G.	P.	In.	P.	In.	
1	036	6	04	03	5	14	00	2	32	0	10	
2	073	4	08	07	2	28	00	5	30	0	20	
3	110	2	12	11	0	08	01	0	28	0	30	
4	147	0	16	14	5	22	01	3	26	1	06	
5	183	6	20	18	3	02	01	6	24	1	16	
6	220	4	24	22	0	16	02	1	22	1	26	
7	257	2	28	25	5	30	02	4	20	2	02	
8	294	0	32	29	3	10	02	7	18	2	12	
9	330	7	02	33	0	24	03	2	16	2	22	

Table II.

*Solid Inches turned into Wine Gallons.*

	X M.			M.			C.			X.		
	G.	P.	In.	G.	P.	In.	G.	P.	In.	P.	In.	
1	043	2	09	04	2	18	00	3	13	0	00	
2	086	4	18	08	5	07	00	6	26	0	20	
3	129	6	27	12	7	26	01	2	11	1	01	
4	173	1	08	17	2	15	01	5	24	1	11	
5	216	3	17	21	5	05	02	1	09	1	21	
6	259	5	16	25	7	23	02	4	23	2	02	
7	303	0	06	30	2	12	03	0	06	2	12	
8	346	2	16	34	5	03	03	3	19	2	22	
9	389	4	25	38	7	20	03	7	05	3	03	

Table

Table III.

*Solid Inches turned into Beer and Ale Gallons.*

	C M.			X M.			M.			C.			X.		
	G.	P.	In.	G.	P.	In.	G.	P.	In.	G.	P.	In.	P.	In.	
1	0354	4	31	035	3	24	03	4	13	0	2	29	0	10	
2	0709	1	27	070	7	13	07	0	26	0	5	23	0	30	
3	1064	2	23	106	3	02	10	5	03	1	0	18	0	20	
4	1418	3	19	141	6	26	14	1	16	1	3	12	1	04	
5	1773	4	15	177	2	15	17	5	29	1	6	05	1	14	
6	2128	5	11	212	6	04	21	2	07	2	1	00	1	24	
7	2582	6	07	248	1	28	24	6	20	2	3	30	1	34	
8	2836	7	03	283	5	17	28	2	33	2	6	24	2	08	
9	3191	7	34	319	1	06	31	7	11	3	1	18	2	18	

Thus for all Bushels, Pecks, and other Measures, whether Dry or Wet, that are like Cylinders, get the Area of the Circular Base in Inches, and multiply the same by the Height in Inches, it gives the solid Content in Inches, which the foregoing Tables will turn into Gallons and Pints of Winchester Measure.

And for obtaining the Circular Base or Area, say,

As 1, to .78539; so the Diameter squared, to the Area.

Or more easily by the Logarithms, thus; Add the Logarithm of the Diameter doubled, to the Logarithm .7853985, and it gives the Area desired, which added to the Logarithm of the Height, gives the Content in Inches; and if the Tables be not at hand, you may divide those Inches by the solid Inches in a Gallon of that Liquor, and it gives the Content in Gallons.

But in measuring the Spheroid or Hoghead, or Vessels that are so figured, you must take the Diameters at the Bounding Head, and by them get the Area's by the last Rule; then take two thirds of the Area of the Circle at the Bounding, and one third of the Area at the Head, and add them together, multiply the Sum by the Length of the Vessel, and the Product gives the Solidity in Inches, which being turned into Gallons by either of the former ways, gives the Content in Gallons and Pints.

Or if you use this Proportion,

As 1, to .5236; so the Diameter squared, to  $\frac{2}{3}$  of the Area.

And,

As 1, to .2618; so the Diameter squared, to  $\frac{1}{3}$  of the Area.

Or, if by the Logarithms, for  $\frac{2}{3}$  you use .5236999, for  $\frac{1}{3}$  .2618999; it will give the Area's as before.

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If you would measure by a Gallon-Rod, so divided as it will find the Gallons and Parts in any Vessel or Cask; take the Cube Roots of 272.25 for Dry Measures, of 231 for Wine, and 282 for Beer and Ale, which are 6.481, 6.134, 6.557, and measuring the same on a Ruler of Inches, take them exactly off, and place them on some Rule severally, and divide that into 100 Parts, and so let the Ruler be divided the Length of a But or Tun, every one of those will be Gallons and 100 Parts, and whatever you measure with this Ruler, after Multiplication, all the Integers will be Gallons, and the rest Decimal Parts; which will be very useful in Gauging.

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CHAP.

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## CHAP. III.

*Of TRIGONOMETRY, or Measuring of  
Plain Triangles, Taking Heights, Depths  
and Distances, Levelling, &c.*

## PREFACE.

**T**His Chapter treats of the Analysis or Resolution of Plain Triangles, and you are not only to consider Triangles drawn before your Eye on Paper, but also those that are conceived to be made on the Ground, in the Air, upon the Sea or Waters, or in the Heavens: And because this Doctrin is of great use, and ought in all its Parts to be perfectly understood, I will therefore take more than ordinary pains to explain and accommodate it to your tender Years and Capacities, desiring you not to skip any part of this Chapter, but perfectly to understand it; and though I cannot say it is perfectly demonstrated, 'till you come to the Last Part, yet I have illustrated it, and explained it so to the full, that you will perceive the Reasons of it very plainly, and with much delight. But before I proceed to the Rules, these General Notions are to be understood.

## SECTION I.

*Of Definitions, and Notable Propositions, belonging to Trigonometry.*

I. **T**RIGONOMETRY is the Doctrin of Measuring Triangles.

II. A Triangle is a Figure comprehending three Angles by three Sides, as in the Figures 1, 2, 3, 4.

K 2

III. A

Fig. 1, 2, 3, 4.



III. A Triangle may be described either upon a Plain Superficies, or a Spherical or Globous.

IV. A Triangle described upon a Plain Superficies is called a *Plain Triangle*, as the two first Figures (1, 2.) BAC and BCD; and this kind of Triangle is always Right-lined.

V. A Triangle described upon a Spherical Superficies, or Globe, is called a *Spherical Triangle*; and such are resembled in the Figures 4, 5, by the Letters *bac* and *bcd*, and the Sides of these Triangles are always Spherical or Crooked, being Parts of the greatest Circles upon the Sphere or Globe.

Fig. 1.

VI. In every Triangle, both Plain and Spherical, any two Sides are called the *Legs* of the Angle, comprehended or contained by them; and the third Side is called the *Base* of the said Angle, as in the Triangle ABC (Figure 1.) the Sides BC and CA are the comprehending Sides, or the Legs of the Angle C, and the third Side BA is the Base of the said Angle C.

Fig. 1.

VII. In every Triangle, both Plain and Spherical, every Side is said to *subtend* or *lie under* the Angle opposite to it; as in the Triangle ABC (Figure 1.) the Side BC subtendeth the Angle A; and the Side BA subtendeth the Angle C, and the Side CA the Angle B.

VIII. In one and the same Triangle, whether it be Plain or Spherical, greater Sides subtend greater Angles, and equal Sides subtend equal Angles.

Fig. 2.

IX. The Measure of an Angle is the Arch of a Circle, described on the Angular Point, and intercepted between the comprehending Sides, being sufficiently produced: As in the Triangle BAC (Figure 5.) the Measure of the Angle ABC is the Arch CH, intercepted between the Sides BC and BA, extended to H. This I should not have repeated, because the same was said before in the last Chapter, which I desire you to call to mind, for this is especially to be noted.

Fig. 5.

X. Every Circle, as was there taught, is divided into 360 Parts, which are called *Degrees*, and every Degree is divided into 60 Parts called *Minutes*, and every Minute into 60 Parts called *Seconds*, &c. in the sexagenary Progression; but better it were to divide the Degree into Ten Parts, and every Tenth Part into Ten again, &c. in the decimal Progression; but because this Progression is not generally used, I proceed upon the former.

XI. Therefore a *Quadrant* (or Quarter of a Circle) is 90 Degrees, as the Arch DH: And the Complement of an Arch less than a Quadrant,

is that which it wanteth of a Quadrant; as the *Complement* of the Arch CH (supposing CH 20°) is the Arch CD 70°, which together make 90°.

XII. *Vertical Angles*, or those Angles which are opposite cross-wise, are equal: As CBH and EBF are equal both to 20°, and likewise the Angles CDE and HBE are equal both to 70°.

XIII. Angles, as was shewed in the foregoing Chapter, are either Right Fig. 5. or Oblique; a Right Angle hath a Quadrant, or 90 Degrees, for its Measure, as DBH; an Oblique Angle is either *Acute* (or sharp) as CBH 20°, always less than 90°, or *Obtuse* (or blunt) which is always greater than a Quadrant, as CBE, which is 160°, that is, DBC 70°, and DBE 90°.

XIV. Many Right-lined Angles, concurring in a Point of a Right Line Fig. 5. extended on both Sides, being all taken together, are equal to two Right Angles, or to 180 Degrees; as the Angles HBC, CBD, and DBE, concurring in the Point B upon the Right Line EH, are equal to two Right Angles, HBD and DEB.

XV. If a Right Line AB fall upon the Right Parallel Lines CD and Fig. 6. EF, it maketh the Angles which are alike placed to be equal, and also the Angles that are alternately placed to be equal, and contrariwise; as the Angles BHD and BGE, which are alike placed, are equal; and again, CHG and HGF, which are alternately placed, are so likewise; and so of the rest; for this I shewed before would follow, because Parallel Lines are as it were one Broad Line.

XVI. Every Triangle, whether Plane or Spherical, is either Right-angled or Oblique.

XVII. A *Right-angled Plain Triangle* is that which hath but one Right Angle; and in such, the Side that subtends the Right Angle is in an especial manner called the *Hypotenuse*, (or Subtense) and one of the Sides, including or containing the Right Angle, is called the *Cathetus* or Perpendicular, and the other is called the *Base*, as in Figure 1. According to Mr. Ough- Fig. 1. tred's Directions, every Right-angled Triangled is to be fitly noted with the Letters ABC, so that BA may be the *Base*, CA the *Cathetus*, and BC the *Hypotenuse*; and again, that B may be the Angle at the Base, C the Angle at the *Cathetus*, and A the Right Angle; as you may see in the Figures 1, 2.

Fig. 1, 2.

XVIII. An *Oblique-angled Triangle*, is that which hath all its Angles Fig. 2 & 3. Oblique, and this is most fitly noted with the Letters BCD; and whether this Triangle be Plain or Spherical, it is reduced into two Right-angled Triangles, by a *Perpendicular* let down from any Angle upon any Side made the Base, extended if need be, which *Perpendicular* will fall either within the Triangle,



Triangle, (when the Angles at the Base are of the same kind, that is, both Acute or both Obtuse, as it may fall out sometimes in Spherical Triangles,) or else without the Triangle, if the Angles at the Base be of divers kinds, (the one Acute, the other Obtuse,) on that part always where the Obtuse Angle is made; as you may see in the following Triangles.

Fig. 7, 8, 9, 10,  
11, 12.

1. Note, That the Angle from which you let down the Perpendicular may be marked with the Letter C, and the End of the Perpendicular (touching the Base BD) with the Letter A, and so the Perpendicular of both Right-angled Triangles, into which the Oblique-angled Triangle is reduced, will be CA, and their Bases BA and DA, which Bases may be called Cafes.

Fig. 8, 9, 11,  
12.

2. Note, That the Base of the Oblique-angled Triangle BD, is either the Sum of the Cafes, as in Figures 6 and 10, BD is equal to BA and DA; or else, it is the Difference of the Cafes, as in the four other Triangles in the Figures 8, 9, 11, and 12; and, that either BD is equal to DA, less by BA, as in the Triangles in the Figures 8 and 11; or BD is equal to BA, less by DA, as in the Figures 9 and 12.

Fig. 13.

XIX. In a Plain Triangle, a Line drawn parallel to the Base, cutteth the Legs proportionally, 2 P. 6 *Euclid*: As in the Plain Triangle BAC, if H I, a Parallel to the Base BA, cut off a third part of the Side CA, it will also cut off a third part of the Side BC; and therefore it will be,

$$As CA . CI :: BC . CH \text{ And } :: IA . HB$$

The reason is, because the Parallel Line cutteth all Right Lines drawn through the whole Space DELK, in such proportion, as it self cutteth the same Space.

XX. If there be two or more Plain Equi-angled Triangles, (that is, such as have the three Angles of one equal to the three Angles of the other, each to its respective Angle,) then have they the Sides about the Equal Angles proportional, 4 P. 6 *Euclid*. This being the chief Foundation of all Trigonometry, is most diligently to be regarded.

To explain it, let the Plain Triangles *bcd* and *BCD* be Equal-angled, so that the Angle *b* be equal to B, the Angle *c* equal to C, and the Angle *d* equal to D; then the Sides about the Equal Angles will be proportional, thus:

1.  $As bd . bc :: BD . BC$
2.  $As bc . cd :: BC . CD$
3.  $As cd . db :: CD . DB$

The reason is this, because the Angle *b* of the little Triangle is equal to the Angle B of the greater Triangle; therefore if *b d* be applied to BD, the Side *bc* will of necessity fall upon the Side BC. Again, because the Angle at *c* is equal to the Angle at C, and the Angle *d* equal to the Angle D, therefore when the little Triangle *bdc* is fitted into the greater *BDC*, the Side *cd* will be parallel to the Side CD; and according to the Proposition

fition next before going, the Sides of the greater Triangle BCD are cut proportionally by the Side *cd*, therefore,

$$As Bd . Bc :: BD . BC$$

Which is the first Proportion, and the same will follow in the other two, by fitting the little Triangle upon any of the Angles of the greater that is Equi-angle.

XXI. If any Side of a Plain Triangle be produced, or continued forth, the outward Angle made by that continuation, is equal to the two inward and opposite Angles, 32 P. 1 *Euclid*: As if the Side BD of the Triangle BCD be continued to G, the outward Angle CDG will be equal to the inward and opposite Angles at B and C; for if DF be drawn parallel to BC, then will the Angle CDG be equal to the Angles CDF and FDG, because Parts. But by Proposition XIV. of this Section CDF is equal to C, and FDG equal to B; therefore CDG is equal to C and B:

XXII. In every Plain Triangle, the three Angles are equal to two Right Angles, that is to say, to 180 Degrees; as in Figure 16, the Angle B, Fig. 16. more C, more the Angle BDC, are equal to 180 Degrees; for the Angles B, C, and BDC, are equal to the Angles FDG, CDF, and BDC, by the last Proposition, which all concur in one Point at D, and are all equal to two Right Angles, or 180°. Therefore,

1. In a Plain Triangle there can be but one Right or Obtuse Angle.
2. If one Angle in a Plain Triangle be either Right or Obtuse, then the other two of necessity must be Acute.
3. If one Angle in a Plain Triangle be Right, then of the two Acute Angles remaining, the one is the Complement or Remainder of the other to 90 Degrees.
4. In any Plain Triangle, if one Angle be subtracted from 180 Degrees, there will remain the Sum of the other two; or if the Sum of any two Angles be subtracted from 180°, the Remainder is the third Angle.
6. If two Plain Triangles have two Angles equal either to other, then the third Angle of the one is equal to the third Angle of the other; and so both the Triangles are Equi-angled.

XXIII. If a Plain Triangle be inscribed in a Circle, every Angle is half of the Arch opposite to it, 20 P. 3 *Euclid*: As the Triangle BCD, Figure 17, being inscribed in a Circle, if the Arch CD be 70°, the Angle Fig. 17. at C is 35°, viz. half the Arch BD; for the Angle at the Center BED is double to BCD, in what part of the Circle soever it is made. The same will happen, if the Center of the Circle falls without the Triangle, as in Figure 18; for the Angle DEB is twice the Angle BCD; and so of Fig. 18. the rest.

1. Note, That if upon the Angular Point of any Triangle, as of ABC Fig. 19. at B, there be three Circles, or more, drawn one bigger than another, the



the lesser Circle is equally a Measurer of that Angle B with the other greater Circles; for the lesser is as great a part of his Circle, as the greater of his; but this was intimated before.

2. Note, That for any thing said to be given, is the same as to be known.

XXIV. In all Plain Right-angled Triangles, one of the Sides may be conceived the Radius or Semidiameter of a Circle, and may be expressed by some Quantity, the other two Sides are expressed in Parts of the first, for all the Varieties of the Acute Angles: See those Tables, which are fitly by some called *Canons of Triangles*, and by others, *Canons or Tables of Sines, Tangents, and Secants*.

And since it is very requisite, that the Nature of *Sines, Tangents, and Secants*, be thoroughly learned by him that intends to study *Trigonometry*, I shall set down their Description in the next Section.

## SECTION II.

*Propositions, shewing the Nature of Sines, Tangents, and Secants, both in Lines, Numbers, and Logarithms.*

Chord.

I. IF A Right Line divide a Circle into two Parts or Segments, that Right Line is called a *Subtense or Chord*, (or *String*), and that part of the Circle which it subtendeth (or lyeth under) is called the *Arch* or *Bow* of the said Subtense or Chord: As in the Circle, Figure 20, K C is a Subtense or Chord, (or String,) and K E C or K F G H A C is the Arch or Bow thereof; so F A is a Subtense or Chord, and F K E C A or F G H A, either of them, the Arch of the same Chord: And so again C H is a Chord, and its Arch is C A H, or C E K F G H.

Fig. 20.

II. A *Subtense or Chord*, when it is greatest, divideth the Circle into two equal Segments, and subtendeth a Semicircle (or Half-circle or  $180^\circ$ ) on either Side; as the Right Line F A; and this is commonly called a *Diameter*.

III. Half of this Diameter is called the *Radius*, which signifieth a Sun-Beam or Spoke of a Cart-wheel, unto either of which, the *Radius* of Circles bears a very fit resemblance, issuing from the Center unto the Circumference; as the Right Lines B F, B E, B C, B A, B H, and B G.

IV. A *Subtense or Chord*, not greatest, is that which divideth the Circle into two unequal Segments, and therefore it subtendeth on the one side an Arch less than a Semicircle, and on the other side an Arch greater than a Semicircle.

Semicircle: As the Right Line C H, subtending the Arch C A H less, and the Arch C H greater than a Semicircle.

V. If a Diameter cut a *Subtense* or *Chord* at Right Angles, it cutteth it also into two equal Parts, and it cutteth also the Arch subtended by that Chord into two equal Parts: As the Diameter F A, cutting the Chord C H at Right Angles in the Point A, cutteth it also into two equal Parts or Halves in the same Point; it cutteth also the Arch C A H into two equal Parts in the Point A, and the Arch C H into two equal Parts at F.

VI. Half of the Chord thus Divided, is called *Sinus Rectus*, or the *Right Sine* of that Half of the Arch so cut by the Diameter it subtendeth. Thus C A is the Right Sine of the Arch C A, and also of the Arch C E F; and likewise A H is the Right Sine of the Arch A H, and also of the Arch H G F. Hence it followeth:

1. That the *Right Sine* of an Arch, less than a Quadrant, and of its Complement to a Semicircle, is one and the same Right Line; as the Right Sine of the Arch C A and C E F, is the same Right Line C A.

2. And therefore when we say, the *Right Sine*, or the Sine of the Complement of an Arch, we mean, the Right Sine of the Complement of the Arch less than a Quadrant, that is, the Complement or Remainder unto a Quadrant or  $90^\circ$ , and not unto a Semicircle: As the Right Sine of the Complement of the Arch C A, namely, of the Arch it self C E, is the Right Line C I.

3. The *Right Sine* of the Complement of an Arch, is equal to that Part of the Diameter or Radius, which is intercepted betwixt the Right Sine of the Arch and the Center of the Circle: As the Right Sine of C E (being the Complement of C A) namely, the Right Line C I, is equal to the Right Line A B.

VII. That Part of the Diameter, dividing the Subtense or Chord, *Verfed Sine*, which is intercepted between the Right Sine and the Circumference, is called *Sagitta* (an Arrow) or *Sinus Versus*, the *Verfed Sine*: As A A is the *Sagitta*, Arrow, or *Verfed Sine* of the Arch C A; and so is F A the *Verfed Sine* of the Arch C E K F.

VIII. Therefore, taking the Right Sine of the Complement of an Arch from the Radius, it leaves the *Verfed Sine* of the same Arch: As B A Radius, less by B A, the Sine Complement of C A, leaves C A, the *Verfed Sine* of C A. And so the Right Sine of the Complement of an Arch, being added to the Radius, gives the *Verfed Sine* of the same Arch.

IX. If a Right Line, touching a Circle at the one End of an Arch, meet with the Radius produced at the other End of the Arch, it is called, the *Tangent* of the Arch thus bounded; and the Radius so produced to the *Tangent* is called the *Secant* of the same Arch, because it cutteth through the

*Tangent.*  
*Secant.*



the Circle: As the Line  $ac$  is the Tangent of the Arch  $aC$ , and the Line  $Bc$  is the Secant of the same Arch  $aC$ ; so likewise  $ED$  is the Tangent of the Arch  $E, C$ , and  $BD$  is the Secant of the same Arch.

X. The *Radius*, the *Right Sine*, and the *Right Sine of the Complement* of any Arch, make a Plain Right-angled Triangle, as  $BAC$ ; and the *Radius*, the *Tangent*, and *Secant* of the same Arch, make another Right-angled Triangle, Equal-angled, or like to the former, as the Triangle  $Bac$ : And lastly, the *Radius*, the *Tangent* of the Complement of the same Arch, and the *Secant* of the Complement of the same Arch, make another Triangle, Equal-angled, or like to both the former, as the Triangle  $BED$ .

Hence, by the former Proposition of Equi-angled Triangles, by comparing one Triangle with another, and taking the Sides about the Equal Angles, will follow these Propositions, between the *Radius*, the *Sine*, *Tangent*, and *Secant*, of one and the same Arch; and the *Sine*, *Tangent*, and *Secant*, of the Complement of the same Arch; thus:

1. As Sine Complement, to Sine; so Radius, to Tangent. Because,  
 $BA . CA :: BA . Ca$
2. As Radius, to Sine; so Secant, to Tangent. Because,  
 $BC . CA :: Bc . Ca$
3. As Sine, to Radius; so Radius, to Secant Complement. Because,  
 $CA . BC :: BE . BD$
4. As Tangent, to Radius; so Radius, to Tangent Complement. Because,  
 $Ca . Ba :: BE . DE$

XI. The *Diameter*, the *Chord* of an Arch, and the *Chord* of the Complement of the same Arch to a Semicircle, make a Right-angled Triangle, as  $FCA$ ; and the *Sine* of the same Arch is always a Perpendicular, drawn from the Right Angle of the said Triangle upon its Base, as the Sine  $CA$ ; and therefore (by *S. P. 6 Euclid*) there are three Right-angled Triangles, all Equi-angled, or like one to another, as the three Triangles  $FCA$ ,  $FAC$ , and  $CAa$ . Hence it followeth, by comparing those Triangles.

1. As Sine Verfed, to Sine; so Sine, to Sine Verfed of the Complement to 180 Degrees. Because,  
 $FA . CA :: CA . Aa$
2. As two Radii, to Chord; so Chord, to Sine Verfed. Because,  
 $Fa . Ca :: Ca . Aa$

Descriptions of  
the Lines upon  
Paper.  
Fig. 21.  
Line of Chords.

XII. Having hitherto treated of these Lines in general, I come now to shew how they may be described upon Paper severally, viz. the Lines of *Chords*, *Sines*, *Tangents*, and *Secants*. And first of the *Chords*.

1. Form the general Figure 21, and divide the Circle (as you have been before taught) into four Quarters or Quadrants, viz.  $M, N, O, V$ , by crossing the Center  $C$  with two Diameters at Right Angles, viz.  $AB$  and  $PQ$ ; divide each Quadrant into 90 Degrees, and number them as in the before-mentioned Figure, that is, the Quadrants  $M$  and  $N$  from  $A$  and

and  $B$  toward  $Z$  into 90 Degrees each, and the Quadrants  $O$  and  $V$  into 90 Degrees each from  $P$ ; then to describe a Line of Chords of 90 Degrees, draw the Chord of 90 Degrees from  $P$  to  $B$  in the Quadrant  $V$ , and setting one Foot of your Compasses in  $P$ , extend the other from Degree to Degree, through all the 90 Degrees of the Quadrant  $V$ , in the Circle  $PB$ , keeping that in the Point  $P$  fixt, and transfer them all into the Chord-Line  $PB$ , as they are actually done in the Figure for every 10 Degrees, and number them from  $P$  to  $B$ , thus, 10, 20, 30, &c. Now it is plain, that this Line is a Line of Chords, all the Chords being actually transferred into it. And because a Line of Chords of 60 Degrees will many times be sufficient for use, you have the same described from  $P$  to  $Q$  in the said Quadrant  $V$ . And these Lines, for a greater or lesser Circle, may be thus divided, and placed upon some Ruler, or otherwise, as you see below in  $pb$  and  $pq$ . Note, that  $pq$  is always equal to the Radius or Semidiameter, by which it was made.

2. The Line of *Sines* being always equal to the Radius of the Circle, *Line of Sines*, and here represented by the Semidiameter  $CZ$ , and  $CA$ , both these being the same, and thus divided, lay a Ruler from Degree to Degree in the Quadrants  $N$  and  $M$ , from  $A$  and  $B$  towards  $Z$ , viz. from  $10^\circ$  to  $10^\circ$ ,  $20^\circ$  and  $20^\circ$ ,  $30^\circ$  and  $30^\circ$ , &c. as you see actually in Figure 21, being all Parallels to  $ACB$  the Diameter, and numbered from  $C$  to  $Z$  accordingly: And that this is a true Line, representing all Sines of each particular Degree in the Quadrant, is visible in the Quadrant  $N$ , where the Natural Sines are let fall perpendicularly, from each 10 Degrees in the Quadrant, upon  $AC$  the Radius, which is equal and alike divided, as  $CZ$ ; and this Line may be placed upon a Ruler, or otherwise, as may be seen below the Figure at  $cz$ .

3. The Line of *Tangents* is represented by the Line  $BRTX$ , raised perpendicularly upon the End of the Diameter  $B$ , and it is divided into Degrees by laying a Ruler upon the Center  $C$ , through and upon every Degree of the Quadrant  $BC$  of the Circle, and to mark out the Divisions upon the Tangent-Line, as you see actually done for every 10 Degrees: And that this Tangent-Line thus divided, is the true Tangent-Line for this Circle, is plain by Proposition IX. of this Section; which may be transferred and placed upon a Ruler, as below is done upon  $bx$ .

4. The Line of *Natural Secants* is represented by the Line  $B, r, t$ , and is described by fixing one Foot of the Compasses in the Center of the Circle  $C$ , and extending the other Foot to every Degree in the Tangent-Line, transfer the same into the Secant-Line  $B, r, t$ , as you see in the Figure, for every 10 Degrees, which is according to the Definition in Proposition X. and is described apart below in the Line  $br$ .

5. I will shew you another Division, very useful in many Propositions of the Sphere or Globe, especially for the Projecting thereof, which is, a Line of Half Tangents. This Line is made upon the Semidiameter or Radius  $CP$ , which is divided by laying a Ruler upon the Point  $A$ , and upon every Degree of the Quadrant  $V$  in the Circle  $PB$ , and marking the Divisions



upon the said Radius PC, as you see done, for every 10 Degrees: By which it is plain, that this Line is a Line of Half the Natural Tangents; for having continued the Tangent-Line downwards to 45 Degrees, every one of those will be two Degrees upon CP, because the Angles at the Center C are double to the Angles at the Circumference A, all represented below by *brr*.

The Line of *Verfed Sines* I meddle not with here, as having said already as much as is sufficient for this place, and shall leave the rest 'till another time.

Note, That 60 Degrees upon the Line of Chords, 90 Degrees upon the Sines, 45 upon the Tangents, and the first Beginning of the Line of Secants, are all equal to the Radius or Semidiameter.

XIII. Having described these Lines already, Geometrically and Naturally, and they being of such wonderful Use, that industrious Mathematicians have made Tables for every Degree, Minute, and TenSeconds, in Numbers, I shall now proceed to give some light for the Making those Tables, and of their Nature, though the Demonstrations I must refer to another place.

After the Table of Logarithms, in the Third Part of this Work, follows the Canon of Triangles, which contains first the Tables of *Natural Sines*, *Tangents*, and *Secants*, and then the *Logarithms* of the Sines and Tangents. Of all these I shall give the following account.

Natural Right  
Sines in Num-  
bers.

1. The *Right Sines*, in order to their Construction in Numbers, are either *Primary* or *Secondary*. The *Primary* are these, (by which the rest are found) first the Radius or Semidiameter, which is always put to be 1,000, 1,0000, 1,00000, or more, and is the Side of a sexangle Figure inscribed in a Circle, equal always to the Chord of 60 Degrees, as has been often remembered, is the first *Primary Sine*; from which it follows, that the half of the Radius, or the Chord of 60 Degrees, is the *Sine* of 30 Degrees, which Number if you seek in the Tables under 30 *Deg.* you will find against it the *Sine* 50000. The other *Primary Sines*, are 60, 18, and 12 Degrees, being the Halves of the Chords 120, 36, and 24 Degrees, and may easily be found. Now the *Secondary Sines* of 6, 3, 1, &c. Degrees, are found from the former, and so the whole Table may be made by such Rules, that will be too long and intricate for you to know at this time.

Description of  
the Tables of  
Natural Sines.

The Table of *Natural Sines* begins with the *Sine* of 1 Minute, which is found to be .00029, such as the Radius is 1,00000, and so proceeds to 60 Minutes, or 1 Degree, and so on in the first Column, from Degrees to Degrees and Minutes, 'till it comes to 45 Degrees, the *Sine* whereof is .70711; and then returns from 45 Degrees to 1 Degree or 60 Minutes, and so back again in the second Column to 90 Degrees, which are the Complements of the first Column, or Remainder to 90 Degrees; as in these Examples.

*Deg.*

Deg. Min.	Sines.	Co-sines.	Deg. Min.
3 45	.06540	.99786	86 15
7 10	.12476	.99219	82 50
27 19	.45891	.88848	62 41
38 30	.62251	.78261	51 30
47 15	.73432	.67880	42 45
59 39	.86295	.50528	30 21
78 40	.98050	.19652	11 20

The first Column contains the Degrees and Minutes, proposed to find the Sines, which are set down in the second Column, and in the third Column is the Complements of those Sines, called for shortness *Co-sines*, and in the last Column are the Degrees and Minutes of the Quadrant, which are the Complements to those in the first Column to a Quadrant.

Thus may any *Sine*, for any Number of Degrees and Minutes to a Quadrant, be found quickly out.

2. The *Natural Numbers* for the *Chords* are easily deduced from those of *Natural Sines*, for because, as I shewed you before, the *Sine* of any Degrees is half the Chord of that doubled Arch; as the *Sine* of 30 Degrees being .50000, doubled makes 1,00000, for the Chord of 60 Degrees, equal to the Radius: So if I desire the Chord of 38 Degrees, I seek in the Table for the *Sine* of 19 Degrees, the half thereof, which I find to be .32557, which I double, and it makes .65114, the Chord of 38 Degrees. And after this manner, I made the Table for the Chords, for each Degree to 90, for the Radius 1,000, of three Places only.

A Table of Chords for whole Degrees to 90°.

D. Chord.	D. Chord.	D. Chord.	D. Chord.	D. Chord.	D. Chord.
1 .017	16 .278	31 .534	46 .781	61 1,015	76 1,231
2 .035	17 .296	32 .551	47 .797	62 1,030	77 1,245
3 .052	18 .313	33 .568	48 .813	63 1,045	78 1,259
4 .070	19 .330	34 .585	49 .830	64 1,060	79 1,273
5 .087	20 .347	35 .601	50 .845	65 1,074	80 1,286
6 .105	21 .364	36 .618	51 .861	66 1,089	81 1,299
7 .122	22 .382	37 .635	52 .876	67 1,104	82 1,312
8 .139	23 .398	38 .651	53 .892	68 1,118	83 1,325
9 .157	24 .416	39 .668	54 .908	69 1,132	84 1,338
10 .175	25 .432	40 .684	55 .923	70 1,147	85 1,351
11 .192	26 .450	41 .700	56 .939	71 1,161	86 1,364
12 .209	27 .466	42 .717	57 .954	72 1,176	87 1,377
13 .226	28 .484	43 .733	58 .970	73 1,190	88 1,389
14 .244	29 .501	44 .749	59 .984	74 1,204	89 1,402
15 .261	30 .518	45 .765	60 1,000	75 1,217	90 1,414

This



This Table of Chords will be of good use, for the Making of Lines of Chords for any given Radius, as I shall forthwith shew you.

Natural Tan-  
gents and Se-  
cants.

3. The *Natural Tangents* and *Secants*, as they are expressed in the said Tables, and go along, (*viz.* the *Tangents* in the fourth and fifth Columns, those in the fourth for all Degrees and Minutes under  $45^\circ$ , and in the fifth for *Tangents* above  $45^\circ$ , and 10 for the *Secants* in the sixth and seventh Columns,) may be made out of the Tables of Sines, by several Proportions, too difficult and tedious to be here set down.

The Usefulness of these Tables will fully appear, when I come to the Resolution of Triangles. But before I go further, I will here shew, how the Scales (for any Radius) of Chords, Sines, and Tangents, may be easily made by them.

Fig. 21, 22.

First for Chords, if you make a Decimal Diagonal Scale of the Length of the Radius, (as for Example, to the Radius of the Circle in Figure 21 is made a Diagonal Scale in Figure 22,) and then with your Compasses if you take from that Scale the Numbers answering the Degrees in the Table of Chords last set down, and prick them down on a Line, you may make a Scale that will be just equal to the Scale of Chords, *p b* for  $90^\circ$ , or *p q* for  $60^\circ$ , described under Figure 21. For Example, if out of the Diagonal Scale you take 551, the Number answering 32 Degrees in the Table, that Distance will reach from *p* in either of those Scales to  $32^\circ$ .

Uses of the  
Chords.

The Uses of these Lines of Chords are very great, for whereas I taught you (in the *Practical Geometry*) to measure or lay down Angles by the Circle divided, now by a Line of Chords you may do the same as suddenly, for if you take the Chord of 60 Degrees, and describe a Circle upon the Point of the Angle, the Scale will measure the Chords as in a Circle; and having three of them made of several Radiusses, they will be more proper than Circles of those Semidiameters.

Scale of  
Chords.

Scale of Tan-  
gents.

So likewise the Scales of *Sines*, *Tangents*, and *Secants*, described by *c z* for Sines, *b x* for Tangents, and *b r c* for Secants, may be made by the Tables, as well as before I shewed by the Circle itself. For Example, if I would find the Length of  $41^\circ$  of the Tangents, I look in the Table of Tangents and find 869/29, and cutting off two Places to the right hand, as too exact for the butinels, I take 869 from the Diagonal Scale in Figure 22, and setting one Foot of the Compasses in *b* on the Tangent Scale, the other will reach to  $41^\circ$  exactly.

Fig. 20.

XIII. These Tables thus described, the Radius to them being 100000, and this Radius being always one Side of a Right-angled Triangle, the other two are expressed in the Canon or Tables by *Sines*, *Tangents*, or *Secants*. For Example, let the Right-angled Plain Triangle B A C in Figure 20 be considered; if you make B C the Hypotenuse Radius, that is 1,00000, and if the Angle at B be 30 Degrees, equal to the Arch *a c* 30 Degrees, then is the Side C A the Right Sine of 30 Degrees, that is 50000, and B A the Sine Complement of B (*viz.* the Sine of the Arch E C, equal to the Angle B C A) that is 86603.

Again, if you consider the Right-angled Plain Triangle B a c, and make B a Radius equal to 1,00000, then will *a c* be the Tangent of 30 Degrees 57735, and B c will be the Secant of 30 Degrees 1,15470. And this may be done for as many Triangles, as there are Lines for Degrees and Minutes in the said Tables; so that if you would know the Quantities of the Sides, and have but the Angles, you may set them down as before very easily.

Near to these Natural Sines and Tangents stand the *Artificial Sines* and *Tangents*, against their respective Degrees and Minutes, and are to be found as was shewed before in the Natural. The *Artificial Secants* are not set down, because they may be omitted, and the Resolution performed by the Sines and Tangents only. The Making of these Artificial Sines and Tangents I shall purposely omit, they being nothing but the Logarithms of the Natural Sines and Tangents, which Logarithms I shall shew the Reason of in the Last Part.

Artificial Sines  
and Tangents.

These things being premised, I shall now come to the Calculation it self of Plain Triangles, which (as much as I here intend) is nothing else, but to find out the Fourth Term from Three given, by the *Golden Rule of Proportion*. And these Four Terms are always Four Right Lines, whereof Two are always the Sides of one Right-lined Triangle, and the other Two are the Sides of another Right-lined Triangle, of Equal Angles with the former; so that all their Sides about their Equal Angles are Proportional, as it appears by Prop. XIX. Sect. I. of this Chapter.

All Right-lined Triangles are already Calculated in the Table of *Sines*, *Tangents*, and *Secants*, according to the Parts of the Radius of the Circle, into which the Triangle is ascribed, the said Radius being supposed to be 1 with Cyphers, as 1,0000 or 1,00000, &c. as before. If therefore you have a Triangle to be Resolved, you may do it by help of one of these Triangles, of Equal Angles with the Triangle to be Resolved; all the Parts of which Triangle are defined by the said Tables of Sines, Tangents, &c. and among the multitude of Plain Triangles defined by those Tables, you shall light upon the right one, by comparing the Parts of it with the Parts of the Triangle to be Resolved, as you may see in the following Problems, which I shew how to Resolve three manner of ways, *viz.* 1. By Scale and Compass: 2. By Natural Sines, Tangents, and Secants: And 3. By Logarithms.



## SECTION III.

## The Calculation or Measuring of Plain Right-angled Triangles.

For the Calculation, there are two Problems, according to the twofold Variety in the Four Parts of the Triangle, which are Ingredients in the Question, whereof the Right Angle (or 90 Degrees) is always one.

## Problem I.

Of these Four, the Right Angle, One of the Acute Angles, the Hypotenuse, and the Side subtending the Acute Angle; any Three being given, to find out the Fourth.

The Right Angle being always 90 Degrees, equal to the Radius, is always given and known, wherefore any Two of the Ingredients will find the Third.

Fig. 23.

Let the Triangle proposed to be Resolved be  $abc$  in Figure 23, where the Angle at  $b$  is  $23^\circ 15'$ , therefore the Angle at  $c$  will be (its Complement to  $90^\circ$ )  $66^\circ 45'$ , the Hypotenuse  $bc$  347 Yards, and it is required to find out the Sides  $ba$  and  $ca$ .

Fig. 24.  
Fig. 25.

1. To perform this by Scale and Compass, which you must have ready, and a Circle, or a Line of Chords divided exactly into Degrees, and let your Scale of Equal Parts be a Diagonal, suppose of Inches, as in Figure 24, with the Line of Chords adjoining to it. Thus in Figure 25 draw a Line to represent the Base  $ba$  at length, set it off by the Line of Chords, taking 60 of it for the Radius, describe the Arch  $fd$ , take out  $23^\circ 15'$  from the Line of Chords, and set it from  $d$  to  $f$ , and draw the Line  $bfc$  at length, from the Diagonal Scale Figure 24, take off 347, (by setting the Compasses in the Line of 3 Inches for 300, then tell 7 of the Parallel Lines in the said Line, and go up that Parallel Line 'till you meet with the Diagonal, that crosseth it, that Distance is 347) which set from  $b$  to  $c$ , then from  $c$  let fall a Perpendicular  $ca$  upon the Base Line  $ba$ , and where it meets, as at  $a$ , the two Sides  $ba$  and  $ca$  are given and terminated, and taking them one after another, and applying them to the Scale Figure 24, you shall find  $ba$  318.8, and  $ca$  136.9 Yards, which is 318 Yards, and  $\frac{8}{10}$  of a Yard, and 136  $\frac{9}{10}$  Yards. The same would follow, if you set off the Angle  $c$ , and let fall the Perpendicular  $ba$ .

But suppose the Base  $ba$  was given 318.8, and the Angle as before, to find out the Hypotenuse and Cathetus  $ca$ , I draw a Line for the Base  $ba$ , and set off from the former Scale 318.8 from  $a$  to  $b$ , then upon  $b$  I set off  $23^\circ 15'$ , and draw  $bc$  at length, lastly upon  $a$  I raise the Perpendicular  $ac$ , and

and so find by Measure  $bc$  347, and  $ca$  136.9. Thus is this Problem easily resolved mechanically.

2. By *Natural Sines* the Proportion will be found thus: *As* Radius, or Sine of  $90^\circ$ , (the first Term,) *to* the Sine of the Acute Angle; (the second Term;) *so* is the Hypotenuse, (the third Term,) *to* the Side subtending the Acute Angle, (the fourth Term.)

The four Terms may be altered to find any of the things sought; for the Rule being,

$$1. 2 :: 3 . 4$$

By multiplying the second and third Terms, and dividing the Product by the first, you will find out the fourth Term.

But if the third Term was sought, then say,

$$2. 1 :: 4 . 3$$

And if the second Term was sought, then say,

$$3 . 4 :: 1 . 2$$

And so of any such Terms, which must be diligently observed.

Now the former Proportion is found out, as in Figure 25, where the Triangle proposed to be Resolved is  $abc$  as before, and the Circle has in it the Triangle  $ABC$ , Equi-angled to  $abc$ , and therefore their Sides about  $B$  and  $C$  are proportional, that is, *As*  $BC$  Radius, *to*  $CA$  the Sine of  $C$  or  $c$ ; *so* is  $bc$  the Hypotenuse, *to* the Side  $ba$ . Because they are both Right-angled, and the Angle  $B$  being made equal to the Angle  $b$ , the Angle  $C$  is equal to the Angle  $c$ . And so the Rule holds as above.

Therefore if the Side  $ca$  was demanded, it will be, *As* Radius 1,00000, *to* the Sine of the Angle  $b$  39474; *so* is the Hypotenuse  $bc$  347, *to* the Side  $ca$ . Multiply 39474 by 347, and it gives 136.97478, which divided by 1,00000, gives for Answer 136.9, for the Side  $ca$ .

3. By *Logarithms*, which performs all without any labour of Multiplication and Division; in stead of multiplying the second and third Terms, add their Logarithms, and in stead of dividing by the first, subtract its Logarithm from the Sum of the other two, and the remaining Logarithm will give the Answer. But now you must call to mind the former Rules in *Arithmetick*, concerning Decimals and Logarithms.

The General Rule for Resolving the last Problem, made by comparing the two Triangles, gives the following Analogies, wherein for the Hypotenuse I take  $bc$ , for the Base  $ba$ , and the Cathetus  $ca$ , the Angles, *fi* for Sine, *ft-co* for Sine Complement, *t* for Tangent, and *t-co* for Tangent Complement; the Secants are set by.

To find  $ca$ , by  $bc$  and the Angle at  $b$ .

1. For $ca$	As Radius,	10,00000
	to $bc$ 347;	2,540329
	So $fi$ $b$ $23^\circ 15'$ ,	9,9596315
	to $ca$ 136.98.	82,136644

So the Cathetus  $ca$  is 136  $\frac{9}{10}$  Yards.

M

2. For



2. For $ba$	{	As Radius,	10,000000
		to $bc$ 347;	2,540329
		So $fi$ of $c$ $66^\circ 45'$ ,	9,963217
		to $ba$ 318.82	2,503546

So the Base  $ba$  is  $318\frac{1}{4}$  Yards.

Having the Base, or Cathetus, and one of the Angles,  $b$  or  $c$ , to find the Hypothenuse.

3. For $bc$	{	As $fi$ $c$ $66^\circ 45'$ ,	9,963217
		to Radius;	10,000000
		So $ba$ 318.8,	2,503545
		to $bc$ 347.	2,540328

So the Hypothenuse is 347 Yards.

Again, $bc$	{	As $fi$ $b$ $23^\circ 15'$ ,	9,596315
		to Radius;	10,000000
		So $ca$ 136.98,	2,136644
		to $bc$ 347 Yards.	2,540329

So is the Hypothenuse 347 Yards, as before.

Having the Hypothenuse and Cathetus, or Base, to find the Angles.

4. Angle at $c$	{	As Hypothenuse $bc$ 347,	2,540328
		to Radius;	10,000000
		So Base $bc$ 318.8,	2,503545
		to $fi$ Angle $c$ $66^\circ 45'$ .	9,963217

So is the Angle at  $c$  found to be  $66^\circ 45'$ .

5. Angle at $b$	{	As $bc$ 347,	2,540328
		to Radius;	10,000000
		So $ca$ 136.9,	2,136644
		to Angle at $b$ $23^\circ 15'$ .	9,596316

So the Angle at  $b$  is found to be  $23^\circ 15'$ .

Problem

### Problem II.

Of these Four, the Right Angle, the Acute Angle at the Base, the Base, and the Cathetus; any Three being given; to find out the Fourth.

The Operation in the last Problem, by the Compass and a Circle divided, will shew this or any other Proposition in Right-angled Plain Triangles; for suppose either of the Acute Angles, and either Base or Cathetus, be given, work thus: Upon Paper draw a Line that shall represent the Base  $BA$ , Figure 26, raise a Perpendicular at  $A$ , viz.  $AC$ , then for either the Base or Cathetus being given, set the same off from your Scale from  $A$  to  $B$  or  $C$ , then at  $B$  or  $C$  set off the Angle given, it will limit the Triangle, and give you the Hypothenuse, or the other Side.

I shewed you the Practice by the last Problem, and when you will exercise your Pen to Arithmetick, you may work this by Natural Sines and Tangents, multiplying in stead of adding, and dividing in stead of subtracting, as followeth by Logarithms.

First for the Analogy, As Radius, (1,) to the Tangent of the Acute Angle at the Base; (2;) so is the Base, (3,) to the Cathetus, (4.) And if it be

$$1. 2 :: 3. 4$$

It will follow

$$2. 1 :: 4. 3$$

And

$$3. 4 :: 1. 2$$

This ariseth from comparing the Triangle  $BAC$  (Figure 26) with the Triangle  $BKD$ , (Figure 25,) alike and Equi-angled, because the Angle  $B$ , in the Triangle  $BAC$ , to be resolved, is equal to the Angle  $KBD$ , in the Triangle to be compared, and having either of them, the remaining Angles will be equal; and therefore, As  $BD$  Radius, to  $DK$  the Tangent of the Angle at the Base  $B$ ; so is the Base  $BA$  given, to the Cathetus  $CA$ ; which is the former Analogy, and to be varied as before, therefore, &c.

For $CA$	{	As Radius,	10,000000
		to Tangent of $B$ $23^\circ 15'$ ;	9,635098
		So $BA$ 318.82,	2,503545
		to $CA$ 136.98	2,136643

For $BA$	{	As Radius,	10,000000
		to $fi$ of $C$ $66^\circ 45'$ ;	10,366901
		So is $CA$ 136.98,	2,136657
		to $BA$ 318.82	2,503558



For the Angle at B	As BA 318.82,	2,503545
	to Radius;	10,000000
	So is CA 136.98,	2,136657
For the Angle at C	to t. Angle B 23° 15'	9,633112
	As CA 136.98,	2,136657
	to BA 318.82;	2,503545
	So is Radius,	10,000000
	to t. Angle C 66° 45'.	10,366888

47 Pr. 1 Eucl. Here I think fit to declare the 47th Proposition of the First of Euclid, that is, That the Square of the Hypotenuse of a Right-angled Triangle, is equal to both the Squares made upon the Base and Cathetus; for Example see Figure 27, where ABC is a Right-angled Triangle, the Right Angle is A, the Square of the Hypotenuse is B C D F, which is always equal to the two Squares BAKI and ACCH; for 5, 4, 3, will be the Sides of such a Triangle, 5 for B C, 4 for B A, and 3 for A C, the Square of 5 is 25, the Square of 4 is 16, and of 3 is 9; now the Square of B C is 25, and the Squares of B A and C A are 16 and 9, which are equal to 25.

By this Proposition, if any two Sides of a Plain Right-angled Triangle be given, the third Side is easily found; for suppose B A, 4; and C A, 3; to find B C, square 4 and 3, and they make 16 and 9, which added together make 25, the Square Root whereof is 5 for the Hypotenuse or B C.

Again, if the Hypotenuse B C, 5, and B A, 4, were given, to find the Cathetus; square them, and they make 25 and 16, take 16 out of 25, and there remains 9, the Square Root whereof is 3 for the Cathetus.

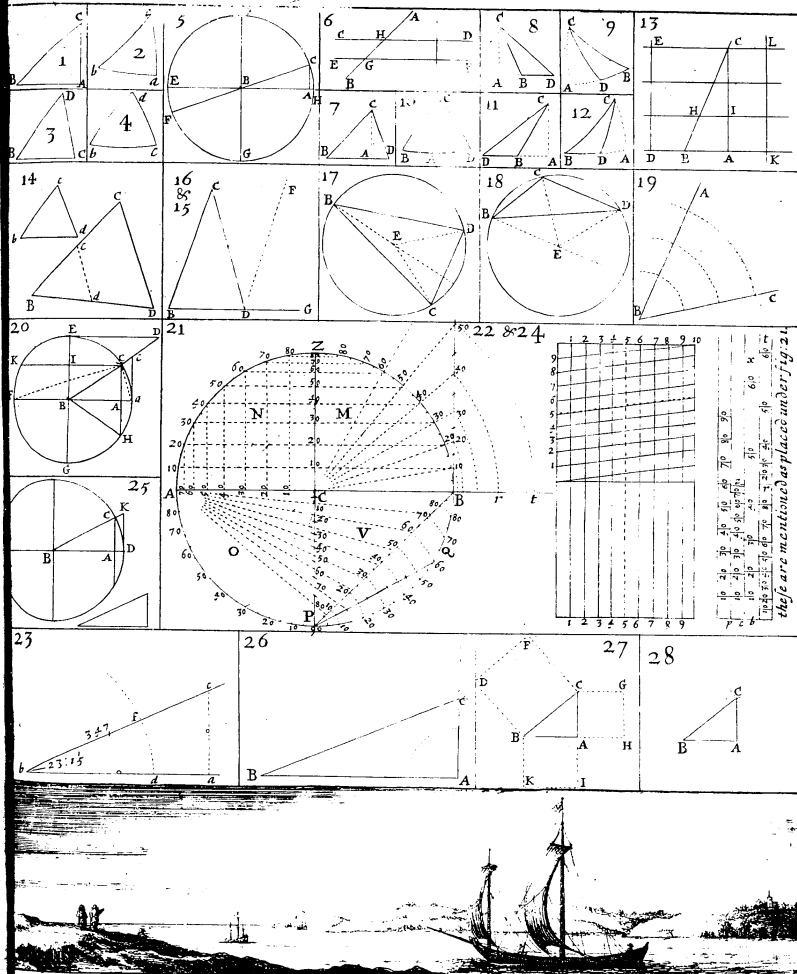
Here note, By these three Numbers, 5, 4, 3, you may either upon Paper, or upon the Ground, raise a Perpendicular most easily, even upon the End of a Line; for if it were demanded to raise a Perpendicular upon the Point A in Figure 28, from the Scale equally divided take 4, and set it from A to B, then take 3 in your Compasses, and make an Arch above A at C, as you see in the Figure, then from your Scale take 5, and setting one Foot of your Compasses in B cross the former Arch at C, then draw C A, so shall B C A be a Right Angle.

Fig. 28.

Upon the Ground.

But if the Right Angle were to be laid down on the Ground, stake out the straight Line, then take a long Chord or Chain, and dividing it into Yards, Feet, or Fathoms, (a Fathom being 6 Feet) at every Yard or Fathom make a Knot, then upon the Line whereon it is required to raise a Perpendicular, fix the End of the Chord or Chain, and first mark out 4 Knots in the Line, after which taking an Iron Pin or Picket fasten it in the third Knot, and make a Score with your Pin over the Point, then shift your Pin into the fifth Knot, and fastening the End where you marked 4, cross that Arch, and from that place a Perpendicular, which will fall upon the Point given.

Pro-





## Problem III.

*In all Plain Triangles, whether Right or Oblique-angled, of these Four Parts, Two Angles, and Two Sides subtending those Angles; any Three being given, to find out the Fourth.*

**T**He Analogy for resolving this Problem will be this, *As the Sine of one Angle, to the Side that subtends it, or is opposite; so the Sine of another Angle, to the Side that subtends it.*

In Right-angled Triangles this Proportion is the very same with the first Problem, because the Radius is the Sine of the Right Angle, which is always subtended by the Hypotenuse. Yet in General, for all Plain Triangles, it is grounded upon the Proportion, that is between the Sides of a Triangle inscribed in a Circle, and the Triangle proposed to be resolved, being of Equal Angles with the Inscribed Triangle. Thus, let the Triangle proposed to be Resolved be BCD, and the Triangle inscribed be *bcd* Fig. 29. Equi-angled to the former, wherein every Side is half the Sine of the opposite Angle, as shall be demonstrated; and seeing that the Halves of Proportional Numbers, bear the same Analogy that their Wholes do, it will be plain, *bc* is proportional to BC, *cd* to CD, and *bd* to BD; or, *As the Sine of b, to BC; so the Sine of b, to CD; and the Sine of c, to BD; or, because the Triangles are Equi-angled, the Sine D is to BC, as the Sine B to CD, and as the Sine of C to BD.*

## Example.

*Let there be given the Angle at D  $22^{\circ} 30'$ , the Angle at B  $52^{\circ} 30'$ , the Side BC 346 Yards, and let the Sides BD and CD be sought.*

1. By Scale and Compass: Draw a Line EF, whereon by your Compasses and Scale set off 346 from B to C. Then set off  $105^{\circ}$ , which is thus gotten, sum up the Angles B and D, which make  $75^{\circ}$ , take that from  $180^{\circ}$  (the Sum of all the Angles) and there remains 105 for C. Then taking 60 upon your Circle, or Line of Chords, for the Radius, describe two Arches upon the Points B and C at *x* and *y*, and at B set off  $52^{\circ} 30'$  from *y* to *r*, and at C from *x* to *s*, and draw the Sides BD and DC; then have you the Point D for the Triangle. And upon the same Scale, if you measure CD, you will find it 717.3 Yards; and BD, 873.3 Yards. By Scale and Compass. Fig. 29.

2. By Natural Sines, the Proportion, as before is declared, will stand thus: *As the Sine of D  $22^{\circ} 30'$ , 38268, to the Side BC 346; so the Sine of B  $52^{\circ} 30'$ , 79335, to the Side CD, which is 717.3, as by working this Question will appear. First, I multiply the Third Term, 79335 by 346 the Second, which makes for the Product 27449910; and then I divide that by 38268, which gives the Quotient 717.3, that is  $717 \frac{3}{4}$  Yards for the Side CD.* By Natural Sines.



38268 . 346 :: 79335 . 717.3

346  
476010  
317340  
238005

38268) 274.49910 ( 717.3

267876  
66231  
38268  
279630  
267876  
117540  
114804  
2736

The next Operation by the Logarithms will shew you, what ease in Calculation comes by that Noble Invention.

By Logarithms. 3. By the Logarithms, thus: Set the Logarithms of the first, second, and third Terms down, as in the following Work, then add the second and third Terms together, which make 12,438542, out of that take the first Logarithm 9,582839, and there remains 2,855703, the Logarithm of 717  $\frac{1}{4}$  Yards.

Sine of D 22° 30', its Logarithm	9,582839
The Side BC 346, its Logarithm	2,539076
Sine of B 52° 30', its Logarithm	9,899466
Sum of the second and third	12,438542
First out of the fourth	2,855703

Now it was shewed, that all Angles of a Plain Triangle are equal to two Right Angles, therefore having the Sum of the Angles B and D 75 Degrees, take that from 180, and it leaves 105 Degrees; but you must use 75 to find out the Sine amongst the Table of Sines, because the Right Sine of 75 Degrees, is the Sine of 105 Degrees, as you have been taught already; and you may see it by the following Work, in seeking out the Side BD, which is found to be 873.33 Yards. Then have you all the Sides and Angles of the Triangle BCD. And so having the Angles, there is no difficulty to get the Sides.

Sine

Sine of D 22° 30', its Logarithm	9,582839
The Side BC 346, its Logarithm	2,539076
Sine 105°, or 75°, its Logarithm	9,984944
The second and third Terms added	12,524020
The Logarithm of 873.33	2,941181

But if one Angle only be given, and two Sides, whereof one is the greatest Side in the Triangle, and the other opposite to the Angle given, and the Angles be required, then it will be a doubt, whether that Angle be Acute or Obtuse which is opposite to the greatest Side, it is requisite therefore it be declared, by laying down the same by Scale and Compass.

Example.

Having the Side BC 346 Yards, BD 873.33 Yards, and the Angle at D 22 Degrees 30 Minutes; to find the Angle at C.

Lay down the Side BD 873.33 from B to D, on D raise an Arch equal to the Angle 22° 30', draw out BC at length, take BC 346, and cross that Line at C, draw the Triangle BCD, and measuring the Angle at C you will find it 105° Obtuse, whose Complement to 180° being 75° is to be used in its stead.

The Work by the Logarithms finds the Angle 75°, whose Complement to 180° is 105°, for the Angle C.

As the Logarithm of 346,	2,539076
to the Sine of the Angle D 22° 30';	9,582839
So the Side 873.33,	2,941181
	12,524019
to the Sine of the Angle C 75°.	9,984943
Whose Complement 105° is the Angle C.	

#### Problem IV.

In all Plain Triangles, whether Right or Oblique-angled, Two Sides being given, with the Angle between them; to find out the other Two Angles.

This is done by the following Analogy, demonstrated in the Last Part, As the Sum of the two Sides given, to the Difference of those two Sides; so the Tangent of Half the Sum of the opposite Angles, to the Tangent of Half the Difference of these Angles.

And



And if you add together the Half-sum and half the Difference of the Angles, it makes the greater Angles, and subtrah't them, it makes the less.

*Example.*

Let there be given the Side  $CD$  717.3, the Side  $BC$  347, and the Angle  $C$  105°; to find out the Angles  $B$  and  $D$ .

By Scale and  
Compass.

1. By Scale and Compass, lay down upon Paper the Angle  $BCD$  105°, and take with your Compasses the Distances 717.3 and 347, and set them off from the Point  $C$  on either Leg to  $B$  and  $D$ , draw  $BD$ , and measuring the Angles, you will find  $B$  52°½, and  $D$  22°½.

By Logarithms.

2. By the Logarithms, the Work will stand thus:

Sum of the two Sides 1064.3, its Log.	3.027064
Difference of the Sides 370.3, its Log.	2.568554
Half the Sum of the Angles 37° 30', <i>r.</i>	9.884980
	<hr/> 12.453534
Tangent of Half the Difference 15° is	9.426470

Now, to explain this Example, the Angle given is 105° an Obtuse Angle, I subtrah't this from 180°, equal to two Right Angles, and it gives me 75° for the Sum of the Angles  $B$  and  $D$ , the Half-sum is 37° 30', and the Half-difference is found as above 15°, I add that to the Half-sum, and it makes 52° 30' for the Angle  $B$ , and then subtrah'ting 15°, the Half-sum, from 37° 30', the Half-difference, it leaves 22° 30' for the Angle  $D$ .

### Problem V.

In all Plain Triangles, whether Right or Oblique-angled, all the Three Sides being given; to find out the Cases made by the Perpendicular, falling upon any Side put for the Base, (extended if need be) and consequently all the Angles, and the Perpendicular it self.

By Scale and  
Compass.

Fig. 30.

TAKE any Side, which you please, suppose  $BD$  873.3 Yards, and lay it down with your Compasses upon the Line drawn at length, taken from your Scale, then take from that Scale  $BC$  346, and make an Arch about  $C$ ; lastly take  $CD$  717.3, and setting one Foot of your Compasses in  $D$ , cross that Arch at  $C$ , and draw  $CB$  and  $CD$ , and measuring them, you shall find  $C$  105°,  $B$  52°½, and  $D$  22°½, in all 180°. And that you may not be deceived by an impossible Question, you must be sure, that any two Sides of your Triangle be longer than the third.

But to Calculate this Problem, the Resolution whereof depends upon the the 36 Prop. 3 Euclid, it is demonstrated in Figure 30, where the Rectangle made

made of  $DB$  into  $Db$ , is equal to the Rectangle of  $DH$  into  $DG$ , that is,  
 $DB \cdot DH :: DG \cdot Db$

This premised (in that Figure) it is plain, by letting fall the Perpendicular  $CA$ , that  $Db$  is the Difference of the Cases of the Base  $DA$  and  $AD$ , and  $DG$  is the Difference of the Sides  $DC$  and  $CB$ , equal to  $CH$ ; therefore the former Proportion will stand, viz.

As the Base, or the two Cases of the Base,  $BD$ ,  
To the Sum of the Legs:  
So is the Difference of the Legs,  
To the Difference of the Cases.  
 $DH = DC - CB$   
 $GD$   
 $bD$

*Example.*

In the Triangle  $BCD$  (Figure 30) let the Sides be thus,  $BC$  346 Yards, Fig. 30.  
 $CD$  717.3 Yards,  $BD$  873.3 Yards; and let the Cases of the Base  $BA$  and  $AD$  be enquired.

First make the Terms fit for the Analogy, thus:

The Side $DC$	717.3
The Side $BC$	346
Their Sum	<hr/> 1063.3
Their Difference	371.3

Then,

As the Side $BD$ 873.3,	2.941663
to the Sum of the Sides 1063.3;	3.026655
So is the Difference 371.3,	2.569724
	<hr/> 5.596379
to the Diff. of the Cases 451.56 $bD$ .	2.654716

By Logarithms.

And  $BD$  873.3, made less by  $bD$  451.56, gives 421.74 for  $Bb$ , which divided by 2 gives 210.87 for  $BA$ , and added to  $bD$  gives 662.43: Then in the two Right-angled Triangles  $BCA$  and  $CAD$ , you have the Bases and Perpendiculars to find the Angles, and by consequence all the Angles of the Triangle  $BCD$ , with the Perpendicular  $CA$ .

The Analysis of Plain Right-angled Triangles.

Problem I. & II.

By the Hypothenuse and Angle, to find the Side.

$R \cdot S, B : BC \cdot CA$   
 $R \cdot S, C : BC \cdot BA$

N

By



By the Hypotenuse and Side, to find an Angle.

$$\begin{aligned} BC : CA &:: R : s_3B \\ BC : BA &:: R : s_3C \end{aligned}$$

By the Angle and Side, to find the Hypotenuse.

$$\begin{aligned} s_3B : R &:: CA : BC \\ s_3C : R &:: BA : BC \end{aligned}$$

#### Problem III.

By two Angles, and a Side opposite to the one, to seek the Side opposite to the other.

$$s_3D : BC :: s_3B : CD$$

By two Sides, and an Angle opposite to one, to find the Angle opposite to the other.

$$BC : s_3D :: CD : s_3B$$

#### Problem IV.

By two Sides, with the Angle between them, to find the other two Angles.

As the Sum of the Sides,

To their Difference;

So the Tangent of Half the Sum of the opposite Angles,

To the Tangent of Half the Difference.

Half the Sum added to Half the Difference is the greater Angle, and Half the Sum less by Half the Difference is the lesser.

#### Problem V.

By three Sides, to find the Angles.

As the Base,

To the Sum of the Legs;

So the Difference of the Legs,

To the Difference of the Cases of the Base.

The Base less by the Difference of the Cases divided by 2 is the lesser Segment, which added to the said Difference gives the greater.

### SECTION

### SECTION IV.

The Measuring of Distances inaccessible, of Heights, Depths, &c.

I For the Instruments for Taking of Angles for Distances, Heights, &c. there have been almost infinite sorts invented and proposed, but because they are all deduced from that of a Circle (which has been sufficiently explained already) I shall mention only those of a Circle, a Semicircle, and a Quadrant.

1. The Circle (as in Figure 1) being divided into 360 Degrees, and every Degree divided into Parts, according to the bigness of your Instrument; as little ones into Half-degrees, or 30 Minutes; greater into Quarters or 15 Minutes, or into six Parts or 10 Minutes. I say, this Circle being divided into four Quadrants, each Quadrant containing 90 Degrees, or into two Semicircles, each Semicircle containing 180 Degrees, and planted on a Three-legg'd Staff, it will take the Angles at Land: Or if it be hung on your Finger by a small Ring, as *a*, by the Index *bcd*, on which are placed two Dioptricks, or little Holes, either to look or let the Sun shine through, you may take the Angles of Heights and Depths, and the Height of the Sun and Stars.

Note, That in the last Position, care must be taken, that the Line *af* be Perpendicular, which may be tried by a small Hair and Plummert before it be used.

Note also, That for taking Angles at Land, a Semicircle according to Figure 2 will be more commodious than the whole Circle.

2. The Quadrant, or Quarter of a Circle, divided into 90 Degrees, and those subdivided as before into Parts, is the only Instrument for Heights and Depths, as Figure 3 makes plain. It is either to be fixed upon a Staff, and then it is called the Fixed Quadrant; or else it is to be held moveable in the Hand, and to play with a moving Thread and Plummert, and it is then named the Moveable Quadrant.

Note, That when you make use of the Fixt Quadrant, the Side *AB* must be truly Perpendicular, which may be tried by a Hair and Plummert, for a little deviation will cause a great Error.

Note likewise, That the Moveable Quadrant with a Pendant never needs to be regarded, in respect of the last Note; but there are two things which must be observed, lest Errors be committed; one is, that the Hair (or Silk) and Plummert may play free from touching or hanging upon the Face of the Quadrant, whilst you are trying to take the Height desired; the other, that the Line and Plummert rest quietly, to which end you may easily stay the vibrations from playing too far, and if at last some motion remain, the middle way between the Extremes may be taken.



II. The Explication of some Terms and Definitions will be needful here, *viz.*

1. The *Height*, is the Perpendicular from the Top of any Place to the Superficies of the Earth, and directs to the Center of the Earth, as CA in the Figures 4, 5, 6, 7, 8, and 9
2. The *Distance* of the Eye to the Bottom of the Height, is always Perpendicular to the Height, as BA in all the before-mentioned Figures. And other Distances, from the Eye to any part of that Perpendicular, are not so.
3. The *Angle of the Height*, is ABC, which the Line of Distance makes with the Line of Height.
4. The *Angle of the Interval* of two Places, is the Angle made by the Lines directed from the Eye to those Places.
5. An *Accessible Height*, is that which may be Mechanically Measured.
6. An *Inaccessible Height or Distance*, is that which cannot be Measured, by reason of some Impediment in the way, as Water, &c.

III. I shall now lay down the manner of Taking an Angle of Altitude three several ways, *viz.*

1. By the *Astralc*, or Whole Circle, hanging perpendicularly either upon your Finger, or upon any other thing, as a Three-legg'd Staff, or upon the Pin of a Stick stuck fast into the Ground: Turn the Plain of the Circle towards the Altitude CA, Figure 4, and directing the Sights towards C, lift them up and down, 'till through the Sights (or by them) you see the Point C, which done, you have the Arch of the Angle between the Horizontal Line SL and the *Dioptra* or Sights. Consider the Work twice, for more certainty.
2. By the *Fixed Quadrant* upon a Staff, so set in the Ground, that FB by a Plummets may be perpendicular: Turn the Sights, as was before directed, and the Angle of Height will be L<sub>o</sub>.
3. By the *Moveable Quadrant*, or that which hath a Moveable Pendulum, being either placed on a Staff or held in your Hand: Move the Quadrant so, that by the Sights B<sub>o</sub> you may perceive the Point C, the Pendulum of F playing by, but clear from the Quadrant, 'till the Plummets rest, and then you have the Arch *ef* for the Angle desired.

Much after this manner, if you lift and fit the Quadrant so, that the Sun may shine through one Sight upon the Point of the other, and the Pendulum play easily upon the Side, the Thread or Hair will shew the Height of the Sun.

And the same, or the like Work, will take the Angle of the Distance, as is visible by the Angle BCA in the Figures 7, 8, and 9.

IV. To find the Angle of the Interval, or the Distance of two Places, either by the Circle, Semicircle, or Quadrant, is very apparent, whether the Angle be Acute or Obtuse; but to do it by the Quadrant alone, will need some Directions, which take in this Example. Suppose the Angle

be Acute, as *adb* in Figure 10; plant the Side of your Quadrant *dr*, to the Mark *a*, so as the Limb may lye towards *b*, as *emt*, then looking at the Mark *b*, the Distance *tm* upon the Limb is the Angle. But if the Angle be Obtuse, as *adl*, then turn the other Side of the Quadrant *dr*, and the Limb from the Mark to *g*, and direct the Sights *dh* to C, then will *th* more 90 Degrees be the Angle desired.

Thus much premised, I come to the Problems themselves.

### Problem I.

Of these Four, the Distance to a Building, the Height thereof, the Hypotenusal Line, and the Angle; any Two being given, to find the rest.

These three are the Sides of a Right-angled Plain Triangle, as you may see in Figure 11, BA being the Distance, CA the Height, and BC the Hypotenusal Line: The Angles of which Triangle are easily found, for the Right Angle is at A, the Foot of the Building, and one of the Oblique Angles may be easily taken by a Quadrant, or the other Instruments lately described, the Observer standing either at B or C, which being known, the other Oblique Angle is the Complement thereof.

The Angles being known, and one of the Sides, the other Sides are easily found by the second and third Problems of Plain Triangles before taught, unto which I refer you, and you may find the same either by Scale and Compass or Calculation.

### Problem II.

A Part of the Distance unto a Building, Hill, or other Height, being known; to find the other Part, the Height, and the Hypotenusal Line.

One Part of the Distance suppose *bB*, the other B A, and the Height CA, together with the Hypotenusal Lines, *bC* or BC, will easily be manifested in this manner.

With your Quadrant, take the Angles at the two Stations *b* and B, *viz.* CbA and CBA. Then,

First, to do it by Scale and Compass, lay down a Line at length *bB* A, set the Distance in Yards, Perches, &c. from *b* to B, then measure out the Angles CbA and CBA, and lay them down, and mark the Place where the Lines *bC* and BC cross, as at C, letting fall the Perpendicular CA upon *bA*; then if you measure the Lines, CA will be the Height, BA the Distance, and *bC* and BC the two Hypotenusal Lines.

Secondly, by Calculation, supposing CA to be the Radius, BA will be the Tangent of the Angle BCA, (which is the Complement of the Angle



Fig. 12.

Angle CBA,) and  $bA$  will be the Tangent of the Angle  $bCA$ , (the Complement of the Angle  $CbA$ ;) and  $bB$  will be the Difference of these Tangents. Take therefore these Tangents out of the Table of Natural Tangents, and find their Difference, by subtracting the lesser out of the greater; which being done, first for the Distance  $bA$ , say, *As* the Tangent of  $bCA$  less by the Tangent  $BCA$ , *to* the Tangent of  $BCA$ ; *so* is  $bB$ , *to*  $bA$ .

Then, for the Height  $CA$ , say, *As* the Tangent of  $bCA$  less by the Tangent  $BCA$ , *to* the Radius; *so* is  $bB$ , *to*  $CA$ .

And lastly, for the Angles, subtract the Angle  $CBA$  out of  $180^\circ$ , and it gives the Angle  $bBC$ ; subtract also the Angle  $CbB$  out of  $CBA$ , and it will give the Angle  $bCB$ ; because the Outward Angle  $CBA$ , is equal to  $CbB$  and  $CBA$ , the two Inward and Opposite Angles.

And thus you have all the Angles of the Triangle  $bCB$ , and the Side  $bB$ , whereby either of the Hypothensal Lines,  $bC$  or  $BC$ , may be found out by the third Problem of Plain Triangles.

## Problem III.

*To take the Height of any Thing above us, removed at a competent distance, as of a Cloud, or the like.*

Fig. 13.

1. **I**F two Stations can be had of the same side of the Thing above us, then the Height is found out the very same way, that the Height  $CA$  is found out in the last Problem. Suppose, in Figure 13, that the Thing above us were  $C$ , and the Angles were taken at the two Stations  $b$  and  $B$ , and the Distance of the Stations measured were the Space  $bB$ , then the Perpendicular Height  $CA$  will be found, as the Height  $CA$  in the Problem aforesaid.

2. But if one Station be on one side of the Thing whose Height is to be taken, and the other Station on the other side, as the Stations  $B$  and  $D$ , then the Tangents of the Angles  $BCA$ , and  $DCA$ , are to be added together, the Analogy for the Perpendicular Height being this, *As* the Sum of the Natural Tangents,  $BCA$  and  $DCA$ , *to* the Radius; *so* is  $BD$ , *to*  $CA$ .

3. But seeing that two such Observations, at several Stations, can scarcely be had for measuring the Height of a Cloud, although the diligence of two Observers were very great, it will not be amiss to shew, how one Observer may supply the place of two, and take the Angles of the Cloud's Altitude for two Stations at the same time, he standing but at one; which is done by this Artifice:

When the Sun shineth, let the Mesurer make choice of a fit Cloud for his purpose, and let him mark the Place upon the Earth where the Shadow of the Cloud falleth; then being removed a convenient Distance from the Place of the Shadow, let him with a Quadrant take the Angle of the Height

of

of the Cloud, and also of the Height of the Sun, which Angle of the Height of the Sun is the Angle of the Cloud's Height in the Place where the Shadow falleth; for if another Observer should stand at the Place of the Shadow, both the Cloud and the Sun to him would have the same Angle of Height. All which may be manifestly seen in Figure 13.

For let  $S$  be the Sun,  $C$  the Cloud,  $b$  the Shadow of the Cloud upon the Earth, and  $B$  the Station of the Observer, where if he take the Angle  $CBA$ , of the Clouds Height, for the Station  $B$ , and the Angle of the Sun's Height at the same time; he taketh also the Angle  $CbA$  of the Clouds Altitude at the Station  $b$ ; the Angle  $SbA$  being equal to the Angle  $CbA$ , and  $b, C$ , and  $S$ , being in a Right Line.

Note, That by the Sun's Height, especially at 45 Degrees, when the Shadow is equal to the Height required, then may be taken the Height by that Shadow, by measuring it accordingly.

## Problem IV.

*A Part of the Height of any Building, or Upright Thing, being known, to find the other Part, and so the whole Height, together with the Distance and Hypothensal Line.*

**I**F you invert Figure 12, belonging to the second Problem, so that  $bA$  Fig. 12. be the Height of the Building,  $bB$  the Part of the Height known, and  $CA$  the Distance, then the Calculation will be the same with that of the said Problem.

## Problem V.

*To find the Distance from the Observer unto a Mark inaccessible.*

**L**et the Place of the Observer be at  $B$ , and let the Distance betwixt  $B$  Fig. 13 and the Mark  $C$  be required. First, from  $B$  side-wise chase another Mark or Station at  $D$ , the further the better, and there set a Beacon. Then,

1. With your Quadrant, or Semicircle, take the Angle  $CBD$ .
2. Measure the Distance  $BD$  in Yards, Perches, &c.
3. Standing at  $D$ , take the Angle  $EDC$ .

By Scale and Compass, if you lay down the Line  $BD$ , and set off the Angles at  $B$  and  $D$ , it will find the Point  $C$ , and give the Distance  $BC$  on the same Scale.

4. Add together the Angles  $B$  and  $D$ , and subtract their Sum from  $180^\circ$ , and the Remainder will be the Angle at  $C$ . Say then, by the Analogy of the third Problem of Plain Triangles, *As* the Sine of  $C$ , *to* the Side  $bD$ ; *so* is the Sine of  $D$ , *to* the Side  $BC$ .

## Problem



## Problem VI.

To find the Distances between any Two Places, both removed from the Observer.

Fig. 15.

Let the two Places be B and D, and let their Distance be required by an Observer standing at the Point C.

1. Let the Angle BCG be taken, between one of the Places, as B, and any visible Mark, suppose G or F, standing about the middle of the Distance; and likewise let the Angle GCD be taken, between the said Marks G or F, and the other of the Places, D.

2. Then leaving a visible Mark at C, let the Observer go backwards unto another Station, as at H, in such manner, as that he being at H, may see the Marks C and G, or F, in a Right Line; and let him measure the Distance between the two Stations C and H.

3. At H let him take the Angles BHG, and GHD, as he did before at C.

This being done, in the Triangle HBC, because the outward Angle BCG is equal to both the inward and opposite Angles BHC and HBC, therefore by subtracting BHC out of BCG, there will remain the Angle HBC. Thus all the Angles in the Triangle HBC, and the Side HC, being given, either of the other two Sides are easily found by the third Problem of Plain Triangles.

Again, in the Triangle HDC, the Angle HDC, and either of the Sides CD or HD, may be found in the same manner.

Lastly, in the Triangle BCD, the two Sides BC and DC being found, (as is already taught) and the Angle BCD, by Observation, the other two Angles CBD and CDB, may be found by the fourth Problem of Plain Triangles, and consequently the Side BD by the third Problem of Plain Triangles, which is the Distance required.

The same also may be had in like manner, by the Sides BH and DH, with the Angle BHD, in the Triangle BHE.

Another way of Resolving the Problem.

Fig. 16.

In Figure 16, let B and D be the two Places, and let their Distance be required by an Observer standing at the Point C.

1. At C let the Angle BCD be taken between the two Places, and also the Angle DCG, between the Place D and a visible Mark F or G, on the side of the Observer, the Sum of which two Angles is the Angle BCG, which for more proof may likewise be taken by the Instrument.

2. Then let the Observer go towards the Mark F as to G in a Right Line, which is easily done at Sea by help of the Compass, and at Land, by looking from C, so that G be in a Right Line from it to F; let him measure also the Distance CG, which at Sea is done by help of the Log-line.

3. At

3. At G let the Observer take the Angle again between both Places, the Angle BGD, and also the Angle GDF, the Sum of which two Angles is the BGF, which may also be taken by the Instrument, for the better satisfaction of the Observer.

Then in the Triangle BCG, because the outward Angle BGF is equal to both the inward and opposite Angles BCG and CBG, therefore by subtracting DCG out of DGF, there will remain the CBG; by which Angle CBG, and the Side CG found by Measure, and the Angle BCG, the side BG is found by the third Problem of Plain Triangles.

Again, in the Triangle CDG, because the outward Angle DGF is equal to both the inward and opposite Angles DCG and CDG, therefore by subtracting DCG from DGF, there will remain the Angle CDG, by which Angle CDG, and the Side CG, and the Angle CDG, the Side DG is found by the Problem aforesaid.

Lastly, in the Triangle BGD, the two Sides BG and DG, being found, as hath been taught, and the Angle BGD by Observation, the other two angles, GBC and BDG, may be found by the fourth Problem of Plain Triangles, and consequently the Side BD by the third Problem of Plain Triangles, which is the Distance required.

Note, in taking Distances, 1. That the two Stations be at as great Distances, as conveniently may be.

2. That the Side Station is much more convenient than directly in a Line.

Note, in measuring Altitudes, That you be not too near, nor yet too far off, but if it may be, chuse the Place where the Angle of the Altitude will be  $45^\circ$ , or near unto it, for thereabouts will be the most sensible alteration of the Angle at C.

## Problem VII.

Of Levelling, or Measuring the Inequality of Places, as to their Heights.

To find out the Difference of Heights of one Place from another, in the Rising and Falling, which is of constant use in conveying of Water, either above the Ground for Fountains, &c. or under the Ground for Adyts or Soughs, &c. let your Instrument be carefully made, whether it be a Quadrant, Water-level, or any other; the best I account to be a Brafs T, the Sights upon the Top of the T to be Perspective Glasses, which must be tried before used, and the Glasses are to stand always one way. This will endure longer Stations than ordinary, and is for many Reasons the best, if substantially made, and there must be two Mark-boards placed upon Quarter-Pikes, that your Assistants may lift them higher or lower, as they shall be directed.

Then let the Level as near as you can betwixt the two Marks with your Assistants hold upright in their hands, with the slipping Marks; turning to  
O  
one,



one, cause him to hold or set the Slit and black Stroke even with the Level-Sights, and so the other. The Difference of these Sights, in Inches and Tenth Parts, gives the Ascend or Defcent, and this is for one simple Station; but if it require both Ascents and Defcents, then in a Note-book set down your Back-stations in one Column, and your Fore-stations in another; sum up both the Columns, and take the Difference of them, if they be equal, the two Places are level, if your Fore-stations exceed, the Difference is lower, if otherwise higher, an example will clear all.

Fig 17.

I am to give the Difference of the Heights of the Places A and B, from the Line of Level SB, choosing my first Station at C, where I plant my Instrument, betwixt the Quarter Pikes A and E, and setting my Level firm, the Assistants lifting up and down the Mark-boards, 'till both ways the Sights take the black Strokes at D and E; in a little Table made set down the Heights of those Strokes from the Ground, in two Columns, one for the Left-hand Height, the other for the Right, as you see in the Table adjoining, wherein AD (for the Left-hand) is found to be 3 Feet, 3 Inches, and  $\frac{2}{5}$  of an Inch, and EF (for the Right-hand) 7 Feet, 1.5 Inches. Again, let the second Station be at G, and the Left-hand Height FH be 10 Feet, 3 Inches, and a Half, and the Right-hand Height IK 3 Feet, 3.7 Inches. Again, the third Station let be at M, and the Heights be IL 2 Feet, 9.4 Inches, and ON 12 Feet, 1.5 Inches. Lastly, let the fourth Station be at P, and the Heights OQ 3 Feet, 10.9 Inches, and BR 11 Feet, 9.8 Inches. The Sum of the Heights on the Left-hand is 21 Feet and 3 Inches, that of those on the Right 34 Feet and 4.5 Inches; their Difference is 13 Feet and 1.5 Inches, and so much is B lower than A.

Stations.	Heights on the Left-hand.		Heights on the Right-hand	
	Feet.	In.	Feet.	In.
1	4	3.2	7	1.5
2	10	3.5	3	3.7
3	2	9.4	12	1.5
4	2	10.9	11	9.8
	21	3.0	34	4.5

Sum of the Heights on the Right-hand 34 4.5

Sum of the Heights on the Left-hand 21 3

Their Difference 13 1.5

Which is the Difference of the Height that B is lower than A.

Problem

### Problem VIII.

*Of Taking the Plot of a Country, City, Bay, or Harbour, or such like Place.*

**T**His Proposition finds the Proportional Distances of divers Objects, (which one would represent and lay down) which is done by two or more Stations, at every one whereof are formed many Triangles, whereof a Side and two Angles are always given, which sufficeth to find out the Distances, both to and betwixt any Places propofed.

For Example, suppose it were required to represent in Proportion the Objects A, B, C, D, E, F, I, K, L. To do which, I take two Stations A and B, so that the Distance betwixt them may be actually measured by Feet, Fathoms, or Perches, upon the Ground, suppose 350 Perches, which set down in your Note, and so, that A and B be taken long enough to make a Common Base, fit for all the Triangles enquired after. First then, placing your Instrument (whether it be a Semicircle, Quadrant, or Circle) upon A, direct the Beginning of the Division upon the Line AB, where by the Skrew or other means fix the Instrument fast, that it may not turn; then begin and take the several Angles BAL, BAK, BAF, BAI, BAE, BAD, and BAC, which set down upon your Note one after another. Secondly, removing your Instrument to B, set the Beginning of the Degrees upon B, and take the Angles ABC, ABD, ABE, ABI, ABF, ABK, and ABL, which set down likewise upon your Note. Then having a clean Sheet of Paper, and having by you a convenient Scale, Line of Chords, Circle, or Protractor, draw a Line below upon the Sheet, as you see *ab*, and from the Scale take 350 Perches, and set it from *a* to find the Point *b*, so is *ab* the Stationary Line whereon the Angles are to be placed, thus, upon *a* from the Line *ab* set off the Angles *bal*, *bak*, *baf*, *bai*, *bac*, *bad*, and *bac*, and upon *b* from the Line *ba* set off the Angles *abc*, *abd*, *abe*, *abi*, *abt*, *abk*, *abl*: So upon the Paper, you have the true Proportional Places at *c*, *d*, *e*, *f*, *i*, *k*, *l*, answerable to the Places upon the Country, C, D, E, F, I, K, L; and by a Pair of Compasses, and the same Scale of Perches that you set off *ab* 350 Perches, you may measure the Distances from *a*, or *b*, to any of the aforesaid Places, and the Distances of one Place from another, as from *c* to *d*, from *i* to *l*, from *e* to *k*, &c. And if you were to describe more of a Country, beyond these Places, from any two Places, as from *c* and *g*, which you may make your Stationary Line, first from one, as at *c*, draw Lines to these new Places, and then intersect them again from *g*, and you may accomplish your desire.

After this manner, you may describe the Plain of any City, or other Place whatsoever.





## CHAP. IV.

# Of Spherical TRIGONOMETRY, or the Calculation of Spherical Triangles.

## SECTION I.

**Y**ou, that desire to be Calculators of *Spherical Triangles*, ought to have some competent Knowledge in the Circles of the Sphere or Globe, which will be sufficiently explained in the next Chapter, without which, it is impossible you should do much in this Doctrin, therefore in this place I will touch only such things, more nearly concerning *Trigonometry* it self in *Sphericals*: And then after the perusal of the next Chapter, you will perceive the Uses and Advantages of this Doctrin.

I. You were taught some Definitions, concerning both Plain and Spherical Triangles together, in the Eight first Propositions of the First Section of *Plain Triangles*; you must know further, That the Sides of *Spherical Triangles* are the Arches of a Great Circle of the Sphere or Globe, every one of those Sides being severally less than a Semicircle.

II. A Great Circle is that which divideth the Sphere or Globe into two Equal Parts, so that it is distant from its Poles every where by a Quadrant, or a Quarter of a Circle; such are the *Horizon*, the *Meridian*, the *Equinoctial*, the *Ecliptick*, &c. on the Globe.

III. You were taught before in *Plain Trigonometry*, That the Measure of a Plain Right-lined Angle, was so much, as the Degrees and Parts of a Circle described upon that Angular Point on a Plane, and intercepted betwixt the Sides of the Angle, would come to. But these Spherical Angles described naturally upon the Globe, and intercepted by two Parts of Great Circles, between the Sides of the Angle drawn forth unto Quadrants, are measured by an Arch of a Great Circle described upon the Angular Point on the Globe or Sphere.

IV. If

IV. If a Great Circle pass through the Poles of another Great Circle, it intersecteth it by Right Angles.

V. A Spherical Triangle, is either *Quadrantal*, or not *Quadrantal*.

VI. A *Quadrantal* is that which hath one Side, or Angle, at the least equal to a Quadrant, and is either *Manifold*, or *Single*.

VII. A *Manifold Quadrantal*, hath either three Right Angles and three Sides equal to Quadrants, or two Right Angles, with the two Sides opposite to those Angles, Quadrants. But of these two last we will not treat, as little to our purpose. Only of.

VIII. A *Single Quadrantal*, which hath one Side only a Quadrant, or one Angle only equal to a Quadrant.

IX. Every *Single Right-angled Spherical Triangle*, hath annexed to it a *Single Quadrantal*, whose Parts agree with the Parts of the *Right-angled Triangle*.

X. A *Single Right-angled Triangle*, hath either two *Acute Angles*, or two *Obtuse Angles*; or lastly, one *Acute*, and the other *Obtuse*.

XI. A *Right-angled Spherical Triangle*, having two *Acute Angles*, hath all its Sides severally less than Quadrants.

XII. A *Right-angled Spherical Triangle*, having two *Obtuse Angles*, hath also two Sides opposing them, greater than Quadrants, and the third Side opposite to the Right Angle lesser than a Quadrant.

XIII. A *Right-angled Spherical Triangle*, having an *Acute* and an *Obtuse Angle*, hath the Side subtending the *Acute Angle* lesser than a Quadrant, and the other two Sides greater than Quadrants.

XIV. A *Spherical Triangle*, not *Quadrantal*, is that which hath none of its Sides a Quadrant, nor any one of its Angles equal to a Quadrant; and this is commonly called an *Oblique-angled Spherical Triangle*.

XV. An *Oblique-angled Spherical Triangle*, either consists of pure *Acute* or *Obtuse Angles*, or of them mixed together.

XVI. In *Obtuse-angled Spherical Triangles*, the Angle that is nearest in Quantity to a Quadrant, and the Side subtending it, are doubtful, whether they be of the same, or divers kinds, except the Accompt or Position declare the same.

XVII. The



XVII. The other two Angles, not so near Quadrants, are always of the same kind with the Sides subtending them; therefore of what kind the one is, it appeareth also of what kind the other is.

XVIII. If any Angle of a Triangle be nearer a Quadrant than the Side subtending it, two Sides thereof shall be of one kind, and the third lesser than a Quadrant.

XIX. But if any Side of a Triangle be nearer a Quadrant than the Angle subtended thereby, two Angles thereof shall be of the same kind, and the third greater than a Quadrant.

## SECTION II.

**H**itherto of the Kinds and Affections of Spherical Triangles, I will now come nearer to their Calculation, which is nothing else, but the finding out of an unknown Part from three given, by help of the *Golden Rule of Proportion*.

I shewed you before, how the Four Terms of a Proportion may be altered, and how any of the Terms may be put in the last Place, which is of that consequence, that I think fit to set it down again; as suppose this Proportion were given, *As the Tangent of one Extream, to the Sine of the Mean; so is the Radius, to the Tangent of the other Extream*; and marked with these Letters,  $A : B :: a : b$  This Proportion may be varied thus,  $B : A :: b : a$  Or,  $a : b :: A : B$  Or,  $b : a :: B : A$

And it matters not how the Middle Terms stand.

The Spherical Triangles to be thus Calculated, are only the Single Quadrantal, and the Not Quadrantal, or Oblique.

All Spherical Triangles are Calculated by the help of Four Axioms, and by continuing the Parts to Quadrants, which being demonstrated in many Books, I will not now trouble you with more than the naming them.

*Axiom I.* In all Spherical Triangles, whether Quadrantal or no, the Sines of the Sides are proportional to the Sines of their opposite Angles.

*Axiom II.* In all Right-angled Spherical Triangles, having the same Right Angle at the Base, the Sines of the Hypotenuses and Perpendiculars are proportional.

*Axiom III.* In all Right-angled Spherical Triangles, the Sines of the Bases, and the Tangents of the Perpendiculars, are proportional.

*Axiom*

*Axiom IV.* In all Spherical Triangles, either Right or Oblique-angled, one side being made the Base,

*As the Tangent of Half the Sum of the Cases of the Base,*

*To the Tangent of Half the Sum of the Legs;*

*So the Tangent of Half the Difference of the Legs,*

*To the Tangent of Half the Difference of the Cases.*



## SECTION III.

Spherical Triangles, of what Nature soever, are Calculated by the foregoing Axioms, only that Case, where Three sides are given to find an Angle, which I will deliver apart.

I shall first begin with Right-angled Spherical Triangles, or Quadrantals, and follow the Method of the Circular Parts invented by the Lord *Neper*, and then deliver the Cases, and Varieties, with Examples.

1. There are six Parts in every single Quadrantal, whereof one only is equal to a Quadrantal (and that is quite left out, as being always known) and the other five not Quadrants are only taken notice of.

2. Of these five Parts, three are always Ingredients into the Question; and therefore in a Right-angled Spherical Triangle, marked as you did the Plain one, *viz.* A the Right-angle, B A the Base, C A the Perpendicular, B C the Hypotenuse, B the Angle at the Base, and C the Angle at the Perpendicular, and in a moment you may learn the Parts, by but naming the Letters, and viewing of Figure 1. All which are in the first place distinguished by the immediate Sequency (or following) of the Parts, or the Not-sequency of them.

3. The immediate Sequency is not hindered by the Part equal to a Quadrant, (for as before that is not to be regarded) therefore in the Spherical Triangle ABC, Right-angled at A, these three, B A, C A, C, are said to follow one another immediately, notwithstanding the Right Angle at A; so in the Spherical Triangle B C E, having B E a Quadrant, these Parts, E, B, and B C, are said to follow one another, notwithstanding the Quadrant Arch B E.

4. Take notice, that in this way the Sides B A and C A, next the Right Angle, are taken simply, that is to say, these two Parts are not changed; but the Angles B and C, and the Hypotenuse B C, are taken by their Complements, (or Difference to a Right Angle) and these makes three Parts more, five in all. Of these five (as before) three are at once Ingredients, whereof two are given, and one demanded, and are to be considered, whether they all follow one another and fall together; as (1.) B, B A, and A C; or (2.) B A, A C, and C; or (3.) C A, C, and B C; or (4.) C, B C, and B; or (5.) B C, B, and B A; being five in Number, according to the Parts, wherein B A, A C, C, B C, and B, are the Means, and the other two the Extremes.

Or they fall to be separated, a funder, or disjunct, *viz.* two are absolutely removed from the third, which is to be accounted the Intermedial; as if I account

*Resolution of Right-angled Spherical Triangles.*

Fig. 1.

Fig. 1.

Fig. 1.



count BA the Intermedial, then is C and BC the Opposites; if C the Intermedial, then is B and BA the Opposites; if BC, then is BA and CA Opposites; if B be an Intermedial, then is CA and C the Opposites. And this is very well expressed by Dr Newton, in his *Geometrical Trigonometry*, by this Table.

Mid. Part.	Extreams.		Opposites.	
BA	B	CA	C	BC
CA	B	A	C	BC
C	CA	BC	B	BA
BC	C	B	B	BA
B	BC	BA	CA	C

Where the first Column is to be accounted the *Means*, or *Middle Parts*, the second the *Extreams* conjunct, and the third is the *Opposites*, or *Extreams* disjunct.

Out of the former Axioms are gathered these two Rules:

Rule 1.

As the Radius,  
To the Tangent of one of the Extreams conjunct ::  
So the Tangent of the other Extream conjunct,  
To the Sine of the middle part.

Rule 2.

As the Radius,  
To the Co-sine of one of the Extreams disjunct ::  
So the Co-sine of the other Extream disjunct,  
To the Sine of the middle part.

Therefore if the Intermedial (or middle part) be sought, the Radius must be in the first place, if either of the Extreams, the other Extream must be in the first place.

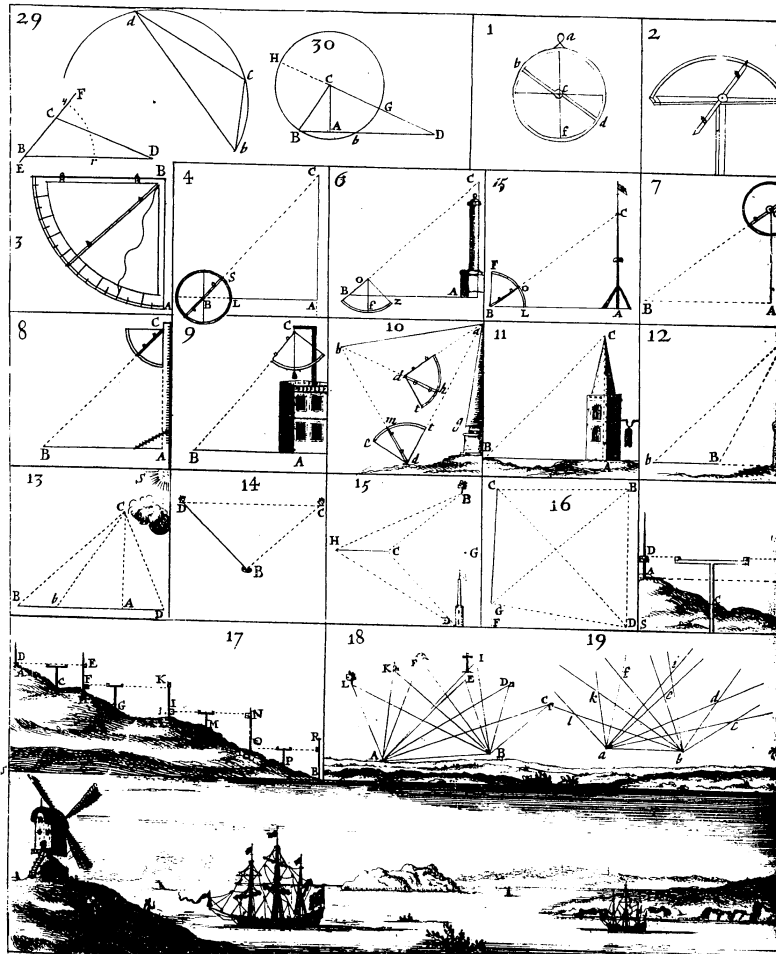
Only Note, That if the Intermedial (or middle part) or either of the Extreams adjacent, or (conjunct) be noted with *Comp.* in the Circular parts of the Triangle, instead of the Sine or Tangent, you must use the Co-sine, or Co-Tangent of such part or parts.

If either of the Opposite Extreams (or Disjunct) be noted with its *Comp.* instead of the Co sine, you must use the Sine of such Extream.

As for Example, In Figure 1, if the Angle at B be  $23^{\circ} 30'$ , (the Angle of the Ecliptick and Equinoctial) and B C a part of the Ecliptick  $34^{\circ} 40'$ , and C A the Declination be required. I consider the three Ingredients, which are B, B C, and C A, and find B and B C to be removed from B A, therefore B A is the Middle Part, and B and B C are the Opposites disjoyned; and then, by the second Rule, As the Radius, so the Co-sine B C; so the Co-sine B, so the Sine C A: But you are bid to take the Complements of B and B C; therefore, as in the following Work,

$$\text{As Radius} \cdot \text{fi. BC} :: \text{fi. B} \cdot \text{fi. BA}$$

As





As Radius,	10,000000
to Sine BC $34^{\circ} 40'$ :	9,754960
So Sine B $23^{\circ} 30'$ ,	9,600699
to Sine CA $13^{\circ} 7'$ .	9,355659

Suppose BC  $34^{\circ} 40'$ , or to be  $4^{\circ} 40'$  of  $\pi$ , and B to be the Angle of the greatest Declination  $23^{\circ} 30'$ , I add BC and B, and it makes 19,355659, from which I take the Radius, and it leaves 9,355659, the Sine of  $13^{\circ} 7'$ .

This would be sufficient, but that I am resolv'd to be plain, and to make all easie, and therefore I will set down Rules and Examples in all the Sixteen Cases of Right-angled Spherical Triangles, taken from the former Directions, which will be sufficient for the young Practitioner, 'till he be able fully to understand what goes before. Therefore for the Resolution of all these sort of Right-angled Triangles take notice, that for the *Data*, or Things given, there can be but six sorts, *viz.*

I. The Hypothenufe and a Side given: 1. To find an Angle opposite. 2. The other Side. And 3. The Angle comprehended.

II. The Hypothenufe and Angle adjoining being given: 1. To find the Side opposite to the Angle. 2. The Side adjoining to the Angle. 3. The other Angle.

III. By a Side, and the Angle opposite to it, given: To find, 1. The Hypothenufe. 2. The other Angle. 3. The other Side.

IV. By a Side, and the Angle adjoining, given: To find, 1. The other Angle. 2. The other Side. 3. The Hypothenufe.

V. By both the Sides given: To find, 1. The Hypothenufe. 2. Either Oblique Angle.

VI. By both Angles given: To find, 1. The Hypothenufe. 2. Either of the two Sides.

Therefore when any Question is propos'd in Right-angled Spherical Triangles, it will fall upon some of these Six Propositions, and the *Data* (which must be two) to seek a Triplicity in the four first Propositions, and a Duplicity in the two last, which makes in all Sixteen Cases. Therefore suppose the Triangle ABC, Figure 2, were propos'd, where let B represent the Equinoctial Point, or Angle made betwixt the Equinoctial and Ecliptick,  $23^{\circ} 30'$ , and let BC be a Part of the Ecliptick  $34^{\circ}$  and  $40'$ , or the  $4^{\circ}$  and  $40'$  of *Taurus*; let BA be the Right Ascension of the Sun  $32^{\circ} 23'$ , CA the Declination  $13^{\circ} 7'$ , and C the Interfection of the Ecliptick and Meridian  $70^{\circ} 19'$ . Now if any two of these be given to find the rest, you may by the former six Propositions, and these following Cases, resolve them and the like with much ease.



Prop. I. By the Hypothenuse and Side given,

1. To find an Angle opposite.	<i>Example.</i>	
Given $\begin{cases} BC, \\ CA. \end{cases}$ Sought B.	From R and <i>fi.</i> of CA $13^{\circ} 7'$	19,355659
<i>Rule.</i>	Take <i>fi.</i> BC $34^{\circ} 40'$	9,754960
<i>Si.</i> BC . <i>fi.</i> CA :: R . <i>fi.</i> B	Refts <i>fi.</i> of B $23^{\circ} 30'$	9,600699
2. To find the other Side.	<i>Example.</i>	
Given $\begin{cases} BC, \\ CA. \end{cases}$ Sought BA.	From R and <i>co-fi.</i> BC $34^{\circ} 40'$	19,915122
<i>Rule.</i>	Take <i>co-fi.</i> CA $13^{\circ} 7'$	9,988519
<i>Co-fi.</i> CA . <i>co-fi.</i> BC :: R . <i>co-fi.</i> BA	Refts <i>co-fi.</i> BA $32^{\circ} 23'$	9,926605
3. To find the Angle comprehended.	<i>Example.</i>	
Given $\begin{cases} BC, \\ CA. \end{cases}$ Sought C.	From R and <i>t.</i> CA $13^{\circ} 7'$	19,367382
<i>Rule.</i>	Take <i>t.</i> of BC $34^{\circ} 40'$	9,839837
<i>Tan.</i> BC . <i>t.</i> CA :: R . <i>co-fi.</i> C	Refts <i>co-fi.</i> C $70^{\circ} 19'$	9,527545

Prop. II. By the Hypothenuse and Angle adjoining,

1. To find the Side opposite to the Angle.	<i>Example.</i>	
Given $\begin{cases} BC, \\ B. \end{cases}$ Sought CA.	To Sine BC $34^{\circ} 40'$	9,754960
<i>Rule.</i>	Add the Sine B $23^{\circ} 30'$	9,600699
R . <i>fi.</i> BC :: <i>fi.</i> B . <i>fi.</i> CA	Refts the Sine CA $13^{\circ} 7'$	9,355659
2. To find the Side adjoining to the Angle.	<i>Example.</i>	
Given $\begin{cases} BC, \\ B. \end{cases}$ Sought BA.	From R and <i>co-t.</i> BC $34^{\circ} 40'$	20,160162
<i>Rule.</i>	Take <i>co-fi.</i> B $23^{\circ} 30'$	9,962398
<i>Co-fi.</i> B . R :: <i>co-t.</i> . <i>co-t.</i> BA	Refts <i>co-t.</i> BA $32^{\circ} 23'$	10,197764
3. To find the Angle adjoining to the other.	<i>Example.</i>	
Given $\begin{cases} BC, \\ B. \end{cases}$ Sought C.	To <i>co-fi.</i> BC $34^{\circ} 40'$	9,915122
<i>Rule.</i>	Add the Tangent of B $23^{\circ} 30'$	9,638302
R . <i>co-fi.</i> BC :: <i>t.</i> B . <i>co-t.</i> C	Refts <i>co-t.</i> C $70^{\circ} 19'$	9,553424

Prop.

Prop. III. By a Side and Angle opposite,

1. To find the Hypothenuse.	<i>Example.</i>	
Given $\begin{cases} CA, \\ B. \end{cases}$ Sought BC.	From R and <i>fi.</i> CA $13^{\circ} 7'$	19,355659
<i>Rule.</i>	Take <i>fi.</i> B $23^{\circ} 30'$	9,600699
As <i>fi.</i> B . <i>fi.</i> CA :: R . <i>fi.</i> BC	Remains <i>fi.</i> B C $34^{\circ} 40'$	9,754960
2. To find the other Angle.	<i>Example.</i>	
Given $\begin{cases} CA, \\ B. \end{cases}$ Sought C.	From R and <i>co-fi.</i> B $23^{\circ} 30'$	19,962398
<i>Rule.</i>	Take <i>co-fi.</i> CA $13^{\circ} 7'$	9,988519
<i>Co-fi.</i> CA . <i>co-fi.</i> B :: R . <i>fi.</i> C	Remains <i>fi.</i> C $70^{\circ} 19'$	9,973879
3. To find the other Side.	<i>Example.</i>	
Given $\begin{cases} CA, \\ B. \end{cases}$ Sought BA.	From R and <i>t.</i> CA $13^{\circ} 7'$	19,367382
<i>Rule.</i>	Take the <i>t.</i> of B $23^{\circ} 30'$	9,638302
<i>Tan.</i> B . <i>t.</i> CA :: R . <i>fi.</i> BA	Refts the <i>fi.</i> of BA $32^{\circ} 23'$	9,729080

Prop. IV. By a Side and an Angle adjoining,

1. To find the other Angle.	<i>Example.</i>	
Given $\begin{cases} BA, \\ B. \end{cases}$ Sought C.	Add the <i>fi.</i> of B $23^{\circ} 30'$	9,600699
<i>Rule.</i>	To <i>co-fi.</i> BA $32^{\circ} 23'$	9,926591
R . <i>fi.</i> B :: <i>co-fi.</i> BA . <i>co-fi.</i> C	Refts <i>co-fi.</i> C $70^{\circ} 19'$	9,527290
2. To find the other Side.	<i>Example.</i>	
Given $\begin{cases} BA, \\ B. \end{cases}$ Sought CA.	Add <i>fi.</i> BA $32^{\circ} 23'$	9,728825
<i>Rule.</i>	To <i>t.</i> B $23^{\circ} 30'$	9,638302
R . <i>fi.</i> BA :: <i>t.</i> B . <i>t.</i> CA	Reft <i>t.</i> CA $13^{\circ} 7'$	9,367127
3. To find the Hypothenuse.	<i>Example.</i>	
Given $\begin{cases} BA, \\ B. \end{cases}$ Sought BC.	Add <i>co-t.</i> BA $32^{\circ} 23'$	10,197766
<i>Rule.</i>	To <i>co-fi.</i> B $23^{\circ} 30'$	9,962398
R . <i>co-t.</i> BA :: <i>co-fi.</i> B . <i>co-t.</i> BC	Refts <i>co-t.</i> BC $34^{\circ} 40'$	9,160164

P 2

Prop.



Prop. V. *By both the Sides,*

1. To find the Hypothenufe.		<i>Example.</i>	
Given $\begin{cases} B A, \\ C A. \end{cases}$	Sought B C.	Add co-fi. B A $32^{\circ} 23'$	9,926591
		To co-fi. C A $13^{\circ} 7'$	9,988519
<i>Rule.</i>			
R. co-fi. B A :: co-fi. C A . co-fi. B C.		Refts co-fi. B C $34^{\circ} 40'$	9,915110
2. To find either of the Angles.		<i>Example.</i>	
Given $\begin{cases} B A, \\ C A. \end{cases}$	Sought B.	From R and t. C A $13^{\circ} 7'$	19,367382
		Take the fi. B A $32^{\circ} 23'$	9,728825
<i>Rule.</i>			
Si. B A . t. C A :: R . t. B.		Refts t. B $23^{\circ} 30'$	9,638557

Prop. VI. *By both the Angles,*

1. To find the Hypothenufe.		<i>Example.</i>	
Given $\begin{cases} B, \\ C. \end{cases}$	Sought B C.	From R and co-t. C $70^{\circ} 19'$	19,553547
		Take t. B $23^{\circ} 30'$	9,638302
<i>Rule.</i>			
Tan. B . R :: co-t. C . co-fi. B C.		Refts co-fi. B C $34^{\circ} 40'$	9,915245
2. To find a Side.		<i>Example.</i>	
Given $\begin{cases} B, \\ C. \end{cases}$	Sought C A.	From R and co-fi. B $23^{\circ} 30'$	19,962398
		Take fi. C $70^{\circ} 19'$	9,913852
<i>Rule.</i>			
As fi. C . co-fi. B :: R . co-fi. C A.		Refts co-fi. C A $13^{\circ} 7'$	9,988546

Thus by six Propositions of two Parts given, you may find any Part in a Right Angled Spherical Triangle of any of the sixteen Cases, with much ease and clearness.

*For Example.*

If a Question were given where the Hypothenufe was  $30^{\circ}$ , and one of the Sides or Base  $27^{\circ} 54'$  (for you may account either Side for the Base) to find out the Angle comprehended betwixt them. First draw the form of a Triangle, as in Fig. 3, mark the *Data* by a small Line, and the Part sought by a Cypher placed upon it; then seeking which of the six Proportions the *Data* will relate to, you will find it *Prop. 1.* and *Case 3.* and the Rule to be, As Tang. B C . Tang. B A :: R . co-fi. B. which you may work as by the Example following,

From Radius, and Tangent B A $27^{\circ} 54'$	19,723844
Take the Tangent B C $30^{\circ} 00'$	9,761439
Refts Co-sine B $23^{\circ} 30'$ (the Angle sought)	9,962405

Lastly to finish the Doctrine of *Right-angled Triangles*, certain Cautions are to be given and observed, as follow.

First, That if the Angle sought for, be Acute, then the Sine or Tangent thereof represents it truly; but if it be Obtuse, then you must take it from  $180^{\circ}$ , and the Remainder is the Angle: Which must be observed in all, the Reason being, that to every Sine and Tangent a double Angle is answerable, one Acute, the other Obtuse. And the same Rule serves for the Sides likewise, by the like Reason.

Secondly, For knowing whether the Angles sought for be Acute or Obtuse, or whether the Sides sought be greater or lesser than  $180^{\circ}$  Degrees, observe the following Rules, appropriate to the 6 Propositions and 16 Varieties, as they have been before taught, and there set down.

I. In *Prop. I. Variety 1.* you shall know, whether the Angle sought be Acute or Obtuse; for if the Side given be less than a Quadrant, then the Angle sought will be Acute; if otherwise, Obtuse.

II. In *Prop. I. Var. 2.* the sought Side will be less than a Quadrant, if the Hypothenufe and the Side given are less than Quadrants; but it shall be greater than a Quadrant, if the Hypothenufe be greater than a Quadrant.

III. In *Prop. I. Var. 3.* the Angle sought will be found Acute or Obtuse by the last Observation.

IV. In *Prop. II. Var. 1.* if the Angle given be Acute, then the Side sought will be less than a Quadrant; if Obtuse, then greater.

V. In *Prop. II. Var. 3.* the Angle sought will be Acute, if the Hypothenufe be less than a Quadrant, and the given Angle Acute; but it will be Obtuse, if the Hypothenufe be less than a Quadrant, and the Angle given Obtuse; or contrarily.

VI. In *Prop. III. Var. 1.* the Hypothenufe will be less than a Quadrant, if the other Angles be both Acute, or both Obtuse, or if the Sides be both of one kind.

VII. In *Prop. III. Var. 2.* the Angle sought will be Acute, if the Hypothenufe be less than a Quadrant, and the other Angle Acute.

VIII. In *Prop. III. Var. 3.* the Side sought will be less than a Quadrant, if the Hypothenufe and the Side given be less than Quadrants.

IX. In



IX. In *Prop. IV. Var. 1.* the Angle sought will be Acute, if the given Side be lesser than a Quadrant; if greater, Obtuse.

X. In *Prop. IV. Var. 2.* if the given Angle be Acute, then the Side sought will be lesser than a Quadrant; if Obtuse, greater.

XI. In *Prop. IV. Var. 3.* the Hypotenuse will be lesser than a Quadrant, if the given Angle be Acute, and the Side less than a Quadrant; and the contrary.

XII. In *Prop. V. Var. 1.* the Hypotenuse will be less than a Quadrant, if the Sides be either of them greater, or either of them less than a Quadrant; and contrarily Obtuse.

XIII. In *Prop. VI. Var. 2.* the Angle sought will be Acute, if the opposite Side be less than a Quadrant; Obtuse, if greater.

XIV. In *Prop. VII. Var. 3.* the Hypotenuse sought for will be less than a Quadrant, if both the Angles given be either severally Acute or severally Obtuse; but it will be greater than a Quadrant if the one be Acute the other Obtuse.

XV. In *Prop. VI. Var. 2.* either of the Sides sought shall be less than a Quadrant, if the opposite Angle be Acute; greater, if Obtuse.

But these Observations need not be regarded, when you shall be well versed in the Sphere or Globe.

Thus you have seen, how Right Angled Spherical Triangles and Quadrants are to be Calculated: I come next to Oblique ones, or not Quadrants.

## SECTION

## SECTION IV.

## The Calculation of Oblique-angled Spherical Triangles.

The Calculating Oblique-angled Spherical Triangles is comprehended in seven *Problems*, according to the seven-fold Variety of the four Parts Ingredients into the Question, as appeareth in this little Table.

In an Oblique-angled Spherical Triangle the four Parts Ingredients into the Question are either	Opposite two to two, that is to say, two Angles } <i>Probl. 1.</i>	
	Opposite to two Sides; & <i>contra.</i>	
	Pure, and that either	Three sides, and then there is fought either { An Angle. } <i>Probl. 2.</i>
		{ Or the Cases of the Base. } <i>Probl. 3.</i>
	Or three Angles which are reducible to three Sides.	
	Or not Opposite two to two, the Parts given being either	{ One Ingredient is removed from three. } <i>Probl. 4.</i>
	Or not Pure, wherein the Order of Ingredients begins with either	{ Or all four Ingredients follow immediately. } <i>Probl. 5.</i>
		{ One Ingredient is removed from three. } <i>Probl. 6.</i>
		{ Or all four Ingredients follow immediately. } <i>Probl. 7.</i>

Problem



## Problem I.

In an Oblique-angled Triangle; of Four Parts opposed, Two to Two, viz. Two Angles and Two Sides, any Three being given, to find the Fourth,

This is the very same with the first Axiom, Sect. II. hereof, of Right-angled Triangles, but that only here is an Oblique Angle in stead of the Right Angle there. And therefore the Resolution is performed by the said first Axiom of Proportion, which was this:

As the Sine of any Side,  
To the Sine of an Angle opposite to it:  
So is the Sine of any other Side,  
To the Sine of the Angle opposite.

## Example.

Fig. 4. In the Oblique-angled Triangle BCD; of these Four Parts, B, DC, D, and BC, let any Three be given, and the Fourth be sought for, suppose BC.

As $\sin B$ $47^{\circ} 34'$ ,	9,868093 (1)
To $\sin DC$ $52^{\circ} 3'$ :	9,896828 (2)
So is $\sin D$ $34^{\circ} 39'$ ,	9,754777 (3)
2d and 3d added	19,651605 (4)
To the $\sin BC$ $37^{\circ} 25'$ .	9,783512 (5)

Having set down the Proportion, and found the Logarithms by the Canon, I add the second and third Terms, which make 19,651605, and subtract from that the first, which is 9,868093, and it leaves 9,783512, the Sine of  $37^{\circ} 25'$ , for the Side BC.

But if you should desire to avoid Subtraction, it is but taking the Arithmetical Complement of the Logarithm of the first Term, and adding all together, it will be the same. Now the Arithmetical Complement of any Logarithm is the Remainder to 10, as of 9,868093 the Arithmetical Complement is 0,131907.

This being understood, and that by altering the Proportion any other Side or Angle may be found, for if it be, As  $\sin B \cdot \sin DC :: \sin D \cdot \sin BC$ , it will be, As  $\sin D \cdot \sin BC :: \sin B \cdot DC$ . Again, As  $\sin DC \cdot \sin B :: \sin BC \cdot \sin D$ , or, As  $\sin BC \cdot \sin D :: \sin DC \cdot \sin B$ , for finding DC, D, or B.

Note, That in the Cases where the greatest Side or Angle is required, it is necessary, that it be known, whether it be greater than a Quadrant, or not; because an Arch lesser than a Quadrant, and the Complement thereof to a Semicircle, have the same Right Sine, as before.

Problem

## Problem II.

In a Spherical Triangle, by Three Sides given, to find an Angle; or by Three Angles, to find a Side.

This Problem will be of great Use in Astronomy and Navigation; for by it the Hour and Azimuth are found, and therefore I will be plain both in the Rule and Example.

Let the Angle C sought be comprehended betwixt the two Sides, whose Sum and Difference I make use of in the Example, viz. BC and CD: Therefore set down the Arithmetical Complements of the Sines of these two Sides, viz. B C  $38^{\circ} 30'$ , and C D  $70^{\circ}$ , and B D the third Side let be 60 Degrees.

Take the Difference of these Sides, which will be  $31^{\circ} 30'$ , and under them set the third Side, whereof take the Sum, which is  $91^{\circ} 30'$ , and the Difference, which is  $28^{\circ} 30'$ ; take the Half of this Sum, which is  $45^{\circ} 45'$ , and the Half Difference  $14^{\circ} 15'$ , and set down the Sines as you see in the following Example; then add up into one Sum those two Sines and the two Arithmetical Complements, and they will make 19,479165, the Half whereof 9,739582 is the Sine of  $33^{\circ} 18'$ , which doubled is  $66^{\circ} 36'$  for the Angle required. This Example practised a few times, will make all easie.

B C	38	30	Arithmetical Complement.	Sine	0,205850
C D	70	00	Arithmetical Complement.	Sine	0,027014
D	31	30	Difference.		
B D	60	00	the third Side.		
91	30		the Sum of D and B D.		
28	30		the Difference.		
45	45		the Half Sum.	The Sine	9,855096
14	15		the Half Difference.	The Sine	9,391205
				The Sum of all four Sines	19,479165
				The Half Sum	9,739582

Which is the Sine of  $33^{\circ} 18'$ , which doubled is  $66^{\circ} 36'$ , the Angle C.

And if three Angles be given, to find out a Side, if in stead of the greatest Side and Angle, you take their Complements to 180 Degrees, the Angles will be Sides; and Sides, Angles; and to be resolved as before.

Problem



## Problem III.

*In all Spherical Triangles, whether Right or Oblique-angled, all the Three Sides being given, to find out the Cases made by the Perpendicular falling upon the Side put for the Base, extended if need be; and consequently the Angles and Perpendicular it self.*

**T**He Cases are formed by this Axiom, *As* the Tangent of Half the Sum of the Cafes, *to* the Tangent of Half the Sum of the Legs :: *fo* is the Tangent of Half the Difference of the Legs, *to* the Tangent of Half the Difference of the Cafes.

Fig. 6.

*As* in the Oblique-angled Triangle BCD, Figure 6, where the Base BD is equal to the Sum of the Cafes BA and DA: Then it will be, *As* the Tangent of Half BD, (that is, the Tangent of BA and DA divided by 2) *to* the Tangent of DC more by BC :: *fo* is the Tangent of DC less by BC divided by 2, *to* the Tangent of DA less by BA divided by 2.

So likewise in the Oblique-angled Triangle bCD, where the Base bD is equal to the Difference of the Cafes DA and BA, it will be, *As* the Tangent of Half BA more by DA, *to* the Tangent of Half DC more by bC; *fo* is the Tangent of Half DC less by bC, *to* the Tangent of Half bD, which is equal to the Half of DA less by bA.

## Example.

*In the Triangle BCD, let the Sides be BC 37° 25', DC 52° 3', and BD 73° 50'.*

BD is 73° 50', the Half BD is 36° 55'; DC is 52° 3', BC is 37° 25', the Sum of DC and BC is 89° 28', and the Half of that Sum is 44° 44'.

Now DC less by BC is 14° 38', the Half is 7° 19', say therefore by the former Analogy, *As* the Tangent of 36° 55', *to* the Tangent of 44° 44' :: *fo* is the Tangent of 7° 19', *to* the Tangent of 9° 37'. Now if you add 9° 37' to 36° 55', it will give 46° 32' for the greater Cafe DA; and if you subtract, it will give the lesser Cafe BA 27° 18'.

Now by B and BA, one of the Cafes, the Angle B is found, by Prop. I. Var. 3. of Right-angled Triangles. And also by DC and DA, the other Cafe, the Angle D is found, by the said Proposition. The same Resolution is made, if Three Angles were given, by turning the Angles into Sides, as in the last Problem.

*Note*, I have omitted to set the Logarithms to the Parts in the former Analogy, which you may supply.

We have now done with *Pure* Parts; but if the Parts given be *not Pure*, the Oblique-angled Triangle is to be reduced into two Right-angled Triangles, by letting fall a Perpendicular (according to the Seventeenth Proposition of the First Section of the Third Chapter, and the Two Notes) in

such

such sort, as that in one Right-angled Triangle, two Parts given may be intire, whereof the one being an Angle is to be noted with the Letter B, and the other a Side to be noted with the Letters B C, as in the Triangles Fig. 7, 8, and 9, are to be fecn. This being done, the whole Calculation will be performed by the Resolution of these Four Problems following.

## Problem IV.

*In an Oblique-angled Spherical Triangle, of the Four Ingredients, whose Order begins with an Angle, and One is removed from Three; the two first being given, and either of the two last, to find the other of the two last.*

**A**S in any of the Three Oblique-angled Spherical Triangles, Fig. 7, 8, 9, Fig. 7. 8. 9. before, noted with BCD:

*Of these Four Parts, B, BC, BCD, and D; B, BC, and BCD, being given, to find D. Or, B, BC, and D, being given, to find BCD.*

This is done by two Operations, for

1. In the Right Angle ABC, there must be found out BCA, by BC and B, which are the Ingredients, and therefore the Analogy will be,

*As* Radius . Tang. of B :: Co-sine of BC . Co-tang. of BCA.

2. The Angle BCA being thus found, then say,

*As* Co-sine of B . Sine of BCA :: Co-sine of D . Sine of DCA.

So that if the Angle BCD be given, by comparing it with the Angle BCA, there will be given the Angle DCA, and so the Angle D by the last Analogy.

Examples of this, and the three Problems following, I do omit purposely, that the Practitioner may exercise himself therein; and the rather, because I have set down all the Parts of the three Triangles next before mentioned, the Calculation whereof these Problems declare.

## Problem V.

*In an Oblique-angled Spherical Triangle, of the Four Ingredients, whose Order begins with an Angle, and all Four do immediately follow one another, the Two first being given, and either of the Two last, to find the other of the Two last.*

**A**S in any of the Three Spherical Triangles last mentioned, and noted with BCD:



Fig. 7, 8, 9. Of these Four Parts,  $B, BC, BCD$ , and  $CD$ ;  $B, BC$ , and  $BCD$ , being given, to find  $CD$ : Or else,  $B, BC$ , and  $CD$ , being given, to find  $BCD$ .

This is done by two Operations, for

1. In the Right-angled Triangle  $ABC$ , there must be found out  $BCA$ , as in the Problem next before, thus, viz.

As Radius . Tang.  $B$  :: Co-sine  $BC$  . Co-tangent  $BCA$ .

2. This being so found, then say:

As Co-sine  $DCA$  . Co-sine  $BCA$  :: Tang.  $BC$  . Tang.  $CD$ :

So that if the Angle  $BCD$  be given, by comparing it with the Angle  $BCA$ , there will be given the Angle  $DCA$ , and so the Side  $BC$  by the last Analogy.

But if  $CD$  be given, then by the last Analogy  $DCA$  will be found, which being compared with the Angle  $BCA$ , there will be found the Angle  $BCD$ .

#### Problem VI.

In an Oblique-angled Spherical Triangle, of Four Ingredients, whose Order begins at a Side, and One is removed from Three; the Two first being given, and either of the Two last, to find the other of the Two last.

As in any of the Three Oblique-angled Spherical Triangles before cited, and noted with  $BCD$ :

Of these Four Parts,  $BC, B, BD$ , and  $DC$ ;  $BC, B$ , and  $BD$ , being given, to find  $DC$ : Or else,  $BC, B$ , and  $DC$ , being given, to find  $BD$ .

This is done by two Operations, for

1. In the Right-angled Triangle  $ABC$ , there must be found out  $BA$ , by  $BC$  and  $B$ , which are the Ingredients, and therefore the Analogy is this:

As Radius . Co-tang.  $BA$  :: Co-sine  $B$  . Co-tang.  $BC$ .

Or else by this Analogy:

As Radius . Tang.  $BC$  :: Co-sine  $B$  . Tang.  $BA$ .

2.  $BA$  being thus found out, say:

As Co-sine  $BA$  . Co-sine  $DA$  :: Co-sine  $BC$  . Co-sine  $DC$ .

So that if  $BD$  be given, by comparing it with  $BA$  there will be given  $DA$ , and so the Side  $DC$ , by the last Analogy.

Problem

#### Problem VII.

In any Oblique-angled Spherical Triangle, of Four Ingredients, whose Order begins at a Side, and all Four do immediately follow one another; the Two first being given, and either of the Two last, to find the other of the Two last.

As in any of the Three Oblique-angled Spherical Triangles before cited, and noted with  $BCD$ :

Of these Four Parts,  $BC, B, BD$ , and  $D$ ;  $BC, B$ , and  $BD$ , being given, to find  $D$ : Or else,  $BC, B$ , and  $D$ , being given, to find  $BD$ .

This is done by two Operations, for

1. In the Right-angled Triangle  $ABC$ , there must be found out  $BA$ , as in the Problem next before, thus:

As Radius . Co-tang.  $BA$  :: Co-sine  $B$  . Co-tang.  $BC$ .

Or thus:

As Radius . Tangent  $BC$  :: Co-sine  $B$  . Tangent  $BA$ .

2.  $BA$  being thus found out, say:

As Sine  $DA$  . Tangent  $B$  :: Sine of  $BA$  . Tangent  $D$ .

So that if  $BD$  be given, by comparing it with  $BA$  there will be given  $DA$ , and so the Angle  $D$ , by the last Analogy.

But if the Angle  $D$  be given, then by the last Analogy  $DA$  will be found, which being compared with  $BA$ , there will be found  $BD$ .

The Analysis of Oblique-angled Spherical Triangles.

1. By two Sides and an Angle opposite, or two Angles and a Side opposite, to find the remaining Side or Angle, and the rest, is performed by the first Problem.

2. By all the Sides to find an Angle, or by all the Angles to find a Side, is performed by the second Problem.

3. By two Sides and the Angle comprehended to find the rest, is resolved by the sixth and seventh Problems.

4. By two Angles and a Side adjacent, or two Sides and an Angle adjacent, to find the rest, is performed by the fourth and fifth Problems.





## CHAP. V.

*Of COSMOGRAPHY, and of the Uses of  
the Sphere and Globes both Celestial and  
Terrestrial.*

**H**AVING taught you *Practical Arithmetick, Geometry*, with the Doctrine of *Pluin and Spherical Triangles*, they will be to you as to many Wings and Helps, whereby to soar up, view, and consider the Heavens, the stupendious Fabrick of the Creator, to wonderful in all its Parts, that it caus'd *David* to say, *The Heavens declare the Glory of God, and the Firmament sheweth his Handy-work*; and the Poet *Ovid* intimates, as if Mankind were framed for this End:

*Pronique cum spectent Animalia cætera Terram,  
Os Homini sublime dedit, Cælimque Tueri  
Jussit, & erectos ad Sidera tollere vultus.*

I might add Reasons; to perswade every one to this Knowledge, but for you it will be evident enough, that without it no Person can be accounted a Navigator, therefore you must learn.

## SECTION I.

*The General Definitions and Notions of Cosmography.*

**I.** **C**OSMOGRAPHY being concerned about the greatest Bodies, and most worthy in the World, the *Heavens*, the *Stars*, and this *Earth* whereon we tread, has its Name rightly given, viz. *The Delineation and Description of the World*, and is right worthily accounted one of the Liberal Sciences. It is divided into two Parts, *Astronomy and Geography*.

II. *Astro-*

II. *Astronomy*, being the first Part of *Cosmography*, treats of the Celestial Spheres.

III. A *Sphere* Mathematical, or *Globe*, is contained under one Superficies, from the middle whereof (called the Center) to the Extream of the said Superficies all Lines drawn are equal. And this may be a Solid Sphere, as the Earth, Sun, Moon, and all the Planets and Stars; or we may conceive it a Hollow Body, which besides the Convex, or outward Superficies, has also a Concave, or inward Superficies, which is likewise equally distant from the Center. And this last is such a Sphere as I am now about to describe, called the *Celestial Sphere*, including all the Celestial Bodies and the Earth within it; which makes me here give notice, that the Celestial Globe is very improper, and not so intelligible to young Learners, unless with this Caution, that the Fancy be informed, that either we may imagine our selves above all the Heavens, or else, which is more proper, that we were in the Center of it, and that the Convex Part were represented by the Concave Shell, where those Constellations and Sines are to be seen. And such Spheres have been made so big, that one might sit in the Center; but lesser are to be had at the Globe-Makers, a Picture or Fashion whereof you Fig. 1. have in the first Figure.

IV. The *Parts* of the Sphere are either, 1. sensible and visible, 2. or not. Those Parts which are sensible, I call that which is really so, and in a clear and serene Night may be seen, as the Stars and Milky-way.

V. The *Stars* are either Fixed, or Wandering and Moving. The Fixed Stars are all those Glorious Bodies seen upon the Concavity of the aforesaid Hemisphere, and are to appearance equally distant in the Eighth Sphere, are infinite in Number, but to Sight may be divided into seven sorts or Ranks; the first Classis are the greatest, the second are a little less, the third less, and so to the sixth, the seventh are certain cloudy and dark Stars, (which by the Prospective Glass are seen to be Multitudes and Heaps of Stars in that Space of the Cloud) there being infinite of this sort.

VI. All this Excellent Frame being so infinite in Number and Place, the old *Astronomers* digested and drew the most Notable of them into certain Forms, or Shapes, of Birds, Beasts, Men, and other Creatures, called *Constellations*, the better to remember and fix them in the Mind, whensoever they had occasion to use them; and they are distinguished, either to be on the North side of the Zodiack, in the Zodiack, or on the South side thereof, yet not so intirely, but some Stars will not, or do not light to be within the same Constellations, and therefore are called *Informes*. All which you may observe upon the Globe, and likewise in the six Maps thereof herewith bound at the End of this Chapter.

VII. The



VII. The Constellations on the North side of the Zodiack are 23, viz.

*Lesser Bear.*

1. The *Lesser Bear* of 10 Stars, whereof 2 of the Second, 1 of the Third, 3 of the Fourth, 1 of the Fifth, and 3 of the Sixth Magnitude. This Constellation is next to the North Pole, that Star in the Tip of the Tail will be but 2 Degrees and 14 Minutes from the Pole in the Year 1700, and will come nearer and nearer to the Pole for about 400 Years, when it will be within half a Degree of it, and then it will depart from it again. This is called the *Pole-star*, the *Sea-star*, because observed by Mariners, and is of the second Magnitude. You must observe, that both in the *Greater Bear*, and in this of the *Lesser*, there are in either of them a Wain, called by us *Charles's Wain*, made of 7 Stars each, (which is the first thing you must learn) you will find them both expressed in Fig. 2 and 3, in both which the Wain is fancied by 4 Stars, the lower 2 for the Wheels, and the Horses by 3; marked by *abcd* for the Wains, and *efg* for the Horses. Here *g* is the Fore-horse for the Pole-star, and *a* for the Brightest in the Wain, called by Seamen the Brightest of the *Guards*, and these are to be perfectly known. To find the Place of the Pole by this Constellation, you may fancy the Pole-star and the next Horse to make an Equilateral Triangle with the Pole, on that Part towards the Bright Star called the *Guard*, and it will point near the Pole itself.

*Pole-star.*

Fig. 2.

*Great Bear.*

2. The *Great Bear* of 35 Stars, whereof 7 of the Second, 3 of the Third, 12 of the Fourth, 8 of the Fifth, and 5 of the Sixth. Of those 4 which make up the Wain, that in the Bear's Shoulder called *Dubhe* is marked in Figure 3 with *A*, and the Wheels with *B* and *D*; the Thill-horse called *Alioth* is marked with *E*, and the other two with *F* and *G*, all of the Second Magnitude. Observe, that the two Stars *A* and *B* are called the *Guards* likewise of the *Greater Bear*, and by imagining a Line to be extended by those two Stars, you will find the Pole-star; and also, that the Pole itself lies between the Thill-horse *Alioth* and the Pole-star.

Fig. 3.

*Dragon.*

3. *Draco*, or the *Dragon*, a Constellation of 35 Stars, that lies wreathing betwixt the two Bears; it has but 1 Star of the Second Magnitude, which follows the last but one in the Tail, it hath 10 Stars of the Third, and is notable, because it hath Stars in every one of the Twelve Signs, and for that the Pole of the Ecliptic lies in the very middle of this Constellation.

*Cepheus.*

4. *Cepheus*, a King of *Ethiopia*, a Constellation that has not any noted Star either of the First or Second Magnitude in it, it contains 21 Stars.

*Bootes.*

5. *Bootes*, the Keeper of the Bear, or *Arctophylax*, has in it 32 Stars, whereof 1 is of the First Magnitude betwixt his Legs, called *Arcturus* by the *Greeks*; and *Arimech* of the *Arabs*, a noted Star.

*Northern Crown.*

6. The *Northern Crown*, or *Ariadne's Crown*, has in it 21 Stars, whereof 1 is of the Second Magnitude, called the Bright Star in the Crown.

*Hercules.*

7. *Hercules*, with his *Club*, watching the *Dragon*, contains 62 Stars, whereof none of the First or Second Magnitude, there are 9 of the Third, whereof that in his Head called *Ras Algethi* is the most noted.

*Harp.*

8. The *Harp*, or *Vultur Cadens*, of 15 Stars, whereof 1 is of the First

First Magnitude, called *Lucida Lyrae*, or the Bright Star in the *Harp*.

9. The *Swan*, of 40 Stars, whereof 1 is of the Second Magnitude, near *Swan* the Tail.

10. *Cassiopeia*, who was the Mother of *Andromeda*, and sits here in her *Cassiopeia* Chair, she has in her Breast a bright Star of the Third Magnitude, called *Scheder*; there are in this Constellation only 28 Stars, according to *Baterra* and others.

11. *Perseus*, the Son of *Danae*, cleared *Andromeda*, and brought away *Perseus* *Medusa's* Head; it contains 42 Stars, whereof 2 are of the Second Magnitude, one in his Left side called *Algenib*, the other in *Medusa's* Head called *Algol*, the rest are of the Fourth, Fifth, and Sixth Magnitudes.

12. *Avriga*, the Carter, of 40 Stars, whereof one at his Back of the *Avriga* First Magnitude, called the *Goat-star*, *Hircus*, and *Capellus*.

13. *Serpentarius*, that holds the Serpent, contains 30 Stars, whereof one of the Second Magnitude in his Head.

14. The *Serpent* of 35 Stars, whereof one only of the Second Magnitude in its Neck.

15. *Sagitta*, or the *Dart*, of 8 Stars, but none of any considerable *Sagitta* dignets.

16. The *Eagle*, or *Flying Vulture*, of 27 Stars, whereof only one is of *Eagle* the Second Magnitude in its Neck, called *Vultur volans*, or *Aquila*.

17. The *Dolphin*, of 10 small Stars, none of the First or Second Magnitude.

18. The *Lesser Horse*, containing 4 Stars of the Fourth Magnitude. *Lesser Horse*.

19. *Pegasus*, or the *Flying Horse*, a fair Constellation of 23 Stars, *Pegasus* whereof 4 are of the Second Magnitude, that in the Tip of the Wing is called *Markab*, these said 4 Stars make a Square.

20. *Andromeda*, or the Chained Woman, Freed and Married to *Perseus*, *Andromeda* containing 27 Stars, whereof 3 are of the Second Magnitude, the first in the Head, the second in the Girdle, and the third in her Leg.

21. The *Triangle*, of 6 small Stars.

22. *Berenice's Hair*, of 13 Stars, all of small Magnitudes.

23. *Cor Caroli*, a small Constellation, formerly *informes*, added by the Worthy and Loyal Knight Sir *Charles Scarbrough*, of 3 Stars, situate betwixt the *Great Bear* and the last Constellation *Coma Berenice*, whereof that of the Second Magnitude is called *Cor Caroli* in Memory of King *Charles* the Martyr.

*Triangle.*  
*Berenice's*  
*Hair.*  
*Cor Caroli.*

VIII. The Constellations in the Zodiack are 12, viz.

1. *Aries*, the *Ram*, the Leader of the Flock, containing 19 Stars; that which is most noted, is that in his Ear of the Third Magnitude, from whence many Astronomical Tables were formerly Calculated, and from this *Opinion* accepted the Proceffion of the Equinoctial.

2. *Taurus*, the *Bull*, containing 48 Stars, whereof one in the Bull's Eye *Taurus* is of the First Magnitude, called *Aldebaran*, and by the *Romans*, *Palilicium*; and another in the Tip of his Horn is of the Second Magnitude. This great



Constellation has two smaller Constellations belonging to it, 1. the *Pleiades*, or Seven Stars, in the Bull's Neck; sometimes they are called *Vergilia*, because of their Circinal Rising in the Spring: 2. *Hyades*, which are Five Stars near the Bull's Eye, called sometimes *Sucula*.

Gemini.

3. The *Twins*, or *Gemini*, a Constellation of 34 Stars, whereof 3 are of the Second Magnitude, the first preceding in the Head is called *Castor*, that in the Neck following is called *Pollux*, and the third is in the Foot.

Cancer.

4. The *Crab*, or *Cancer*, containing 32 Stars, two of them of the Third Magnitude, the rest of the Fourth, Fifth, and Sixth.

Leo.

5. The *Lion*, *Leo*, containing 43 Stars, whereof two are of the First Magnitude, viz. the Lions Heart or *Regulus*, and that in the Extremity of the Tail called *Cauda Leonis*, very fair Stars; and two of the Second Magnitude, viz. that in the middle of the three in his Neck, and that on the top of his Loins.

Virgo.

6. The *Virgin*, *Virgo*, hath 45 Stars belongs to her, and one considerable of the First Magnitude, in the Virgin's Left-hand, called *Spica Virginis* or *Vindemiator*.

Libra.

7. The *Balance*, *Libra*, containing 14 Stars, whereof two are of the Second Magnitude, viz. one in the Southern Scale called *Lanx Meridionalis*, the other in the very End of the Handle called also *Lanx Septentrionalis*.

Scorpio.

8. The *Scorpion*, containing 35 Stars, one of the First Magnitude in the Body called *Cor Scorpionis*, and of the Second in the Head.

Sagittarius.

9. *Sagittarius*, or the *Centaur*, hath 30 Stars in it, two whereof are of the Second Magnitude, one in the Knee of his Right-leg, and the other in the Heel of the same Leg.

Capricornus.

10. *Capricornus*, containing 28 Stars, but none of them either of the First or Second Magnitude.

Aquarius.

11. *Aquarius*, having 42 Stars in it, but none of any considerable Magnitude.

Pisces.

12. *Pisces*, the *Fishes*, have 36 Stars in them, but none of them either of the First or Second Magnitude.

IX. The Constellations on the South side of the Zodiack, are,

Whale.

1. The *Whale*, or *Cetus*, a Constellation of 29 Stars, whereof two are of the Second Magnitude, one near his Mouth, and another near the Tail.

Orion.

2. *Orion*, a most noted Constellation of 56 Stars, whereof there is one of the First Magnitude in his Left-shoulder of a ruddy colour, and another of the same Magnitude in his Right-foot called *Rigel*; there are four of the Second Magnitude, one in his Right-shoulder, and three in his Girdle in a straight Line called the *Tard Wand*: There are two in the Shoulders before-mentioned, two in his Feet, three in the *Tard Wand*, and three below in the Sword, which fashion this great Warriour, and are very notorious.

Eridanus.

3. *Eridanus*, or the *River*, of 44 Stars, in the Extremity whereof one is of the First Magnitude called *Enay*, the rest are small ones.

Hare.

4. The *Hare*, *Lepus*, of 13 Stars, all small ones.

5. The

5. The *Great Dog*, *Canis major*, a Constellation of 19 Stars, whereof *Great Dog*. that in his Mouth is of the First Magnitude, a great sparkling star called *Sirius*, and one near his Left-knee is of the Second Magnitude; the rest are small Stars.

6. The *Little Dog*, *Canis minor*, of 10 Stars, whereof one in his Belly called *Procyon* is of the first Magnitude, the rest are small. *Little Dog*.

7. The *Ship*, or *Argo Navis*, a Constellation of 51 Stars, whereof one *Ship*. in the Rudder called *Canopus* is of the First Magnitude, and there are seven Stars of the Second dispersed in this Constellation.

8. *Centaurus*, or the *Centaur*, a Constellation of 41 Stars, wherein *Centaur*. there are two of the First Magnitude, one in his Left-thigh, and another in the Extremity of his Right-foot; there are five of the Second Magnitude, the rest small.

9. *Crater*, the *Goblet*, is a small Constellation of 11 Stars. *Goblet*.

10. *Corvus*, the *Crow*, another small Constellation of 8 little Stars. *Crow*.

11. *Hydra*, the *Serpent*, containing 29 Stars, whereof one is of the First Magnitude called *Alphard* in the third Wreath, and is sometimes called *Cor Hydra*; the rest are small. *Hydra*.

12. *Lupus*, the *Wolf*, a Constellation of 20 Stars, all small. *Wolf*.

13. The *Altar*, *Ara*, of 6 small Stars. *Southern Crown*.

14. The *Southern Crown*, *Corona Meridionalis*, of 13 small Stars. *Southern Fish*.

15. The *Southern Fish*, *Piscis Notius*, of 12 Stars, whereof one in the Mouth called *Fumham* is of the First Magnitude, the rest are small Stars.

16. There are 12 Constellations more towards the South Pole, viz. 1. The *Peacock*, *Pavo*; 2. *Toucan*; 3. *Gras*; 4. *Phanix*; 5. *Dorado*; 6. *Piscis volans*; 7. *Hydras*; 8. *Chameleon*; 9. *Apis*; 10. *Apis Indica*; 11. *Triangulum*; and 12. *Indus*; the which I shortly expect shall be truly rectified and adjusted, as to their Places and Distances, by the industrious and able Astronomer, Mr. Edmund Halley, now residing at St. Helen's Island for that purpose.

There is besides to be noted, the *Milky-Way*, described upon the Globe round about, and several other little Clouds, or white Spots, the which viewed by a good and long Telescope are found to be very many small Stars together, and infinite in number, so close, that with the bare Eye they disappear, and seem to be a small Cloud and white Way. So that the Number of the Stars mentioned in the former Constellations are not all, nor it may be not the thousandth part of the Stars; for as some Eyes may see more of them than others, so by Glasses still longer than others more are seen, and may be almost accepted infinite.

X. The *Wandering Stars* or *Planets* are 7, and are either greater, as the *Seven Planets*. *Sun* and *Moon*, because of their visible Light; or lesser, and those are either above, or under the *Sun*; those above are three, *Saturn*, *Jupiter*, and *Mars*; those under are two, *Venus* and *Mercury*.

For the knowing of these Planets, first the *Sun* and *Moon* are notable, but the rest of them are not known from the Fixed Stars, but by their



irregular and different Appearances from them, and by the difference of their Lights, which do not twinkle, and of other Colours to the Fixed Stars.

Now because we shall have ordinary use to name these Planets, I shall set down the Characters by which they are usually signified.

☉ The Sun.	♂ Mars.
☾ The Moon.	♀ Venus.
♄ Saturn.	☿ Mercury.
♃ Jupiter.	

## SECTION II.

### Of the Movements of the Heavens, as to Apprehension.

The first Phenomena, of the Motion of the Heavens.

**I.** Here are two Phenomena for the solving these Motions, and rendering the Reasons of them; the first, to consider this Earth and Waters to be in repose in the Center or Middle of the World, and to conceive that the Heavens move about us from East to West, carrying with them all the Stars comprehended under this vast Vault or Hemisphere.

**II.** That the Fixed Stars turn round about from Noon to Noon, or from Midnight to Midnight, in 24 Hours, (it is true, there is some small alteration, by reason of some other Motion of them, but it is inconsiderable, being but 2 Degrees in 200 Years,) from East to West, which is called their *Diurnal Motion*; this is very visible, and to be apprehended easily; and this is the Eighth Sphere so called, or Sphere of the Fixed Stars.

The next Sphere is that of *Saturn*, which is carried about as the rest of the Fixed Stars, but hath a Motion of his own from West to East, so that he accomplisheth it in 29 Years and 183 Days.

The next is the Sphere of *Jupiter*, that contrary to the aforesaid Motion of 24 Hours moves from West to East, so that he makes his Tour in the space of 11 Years and 318 Days.

The next is the Sphere of *Mars*, that performs his Tour contrary to the Motion of the Fixed Stars in 1 Year and 310 Days.

The next is that of the *Sun*, which makes his Motion from West to East almost one Degree in a Day, and performs his Tour in 365 Days, 5 Hours, and near 49 Minutes, but is carried along with the rest of the Stars by the First Mover, as before was said.

Next the Sun is the Sphere of *Venus*, which moves about with the Fixed Stars, but has its own Motion from West to East in about 8 Months.

Next

Next to *Venus* is *Mercury*, seldom seen, he makes his Tour from West to *Mercury*. East in near 3 Months.

Lastly the *Moon*, that makes her Tour from West to East in near 28 Days.

This *Hypothesis* of the Stability of the Earth is fitly explained by Figure 4, where you may perceive the Earth to be the Center, and that the several Spheres have their Places one within another, and that the Sphere of the Fixed Stars incloses them all, as the outward part of an Onion incloses all the other Foldings, as I may familiarly hint it unto you.

**III.** The second Phenomena or Hypothesis for the solving the Motions, is that which is contrary to the former, not that the Fixed Stars and Heavens move about in 24 Hours, but that they all, as the Sun, are in repose and rest, and move not at all; and that this Terraqueous Globe (this Earth, Sea, and Air about it) turns upon its Axis and proper Center in 24 Hours: So then in this Hypothesis the Sun is in the Center immoveable, next him is the Orb of *Mercury*, next *Mercury* the Orb of *Venus*, then the Earth with a Circle about it for the Moon, next that is the Orb of *Mars*, next is the Orb of *Jupiter* with four small Moons about it carried with it, and lastly *Saturn* with two small Moons, and above all, at an immense Distance, is the Sphere of the Fixed Stars; as you may perceive by Figure 5, where all these Orbs are made apparent to the Eye.

Of these two Hypotheses or Principles, the first was followed by *Aristotle*, *Hipparchus*, *Ptolemy*, and by a great many of Philosophers and others: The second was followed by *Ecphantus*, *Aristarchus*, *Philolaus*, *Plato*, the *Pythagoreans*, and by *Archimedes*; and after it had been almost quite forgotten for many Ages, it was revived by *Copernicus*, and after him by abundance of the ablest Astronomers and Philosophers, and at this day seems to be believed by the major part of the Virtuosi of the World.

However both these Hypotheses do equally, though not so rationally, solve this Spherical Doctrine we are about, but I shall chuse here the old *Ptolemaick*, which is the first of the two before-mentioned, as the most easie and agreeable to you, I am about to instruct, though I approve and allow of the second, as most reasonable and rational.

**IV.** The next thing I shall endeavour to make out is, That all this Globe of Earth and Water (and therefore fitly termed the *Terraqueous Globe*) is no more than a Point, or the smallest thing imaginable, in respect of the Wideness of the Sphere of the Fixed Stars, and this is certainly intelligible, for these Reasons: 1. That where-ever one is, either upon Land or Sea, there is one half of the full Heaven in sight, and that two Fixed Stars diametrically opposite, the one shall be setting in the West when the other is rising in the East. 2. That all Astronomical Instruments, and all those made for Dialling, that are used upon the Superficies of the Earth, do declare and shew to us the Motion and Place of the Stars, as to our Sense, as if we were in the Center of the Earth. 3. Whereas Globes and Spheres

are



are in triplicate proportion in respect of their Diameters, if the Diameter of the Earth be put for 1, the Diameter of the Heavens (according to Tycho) is at least 14000, (but according to others is much greater) that is, the Cube of the Earth 1, will be to that of the Heavens 244,000,000,000. But Unity is insensible to such a vast Number, therefore let me a little fly out, and repeat you Seneca's Words, in his Preface to his *Natural Questions*, *Hoc est illud Punctum, quod inter tot gentes ferro & igni dividitur. O quam ridiculi sunt Mortalium termini! Punctum est illud in quo navigatis, in quo bellatis, in quo Regna disponitis, &c.* Now (according to Copernicus) if the Sun should rest in the Center, and the Earth be moved about by its Diurnal, and carried round the Sun by its Annual Motion, not only the Diameter of the Earth, but the Diameter of that great Orb that the Earth is supposed to move in (which is of such a Magnitude, that it certainly contains the Earth's Body 343,000,000,000) will be found nothing, or a Point, in respect of the Firmament of the Fixed Stars.

V. That the Earth, as to our Sense, is in the middle of the Heavens, is manifest by the last Proposition, not only in the common opinion of the first Hypothesis, but even in that of Copernicus; for if the Earth were in the Sun's Place, yet nevertheless by the last Proposition even the great Orb would not be sensible to the Heavens, much less to the Earth.

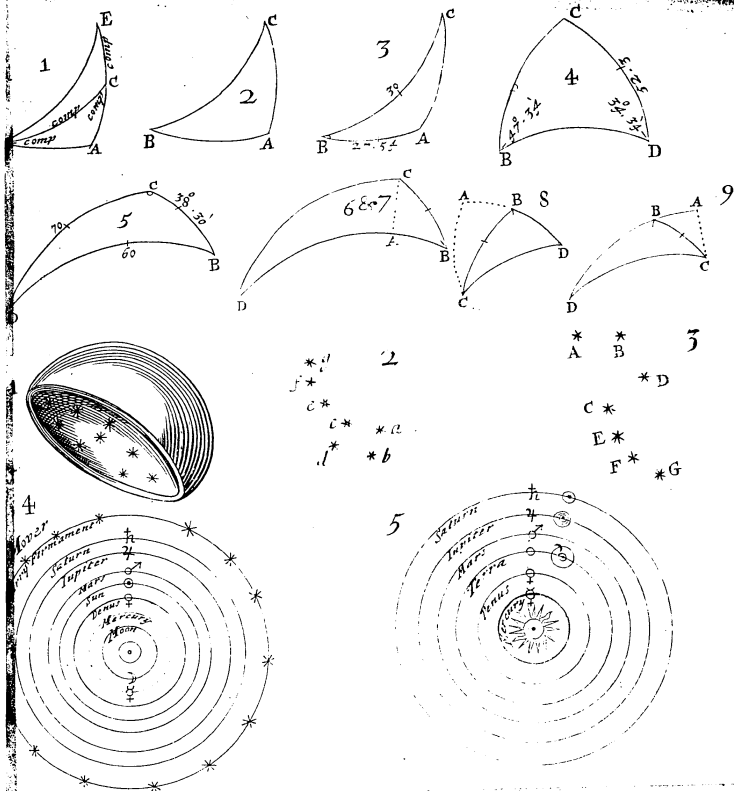
VI. Having thus declared to you the sensible and visible Parts of the Heavens, and the two Hypotheses of their Motions, I come to shew you, what those Circles, Poles, and Points are, which are insensible and invisible, and only feigned and imagined for the better using and understanding of this Work of Spherical Astronomy, invented for very good Ends and Uses.

The Circles that are described upon the Sphere are either called *Great Circles*, because they cut the Sphere into two equal Parts; or *Lesser Circles*, which do not. Also every Circle (as has been often told you) is divided into 360 Degrees, every Degree into 60 Minutes, every Minute into 60 Seconds, and so into Thirds, Fourths, &c. though it had been far better to have used the Decimal way, but Custom carrieth it for the Sexagenary. The Circles and Points considerable are these, viz.

Horizon.

1. The *Horizon*, which is the first Great Circle observable by every vulgar Person, for being upon a Plain in any fair Day or Night, and looking where the Heavens and Earth part, we see a Circle round about, sometimes called the *Finitor* for that cause, but this Horizon thus found is not the true Horizon, but parallel to it, and therefore called the *Sensible, Physical*, and *Visible Horizon*, which I shall treat of in the last Section of this Chapter of Geography, and now speak of the *Rational* and *True Horizon*, which is a Great Circle of the Sphere passing by the Center of the Earth, and divides the Heavens into two Halves, viz. the *Upper* or *Light Hemisphere*, and the *Lower* or *Dark Hemisphere*. Things at first observable are, that all People see the Sun and Stars rise and set upon this Line, the middle betwixt which we call the *Meridian* or *South*, and the Point opposite the *North*, the

True Horizon.  
Upper, light,  
and visible Hemis-  
phere.  
Rising and Set-  
ting.  
South, North.





the middle betwixt these Points are the *East* and *West*; so that the Horizon is divided thus into four Quarters, and these four Points are called the *Cardinal Points* of the Horizon, but as People grew more curious, and for that venturing upon the Sea they had more need of a more exact Division, they first divided these four into four again, having the Name from each Cardinal on either side, the South and North still accounted the chief, and these are, *South-East*, *South-West*, *North-East*, *North-West*; so now the whole is thus divided into eight Parts or Divisions. Again these were divided into Halves, making sixteen in all, and taking their Names from the next two of either side, as *North North-East*, *North North-West*, *East North-East*, *West North-West*, and then from the South, *South South-East*, *South South-West*, *East South-East*, and *West South-West*. Lastly, these sixteen were again divided into Halves, called *By-Points*, from the Cardinal Points, as from the North, *North and by East*, *North and by West*, &c. All which are seen in every Mariners Chard, and you may both see and learn them from Figure 6, where they are clearly expressed. As for Example, *c* is the Center of the Horizon, *su* the Line of South and North, *ew* of East and West, *af* the Line of South-East and North-West, and *gh* of North-East and South-West.

*East and West.**South-East,  
South-West,  
North-East,  
North-West.*

Fig. 6.

This is one Division of the Horizon into 32 Parts, which all Navigators observe, and generally go to no more exactness, but Astronomers and Spherical Men go to a far greater niceness and exactness, for they divide it not only into Quarters or Quadrants, but every Quadrant into 90 Degrees, and every Degree into 60 Minutes, and into more if required; so that the whole Horizon is divided into 360 Degrees, and those Degrees into Minutes, &c.

The very Center of this Horizon is the Place of Observation, and a Line of Direction perpendicular to it passeth through to the Point Perpendicular over our Head, which is called the *Zenith*, and another quite under our Feet, which is called the *Nadir*, which are the two Poles of the Horizon, and are 90 Degrees distant from it. If from the Zenith to every Point or Part of the Horizon, whether greater or smaller Divisions, there pass Circles, they are called *Vertical Circles*, and may be as many as you will imagin; that which passeth by the South Zenith and North is called the *Meridian*, and that Circle which passeth by the Points of East and West is called the *Prime Vertical*, and all the rest are called *Azimuths*, or Circles shewing the Position of any Point of the Heavens, in respect of the Horizon and Cardinal Points.

*Zenith.  
Nadir.**Meridian.**Prime Vertical.  
Azimuths.*

If Circles be drawn through every Degree and Part of these Vertical ones parallel to the Horizon, they will be all Lesser Circles upon the Sphere, and decrease toward the Zenith to a Point: These are called *Almicanters*, and shew in the Sphere how far any Point in the Heavens is high, or distant from the Horizon.

*Almicanters, or  
Circles of  
Height.*

This Circle of the Horizon shews the Rising and Setting of the Stars or Planets; for when they come up from the dark Hemisphere they are said to rise; and contrarily when they go down are said to set.

*Rising and  
Setting.*

And



*Amplitude Or-  
tive and Occa-  
sive.*

*Artificial Day  
and Night.*

*Meridian.*

*Eastern and  
Western Hemi-  
spheres.*

*Poles of the  
Meridian.*

*Natural Day.*

*Poles Height or  
Latitude.*

*Equinoctial.*

And upon this Circle the Distance of the Rising of any Star or Planet from the East Point, or the Setting from the West Point, in Degrees and Minutes, (or grossly upon the Points of the Compass before described) is called the *Amplitude Ortive* for Rising, and *Occasive* for Setting.

The Horizon is the Cause of the Artificial Day and Night, for we call the Time wherein the Sun abideth above the Horizon an *Artificial Day*, and the Time that he continueth under it the *Night*. Many other Uses are made of this Circle, which I shall hereafter declare; but I will come next to,

2. The *Meridian*, a great Circle of the Sphere, passing the Points of South, and North, and Zenith of the Horizon, and cuts the Sphere or Globe into two Parts or Hemispheres, the Eastern and Western: The *Eastern Hemisphere* is all that Part of the World which is on the East side of the Meridian, and the *Western* is that Part on the West.

The Meridian cuts the Horizon at Right Angles, and they two divide the World into four Quarters, and the Poles of the Meridian Circle are in the Horizon in the Points of East and West, and lastly the Meridian and Prime Vertical before described make four equal Quarters of the World.

This Circle divides the Artificial Day and Night into two equal Parts, and shews Mid-day and Mid-night, and when the Stars and Planets are at the highest, or in the Meridian, and are called the *Meridian Altitudes* of the Sun and Stars, which Heights are chiefly observed by Astronomers and Seamen with all diligence.

Astronomers begin their Account of Time (which is measured by the equal Motion of the Equator) from the Meridian: The principal of which Time is the *Natural Day*, which is usually begun from Mid-day or Mid-night, and divided into 24 Hours, and each Hour subdivided into Minutes, Seconds, &c.

The Poles of the World are fixt in this Meridian, and in this Circle are observed and accounted the *Latitudes* or Height of the Poles and of the Equinoctial; for the Height of the Pole or Equinoctial, is nothing else but the Arch of the Meridian, contained between the Pole or Equinoctial and the Horizon, and the Height of the Pole is always equal to the Latitude of the Place, and the Height of the Equinoctial is equal to the Complement of the Latitude, and therefore it being subtracted out of 90 Degrees, there shall remain the Height of the Pole.

Now these two Circles of the Sphere, the Horizon and Meridian, joyning together in the Points of South and North, and being immovable, and certain to one Place, support the whole Spheres and Globes; and being thus particularly described, I will come to the Moveable Circles, which are Great Circles, the *Equinoctial*, the *Ecliptick*, the two *Colures*, and the Circles of *Longitude*.

3. The *Equinoctial* or *Equator*, a great Circle, which incomparteth about the midst of the Sphere or Globe, and is every where of equal distance from both Poles, and has its Name from that Position, or else, because the Sun coming under this Circle makes Equality of Days throughout the whole World.

It is divided into 360 Degrees (as all Circles are used to be) beginning where the Ecliptick crosseth in the first Point of the Sign *Aries*, proceeding from 10 Degrees to 20, and so Eastward 'till you come about to the same Point again. This Circle hath many Uses, for,

First, it is the Measure of the *First Motion*, for this only of all the Great Circles of the Sphere or Globe is moved equally both in a Right and Oblique Sphere, because the Axis of the World, about which all are turned about equally, is perpendicular therunto.

Secondly, it is the Measure of *Time*, because it measures the Quantity of Artificial and Natural Days, of which Months and Years are made: It measureth also the Quantity of Hours, and of other Times, which the Sun makes going under the Ecliptick, and therefore the Degrees of the Equinoctial are called *Tempora*, Times: After which Account, the whole is divided into 24 Hours, 15 Degrees thereof to an Hour, for 15 times 24 makes 360. Every Degree of the Equinoctial is 4 Minutes of Time, because 4 times 15 is 60 Minutes, or an Hour.

Thirdly, it sheweth the two *Equinoctial Points* of the Ecliptick, for seeing it cutteth the Ecliptick in two Places, which are in the Beginning of *Aries* and *Libra*, the Sun when he cometh to those two Points is equally distant from both the Poles of the World, and makes equal Days and Nights as before said, which falls after our Account about the Tenth of March and 13 of September.

Fourthly, the Irregularities of the Rising and Setting of the Zodiack, and of the Signs and other Parts thereof, are measured by this Circle; for seeing the most part of the Apparences are referred to the Zodiack, and the Zodiack it self is not turned about upon its own Poles, but about the Poles of the Equinoctial, and therefore must needs be unequally turned about, and needful it was to regulate it hereby. Hence come the Names of *Right Ascension*, *Oblique Ascension*, *Ascensional Difference*, which are thus defined:

The *Right Ascension* of the Sun, any Star, or Point of the Heavens, is the Arch of the Equinoctial Circle contained betwixt the Beginning of *Aries* and the Meridian which cutteth the Sun, Star, or Point, being first brought under the fiducial Edge thereof, and this either in Degrees, or in Time, allowing 15 Degrees to an Hour, as before was taught.

The *Oblique Ascension*, is the Arch of the Equinoctial intercepted betwixt the Beginning of *Aries*, and the Horizon, when the Sun, Star, or Point, *is*, is likewise brought to the Edge of the Horizon.

The *Ascensional Difference*, is the Difference of the Right and Oblique Ascensions, and may be had by subtracting one of them from the other, and all these are to be had either in Degrees or Time.

Fifthly, the Equinoctial divides the Globe or Sphere into two equal Hemispheres, the *Northern* and the *Southern*, and the Poles of this Circle are the Poles of the World, one called the *Arctic* or the North Pole, the other *Antarctic* or South Pole; from which Poles the said Circle is distant 90 Degrees.



Meridians.

Hour-Circle.

Parallels of  
Declination.  
Declination.  
North.  
South.

Tropicks.

Tropick of  
Cancer.  
Tropick of Ca-  
pricorn.  
Arctic Circle.  
Antarctic  
Circle.

fig. 7.

Sixthly, If from the North Pole to every Degree of the Equinoctial, and so to the South Pole, Circles be drawn, these are called *Meridians* or *Hour-Lines*, the chief whereof is the Great Meridian or Twelve of the Clock Hour-Line, that passeth by the Zenith and the South and North Points of the Horizon, in the Globe and Sphere. These Meridians are supplied by the Hour-Circle, which is fixed upon the Meridian, and has the Pole for the Center, and has a moveable Index, which turns as the Globe doth, and fits instead of all those Meridians before-mentioned, which in the laying down of the Globe *in plano* is omitted, and all or most of the Meridians are drawn; therefore it will be of great use to explain this, and that the young Scholar may fully understand, how this Hour-Circle and Index are supplied in the Draughts and Uses of the Globe *in plano*.

Seventhly, Upon the Globe or Sphere, if at every Degree upon the Great Meridian, or all the Meridians, there be Circles drawn parallel to the Equinoctial, they will decrease to nothing at the Poles, and these are called *Parallels of Declination*, and shew what Declination any Planet, Star, or Point, hath from the Equinoctial, the Complement whereof is the Distance of that Star or Point from either of the Poles; if that Planet, Star, or Point, be in the Northern Hemisphere it is called *North Declination*, if in the Southern, *South*. The Declination therefore, is nothing but the Distance from the Equinoctial in Degrees and Minutes, accounted upon the Great Meridian, or upon any other Meridian.

Eighthly, The two Parallels, that are 23 Degrees and an half from the Equinoctial on either side, are called *Tropicks* from turning, for there the Sun turns back again from either of them towards the Equinoctial. That which is in the Northern Hemisphere is called the Tropick of *Cancer*, the other on the other side is called the Tropick of *Capricorn*.

Other two of these Parallels, which are 23 Degrees and an half from the Poles, are described on the Globes; that towards the North Pole is called the *Arctic Circle*, the other on the South side the *Antarctic Circle*.

Lastly, These Tropicks shew the Tropical or Solstitial Points of the Ecliptick, which I am next to describe, they bound the greatest Declination of the Sun, in an Oblique Sphere they point out the shortest and longest Artificial Days. And to the end you may the better understand what has been said, both of the Equinoctial, the Meridians, and Parallels, and likewise of the Horizon, Azimuths, and Almucanters, for in each Case they are alike, and alike situate; I have drawn the Fashion of them in Figure 7, where *ab* may represent the Half of the Equinoctial divided into twelve 90 Degrees, then let *c* be the North Pole, and *d* the South Pole, those Circles which come from either Pole will be the Meridians, and pass by every 10 Degrees of the Equinoctial, the other straight Lines are the Parallels, *mn* may be the Tropick of *Cancer*, and *pq* that of *Capricorn*, distant 23 Degrees and an half from the Equator; the upper Half is then the Northern Hemisphere, and the lower the Southern; the outermost Circle is the Great Meridian of Twelve of the Clock; even so for the Horizon, let the outermost Circle be the Meridian of Twelve as before, then

then let *ab* be the Horizon, so will the Hemisphere *acb* be the light Hemisphere, and *adb* the dark, *c* will be the Zenith, and *d* the Nadir: Those Circles which were Meridians before, are now Vertical Circles or Azimuths, and come through the Horizon to the Nadir; and those straight Lines which were Parallels before, do now become Parallels to the Horizon, or Almucanters. These will be of great Use to be learnt and well understood, and will much facilitate the Work of the Uses of the Sphere. We come now to

4. The *Zodiack*, which is a broad Circle of about 14 Degrees, and encompasseth about the Sphere obliquely like a Belt or Girdle, coming nearer the Pole of the Sphere in one Place than in another. In the midst of this Zodiack is a great Circle drawn, which is called the *Ecliptick Line*, or the *Sun's Way*: This Ecliptick is drawn upon the Globe, and not the Zodiack, it crosseth the Equinoctial in two Points, called the *Equinoctial Points*, and is divided into 12 Parts called *Signs*, and every Sign into 30 Degrees, so that the whole is divided into 360 Degrees, and each Degree into Minutes, &c. it is graduated from West to East beginning at *Aries*. The 12 Signs are, 1. *Aries*, its Mark  $\Upsilon$ , 2. *Taurus*  $\mathbf{\text{♉}}$ , 3. *Gemini*  $\mathbf{\text{♊}}$ , 4. *Cancer*  $\mathbf{\text{♋}}$ , 5. *Leo*  $\mathbf{\text{♌}}$ , 6. *Virgo*  $\mathbf{\text{♍}}$ , 7. *Libra*  $\mathbf{\text{♎}}$ , 8. *Scorpio*  $\mathbf{\text{♏}}$ , 9. *Sagittarius*  $\mathbf{\text{♐}}$ , 10. *Capricorn*  $\mathbf{\text{♑}}$ , 11. *Aquarius*  $\mathbf{\text{♒}}$ , and 12. *Pisces*  $\mathbf{\text{♓}}$ . These things are to be noted:

First, The Signs are not to be confounded with the Constellations of the same Name, for the Constellation of *Aries* is another thing to the Sign of *Aries*; the one has the Picture of a Ram, wherein 19 Stars are placed, as before was taught; but the Sign of *Aries* is only 30 Degrees of this Ecliptick imaginary Line, from the Equinoctial to the Beginning of *Taurus*, and numbered to 30 Degrees from the Equinoctial: And what I say of *Aries* you may account of all the rest of the 12 Signs. It is true, these Signs and the Constellations were near unto one another some thousands of Years since, but the Fixed Stars, by their Motion upon the Poles of the Ecliptick, though slowly, have (as you will find upon the Globe) removed the Constellation of *Aries* near upon 30 Degrees forwards into *Taurus*, and the Constellation of *Pisces* the like into the Sign of *Aries*, and so of the rest; which deserves to be considered, lest you fall into a Mistake. Peruse Figure 8, and you will learn the Name, Figure, and Mark of the 12 Signs of the Ecliptick.

Secondly, The Ecliptick has two Poles, one on the North side, and another on the South, 23 Degrees 30 Minutes from the Poles of the World, and so much doth the Ecliptick lye obliquely from the Equinoctial, and so much is the Angle that the Ecliptick makes with the Equinoctial.

Thirdly, The Meridian that passeth by the Beginning of the Signs *Aries* and *Libra* is termed the *Equinoctial Colure*, and that Meridian which passeth by the Beginning of the Signs *Cancer* and *Capricorn* is called the *Solstitial Colure*, and this Colure passeth likewise through the Poles of the Ecliptick. These two Colures divide the Ecliptick, and indeed the whole Globe into four Parts. That Quarter betwixt the Beginning of *Aries* and Beginning of *Cancer*, contains 3 Signs  $\Upsilon$ ,  $\mathbf{\text{♉}}$ , and  $\mathbf{\text{♊}}$ , or thrice 30 Degrees, equal to

Equinoctial  
Colure.  
Solstitial Co-  
lure.

a Quo.

Fig. 8.



Quarters of  
the Year.  
Spring.

Summer.  
Autumn.

Winter.

a Quadrant or 90 Degrees, and whilst the Sun is under this Quarter, the Days are longer than the Nights; and this may be called the *Vernal* or *Spring Quarter*, and as long as the Sun is here, which is most of *March*, all *April* and *May*, is accounted the First Quarter of the Year. The next, of *Cancer* to *Libra*,  $\mathfrak{C}$ ,  $\mathfrak{L}$ ,  $\mathfrak{B}$ , is *Astus*, or the *Summer Quarter*, *June*, *July*, and *August*. The next, from *Libra* to *Capricorn*,  $\mathfrak{L}$ ,  $\mathfrak{B}$ ,  $\mathfrak{C}$ , is the *Harvest Quarter* or *Autumnus*, *September*, *October*, and *November*. The fourth and last, from *Capricorn* to *Aries*,  $\mathfrak{B}$ ,  $\mathfrak{C}$ ,  $\mathfrak{L}$ , is the *Winter Quarter*, called *Hyems*, and falls in *December*, *January*, and *February*. In the two first, the Days are longer than the Nights; in the two last, the Nights are longer than the Days. And note, That every Quarter is divided as before into 3 Signs, or into 90 Degrees.

Fourthly, It is very necessary the young Student have an apprehension, how the Motion of the Sun is made under the Ecliptick, for he must know, that the Sun, though he be carried by the First Mover, as is commonly apprehended, along with the rest of the Heavens, from East to West round in 24 Hours, yet by his own particular Motion from West to East he moves about a Degree in every 24 Hours, and performs his whole Tour in 365 Days, 5 Hours, and near 49 Minutes. A better representation on the Sphere or Globe cannot be made, than by placing a small Fly or Lowie upon the first Point of *Aries*, and then turn the Globe about from East to West one whole Turn, or 24 Hours, and if the Fly creep in the mean time one Degree, or be imagined so to do, and so for every Degree one Turn, you will then easily perceive the Motion, and that whilst the Sun moves thus up the first Quarter to *Cancer*, he draws nearer to the North Pole and lengthens the Days, in the second and third he draws nearer to the South Pole and shortens the Days, in the fourth and last Quarter he lengthens as in the first.

Thus the Sun's proper Motion is made, not upon the Center of the Earth, (for then the Sun's Body would appear always to have one and the same Diameter) but upon another Center, as all the Planets do, which shall be particularly explained in the Last Part.

The other Motion from the *Primum Mobile* is likewise fully and clearly to be apprehended, how the Sun and all the Stars are carried about in their several Parallels, (though indeed it be spirally) but being broken off under the Horizon, as to our sight, we represent them by one of the Parallels to the Equinoctial, which by the Ninth Figure will be made more plain to the Understanding, where the two Motions are considered, for if the Sun had only one from West to East, then he would keep one Parallel, and never change the Seasons of the Year; but that he has two may in a few Days be perceived; and if you consider, that when a Ship is under Sail, and goes a swift course, the Passengers walk upon the Deck a contrary Motion without any confusion, where is then two Motions made, one progressive with the Ship, the other back otherwise, as in the said Figure 9, where let the Globe or Sphere be moved upon the two Poles F and G, which are immovable, suppose the Sun be in H, in the moveable Circle H I B, which

which let represent the Ecliptick, it is evident, that the Sun being in H, Fig. 9. and turning about in 24 Hours, will describe a Parallel (to the Equinoctial C E D) which is H K by the Point H. But when the Sun by his own Motion has advanced from H to L, by his proper Motion he will not describe the Parallel H K, but another L M, 'till at last he arrive at the Point E, equally distant from the Poles F G. Then by his Diurnal Motion he will describe a great Circle of the Sphere, which is the Equinoctial C E D. Lastly, when the Sun shall arrive at the Point B, he will describe the Parallel A B, and so he will rise again on the other side, 'till he come to H, describing the same Parallels again. The lesser Circles H K and A B are the Tropicks.

So that the Sun advanceth every Day about a Degree in the Ecliptick, and changeth his Declination or Distance from the Equinoctial, and consequently his Height at Noon, and the Place of his Rising and Setting on the Horizon.

Fifthly, The Sun making his Motion exactly under the Ecliptick Line, I must explain to you why the Zodiac is made so broad, for that the rest of the Planets, viz.  $\mathfrak{J}$ ,  $\mathfrak{U}$ ,  $\mathfrak{S}$ ,  $\mathfrak{Z}$ ,  $\mathfrak{V}$ , and  $\mathfrak{M}$ , do not keep under the Ecliptick Line, but have several Circles of their own, which cross the Ecliptick, but seldom exceed 7 Degrees of either side from it, and so wide is the Zodiac made to contain 14 Degrees, in which Zodiac the rest of the Planets are to be found by their Longitude and Latitude. You must therefore know, that the Ecliptick's Poles are placed in the Solstitial Colure, 23 Degrees 30 Minutes from the Pole; and even as from the Poles to the Equinoctial the Meridians are drawn, so from the Poles of the Ecliptick, if Circles be drawn to the Ecliptick, those are called *Circles of Longitude*, and all Circles parallel to the Ecliptick are *Circles of Latitude*, and all the Planets, Stars, or Points, are limited by these Circles to be so much in Longitude, viz. in what Degree and Minute of the Ecliptick, whether in *Aries*, *Taurus*, &c. and so much in Latitude, that is, how far from the Ecliptick, either towards the North, and then it is *North Latitude*, or to the South, and then *South Latitude*.

Having (I hope) cleared your Judgments, from mistaking the Signs for the Constellations, you must know, that  $\mathfrak{A}$ ,  $\mathfrak{B}$ ,  $\mathfrak{C}$ ,  $\mathfrak{D}$ , and  $\mathfrak{E}$ , are Northern Signs, the rest  $\mathfrak{F}$ ,  $\mathfrak{G}$ ,  $\mathfrak{H}$ ,  $\mathfrak{I}$ , and  $\mathfrak{K}$ , are Southerly Signs, on the South side of the Equator.

Likewise  $\mathfrak{A}$ ,  $\mathfrak{B}$ ,  $\mathfrak{C}$ ,  $\mathfrak{D}$ , and  $\mathfrak{E}$ , are Signs ascending, in which the Sun is still approaching to us, and towards the North;  $\mathfrak{F}$ ,  $\mathfrak{G}$ ,  $\mathfrak{H}$ ,  $\mathfrak{I}$ , and  $\mathfrak{K}$ , are Signs descending.

Sixthly and Lastly, The Ecliptick is a great Circle, dividing the Globe or Sphere into Halves; it measures the Movements of the Planets, and they are placed within its compass, and are there to be found by their Longitude and Latitude. The Eclipses of the Sun and Moon are here limited and found, and many other Uses, which hereafter will more fully appear.

I will now say something of the Motion of the Moon, the Reason of the Eclipses of the Sun and Moon, of the Rising and Setting of the Stars,



of Time and that which appertains thereto; and lastly, I will sum up in brief what has been here delivered of the Sphere, and then come to the particular Uses thereof.

Of the Moon.

Dragon's Head  
and Tail.

I. The Moon has a particular Ecliptick to her self, which crosseth the Sun's Ecliptick in two places, that which comes to the Northward is called the *Head* of the Dragon, that to the South the *Tail* of the Dragon. The Moon's Ecliptick bendeth obliquely from the Sun's, and makes the Angle about 5 Degrees, so that as the Sun's Ecliptick declineth from the Equinoctial 23 Degrees 30 Minutes, in like manner these two Eclipticks do 5 Degrees.

So then the Moon moving in her Circle, near 13 Degrees each Day, she will go her own Ecliptick about in near 28 Days. But the Moon has some other Motions, which I defer 'till I treat of her in the Last Book.

Change of the  
Moon.

The Moon is seen after her Conjunction with the Sun (which is commonly called the Change) sometimes in two Days, and sometimes not before the fourth Day, which falls out for three Reasons, the first, because of her Obliquity; the second, by reason of her Latitude; the third, by reason of the unequal Motion of the Zodiac; which will be made clear in the Fourth Part or Book.

Phases.

Fig. 10.

The *Phases* of the Moon, or the several Shapes which she makes in one Revolution from the Sun, are gathered from the Tenth Figure; where let the Earth be A, ☉ the Sun; then have you 8 Phases, F will be the Full of the Moon, B is the Change when the Moon cannot be seen, D and d the Quarters; and so at any time of her Motion you will see her Face how to us, though the Sun doth enlighten more than half of her, because much bigger than the Moon.

Of Eclipses.

Eclipse of the  
Sun and Moon.

Fig. 11.

Fig. 12.

II. An *Eclipse* is the Obscuration of a Celestial Body from our sight, by interposition of some dark Body, and is generally taken notice of by us in the Sun and Moon.

The Eclipse of the Sun is made by the interposition of the Moon betwixt us and the Sun's Body, the Sun not concerned. The Eclipse of the Moon is an obscuration of the Moon's Body, by passing into the Shadow of the Earth made by the Sun, which will appear plainly if you consider Figure 11, where from the Earth the Moon takes away the Sight of some part of the Sun's Body, which we call the Eclipse of the Sun; and in Figure 12, the Moon passing into the Earth's Shade made by the Sun is totally Eclips'd.

Rising and Setting.

Cosmical Rising  
and Setting.

Cronical Rising  
and Setting.  
Helical Rising  
and Setting.

III. The *Rising* of a Star is when it appears above or at the Horizon on the East, and *Setting* on the West; and they are distinguished into *Poetical* and *Astronomical*. The *Poetical* is either *Cosmical Rising*, when any Star riseth at the same Moment that the Sun doth upon the Horizon; or *Cosmical Setting*, which is when any Star sets at the Moment when the Sun riseth. *Cronical* or *Evening Rising*, is when any Star riseth, the Sun setting. *Cronical Setting*, is when any Star sets with the Sun. *Helical Rising*, is when any Star, having been hid under the Sun's Rays, doth begin to appear. *Helical Setting*, is when a Star comes to be hid in the Sun's Rays.

Astro-

*Astronomical Rising and Setting*, is the Ascension or Descension of any Sign of the Ecliptick compared with the Equator, and is termed *Right* when a greater portion of the Equator riseth or setteth than the Degrees of the Sign; and *Oblique*, when a less.

*Astronomical  
Rising and Set-  
ting.*

IV. *Time* is either *Astronomical* or *Civil*, and is a certain Measure depending upon the Motion of the Luminaries, by which the Distance and Duration of things are measured.

*Time.*

And first, The *Astronomical Time* is that which is simply taken from the Motion of the Stars, and is a *Day* either *Natural* or *Artificial*. A *Natural Day* is the Time determined by the Sun's Motion in 24 Hours; an *Artificial Day* is the Time betwixt the Sun's Rising and Setting, to which is opposed the *Night*, that is the Time the Sun is under the Horizon, and is equal, that is of 12 Hours, when the Sun is in the Beginning of *Aries* and *Libra*, or unequal, when the Days are longer or shorter than the Nights, as in all the rest of the Signs; the longest Days and shortest Nights are when the Sun is in the Beginning of *Cancer*, and the contrary in *Capricorn*.

*Natural and  
Artificial Day.*

*Equal and un-  
equal.*

The Parts of the Days and Nights are *Hours*, the Day containing 24 Hours, and every Hour being divided into 60 Minutes, and every Minute into 60 Seconds, &c. and they begin to be numbered either from the Meridian or Horizon. Those that begin from Noon, and so to Noon again, of 24 Hours, are called *Astronomical Hours*, because Astronomers use these Hours in their Practice. But we, and many other *Europeans*, reckon but 12, viz. from Noon to Midnight 12, and from Midnight to Noon other 12 Hours.

*Hours.*

*Astronomical.*

Those that account their Hours from the Horizon, begin either at the Sun's Rising or Setting; if from the Sun's Rising, then they are called *Babylonish Hours*, and accounted from the Sun's Rising to it again 24 Hours: But those that account the Day from the Sun's Setting to its Rising again, and divide that space into 24 Hours, (as is now done in *Italy*) are called *Italian Hours*.

*Babylonish.*

*Italian.*

There is yet another Division, (as the *Jews* of old) that is the Day and Night, whether shorter or longer, from Sun's Rise to Sun's Setting, and so the Night is divided into 12 equal Parts, and these are called *Jewish Hours*, and are termed the *first Hour*, *second Hour*, *third Hour*, &c. of the Day or Night.

*Jewish.*

Time that is accounted from the Moon, is termed a *Month*, and is either *Periodical*, which is the Time the Moon is making from any Point of the Ecliptick to it again, which is in 27 Days and about 8 Hours; or *Sinodical*, which is from New Moon to New Moon in 29 Days and some odd Minutes.

*Month Peri-  
dical.*

*Sinodical.*

Time that is accounted from the Sun's Motion is that of a Year, and is either a *Sidereal Year*, wherein the Sun departing from a Fixed Star returns to it again, and that is in 365 Days 6 Hours and 9 Minutes; or a *Tropical Year*, which is the Space wherein the Sun passeth from any Point of the Ecliptick to it again, and that is in 365 Days 5 Hours and 12 Minutes.

*Year Sidereal.*

*Tropical.*

This Year again is divided into 12 Months by the *Romans*, viz. *January*, *February*, *March*, *April*, *May*, *June*, *July*, *August*, *September*, *October*, *November*,



November, and December; and the Days in each Month are known by these English Verfes.

Thirty Days hath September,  
June, April, and November;  
All the rest have Thirty One,  
Except February alone.

February in the Leap-Year has 29 Days, in the other 28. Whilst the Sun performs his Course under the Ecliptick in this Year, in every Month he enters into some one of the Twelve Signs of the Ecliptick, and what Day of the Month in general (for I speak not exactly) that shall be, these two Latin Verfes will shew near enough for common use, taken out of *Metius*.

☿ ☿ ♀ ♀ ♀ ♀  
Gaude, Christus adest, Titan apertissimus exit,  
♂ ♀ ☿ ♀ ♀ ♀  
Intro ibit Julius, impius exul erit.

Suns entrance  
into the Signs.

The Meaning thus, there are Twelve Words for the Twelve Months, the first *Gaude* for January, and so on to *Exit* for December. Over every Word stands the Sign appertaining to that Month, as ♀ for March, the third Word and Month; then observe with what Letter the Month begins, for if it be a Consonant, then it signifieth the Tenth Day; if with a Vowel, then consider that *a* is the first, *e* the second, and *i* the third Vowel, and to those Words or Months that begin with Vowels, you must add to 10 Days so many Figures as the Vowel intimates; as suppose for March, *adest*, here 1 Day must be added to 10, which makes the 11th Day of March for the Sun to enter into Aries, and so for October, *impius*, *i* is 3, and ten 13, which is that the Sun enters in the 13th of October. Again for February, *Christus*, because *c* is a Consonant, the Sun enters into ♀ the Tenth of February, and for any other Day of the Month, if for every day past the aforesaid day you add one Degree, it will give near the Degree of the Ecliptick the Sun is in that Day. Example, I desire to know what Degree and Sign the Sun is in the second Day of June. First, I seek what Day of May the Sun entered into ♀, for so *Apertissimus* intimates, and *a* tells me the Eleventh Day, then I account how many Days betwixt the 11th of May and the second of June, which by considering that May hath 31 Days (as before was taught) it will be 22 Days; and therefore the Sun will be in 22 Degrees of ♀.

Civil Time.

Secondly, for the Civil Time, which is the Astronomical accomodated to vulgar uses, as from the Sun the Julian Year which is either Common or Bissextile.

Common Year. The Common Year contains 365 Days.

Bissextile. The Bissextile or Leap-year contains 366.

Both

Both these Years are divided into 4 Quarters, viz. the Spring, Summer, Autumn, and Winter; or into Months, which are 12, before recited; or into Weeks, every one of 7 Days; or into Days, and these are either Festival Days or Working Days.

And because I am now upon the Civil Account or Kalender, I will here, very shortly and plainly, in some few Problems, shew you how to find out the Years, whether Leap-Year or Common, with the Moveable Feasts, Moon's Age, and the like, where I shall borrow from my good Friend, and worthy Astronomer, Mr. Thomas Street, his Memorial Verfes concerning the Kalender, which will both please and fit my young Scholar for this Matter.

Prop. 1. To find whether the Year of our Lord be Leap-Year, or the first, second, or third after.

Rule.

Divide the Year by 4; what's left shall be,  
For Leap-Year 0, for past 1, 2, or 3.

Here you may omit the Hundreds and Twenties of the Year of our Lord, Leap-Year and only divide the Residue by 4. Example, 1678, omitting the Hundreds and Threecore, I divide the Residue 18 by 4, and there remains 2, which is the second after Leap-Year.

Prop. 2. To find the Golden Number, the Cycle of the Sun, and Indiction.

Rule.

When 1, 9, 3, to the Year hath added been,  
Divide by 19, 28, 15.

The Golden Number is a certain Figure from 1 to 19, which was so placed in the ancient Kalender, that it might shew the Day of each Month wherein the Moon changed, and being written in Gold got that Name; for the New Moons return to the same Day of the Month every 19 Year.

The Cycle of the Sun is a Number of 28 Years, in which the Dominical Letter returns in a Cycle.

The Indiction is the Space of 15 Years, which sometimes shewed the Year wherein the Roman Tribute was to be paid.

Examples by the former Rule for the Year 1678.

To 1678 adding 1, it makes 1679, which divided by 19, there remains 7 for the Golden Number.

To 1678 adding 9, it makes 1687, which divided by 28, there remains 7 for the Cycle of the Sun.

To 1678 adding 3, it makes 1681, which divided by 15, there remains 7 for the Indiction.

T

Prop.



## Prop. 3. To find the Dominical Letter.

Rule.

Divide the Year, its Fourth, and 4, by 7,  
What's left, subtrakt from 7, the Letter's given.

Dominical  
Letter.

For if you account *A* 1, *B* 2, *C* 3, *D* 4, *E* 5, *F* 6, and *G* 7, the Number found by the Rule will be the Dominical Letter; as for Example; to find the Dominical Letter for the Year 1678. The Fourth of 1678 is 419, and 4 and 419 added to 1678 makes 2101, which divided by 7 leaves 1, and that taken from 7, there remains 6, which is *F*, the Dominical Letter for the Year 1678.

But the Leap-Year hath two Dominical Letters, the latter found by this Rule serveth from St. Matthias Day to the Years End, the former (next following in order from *A* to *G*, and beginning again at *A*) serveth from New-Years Day to St. Matthias.

## Prop. 4. To find the Epact, the Prime or Golden Number being given.

Rule.

Divide by 3; for each one left add 10,  
30 reject, the Prime makes Epact then.

Examp.

Example for the Year 1678, the Golden Number was before found to be 7, which divided by 3 leaves 1, that by the Rule call 10, which added to 7 makes 17, the Epact desired.

## Prop. 5. To find the Age of the Moon, or the Day of her Change.

Rule.

J. F. M. A. M. J. J. A.  
Janus 0, 2, 1, 2, 3, 4, 5, 6,  
S. O. N. D.  
8, 8, 10, 10, these to the Epact fix,  
The Sum (bate 30) to the Month Day add,  
Or take from 30, Age or Change is had.

Age and change  
of the Moon.

Over every Figure in the Rule, you have the first Letter of the Month in order, as *January*, *February*, *March*, &c. which Figure being added to the Epact, gotten by the foregoing Proposition, the Sum if it be less than 30, or else the Excess above 30, added to the Day of the given Month, (rejecting 30 if need be) gives the Age of the Moon that Day; but subtracted from 30, leaves the Day of the Change in (or from the Beginning of) that Month.

For the Day of the Full Moon, add or subtract 15 to or from the Day of the Change.

Exam-

## Example 1. To find the Age of the Moon, May 29, 1678.

The Number for the Month is 3, for you find that Number in the Rule under *M*. for *May*, which added to the Epact 17 makes 20, and that added to 29 (the Day proposed) makes 49; rejecting 30 there remains 19, which is the Age of the Moon the 29th of *May*, 1678.

## Example 2. To find the Day of the Change in May, 1678.

The Epact 17 being added to 3 for that Month makes 20, as before, which subtracted from 30, there remains 10, for the Day of the New Moon in *May*, 1678.

Add 15 to 10, and it makes 25, for the Full Moon.

These Rules must be learnt perfectly, for hereafter there will be great use made thereof.

V. The Sum of all that I have said, concerning the Circles of the Sphere or Globes, comes to this:

1. The *Horizon* or *Finitor*, divided into 4 Quarters by the Points of East, West, South, or North, each Quarter into 8 Points, making in all 32 Points, or each Quarter into 90 Degrees, accounted either from East or West towards South or North, or else from South or North towards East or West. The Poles of this Horizon are the Zenith over our Heads, and the Nadir directly under us; and these being 90 Degrees from it, the Circles drawn from Zenith to Nadir by every Degree of the Horizon, are called Vertical Circles; that which passeth by North and South, is likewise the Meridian Line; that by East and West, the Prime Vertical; the rest, Vertical Circles, or Azimuths; and all those parallel to the Horizon, Circles of Altitude, or Almucanters; and the Eighteenth Circle under the Horizon, the *Crepusculum*, or Circle of Twilight.

2. The *Equinoctial*, or *Equator*, a great Circle divided into 360 Degrees, *Equinoctial* beginning at the first Point of *Aries*, where the Ecliptick crosseth it, and so numbred round about. The Poles of this Circle are the Poles of the World, the Artick or North Pole elevated to us, and the Antarctic or South Pole not seen. The Circles that pass from one Pole to the other, through every Degree of the Equinoctial, are called Meridians or Hour Circles, and the chief is that which passeth by the Zenith, called the Twelve of the Clock or Chief Meridian, and another which passeth in the Middle by Six of the Clock and the Points of East and West, called the Meridian of Six of the Clock. The Circles, which are lesser Circles, and parallel to the Equinoctial, are called the Parallels; those which are 23 Degrees 30 Minutes from it, are called the Two Tropicks, one next the North Pole called the Tropic of *Cancer*, that next the South the Tropic of *Capricorn*; those within 23 Degrees 30 Minutes of each Pole, the Artick and Antarctic Circles.

T 2

3. The



Ecliptick,

3. The *Ecliptick*, a great Circle divided into 12 Signs, each Sign into 30 Degrees, in all into 360 Degrees. The Poles are in the Arctick and Antartick Circles, it crosseth the Equator in the Beginning of  $\gamma$  and  $\epsilon$ , and deviateth 23 Degrees 30 Minutes from it, in the Beginning of  $\otimes$  and  $\psi$ , and maketh an Angle of the same Degrees with it. Those Circles which come from the Poles of the Ecliptick, and pass through each Degree of it, are called Circles of Longitude, one of these is a Meridian, and is called the *Equinoctial Colure*, passing by the Poles of the World and the Beginning of  $\gamma$  and  $\epsilon$ : The *Solstitial Colure*, is a Meridian passing by the Beginning of  $\otimes$  and  $\psi$ .

Equinoctial  
and Solstitial  
Colures,

These three Circles, the Horizon, the Equinoctial, and the Ecliptick, with their Circles passing by their Poles, and parallel to them, are all alike, and altering their Position may serve for one another. This being considered and known, I come to the particular Uses, not only of the Globe and Sphere, which I account were invented to help the Fancy, and not for real use, because cumbersome, troublesome, and uncertain; but also of the *Analemma*, and Operation by Scale and Compas, and by Spherical Triangles: And I shall not ramble into an abundance of Propositions, but keep within the Bounds of a very few Triangles, shewing how they are found and posited, both upon the Globe and *Analemma*, and so carrying on this Practice, that what goes before may illustrate and explain what follows. And because Observations are supposed in some things to precede and to be given, I will begin with them, and shew what first is to be gotten, to obtain those which follow.

## SECTION III.

*Propositions and Problems particularly concerning the Celestial Spheres.*

## Problem I.

Of these Three; 1. The Length of a Stile perpendicularly erected upon an Horizontal Plain, 2. The Length of the Shadow upon the Plain, called the Right Shadow, 3. The Altitude or Height of the Sun above the Horizon: Any Two being given, to find out the Third.

IT is requisite that the Horizontal Plain be tryed with a Level, and the Perpendicular by a Square, for then this Analogy will perform the Problem, As the Length of the Stile, to the Length of the Shadow :: So is Radius, to Co-tangent of the Altitude of the upper Edge of the Sun. These four Parts may be varied so, as to put any

of

## Sect. 3.

## Of Cosmography.

of the Terms into the last Place; which I again propose, that you may be perfect in that necessary Rule; for let the Stile be  $\beta$ , the Shadow  $\beta$ , and the Height  $ht$ , then the former Analogy will be thus,

$$\beta . \beta :: R . \text{Co-tang. } ht \circ$$

Again,

$$\text{Co-tang. } ht \circ . R :: \beta . \beta$$

Again,

$$R . \text{Co-tang. } ht \circ :: \beta . \beta \quad \text{And so of any other.}$$

For the Perpendicular Stile, the Right Shadow, and the Beam proceeding from the upper Edge of the Sun, are the three Sides of a Right-angled Plain Triangle, and the Angle at the Plain is the Angle of the Altitude, the Complement whereof is the Angle at the Top of the Perpendicular; as in Figure 13, CA is the Stile, AB is the Shadow, and CD a Beam proceeding from the upper Edge of the Sun, which make the Right-angled Plain Triangle CAC, wherein the Angle ABC is the Angle of the Sun's Altitude, the Angle C its Complement; and by the former Problems of Right-angled Triangles, you may Resolve it: either by Scale and Compas, or by Calculation.

And here is to be noted, That the End of the Shadow that can be discerned cometh from a Beam that proceedeth from the upper Edge of the Sun,  $\omega$ z. the Beam SCB, and not from the Center of the Sun represented by the Line iCD, and that because the part of the Shadow BD is not to be discerned, being enlightened by the upper Semidiameter of the Sun iS. If therefore you would have the true Altitude of the Sun, that is, of his Center i, you must subtract the Semidiameter of the Sun iS, or the Angle BCD, (being about 15 Minutes) from the Altitude thus found by the right Shadow, and you will have the true Altitude.

Again, for the same Reason, if you would have the Length of the Stile, or Shadow, you must add 15 Minutes of a Degree to the true Altitude, that you may have the Altitude of the upper Edge of the Sun, which determineth the right Shadow.

And no way differing would it be, if the Stile were fixed upon a Perpendicular or Vertical Plain, the Shadow would then be a Verfed Shadow, and the Angle for the Height of the Sun would be the Angle at the Stiles Top.

## Problem II.

*To take the Height of the Sun or Star by a Quadrant.*

YOU were taught Chapter II. Section 4. how to use a Quadrant, whether fixed, or loose in your Hand, and the same I shall not need to repeat now; only, in taking the Height of the Sun, hold the loose Quadrant with its Edge towards the Sun, and move it so, as a Beam of the Sun may shine

Height of the  
Sun or Star.



shine through one Sight upon the other, at a Mark appointed; then if the Thread with the Plummets play easily by the Side, so as it stick not upon the Quadrant, the Thread shews the Sun's Height upon the Limb. But if you would take the Height of a Star, or the Moon, then holding the Quadrant up, so as the Plummets may play freely, and directing the upper Edge of the Sights upon the Star, the Thread then stopp shews the Height. This practised will shew all things easily.

This same may be done by the Astrolabe, which is a whole Circle, after the same manner.

## Problem III.

*To draw a Meridian Line upon an Horizontal Plain.*

Fig. 14.

1. Way. **U**Pon any Plain, tried to be Horizontal by a Level, from any Center about the middle, with your Compasses describe Arches at convenient distances, as you see in Figure 14, from the Center A, the Stile is AF, set up perpendicularly by the help of a Square; then observe in the Forenoon, about 9 of the Clock, when the Shade of the Top of the Stile F shall fall in any one of the Circles, as here in the second at B; when this is done, come again about the Hour in the Afternoon that shall be equally distant from Twelve of the Clock, as suppose if your first Observation was about 9 of the Clock, the second will be about 3 in the Afternoon, (or a little before, left the time be past) and then observe when the Shade of the Top of the Stile falls into the same Circle as before, as here at C; then, if with your Compasses you divide the Distance BC into Halves at D, the Line AD will be a Meridian Line.

2. Way. By taking the Height of the Sun about 9 of the Clock with the Quadrant, and as before having drawn the Line of the Sun's Shadow, made by an upright Stile upon an Horizontal Plain, at length, for now it makes no matter for the Shade of the Top of the Stile; observe in the Afternoon, when the Sun comes to the same Height, if then you draw out the Shade, the Middle betwixt these two Lines is the Meridian Line, as in the last Proposition.

3. Way. By the Pole-star, or rather by the Pole itself, and two small Cords, one hung up upon the End of some Tree or Beam, and going back, hang the other Cord so, as a Line imagined to be drawn by them by the Eye would pass into the Pole, then are those two Lines in the Meridian. You were taught before in the first Section of this Chapter, how to find very Point in the Heavens where the Pole is.

4. Way. The Distance from the Pole-star to the Pole, is now 2 Degrees and 25 Minutes, and the Pole lies in a direct Line betwixt the Pole-star and *Alioth*; if therefore you cut but off from the Pole-star in that Line 2 Degrees and 30 Minutes, which you may do many ways, you may thereby set off a Meridian Line, as before in the third Way.

Problem

## Problem IV.

*To get the Height of the Pole.*

1. Way. **I**F either by the Pole-star, or any other Star which never sets, but is always in sight, you take with your Quadrant its highest Altitude above the Pole, and its lowest under, these two Heights added together, the Half thereof will be the Height of the Pole above the Horizon, allowing for Retraction, as you shall presently be taught.

2. Way. When *Alioth*, or the Thill-Horfe of *Charles's Wain* in the *Great Bear*, comes into the Meridian under the Pole, take the Height of the Pole-star, and out of that Height subtract the Distance of the Pole-star from the Pole, which is now  $2^{\circ} 25'$ , the Remainder will be the Height of the Pole.

## Problem V.

*To find by Observation, the Distance of the Tropicks, the greatest Declination of the Sun, and the Altitude, or Elevation of the Pole above the Horizon.*

**T**AKE the Altitude of the Sun above the Horizon, just at high Noon, when he is the nearest to us in the Summer Solstice, in the Tropick of *Cancer*, (which is on the Eleventh of *June*,) and also when he is in the Winter Solstice, or Tropick of *Capricorn*, (which is upon the Eleventh of *December*,) then subtract the lesser of these Altitudes from the greater, and the Remainder is the Distance of the Tropicks, half of this Remainder is the greatest Declination of the Sun, which being subtracted from the greater Altitude, or added to the lesser, either way, there will be left the Height of the Equinoctial, the Complement of which is the Altitude or Elevation of the Pole above the Horizon. When the Globe is rectified, and set to the Elevation of the Pole here at *London*, which is found by Observation to be 51 Degrees 30 Minutes, if you shall stand upon the East part of it, and imagin every part of it to be pressed down upon the Plain of the Meridian perpendicularly, then will it form that Projection called the *Analemma*, all the Meridians will be *Ellipses*, except the Meridian of Twelve, which is the outmost Circle, and is the Plain whereon it is drawn, and the Solstitial Colure; and the Meridian of Six of the Clock, which is a straight Line, and represents the Equinoctial Colure: And I would have the Youngs to be set to draw this Projection, and be shewn how it represents the Globe; as for Example in Figure 15; upon any Paper and bigness, as you please, draw a Circle, which let it represent the Brasse Meridian in the Globe, then by the Center draw a Diameter HO, which let represent the Horizon, the Center V will be the Point of East and West upon the Horizon, H will be

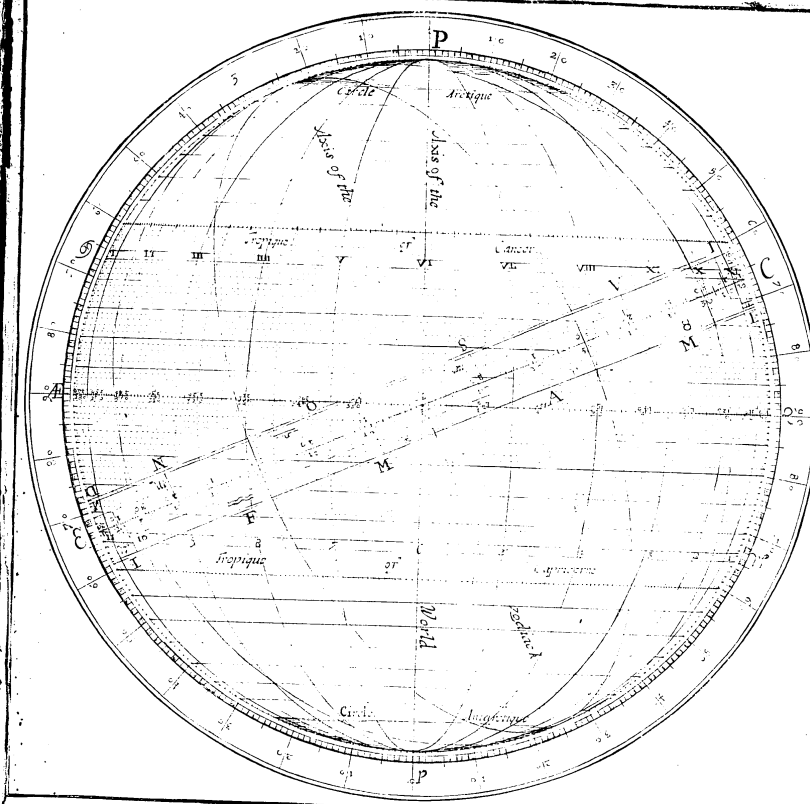
*Analemma.*

Fig. 15.



be the South Point, and O the North. Now for *London*, where the Pole is Elevated  $51^{\circ} 30'$ , if you have a Line of Chords, or a Circle divided, of that Radius, (which you have been fully instructed how to do) take from it  $51^{\circ} 30'$ , and set it from O to P the North Pole, draw  $P\gamma p$  for the Six of the Clock Hour-Line, it is the Equinoctial Colure, and p is the South Pole, then take 90 Degrees from your Circle or Chord-Line, and set it from H or O to Z and N, and from P to E or Q, so shall Z be the Zenith, N the Nadir, or the two Poles of the Horizon, and ZVN is the Prime Vertical Circle, or the Azimuth of East and West; from the Point E, which is 90 Degrees from the Poles, draw EQ for the Equinoctial Circle, E on the Meridian above the Horizon, and Q below; then, because by the best Observations the greatest Declination of the Sun is found to be  $23^{\circ} 30'$ , take those from the Circle divided, and prick it off from E to E, and from Q to C, and draw EVC for the Ecliptick, the Center V will be the Equinoctial Point, and the Place of  $\gamma$  and  $\Delta$  in the Ecliptick, E will be the Point of  $\mathcal{S}$ , and C of  $\mathcal{W}$ ; then from E draw E $\mathcal{S}$ , parallel to EQ the Equinoctial, it will be the Tropick of *Cancer*, and draw from C another Parallel, it will be C $\mathcal{W}$  the Tropick of *Capricorn*. The Poles of the Ecliptick will be 23 Degrees 30 Minutes from the Poles of the World, at n and m. And so much for this Figure at this time, which if moderately understood will conduce much to the Knowledge and Practice of the Globe or Sphere; for it will explain the last Proposition very exactly; for supposing the greatest Meridian Height of the Sun the Eleventh of June was HE, the least the Eleventh of December H $\mathcal{W}$ , now if I take H $\mathcal{W}$  from HE, it will leave  $\mathcal{W}$ E the Distance of the Tropicks, and half of that will be AE or AE $\mathcal{W}$  the greatest Declination of the Sun, and forms the Angle that the Equinoctial makes with the Ecliptick AE $\gamma$ E, which is found to be  $23^{\circ} 30'$ , and constantly so; now the second part of the Problem bids you to take the half of the Distance of the Tropicks equal to AE from the greater Height HE, or add it to the lesser Height H $\mathcal{W}$ , it shall give the Height of the Equinoctial HE, which is very plain from the Figure; lastly, that this Equinoctial Height is equal to the Complement of the Poles Height is thus cleared, PQ is equal to 90 Degrees, PO is the Poles Height, which taken from PQ, leaves OQ its Complement. But OQ is equal to HAE, (because the Head Angle O $\gamma$ Q is equal to the Angle AE $\gamma$ H,) but HAE is the Height of the Equinoctial, and therefore the Complement of the Height of the Pole. Lastly, observe what I said before, that the greatest Obliquity of the Ecliptick, or the greatest Declination of the Sun is found by diligent observation to be  $23^{\circ} 30'$ , equal to the Angle AE $\gamma$ E, or Q $\gamma$ C, and that the Poles Height at London is  $51^{\circ} 30'$ .

## Problem



between page 144 and 145 Cosmog



## Problem VI.

*Of these Three ; 1. the Meridian Altitude of the Sun or Star. 2. the Elevation of the Pole, and 3. the Declination of the Sun or Star : any Two being given, to find the Third.*

**I**F the Meridian Altitude be to be taken in the South Quadrant of the Meridian Line ZH, then,

1. Altitude of the Equinoctial, less the Meridian Height, is equal to the Declination South.
2. Meridian Altitude, less the Altitude of the Equinoctial, is equal to the Declination North.

But if the Meridian Altitude be in the North Quadrant of the Meridian Line ZO, then,

1. Poles Elevation, less by the Meridian Altitude, is equal to the Complement of the Declination North.
2. Meridian Altitude, less by the Poles Elevation, is equal to the Complement of the Declination North.

## Problem VII.

*Of these Five ; 1. the greatest Declination of the Sun, 2. the Longitude of the Sun from the next Equinoctial Point, 3. the Right Ascension of the Sun from the same Equinoctial Point, 4. the Declination of the Sun in that Place, and 5. the Angle that the Ecliptick makes with the Meridian ; any Two being given, to find out the rest.*

**T**HIS Proposition brings me to the Use of the Globe or Sphere, and to the Use of the *Analemma*, whether by Scale and Compass, or by the Projection which I have fitted for Use, and likewise to the Practice of Spherical Triangles; for when the Work is thus carried on, it will give more knowledge, and make the Scholar more perfect. I will therefore explain the Business first upon the Globe.

1. The Globe fixed only in the Meridian, without any consideration had to the Horizon at all, performs this Problem, and therefore needs not rectifying.

2. The *Analemma*, made on purpose, and fitted on Pastboard, where the Horizon HO is fixed fast, and the Meridian, with the Equinoctial, its Parallels and Hour-Lines, with the Ecliptick, move about the Center, and are to be rectified and raised for the Elevation of the Pole, even as the Globe, and is very easie to be understood, which is all I aim at. For the making and drawing of it, if you know how to divide the Diameters, and



which I shewed you in the Doctrine of *Plain Triangles*, according to a Line of Sines, as these are done, there is no further difficulty but in the Ellipses, which will not now be material to reach you.

3. By Scale and Compass, the Work is declared before in the Fifth Problem, and shall be explained again as need requires.

4. By Spherical Triangles, the Doctrine is already delivered in the Fourth Chapter, and thereto reference shall be made.

The Terms of this Problem are thus explained:

1. The greatest Declination of the Sun is 23 Degrees 30 Minutes, and the present Declination of the Sun, or any Star, is how many Degrees and Minutes they lye from the Equinoctial, and that is known by the Parallel that passeth by them.

2. The Longitude of the Sun, or of any Point of the Ecliptick, from the next Equinoctial Point, is the Distance therefrom in Degrees and Minutes. The Sun's Longitude tells in what part of the 12 Signs he then is, suppose in  $4^{\circ}$  and  $40'$  of *Taurus*; but to fit all for Calculation, it is required to know how far we are from the Beginning of *Aries* and *Libra*, as in the former Example, the  $4^{\circ}$   $40'$  of *Taurus* is  $34^{\circ}$   $40'$  from the Beginning of *Aries*, for the Sign *Aries* is  $30^{\circ}$ , which added to  $4^{\circ}$   $40'$  of *Taurus*, makes the aforesaid Longitude. Therefore in the first Quarter of the Ecliptick, (*Aries*, *Taurus*, and *Gemini*,) turning the Signs into Degrees, it is without alteration; in the second Quarter, (*Cancer*, *Leo*, and *Virgo*) turn the Signs into Degrees from *Aries*, and subtract them from  $180^{\circ}$ , it leaves you the Distance from the Equinoctial Point of *Libra*. The like is to be observed in the other two Quarters, to find the Longitude sought from the two Points of *Aries* and *Libra*.

3. The Right Ascension of the Sun, or Star, is that Arch of the Equinoctial, contained betwixt the Beginning of *Aries*, and the Point of the Equinoctial that comes to the Meridian with the Sun or Star. And this is the Regulator of all the uneven Motions upon the Pole of the Ecliptick. But when the Right Ascension is found always less than  $90^{\circ}$ , and that is accounted from the next Equinoctial Point, you must observe,

The Right Ascension of the Sun from the next Equinoctial Point,	[In the first Quadrant, without alteration,	Is the true Right Ascension from the Beginning of <i>Aries</i> .
	In the second Quadrant, being subtracted from $180^{\circ}$ ,	
	In the third Quadrant, being added to $180^{\circ}$ ,	
	In the fourth Quadrant, being subtracted from $360^{\circ}$ ,	

*Note also*, That the whole Right Ascension, or  $360^{\circ}$ , or Part, is required often to be turned into Time, and so sometimes the Time to be turned into Degrees and Minutes. To do this, you must reckon for every 15 Degrees 1 Hour, every Degree 4 Minutes of Time, and every Minute 4 Seconds,

Seconds, and contrarily; so that if you divide the whole Degrees by 15, it gives the Hours, and the Remainder as before will give the Minutes, and contrarily, multiply the Hours by 15, and the Minutes by 4, &c. it gives the Degrees. However in the third Book you have Tables to do the same. These Hours and Minutes of the Right Ascension, shew the Time, how long the Sun, or any Point, cometh to the Mid-heaven, or the South Part of the Meridian Line, after the Beginning of *Aries*.

Having cleared the Terms, we come to the Resolving the Problem.

#### 1. By the Globe.

This Problem, respecting only the Ecliptick and Equator, may be performed by the Globe and Meridian only. Suppose then, for an Example, that on April 14, 1678, at Noon, it be demanded to give the Sun's Place, his Declination and Right Ascension; first, upon the Horizon of the Globe (where there is a Kalender for the Sun's Place answering the Days of the Month) I seek for the 14 of April, and just against it I find 4 Degrees and about  $30'$  of *Taurus*, for the Sun's Place that Day in the Ecliptick, he having moved and crept along, as I familiarly instanced before, from the First of *Aries*, where he was the Tenth of March before, to the Fourth Degree of *Taurus*, that is near a Degree of the Ecliptick in a Day, so that in about 34 Days the Sun's Longitude will be from *Aries*  $34^{\circ}$   $30'$ . Then I come to the Globe, and in the Ecliptick seek for  $4^{\circ}$   $30'$  of *Taurus*, and bring it to the Meridian, and telling the Degrees upon the Meridian (under the fiducial Edge, or that divided) betwixt the Ecliptick and Equinoctial, I find them 13 Degrees and something more, and that is the Declination; and at the same time find what Point of the Equinoctial the said Meridian cuts, which is 32 Degrees and almost an half, for the Sun's Right Ascension. Lastly, I consider how all this comes to pass, and find out the Spherical Triangle, which is made by the Ecliptick, from the Beginning of *Aries* to the  $4^{\circ}$   $30'$  of *Taurus*, for one side; by the Equinoctial, from the said Point to the Meridian, for another side; and by that Part of the Brass Meridian, contained betwixt the Ecliptick and Equinoctial, for the third side. And in this Triangle are the Five Parts of the Problem contained, viz. BC the Longitude of the Sun, BA his Right Ascension, CA the Declination, the Angle at B  $23^{\circ}$   $30'$  the greatest Declination, which is always the same, and the Angle at C  $70^{\circ}$   $15'$ , which we shall not here meddle withall. You must note, That any Two of those Five Parts will find the Three remaining by the Globe; for by the Sun's Longitude or present Declination you might find the Right Ascension and greatest Declination, or by the Right Ascension and Declination, or any two, the rest might be found, by bringing the Parts to the Meridian, and working as before. And there might be 16 several Varieties thereof.

*Sun's Place in the Edge of the Ecliptick.*

*April 14, the Sun's Place in 4 deg. 30 min. of Taurus.*

*Sun's Longitude.*

*Sun's Declination.*

*Sun's Right Ascension.*

*Fig. 16.*



## 2. By the Analemma, or Instrument.

If you seek the Day of the Month on the Out-lines of the Zodiac, there will be answering in the Ecliptick Line (that is in the midst of the Zodiac the Sun's Place) 4 Degrees 30 Minutes of *Taurus*, which is distant  $34^{\circ} 30'$  from the Beginning of *Aries*. Mark the Meridian that comes from the Pole P, and falls upon that Point, or imagin one, and you will find it cuts the Equator in  $32^{\circ} 15'$  for the Right Ascension; then tell the Parallels from the Equinoctial to the Sun's, and you will find that which passeth through the Sun's Place to be 13 and a little more, which is the Declination; and there you may find the aforelaid Spherical Triangle, from the Center, or *Aries*, to those Places; and by any Two of the Five Parts in the Problem you may find the rest.

## 3. By Scale and Compass.

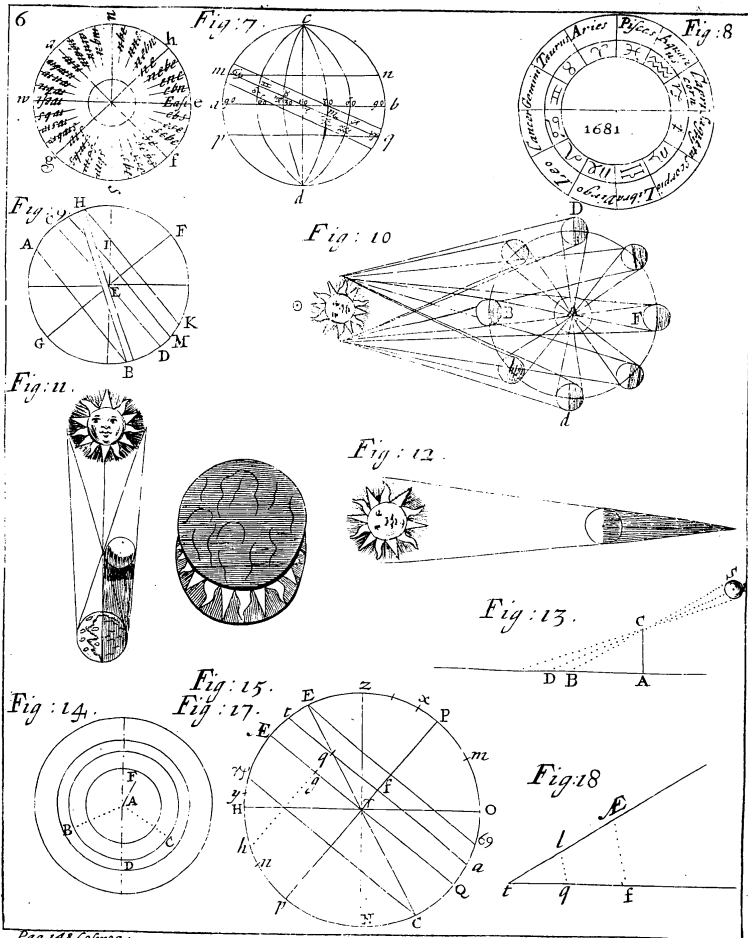
By the Line of Chords, or a Circle divided, as you did in Figure 15 to note in this Figure 17, draw the Out-circle for the Meridian, and draw the Equinoctial and Ecliptick, and mark their Poles, then by the *Latin Verses*, or by your Almanack, or some such way, you may find the Sun's Place to be 4 Degrees 30 Minutes of *Taurus*, that is  $34^{\circ} 30'$  Minutes from the Beginning of *Aries*. From *m* and *n*, the Poles of *EC*, set off  $34^{\circ} 30'$  either way to *x* and *y*; lay a Ruler to *x* and *y*, and crossing *EC* at *q*, there is the Sun's Place. By *q* draw a Parallel to the Ecliptick *fa*, and you will find *AE* or *Qq* the Declination to be  $13^{\circ}$  and something more; and if you divide the Radius of the Equinoctial *AE*, like as the Radius of the Parallel *ft* is already divided, thus, draw a Line at length, in which set off *tf* equal to *ft*, and *tq* equal to *tq*, make what Angle you please, as *ftE*, set off *tE* for the Radius of the Equinoctial, and draw *fE* and *ql* parallel, let *tl* from the Center *T* to *q*, raise a Perpendicular from *q* to the Equinoctial, the Distance from that Point *h* to the Pole *P* is the Degrees answering to the Right Ascension  $32$  Degrees  $15$  Minutes. All which may be varied to any Two of the given Parts in the Problem to find the rest.

## 4. By Calculation.

The Spherical Triangle on the Globe *ABC*, or in the Instrument *rqf*, is Right-angled at *A* or *l* by the Meridian falling on the Equator, the Hypotenuse *BC* is the Longitude  $34^{\circ} 40'$ , (found in an *Ephemeris* of the Sun,) the Angle at *B* is the greatest Declination  $23^{\circ} 30'$ , always constant; *BA* is the Right Ascension, and *CA* the present Declination.

Now if the Right Ascension be sought,

There





There is given the Hypothense  $BC$   $34^{\circ} 40'$ , and the Angle at  $B$   $23^{\circ} 30'$ ; To find the Side  $BA$ .

If you remember, it is the second Proposition and second Variety of *Right-angled Spherical Triangles*, by the Hypothense and Angle adjoining to find the Side adjoining to that Angle. And the Rule is,

As Co-sine  $B$  . Radius :: Co-tangent  $BC$  . Co-tangent  $BA$

That is, if you add the Logarithm of the Co-tangent  $BC$  to the Radius, and subtract the Co-sine of  $B$ , it will leave you the Co-tangent of  $BA$ .

Radius	10,000,000
Co-tangent $BC$ $34^{\circ} 40'$	10,160,162
Co-sine $B$ $23^{\circ} 30'$	9,962,398
Co-tangent $BA$ $32^{\circ} 23'$	10,197,764

Calculation of  
the Right Ascen-  
sion.

Thus the Right Ascension will be found to be  $32^{\circ} 23'$ , and if you will take the pains, a Table of Right Ascensions may after this manner be Calculated; but this is done to your hands for every Degree of Longitude.

To find the Declination of  $34^{\circ} 40'$  of Longitude,

There is given the Hypothense  $BC$ , and the Angle adjoining  $B$ ; To find the side opposite to the Angle given  $CA$ .

By the aforesaid second Proposition of *Right-angled Triangles* and the first Variety, the Rule is,

As Radius . Sine  $BC$  :: Sine  $B$  . Sine  $CA$

That is, add the Sine  $BC$  to the Sine  $B$ , and take away the Radius, and it gives the Sine of  $CA$ .

Sine $BC$ $34^{\circ} 40'$	9,754,960
Sine $B$ $23^{\circ} 30'$	9,600,699
Sine of $CA$ $13^{\circ} 07'$	19,355,659

Declination.

Thus you find the Declination to be  $13^{\circ} 07'$ ; and after this manner the Table of Declinations in the second Book was made.

And in the Right-angled Triangle  $BAC$ , any Two Parts of the Problem will find Three more, and make 16 Varieties; all which were the Examples in the 6 Propositions of *Right-angled Triangles*, and 16 Cases, where you will find them all wrought, to which I refer you. And what has been said of the Sun, is explicable of the Stars.

Problem



## Problem VIII.

Of these Three; 1. the Right Ascension of the Sun, 2. the Hour of the Day, and 3. the Right Ascension of Mid-heaven; any Two being given, to find out the Third.

I shewed you before, how the Equinoctial might be either divided into Degrees, as it is upon the Globe, or else (being that is the Measure of Time) into Hours, Quarters, and Minutes, every 15 Degrees being an Hour, and so the whole into 24 Hours, for 15 times 24 is 360 Degrees. Therefore first know, that if you add the Sun's Right Ascension in Time, to the Time from Noon, the Sum will be the Right Ascension of Mid-heaven, or the Right Ascension of the Point of the Ecliptick, that at that very Point of Time is in the Meridian. But if it be required to have the Right Ascension of Mid-heaven in Degrees and Minutes, then turn the Time from Noon into Degrees and Minutes, by multiplying the Time by 15, as before was shewed, and it gives your desire. Example of the 14th of April, 1678, at Half an Hour past 4 in the Afternoon: The Time past Noon is 4 Hours and an half, which is  $67^{\circ} 30'$ , for 4 times 15 is 60; and the half of 15 is 7½, in all  $67^{\circ} 30'$ : The Right Ascension of the Sun before was found to be  $32^{\circ} 23'$ , that is, 2 Hours, 9 Minutes, and 32 Seconds, for 30 Degrees is twice 15°, which is 2 Hours, and 2 Degrees is 8' of Time, and 23 Minutes is 92' of Time, that is 1° 32', in all 2 Hours, 9' 32"; so that the Right Ascension of Mid-heaven is 6 Hours, 39', and 32", and in Degrees  $99^{\circ} 53'$ .

Now to find the Hour of the Day by the Right Ascension of the Sun, and the Right Ascension of Mid-heaven, if you subtract the former from the latter, it gives the Answer in Degrees, or in Time, as you please.

If you would know the Right Ascension of any Star, then observe diligently, by some exact Clock, Watch, or Hour-Glass, the Time betwixt the Star's coming to the Meridian at South, after the Sun, that is, at what Time after High-Noon the Star cometh to the Mid-heaven, for the Right Ascension of Mid-heaven at that time is also the Right Ascension of that Star that is in the Mid-heaven; therefore the Right Ascension of the Sun, more by the Time of the Star's Southing, is equal to the Right Ascension of the Star.

## Problem

## Problem IX.

Of these Five; 1. the Elevation of the Pole, 2. the Declination of the Sun or Star that may Rise or Set, 3. the Amplitude Orive or Occasive of the Sun or Star, 4. the Ascensional Difference of the Sun or Star, and 5. the Angle at the Sun or Star, shewing the Position thereof, in respect of the Pole of the world, and the North Part of the Horizon; any Two being given, to find any one of the rest.

First I shall explain the Terms not formerly mentioned, that is, the Amplitude Orive, which is the Degrees and Minutes of the Horizon, contained betwixt the Point of East and the Point of the Horizon where the Sun or Star riseth, or if you will go by the Mariners Account, the Point of the Sea-Compass, or one of the 32, where they Rise. Or if the Amplitude Occasive be required, it is the same on the West side from the Point of West.

The Ascensional Difference, is the Time, or Degrees and Minutes of the Equinoctial, that is contained betwixt the Hour of Six, either Morning or Evening, and the Time of the Sun or Star's Rising or Setting.

The Angle at the Sun or Star, is what Angle the Meridian makes there with the Horizon.

## 1. By the Globe.

Let the Example be the 14th of April, 1678. the Sun's Place 4 Degrees and 40 Minutes of Taurus.

This Problem compares the Equinoctial, its Parallels and Meridians, with the bare Horizon; therefore if the Sun's Place be given, the Declination is  $13^{\circ} 7'$ , and the Poles Height at London  $51^{\circ} 30'$  as before. Now therefore I must rectifie my Globe, first to the Latitude, by lifting the Meridian up or down, so that there may be  $51^{\circ} 30'$  betwixt the North Pole and the Horizon, (which always must be observed to be done in that or any other Latitude,) if the Horizon or its Circles be in the Question. And secondly, it must be rectified, as to the Sun, by altering the Hand of the little Hour-Wheel fixed upon the Meridian about the Pole, which by bringing the Sun or Star to the right Edge of the Meridian, and then turning the Hand to 12 of the Clock at Noon, which is that 12 farthest from the Horizon. This is done, because that no other Point is so certain, and that when the Sun comes under the Meridian it is 12 of the Clock. Therefore bring the Sun's Place to the Horizon, (by turning the Globe about) and there hold him, the Index upon the Hour-Circle shews the Ascensional Difference, that is, how many Hours and Minutes before or after 6 of the Clock the Sun riseth; and accounting how many Degrees and Parts is contained be-

twixt



Amplitude Or-  
tive.

Occafive.

Fig. 19.

twixt the Point of East and the Sun upon the Horizon, that Number is the Amplitude Ortive; as in our Example; the Ascensional Difference is 17 Degrees 0 Minutes, or 1 Hour 8 Minutes, and the Amplitude Ortive 21 Degrees 15 Minutes from the East towards the North. And the same Amplitude will be at the West that Day for Occafive.

This being performed, you may observe the Triangle upon the Globe that forms this Resolution, that is, Part of the Meridian from the Pole to the Horizon  $51^{\circ} 30'$ , Part of a Meridian imagined to be drawn from the Pole by the Index, and to the Sun's Place at the Horizon, which is the Complement of the Sun's Declination  $76^{\circ} 53'$ , and laid down in Figure 19. You must note likewise, That any Two of the Five being given, you may by the Globe find the rest: As for Example, by the Amplitude  $21^{\circ} 15'$ , and the Ascensional Difference 17 Degrees, or 1 Hour 8 Minutes, to find the Latitude. Mark the Amplitude in the Horizon from East towards the North, then having rectified the Globe, as to the Sun's Place, to that Amplitude, bring the Sun (keeping the Hour Index at 1 Hour and 8 Minutes before 6) by lifting the Globe up and down, till he rises just at that Amplitude, then you may find the Elevation of the Pole; and the rest may be done thus very easily.

## 2. By the Analemma.

Here this Instrument must be rectified, by turning the North Pole P to the Height above the Horizon, at London  $51^{\circ}$  Degrees 30 Minutes, and then finding the Sun's Place, and its Parallel, follow the Parallel to the Horizon, and there you will find the Amplitude  $21^{\circ} 15'$ , and the Difference from 6 1 Hour 8 Minutes as before, and all things as plain as in the Globe.

## 3. By Scale and Compass.

Fig. 20.

Describe the *Analemma* as was shewed before, and describe the Sun's parallel as before, mark where it cuts the Horizon HO, as at r, if from r you raise a Parallel to YZ, you will find the Arch Zk to be the Amplitude  $21^{\circ} 15'$ , and if you cut the Equinoctial in proportion as the Parallel is cut by the Horizon, and raise a Parallel to YP, and it will give you the Ascensional Difference  $17^{\circ}$ , or 1 Hour 8 Minutes.

## 4. By Calculation.

Fig. 20.

In the *Analemma*, or in the last Scheme, if you mark the Spherical Right-angled Triangle POY, you will find it to agree with that formerly observed on the Globe, where PO is the Poles Height, rO the Complement of the Amplitude, and Pr the Complement of the Sun's Declination, the Angle at P is the Complement of the Ascensional Difference, the Angle P rO is the Angle the Meridian makes with the Horizon. Now to Calculate this Triangle, where the Five Parts of the Problem are to be found, and

any two being given, you may find the rest, by the 6 Propositions of Right-angled Spherical Triangles, and the 16 Varieties.

## Example.

There is given, 1. the Declination of the Sun  $13^{\circ} 7'$ , and his Complement  $76^{\circ} 53'$  for rP; and 2. the Height of the Pole PO  $51^{\circ} 30'$ ; To find 1. rO, the Complement of the Amplitude; and 2. the Angle at P.

For the first, by the Hypothenufe rP, and a Side PO, to find rO, marked as in Figure 19 with ABC, the Rule by the first Proposition and second Variety will be,

As Co-sine CA . Co-sine BC :: Radius . Co-sine BA

Co-sine CA $51^{\circ} 30'$	9,794149
Co-sine BC $76^{\circ} 53'$	9,355901
Radius	10,000000
Co-sine BA $68^{\circ} 37'$	9,561752

Whole Complement  $21^{\circ} 23'$  is the Amplitude Ortive.

Here working the Question as was done in the last, the Side rO is found, and its Complement will be Yr the Amplitude.

Again, with the same Data to find the Ascensional Difference, or the Angle rPO, which is its Complement, that is, by the Hypothenufe, and a Side, to find the Angle at P. The Rule, by the first Proposition and third Variety, is,

As Tangent BC . Tangent CA :: Radius . Co-sine C

Tangent BC $76^{\circ} 53'$	10,632618
Tangent CA $51^{\circ} 30'$	10,099395
Radius	10,000000
Co-sine C $72^{\circ} 58'$	9,466777

Thus I find the Angle at P  $72^{\circ} 58'$ , its Complement  $17^{\circ} 2'$ , or 1 Hour 8' 8", for the Ascensional Difference.

After this manner, and after the 6 Propositions and 16 Varieties before taught, you may vary all the Five Parts of the Problem, and with any Two find the other Three, which I advise the Learner to do. And what has been laid of the Sun, is applicable to any Star that Setteth and Riseth. And note, for the Not-setting or Not-rising of certain Stars, That,

1. If the Elevation of the North Pole be greater than the Complement

X

of



of the North Declination of the Star, then that Star Setteth not: But if it be greater than the Complement of the South Declination of the Star, then that Star Riseth not.

2. If the Elevation of the South Pole be greater than the Complement of the South Declination of the Star, then that Star Setteth not: But if it be greater than the Complement of the North Declination of the Star, then that Star Riseth not.

Lastly, note in the Figures, and likewise in the Globe, That there is another Right-angled Triangle under the Horizon  $\Upsilon rs$ , that being resolved, will perform this Problem as the former; it is made up of Parts of three Great Circles, *viz.*

Of these Five,	{	1. $rs$ the Declination of the Sun,	} Any Two being gi-		
		2. $\Upsilon s$ the Ascensional Difference,		ven, to find out any	
		3. $\Upsilon r$ the Amplitude Ortive,			One of the rest.
		4. The Angle $s\Upsilon r$ the Comple-			
		ment of the Poles Elevation,			
5. The Angle $\Upsilon rs$ ,					

And this Triangle being marked with  $ABC$ ,  $A$  representing the Right Angle, which here is  $\Upsilon sr$ , may be resolved sixteen various ways, and will bring forth the same Resolutions of this last Problem, as before was declared; and may be wrought by Scale and Compass, as before.

### Problem X.

*The Declination, the Right Ascension, and the Difference of Ascension, of the Sun or Star, being given; To find the Oblique Ascension and Descension of the Sun or Star.*

1. IF the Elevation of the Pole and Declination be both either North or South, subtract from the Right Ascension the Difference of Ascension, and there will be the Oblique Ascension; or, add to the Right Ascension the Difference of Ascension, and there will be the Oblique Descension.

2. If the Elevation of the Pole and Declination be one North and the other South, add to the Right Ascension the Difference of Ascension, and there will come the Oblique Ascension; or, subtract from the Right Ascension the Difference of Ascension, and there will come the Oblique Descension.

Problem

### Problem XI.

*To find the Semidiurnal Arch of the Sun, or any Star that Riseth and Setteth, and when it Riseth and Setteth.*

1. IF the Elevation of the Pole and Declination of the Sun or Star be both of a kind, that is to say, if they be both North, or both South, then the Difference of Ascension being converted into Hours and Parts, and added to 6 Hours, there will be produced the Semidiurnal Arch.

2. But if the Elevation of the Pole and Declination of the Sun or Star be not both of a kind, but the one be North and the other South, then the Difference of Ascension, being converted into Hours and Parts, and subtracted from 6 Hours, the Remainder will be the Semidiurnal Arch.

The Semidiurnal Arch is half the Time that the Sun or Star moveth above the Horizon: And therefore,

1. If it be subtracted from the Time of the Sun or Star's coming to the South, the Remainder will be the Time of the Rising of the Sun or Star.

2. But if it be added to the Time of the Sun or Star's coming to South, the Sum will be the Time of the Setting of the Sun or Star, casting away 12 if need be.

3. If the Semidiurnal Arch be doubled, it sheweth the whole Continuance of the Sun or Star above the Horizon.

### Problem XII.

*Of these Six; 1. the Elevation of the Pole, 2. the Declination of the Sun or Star, 3. the Altitude of the Sun or Star above the Horizon, 4. the Distance of the Sun or Star from the Meridian in Degrees or Hours, 5. the Azimuth of the Sun or Star from the North, and 6. the Angle at the Sun or Star: Any Three of them being given, to find out any One of the rest.*

THIS Problem is resolved, by comparing the Equinoctial, its Meridians, and Parallels, with the Horizon, and its Vertical Circles called Azimuths, and its Parallels called Almucanters; and it being chiefly employed to find the Hour of the Day and Azimuth, is of great Use both in Astronomy and Navigation.

1. By the Globe.

Let the Example be the 14th of April, 1678, the Sun being in 4 Degrees and 40 Minutes of Taurus, and its Declination 13 Degrees 7 Minutes, the Poles Height 51 Degrees 30 Minutes, and the Sun's Height 30 Degrees above the Horizon.

X 2

First:



*Globe rectified  
in the Hour-  
Circle and In-  
dex.*

*In the Height  
of the Pole.*

*In the Q-  
drant of Alt-  
itude to the Ze-  
nith.*

First, the Globe must be rectified, that is, the Hour-Circle, by bringing the Sun to the true Edge of the Meridian, and setting the Hour-Index to 12 of the Clock of the Day, that Index supplying the Place of Meridians, which in the Projection of the Globe cannot be, and therefore are expressed. Secondly, it must be rectified to the Height of the Pole. And thirdly, the Quadrant of Altitude, which is a thin Plate of Brafs divided into 90 Degrees, equal to 90 Degrees of the Equator, Ecliptick or Horizon, and must be fixed by a Skrew to the Zenith, which must be as far from the Equinoctial as the Elevation of the Pole comes to; or if you tell from the Pole P towards the Equinoctial, the Complement of the Poles Height that way will find the Zenith, for betwixt the Zenith and the Horizon is 90 Degrees, and taking out of 90° the Poles Height, it leaves the Complement for the Zenith; as for Example,  $38^{\circ} 30'$  is the Complement of  $51^{\circ} 30'$ , the Height of the Pole at London, which being told from the Pole towards the Equinoctial, there fix the Skrew, for that is the Zenith, and the Center or Middle of the Pin that the Quadrant of Altitude turns upon must be sure to be directly under the divided Part of the Meridian; and observe, that in turning the Quadrant about, the lowest Division thereof agree with the Edge of the Horizon, and so round about.

Having thus fitted the Globe, you must move the Sun's Place and this Quadrant up and down, and in such manner, as that the Sun's Place, viz.  $4^{\circ} 40'$  of Taurus, may exactly meet with 30 Degrees of the Quadrant of Altitude, which after some attempts you may do: And then,

1. The Index upon the Hour Circle shews it to be 8 Hours and half a Quarter before Noon, the true Time of the Day.

2. The Quadrant of Altitude, by his true Edge, betwixt the Globe and the Horizon, shews the Azimuth to be  $72^{\circ} 15'$  from the South, or from the East, if you please,  $17^{\circ} 45'$ .

Observe, That the Brafs Meridian describes and supplies all the Parallels or Distances from the Equinoctial, and the Hour-Circle and Meridian supplies all the Meridian or Hour-Circles.

The Azimuth is the Distance of any Vertical Circle from South or North, or from East or West, as you please to accompt.

Lastly note, That the Triangle made upon the Globe for this Resolution, is thus, from the Zenith to the Pole is one Side, which is the Complement of the Latitude; from the Zenith upon the Quadrant of Altitude to the Sun's Place is another, which is the Complement of the Sun's Height; and from the Sun's Place to the Pole, by an Imaginary Meridian Line, supplied by the Index and Hour Circle, another Side, and is the Complement of the Declination; the Angle made at the Pole, by the Brafs Meridian and the Imaginary Hour-Circle passing to the Sun, is the Degrees from Noon, which turned into Hours is the Time from Noon; the Angle made at the Zenith, by the Brafs Meridian and Quadrant of Altitude, is the Azimuth from the North Part of the Meridian; there is another Angle made by the Quadrant of Altitude and Hour-Circle, which makes the six Parts of the aforesaid Problem.

2. By

2. By the Analemma.

This is to be rectified to the Pole's Height, by bringing the North Pole P  $51^{\circ} 30'$  above the Horizon (here at London) and there let it rest; next find out the Sun's Place in the Ecliptick, and its Parallel: And well considering that Parallel, you may observe in it, at what Hour the Sun riseth, the Amplitude and Height of the Sun or any Star or Point being limited by the Parallels to the Horizon, as you may see them expressed, (which by a Silk Thred laid over all equally on both sides from the Horizon, shews the Almucantar.) If you lay a Thred over the Point of 6 of the Clock Parallel, as aforesaid, it shews the Height of the Sun at 6 of the Clock in Summer. And yet further tracing the Parallel 'till the Sun come into the Prime Vertical, there among the Hour-lines you may find the Time of the Day: As in our Example, crossing a Thred over 30 and 30, in that Height you shall find it cut the Parallel a Quarter past 8 of the Clock in the Morning. And so when the Sun or Star shall pass to 12 of the Clock or Mid-day, then you must trace him back again along the same Parallel 'till he descend to the Horizon, noting, that then you must account by the Afternoon-Hours, viz. 1 for 11, 2 for 12, 3 for 9, &c.

3. By the Scale and Compass.

In Figure 20 draw a Line  $gi$ , 30 Degrees on either side from H and O, Fig. 20. where that crosseth the Sun's Parallel, as at  $g$ , there is the Sun's Place at that Height; and if you cut  $\gamma \text{ } \text{AE}$  proportionally as the Parallel  $tf$  is cut at  $g$ , and raise a Perpendicular at  $k$ , the Degrees cut in the Circle is the true Time from 6, viz. 2 Hours 15 Minutes, or  $37'$ ; and so of the rest.

4. By Calculation.

In the Figure you will find the Oblique-angled Triangle Z P  $g$ ; that Z P, as I shewed before, is the Complement of the Height of the Pole  $38^{\circ} 30'$ , Z  $g$  the Complement of the Sun's Height  $60^{\circ}$ , and P  $g$  the Complement of the Declination of the Sun  $76^{\circ} 53'$ : All these are given to find the Angle at P, which is the Sun's Distance from the Meridian in Degrees, and the Hours in Time. By the second Problem of Oblique-angled Spherical Triangles, you will find the Rule and Example thus:

DeG.



	Deg.	Min.		
Compl. of the Pole's Height	Z P	38 30	Arith.Sine	0,205850
Compl. of the Declination	P q	76 53	Arith.Sine	0,011481
Difference		38 23		
Complem. of the Sun's Height		60 00		
Sum		98 23		
Difference		21 37		
The Half Sum		49 11	Sine	9,878984
The Half Difference		10 48	Sine	9,272726
Sum of all the four Sines				19,369041
Half Sum will be				9,684520

Which is the Sine of  $28^{\circ} 56'$ , which doubled will be  $57^{\circ} 12'$ , and that converted into Time is 3 Hours 51 Minutes, that which the Sun wants of 12 or 8 of the Clock and 9 Minutes that Day.

Ex. 2. Having the same things given, to find the Azimuth, viz. the Angle contained betwixt the Meridian and Vertical Circle; that is, having Z P as before  $38^{\circ} 30'$ , and Z q the Complement of the Sun's Height  $60^{\circ}$ , including the Angle sought, and the Base P q the Complement of the Declination  $76^{\circ} 53'$ ; to find the Azimuth from the North, viz. P Z q.

	Deg.	Min.		
Complem. of the Pole's Height	38 30		Arith.Sine	0,205850
Complem. of Sun's Height	60 00		Arith.Sine	0,062469
Diff. of the last	21 30			
Compl. Declin.	76 35			
The Sum	98 23			
The Difference	55 23			
The Half Sum	49 11	Sine	9,878984	
The Half Diff.	27 47	Sine	9,667075	
Sum of all the four Sines				19,814368
The Half Sum				9,907184

Which is the Sine of  $53^{\circ} 52'$ , and that being doubled comes to  $107^{\circ} 44'$ , the Azimuth from the North; and taken from  $180^{\circ}$ , leaves  $72^{\circ} 16'$ , the Azimuth from the South; and subtract  $90^{\circ}$  from it, leaves the Azimuth from the East,  $17^{\circ} 44'$ .

There are many ways for resolving this Problem, but this last way is most easie in my apprehension; however, 'till the young Practitioner be expert, it is good to try two ways, viz. if they agree you may assure the Work: Therefore I will give you this following Example for the same.

Deg.

	Deg.	Min.		
Base Z S	60 00			
The Side P S	76 53			
The Side Z P	38 30			
Sum	175 23			
Half Sum	87 41			
Diff. of Base and Half Sum	27 41		Arith.Sine	0,000355
Difference of Sides	10 48		Arith.Sine	0,332934
	49 11		Sine	9,272725
			Sine	9,878984
The Sum of all four				19,484998
The Half Sum				9,742499

	Deg.	Min.		
Base P S	76 53			
The Side Z S	60 00			
The Side Z P	38 30			
Sum	175 23			
Half Sum	87 41			
Diff. of Base and Half Sum	10 48		Arith.Sine	0,000355
Diff. of 2 Sides and Half Sum	27 41		Arith.Sine	0,727274
	49 11		Sine	9,667065
			Sine	9,878984
The Sum of all four				20,273678
The Half Sum				10,136839

Now these two found Numbers 9,742499 and 10,136839 are no Sines, as in the former Operations, but Tangents, and give for Degrees and Minutes in the first  $28^{\circ} 56'$ , in the second  $53^{\circ} 52'$ , which being doubled makes  $57^{\circ} 42'$  the Distance from the South, and  $17^{\circ} 44'$  for the Azimuth from the East; and being the same that was found the first way, confirms the Operation, and are to be applied as before.

This Problem may be varied many ways.

First, For resolving this Spherical Triangle, by having all the Sides given, to find the rest.

1. Given  $\left\{ \begin{array}{l} \text{The Com. of the Pole's Height Z P} \\ \text{The Compl. of Sun's Declinat. P q} \\ \text{The Compl. of the Sun's Height Z q} \end{array} \right\}$  to find  $\left\{ \begin{array}{l} \text{The Hour } \angle P \\ \text{The Azim. } \angle Z \\ \text{The Angle } q \end{array} \right.$

This Case is wrought before two several ways, and is the second of the four Cases in the Analysis of *Oblique-angled Spherical Triangles*, to be wrought by the second Problem thereof.

Secondly, Having two Sides and an Angle opposite, or two Angles and a Side opposite, to find the rest.

1. Given



1. Given  $\begin{Bmatrix} ZP \\ Zq \\ q \end{Bmatrix}$  To find  $\begin{Bmatrix} Z \\ P \\ Pq \end{Bmatrix}$  or Given  $\begin{Bmatrix} ZP \\ Pq \\ q \end{Bmatrix}$  To find  $\begin{Bmatrix} Z \\ P \\ Zq \end{Bmatrix}$  or Given  $\begin{Bmatrix} Z \\ P \\ Zq \end{Bmatrix}$  To find  $\begin{Bmatrix} Pq \\ P \\ q \end{Bmatrix}$  or Given  $\begin{Bmatrix} Pq \\ P \\ q \end{Bmatrix}$  To find  $\begin{Bmatrix} ZP \\ Zq \\ P \end{Bmatrix}$
2. Given  $\begin{Bmatrix} ZP \\ P \\ Zq \end{Bmatrix}$  To find  $\begin{Bmatrix} ZP \\ Pq \\ q \end{Bmatrix}$  or Given  $\begin{Bmatrix} Z \\ P \\ Zq \end{Bmatrix}$  To find  $\begin{Bmatrix} Pq \\ Zq \\ P \end{Bmatrix}$  or Given  $\begin{Bmatrix} Pq \\ Zq \\ P \end{Bmatrix}$  To find  $\begin{Bmatrix} Zq \\ Pq \\ P \end{Bmatrix}$

All these Varieties, being the first Case of the *Analysis* of *Oblique-angled Triangles*, are performed by the first Problem thereof.

Thirdly, Having two Sides and the Angle comprehended given, to find the rest.

1. Given  $\begin{Bmatrix} ZP \\ Zq \\ q \end{Bmatrix}$  To find  $\begin{Bmatrix} Pq \\ P \\ q \end{Bmatrix}$  or Given  $\begin{Bmatrix} ZP \\ Pq \\ q \end{Bmatrix}$  To find  $\begin{Bmatrix} Zq \\ Z \\ P \end{Bmatrix}$  or Given  $\begin{Bmatrix} Zq \\ Z \\ P \end{Bmatrix}$  To find  $\begin{Bmatrix} ZP \\ Pq \\ P \end{Bmatrix}$

These Varieties, being the third Case of the *Analysis*, are performed by the sixth and seventh Problems of *Oblique-angled Spherical Triangles*.

Fourthly, Having two Angles and a Side adjacent, or two Sides and an Angle adjacent, to find the rest.

1. Given  $\begin{Bmatrix} Z \\ P \\ Pq \end{Bmatrix}$  To find  $\begin{Bmatrix} ZP \\ Zq \\ q \end{Bmatrix}$  or Given  $\begin{Bmatrix} Z \\ P \\ Zq \end{Bmatrix}$  To find  $\begin{Bmatrix} Pq \\ P \\ q \end{Bmatrix}$  or Given  $\begin{Bmatrix} Pq \\ P \\ q \end{Bmatrix}$  To find  $\begin{Bmatrix} ZP \\ Zq \\ P \end{Bmatrix}$
2. Given  $\begin{Bmatrix} ZP \\ Pq \\ Zq \end{Bmatrix}$  To find  $\begin{Bmatrix} Pq \\ q \\ P \end{Bmatrix}$  or Given  $\begin{Bmatrix} ZP \\ Zq \\ P \end{Bmatrix}$  To find  $\begin{Bmatrix} Pq \\ Zq \\ P \end{Bmatrix}$  or Given  $\begin{Bmatrix} Pq \\ Zq \\ P \end{Bmatrix}$  To find  $\begin{Bmatrix} ZP \\ Pq \\ P \end{Bmatrix}$

These Varieties, being the fourth Case of the *Analysis*, are resolved by the fourth and fifth Problems of *Oblique-angled Triangles*: All which I leave to the Practitioner, there being 60 Varieties in this one Triangle.

1. Note, That if the Point at  $q$  be the Sun (as before was in the Example) then the Angle  $ZPq$ , or the Distance of the Sun from the Meridian, is the Time either before High-noon, if the Sun be in the Eastern part of the World, *viz.* moving from the North part of the Meridian towards the South part thereof: Or else it is the Time after Noon, if the Sun be in the Western part of the World, *viz.* moving from the South part of the Meridian towards the North part thereof.

2. But if the Point at  $q$  be a Star, then the Angle at  $P$ , or Distance from the Meridian, is what that Star wants of 12 in the Eastern part, or what past 12 in the Western.

3. Note here, That sometimes the Hour of Six is named, and of the Elevation of the Pole, &c. in the Problem belonging to the Sun, some are required from others given; in which Case the Triangle is right angled

at

at the Pole, as in the Triangle (*Fig. 20.*)  $ZPt$  right-angled at  $P$ , (for the *Fig. 20.* Hour Lines of 12 and 6 are cut at right Angles) and therefore particularly for the Hour of Six this Problem may be thus exprest, *viz.*

- Of these Five,  $\left\{ \begin{array}{l} 1. \text{ The Elevation of the Pole,} \\ 2. \text{ Declination of the Sun,} \\ 3. \text{ The Sun's Height at 6 of the Clock,} \\ 4. \text{ The Azimuth at 6 of the Clock,} \\ 5. \text{ The Angle at the Sun,} \end{array} \right\}$  Any Five being given, to find any One of the rest.

Because in the Triangle  $ZPt$  Right-angled at  $P$ , the Side  $Pt$  being the Hour Line of 6 of the Clock:

1.  $PZ$  is the Complement of the Elevation of the Pole.
2.  $Pt$  is the Complement of the Declination.
3.  $Zt$  is the Complement of the Sun's Height at the Hour of 6.
4.  $tZP$  is the Azimuth of the Sun from the North at 6.
5.  $PtZ$  is the Angle at the Sun, shewing the Position thereof, in respect of the Pole and Zenith, at 6 of the Clock.

And therefore by the 16 Cases and 16 Varieties of *Right-angled Spherical Triangles*, any one of these may be found out by any two given, and the Radius.

4. Sometimes again the Azimuth of East or West is named, and of the Elevation of the Pole, and the rest in the Problem, some are required from others given; in which case the Triangle is Right-angled at  $Z$ , as the the Right-angled Triangle  $PZs$ ; and particularly for the Azimuth of East or West, this Problem may be thus exprest:

- Of these Five,  $\left\{ \begin{array}{l} 1. \text{ The Elevation of the Pole,} \\ 2. \text{ The Declination of the Sun or Star,} \\ 3. \text{ The Sun or Star's Altitude in the East or West Azimuth,} \\ 4. \text{ The Distance of the Sun or Star from the Meridian, when it is in the East or West,} \\ 5. \text{ The Angle at the Sun or Star,} \end{array} \right\}$  Any Two being given, to find any One of the rest.

Because in the Triangle  $Psz$  Right-angled at  $Z$ , the Side  $Zs$  being *Fig. 20.* the Azimuth of East and West:

1.  $PZ$ , is the Complement of the Elevation of the Pole.
2.  $Ps$ , is the Complement of the Declination of the Sun or Star.
3.  $Zs$ , is the Complement of the Altitude of the Sun or Star, being full East or West.
4. The Angle at  $P$ , is the Distance of the Sun or Star (being in the East or West Azimuth) from the South Part of the Meridian.
5. The Angle at  $s$ , is the Angle at the Sun or Star, shewing the Position thereof in respect of the Pole and Zenith, when it is in the Azimuth of East and West.

Y

And



And therefore by the Problems of the Calculation of the Right-angled Spherical Triangles, any one of these may be found out, by any two given.

Lastly, There are many other Triangles and Problems to be considered upon the Globe and Projections, which I reserve for the Last Part, these being sufficient at this time, and for this purpose.

### Problem XIII.

*Of the Uses of the Eight Maps of the Fixed Stars, in their Prints, annexed at the End of this Chapter.*

I. **T**Here be six of the Planispheres all equal in bigness, from whence follows, 1. That all make one Cube; 2. That the Sphere, which is so reduced, may be imagined a Cube; 3. That they touch the Sphere only in six Points, *viz.* the two Poles, the two Equinoctial Points, and other two Points in the Equinoctial answering the Solstices.

II. The Rays or Lines of the Projection are drawn from the Center of the Sphere, from whence follows, 1. An easie way to find the Right Ascension and Declination of the Stars; 2. That the Great Circles are always straight Lines.

III. There are only 45 Degrees projected in each Table from the Center, from whence it comes, that the Figure of each Constellation scarce exceeds its due Magnitude.

IV. The Tables are placed in this order, the first, that about the Arctick Pole, as most known; the last, that about the Antartick, always hid to this Latitude; the rest follow the Order of the Signs.

The Contrivance of these six Maps, made by Father *Pardie* at *Paris*, affords, that the Stars may be more easily found by them than by the Globes or Spheres, for that in the Globe the Stars are set on the convex Superficies, but in the Heavens, and these Maps, in *Plans*, as to apprehension; for placing one Eye at the Distance of the Semidiameter of the Chart, and perpendicularly on the Center, and holding the Map in a right Position, if the Stars on the Map were perforated, the Eye would see all the Stars of the Heavens answering thereto through the Holes. This premised, the Uses follow.

#### 1. By the Maps, to find the Stars in the Heavens:

First, turning towards the North, find out the notorious seven Stars of the Great Bear called *Charles's Wain*, four whereof (fancied to be the Wain) make a Quadrilateral Figure, and the other three a scalenous Triangle, which are the Horses, that next the Wain is called *Alioth*. Having found these, consider what Figure they make with other Stars: As for Example: Draw a Right Line by the two farthest of the Wain from the Horses, and it will direct you to the Pole-Bar in the Tip of the *Little Bear's* Tail, distant from the Pole it self in this Year, 1673, 2 Degrees 25 Minutes, and from the Pole.

Pole-star you will find the seven Stars of the *Little Bear* almost in the same Site and Position with the former of the *Great Bear*. Now the *Dragon* lies wreathed betwixt these two Constellations of the *Bears*, as you may see by the Maps: Now to find first the greatest Star in the *Dragon*, conceive a Line drawn from the Middle Horse of *Charles's Wain* to another Star of the Third Magnitude which the *Little Bear* has in his Right Shoulder; this Line passeth by a Star of the Second Magnitude in the *Dragon*. This being found, ascend to the other three of the Third Magnitude, and so to the rest in that Constellation. And thus by observing the Position of the Stars in the Maps, either as they lye in Quadrangles, Triangles, or straight Lines, those known with the unknown, all the Stars of one Chart may be found in one Night.

#### 2. To find the Distance of any two Stars.

This being the Parts of an Arch of a Great Circle, passing through the two Stars, if both of them be found in any of the Circles divided, as in the Equator, Ecliptick, or Colures, then the Distance it self is found by the Degrees intercepted. But if the two Stars, whose Distance is required, be found in any Right Line that passeth by the Center of the Chart, or near unto it, take the Distance from the Center to one of them, and transpose it from the Center on any of the Divided Lines, and set that Number of Degrees down by it self, do the same Work for the other, the Sum of those two Numbers is the Distance required. The third way, to find the Distance of any two Stars, generally not posited as above said, is shewed in the sixth Section following.

#### 3. To find the Right Ascension and Declination of any Star in the Charts.

First for the Right Ascension, if the Star be found in the two Polar Charts, lay a Ruler to the Center or Pole by the Star, and where it cuts the Limb you will find the Right Ascension in Degrees and Parts. But if the Star be found in some of the other four Charts, it either falls in some Meridian, which followed to the Equinoctial, shews the Right Ascension; or else betwixt two Meridians, which by a Ruler, parallel to a Meridian, shews the same, as before. Example: In the first Map or Polar Chart, the Right Ascension of *Alioth* will be found 190 Degrees; of *Arcturus*, in the fourth Map, the Right Ascension will be 210 Degrees and a little more.

The Declination (being the Distance of a Star from the Equinoctial) is found by the Circle of Declination that passeth by it, or estimated betwixt two, which are Parallel to it; as in the first Map, or Polar Chart, the first Horse in *Charles's Wain* is 51 Degrees of Declination North; the Declination of the Bright Star in *Andromeda's* Head, in the second Map, is 27 Degrees 30 Minutes North; and the *Great Dog-star*, in the third Map, is found to be 16 Degrees of Declination South.



*Note*, That the Right Ascension and Declination of the Stars are computed for the Year 1680, and may serve without Error for many Years after.

4. *To find by the Charts, to trace out the Way of a Comet, when seen.*

First, find out the Place or Point in the Maps where the Comet first appears, thus; Take Four Stars, whereof Two one way and Two another, that pass in a Right Line with the Comet, draw these Lines in the Chart, and the Crossing of them will point out the Place of the Comet: Do this for another Observation or two: A freight Line drawn by these Two or more Places, describes the Way of the Comet for its future Appearance, according to the best Theories of Comets.

5. *To find by the Charts what Stars do perpetually appear, and what are always hid.*

Knowing the Height of the Pole, as at London  $51^{\circ} 30'$ , all the Stars that lye between the Pole and the Parallel that is distant from the Equinoctial above  $38^{\circ} 30'$  the Complement of the Pole's Height, always appear; and on the contrary from the South Pole, disappear. And so for any other Latitude.

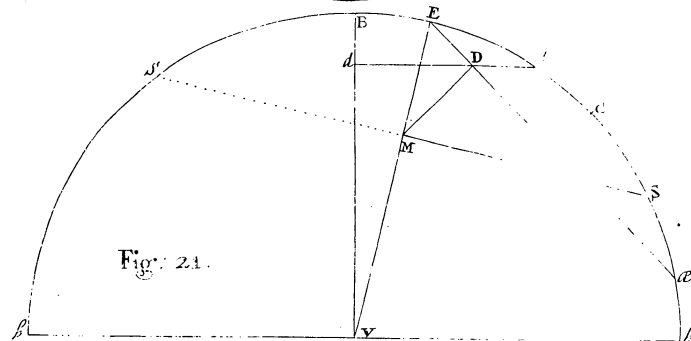
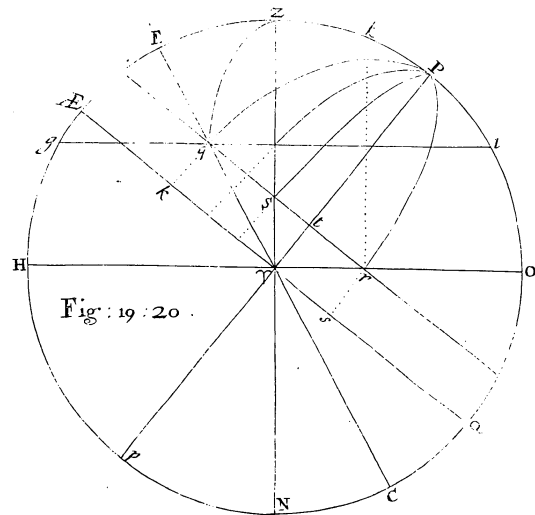
For the Longitude and Latitude of the Stars, though Father *Pardie* hath drawn them in his great Maps, yet I have omitted them here, for fear of the confusion too many Lines might cause.

6. *To find the Distance of any two Stars upon the 6 Charts.*

This distance is part of a great Circle which passeth betwixt the Stars proposed, and therefore if the two Stars fall under one and the same Meridian, the Difference of Declination will shew the Distance; but if otherwise, then you must work this Geometrical Problem, viz. *Having the Right Ascension and Declination of any two Stars given, To find the Distance.* Which is performed several ways by the Projection of the Sphere; but I find it most easily solved by Mr. *Thomas Baker*, Minister of *Bishop-Nympton* in *Devonshire*, my worthy Friend, amongst his resolutions of all Spherical Triangles, whether Right or Oblique, Geometrically; which he was pleased to impart to me, and it is the third Problem of Oblique Spherical Triangles, viz. *By the two Sides of any Spherical Triangle, and the Angle included, to find the third Side.* Which is performed after this manner.

*For Example.*

Let the bright Star in *Cassiopeia's* Chair, of the third Magnitude, in the first Polar Map be proposed, whose Right Ascension is  $357^{\circ} 59'$ , and Declination North  $57^{\circ} 25'$ : And the bright Star in the *Swans* Tail, of the third Magnitude, whose Right Ascension is  $307^{\circ} 37'$ , and Declination North





North  $44^{\circ} 10'$ . Now to form the Triangle at the Pole, take the Differences of the Right Ascensions, by subtracting the less from the greater, viz.  $357^{\circ} 59'$ , less by  $507^{\circ} 37'$ , reits  $50^{\circ} 22'$ , for the Angle at the Pole; and take the Complements of the Declinations, viz. of  $57^{\circ} 25'$  and  $44^{\circ} 10'$ , gives  $32^{\circ} 35'$  and  $45^{\circ} 50'$ , for the two Sides of the Triangle proposed; Fig. 21. which done, divide a Circle into two Quadrants  $VbB\beta$ , let  $B$  to the top, Point, and let  $V$  be the Center, measure  $BC$  an Arch equal to one Side  $45^{\circ} 50'$ , (and this do by dividing the Circle into Parts, or from a Line of Chords) and  $CE$  and  $C\alpha$  equal to the other side  $32^{\circ} 35'$ , draw the Lines  $E\alpha$ , and make  $ES$  equal to the Angle given  $50^{\circ} 22'$ , draw the Radius  $VE$ , and from  $S$  let fall the Perpendicular upon it  $SM$ , and from  $M$  upon  $E\alpha$  let fall the Perpendicular  $MD$ , and by  $D$  draw the Line  $dDd$  Parallel to the Diameter  $bV\beta$ . Then is the Arch  $Bd$   $33^{\circ} \frac{1}{2}$  the Side sought, and the Distance of the two Stars in *Cassiopeia's* Chair and the Swans Tail. This Problem is very easie to work, and will be of great use, as well for the finding the Distance of the Stars, as the Distance of two places upon the Terrestrial Globe, and the Operation will find the same Distance from the Longitude and Latitude of the same Stars, viz. that in *Cassiopeia*, the Longitude  $00^{\circ} 38'$  of  $\gamma$ , and Latitude North  $51^{\circ} 17'$ ; that in the Swan, Longitude  $00^{\circ} 58'$  in  $\kappa$ , Latitude North  $59^{\circ} 57'$ . If you take the Complements of the Latitudes  $38^{\circ} 43'$ , and  $30^{\circ} 3'$ , they will be the Sides of the Triangle, and the Angle will be the Difference of the Longitudes of the two Stars, viz.  $59^{\circ} 40'$ , the Distance will be found  $32^{\circ} \frac{1}{2}$ .

And because the Solution of the Oblique-angled Spherical Triangle is of such great use, viz. Where the two Sides and an Angle included are given, to find the third Side. I will work the Problem by Artificial Sines and Tangents, according to the sixth Problem of Oblique-Angled Spherical Triangles, taught before, pag. 116, viz.  $BC, B$ , and  $BD$  being given, to find  $DC$ : By the second Analogy, (1)  $As$  Radius . Co-tang.  $BA$  :: Co-sine  $B$  . Tang.  $BA$ . Compare  $BD$ , the Side whereupon the Perpendicular falleth, with  $BA$ , and you will find  $BD$ . Then say,

$$As \text{ Co-sine } BA . \text{ Co-sine } DA :: \text{ Co-sine } BC . \text{ Co-sine } DC.$$

<i>As</i> Radius	10,000000
To tang. of $BC \ 32^{\circ} 35'$	9,805580
So Co-fi. of $B \ 50^{\circ} 22'$	9,804733
To tang. of $BA \ 22^{\circ} 11'$	39,610313
$BD \ 45^{\circ} 50'$	
$DA \ 23^{\circ} 39'$	



As Co-fi. BA 22° 11'	9,966601
To Co-fi. DA 23° 39'	9,961901
So Co-fi. BC 32° 35'	9,925626
	<u>x9,887527</u>
To Co-fi. DC 33° 32'	9,920926

First, to find the Distance of the former two Stars, by their Difference of Right Ascension 50° 22', for the Angle B, and the Side BD 45° 50', and BC 32° 35'; according to the Rule work as in the Example, and you will find BA 22° 11', which taken from BD 45° 50', leaves DA 23° 39'. Then working the second time, and you shall find the third Side sought to be 33° 32', for the Distance of the said two Stars.

As Radius —————	10,000000
To Tang. BC 38 43'	9,903973
So Co-fi. 59° 40'	<u>9,703317</u>
To Tang. of BA 22° 2'	4,9607290
BD 30° 3'	
DA 08° 1'	
As Co-fi. BA 22° 02'	9,960063
To Co-fi. DA 8° 1'	9,925735
So Co-fi. BC 38° 43'	<u>9,892233</u>
	<u>x9,887963</u>
To Co-fi. DC 33° 32''	9,920905

The like Operation and Distance will be found from the Longitude and Latitude of the said Stars, their Difference of Longitude being 59° 40' for the Angle B, the Complements of Latitude 38° 43', and 30° 3', for BD and BC, the Operation will be as you find in the Example; and the third Side will be found 33° 32', for the Distance of the two Stars.

Thus both Geometrically, and by Calculation, the Distances of any two Stars may be found, with this Caution only, That if the Angle given be Obtuse, or above 90°, then take its Complement to 180°, and instead of the Side found, take its Complement likewise.

7. To

7. To use the said Six Charts of the Stars for the finding, or learning to know the Stars in the Heavens by Observation, and are so many Astriscopes when thus used.

According as the Radius for these six Charts is greater or lesser, so must the Instrument be made accordingly. I will begin with the two Polar Charts, that of the North Pole, and that of the South Pole. The Radius of these small Charts is 4 Inches, if you make a Nocturnal, which shall have an Axis 4 Inches from the Plane of the Chart, and whereupon the Chart must be pasted, with a Cavity through it to look upon the North, and finding at any time which of the Stars in the Chart are in the Meridian, and set the Chart accordingly, then will all the Constellations near the Pole be visible, and may be easily learnt; and the time of the Night may be known, by comparing the Right Ascension of the Sun, with that of the Star.

The same may be practised by the Chart of the Southern Pole, after the same manner.

But for the four other Charts, they must be placed at Right Angles to the Equinoctial or Parallel to the Axis of the World. Therefore if you prepare an Instrument so fixed upon an Horizontal Plane, that it may have a Pin of a sufficient length, elevated to an Angle, equal to the Latitude of the Place where it is to be used; and that it may be turned so, that the Axis may lie in, or over the Meridian Line; then let any of the four Plates be fixed upon this Axis, so that they may be four Inches from this Axis, and turn round about it. For use, turn this Chart round about, till you see it agree with any of the Stars thereupon; so will you see all the rest in their places, and may thereby know all, or any of the Stars that are in the Charts.

8. Of the strange (and wonderful, 'till the Invention of Perspective-Glasses) Appearances of the Stars, some new, some ancient, and of the Planets in these latter Ages.

I. In the Appearance and Disappearance of several Stars that have no Parallax visible, and have and now do alter their bigness, and some are not found to return any more.

1. The first that was notable, was that in *Cassiopeia*, Anno 1572. observed by the famous *Tycho Brahe*, which from the fourth, increased to as big as any of the first, and bigger, and after some Months grew less, and disappeared.

2. That in the Swan's Breast, observed by *Kepler*, and by *Hewelius*, from 1658 to 1672, many times appearing and disappearing.

3, 4. In 1648, one new Star appeared in the Whales Mouth, and this Star in the same place was observed by *Bullialdus* many times, and by *Montieur Hewelius*, and another in the Whales Neck.

5. One



5. One in *Anno* 1665, observed in the Girdle of *Andromeda* by *Bullialdus*, and formerly by *Marius*, 1614; other new Stars have appeared in the Swan, observed by *Monfieur Hevelius*; and some likewise in the Swan by *Monfieur Caffini*, and many others in *Orion*, and other Constellations, as may be found in the Relations of *Ricciolus*, and several other persons.

II. In the strange Discovery that the Telescopes have made in the Planets:

1. *Saturn* appearing Tricorporeal to *Galileus* first, and since their alteration, that sometimes those two Bodies about him seem one Line, and *Monfieur Caffini* has discovered two small Stars move with him, like our Moon.

2. *Jupiter* with four Moons or Stars moving about him, as his own Body turning about shewed by a spot upon *Jupiter*.

3. *Mars* turns about, and upon his *Axis*, as *Jupiter*.

4. *Venus* horned, full, and in the Wane, as our Moon.

5. The spots and shadows in the Sun, and the turning of his whole Body about it.

6. The spots and strange Extuberances in the Moon, and the Fibration of her Body.

These I say are admirable and worthy of *Ovid's* Verse:

*Felices anima, quibus hac cognoscere primum,  
Inque Demos superas scandere cura fuit.*

## SECTION IV.

## Of the Plain SCALE.

To make the Lines of Chords, Natural Signs, Tangents, Secants, Semitangents, Rumbs, Hours and M. Longitude, which are on the Plain Scale.

**D**Escribe a Circle as ADEF, and Quarter it with the two Diameters AE, DF, at Right-angles one the other.

1. Divide the Arch DE into nine equal parts, and setting one foot of the Compasses in E transfer the divisions of the Arch marked 10, 20, &c. to the strait Line ED: so is ED a *Line of Chords* for every 10 degrees, the single degrees may be divided by judgment.

2. Through the Division 10, 20, &c. draw parallels to CD, which will divide CE into a *Line of Signs*.

3. On E raise EG perpendicular to CE, and laying a Ruler over C and the Points 10, 20, 30, &c. draw the Lines 10, 20, 30, &c. so is EG a *Line of Tangents*.

4. Setting one foot on C, extend the other to the several degrees, of the *Tangent Line* EG and describe the Arches 10, 10, 20, 20, 30, 30, &c. which makes the Line CDH a *Line of Secants*.

5. Laying a Ruler over A and the degrees 10, 20, 30, &c. of the Arch ED, make marks on the Line CD, which becomes a *Line of Semitangents*.

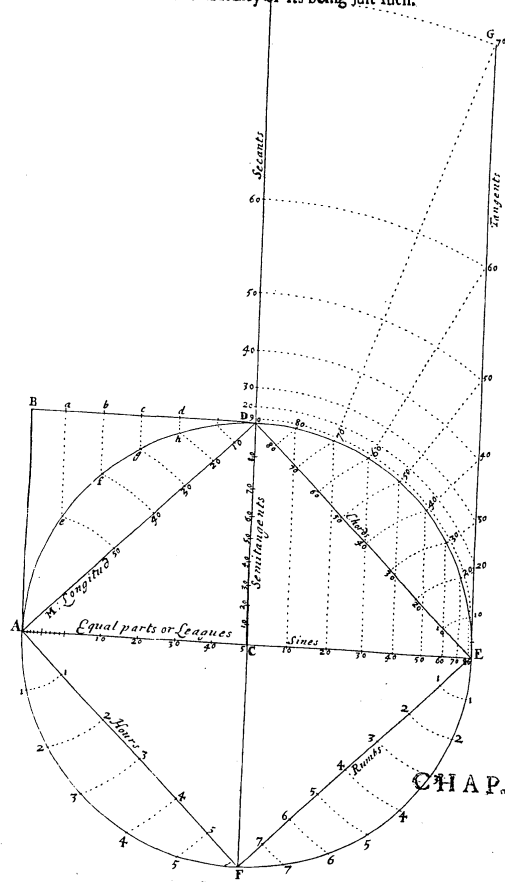
6. Divide the Arch EF into eight equal parts, and setting one foot of the Compasses in E with the other transfer the Divisions of the Arch 1, 2, 3, &c. to the strait line, which Line EF so divided is called a *Line of Rumbs*.

7. Divide the Arch FA into six equal parts, and setting one foot in A, transfer them to the strait line FA which becomes a *Line of Hours*. This serves only for the dividing a Circle readily into twenty four equal Parts.

8. Make the square ACDB, and divide its sides AC, BD into six equal Parts; drawing the lines a e, b f, c g, &c. parallel to AB; then setting one foot in A with the other transfer the marks e, f, g, &c. to the strait line AD, which line so divided is called the line of *Miles long*.



9. AC serves for a line of equal parts to take off Leagues, or Miles, &c. from. Though indeed any other line of equal Parts would serve as well: for there's no necessity of its being just such.







CHAP. VI.  
Of NAVIGATION.

SECTION I.  
DEFINITIONS.

**N**avigation Teacheth and Demonstrateth, how a sufficient Ship may be conducted the shortest way, and in the shortest time between any places assigned in Passages Navigable.

If the places assigned be at no great Distance, but so that a Ship may Sail in sight of Land, or within Soundings between them, then it's called a *Coasting*.

For the performance of which there's required good knowledge of the Lands, the use of the Compass, and Lead or *Sounding Line*, such are the Voyages on the Narrow, or *British Seas* between *England, Holland, and France*, also all about the *Baltick Seas*, and indeed those in the *Mediterranean* are little other.

Sometimes I had thoughts of inserting here a Rutter, with all the helps that might be for Coasters: but considering that every Sea Chart has the Depths, Bearing, and Distances, and what they are wanting in, the *Waggoners* indifferently will supply, I have omitted it.

If the Voyage be to be performed in a Vast Ocean, where all that's visible for many days, nay weeks together is *nisi Pontus & Aether*, then it may be called *Navigation Proper*; and requires not only the Lead-Line and ordinary Compass, but Azimuth Compass, Charts, and Log-board, with instruments for Celestial Observations, as the Quadrant, Forestaff, &c. and the Navigator must be able by these to find at any time in what Place the Ship is, which is done by comparing it with any known Place, that is, how far the same known Place is situate from the Ship, either towards the North or South, which is called the Difference of Latitude, or towards the East or West, which if in proper Degrees is called the Difference of Longitude.







The Distance of the Rumbs, or Points from the Meridian.						
North	South	D.	M.	South	North	Point.
		2	49			
		5	38			
		8	26			
N by E	S by E	11	15	S by W	N by W	1
		14	4			
		16	53			
		19	41			
N N E	S S E	22	30	S S W	N N W	2
		25	19			
		28	8			
		30	36			
N E b N	S E by S	33	45	S W by S	N W b N	3
		36	34			
		39	23			
		42	11			
N E	S E	45	00	S W	N W	4
		41	49			
		50	37			
		53	16			
N E b E	S E by E	56	15	S W b W	N W b W	5
		59	4			
		61	52			
		64	41			
E N E	E S E	67	30	W S W	W N W	6
		70	19			
		73	07			
		75	56			
E by N	E by S	78	45	W by S	W by N	7
		81	34			
		84	22			
		87	11			
Eas <sup>t</sup>		90	00	West.		

The

**N**avigation or Sailing in respect of the Rumb, or Point Sailed on is Sailing according to the Right and Oblique.

Right Sailing is, when the Voyage is performed on some one of the four Cardinal Points.

If a Ship Sail under a Meridian, that is, on the North or South Points, she varieth not the Longitude at all: but only changeth the Latitude, and that just so much as the number of Degrees she has Run.

If a Ship Sail under the Equinoctial upon the very East or West Points, she altereth not her Latitude at all: but only changeth the Longitude, and that just so much as the number of Degrees she hath Run.

If a Ship Sail directly East or West under any Parallel, she there also altereth not her Latitude, but only the Longitude; yet not according to the number of Degrees of a Great Circle, she hath Sailed as under the Equinoctial: but more than so many according as the Parallel is remoter from the Equinoctial towards the Pole: For the less any Parallel is, the greater is the Difference of Longitude in Sailing so many Degrees of a Great Circle.

Oblique Sailing is when the ship runneth upon some Rumb between any of the four Cardinal Points: making an Oblique Angle with the Meridian. And then she changeth continually both Latitude and Longitude.

There be three kinds of Oblique Sailing, or rather methods of practising the way and pricking down the place of the Ship.

The first is called Plain Sailing, manifesting all the varieties of the Ship's motion on a Plain, where all the Meridians are made parallel, and the parallels at Right Angles to the Meridians, and the Degrees of each parallel equal to those of the Equinoctial.

Which though notoriously false in it self, supposing the Earth and Sea to be a plain flat, and each Parallel equal to the Equinoctial, yet by laying down places accordingly, and breaking a Long Voyage into many short ones, a Voyage may pretty well be performed thereby near the same Meridian.

The Second is called Mercators, or more truly Wrights Sailing, or Sailing by Wrights Chart; which Demonstrates also on a Plain the motion of the Ship upon any Course assigned, true in Longitude, Latitude and Distance, the Meridians being also Parallel, and the Parallels of Latitude straight Lines.

The Third is Great Circle Sailing, which teacheth how upon or by a Great Circle passing through any two Places assigned, the Ship may be conducted by a skillful Seaman: and this is the shortest way between Place and Place that may be.

The Operation of all which three kinds shall be shewed by Delinca-tions, or Geometrically if the use of a Line of Chords may be admitted as Geometrical by Computation, or Arithmetically, and Mechanically, or Instrumentally.

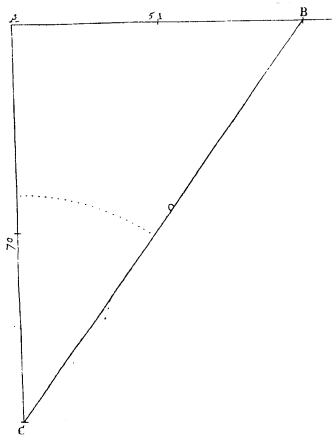
SECTION



## SECTION II.

## Plain SAILING.

**F**OR Methods sake make always the fore Part of the Book, Slate, or whatever else you draw or work upon, the North Part, that nearest to you the South, then will that towards the Right hand be the East, and that towards the Left hand the West; and imagine that by the Rumb Line, Meridian and Parallel of Latitude will always be formed a Right angled Triangle, as the Triangle BAC Right-angled at A, (for so shall the Right-angle be always marked throughout the work :) Then is that Part of the Meridian or North,



and

and South line contained between A and C the difference of Latitude, the side BA the departure, BC the distance failed, the Angle C the Course, and the Angle B the Complement of the Course. Any two of which, with the Right Angle, being given, the Triangle may be protracted, and the other three Parts found, as in the following Examples will appear.

## CASE I.

*The Course and Distance given, to find the Difference of Latitude, and Departure from the Meridian.*

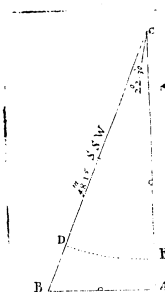
Admit a Ship from the Latitude  $50^{\circ} 10'$  North, Sails SSW  $48.5$  Miles: I require the Latitude she's in, and her Departure or Separation?

*Geometrically.*

First, Draw the North and South line AC, and taking with the Compasses  $60^{\circ}$  from the *Line of Chords* set (because she Sails Southward) one foot in some point towards the North on the said line AC as at C and describe the Arch DE, and lay thereon two Points or  $22^{\circ} 30'$  the Course from E to D, and draw CB.

Secondly, taking the given distance  $48.5$  m. from the *Line of Equal Parts*, lay it on the Rumb-line CB from C to B.

Lastly, from B let fall the Perpendicular BA, which includes the Triangle BAC, whose required Parts BA and AC being taken one after the other between the Compasses, may be measured, by applying them to the Scale.



*Arithmetically.*

Say, *As the Radius,*  
*Is to the Distance run, BC 48.5m.*  
*So is the sine of the Course  $22^{\circ} 30'$*   
*To the Departure 18.56 miles*  
 Which in this Example is Westing.

10,000,000

Arith.

1,685,7420

9,582,8397

11,268,5817

A a

Then



Then again,

As the Radius

10,000000

Is to the Distance BC 48.5 Miles

1,6857420

So is the Cosine of the Course S:67° 30'

9,9656153

To the Difference of Latitude CA 44.8 Miles

1,6513573

Which because she Sailed towards the Equator, I subtract from the Latitude she set out from, viz. 50° 10' and the Remainder 49° 25' is the Latitude she's arrived in. If the Difference of Latitude CA had been more than 60 I must have divided by 60, and the quotient had been the Degrees, and the Remainder-minutes, which must have been added or subtracted as before.

By Gunter's Scale.

Infr.

Set one foot of the Compasses in the Radius or sine of 90°, and extend the other to two Points on the *sine Point Line*, or on 22° 30' of the lines: Then keeping that extent set one foot in 48.5 of the *Line of Numbers*, and turning the other backwards, viz. that way you did turn it from the first term the Radius, to the third two Points, and the other foot will fall on 18.6 the Departure as before.

Again, set one foot in the Radius and extend the other to six Points (which is the Complement of two Points the Course:) then keeping that extent set one foot in 48.5 of the *Line of Numbers*, and turning the other foot backward it will fall on 44.8 the Difference of Latitude as above.

Which difference of Latitude and Departure being found by the estimate distance from the Log, which by many accidents is viciated, as by the Wind and Seas when high throwing it after the Ship, or Currents, &c. is naught and not to be relied on, but as soon as the Sun or Stars appear, the Latitude ought to be observed by the Rules following towards the end of this Treatise, which if found differing from what it was made by the former way called *Dead Reckoning*, you must take the difference of this last observed Latitude, and the Latitude you departed from, and with this true difference of Latitude and the Course by the following Prop. find the departure and distance.

For the ready performance of this Prop. is the Table Page 59 of the *Vol. of Tables*. Thus, enter with the Course on the head, and with the distance down by the side, and you'll be directed by such entry to the departure and difference of Latitude.

Case

### CASE 2.

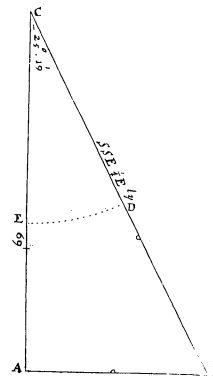
The Course and Difference of Latitude being given to find the Departure and Distance.

Admit a Ship Sail from Latitude 48° 30' North, SSE  $\frac{1}{2}$  Easterly till she be in Latitude 47° 21': I demand the Departure and Distance Sailed.

Geometrically.

Geom.

First, Draw the North and South Line CA and subtracting the Latitudes one from the other take 69 Miles their difference, and set from C to A making the point C towards the upper or North end of the Line, and on A raise the Perpendicular BA. Lastly, taking the Radius and setting one foot in C, with the other describe the Arch DE, and lay thereon 2 $\frac{1}{2}$  Points or 25° 19' from E to D and draw CD, which compleats the Triangle BAC, whose required Parts may be measured by the Scale.



A 2 2

Say,



## Arithmetically.

Say, As the Cosine of the Course $S: 64^{\circ} 41'$	9,9561483
Is to the Difference of Latitude 69 Miles	1,8388490
So is the Radius	10,0000000
To the Distance Sailed BC 76.3	11,8388490
	1,8827007
Then, As the Radius	10,0000000
Is to the Distance Sailed CB 76.3	1,8827010
So is the sine of the Course $2\frac{1}{2}$ Points the $\angle C$	9,6310590
To the Departure AB 32.6 Miles	11,5137600

## Instrumentally.

Set one foot of the Compasses on the SR line in  $5\frac{1}{2}$  Points the Compl. of the Course, and extend the other to the Rad. then keeping the Compasses at the same extent, set one foot in 69 the Difference of Latitude on the Line of Numbers, and turn the other forward, and it will fall on 76.3 the Distance Run.

Then, set one foot in the Radius and extend the other to  $2\frac{1}{2}$  Points: afterward keeping the Compasses at that extent, set one foot in the Distance Sailed, and turn the other backward (because it was turned backward before from the Rad. to  $2\frac{1}{2}$  Points) and it will fall on 32.6 the Departure.

If having no cause to suspect the Distance for the former or any other Reasons, and are assured in your self of having made a good estimate thereof: but mistrust the care or skill of the Helmsman that he has let her yaw or fall off, or that you have neglected the Variation, then with the true Difference of Latitude, and the Distance by the following Prop. find the Course and Departure.

## CASE 3.

The Difference of Latitude and Distance Sailed given, to find the Course and Departure.

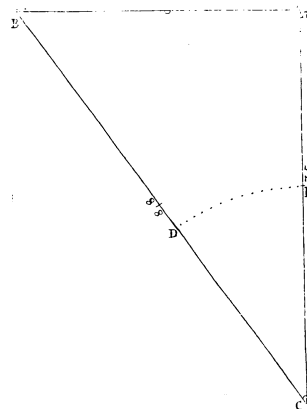
Admit a Ship sail from Latitude  $42^{\circ} 15'$  North, on some Point between the North and West 88 Miles, and then finds her self in Latitude  $43^{\circ} 30'$ : I demand the Course and Departure.

Geome-

## Geometrically.

Having drawn the Meridian Line AC, prick the Difference of Latitude 75 Miles from C to A, and on the Point A raise the Perpendicular BA: then take the Distance 88 Miles and setting one foot in C, with the other cross BA as it will somewhere as in B, and draw BC, now the line BA measured on the equal Parts is the Departure, also upon C as a Center with  $60^{\circ}$  of the Chords describe the Arch DE which measured on the Chords or Rumbs shews the Course  $2\frac{1}{2}$  Points from the North Westward, viz. NNW  $\frac{1}{2}$  Westerly.

43°	30'
42	15
1	15
60	
75	



Note



Note, that where ever a side is to be measured or laid down, as the Distance, Departure or Difference of Latitude, you must always use the equal Parts, but when an Angle, the Chords.

*Arithmetically.*

As the Distance Run BC 88.	1,9444827
Is to the Radius.	10,0000000
So is the Difference of Latitude CA 75	1,8750613
	11,8750613
To the Cosine of the Course, the Angle B $58^{\circ} 27'$	9,9305786
Whole Complement $31^{\circ} 33'$ is $2\frac{1}{2}$ Points from the Meridian which is NNW $\frac{1}{2}$ Westerly.	
Then, As the Radius.	10,0000000
Is to the Distance Run CB 88 m.	1,9444827
So is the sine of the Course $31^{\circ} 33'$	9,57187030
To the Departure from the Meridian AB 46 Miles West.	1,6631857

*By the Gunter.*

Set one foot in 88 of the *Line of Numbers*, and extend the other to 75, then set one foot in the *Radius*, or line of  $90^{\circ}$  and turn the other backward, and it will fall in the line of  $58^{\circ} 27'$  the Complement of the Course.

Again, Set one foot in the *Radius*, and extend the other to the line of  $31^{\circ} 33'$ ; then set one foot in 88 m. and turn the other backward, and it will fall on 46 m. the separation from the Meridian.

#### CASE 4.

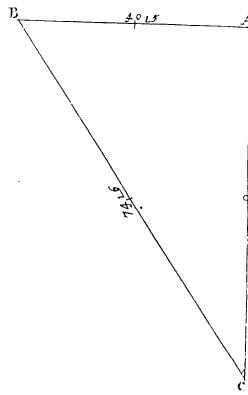
*The Distance Run, and Departure from the Meridian given, to find the Course and Difference of Latitude.*

A Ship being in the Latitude  $59^{\circ} 00' N$ , Sails North Westward, 'till her distance Run be 74.6 Miles, and the Departure be 40.5: I demand the Course and Difference of Latitude, and consequently the Latitude the ship is in.

*Geom.*

*Geometrically.*

Having drawn the Meridian AC on the point A, taken somewhere towards the upper, or North end of the Line (because the Ship Sails Northward) raise the Perpendicular BA, laying thereon 40.5 Miles the Departure from A to B, then take the Distance 74.6 Miles, and setting one foot in B, with the other cross the Meridian AC in C and draw BC.



*Arith.*



## Arithmetically.

<i>Arith.</i>	As the Distance Run BC 74.6	1,8727388
	Is to the Radius	10,0000000
	So is the Departure BA 40.5	1,6074550
		11,6074550
	To the sine of the Course $\angle C$ $32^{\circ} 53'$	9,7347162
	Which is three Points from the Meridian, viz. NW by N nearly.	
	Then, As the Radius	10,0000000
	Is to the Distance BC 74.6	1,8727388
	So is the Cosine of the Course $57^{\circ} 7'$	9,9241644
	To the Difference of Latitude AC 62.6 Miles	1,7969032
	Which turned into degrees is $1^{\circ} 3'$ , and is to be added to $59^{\circ} 00'$ the Latitude she Departed from, because she Raides the Pole: fo is the sum $51^{\circ} 3'$ the Latitude the Ship's in.	

## By the Gunter.

*Instr.*

Set one foot of the Compasses in 74.6 Miles, and extend the other to 40.5, then keeping the same extent, set one foot in the sine of  $90^{\circ}$ , and turn the other backward, and it will fall on the sine of  $32^{\circ} 53'$  the Course.

Again, Set one foot in the sine of  $90^{\circ}$ , and extend the other to the sine of  $57^{\circ} 7'$  the Complement of the Course, then retaining the same extent, set one foot in 74.6 of the Line of Numbers, and turn the other backward, and it will fall on 62.6 the Departure.

## CASE 5.

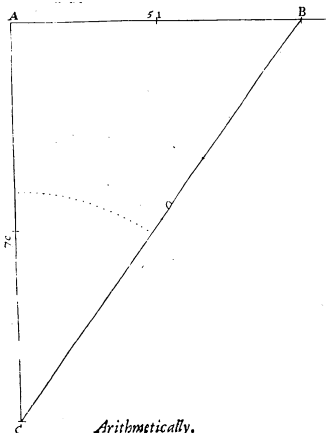
The Alteration of Latitude, and Departure from the Meridian given, to find the Course and Distance.

A Ship from Latitude  $59^{\circ} 00'$  North, Sails North Eastward 'till she has altered her Latitude  $1^{\circ} 10'$  or 70 Miles, and is departed from the Meridian 51 Miles: I demand the Course and Distance.

Geom.

## Geometrically.

Having drawn AC and laid thereon the 70m. from C to A, and on Geom. A raised the Perpendicular AB, lay 70m. from A to B and draw BC.



Arithmetically.

As the Difference of Latitude AC 70m.	1,8450980	<i>Arith.</i>
Is to the Radius	10,0000000	
So is the Departure AB 51	1,7075702	
	11,7075702	
	9,8624722	
The Sine of the Course $\angle C$ $6^{\circ} 05'$		
Which is 1 <sup>st</sup> Point, or NE by N ly nearly.		
Then, As the sine of the Course $\angle C$ $4^{\circ} 05'$	9,708760	
Is to the Departure AB 51	1,7075702	
So is the Radius	10,0000000	
Is to the Distance BC	1,8450980	



By the Gunter.

177.

Set one foot of the Compasses in 70m. and extend the other to 51 of the Line of Numbers, then keeping the same extent, set one foot in the Tangent of  $45^\circ$ , turning the other backward, and it will fall on the Tangent  $43^\circ 14'$  the Course.

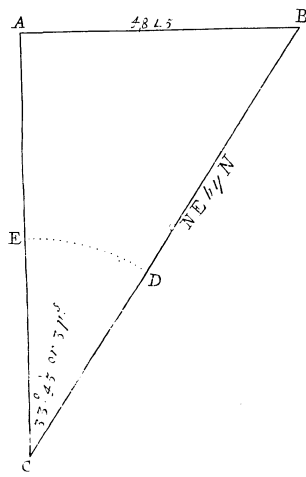
Again, Set one foot in the line of  $43^\circ 14'$ , and extend the other to the line of  $60^\circ$ , then keeping the same extent, set one foot in 51 of the Line of Numbers, turning the other forward, and it will on 74.4 the Distance.

This Proposition is of use at the beginning of a Voyage or close of a Traverse.

## CASE 6.

The Course and Departure given, to find the Distance and Difference of Latitude.

A Ship from the Latitude  $48.30^\circ N$ , sails NE by N till her departure from the Meridian be  $48\frac{1}{2}$  miles, what is the distance sailed and difference of Lat.



Geom.

Geometrically.

Having drawn the Meridian AC, and on the point C, taken somewhere towards the lower or South end, as a Center, with the Chord of  $60^\circ$  described the Arch DE, and laid thereon three Points from E to D, and thereby drawn the Rumb-line CB, at the extent 48.5 taken from the Scale of equal Parts, draw a parallel to AC, as FG, cutting the Rumb-line in B, from which point B let fall a Perpendicular to AC, as BA.

Geom.

Arithmetically.

As the sine of the Course  $33^\circ 45'$   $\angle C$ 

9,7447390 Arith.

Is to the Departure AB 48.5

1,6857417

So is the Radius,

10,0000000

To the Distance CB 87.3 Leagues.

11,6857417

1,9410027

Then, As the Radius,

10,0000000

Is to the distance Run CB 87.3

1,9410027

So is the Cosine of the Course,  $S: 56^\circ 15'$ 

9,9198464

To the Difference of Latitude AC 72.6

11,8608491

1,8608191

By the Gunter.

Set one foot of the Compasses in the line of three Points, and extend the other to the Radius, or line of eight Points; then keeping that extent, set one foot in 48.5 of the Line of Numbers, and turn the other forward, and it will fall on 87.3 the Distance Sailed.

Instr.

Again, Set one foot in the line of eight Points, and extend the other to the line of five Points: then set one foot in 87.3 Leagues, and turn the other backward, and it will fall on 72.6 Leagues; the Difference of Latitude, which is 217.3 Miles or Minutes which divided by 60 makes  $3^\circ 37'$  which because she saileth the Pole. I add to  $48^\circ 30'$  the Latitude she departed from, and the sum  $52^\circ 7'$  is the Latitude she's arrived in.



## A TRAVERSE.

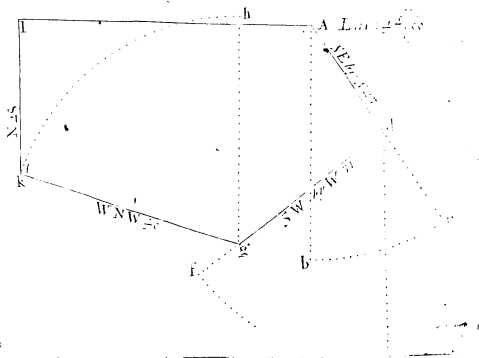
A Traverse is the Variation or Alteration of the Ships Course upon the shifting of Winds, &c.

Note, That Sailing in respect of the wind is either *before a Wind*, *by a Wind*, or *Lurging*.

If a Ship Sail by or against a wind there ought to be an allowance for her Lee-way, and that more or less according to the growth and surge of the Sea, and mould of the Ship, and Sail she bears, &c.

## Example '1. Of a Traverse.

A Ship from Latitude  $47^{\circ} 00' N$ , Sails SE by S 23 Miles, and then Sails S W by W 31 Miles, and afterwards W N W 40 m. and lastly, N 28 m. I demand the Course and Distance Sailed from the first place of Departure, and the Latitude she's now in.



Geom.

## Geometrically.

Take any convenient point on your Slate or Paper, for the Ships place *Geom.* at first, as A, and from thence having drawn the Meridian A b, with  $60^{\circ}$  of the Chords describe the Arch b c, and lay thereon 23 Miles from A to d, so have you protracted the first Course and Distance.

Secondly, Through the point d, draw the Meridian d e parallel to A b, and with  $60^{\circ}$  of the Chords setting one foot of the Compasses in d as a Center describe the Arch e f, laying thereon 5 points from e to f, and draw d f, then prick 31 Miles from d to g on the Line d f, so have you laid down the second Course and Distance.

Thirdly, From the point g draw g h parallel to A b, and with  $60^{\circ}$  of the Chords describe the Arch h i, laying thereon six points from h to i, and draw g i, then prick 40 Miles from g to k.

Fourthly, From k draw the Meridian k l parallel to A b, and because she Sails now under the very Meridian it self, lay 28 m. the Distance on this Rumb from k to l, which point l is the Ships place at the end of this Traverse: then draw l A, and that measured on the line of equal Parts or Miles gives 50.4 m. the distance from the place of Departure, and the Angle A l k being measured on the Chords gives  $82^{\circ}$  or  $7\frac{1}{2}$  Points from the Meridian, so that if she had Sailed on a straight line, and single Course from the first point A to l that Course had been W by N  $\frac{1}{2}$  Westerly, and the Distance 50.4 m, and if she were to Sail back again from l to A, she must stand E by S  $\frac{1}{2}$  Easterly till she has run 50.4 m.

## Arithmetically.

As the Radius,	10,000,000	Arith.
Is to the Distance on the first Course 23 m.	1,361,7278	
So is the sine Complement of the Course S: $56^{\circ} 15'$	9,919,8464	
To the Difference of Latitude in the first Course 19.1 Miles.	1,281,5742	
Then, As the Radius,	10,000,000	
Is to the Distance A l 23 m. Run on the first Course	1,361,7278	
So is the sine of 3 Ps. or $33^{\circ} 45'$ $\angle$ d A B the first Course	9,744,7390	
To the Departure in the first Course 12.8	11,106,4668	

Thus proceeding with the several Courses and Distances given, find the Departures and Difference of Latitude to them all.

If



If the Course be between the North and East, then the Difference of Latitude is called Northing, and the Departure Easting; if the Course be in the North West Quarter, then the Difference of Latitude is called Northing and the Departure Westing: If the Course be between the South and East the Difference of Latitude is called Southing, and the Departure Easting, &c.

Now place all the said Differences of Latitude and Departures in a Table, the Northings all under one another under the Title *Northing*, and the Southings under *Southing*, the Eastings in the *East* Column, and the Westings in the *West* Column, as in the Specimen.

Then add up all the Northings, as likewise the Southings, and so the Eastings and also the Westings; Lastly, take the sum of the Northings from that of the Southings if the Southings make most, or the sum of the Southings from the Northings, that you may have their Difference, which is the Difference of Latitude; also take the Difference of the Totals of Easting and Westing for the Departure; by which Difference of Latitude and Departure, according to Case fifth, find the direct Course and Distance.

Lat. depav. } 47° 00' N,  
red from S  
Diff. of Lat. 0 07

Lat. fix's in 47 7 N,

Course	Point	Dist.	North	South	East	West
S E by S	3	23		19 12	12 78	
S W by W	5	31		17 22		25 78
W N W	6	40	15 31			36 96
North	0	28	28 00			
from sum			43 31	36 34	12 78	62 74
take			36 34		12 78	
Rems	1		6 57			49 96
			Dep. West.			

As the Difference of Latitude 7 m.

Is to the Radius.

So is the Departure 49.9 m.

To the Tangent of the Course, 82° 1'

And, As the sine of the Course 82° 1'

Is to the Departure 49.9 Miles

So is the Radius

To the Distance 50.4 Miles

0,8450980

10,0000000

1,6981005

11,6981005

10,853005

9,9957705

1,6981005

10,0000000

11,6981005

1,7023300

By

By the Gunter.

Set one foot in eight Points, and extend the other to three Points, *Infir.*  
then with the same extent set one foot in 23 m. and turn the other backwards, and it will fall in 12.8 the Easting in the first Course.

8 Ps.  
3 Ps.  
5 Ps. Set one foot in eight Points, and extend the other to five Points, Then set one foot in 23 m. and turn the other backward, and it will fall in 19.1 the Southing in the first Course.

Secondly, Set one foot in eight Points, and extend the other to five Points, Then keeping the same extent set one foot in 31 m. turning the other backward, and it will fall on 25.3 the Westing in the second Course.

8 Ps.  
5 Ps.  
3 Ps. Set one foot in eight Points, and extend the other to three Points; Then keeping the same extent set one foot in 31 m. turning the other backward, and it will fall in 17.2 the Southing in the second Course.

Thirdly, Set one foot in eight Points, and extend the other to six Points; Then retaining the same extent set one foot in 40 m. turning the other backward, and it will fall on 36.9 the Westing in the third Course.

8 Ps.  
6 Ps.  
2 Ps. Set one foot in eight Points, and extend the other to two Points, Then set one foot in 40 m. turning the other backward, and it will fall on 15.3 the Northing in the third Course, which Northings, Southings, Eastings, &c. being collected as before, and the sums of Differing Denomination subtracted, the Difference of Latitude will be 7 m. North, and the Departure 49.9 m. West.

Then set one foot in 49.9 m. and extend the other to 7 m. afterwards remove one foot to 1.45° turning the other backward, and it will fall on 82° which is the Course from the North Westward.

Again, Set one foot in the sine of 82°, and extend the other to the sine of 90 Degrees, then keeping the Compasses at the same extent, set one foot in 49.9 turning the other backward, and it will fall on 50.4 m. the direct Distance from the first place of Departure.

Example 2.

A Ship being bound to the Eastward, and finding the Wind Variable, a small Gale, and smooth water, plies upon these several Courses, with the Distances on each Course as followeth.

The



*The Lar-board Tack on Board, Wind from SSW to S, and so to SSE and E.*

	Miles.
South East by East $\frac{1}{2}$ Easterly, .....	5
East South East, .....	4
East by South, .....	7
East $\frac{1}{2}$ Northerly. ....	3

*The Star-board Tack on Board, the Wind SE, ESE, E, &c.*

South South West, .....	5
South by West, .....	6
South, .....	4
South South East, .....	7
South East by South. ....	3

I require the Direct Course and Distance from the first place of Departure.

*The manner of delineating it is omitted, I presuming it's well enough understood, by what has been said on the first Example.*

## The Work by the Traverse Table.

Course	Points.	Dist.	North	South	East	West
SE by E $\frac{1}{2}$ Ely	5 $\frac{1}{2}$	5		2 36	4 41	
ESE	6	4		1 53	3 70	
E by S	7	7		1 37	6 86	
E $\frac{1}{2}$ Nly	7 $\frac{1}{2}$	3	0 29		2 98	
SSW	2	5		4 62		1 91
S by W	1	6		5 88		1 17
South	0	4		4 00		0 00
SSE	2	7		6 47	2 08	
SE by S	3	3		2 49	1 67	
Sum			0 29	28 72	21 70	3 08
				0 29	3 08	
				28 43	18 62	

Having drawn several Columns, and therein set down the several Courses and Distances as in the specimen, turn to the *Traverse Table*, Page 59, of the *Volum* of Tables, looking the Course on the head of the Table if under four Points, but at the bottom if above four Points; and look the Distance in the left hand Column, and in the square of meeting will be the Difference of Latitude and Departure under the respective Titles.

Thus, Above 5  $\frac{1}{2}$  Points and right against 5 *m.* find over the Title Diff. Lat. 2.36 *m.* the Diff. of Lat. and over *Dep.* 4.14 *m.* the Departure in the first Course, which being placed in their proper Columns according as they are Northing or Southing, &c. proceed in the manner with all the other Courses and Distances entering the corresponding Differences of Latitude and Departures in their Columns: then add up the Columns of Difference of Latitude and Departure, subtracting the lesser Difference of Latitude from the greater, and the lesser Departure from the greater and the Remainders are the whole Difference of Latitude and Departure, she hath made from the place of her Departure: So in this Example she's 28.43 *m.* to the South of the Place of Departure, and 18.62 *m.* East, with which by Case fifth I find her Course SE by S 2° Southerly, and Distance 34.5 *m.*

C c

As

The



As I have intimated in a single Course that the account by Course and Distance is not altogether to be trusted to, so here I say care must be taken as often as may be to make observations by which to correct the dead Account; the manner how to correct it from Observations shall be explained in the following Examples.

## Example 3.

Anno 1672, From the 25th. of July to the 26th. the Courses and Distances Sailed by the Log were,

	<i>m.</i>	
E	32	A Wind from the S S E Variable to the SE by S an indifferent Gale, and the variation of the Compass by Observation 5° East, The true Course and direct Distance is required.
E N E	22	
N E by E	4	
S W by S	20	
S S W	5	
	83	

## The work by the Traverse Table.

Course	Points.	Diff.	North	South	East	West
East	8	32			32 00	
E N E	6	22	8 42		20 32	
N E by E	5	4	2 22		3 32	
S W by S	3	20		16 63		11 11
S S W	2	5		4 61		1 91
			10 64	11 25	55 64	13 02
				10 64	13 02	
				10 61	42 62	

The Course being Computed by the former Method is East 14° South, and the Distance 44 *m.* but by reason of the Variation the true Course is East 19° South, with which and the Distance 44 *m.* I work for the Difference of Latitude and Departure by Case 1, and find the Difference to be 14.3 *m.* and the Departure 41.6 *m.* My Latitude by Observation on the 25th. day was 29° 12', and this day by Observation 29° 22' S, the Difference is but 10' which is 4 *m.* less than

than the former, so that I am 4' more Northerly than I estimated by my dead reckoning, which difference between the Observed and dead Latitude must be attributed to something.

But I have no cause to suspect my Course, and have been careful in trying and find no current, therefore I conclude it's caused by her Leeway; then by the true Difference of Latitude 10', and the Distance 44 *m.* I compute my Course again according to Case 3. and find it E 13° S, which will give my Departure 43 *m.* and Difference of Latitude 10' according to Observation. But if having been well experienced in the qualities of my Ship, and certain what allowance to have made for her Leeway, yet had not Observed the Variation, I should have argued another way, and attributed the error to a Variation especially if I had made any Tryal for a Current.

Then to be able to give a good account of the Ships place is no light easie thing, but requires besides an experienced judgment in estimating the Ships way, and frequent Observation of the Latitude, a perfect understanding the Qualifications of the Ship, a true and constant Observation of the Variation, and no long omission of the tryal for the discovery of Currents.

If there be an omission of the Observation of any one of these, it may nevertheless be found by the other: but if two or more be omitted, it will be doubtful to which of them to attribute the error, and consequently, hardly any true correction to be made. Yet note this, that if you have omitted every thing but the Course and Distance, as most commonly it happens, then if the Course be less than four points from the Meridian, take the Course to be true, and with that and the true Difference of Latitude find the Departure.

But if the Course be above four Points from the Meridian, take your Distance and true Difference of Latitude produced by observation, and by them find the Departure, and once in two or three days if it may be observe carefully the Variation, which will confirm you much in the truth of your account of Easting or Westing, if true or else manifest to you an error, as well as perfect your Course; for it's regular and orderly to them that well observe it.

Many neglecting the Observation of the Variation, by arguing from their reckonings, many times talk of Variation where there's none, and sometimes East Variation when it's West, and sometimes tell us of no Variation or a sudden mutation where there's a great Variation and very regular. Others again carrying an *Azimuth* Compass, and being acquainted with the manner of observing the Variation, lay all errors in Reckoning to Currents making many hundreds more than really are or can be.



## Example 4.

From July 26th, at noon, to Noon the 27th, the Courses and Distances Sailed by the *Log* were,

ENE 60 m. } The wind at N by W and N; fair weather  
ENE  $\frac{1}{2}$  Nly 24 } but a fresh Gale, and a deep Northern Sea;  
NE by E 14 } and the Variation 17' West by Observation.  
98 } The true Course and Distance is required.

Variat:  $25^{\circ} 20'$   
17'

Lee-way  $42^{\circ} 20'$   
11 15

True Course  $31^{\circ} 5'$

Courses	Diff.	North	South	East	West
ENE	6	60	22	58	
ENE $\frac{1}{2}$ Nly	5	24	11	31	
NE by E	5	15	7	78	
		41	67	88	24

The Course computed from this tabular Difference of Latitude and Departure, is East  $25^{\circ} 20'$  Nly, and the Distance 93 Miles, but by reason of the Variation her Course is East  $42^{\circ} 20'$  N, and after the allowance of a Point Lee-way East  $31^{\circ} 5'$  Nly; with which and the distance 98 m. I find the Difference of Latitude  $50'$  and the Departure  $84'$  East, but by my Observation I make my Difference of Latitude  $53'$ . *Scilicet* 3' more than my account, which I attribute to a stream.

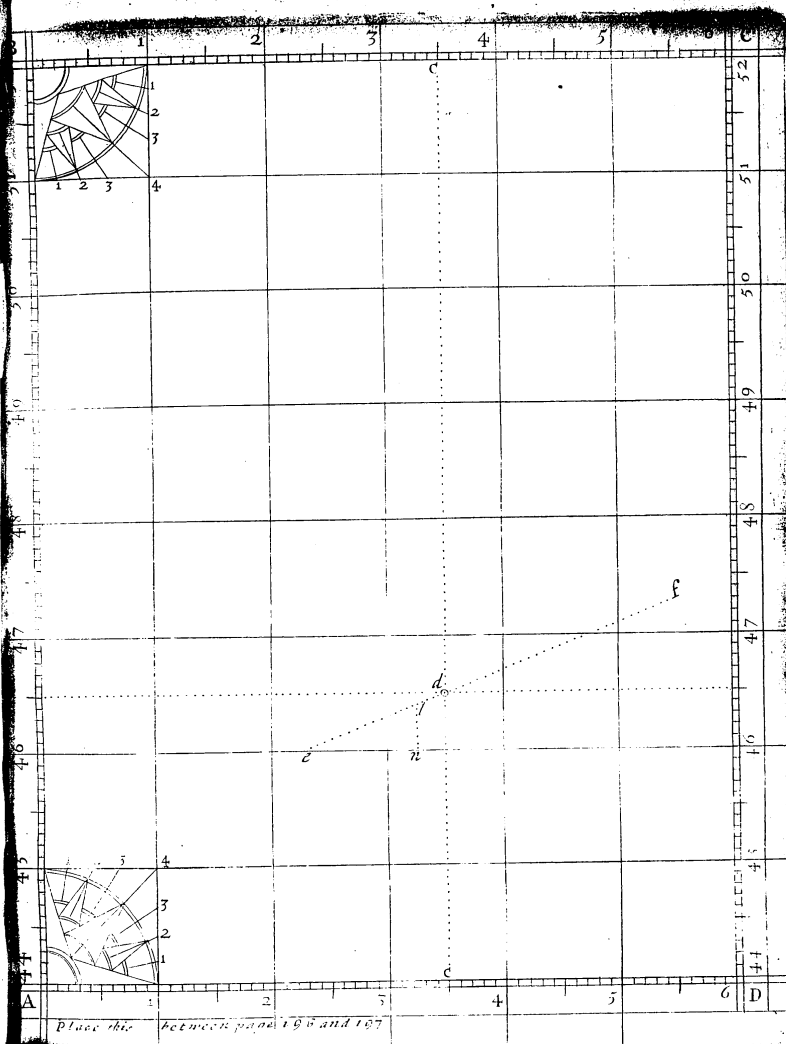
## To make a PLAIN CHART.

Let it be required to make a Particular Chart for a Voyage between the Parallels of  $44^{\circ}$  and  $52^{\circ}$  North Latitude, and to contain  $6^{\circ}$  of Longitude.

First draw the Meridian or North and South Line AB, and cross it at right Angles in the Point A, with another right Line AD representing the Parallel of  $44^{\circ}$ .

$\frac{52}{44}$  Then taking any convenient length for a Degree, Prick it  
8 seven times from A to B marking them 44, 45, 46, &c.  
and five times from A to D marking them 1, 2, 3, &c.

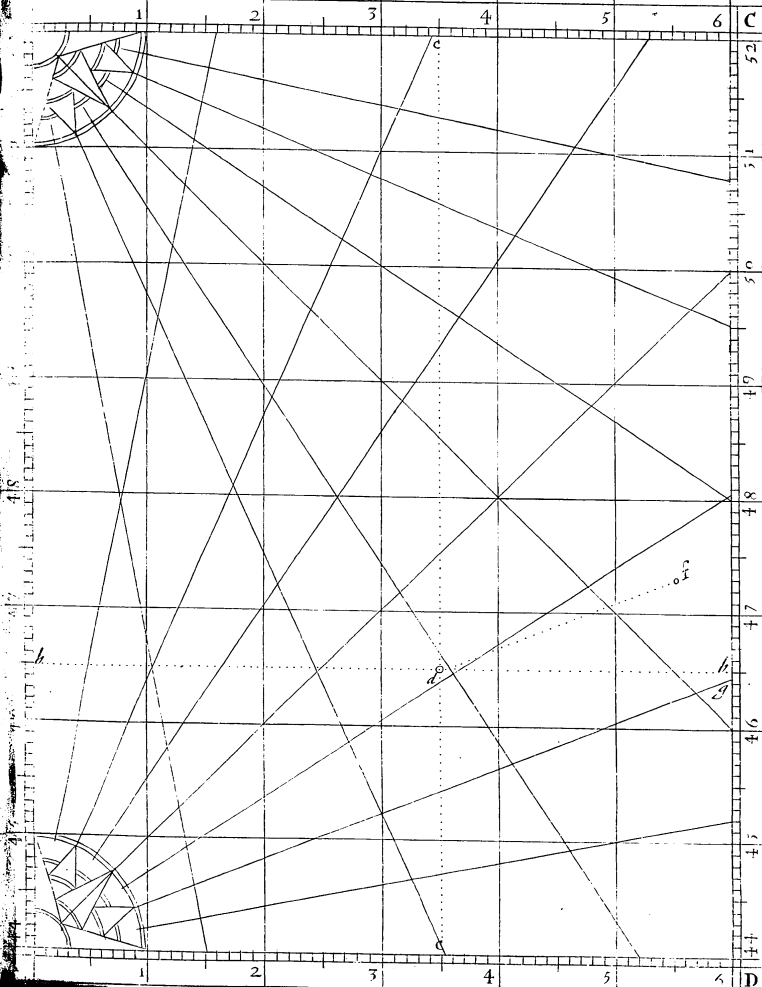
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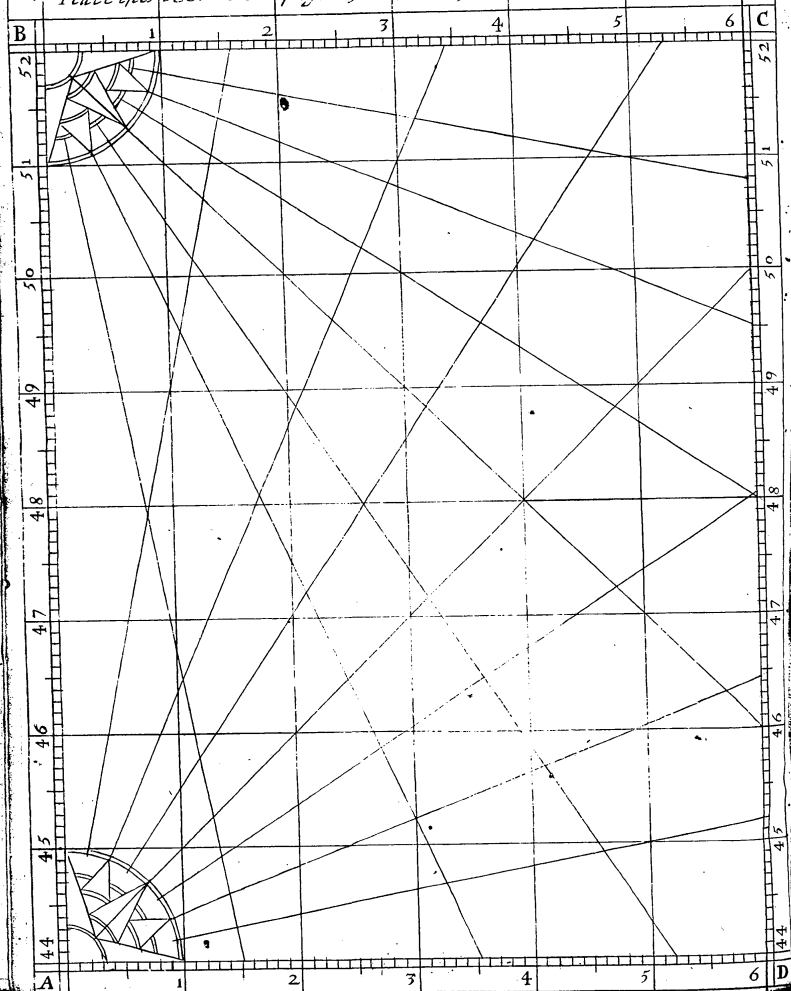
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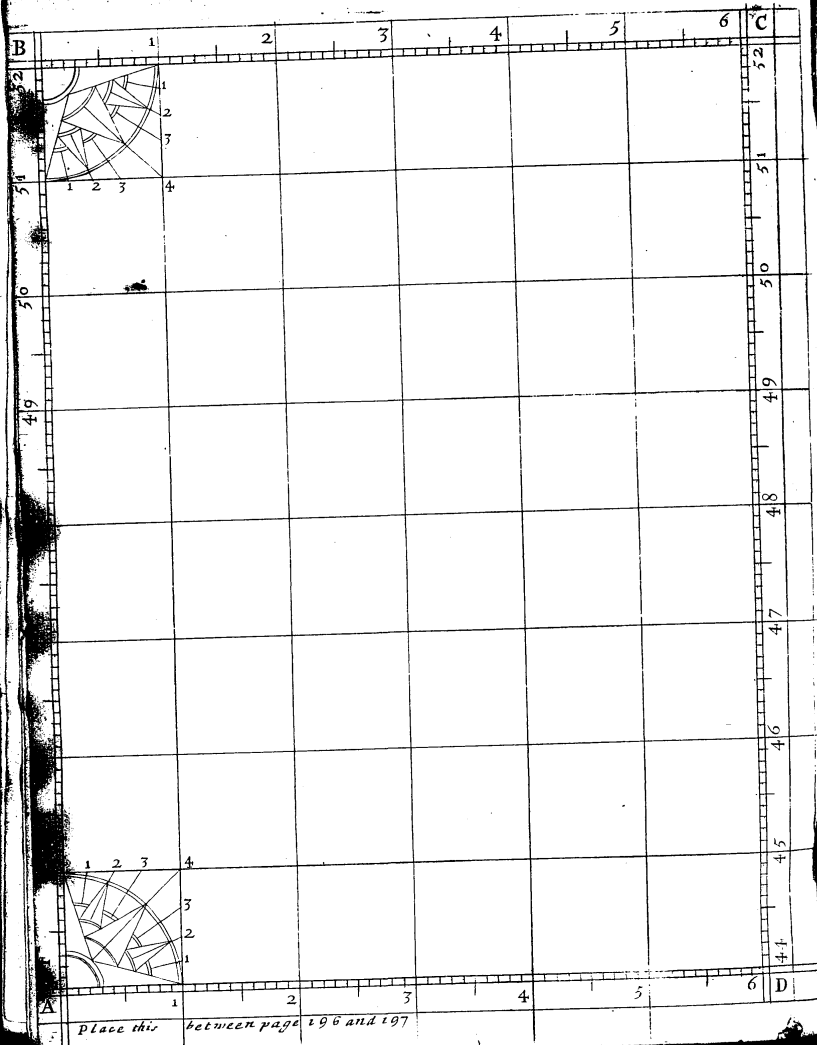


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18







Through D, 5, 4, 3, 2, &c. draw parallels to A B for Meridians, and through B, 50, 49, 48, &c. parallels to A D for Parallels of Latitude, subdividing each Degree both of the extrem Parallels and Meridians into 60, 30, 20, 10, or 12, equal Parts as it will bear, in some convenient place depicting the Compass, with the Rumb-lines drawn forth quite through the Chart.

### To lay down a Place on the Chart.

Let A represent some place in the Latitude  $44^{\circ}$ , and I would lay down another Place that's  $3^{\circ} 30'$  East thereof, and in Latitude  $46^{\circ} 30'$  North.

First, Laying a Ruler over  $46^{\circ} 30'$  of the extrem Meridians, draw the Parallel of  $46^{\circ} 30'$  as *bb*, and laying it over  $3^{\circ} 30'$  of the extrem Parallels draw the Meridian *cc*, and where this Meridian and Parallel cross, as at *d*, is the Place required.

But if I had been to lay down the Place *d* by a Course and Distance given, as suppose I know it should lie North East from A: then from A I draw a Parallel to the North East Rumb-line as *Ad*, and taking five Degrees or 300 *m*, from the Meridian-line, set it from A on the Line *Ad* to *d*.

If I had been to lay it down by the Course and Latitude, by a Ruler over  $46^{\circ} 30'$  of the extrem Meridians, I draw the Parallel of Latitude *bb*, and from A a parallel to the North East Rumb-line as *Ad*, and where these cut one the other as at *d* is the Place to be laid down.

If the Rumb-lines be not drawn on the Chart, you may prick down the line *Ad*, by setting one foot in A as Center, with  $60^{\circ}$  of the Chords describing an obscure Arch, &c. after the Manner of Cases the first and second of this Section.

### To find the Course and Distance between any two Places on the Chart.

Laying a Ruler over the two Places as *df*, see what Rumb-line runs parallel thereto as A *g*, and that shews the Course, which from *d* to *f* is East North East.

But if the Rumb-line be not drawn, only a Compass Card depicted on some part of the Chart as in the second draft, then laying the Ruler over the Places, see how it cuts the Parallels of Latitude or Meridians as in *b* and *l*, taking *ab*, set it from *e* to *n*, and taking *nl* apply it to the side of the square wherein the Compass is, and it shews the Course 2 Points from the East nearly. Then take the extent *df* and apply it to the Scale if there be one, or else apply it to the Meridian, and so many Degrees as it's equal to, so many score Leagues are the Places distant.

How

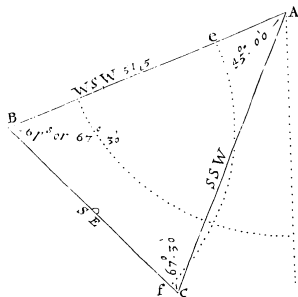


How to make a prick daily or weekly through a whole Voyage, on the Chart by the Courses and Distances, needs no more instructions than what are already given at the beginning of this Section where I have delineated the *Traverse*. I would advise all to keep their reckonings or account of the Voyage in Numbers daily correcting the *dead Reckoning*, and tabulizing the Correct Eastings and Westings, Northings and Southings in particular Columns, and then if at any time a man be desirous to make a prick for the Ships place on his Chart, let him draw a Parallel of Latitude, and a Meridian at his true Departure and where they two cut will be the Ships place.

## SECTION III.

## Oblique Triangles applied to Sailing.

1. **C**oasting along the Shore, I set an Head-land C bearing off me SSW, I sail WSW 51.5 Miles to B, and then the Head-land C bears SE from me: I demand my several Distances to the Head-land?



Geome.

## Geometrically.

Taking any convenient point as A for the Place of the Ship at first, from thence draw a SSW line as AC and a WSW line as AB, and on A B prick 51.5 m. from A to B. Then, Setting one foot of the Compasses in B, with  $60^\circ$  of the Chords describe the Arch  $ef$ , and lay thereon six Points (the Points between ENE and SE) from  $e$  to  $f$  draw- ing Bf.

## Arithmetically.

In the Triangle BAC is given the side BA 51.5 m. and all the Angles, viz. the Angle A  $45^\circ$  or 4 Ps, between the WSW and SSW, the Angle B between the ENE and SE six Points or  $67^\circ 30'$ , and the Angle C between the NW and NNE six Points, to find the sides BC and CA.

As the sine of the Angle at the Head-lands: C 6 Points	9,9656153
Is to the Distance run, AB 51.5 miles	1,7118072
So is the sine of the Angle at the first Place of Observation $\angle A 45^\circ 00'$ ,	9,8494850
To the Distance BC 39.4	11,5612922
	1,5956769

After the same manner you may find the Distance thereof from the first Place of Observation A, but in this Example for as much as the Angles B and C are equal, the side AC will be concluded equal to BA 51.5, without another work.

2. A Ship in the Parallel of  $46^\circ N$  at B, descries an Head-land at C distant from her 67 Miles, she Sails ESE 63 Miles to D, and then the Head-land at C bears SW by W from her. How did the Head-land bear from the Ship when she was at B, and how far is it distant from her now she's at D?

Geome.



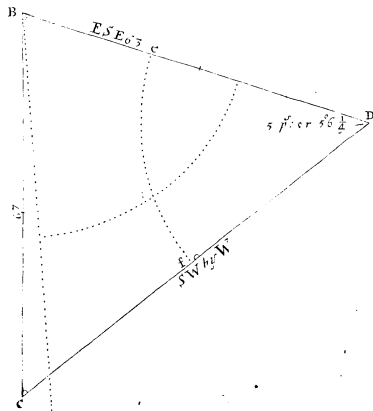
Geometrically.

Geom.

Take any convenient Point as B for the Place of the Ship at first, from thence draw a ESE line, and prick thereon 63 m. from B to D.

Then on D, as Center, with  $60^\circ$  of the Chords describe the arch  $e f$ , and prick five Points (the Points between WNW and SW by W) from  $e$  to  $f$  drawing DfC.

Lastly, Take 67 m. in the Compasses, and setting one foot in B, with the other cros D C in C, and draw B C.



Arithmetically.

Arib.

As the Distance BC 67 m.

Is to the sine of the Angle D  $56^\circ 15'$   
So is the Distance Sailed BD 63 m.

To the sine of the Angle C  $51^\circ 26'$ 

1,8260748
9,9198464
1,7991405
11,719,869
9,8931121

Or

 $51^\circ 26'$  $56 15$  $107 41$  $180 00$  $72 19$ 

Or  $4\frac{1}{2}$  Ps. which added to the Angle D  $56^\circ 15'$ , and that sum taken from  $180^\circ$  the Remainder  $72^\circ 19'$  or  $6\frac{1}{2}$  Ps. is the Angle B, which added to the ESE gives the bearing of C to be  $S\frac{1}{2} W$  by  $fere$ .

\* Then, As the sine of the Angle D  $56^\circ 15'$

9,9198464

Is to the Distance BC 67 m.

1,8260748

So is the sine of the Angle B  $72^\circ 19'$ 

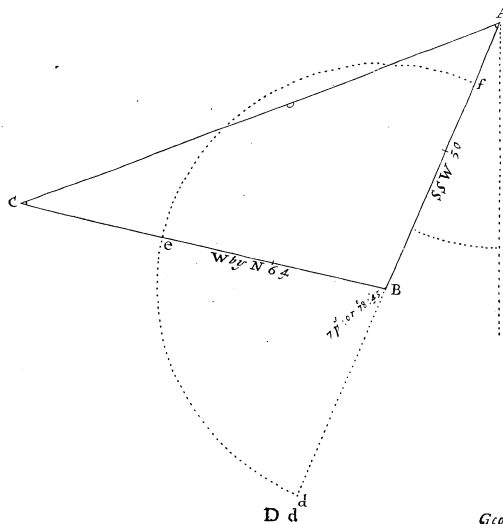
9,9789789

To the Distance DC 76.8

11,8050537

1,8852073

3. If I Sail SSW 50 miles, and then W by N 64 miles. I demand the Courfe and direct distance from the place of Departure.



Geom.



## Geometrically.

Geom.

From A, the point taken for the Ships place at first, draw the SSW line, and lay thereon 50 m. from A to B. Then setting one foot of the Compasses in B with 60° of the Chords describe the semicircle *d e f*, and either prick seven Points (the Points between SSW and W by N) from *d* to *e*, or nine Points from *f* to *e*, and through *e* draw *B e* laying thereon 64 m. from B to C, lastly draw A C.

## Arithmetically.

Arith.

In the Triangle CBA there's given the two sides CB and BA, and the contained Angle CBA, nine Points, to find the Angles A and C, and the third side CA.

Therefore,

As the sum of the two sides A B and B A, } 114 m.		2,0569048
CB 64	Is to their Difference 14 m.	1,1461280
BA 50	So is the Tangent of half the sum of the } Angles C and A: 39° 23'	9,9143020
Sum 114		11,0604300
Diff. 14	To the Tangent of half their difference 5° 45'	9,0035252

$$\begin{array}{r} 16 \text{ Ps. } \angle B \\ 9 \text{ Ps. } \angle C + \angle A \\ \hline 7 \text{ Ps. } = \angle C + \angle A \\ 3 \frac{1}{2} \text{ Ps. the } \angle C + \angle A. \\ \hline 2 \end{array}$$

Which subtracted from 39° 23' there remains 33° 38' the Angle C: but 5° 45' added to 39° 23' makes 45° 8' the Angle A, wherefore seeing A D is a SSW line, A C is WSW nearly, viz. WSW S' Wly.

Then for the Distance A C, Gay,  
As the sine of the Angle A 45° 8'

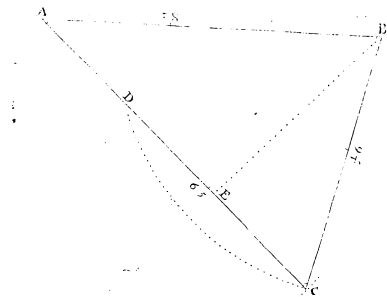
Is to the Distance BC 64 m.  
So is the sine of the Angle B 101° 15' or rather its }  
Complement to 180° Degrees, viz. 78° 45' }

To the Distance A C 88.5 m.

$$\begin{array}{r} 9,8504930 \\ 1,8661800 \\ \hline 9,9915739 \\ 11,7977539 \\ \hline 1,9472609 \end{array}$$

4. Admit

4. Admit two Ports lying in the same Parallel or Latitude, differing in Longitude 58 miles, and a Ship having Sailed from the Westernmost between the S and E 65 miles, be then 46 miles from the Easternmost: I demand the Course she steered, and her Course to the Easternmost Port.



## Geometrically.

Having drawn an East and West line, and laid thereon 58 m. from A to B, take 65 m. in the Compasses, and setting one foot in A with the other describe an Arch, afterwards take 46 m. and setting one foot in B, with the other cross the former Arch in C, Lastly draw A C and B C.

## Arithmetically.

As A C 65 m.		1,8129134
58	Is to the sum of the distances A B and B C, 104 m.	2,0170333
46	So are their Difference 12 miles.	1,0791812
104		1,0962155
12	To A D 19.2.	1,2833011

Which added to A C 65, makes 84.2 whose half 42.1 is A E.

D d 2

Then,



Then, As  $AB$  58 m.

1,763,4280

Is to the Radius

10,000,0000

So is  $AE$  42.1

1,624,1821

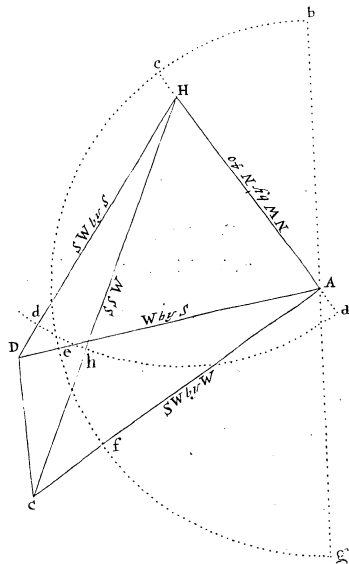
To the Cosine of the Angle  $A$   $43^{\circ} 28'$

11,614,1811

9,860,8541

That is,  $SE$   $1^{\circ} 32'$  Ely, the Course she steered.

5. Coasting along the Shore, I set two Head-lands, the one at  $C$  bearing  $SW$  by  $W$ , the other at  $D$  bearing  $W$  by  $S$ , I sail away  $NW$  by  $N$  to  $H$  40 Miles, and then the Head-land at  $C$  bears  $SSW$ , and that at  $D$   $SW$  by  $S$ . I demand how far these Head-lands are asunder, and how they bear one from the other?



Geom.

*Geometrically.*

First, draw a North and South line as  $bA$ , and with  $60^{\circ}$  of the Chords *Geom.* setting one foot on some convenient point for the Ships place at first as  $A$ , describe the semicircle  $bAg$ , then prick thereon five points from  $g$  to  $f$ , seven points from  $g$  to  $e$ , and three points from  $b$  to  $c$ , and draw  $AfC$ ,  $AdC$ , and  $AHc$ , laying 40 m. from  $A$  to  $H$

Secondly, Set one foot of the Compasses opened to  $60^{\circ}$  of the Chords on  $H$ , and describe the Arch  $ad$ , and prick thereon five points (the points between South East by South, and South South West) from  $a$  to  $b$ , and six points (being the points between the South East by South and South West by South) from  $a$  to  $d$ , and draw  $HbC$ ,  $HdC$ , and  $DC$ . Then is  $D$  one Head-land and  $C$  the other.

*Arithmetically.*

In the Triangle  $HAC$ , there's given the Angle  $HAC$ , eight points *Arith.* (*viz.* the points between the South West by West, and the North West by North,) the Angle  $AHC$  five points (between the South East by South, and South South West) and the Angle  $ACH$  three points (the points between the North East by East and North North East,) and the side  $HA$  40 Miles, to find the side  $CH$ .

Therefore,

As the sine of the Angle  $HCA$   $33^{\circ} 45'$

9,744,7390

Is to  $AH$  40 Miles

1,602,0600

So is the sine of  $90^{\circ}$  the Angle  $HAC$

10,000,0000

11,602,0600

To the side  $HC$  72 Miles.

1,857,2310

Then in the Triangle  $DHA$ , there's given the Angle  $HAD$  six points (*viz.* the points between the North West by North, and West by South,) and the Angle  $AHD$  six points (*Scilicet:* the points between the South East by South, and South West by South) and the Angle  $HDA$  four points (between the North East by North, and the East by North) and the side  $AH$  40 Miles to find the side  $DH$ .

Thus,



Thus,

As the sine of the Angle HDA  $45^{\circ} 00'$

9,8494850

Is to the side AH 40 Miles

1,6020600

So is the sine of the Angle HAD  $67^{\circ} 30'$

9,9656153

11,5676753

To DH 52.3 Miles

1,7181903

1                      Lastly, In the Triangle DHC, there's given the  
16 Ps. two sides CH 72 Miles, and DH 52.3 Miles, and  
1 Ps. and their contained Angle CHD one point, to find the  
2) 15                      other two Angles HDC, HCD, and the third  
       $7\frac{1}{2}$  Ps.                      side DC.

As the sum of the sides HC and HD 124.3

2,0944711

Is to their Difference 19.7

1,2944662

So is the Tangent of half the sum of Angles HDC }  
and HCD  $7\frac{1}{2}$  points or  $84^{\circ} 22'$  }

11,0059546

12,3004208

To the Tangent of half their Difference  $58^{\circ} 6'$

10,059497

Which added to  $84^{\circ} 22'$  makes  $145^{\circ} 28'$  the Angle HDC, but  
subtracted leaves  $25^{\circ} 16'$  the Angle HCD which is North a quarter  
point Westerly.

As the sine of the Angle HCD  $25^{\circ} 16'$

9,6302568

Is to DH 52.3 Miles

1,7181903

So is the sine of the Angle DHC  $11^{\circ} 15'$

9,2902357

11,0084260

To DC 23.9 Miles the Distance between the }  
two Head-lands. }

1,3781692

## SECTION

## SECTION IV.

### MERCATORS Sailing.

Though the *Plain Chart* be very desirable for its easiness, and very useful in short Voyages, and will serve in the longest Voyages if a man Sail home in or near the opposite Rumb he went by; as the Antients, who being Coasters did before the Use of the Compass. Yet forasmuch as few places or indeed none but such as lie under the same Meridian, or under the Equinoctial, can therein be expressed according to their true Situation and distance one from another: but if they be laid down true by the Course and distance, the Difference of Longitude will be false; if they be laid down by the Course and Difference of Longitude, then will the distance and difference of Latitude be more than it should be; and if they be laid down by their distance and difference of Longitude, which in many cases is impossible, the difference of Latitude will always be too little, and the Rumb too wide from the Meridian; and if they be laid down by their Latitudes and Separation, then the Course will be wide and the distance too much, &c. And since that the places in Particular *Maps* or *Charts* being laid down in some one way, and in others another, and these Pieces many times tackt together without due consideration of the differing Methods places have been laid down by, the *Geography* and *Hydrography* of the World is so corrupted, that there are scarce extant any Descriptions of the whole, or large parts, that are not notoriously erroneous, and the shape of the Lands much distorted, it were to be wish'd that the World would not put over much value thereon, nor use it in the laying down Places, but by degrees as much as may be wean it self from the use of the *Plain Chart*, and by making the *True Chart* easie and familiar bring it in request and use, seeing there is such a thing.

It was the great Study of our Predecessors, to contrive such a *Chart* in *Plana* with trait lines, on which all or any parts of the World might be truly set down according to their Longitudes, Latitudes, Bearings, and Distances; a way was hinted almost 2000 Years since by *Ptolomy*, and a general *Map* according thereto made in our preceding age by one *Mercator* (whence it's called *Mercators Chart*;) but the thing demonstrated, and a ready way shew'd of describing it, was not till Mr. *Wright* about 100 Years since taught to enlarge the Meridian-line, by the continual addition of Secants, so that all the Degrees of Latitude might be proportional to those of Longitude, as on the Globe, which he has done after such an excellent manner, that in many respects it's far more convenient for the *Navigators* use than the Globe it self, and will truly shew the Course and Distance from Place to Place, which way forever a Ship Sail forth or returns.



To find the Meridional Miles or Minutes answering to any Difference of Latitude.

First, By the Table of Meridional Parts, Page 68th of the *Volum of Tables*. Look the Degrees of either Latitude over head, and the minutes in the left hand Colum downward, and in the Angle of meeting are the parts for that Latitude.

So also look out the parts for the other, then if both Latitudes be of the same name, that is both North or both South, subtraſt theſe one from the other, and that remainder contains the Meridional Miles ſought.

Example 1.

Let it be required to find the Meridional Minutes or Miles, between Latitude  $43^{\circ} 15' N$ , and  $50^{\circ} 20' N$ .

Latitude $50^{\circ} 20'$	350572	Merid. Parts.
Latitude $43 15$	288375	
The Meridional parts or Miles in the Difference of Latitude.	622.0	(Difference.

Example 2.

Let one Latitude be $20^{\circ} 17' S$ ,	12432	Merid. Parts.
The other Latitude be $18 53 N$ ,	11541	
The Merid. Miles between theſe two Latitudes.	2397.3	(Sum.

To find the Parts by the Table of Artificial Tangents.

The *Logar. Tangents* above  $45^{\circ}$ , accounting every  $30'$  to be one Degree, and every minute to be two minutes of the Meridian-line, are in the ſame Ratio with the Meridional parts made by the continual addition of *Nat. Secants*.

Therefore, Take half of each of the given Latitudes, and to each half add  $45^{\circ}$ , looking the Tangents of theſe Arches in the Table of *Logar. Tangents*, the difference of theſe *Tangents* divide by 1263, and the Quotient ſhall be the Meridional minutes or miles, or if you divide by 3789.7, the Quotient will be the enlarged Difference of Latitude in Leagues.

In

Example 1.

In the firſt of the former *Example*, Lat.  $50^{\circ} 20'$  }  
its  $\frac{1}{2}$  is  $25^{\circ} 10'$  which added to  $45^{\circ}$  makes  $70^{\circ} 10'$  } 4428786  
the *Tangent* whereof is,

The  $\frac{1}{2}$  of Lat.  $43^{\circ} 15'$  is  $21^{\circ} 37' \frac{1}{2}$  which added to  
 $45^{\circ}$  makes  $66^{\circ} 37' \frac{1}{2}$  the *Tangent* whereof is,

1263)	785846	(622 the
	280	Merid.
	278	Miles as
	260	before.

Example 2.

The  $\frac{1}{2}$  of Latitude  $20^{\circ} 17' S$ outh, is  $10^{\circ} 8' \frac{1}{2}$  which  
added to  $45^{\circ}$  makes  $55^{\circ} 8' \frac{1}{2}$  the *Logar. Tan.* } 1570607  
gent whereof is,

The  $\frac{1}{2}$  of the Latitude  $18^{\circ} 53'$  is  $9^{\circ} 26' \frac{1}{2}$  which  
added to  $45^{\circ}$  makes  $54^{\circ} 26' \frac{1}{2}$  the *Logar. Tan.* } 1457970  
gent whereof is,

1263)	3028577	(2397
	50160	The Miles
	123	between
	100	theſe two
		Latitudes.
	1166	

1. The Latitudes and Difference of Longitude of two Places given,  
to find the Courſe and Diſtance.

Admit the Courſe and diſtance between *Teneriffa* in Latitude  $28^{\circ} 20' N$ ,  
and St. *Michael* (one of the *Azores* Iſles) in Latitude  $38^{\circ} 00' N$ , whole  
Difference of Longitude is  $8^{\circ} 48'$  be required.

E c

Geome.

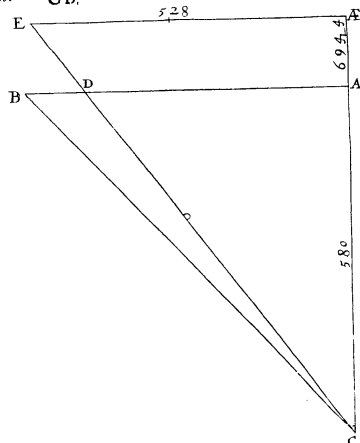


## Geometrically.

Geom.

58	45'
60	
<hr/> 628 Miles.	
Latitude	38° 00'
Latitude	28 20
60	
<hr/> 580 Miles.	

Having drawn the Meridian  $\text{ÆC}$ , and laid 694.4 Miles, the Difference of Latitude enlarged from  $\text{Æ}$  to  $\text{C}$ , and on  $\text{Æ}$  raised a Perpendicular, prick 528 Miles, the Difference of Longitude on  $\text{ÆE}$ , from  $\text{Æ}$  to  $\text{E}$ , and draw  $\text{CE}$ , then prick 580 Miles the true Difference of Latitude from  $\text{C}$  to  $\text{A}$ , also on  $\text{A}$  raise a Perpendicular, as  $\text{AB}$ , pricking thereon 528 Miles from  $\text{A}$  to  $\text{B}$ , and draw  $\text{CB}$ .



Then is  $\text{C}$  the Isle *Teneriff*,  $\text{B}$  *St. Michael* according to the *Plain Chart*,  $\text{E}$  *St. Michael* according to the true *Chart*,  $\text{BC}$  the distance between them on the *Plain Chart*,  $\text{CE}$  the enlarged distance, and  $\text{CD}$  the true distance,  $\text{BC}$  the *Rumb*-line between them according to the *Plain Chart*,  $\text{CE}$  the true *Rumb*-line,  $\text{BCA}$  is the Course according to the *Plain Chart*, and  $\text{ECÆ}$  the true Course according to the *Mercators Chart*,  $\text{EÆ}$  is the true Difference of Longitude,  $\text{AD}$  the true Meridian distance or Departure.

For

## For the Course.

Say,	
As the Difference of Latitude enlarged $\text{CÆ}$	694.5 m.
Is to the Radius,	
So is the Difference of Longitude $\text{EÆ}$	528 m.
To the Tangent of the true Course $\text{ECÆ}$	$37^{\circ} 15'$

Which sheweth the Course from *Teneriff* to *St. Michael*, to be  $3\frac{1}{2}$  points from the North Westward, that is  $\text{NW}$  by  $\text{N}\frac{1}{4}\text{W}$  or neerer  $\text{NW}$  by  $\text{N}3^{\circ}30'$  Westerly.

## For the Distance.

As the Cosine of the Course $\text{Cof: } \angle \text{ECÆ}$	$37^{\circ} 15'$
Is to the Difference of Latitude $\text{CA}$	580 miles
So is the Radius,	
To the true Distance on the Rumb $\text{CD}$	728.7

But by measuring  $\text{BC}$ , I find the Distance according to the *Plain Chart* 784, so that the *Plain Chart* sheweth the Distance more than it is by 56 Miles, and the Course more Westerly than the truth by almost  $\frac{1}{2}$  a point, and the Departure a great deal too much.

## For the Course.

Set one foot of the Compasses in 694.4 on the Line of Numbers, and extend the other to 528; then keeping the same extent, set one foot on the Tangent of  $45^{\circ}$  turning the other backward, and it will fall on  $37^{\circ} 15'$  the Course.

## For the Distance.

Set one foot in  $52^{\circ} 45'$  of the Line of Sines, and extend the other to the sine of  $90^{\circ}$ , then keeping the same extent, set one foot in 580 of the Line of Numbers, and turn the other forward, and it will fall on 728.7 the Distance on the Rumb. There is a neerer passage between these two Places, which is by the Arch of a Great Circle; of which in its Place.

This Proposition is first of use in a Voyage.

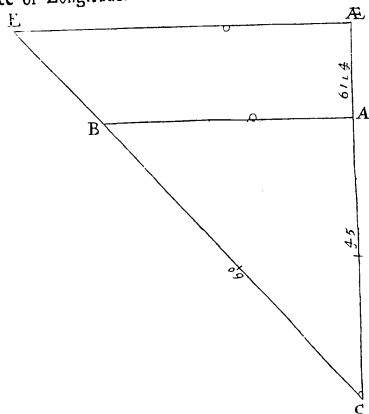
E c 2

2. The



2. The Latitudes of two Places, and their Distance given, to find the Course and Difference of Longitude.

A Ship from the Latitude  $42^{\circ} 30'$  North, Sails North-westward 60 Miles, 'till she be in the Latitude  $43^{\circ} 15'$ . I demand the Course and Difference of Longitude.



Geometrically.

First, With the Difference of Latitude and Distance given, delineate according to the third Proposition of Plain Sailing. Then produce the Meridian and Rumb-line, and lay 61.4 the Difference of Latitude enlarged from C to Æ, Lastly, through Æ draw Æ E Parallel to B A.

Geom.

$43^{\circ}$	$15'$
$42^{\circ}$	$30'$
<hr/>	
0	45

Eor

For the Course.

As the Distance Sailed CB 60 m.

1,7781513

Is to the Radius,

10,0000000

So is the Difference of Latitude CA 45 m.

1,6532125

To the sine Complement of the Course  $\angle 41^{\circ} 25'$  }  
that is NW by N  $7^{\circ} 40'$  Westerly. }

11,6532125

9,850612

For the Difference of Longitude.

First, Find the Meridional Miles in the Difference of Latitude, which are here 61.4.

Then say,

As the Radius,

10,0000000

Is to the Difference of Latitude enlarged C Æ 61.4 Miles,

1,7881684

So is the Tangent of the Course  $\angle C 41^{\circ} 25'$

9,9455354

To the Difference of Longitude in Miles Æ E 54.17.

1,7337038

For the Course.

The extent of the Compasses from the Distance Sailed 60 m. to the Difference of Latitude 45 m. will reach (the same way) from the Radius to the sine of  $41^{\circ} 25'$ , the Complement of the Course, which subtracted from  $90^{\circ}$ , leaves the Course required.

For the Difference of Longitude.

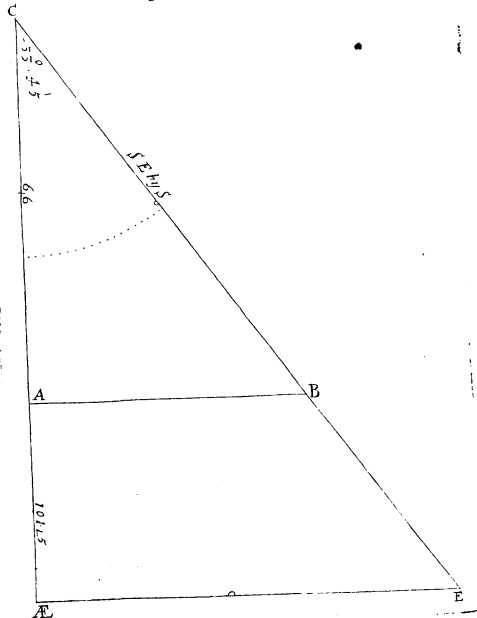
The extent from the Radius t.  $45^{\circ}$ , to the Tangent of the Course  $41^{\circ} 25'$ , will reach from the Difference of Latitude enlarged 61.4 m, to the Difference of Longitude 54.17 m.

3. Both



3. Both Latitudes and the Course being given, to find the Distance and Difference of Longitude.

A Ship from the Latitude  $50^{\circ} 00'$  North, Sails South East by South, 'till she be in the Latitude  $48^{\circ} 54'$  North, I demand the Distance Run and the Difference of Longitude.



Geometrically.

Given.

$50^{\circ} 00'$   
 $48^{\circ} 54'$   
 $1^{\circ} 06'$   
 $60$   
 $66$

Having drawn a Meridian line  $CAE$ , described an Arch, laid thereon the Course, drawn the *Rumb-line*  $CE$ , and raised the Perpendicular  $BA$ , according to the second Case of *Plain Sailing*, enlarge the Latitude, and lay the Difference of Latitude enlarged  $101.5 m$ . from  $C$  to  $A$ , and on  $A$  raise the Perpendicular  $AE$ .

For

For the Distance.

As the Cosine of the Course $33^{\circ} 45'$	9,915,8464	Arith.
Is to the Difference of Latitude $CA$ 66 m.	1,8195439	
So is the Radius	10,0000000	
To the Distance $CB$ 79.3	11,8195439	
	1,8996975	

For the Difference of Longitude.

As the Radius,	10,0000000	
Is to the Difference of Latitude enlarged $CAE$ 101.5 miles,	2,0064660	
So is the Tangent of the Course $t. \angle C$ $33^{\circ} 45'$	9,8248926	
To the Difference of Longitude $AE$ 67.8	21,8313586	
	1,8313586	

4. One



4. One Latitude, the Course and Difference of Longitude, being given, to find the other Latitude and the Distance.

Admit I Sail from Latitude  $32^{\circ} 00'$  North, North East by North  $3^{\circ}$  Easterly until I have altered my Longitude  $1^{\circ} 3'$ : How much have I raised the Pole, and what is my Distance Sailed?

*Geometrically.*

*Geom.*

Having drawn the Meridian  $C\bar{A}E$ , described an Arch, pricked thereon the Course, and drawn the *Rumb-line*  $CE$ , at the extent 63 of the equal Parts or Miles, draw a parallel to the Meridian  $C\bar{A}E$  as  $F\bar{E}$ , and from the point  $E$  let fall a perpendicular to  $C\bar{A}E$  as  $E\bar{A}$ ; then add to the measure of  $C\bar{A}E$  84.3 m. the Difference of Latitude enlarged the Meridional Miles for  $32^{\circ} 00'$  of Latitude, and the sum looked in the Table of Meridional Parts gives  $33^{\circ} 11'$  the Latitude she's arrived in.

Lastly, Subtract these Latitudes one from the other, and the difference turned into Miles prick from  $C$  to  $A$ , through  $A$  drawing  $AB$  parallel to  $\bar{A}E$ .

*For the Difference of Latitude.*

*Arith.*

As the Tangent of the Course the Angle  $C$   $36^{\circ} 45'$

9,3731663

Is to the Difference of Longitude  $E\bar{A}$  63 miles,  
So is the Radius

1,7993405  
10,0000000

To the Difference of Latitude enlarged  $C\bar{A}E$  84.3

11,7993405  
1,9261737

The Meridional Miles answering to  $32^{\circ} 00'$  of Latitude are  
To which add

2028.4  
84.3

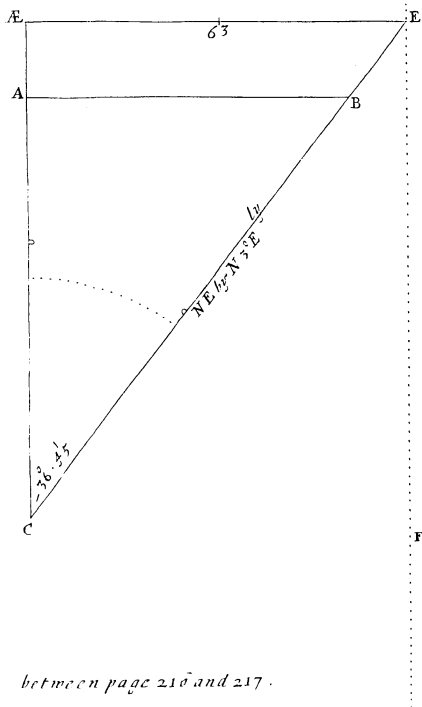
The Sum is

2112.7

Which looked in the Table of Meridional parts gives the Latitude  $33^{\circ} 11'$ .

*For*





For the Distance,

As the Cosine of the Course  $36^{\circ} 45'$

9,9037701

Is to the true Difference of Latitude AC 71 Miles

1,8512583

So is the Radius

10,0000000

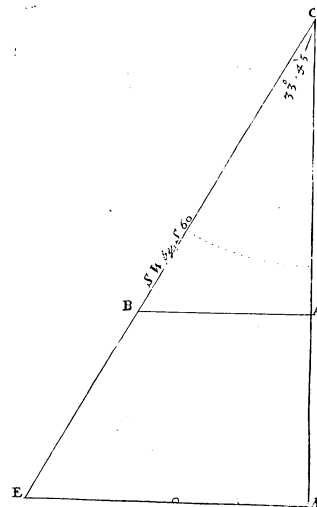
To the Distance CB 88.7 Miles

11,8512583

1,9474882

5. The Course and Distance and one Latitude being given, to find the other Latitude and the Difference of Longitude.

If a Ship from Latitude  $53^{\circ} 30'$  North, Sail South West by South  $60$  Miles; what Latitude will she then be in, and what will be the Difference of Longitude?



E f

First,



First, Protract the Course and Distance according to *Case first of Plain Sailing*.

Then measure the Difference of Latitude CA, and that measure subtract (because she depresses the Pole) from Latitude  $53^{\circ} 31'$ , and the remainder  $52^{\circ} 40'$  is the Latitude she's arrived in. Thirdly, by the Table of Meridional Parts find the enlarged Difference of Latitude as formerly directed, and prick that, viz.  $83.2$  from C to Æ.

Lastly, On Æ raise a perpendicular to C Æ as Æ E, and produce the *Rumb-line* B C 'till it meets which Æ E.

*For the Difference of Latitude.*

<i>Arith.</i>	<i>As the Radius,</i>	10,000000
	<i>Is to the distance Sailed B C 60 miles.</i>	1,7781512
	<i>So is the Cosine of the Course <math>33^{\circ} 45'</math></i>	9,9198464
		1,6979976
	<i>To the Difference of Latitude CA 50 miles or minutes.</i>	1,6979976

Which subtracted from  $53^{\circ} 30'$  leaves  $52^{\circ} 40'$  the Latitude required, the difference of which two Latitudes enlarged is  $83.2$ .

*For the Difference of Longitude.*

<i>As the Radius,</i>	10,000000
<i>Is to the Difference of Latitude enlarged C Æ 83.2 miles.</i>	1,9201233
<i>So is the Tangent of the Course <math>33^{\circ} 45'</math></i>	9,8248926
	1,7450159
<i>To the Difference of Longitude Æ E 55.6 miles,</i>	1,7450159

*For the Difference of Latitude.*

*By the Gunter.* Set one foot in the sine of  $90^{\circ}$ , and extend the other to the sine of  $56^{\circ} 15'$ . Then keeping the same extent set one foot in 60 on the *Line of Numbers*, and the other turned backward will fall on 50 Miles the Difference of Latitude, which because she depresses the Pole, subtract from  $53^{\circ} 30'$ , and the remainder  $52^{\circ} 40'$  is the Latitude the Ship is in. The Difference of which two Latitudes enlarged is  $83.2$ .

For

*For the Difference of Longitude.*

Set one foot of the Compasses in the *Tangent* of  $45^{\circ} 00'$ , and extend the other to the *Tangent* of  $33^{\circ} 45'$ : then keeping the same extent set one foot in 83.2 on the *Line of Numbers*, and turn the other foot backward and it will fall on 55.6 m. the Difference of Longitude.

There be several other Propositions of *Mercators Sailing*, as

6. By the one Latitude, Distance Sailed, and Departure, to find the Course, Latitude the Ship is in, and the Difference of Longitude.

7. By the Departure, and both Latitudes given, to find the Distance Sailed, Difference of Longitude and Course.

8. The Course, one Latitude, and the Departure given, to find the Distance, Difference of Latitude, and Difference of Longitude.

But these being of no great use I shall omit, and insert two or three Propositions of Sailing under a Parallel of Latitude.







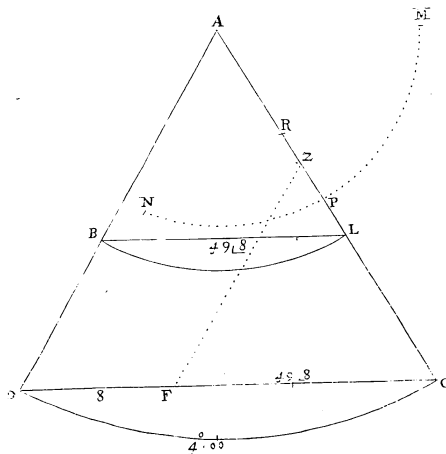
Arithmetically.

Arith.	As AL the Cosine of $51^{\circ} 30'$ the Latitude	9,794,1496
80	Is to AC the Radius or sine of $90^{\circ}$	10,000,0000
3	So is the Distance Sailed BL 49.8 Leagues	1,697,2396
60   24   0		11,697,2396
4 00	To the Difference of Longitude DC 80 Leagues.	1,903,0900

Which turned into degrees is  $4^{\circ} 00'$ .

By this Canon was made the Tables beginning Page 94, and Page 108 of the Volumn of Tables.

By the Gunter. Set one foot in the sine of  $38^{\circ} 30'$ , and, extend the other to the Radius or sine of  $90^{\circ}$ , then keeping that extent set one foot in 49.8 of the Line of Numbers, turning the other forward, and it will fall on 80 the Difference of Longitude.



between page 222 and 223. this Sch. belongs to f  
Prop. on the next Page viz. page 223

3. The

3. The Distance Sailed under any Parallel of Latitude, and the Difference of Longitude being given, to find the Parallel or Latitude.

If a Ship Sail East or West 49.8 Leagues, and thereby differ her Longitude  $4^{\circ} 00'$ : what Parallel or Latitude has she Sailed under?

Geometrically.

Having drawn the Meridian AC, and with  $60^{\circ}$  of the Chords described the arch NM, and with AC (the double of AP) described the arch DC, and laid 80 Leagues the Difference of Longitude from C to D and drawn DC, AD, prick 49.8 Leagues the Distance, on CD from C to F, and through F draw a Parallel to DA as FZ, then with ZC, as Radius, setting one foot of the Compasses in A, with the other describe the arch BL. Lastly, bisect AL with a line at right Angles thereto as NM, then is the arch PN or PM cut off by this line equal to the Latitude.

Arithmetically.

As the part of the Equinoctial CD, 80 Leagues, the Difference of Longitude.	1,903,0900	Arith.
Is to the Semidiameter of the Equinoctial CA, the Radius or sine of $90^{\circ}$ .	10,000,0000	
So is the part of the Parallel LB 49.8 Leagues the Distance Sailed.	1,697,2396	
To AB the Semidiameter of the Parallel, which is equal to the Cosine of the Latitude S: $38^{\circ} 30'$ .	11,697,2396	
	9,794,1496	

By the Gunter.

The Extent of the Compasses, from the Difference of Longitude 80 Leagues to the Distance 50 Leagues, will reach from the sine of  $90^{\circ}$  to S:  $38^{\circ} 30'$  the Complement of the Latitude.

There be several other of this kind, as  
Admit two Ships under the Equinoctial 100 Leagues distant asunder, and they Sail both directly North 550 Leagues. How far will they then be asunder?

Two



Two Ships in Latitude  $50^{\circ} 40'$  North distant 50 Leagues one from the other, they Sail both directly North 700 Leagues: how far shall they then be Distant asunder, &c?

## SECTION V.

*To make a MERCATORS Chart.*

**T**HE Chart may be made either General for the whole World, or Particular, for some certain part thereof.

He that understands the making of the one cannot be ignorant how to proceed for the other, therefore I shall only shew

*To describe a Particular Chart, for some certain Number of Degrees of Longitude, and Latitude: more or less according as a Voyage shall require.*

Let it be required to draw a Chart for a Voyage, between the Parallels of  $44^{\circ}$  and  $50^{\circ}$  of North Latitude, and to contain  $6^{\circ}$  of Longitude.

First, Draw the North and South Line A B, and cross it at right Angles in the point A, with another right line A D, representing the Parallel of  $44^{\circ}$ .

Then taking 1 or 10 from any line of equal parts or Diagonal Scale, prick it on A D six times from A to D for the  $6^{\circ}$  of Longitude, marking them 1, 2, 3, &c. As in the Draft, subdividing each of these Degrees into ten equal parts which will be  $6'$  each, and afterwards through A, draw A B Parallel to D C.

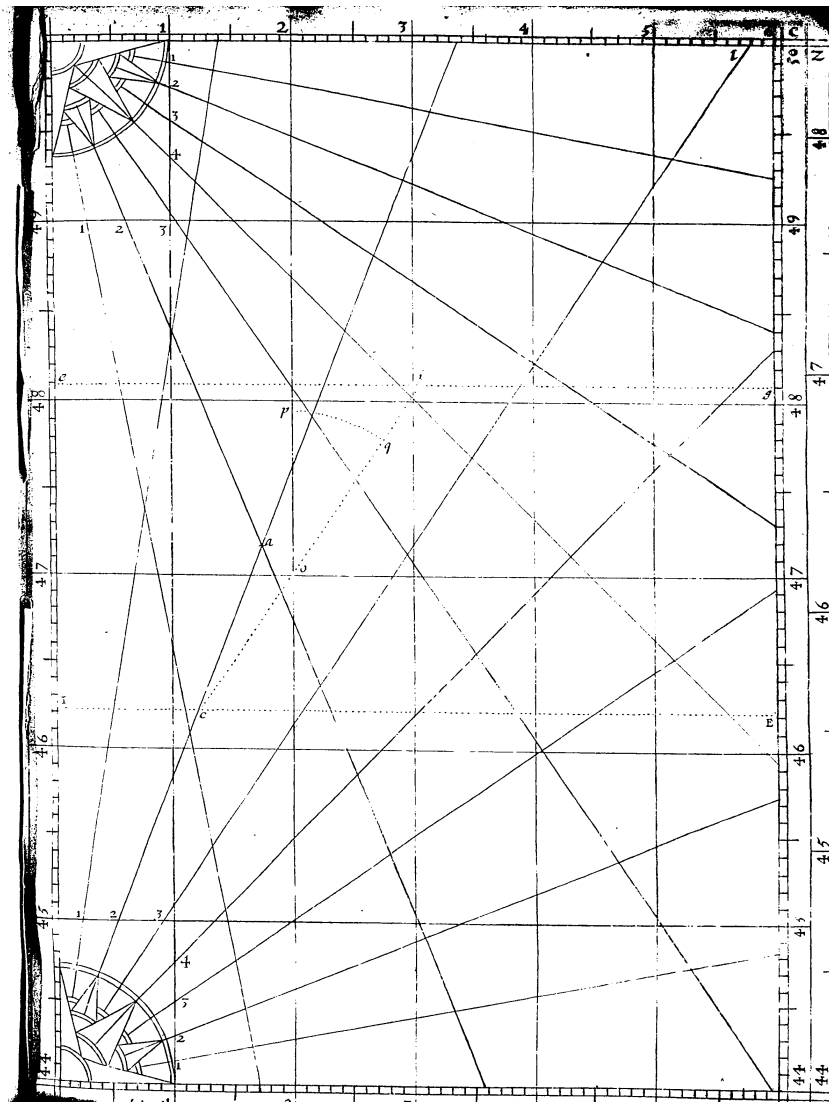
Secondly, Look in the Table of Meridional parts, for the parts answering to both Latitudes,

$$\text{Against } \left. \begin{array}{l} 50^{\circ} \\ 44 \end{array} \right\} \text{ are } \left\{ \begin{array}{l} 34745 \\ 29459 \end{array} \right.$$

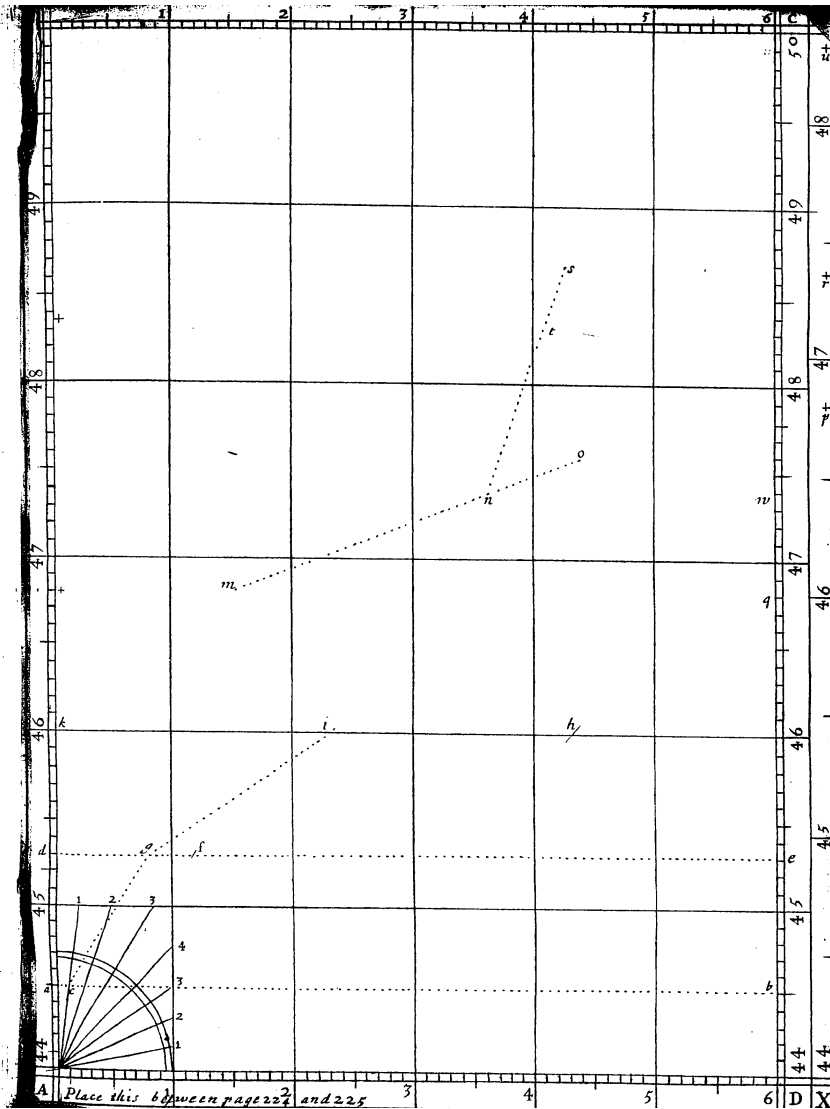
528.6 the Difference.

The Difference of these Numbers answering to both Latitudes, viz. 528.6 Miles, take from the Diagonal Scale and prick on the Meridians from A to B, and from D to C, and draw B C, the Parallel of  $50^{\circ}$  of Latitude, so are both the extrem Meridians and Parallels drawn.

Thirdly,









Thirdly, Through 1, 2, 3, 4, &c. of the Line A D draw Parallels to A B, which will be the Meridians of the *Chart*. Now if you have a *Meridian Line* answerable to the equal parts used, as there is one on the *Gunters Scale*, it is but transferring the Divisions thereof to the Meridian A B, either by laying the edge of the Scale that has the Meridian Line graduated on to the Meridian A B, or taking them with the Compasses, &c. and through these points 45°, 46°, 47°, &c. of the Meridian A B drawing Parallels to A D, and the *Chart* is compleatly graduated.

Else taking out of the Table of Meridional parts the Numbers for Latitude 44°, and any other Degree you have a mind to prick down, subtract them one from the other, and the Difference taken from the Diagonal Scale lay from A upwards.

$$\text{Thus the parts for } \left. \begin{array}{l} 47^\circ \\ 44^\circ \end{array} \right\} \text{ are } \left\{ \begin{array}{l} 3:0:8 \\ 29459 \end{array} \right. \\ \hline 256.9$$

The Difference 256.9 prick from A to 47°, so proceeding for the rest, even the subdivisions also.

If the two extream Latitudes be one South, and the other North, that is not both in one Hemisphere, then add the Meridional parts of both Latitudes together, and the Sum pricked on the North and South line gives the length of the *Chart*. You may describe a Compass in some convenient place, and draw the *Rumb-lines* as in the first draft.

Lastly, On the out side of D C, make another line of equal parts X Z, whereof each degree may be twice as large as a degree of Longitude, and divide and graduate it as you see in the draft, I call this line the *Assistant*.

Sometimes the line A D must be used as a line of Leagues, and then will this *Assistant-line* be of use and not else.

*To lay down a Place, or make a prick on the Chart.*

*To lay down a Place by the Course and Distance.*

Admit you have Sailed from A, a place in Latitude 44° North, 48 Leagues North North West, and it be required to prick the place the Ship is in.

Take 48 Leagues out of the line of Longitude A D, and enter it on the second *Rumb* or North North West line from A to *a*, the nearest distance from *a* to A D prick in the *Assistant-line* from X to *b*, and it shews that the Ship is arrived at the end of 48 Leagues Sail in Latitude 46° 14' to which Latitude looked on the Meridian A B, set the Letter I.

G g

Secondly,



Secondly, Through the point I, draw the Parallel of Latitude IE, and where that cuts the *Rumb-line* as at C is the place the Ship is in.

*To lay down a Place by its Latitude and Longitude.*

Draw a Meridian-line at the given Longitude of the Place, and a Parallel of Latitude at the Latitude given, and the point where this Meridian and Parallel cut one the other is the Prick representing the Place.

*By the Course and Latitude to lay down a Place, or make a Prick.*

Admit from C a place in Latitude  $46^{\circ} 14'$ , I Sail North West by North 'till I am in Latitude  $48^{\circ} 6'$ , and would prick the Place of the Ship.

At  $48^{\circ} 6'$  of the Meridian-line, I draw the Parallel of Latitude  $e g$ , and through C, I draw a Parallel to the North West by North *Rumb-line* as  $c i$ , and where that cuts the Parallel  $e g$ , as at  $i$  is the Ships Place.

What has been done thus by drawing lines, may be performed by the intersection of two small arches or lines, and a Ruler, without drawing long lines through the *Chart*: for a Ruler will supply lines without drawing them.

*To find the Latitude, Longitude, Course and Distance between any two Places already laid down in the Chart.*

*To find the Latitude.*

Take with the Compasses the nearest distance, between the given Place  $c$ , and some Parallel of Latitude as AD: then setting one foot of the Compasses on the end of that Parallel as at A, apply that extent to the graduated Meridian, the right way, (*viz.* that way that the Place lyeth from the Parallel) and the other foot will shew at I, the Latitude of the Place.

*To measure the Longitude or rather Difference of Longitude.*

Take with the Compasses the nearest distance, between the given Place  $c$ , and some Meridian as AB: then setting one foot on the end of that Meridian A, apply that extent to the graduated Parallel, and the other foot will shew the Difference of Longitude, that the place  $c$  is from that Meridian A B.

*To find the Course between any two Places in the Chart.*

Lay a Ruler over the two Places as  $c i$ , see what *Rumb-line* runs Parallel thereto as A I, and that shews the Course. But if the *Rumb-lines* be not drawn, take  $60^{\circ}$  from the Chords, and setting one foot in  $e$  where the Ruler cuts some Meridian, describe the obscure arch  $p q$ , which measured

measured on the line of *Rumbs* on the Scale, shews the Course 3 Points from the Meridian, *viz.* North West by North.

*To measure the Distance between two Places.*

If the two Places differ only in Latitude, the Difference of Latitude is the distance between them.

If the two Places are both in the same Latitude, take the distance between them, and apply the Compasses to the graduated Meridian, one foot standing as much above the Latitude as the other below, the degrees intercepted is the distance, or rather thus:

Take a degree of the Meridian-line at that Latitude, and turn it between the two Places by a strait-line, and so often as you shall find that length between the two Places, so many score Leagues is the distance between them.

If two Places differ both in Latitude and Longitude, take their Difference of Latitude in degrees from the line AD, and laying a Ruler upon the two Places, apply one point of the Compasses to the edge of the Ruler, that the other turned about may just touch some East and West-line crossed by the Ruler, then take the distance by the edge of the Ruler, from the Place where the Compasses rested, to the Place where the Ruler crosses the said East and West-line, that extent measured on the line AD, shews the degrees or scores of Leagues between the two Places.

*To keep a Mercator-account of the Ships Place daily by the observed Latitude, and the Course.*

Admit a Ship Sail from A, a Place in Latitude North  $44^{\circ} 00'$ , North by West till she's arrived in the Latitude  $44^{\circ} 30'$ , and from thence North West by North 'till in the Latitude  $45^{\circ} 18'$ , and afterwards North West by West 'till she fall in Latitude  $46^{\circ}$ : what is the Difference of Longitude, and also the Course and distance made good from the first Place of Departure?

First, Draw the Parallel of  $44^{\circ} 30'$  Latitude, and where it cuts the North by West, or first *Rumb-line* from the Meridian as at  $c$  is her place on that *Rumb*. Then draw the Parallel of  $45^{\circ} 18'$  of Latitude  $d e$ , and continue the North West by North or third *Rumb-line* 'till it cuts it in  $f$ : then through  $c$  draw a Parallel to the *Rumb-line* A  $f$  as  $e g$ , the point  $g$  where it cuts the Parallel of Latitude, is the place of the Ship at the end of her North West by North Course.

Thirdly, Draw the Parallel of  $46^{\circ}$  of Latitude, and continue the North West by West *Rumb-line* 'till it cut it in  $h$ , and through  $g$  draw a Parallel to A  $h$  as  $g i$ , so is  $i$  her place at last. Now taking  $i k$ , and applying it to AD you'll find she's  $2^{\circ} 20'$  Longitude West from A, and by laying a Ruler over A and  $i$ , you will find by comparing it with the *Rumb-lines*,

G 2 h



she has made a North West by North Course half a point and better Westerly.

*Arithmetically.*

*Arith.* It may be performed by the third Case, or Proposition of *Mercators* Sailing.

This way of keeping an account of a Voyage, is not contemptible, in parts where there's a certainty of a clear Heaven to observe in, so that care be taken still to rectify the Compaſs, keep her ſteer ſteady, Lee-way allowed for, and the Currents tryed once a day, all which trouble is pretty well recompenced in the omitting the continual keeping an account of the Diſtance.

But it's objected that becauſe there is no way of examining, or diſcovering whether any error be in the account or not, unleſs ſome ſmall glimpse from the Variation, and if diſcovered yet here's no way of correcting it, until ſome way be found for obſerving the Longitude (after which this will be the beſt and only way) it's not a ſafe method to rely on.

To which I anſwer, that if an account of the Ships way be kept, alſo the correction may be made by that, but then it will be better to keep the whole account by her courſe and diſtance, and correct by the obſerved Latitude like as in Plain Sailing, and as follows.

*To keep a true account of the Ships place daily, by her Courſe and Diſtance.*

Suppoſe a Ship Sail from A in North Latitude  $44^{\circ}00'$ , North North Weſt 60 Leagues or 180 Miles, then Weſt North Weſt 30 Leagues or 90 Miles, afterwards North by Weſt half a point Weſterly 20 Leagues or 60 Miles: what's the Latitude ſhe's in, the Difference of Longitude, Courſe and Diſtance ſhe has made good?

*Geometrically.*

*Geom.* Taking 60 Leagues from the line AD prick them on the North North Weſt line from A to *m*, and taking the neareſt diſtance to AD, and applying it to the line XZ you will ſee ſhe's in Latitude  $46^{\circ}48'$ : then drawing the Parallel of Latitude  $46^{\circ}48'$ , and producing the North North Weſt line, they will meet in *m* the firſt point.

Secondly, Through *m* draw a Parallel to the Weſt North Weſt line, as *mn*, and lay thereon 30 Leagues from *m* to *o*, and taking the neareſt diſtance from *o* to the Parallel of  $46^{\circ}48'$  Latitude *mq*, ſet it on the *Assistant-line* from *p* to *r* which ſhews you are now in Latitude  $47^{\circ}22'$ , and drawing the Parallel of  $42^{\circ}22'$  Latitude where it cuts *mo*, as at *n*, is her place on the *Chart*, at the end of the ſecond Courſe.

Thirdly,



*between page 248 and 249.*



Thirdly, Through  $n$  draw a parallel to the North by West  $\frac{1}{2}$  W easterly *Rumb-line*, and prick thereon 20 Leagues from  $n$  to  $r$ , and taking the nearest distance from  $r$  to  $u$  the Parallel of  $42^{\circ} 22'$  Latitude, apply it to the *Assistant-line* from  $r$  to  $u$ , which shews the Latitude now to be  $48^{\circ} 20'$ .

Lastly, Draw the Parallel of  $48^{\circ} 20'$ , and where it cuts  $us$  as at  $t$  is the Ships place at the end of this third Course. Thus must they be proceeded with if more. Now find the Longitude of the point  $t$  by the former directions, and also the Course and Distance made good from A.

By the Tables Page 59, and 108, of the Volumn of  
TABLES.

Arithmetically.

Courses	Points.	Dist. D <sup>par</sup> .				Alter. of Latitude.		Lat. the Ship is in.		Diff. of Longitude.	
		M	PM	P	M	P	O	'	"	'	"
0	0	0	00	0	00	00	44	00	0	0	0
North North West	2	100	38	26	92	38				1	26
		80	30	61	73	91				0	12
		180	68	87	166	26	46	46	1	39	19
West North West	6	90	83	14	34	44	47	20	1	57	18
									0	4	24
North by West $\frac{1}{2}$ Wly.									2	01	4
	$1\frac{1}{2}$	60	14	57	57	41	48	18	0	14	57
									0	7	28
									0	22	25

The Difference of Longitude. + 03 26

Having drawn several Columns, and entred therein the Courses and Distances, Departures and Alterations as directed before in a *Plain Chart Traverse*, and as you see in this specimen, by adding or subtracting the Northings or Southings according as the Latitude increaseth or diminisheth, find the several Latitudes putting them in another Column.

Then



Then enter the Table (beginning Page 108 of the *Voll.* of Tables) with the respective Latitude in the Left Column, and the Departure on the head, and the Degrees, Minutes, and Seconds thence taken put in the Column under Difference of Longitude.

Lastly, Collect all the East differences into one sum, and the West differences into another, then subtract these sums the one from the other, and the Remainder is the Difference of Longitude in Degrees, Minutes and Seconds.

Note that when you cannot find the whole Departure at once, you must take it out at twice or thrice, as you was directed to do with the distances in the *Plain Chart Traverse*.

Thus, looking  $46^{\circ}$  Latitude in the Left Column of the Table, and 60 (the Articular part of the Departure 68 miles 87 parts) on the head, in the Angle of meeting I find  $1^{\circ} 26' 22''$ , and under (8 m. 87 par. or instead thereof) 9 m. is  $0^{\circ} 12' 57''$ , the sum of these two makes  $1^{\circ} 39' 19''$  the Difference of Longitude made in the first Course. Then looking  $47^{\circ}$  of Latitude in the left Column, and 80 on the head of the Table, I take out  $1^{\circ} 57' 18''$ , and under three miles and against  $47^{\circ}$  Latitude I find  $0^{\circ} 4' 24''$ , their sum  $2^{\circ} 1' 43''$  is the Difference of Longitude in the second Course.

Afterwards looking  $48^{\circ}$  Latitude in the left Column and 10 m. on the head of the Table I find  $0^{\circ} 14' 57''$ , and under 5 (which I take instead of 4 m. 57 par.) against  $48^{\circ}$  Latitude I find  $0^{\circ} 7' 28''$ , the sum  $0^{\circ} 22' 25''$  is the Difference of Longitude in the third Course. And thus must I have proceeded if there had been more Courses.

Now seeing my Differences are all of one name, viz. all West, I add them all together, and the sum  $4^{\circ} 03' 26''$  is the whole Difference of Longitude made in this *Traverse*.

#### A second Example.

Admit a Ship Sail from Latitude  $53^{\circ}$  North, first South South West 12 Miles, then South West by South 17 Miles, South West 23 Miles, West South West 18 Miles, and West 15 Miles: afterwards South by East 8 Miles, South East by South 27 Miles, East by South 30 Miles, and East 19 Miles. The Difference of Longitude, Course and Distance is required.

Courses

Courses	Points.	Dist.		Depart.		Alter. of Latitude.	Lat. the Ship is in.	Diff. of Longitude.
		M	P	M	P			
		0	0	0	0	0	53	00
South South West	2	12	4	59	11	09		00
							52	49
South West by South	3	17	9	44	14	13		07
							51	35
South West	4	23	16	26	16	26		16
							0	10
West South West	6	18	16	63	6	8		26
							51	19
West	8	15	15	00	00	00		16
							52	12
South by East	1	8	1	56	07	85		27
							52	12
South East by South	3	27	15	15	22	45		04
							51	42
East by South	7	30	29	42	5	85		46
							51	36
East	8	19	19	00	00	00		16
							51	36
							51	36

Courses

6	0	02	30
7	0	24	36
8	0	46	47
9	0	30	18
1	44	11	East Long.

Courses

1	0	7	37
2	0	15	30
3	0	26	34
4	0	27	11
5	0	24	31
1	41	23	West Long.

Having



Having made several Columns and Tabulized the Courses and Distances as before, and by making Entries therewith in the first *Traverse Table*, beginning *Page 59* of the Tables, found the Alterations of Latitude and Departures, and by adding or subtracting found the Latitudes all as in the last *Example*, then enter the Table *Page 108* with the Departure and Latitude, and take out the Differences of Longitude as in the first *Example*.

But some think it enough once a week to transfer their account to the *True Chart*, keeping it daily by the *Plain Chart*, such may take their whole weekly Easting or Westing, and their middle Latitude, and by entering the Table *Page 108* readily take out their Longitude.

*Of Currents and how to allow for them in your account.*

If a Current set directly against a Ship in her Course, it lessens her Distance Sailed by so much as is the drift or race of the Current in the same time.

If a Current run direct with the Course a Ship Sails, it will augment her Distance, by so much as is the drift of the Current in the same time.

If a Current thwart the Ship's Course, it not only augments or diminisheth her distance but makes her err in her Course, so that without knowing where they are (which I shall at the end of this part shew how to find) and when found take care to prevent the errors that would proceed from them, by allowing for them in the Reckoning, you may in Sailing to some small lone *Island*, be at such a loss, that you may not know which way to Steer, as it has happened to several. To avoid this it is usual now not to make directly for such *Islands*: but to get into the Latitude thereof while they are certain whether they be to the East or West of it; and then keep in that Latitude Sailing directly East or West according as the Place lieth, diligently looking out for it till they get sight thereof.

But in long Voyages, where there can be no such groping for Land every few days without quite spoiling their Voyage, yet must cross many Currents and keep a continued account for many weeks together, there must be skill to allow for the Current upon any *Rumb* whatever, so that by Observation of your Latitude, you might have by computation your true Longitude.

Admit

Admit a Ship sail from Latitude  $40^{\circ} 00'$  North, 36 hours: first North East 48 miles, then North by East 57 Miles, in a Current that sets directly towards the North, one mile an hour; what Latitude is she arrived in, and what Distance and Difference of Longitude has she made?

Hours.	Courses.	Points.	Dist.	Depr.	Alter. of Latitude.	Lat. the Ships in.	Difference of Longitude.
	0		M	P	M	P	0
		0	0	0	0	0	0
20	North East The Current.	4	+8	33	04 33	04	0 39 46
				0	00 20	00	0 03 57
				33	04 53	04	0 43 43
16	North by East Current.	1	57	0	11 12 55	90	0 13 21
				0	00 16	00	0 01 20
				11	12 71	90	0 14 41
							0 58 24

Without regard to the Current, the Ship should be at the end of her first Course in Latitude  $40^{\circ} 33'$ , to which add 20 miles for the drift of the Current, and the sum is  $40^{\circ} 53'$ , the true Latitude, with which and the departure 33 m. 04 p. enter the Table page 108, and you will find the difference of Longitude thereto  $0^{\circ} 43' 43''$ .

Again at the end of the second Course she should be, without regard to the Current, in Latitude  $41^{\circ} 44'$ , but adding thereto the drift of the Current in 16 hours, viz. 16', the sum  $42^{\circ} 05'$  is the true Latitude she's in, with which and the departure 11 m. 12 p. enter the said Table again and you will find the difference of Longitude answering thereto  $0^{\circ} 14' 41''$ , which added to  $0^{\circ} 43' 43''$ , makes  $0^{\circ} 58' 24''$  the true difference of Longitude made in this 36 hours sail, the Current allowed; but without allowing for the Current she had been but in  $41^{\circ} 29'$  of Latitude, and had made but  $0^{\circ} 58' 00''$  difference of Longitude: and if the Current had been allowed yet the account kept by the *Plain Chart*, she would have been nevertheless in Latitude  $42^{\circ} 05'$ , but her difference of Longitude would have been but  $44'$ . If the Current had set directly South you must have subtracted the drift of the Current from the differences of Latitude, if it had set East the drift thereof must have been added to the Departure, because she makes East Departure, &c.

Admit between July the 27th at noon, and noon the 29th, a Ship sail from Latitude  $45^{\circ} 00'$  North, first 6 hours North 27 minutes or miles, secondly

H



secondly 7 hours North North East 35 miles or minutes, ten hours West North West 48 miles, afterwards 9 hours West by North 50 miles, then again ten hours North West 53 miles, and lastly six hours West 38 miles, crossing a Current that sets North East half a knot, a small gale, smooth water, and little or no Variation; what is the true Course and Distance, and difference of Longitude she has made, and the Latitude she is now in?

Hours.	Courses.	Points.	Dist.	Depar.	Alter. of Lat.	Lat. the Ship is in.	Diff. of Longitude.
	o		M P M P	P	o ' o ' "		
6	North Current.	o 27 4 3	o 00 00 00	o 00 00	45 00	o 00 00	o 00 00
					02 12 29 12	45 29	o 03 02
7	North North East Current.	2 35 4 3	o 13 39 32 34	o 02 48 02 48		o 14 24	o 08 28
					15 87 34 82	46 04	o 22 52
10	West North West Current.	6 48 4 5	o 44 35 18 37	o 03 54 03 54		o 58 06	o 01 11
					40 81 21 91	46 26	o 59 17
9	West by North Current.	7 59 4 4	o 49 04 09 75	o 03 19 03 19		o 58 16	o 08 33
					45 85 11 94	46 39	o 06 49
10	North West Current.	4 53 4 5	o 37 48 37 48	o 03 54 03 54		o 44 16	o 05 49
					33 94 41 02	47 20	o 50 05
6	West Current.	8 38 4 3	o 38 00 00 00	o 02 12 02 12		o 44 10	o 08 43
					35 88 02 12	47 20	o 52 53
					West Long. 3	49 03	
					East Long. 0	25 54	
					Diff. Long. West. 3	23 09	

With these two Latitudes  $45^{\circ} 00'$ ,  $47^{\circ} 22'$ , and the Difference of Longitude  $3^{\circ} 23' 09''$ , by the first Case of Mercator's sailing, find the Course and Distance.

Suppose

Suppose a Ship sail in 48 hours from Latitude  $45^{\circ} 00'$  North, first 6 hours North by East 27 miles or minutes, secondly 7 hours North East by North 35 miles, 10 hours North West by West 48 miles, afterwards 9 hours West North West 50 miles, then again 10 hours North West by North 53 miles, and lastly 6 hours West by North 38 miles, the Compass Varying 1 Point from the North Eastward, and crossing a Current that sets North East by East half a knot, a small gale and smooth water; what is the true Course and Distance and Difference of Longitude she has made, and the Latitude she is now in?

Courses.	Hours.	Courses correct by the Variation.	Points.	Dist.	Depar.	Alter. of Lat.	Lat. the Ship is in.	Diff. of Longitude.
				M P M P	P	o ' o ' "		
N by E	6	North	o 27 4 3	o 00 00 00	o 00 00	45 00	o 00 00	o 00 00
Cur. N E by E.		North East.	o 27 4 3	o 00 00 00	o 02 12	2 12		
					02 12 29 12	45 29	o 03 02	
NE by N	7	NNE	2 35 4 3	o 13 39 32 34	o 02 48		o 14 24	o 08 28
Cur. NE by E.		North East.	2 35 4 3	o 13 39 32 34	o 02 48		o 14 24	o 08 28
					15 87 34 82	46 04	o 22 52	
NW by W	10	W N W	6 48 4 5	o 44 35 18 37	o 03 54		o 58 06	o 01 11
Cur. NE by E.		North East.	6 48 4 5	o 44 35 18 37	o 03 54		o 58 06	o 01 11
					40 81 21 91	46 26	o 59 17	
W N W	9	West by North	7 59 4 4	o 49 04 09 75	o 03 19		o 58 16	o 08 33
Cur. NE by E.		North East.	7 59 4 4	o 49 04 09 75	o 03 19		o 58 16	o 08 33
					45 85 11 94	46 39	o 06 49	
NW by N	10	North West	4 53 4 5	o 37 48 37 48	o 03 54		o 44 16	o 05 49
Cur. NE by E.		North East.	4 53 4 5	o 37 48 37 48	o 03 54		o 44 16	o 05 49
					33 94 41 02	47 20	o 50 05	
W by N	6	West	8 38 4 3	o 38 00 00 00	o 02 12		o 44 10	o 08 43
Cur. NE by E.		North East.	8 38 4 3	o 38 00 00 00	o 02 12		o 44 10	o 08 43
					35 88 02 12	47 20	o 52 53	
					West Long. 3	49 03		
					East Long. 0	25 54		
					Diff. of Long. West. 3	23 09		

If she had made any Lee-way, it ought to be allowed on each single Course, just as the Variation is here.



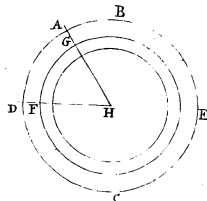
Some think it well enough to keep their daily account according to the *Plain Chart*, and to transfer it to the *True hart* once a week: such may take their whole weeks Easting or Westing and their middle Latitude, and by entring therewith the said Table page 108, readily take out their Longitude.

## SECTION VI.

*Of Observation and the use of Instruments.*

**C**elestial Observation is founded on these two principles.

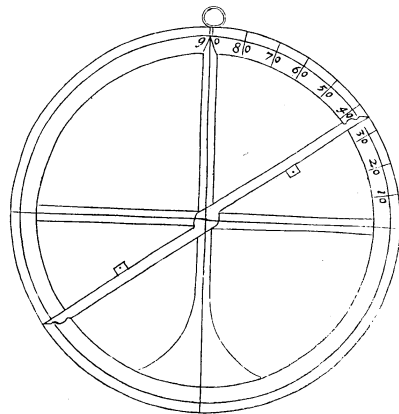
1. That when many Circles are Concentrick, the lines drawn from the Center to the circumference divide them all in the same manner, as in *Examples* If the Circles *DBE*, *FGR* be described from the same center *H*, and the lines *HFD*, *HGA* drawn, the Arches *DA*, *FG* shall be like Parts of the Circumferences, and contain a like number of Degrees.



2. That the Terraqueous Globe or Mass of Earth and Water we live on, compared with the Sphere of the Sun (or rather Earths orbit) is of no sensible quantity, but only as a prick or meer point in respect thereof, and consequently that any point on the Earths surface may very well be accepted for its Center, as also for that of the Heavens; therefore, is the Center of every Instrument substituted Center of the Heavens.

This being supposed, I say, that a Circle divided into 360 equal Parts or Degrees, is the first and most natural Instrument of all others, and is commonly called an *Astrolabe*; but is not always the most convenientest for the Navigators use, because of the instability of the Ship, yet it's in calm weather and between the *Tropic*, where the Sun comes near the *Zenith*, no contemptible Instrument, is made and poised as they ought to be, and as I have seen some.

The

*The Figure of the Astrolabe.**The Description and use of the Fore-staff or Cross-staff.*

The *Fore-staff* consists of a strait square graduated staff, and four Crosses or Vanes, (as the figure A,) the first and shortest is called the *Ten-cross* or *Vane*, and belongs to that side of the staff, where the Divisions begin at about three Degrees proceeding towards the eye (or flat) end to 10 Degrees, sometimes the *Thirty Cross* is so made, as that the breadth thereof serves instead of this *Ten Cross*.

The next longer is called the *Thirty Cross* or *Vane*, and belongs to that side of the staff where the Divisions begin at 10 Degrees, and end at 30 Degrees, and this is called the thirty side: half the length of the *Thirty Vane* will reach on this *Thirty side* from 30 Degrees to 23° 52', and the whole length from 30 Degrees to 19° 47'.

The



## The Figure of the Cross-Staff.



The

The next longer is called the *sixty Cross* or *Vane*, and belongs to that side where the divisions begin at 20 Degrees and end at 60°, and is called the *60 side*. The length of this *Cross* will reach on this *sixty side* from 60 Degrees to 30 Degrees.

The longest *Cross* is called the *ninety Cross*, and belongs to that side where the divisions begin at 30 and end at 90, and is called the *ninety side* of the Staff: sometimes the several sides of the Staff are numbred also with their Complements to 90 in small figures.

*The use of the Forestaff.*

The chief use is either to take the Altitude of the Sun or Stars, or the distance of two Stars, and the 10, 30, 60 and 90 Crosses are to be used according as the Altitude or Distance is greater or lesser, that is, if it be less than 10 Degrees use the *Ten Cross*, if above ten but less than thirty, the *thirty Cross* and if above 30 but less than sixty Degrees, use the *sixty Cross*, above which this is not so convenient for use as other Instruments.

*To Observe an Altitude.*

Place the flat end of the Staff to the out side of your eye as near the eye as you can, not to hinder your sight, and look at the upper end of the Cross for the Center of the Sun or Star, and at the lower end for the *Horizon*, if you see the sky instead of the *Horizon*, draw the Cross a little nearer to your eye, but if you see the Sea instead of the *Horizon*, put the Cross a little farther from your eye, and so continue moving and removing the Cross, till you see exactly the Sun or Stars Center by the top of the Cross, and the *Horizon* by the lower end thereof. The Degrees and minutes cut by the inner edge of the Cross, upon the side of the Staff peculiar to the Cross you use, is the present Altitude of the Sun or Star: but if it be the Meridian or greatest Altitude which you are to find, you must continue your Observation as long as you find the Altitude increase, still drawing the Cross nearer to your eye, but when you perceive the Altitude is diminished, which you will easily discover by seeing at the repeating of the Observation, the Sea instead of the *Horizon*, forbear any farther Observation, and do not alter your Cross, but as the Cross stands, count the Degree and Minute on the side proper to the Cross, which gives the *Meridian Altitude* required, and the *Meridian Altitude* subtracted from 90 gives the *Zenith Distance*, if it be not graduated on the Staff.

Fig. B.

To



To which *Zenith* distance add the minutes allowed for the height of your eye above the surface of the Sea, according to the little Table in the Margin, or subtract it from the Altitude, to have you the true *Zenith* distance and Altitude.

Height of the Eye.	Allow- ance.
Feet.	Min.
1	1
2	1 $\frac{1}{2}$
3	2
4	2
5	2 $\frac{1}{2}$
6	3
7	3
8	3
9	3 $\frac{1}{2}$
10	3 $\frac{1}{2}$
12	4
16	4 $\frac{1}{2}$
20	5
24	5 $\frac{1}{2}$
28	6
32	6 $\frac{1}{2}$
36	7
40	7
44	7 $\frac{1}{2}$
48	8

If it be hazy or somewhat thick weather the *Fore-staff* may be used as above, but if the Sun shine out they either observe the upper limb of the Sun, and afterwards subtract the Suns Semidiameter from the Altitude, or else use a coloured Glass on the top of the Cross to defend the sight from the splendour of the Sun,

To observe the distance of two Stars, or the Moons distance from a Star, place the Staffs flat end to the Eye as before directed, and looking to both ends of the Cross draw it nearer or remove it farther from the Eye as you shall find occasion, 'till you can see the two Stars the one on the one end, and the other on the other end of the Cross, then look what Degrees and Minutes are cut by the Cross on the side of the Staff proper to that Vane in use, and that is the true distance of the two Stars observed.

But that there may be no mistake in the placing the Staff to the Eye, which is the greatest difficulty in the use of this Instrument, first before observation put on the sixty Cross, and place it to 30 Degrees on its proper side, and also the ninety Cross sliding it to 30 Degrees likewise on his right side; then place the end of the Staff to the corner of your Eye as directed, moving it somewhat higher or lower about the Eye, 'till you see the upper ends of the two Crosses at once exactly in one line, and also their lower and that is the true place of your Staff in time of Observation.

Some use this *Cross-staff* backward in taking the Suns Meridian Altitude, thus.

To make a backward Observation of the Suns Altitude with the *Cross-staff*.

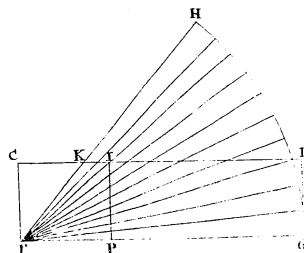
You must have an Horizontal Vane to fix upon the Center or eye end of your Staff, also a shoe of brass to fit on to the end of any of the Crosses, which is fitted of a sight Vane. Then, when you would observe, having put on the Horizon Vane, and fixt the shoe to the end of a convenient Cross, turn your back to the Sun, and looking through the sight in the shoe, lift up or down the end of the Staff, till the shadow made by the upper end of the Cross, fall upon the slit in the Horizon Vane, and at the same time you can see the Horizon through the Horizon Vane; then the Degree and Minute cut by the Cross on the proper side is the Altitude,

Altitude, but if their be fixt a lens or small double convex glass, to the upper end of the Vane to contract the sun beams, and cast a small bright spot on the *Horizon* Vane; possibly it may be found more convenient than the shadow, for as much as that is commonly imperfect and double.

### How to make the *Fore-staff*.

It may be graduated either Arithmetically by the Table of Natural Tangents, or Geometrically from the division of a quarter of a Circle.

### To Graduate it Geometrically.

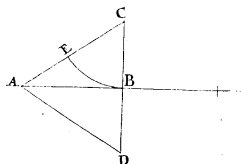


Upon a Table, or on a large Paper smooth pasted on some plane, draw the line FG of the length of the Staff to be graduated, and on F and G raise the Perpendiculars FC, GD, laying thereon the length you intend for the half length of the Cross, from F to C, and from G to D, and draw CD representing the Staff to be graduated. Then on the Center F describe your Arch GH being the half quarter or an eight part of the Circle, and divide it into 90 equal parts or degrees, thus; First divide it into three equal parts, and each of these again into three, these parts each into two, and each of the last parts into five. Thirdly from F draw straight lines through each of these points 10, 20, 30, &c. Which shall divide the line CD as the Staff ought to be graduated.



*In graduating the Staff by the Table of Tangents.*

Note that the graduations are only the Natural Co-tangents of half Arches, the half Crofs being *Radius*: Therefore divide the length of your half Crofs into 1000 or rather 100000 equal parts if it may be, according to the *Radius* of the Tables of Natural Tangents, then take from this the Co-tangents as you find them in the Table, and prick them from F orderly and your Staff will be exactly graduated for that Vane, so do for the rest severally. If it be required to prick the eightieth degree, the half of 80 is 40, and the Natural Co-tangent of 40° is 119175, which take from the Scale or half Crofs so divided, and prick it from F to P where it shall be the point for 80°, &c. So again to put on the 64th degree, the half of 64 is 32, and its Co-tangent 160033 which take from the divided Crofs (prolonged) prick it from F, and it will give you the 64 degree.



Now that the Crofs CD when transferred to B, shall make the Angle CAD eighty degrees, is demonstrable thus.

Seeing CB the half Crofs is *Radius*, and AB is by construction the Tangent of 50° the Angle ACB is 50°, and seeing the Triangle ABC is right angled, the Angle BAC will be 40 degrees, viz. the Complement of 50°: But DAC is the double of BAC, therefore the Angle DAC is 80, and the point B the true point on the Staff for 80 degrees. The same manner of Demonstration holds let the Crofs be what it will.

*To Graduate the Staff by any Diagonal Scale.*

Measure the half length of your Vane by the Scale, and say as the *Radius* of the Tables 1000000 is to the measure of the half Crofs, so is the Natural Co-tangent of the half of any degree desired to be pricked on the Staff, to the space between the Center of the Staff F, and the point for the Degree.

Admit:

Admit the half Vane measure on the Diagonal be 945, to find what Number must be taken off the Diagonal for the eightieth Degree. The Co-tangent of 40° (the half of 80) is 11917536, which multiplied by 945 makes 11261, &c. which taken from the Diagonal Scale will prick the degree desired.

*A Vane or Crofs being lost to find of what length it was.*

If it be the ninety Crofs, the distance of the 90° from the Center, or eye-end of the Staff is the half length of the Crofs.

If it be the thirty Crofs that's lost, say,

As the Co-tangent of 15°.

Is to the distance of 30, from the Center or eye-end of the Staff:

So is the *Radius*, to the half length of the Crofs.

If the tenth Crofs be wanting, say,

As the Co-tangent of 5 degrees (viz. the half of ten,)

Is to the space between 10 degr. and the eye-end of the Staff:

So is the *Radius*,

To the half length of the Crofs.

*The Description and use of the Demi-Crofs.*

This Instrument is sometimes used by the *Dutch*, but has been wholly neglected by the *English*, we preferring the whole Crofs or Forestaff.

This Staff is easily graduated it being only a line of whole Tangents, whose *Radius* is the length of the Crofs or Transum. A is the Horizon Vane, H the sight Vane, and E the shade Vane.

*To take the Suns Altitude with it.*

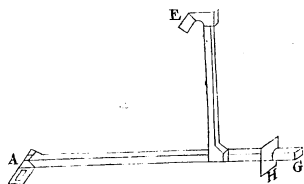
Having put the Vanes on their proper ends, hold up the Instrument with the Transum as upright as you can, and looking through the sight Vane H, see for the *Horizon* through the slit in the *Horizon* Vane, sliding the Crofs or Transum to and fro, till you see the shade of the Vane E fall at the same time upon the slit of the *Horizon* Vane A. Then are the Degrees cut on the Staff by the Transum the Altitude of the Sun required.

*To observe the height of a Star with it.*

Remove the *Horizon* Vane A, and put it on the end G, and transfer the sight Vane H to A, then holding up the Instrument with the Transum upright, and looking through the sight Vane, see for the *Horizon* through the *Horizon* Vane, and for the Star by the shade Vane, sliding the Transum to and fro till the *Horizon* and Star are both seen by their respective Vanes, then will the Transum cut the degrees of Altitude, allowing for your height above the level of the *Horizon* or Sea.



### The Figure of the Demi-Cross.



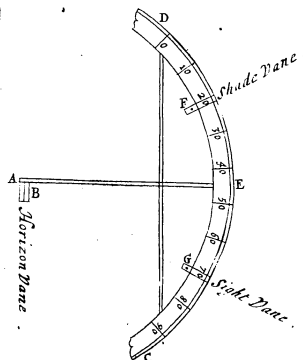
### The Description and use of the Bow.

This Instrument consists of only one large Arch of  $90^\circ$  well and truly graduated, three Vanes and a shank or staff, as you see in the Figure, where DEC is the Arch, AE the staff or shank, passing the Arch at  $45^\circ$  in most, but in some in  $50$  or  $55^\circ$ , F is the shade Vane, G the sight Vane, and AB the Horizon Vane placed on the very center of the Arch; the manner of making it is conspicuous enough from the description and figure. Its chief use is to take the Suns height, which is done thus, take the handle C in your hand, and holding the Bow as upright as you can, move the sight Vane up and down still looking through the sight, 'till you see the shade of the upper part of the shade Vane, on the slit of the Horizon Vane, and at the same time you see also the Horizon through the slit of the Horizon Vane, in doing which if you see the Sky and not the Horizon, then draw the sight Vane a little lower down towards C, but if you see the Sea instead of the Horizon then slide it upwards. If it be the Meridian Altitude that is to be observed: then you must wait, and make observation as often as you judg fit, 'till you see at repeating the observation the Sea instead of the Horizon before you desist; the difference between the degrees and minutes cut by the sight Vane, and these cut by the upper part of the shade Vane, is the distance of the Suns upper limb from the Horizon, from which if you subtract  $16'$  which is the Suns Semidiameter, the Remainder will be the distance of the Suns Center from the Horizon, from which if you subtract the Refraction as you find it, page 257 of the Tables, the residue will be the true correct height of the Sun. But note that if instead of  $16'$  the Suns Semidiameter you subtract but 8 or 10 it will be sufficient, the rest being allowed for your height above the level of the Horizon.

The

### The Figure of the Bow.

The Figure of the Bow.



To observe the height of a Star, place the sight Vane at A, and the Horizon Vane on the Arch at G, then looking through the sight Vane at A, move the Vane F higher or lower, 'till you can see the star by the Horizon through the Horizon Vane at G, so shall the Degrees and Minutes between the two Vanes F and G be the Altitude of the Star. So to take the Distance of two Stars, having placed the sight Vane at A, and the Horizon Vane at G, look through the Vane at A; moving the Vane F to and fro on the Arch 'till you see the one star through the Vane G, and the other by the Vane F, then do the Degrees and Minutes between the two Vanes F and G shew the distance of the Stars.

### The Description and use of the Plough.

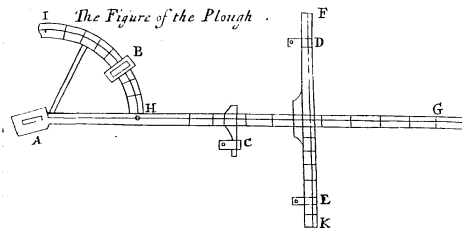
This Instrument is Antient though now not much used. It consists of a staff A L G, small Arch H I, Cross F K, and three Vanes, A an Horizon Vane, B a shade Vane, and C a sight Vane, to move upon the Staff. This will supply many Instruments, even all that has been before mentioned, but here I shall shew only its proper use as a different or distinct Instrument from the other.

To observe the Suns Altitude with it.  
Fit on the Horizon Vane, and place the shade Vane to any degree or pleasure, so it exceed not the Altitude to be observed, nor be above ten degrees.



degrees less (which may indifferent well be judged of by the eye;) for in both these cases the divisions on the staff are deficient: then put the sight Vane on the staff holding up the Instrument, and turning the back of the Arch to the Sun, move the sight Vane on the staff backward and forward 'till the shade of the upper edge of the shade Vane, fall on the upper part of the slit of the Horizon Vane, and that at the same time looking through the sight Vane you may see the Horizon through the Horizon Vane, as above directed in the use of the Bow, then will the sum of the degrees on the Arch and on the staff be the Suns Altitude, allowing for the height above the Horizon, and for Refraction as before directed. If in observing you see the Sea instead of the Horizon, then remove the sight Vane towards the Arch: but if on the contrary you see the Sky, and not the Horizon, then draw the sight Vane backwards from the Arch. If you observe for a Meridian Altitude, then repeat this work as often as is thought fit 'till you find the Sun begin to fall.

*The Figure of the Plough.*



The Cross serves by taking the Horizon Vane off, and setting the end of the staff A to your eye, to find the Altitude with, after the manner of a Cross-staff.

*The Description and use of the Quadrant.*

It's only a Quarter of a Circle accurately divided, having a moveable Index whereon are two sights, as also two other sights fixt to one edge of the Quadrant. See the Figure.

A is the Center, B and AC the two sides, BC the limb, DE two sights fixed upon the moveable Index or Label: FG two other sights for observing the Horizon, I the Handle.

*The*

*The Figure.*





When you would Observe the Suns Altitude by it, take hold of the handle and holding the Quadrant as upright as you can, turn the limb to the Sun and look through the sights F G, moving the Instrument too and fro 'till you can see the Horizon through them, then move the *Index* higher or lower 'till the bright spot coming through the first D, fall upon the second sight E, then shall the Arch H B be the Suns height required, allowing for your height above the level of the Horizon and for Refraction. If you be to observe the Altitude of the Moon or any Star, then after you have placed the side B A parallel to the Horizon, you must move the *Index* 'till the object (be it either Moon or Star) be seen through the holes or slits of the sights D E placed on the *Index*, and then shall the Arch H B be the Altitude.

If you be to observe the distance of two Stars, hold up the Quadrant so that looking through the sights F G you may see one of the Stars, then move the *Index* 'till you can see the other Star through the sights thereon, then will the Arch H B be the distance required.

#### Of the common Sea Quadrant or Back-staff.

This Instrument if well made is no whit inferiour to any before described, or scarcely to any that can be thought of for a backward Observation, it was the contrivance of one Captain Davis an English-man, and therefore is often called by us *Davis's Quadrant*, but by the French the *English Quadrant*. It consists of three Vanes A, B, C, and two Arches. That at A is called the *Horizon Vane*, that at B the *shade Vane*, because of its giving the shadow upon the *Horizon Vane* in time of Observation, and that at C the *sight Vane*, because in time of Observation it's placed at the eye. The lesser Arch d e is the sixty Arch, and that marked f g the thirty Arch, both Arches together making 90 degrees, (yet of different Radii's) whence its properly called a Quadrant. The sixty Arch is divided into sixty degrees, commonly by every five, but sometimes by single degrees. In time of Observation the *shadow Vane* is placed upon this Arch always to an even degree.

The thirty Arch is divided into thirty degrees, and each of those degrees into minutes by Diagonal lines, and concentrick Arches, as follows.

#### To divide the limb of the Quadrant.

Upon the plain of this Arch describe five, six, ten, or twelve Concentrick Circles, as you please, or as your Instrument will best bear, and between the terms of each degree draw, one, two, three, or more diagonal lines as you shall see convenient, noting this for a general Rule, that if you divide 60 the number of minutes in a degree, by the product of the number of concentrick Circles, multiplied by the number of Diagonals in the extent

of a Degree, the quotient will shew how many minutes each intersection of the Diagonals, and concentrick Arches increases by; as suppose the concentrick Arches on the Limb were 10, and the Diagonals in each Degree 3, then 10 multiplied by 3 makes 30, by which if you divide 60 the quotient is 2, which shews that the intersections encrease by two minutes, as you see them marked with small numbers.

#### To Observe the Suns Altitude with this Quadrant.

Having put the *Horizon Vane* upon the upper end or center of the Quadrant at A, the *shade Vane* upon the sixty Arch d e, to a number of Degrees less than you judge the Co-altitudes will be by ten or fifteen Degrees, and the *sight Vane* upon the thirty Arch f g, turning your back towards the Sun lift up the Quadrant, and look through the small hole in the *sight Vane*, and so raise or lower the Quadrant, 'till the shadow of the upper edge of the *shade Vane* fall upon the upper edge of the slit in the *Horizon Vane*, if then at the same time the *Horizon* appear through the said slit the Observation is finished; but if the Sea appear instead of the *Horizon*, then remove the *sight Vane* lower towards f; but if the sky appear instead of the *Horizon*, then slide the *sight Vane* a little higher, and so continue removing your *sight Vane* 'till the *Horizon* appear through the slit of the *Horizon Vane*, and the shadow of the *shade Vane* fall at the same time on the said slit of the *Horizon Vane*. Then look how many Degrees and Minutes are cut by the edge of the *sight Vane* that answers to the *sight-hole*, and to them add the Degrees that are cut by the upper edge of the *shade Vane*, the sum is the Zenith Distance or Complement of the Altitude. But to find the Suns Meridian or greatest Altitude, you must continue your Observation as long as you see the Altitude increase, which you will perceive by having the Sea appear at the repeating the Observation instead of the *Horizon*, removing the *sight Vane* lower, but when you see the sky appear instead of the *Horizon*, the Altitude is diminished, therefore desist from farther Observation at that time, and

K k

add



add the Degrees upon the sixty Arch, to the Degrees and Minutes upon the thirty Arch, the sum is the *Zenith* distance or Co-altitude of the Suns upper limb or edge.

And because it is the *Zenith* distance or Co-altitude of the upper limb of the Sun, that is given by the Quadrant, when Observing by the upper edge of the *shade-Vane* (as it's customary to do) and not the Center, you ought to add 16, the Suns Semidiameter, to that which is produced by your Observation, and the sum is the true *Zenith* distance of the Suns Center. But if you Observe by the lower part of the shadow of the *shade-Vane*, then it's the lower limb of the Sun that gives the shadow, and therefore you must subtract 16', from what your Instrument gives: but considering the height of the Observer above the water, which is commonly between 16 and 20 feet, you may take away 3 or 6' from the 16', and make the allowance but 10 or 12' to be added instead of 16'.

Note also that the Refraction of the Sun or Stars causeth them to appear higher than they are: there ore when you have made your Observation look in Page 257 of the *Vol. of Tables*, for the Refraction answering thereto and subtract it from your Altitude, or add it to the *Zenith* distance, so shall you have the Altitude, or *Zenith* distance, exact and correct.

Of late there has been used a lens or double convex-glass, fixt in the *shade-Vane*, which contracts the rays, and casts them in a small bright spot on the slit of the *Horizon-Vane* instead of the shade, which has much improved the Instrument, if the glass be well and truly fixt: for now it may be used in hazie weather, and that so thick an haze that an Observation can hardly be made with the *Fore-staff*, also in clear weather the spot is more defined and conspicuous than the shadow, which at best is not terminated. This was the contrivance of Ingenious Mr. Flamsted.

*Rules for finding the Latitude or height of the Pole, by the Zenith Distance, or Meridian Altitude, of the Sun or Stars and their Declinations.*

Note that if the Sun or Star have no Declination, the *Zenith* distance is the Latitude, and if the Sun or Star come to the Meridian due North the Latitude is Southerly, if it come to the Meridian South, the Latitude is Northerly.

If the Sun or Star be in the *Zenith*, the Declination is the Latitude, and if the Declination be Southerly the Latitude is Southerly, but if the Declination be Northerly, the Latitude is Northerly.



## Rule 1.

If the Declination be North or South either of the Sun or Stars, and the Meridian Altitude be the same way that the Declination is, the Difference between the Declination and Zenith distance is the *height of the Pole* towards which the Declination is.

## Example 1.

The Declination North	23°	50'	Æ K	Fig. A.
The Zenith distance North	8	30	Z K	
the Latitude North,	15	00	Æ Z	

Except the Declination be less than the Zenith distance, then the contrary Pole to the Declination is elevated.

## Example 1.

The correct Zenith distance South	71°	30'	Z K	Fig. B.
The Declination South	20	00	Æ K	
the Latitude North,	51	30	Æ Z	

## Example 2.

The Zenith distance North	30°	00'	Z K	Fig. C.
The Declination North	20	00	Æ K	
the Latitude South,	10	00	Z Æ	

## Rule 2.

If the Declination of the Sun or Stars be North or South, and the Zenith distance be contrary to the Declination, the sum of the Co-altitude and Declination is the height of that Pole, that the Declination is towards.

## Example 1.

The Zenith distance South	31°	30'	Z K	Fig. D.
The Declination North	20	00	Æ K	
Latitude North,	51	30	Z Æ	



## Example.

But if the Sun or Star may have two Meridian Altitudes, which you shall know by the following instructions, then the sum of the Co-declination and Altitude is the height of the Pole towards which the Declination is.

If the Declination be the same way that the Meridian Altitude is, and the Declination greater than the Meridian Altitude, then the Sun or Star may have two Meridian Altitudes in 24 hours, viz. the one above the Pole and the other below.

## Example.

Fig. E.

Declination North $23^{\circ} 30'$ Complement	_____	$66^{\circ} 30'$ P K.
The correct Meridian Altitude North	_____	$8^{\circ} 30'$ K O.
The Elevation of the North Pole, $75^{\circ} 00'$ P O.		

Except the Meridian Altitude be more than the Declination, then you must subtract the Zenith Distance from the Co-declination, and the remainder is the height of that Pole towards which the Declination is.

## Example.

Fig. F.

The Declination North	_____	$80^{\circ} 00'$ Æ K.
The Zenith distance North	_____	$5^{\circ} 00'$ Z K.
Latitude North, $75^{\circ} 00'$ Z Æ.		

Lastly Note, that which way soever the Meridian Altitude be, if the Meridian Altitude and twice the Co-declination be less than  $180^{\circ}$  degrees, the Sun or Star hath two Meridian Altitudes in 24 hours, and by the second Rule you may have the Latitude.

## Example.

Fig. G.

The Meridian Altitude South	_____	$77^{\circ} 00'$ H K.
The Declination $62^{\circ} 00'$ North, the Comp.	_____	$28^{\circ} 00'$ K P.
	_____	$28^{\circ} 00'$ P $\pi$ .
The sum, $133^{\circ} 00'$ less than		
$180^{\circ}$ therefore by the second Rule.		
The Zenith distance South	_____	$13^{\circ} 00'$ K Z.
The Declination North	_____	$62^{\circ} 00'$ Æ K.
The Latitude is North, $75^{\circ} 00'$ Z Æ.		

To

## To find the time of a Stars coming to the Meridian any day.

Having looked the Right-ascension of both the Star and Sun in their proper Tables, Subtract the Right-ascension of the Sun from the Right-ascension of the Star: but if the Stars Right-ascension be less than the Suns, so that you cannot subtract, add thereto 24. hours and then subtract, and the Remainder if under 12 hours is the time of the Stars coming to the Meridian afternoon, but if the Remainder be more than 12 hours subtract 12 therefrom, and the residue is the time after midnight.

## Example 1.

September 15<sup>th</sup> its required to know when Fomalhaut comes to the Meridian.

I find in the Table Page 260 of the Vol. of Tables, the Stars Right-ascension to be  $22^h 41'$ , and in the Table Page 258<sup>th</sup> the Suns Right-ascension to be  $12^h 10'$  which subtracted from the Stars Right-ascension, leaves  $10^h 31'$  the time of the Stars coming to the Meridian afternoon.

## Example 2.

Suppose the time that Aldebaran comes to the Meridian, the 28<sup>th</sup> of Feb. 1683 be Required.

The Right-ascension of the Star	_____	$22^h 40'$
Twenty four hours added	_____	$24^h 00'$
	_____	$46^h 40'$
The Suns Right-ascension to be subtracted	_____	$23^h 25'$
The time of the Stars coming to the Meridian that night		$23^h 15'$

## The Description and use of the Nocturnal.

There are many kinds of Nocturnals, some for one Star some for another, of which we shall take notice only of two, the one made for the Constellation of the great Bear, and the other for the little Bear. And they both consisting of like parts, one description shall serve both.

This Instrument then is composed of three pieces or parts, the first and biggest on which is the handle by which to hold it in time of Observation, hath on the fore side two Circles, in the outermost of which are the days of the Months, and upon the innermost the 24 hours of a day Natural: upon the backside are the 32 Points of the Compaſs, and sometimes especially if it be for the little Bear, the distance of the Pole Star above or beneath the Pole.

E.



If the Nocturnal be for the Pointers (or as some call them the Guards) of the *great Bear*; then you will see in the Circle of Months *February* 17 at the top, because the Star that night comes to the Meridian at midnight; but if it be for the Fore-guard of the *little Bear* you will see *April* 25 at the top right under the middle of the tip, for the like reason.

The second or middle Piece or Part contains two Circles, and a small Tooth or Index, the outermost Circle is divided into 29 $\frac{1}{2}$  days for the Moons age, the innermost into 24 hours. The Index is a little short peg standing out from the edge, and is to be set to the day of the Month as occasion requires.

The third and upper or innermost Part or Piece is a long Index, the edge of which that comes from the center must be brought over the Guards in Observing. Sometimes one Instrument is made to serve both *Bears*.

*To find the hour of the Night, and upon what point of the Compass the Guards are.*

First, Set the Tooth of the middle Part to the day of the Month, then lift up the Instrument and hold it as upright as you can with the fore side towards you; and afterwards bow the upper end or tip on the top of the Nocturnal, so much towards you, that looking through the hole in the middle of the Nocturnal you may see the Pole Star: Now when you see the Pole Star through the hole, turn the long Index or Ruler about 'till by the edge coming from the Center, you can see the *first of the Guards of the little Bear*, or to the *Pointers of the great Bear*, if for the *great Bear*, then shall the edge of that Index or Ruler shew upon the innermost Circle of the middle Part or Piece the hour of the Night; and at the same time on the backside of the Nocturnal the Point of the Compass on which the Guards are.

If you desire to be more exact in the time of the Night take the Altitude of some known Star, and proceed according to the Directions in Page 155 of the *Cosmography*.

*To find the time of the Moons coming to the Meridian by the Nocturnal.*

Look for the Moons age in the outermost Circle upon the middle Piece of the Nocturnal, and right against it on the innermost Circle of the same Piece stands the time of her coming to the Meridian.

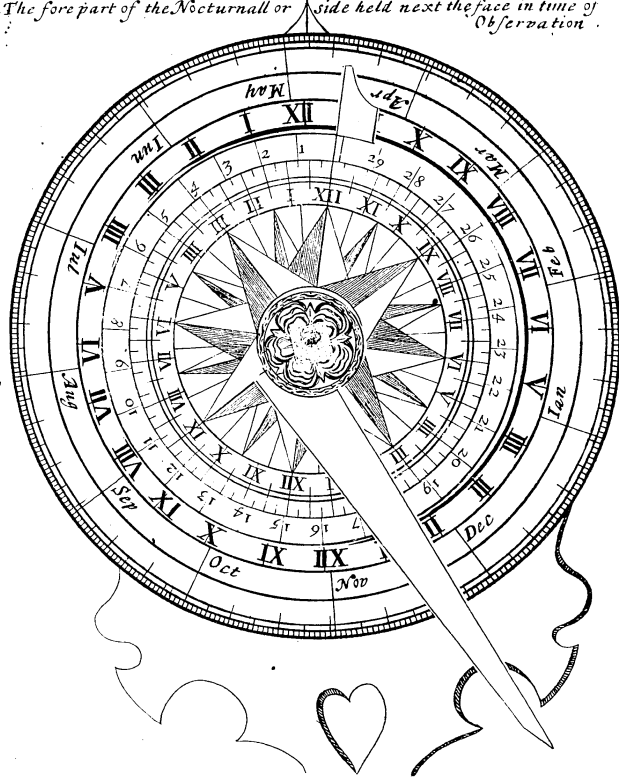
*To find the Time of her coming to the Meridian otherwise.*

Multiply her age by 4 and divide the Product by 5, and the Quotient gives hours, and every unit that remains is 12 minutes more.

Admit the time of the Moons coming to the Meridian, be required for May 18, 1681.

Her

*The fore part of the Nocturnal or side held next the face in time of Observation.*



*between Page 254 and 255.*



If the Nocturnal be for the Pointers (or as some call them the Guards) of the *great Bear*; then you will see in the Circle of Months *February* 17 at the top, because the Star that night comes to the Meridian at midnight; but if it be for the Fore-guard of the *little Bear* you will see *April* 25 at the top right under the middle of the tip, for the like reason.

The second or middle Piece or Part contains two Circles, and a small Tooth or Index, the outermost Circle is divided into  $2\frac{1}{2}$  days for the Moons age, the innermost into 24 hours. The Index is a little short peg standing out from the edge, and is to be set to the day of the Month as occasion requires.

The third and upper or innermost Part or Piece is a long Index, the edge of which that comes from the center must be brought over the Guards in Observing. Sometimes one Instrument is made to serve both *Bears*.

*To find the hour of the Night, and upon what point of the Compass the Guards are.*

First, Set the Tooth of the middle Part to the day of the Month, then lift up the Instrument and hold it as upright as you can with the fore side towards you; and afterwards bow the upper end or tip on the top of the Nocturnal, so much towards you, that looking through the hole in the middle of the Nocturnal you may see the Pole Star: Now when you see the Pole Star through the hole, turn the long Index or Ruler about 'till by the edge coming from the Center, you can see the *first of the Guards of the little Bear*, or to the *Pointers of the great Bear*, if for the *great Bear*, then shall the edge of that Index or Ruler shew upon the innermost Circle of the middle Part or Piece the hour of the Night; and at the same time on the backside of the Nocturnal the Point of the Compass on which the Guards are.

If you desire to be more exact in the time of the Night take the Altitude of some known Star, and proceed according to the Directions in Page 155 of the *Cosmography*.

*To find the time of the Moons coming to the Meridian by the Nocturnal.*

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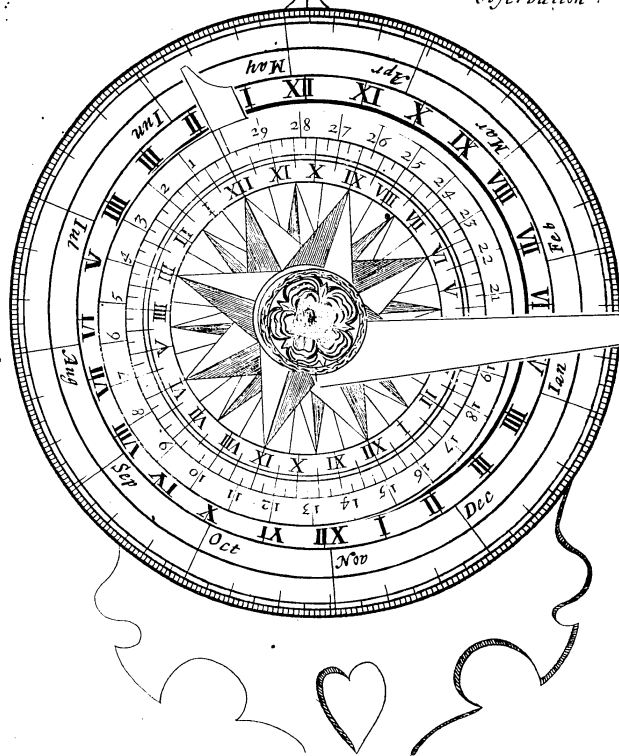
*To find the Time of her coming to the Meridian otherwise.*

Multiply her age by 4. and divide the Product by 5, and the Quotient gives hours, and every unit that remains is 12 minutes more.

Admit the time of the Moons coming to the Meridian, be required for May 18, 1651.

Her

*The fore part of the Nocturnal or side held next the face in time of Observation.*



*between Page 254 and 255.*



Her age is found according to the Directions in the *Cosmography* to be 11 days, which multiplied by 4 makes 44, and this divided by 5 gives 8 hours, and for the 4 remaining you must add 48', to the time of her South- ing is 48 minutes after eight of the Clock.

The reason why you are directed to multiply by 4, and divide by 5 is because allowing the Moon 30 days between New and New, she departs 12 degrees which is  $\frac{1}{5}$  of an hour each day from the Sun.

*To find the time of High water in any Place.*

Add to the time of the Moons coming to the Meridian on the given day, the time of high water in that place on the day of the change or full, and the sum is the time of high water on the day proposed.

The time of high water on the change day is found by Observation at every particular place.

*May 18, 1681.* Let it be required to find the time of high water at *London*, where it flows constantly 'till three of the Clock on the days of the New and Full Moon.

The time of the Moons Southing this day was found to be  $8^h 48'$ , to which if you add  $3^h$ , the sum  $11^h 48'$ , is the time of high water there that day. But this is sometimes very much wide of the truth.

*To find the time of High water more truly by the following Table.*

The Ds. Age	Tides	
	Days.	H. M.
1	16	0 43
2	17	1 20
3	18	1 52
4	19	2 22
5	20	2 52
6	21	3 26
7	22	4 07
8	23	4 55
9	24	5 50
10	25	6 53
11	26	7 59
12	27	9 04
13	28	10 03
14	29	11 05
15	30	12 00

Look the Moons age in the first Column, and the Number right against it in the second, being added to the hour of High water on the change day, makes the exact time of High water at the Place and time proposed.

Thus, right against 11 days I find  $7^h 59'$ , to which adding  $3^h$  the sum is  $10^h 59'$ , the true time of High water at *London*, differing almost an hour from the time given the other way. But this is out of place, and therefore I shall forbear any farther discourse hereof.



A Table of the Distance of the Pole Star, above or beneath the Pole, upon every Point of the Compass, the Guards and Pointers are upon.

Points on the Nocturnal.	For the fore- most Guard of the little Bear.		For the Pointers of the Great Bear.	
	°	'	°	'
North	2	09	2	20
N by E	1	52	2	30
NNE	1	29	2	35
NE by N	1	02	2	33
NE	0	35	2	26
NE by E	0	06	2	13
E NE	0	22	1	55
E by N	0	52	1	33
East	1	18	1	07
E by S	1	41	0	38
ESE	2	01	0	08
SE by E	2	16	0	22
SE	2	25	0	52
SE by S	2	30	1	20
SSE	2	29	1	44
S by E	2	22	2	04
South	2	11	2	20
S by W	1	55	2	30
SSW	1	34	2	29
SW by S	1	10	2	23
SW	0	43	2	26
SW by W	0	14	2	13
WSW	0	15	1	55
W by S	0	44	1	33
West	1	11	1	07
W by N	1	36	0	38
WNW	1	58	0	03
NW by W	2	14	0	22
NW	2	25	0	52
NW by N	2	30	1	20
NNW	2	29	1	44
N by W	2	22	2	04

The

The use of this Table of the North Stars distance above or beneath the Pole.

Having taken the Altitude of the Pole Star; Observe with the Nocturnal as before directed, upon what point of the Compass the Guards or Pointers are: then look in this Table for the distance or declination, and if the Star be below the Pole add it to the Altitude; but if the Star be above the Pole subtract, and the sum or remainder is the Latitude of the Place.

There ought to have been in the composing of this Table, some consideration to the Latitude: but the error that can at any time arise upon the omission of that consideration is only 4' at the most, when as you cannot have by your Nocturnal the Point the Guards are upon nearer than  $\frac{1}{2}$  or  $\frac{1}{4}$  a Point, which makes a much more considerable error, and therefore this is not to be taken notice of.

### Of the Compass.

This Divine Instrument the Compass, whose rare properties are truly admirable, and worthy of all mens contemplation and endeavours to explicate, especially Philosophical men, consists only of a Card and two Boxes. The Card is such as you have seen Page 173, with a small Cupulo or brass Center, with two wyers glewed to the under part, the ends directly under the North and South points of the Card. These wyers ought to be of Steel well tempered bended together in the form A, so that the ends joyn close and even, and to be touched with a good Loadstone, which is that which gives it life, and a property of standing with its North and South Points inspecting the North and South Points of the Horizon,

or points in the Heavens where the Meridian and Horizon intersect, and consequently all the other points, to inspect points or Azimuths in the Heavens at like distance from the Meridian; yet not so constant but that most times it has a Deflection or Variation, that is, the Meridian or North and South Line of the Card points some degrees from the intersections of the Horizon and Meridian or true Meridian line, which though taken by some for an imperfection, I rather take to be its greater perfection,

L I

Providence



Providence therein pointing at some things more excellent than yet apprehended, that are greater Mysteries in the frame and compofure of the World; and it's now a greater good to mankind than if it had only been directed conftant without any Variation, as every man that has been at the *East Indies* can make evident.

This Card or Fly thus ordered is put into a fmall round Box fit for it, having a pin in the middle on which the hollow of the Cupulo is to be placed, and the Card poifed that it may lie Horizontal in the faid Box, and fwing freely according as the Verrue of the touch fhall lead it.

This Box is to be hanged in two Circles or hoops of Brafs, or Tin, and thofe with the Box put in another Box, that this inermoft Box, and confequently the Card, may ftand Horizontal, which way foever the Ship heelds.

As to the touching of the wyers, let the ftone be good, the bigger the better, fo of the fame goodnefs in equal quantity and of the fame fhape, and let the wyers be fmooth and polifhed, then begin your touch near the middle of the wyer, and preffing it pretty hard on the Pole of the Stone, draw it flowly along to the very end of the needle, and lifting your hand a good diftance from the Stone while you put the wyer forward again, begin a fecond touch in the fame manner, and after that a third, which is enough, unlefs you will touch the other end of your wyers alfo, and then you muft touch that with the other Pole of the Stone in the fame manner you did the former, always remembering not to rub the wyer too and fro on the Stone, whereby the backward rubs take away what vertue the forward ones gave, but lift it out of the Sphere of the Stones Virtue, when you carry it forward again to begin a new touch.

*The Description and Ufe of the Azimuth Compaſs, or Compaſs to obferve the Magnetical Azimuth, that is the Suns Azimuth from the North or South points of the Compaſs.*

This is fomewhat differing from the common *Sailing Compaſs*, for upon the round Box (wherein are the Fly and wyer) is faftened abroad Circle of braſs, one femicircle thereof is divided into 90 equal parts or Degrees, numbred from the middle of the faid Diviſions both ways, with 10, 20, &c. to 45 Degrees: which Degrees are alfo fubdivided into minutes by Diagonal lines, and Circles after the fame manner that the Limb of the *Dutch Quadrant* was: but thefe graduating lines are drawn from the oppoſite part of the Circle, *viz.* from that point whereon the Index turneth in time of Obſervation.

On this Index is erected a fight which moves with a hinge, that it may be reifed or laid down as occaſion requires, and from the upper part of this fight, down to the middle of the Index, is faftned a fine thred or Lute-firing, to give a ſhadow upon a line that is on the middle of the faid Index.

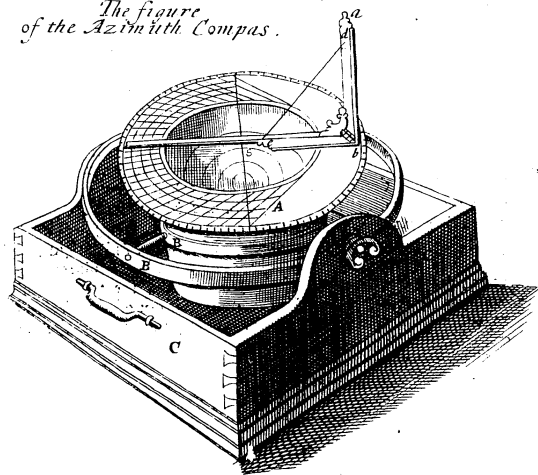
The

The reaſon of making the Index to move on a pin that's faftened to the circumference, is that the degrees and diviſions might be the larger: for now they are as large again as they would have been if divided from the Center, and the Index made to move thereon *vide 20 e 3.*

This broad braſs Circle is croſſed at right Angles with two threads, and from the ends of thoſe threads are drawn 4 ſmall black lines on the inſide of the Box, alſo there are 4 right lines drawn at right Angles one to the other on the Fly.

This Box thus fitted with its Fly, graduated Circle, and Index, &c. is to be hung, in Rings or Hoops of Braſs or Copper, and thoſe to be faftned into another Box, which is commonly ſquare. See the Figure.

*The Figure  
of the Azimuth Compaſs.*



A is the great Broad graduated braſs Circle.

ba the Index, moveable on the point b.

ba is the ſight erected.

de the Hypothenuſal Lute-firing, or thread.

BB the Braſs or Copper Hoops, or Rings which the round Box hangs in.

CC the ſquare Box that contains all the reſt.

L 1 2

T



## To Observe the Magnetical Amplitude or Azimuth.

If the Observation be for an Amplitude at Sun Rising or an Azimuth before noon, you must put the Center of the Index upon the West point of the Card or Fly within the Box, so that the four lines on the edge of the Card, and the four lines on the inside of the Box may agree or come together. But if the Observation be for the Suns Amplitude setting, or an Azimuth afternoon, then you must turn the Center of the Index right over the East point of the Fly, and make the lines within the Box to concur with those on the Fly. Having thus fitted the Instrument for the Observation, turn the Index towards the Sun, 'till the shadow of the thread *d e* do fall directly on the slit of the sight, and upon the line that is along the middle of the Index; then will the inner edge of the Index cut the degree and minute of the Suns Magnetical Azimuth from the North or South.

But note, that if the Compass being thus placed, the Azimuth be less than 45 degrees from the South, and you turn the Index towards the Sun, it will then pass off the divisions of the Limb, and so they become useless as it now stands. Therefore you must turn the Instrument just a Quarter of the Compass, that is, place the Center of the Index on the North or South point of the Card according as the Sun is from you, and then the edge thereof will cut the degree of the Magnetical Azimuth or Suns Azimuth from the North as before.

Having by this Instrument found the Magnetical Azimuth or Amplitude, find the Suns true Azimuth by calculation according as directed in Problem 12. of the 3<sup>d</sup> Section of the Cosmography, and the true Amplitude by Problem the 6<sup>th</sup> of the 3<sup>d</sup> Section, or take it out of the Table of Amplitudes Page 38, 39, of the Vol. of Tables; then to find the Variation, and which way it is, do as followeth.

With the Chord of 60 describe a Circle, and Quarter it with two Diameters at Right angles the one to the other, writing against the extremities of the Diameters, North, South, East, West, as you see in the figure, then take the true Amplitude or Azimuth, and prick it from the right point the right way, and so also prick off the Magnetical Amplitude or Azimuth.

Lastly, Take the distance between the Magnetical Amplitude or Azimuth and the North, and set it from the true Amplitude or Azimuth Northward, and the foot of the Compasses will fall in a certain point, from which if you draw a line through the Center, that line will represent the North and South line of the Compass or Magnetical Meridian, and that way that this point lieth from the North that way is the Variation, and as much as is the Arch between the said point and the North, which may be measured by the Chords.

Example.

## Example 1.

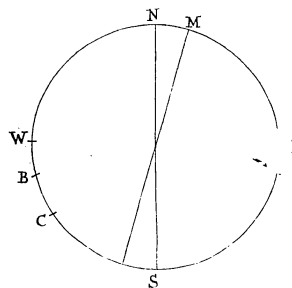
Admit one being in the Latitude  $48^{\circ} 00'$  North, the Sun having  $18^{\circ} 00'$  North Declination, observes the Magnetical Amplitude at Sun rising to be  $36^{\circ} 00'$  from the East Northward: and would know the Variation of the Compass.

First, With this  $18^{\circ}$  Declination, and  $48^{\circ}$  Latitude entering the Table of Amplitudes, Page 42 of the Vol. of Tables, you'll find the true Amplitude to be  $27^{\circ} 30'$ .

Then having described the Circle and quartered it, prick the true Amplitude from E or the East point towards the North to B, and taking the Magnetical Amplitude  $36^{\circ}$ , prick that also from E

Mag. Ampl.	$36^{\circ} 00'$	Northward to C,	and taking in the Compasses
True Ampl.	$27^{\circ} 30'$	the distance between C and N the North,	set
Variat.	$8^{\circ} 30'$	one foot in B the point of true Amplitude, and	

the other being turned towards the North reaches to M, the point to which the North point of the Compass is directed, so that M N  $8^{\circ} 30'$  is the quantity of Variation, and because M falls towards E, that is between N and E, it is Eastward.

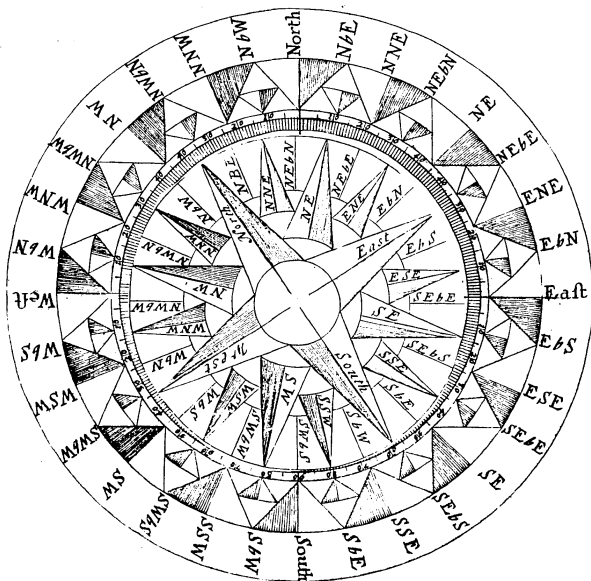


Now if you take an old Compass Card, and lay within this Circle, so that its North and South line may lie on the line MP, then will this Compass Card represent the Varied Compass, and the Circle NESW the Horizon or Compass without Variation, so that if you take with a pair of Compasses the distance between the North or point N, of this outermost Circle, and the point of your Course on the Varied Compass, or Card representing it, and afterwards set one foot on M, the other will shew on the Compass Card amongst the points the True Course.

Or



Or thus, you may have two Compass Cards, to move one upon the other, as you see here, and taking the true Amplitude from the graduated limb let it from the East point, if the Observation be at rising, or else West point of the under or fix Compass, either towards the North or South according as the Amplitude is, prick also the Magnetical Amplitude thereon after the same manner as to C, then take the distance between the point of *Magnetical Amplitude* C, and the North point of the lower or fix Compass, prick it from B, the point of true Amplitude to M, and bring the North point of the moveable or upper Compass to M: then if you look any Course on the upper Compass, the point against it on the neather Compass is the true Course, or the Contrary.



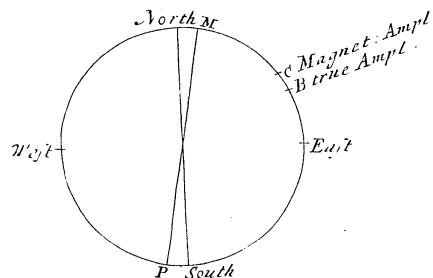
Example

## Example 2.

In Latitude  $41^{\circ} 00'$  North, the Sun having  $17^{\circ} 00'$  Declination South, the Magnetical Amplitude at Sun-set is observed to be  $36^{\circ} 00'$  from the West Southward, what is the Variation, and which way is it?

By entering the Table of Amplitudes with the Latitude and Declination as before directed, the *true Amplitude* will be found to be  $22^{\circ} 47'$ , which being pricked on the Circle from W (as before directed) to B, and also the *Magnetical Amplitude* to C, the distance between MN shews the Variation to be  $13^{\circ} 13'$ , and that Eastward from the North.

Mag. Ampl.	$36^{\circ} 00'$
True Ampl.	$22^{\circ} 47'$
Variat.	$13^{\circ} 13'$



Example



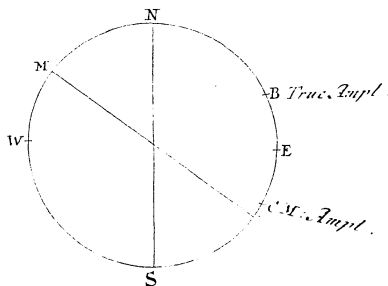
## Example 3.

Let the Declination be  $15^{\circ} 00'$  North  
 The Latitude be  $50^{\circ} 00'$  North  
 And the Magnetical Amplitude at Sun rising  $29^{\circ} 00'$  South  
 And it be required to find the Variation of the Compaſs.

Having deſcribed a Circle and quartered it, prick the *true Amplitude* (which by the Table of Amplitudes is found to be) twenty three Degrees forty four Minutes from E the Eaſt point towards the North to B, and the

*Magnetical Amplitude*  $29^{\circ} 00'$ , from E Southwards (according to the Obſervation) to C: then taking the diſtance between C the *Magnetical Amplitude*, and N the true North, ſet it from B Northward, and it finds the point M, the

Diſtance between M and N is  $52^{\circ} 44'$  the Variation, which is Weſtward, becauſe M falls between N and W.



Example

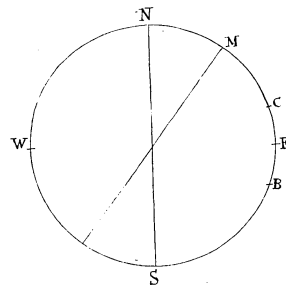
## Example 4.

Let the Declination be  $11^{\circ} 00'$  South  
 The Latitude be  $49^{\circ} 00'$  North  
 And the Magnetical Amplitude at Sun Riſing  $17^{\circ} 00'$  North  
 To find the Variation.

The *True Amplitude* by the Tables is  $16^{\circ} 54'$ , from the Eaſt Southward, becauſe the Declination is South.

*Magnetical Amplitude*  $17^{\circ} 00'$   
*True Amplitude*  $16^{\circ} 54'$   
 The Variation from the North Eaſtward  $33^{\circ} 54'$

As is ſeen by the Figure.



M m

Example



## Example 5.

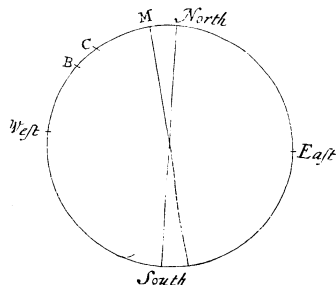
Being in Latitude  $51^{\circ} 30'$  North, the Sun having  $21^{\circ} 00'$  Declination North, I observe the *Magnetical Amplitude* at Sun set to be  $49^{\circ} 00'$  from the West Northward, and require the Variation.

First, by entering the *Table of Amplitudes*.

I find the *True Amplitude* to be  $35^{\circ} 8'$ , which being pricked on the Circle, as before directed, and also the *Magnetical Amplitude*.

I see thereby the Variation to be  $13^{\circ} 52'$ , that is, the North point declines from the true North, or interfection of the Horizon and Meridian  $13^{\circ} 52'$  towards the West.

<i>Magnetical Amplitude</i> .....	49°	00'
<i>True Amplitude</i> .....	35	08
<i>The Variation</i> .....	13	52



## EXAMPLES.

## EXAMPLES.

*The Variation by the Azimuth.*

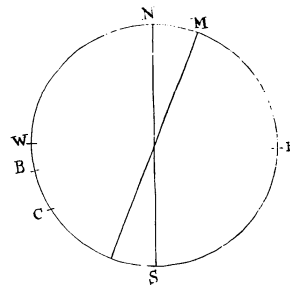
## Example 1.

May 1, 1680. Afternoon, in the Latitude  $59^{\circ} 00'$  North, the Sun having  $30^{\circ} 00'$  Altitude, the *Magnetical Azimuth* was Observed to be  $126^{\circ} 30'$  from the North westward, that is,  $53^{\circ} 30'$  from the South Westward: what was the Variation of the Compass?

By calculation as directed in the Cosmography, the true Azimuth is found  $74^{\circ} 26'$  from the South Westward, which you must prick from S Westward to B, and the *Magnetical Azimuth*  $53^{\circ} 30'$  from S to C: then taking the distance CN, and setting it from B Northward, it will find the point M, and MN is the Variation.

<i>True Azimuth</i> .....	74°	26'
<i>Mag. Azimuth</i> .....	53	30

*The Variation from the North Eastward* .....



Miles of  
whole Cir.  
than ...

Mm 2

Example

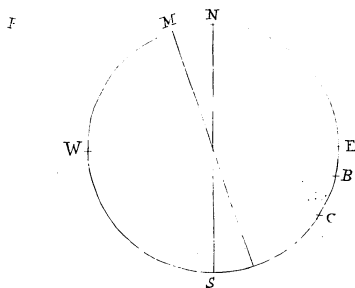


## Example 2.

May 9, 1680. Beforenoon, in Latitude  $58^{\circ}00'$  North, the Sun having  $32^{\circ}00'$  Altitude, the Magnetical Azimuth from the North was Observed  $127^{\circ}00'$ , which is  $53^{\circ}00'$ , from the South Eastward: what was the Variation?

By the Latitude, Declination, and Altitude, the *True Azimuth* will be found to be  $76^{\circ}10'$  from the South, which being prick'd on the Circle towards its proper Coast, and also the Magnetical Azimuth  $53^{\circ}00'$ , the Variation will appear to be  $23^{\circ}10'$ , from the North Westward.

True Azimuth	_____	76° 10'
Mag. Azimuth	_____	53 00
The Variation.	_____	23 10



Of the Quantity of a Degree of a great Circle on the Earth,  
and how it's found.

There are many ways of discovering the quantity of a Degree on Earth, but none so natural as that used by our Country-man Mr. *Norwood*, which was to measure withal exactness possible the distance between some two places lying directly under the Meridian, or North and South one of another the farther distance the better, and to Compare that with the Degrees and Minutes in the difference of the Latitudes of those two Places, the Latitudes of both places being observed with all the niceness and curiosity imaginable. By this means he found no less than 367200 of our *English* feet to answer to a Degree of Latitude, which hath been farther since confirmed by many other experiments in our own Country, but the greatest confirmation is that by the very same manner of Experiment, viz. by measuring between two places under a Meridian in *France*, hath been found 365184 *English* feet in a Degree. But Mr. *Norwood* considering that the Ships way is more than is really given by the *Log-line*, and that it is more safe to have the Reckoning somewhat before the Ship, flung away the 7200, retaining only 360000 to one Degree, and consequently 6000 feet to a Minute or  $\frac{1}{60}$  part of a Degree, according to which account there is of our Statute measure of 5280 feet to the Mile, 68  $\frac{1}{4}$  Miles to a Degree, and of the *English* Sea Miles, or *Italian* Miles of 5000 to the Mile, 72 Miles, or 24 Leagues in a Degree, and the whole Circumference of the Earth is 8640 Leagues, which is 120 Leagues less than the *French* experiment makes it, and than really are.

5280	360000	(68	5000	360000	(72	360
	3168			35		24
	4320			10		1440
	4224			10		720
	960			0		8640

Of the Estimation of a Ships way at Sea.

In the now practice of *Navigation*, there's hardly any thing more necessary than to be able to make a good estimate of the Ships way with any Wind.

For

Of



For which many ways have been thought of by Wheelworks, &c. but to little purpose, the Nations now of Fame and Experience at Sea making better work, by means of less contrivance and intricacy. Some only guessing by the Sail born and running of the froth or water by the Ships side, as the *Spaniards* and *Portuguese*, others by flinging into the water a Chip or the like, and counting how many equal timed paces they can make on the Deck, while the said Chip drives between any two bolt heads or marks on the side, which is usual amongst the *Dutch*: But the most approved way and now most followed, is by our *English-Log* and *Log-line*.

### Of the Log, and Log-line,

The *Log* is only a piece of wood, which being tyed to a line and cast over board, and the line veered out as fast as the *Log* will carry it away, or as the Ship Sails so that it may have leave to pull away as much line, as it can without being dragged by the Ship, any more than what the weight of the line will do, doth shew according to the time it's veering how much she has Sailed, and consequently her rate of Sailing.

This line at about 10 Fathoms from the *Log*, (which is allowed that the *Log* may be out of the eddy of the Ships wake, before the half minute, which is the time most commonly allowed for the veering the line, begins to run) has a mark or knot for the beginning, and from thence is marked into spaces called knots.

The space of line between knot and knot ought to be such a part of a Minute of a Degree, as the half Minute of time is of an hour, so that the half Minute being the one hundredth and twentieth part of an hour, the length of line between knot and knot should be the one hundredth and twentieth part of a minute of a Degree of a great Circle of this Terraqueous Globe. And a minute being as is before proved six thousand *English* feet, the length of the line between the knots ought to be 50 feet: But they are commonly knit at but 7 Fathoms or 42 feet distance, ground-

ing upon this error, that there's but 300000 feet in a Degree, and but 5000 in a Minute. Yet it being still found by the Ships run, that this did not answer to the parts of a Degree, they have lessened their half Minute by about five seconds of time, which brings it to the same thing in effect. Never-

theless it were to be wished that the latter though it serve a turn, might be omitted, and the true half minute brought in use with the *Log-line* knit at its true lengths.

$$\begin{array}{r} 12|0 \\ 60 \overline{) 600} \\ 60 \\ \hline 00 \end{array}$$

So many knots as are veered in half a Minute, so many Miles the Ship Sails in an hour, or so many Leagues and so many Miles in a Watch, or four hours.

As three knots in half a minute is three Miles in the hour, or four Leagues in a Watch; Four knots in half a minute is four miles in an hour, or five Leagues one mile in a Watch.

The *Log* is commonly thrown every two hours, but some throw it every hour. Every Noon if possible the Latitude ought to be Observed, but whether Observation or none, the Master and his Mates, then call for the *Log-board*, and add up the knots and Fathoms run since the last noon, the sum shews the miles Sailed that twenty four hours, if the *Log* were Cast every hour; but if it were cast but once in two hours, they double the sum of the knots run, and that shews the miles Sailed. If you would have the Leagues Sailed divide by three.

This account ruff taken off the *Log-board*, ought to be entred into a Book called a *Traverse Book* or *Log Book*, and afterwards the *Traverse* from last day noon being worked, and the difference of Latitude and Departure found and Corrected by Observation if any made, must be entred fairly in another Book called a *Journal*.



*The Traverse or Log-Book for a Voyage intended  
by Gods assistance, for the Cape Good-hope in the  
Ship*

Anno, 1679.

b	t	fa	Courfes.	Winds.	
4	16	0	SSW	ESE	June 9th. Being Sunday, at about $\frac{1}{2}$ an hour after 4 in the morning, we saw the <i>Lizard</i> point bear NNE about 4 Leagues off us. We had a fresh gale, fair weather, and smooth water.
5	6	1	WSW		
6	6	3			
7	6	3			
8	6	3			
9	6	3			
10	6	3			
11	6	4			
12	6	4			
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b	k	ta	Courset.	Winds.	June 13th. Fryday, little wind, fair weather and smooth Water.
1	2	4	S W	S S E	
2	3	0			
3	2	0			
4	2	0			
5	2	0			
6	2	5			
7	2	1	S W by W	S by E	
8	1	0			
9	1	0	W	S by E	
10	2	3	W by S	we bore up.	
11	2	0	S W by W		
12	2	4	S W $\frac{1}{2}$ W	S S E	
1	2	4	S W		
2	3	2			
3	3	2			
4	3	6			
5	2	0			
6	2	0			
7	2	0			
8	1	4	S W by W	S by E	
9	1	0	S W	S S E	
10	2	4			
11	1	0			
12	0	3			
21	50	1	Miles Run.		
1	1	0	S W	S S E	
2	1	0	S W by W	S by E	
3	0	6	W S W $\frac{1}{2}$ S	S	
4	1	2			
5	0	3		S by E	
6	1	0			
7	0	6	S W by W		
8	1	1	W $\frac{1}{2}$ S		
9	2	2			
10	1	6	W		
11	0	6			
12	1	1	S W $\frac{1}{2}$ W	S S E	
1	1	3	S W by W	S by E	
2	1	3	S W by W	S by E	
3	1	4	W S W	S	
4	2	0			
5	2	4	S W	S S E	
6	3	3	S W by W	S by E	
7	3	6	W S W	S	
8	2	6			
9	3	2			
10	0	6	we lay by		
11	2	3			
12	2	0	W by S	S by W	
21	37	0	Miles Run.		

June 13th. Fryday, little wind, fair weather and smooth Water.

Zenith Dist.  $24^{\circ} 31'$   
Declin. North.  $22^{\circ} 48'$   
Lat. North.  $47^{\circ} 19'$

The true Course I make to be West  $32^{\circ}$  South, Distance Run  $40 m.$  and the Meridian Distance  $41 m.$  West.

June 14th. Saturday, the wind very scant, the weather pretty fair, a great S.e. coming from the South West, which makes us believe we shall have fresh North Westerly winds to morrow.

Zenith Dist.  $24^{\circ} 30'$   
Declin. North.  $22^{\circ} 43'$   
The Lat. North.  $47^{\circ} 13'$

The true Course I make to be West  $10^{\circ}$  South, her Distance Run  $37 m.$  and her Merid. Distance  $36 m.$  West.

The

The Journal to the former Log-Book, for a Voyage intended by God's assistance for the Cape Buona Speranca.

Anno, 1679.

Month & Day.	Latitude by Observation.	True Course correct by Variation.	Corr. Dist.	North. Leg.	South. Leg.	East. West. Legs.	Departure from the Lizard, or Long. according to the P.C.	Longitude from the Lizard.
				M. Miles	Mil.	Mil. Mil.		
June 9	49 35	W 33 South	64		35	53	0 53	1 21 36
10	48 55	W 26 South	91		40	81	2 14	3 25 01
11	48 27	W 19 South	83		27	78	3 32	5 22 43
12	47 45	S 31 West	48		42	25	3 57	6 00 04
13	47 19	W 32 South	49		26	41	4 38	7 00 26
14	47 13	W 10 South	37		6	36	5 14	7 53 28
15		W 5 North	53	5	0	57	6 11	9 17 26
16	47 30	W 15 North	50	12		48	6 59	10 28 26
17	47 13	W 22 $50^{\circ}$ S	46	0	17	42	7 41	11 30 10
18	46 43	S 23 $35^{\circ}$ E	33		30	13	7 21	11 11 14
19	45 22	S 9 $50^{\circ}$ East	82		81	13	7 08	10 52 14
20		South near.	104		102			
21		S $5^{\circ} 30'$ W	130		130	12	7 20	11 08 48
22	39 06	S $2^{\circ} 50'$ W	144		144	8	7 28	11 19 06
23	36 55	S $10^{\circ}$ West	133		131	23	7 51	11 47 54
24	34 42	S 5 West	134		133	12	8 03	12 02 29
25	32 55	S 9 West	109		107	8	20	12 22 45
26	31 06	S 9 West	110		109	17	8 37	12 42 33
27	29 27	S 6 West	100		99	10	8 47	12 54 05
28	28 50	W 34 South	67		37	53	9 42	13 57 05
29	27 12	S $36^{\circ}$ West	134		108	78	11 01	15 25 51
30	24 56	S 6 West	136		135	14	11 15	15 41 18
July 1	22 19	South	157					
2	19 46	S 1 East	153	153		3	11 12	15 44 30
3	13 33	South	71		71		11 12	
4	16 33	South	120		120		11 12	
5	14 33	S $1^{\circ}$ East	120		120	2	0 11	10 15 42 26
6	14 02	S $10^{\circ} 15'$ W	35		33	11	11 21	15 53 46
7	13 23	S $25^{\circ} 30'$ E	43		39	18	11 03	15 35 16
8	12 29	S $38^{\circ} 50'$ E	70		54	44	10 19	14 50 13
9	11 09	S $23^{\circ} 15'$ E	82		80	17	11 9	14 33 00
10	9 45	S $25^{\circ}$ East	93		84	39	9 23	13 53 20
11	8 35	S $40^{\circ}$ East	90		70	58	8 25	12 55 00



### *Sailing by the Arch of a Great Circle.*

**T**His though it shew the nearest way and Distance between two Places, yet cannot come so much in use as the two former kinds of Sailing, Men being either drawn from it by conveniences of winds and streams; or else forced from it by cross winds, and Pirates, or interposition of Shoules, Islands, Headlands, &c. Nevertheless for their sakes whose Curiosity leads them to a desire of understanding this also, I shall add a few pages thereof.

If the two Places to be Sailed between, be both under the Equinoctial, the Course is directly East and West, and the Degrees Difference of Longitude tis the Distance.

If the two Places be both under one Meridian, the Course is directly North or South, and the Degrees Difference of Latitude is the Distance, unless the two Places be one in South Latitude, and the other in North, and then the Sum of the two Latitudes is the Distance.

#### *Proposition 1.*

1. Two Places one under the Equinoctial, the other in North or South Latitude, the Latitude of this latter Place, and their Difference of Longitude being given, to find their Distance on the Arch of a Great Circle, The position of the first Place from the second, and also of the second from the first.

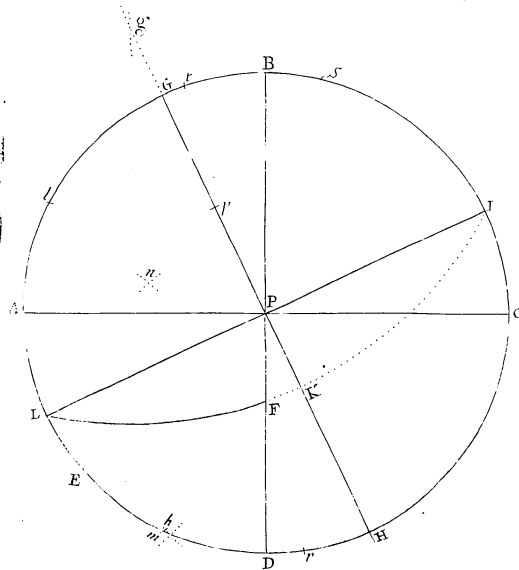
Let the Difference of Longitude between to Places be  $66^\circ$ , and the Latitude of that Place having Latitude  $50^\circ 00'$ .

#### *Geometrically.*

With the Chord of  $60^\circ$ , describe the Circle ABCD, which is to represent the Equinoctial, draw the Diameter AC, and at right Angles thereto the Diameter BD, from D, Prick the Difference of Longitude given  $66^\circ$  to L, and draw the line PL the Meridian of that Place in the Equinoctial, and the line GH at right Angles thereto.

Prick

Prick the Latitude given  $50^\circ$  from D to E, and laying a Ruler over C and E, find the Point F representing the Place in  $50^\circ 00'$  Latitude, with any convenient extent of the Compasses, setting one foot in L, with the other make a small Arch at *m*, and another at *n*, and afterwards fixing one foot in F, with the other make two other Arches crossing the former in *m* and *n*, over which a Ruler being laid will find on the line HG produced the Point *g*. Lastly, Setting one foot in *g*, with the other describe the Circle LFI, representing the Great Circle passing over the two Places.



Tp



To Measure the Arch LF which is the Great Circle Distance.

Lay a Ruler over I and K, and thereby make on the Limb the mark *h*, then prick *Hh* from L to *l*, and laying a Ruler over *l*, make the mark *p*, which is the Pole of the Arch LKl. Lastly, Laying a Ruler over the points *p* and F, find the point *r*, to is *Lr* the measure of the Arch LF, the Great Circle Distance.

To Measure the Angle FLD.

Which shews the Position of the place F in  $50^{\circ} 00'$  Latitude from that at L under the Equinoctial, lay a Ruler over the points *p* and L, and make the mark *t*, the Arch *Lt* is the measure of the Angle FLD.

To Measure the Angle LFD.

A Ruler laid over F and *p* finds the point *t*, and the Arch *At* is the measure of the Angle F.

Arithmetically.

In the Rightangled Spherical Triangle LDF, Rightangled at D are given the sides LD the Difference of Longitude, and FD the Latitude of the Place having Latitude, to find the Angles L and F, and side LF.

To find the Angle FLD.

DL is the Mean, and the Angle L, and side DF are adjacent extremes; Therefore,

As the Tangent of FD $50^{\circ} 00'$	10,076189
Is to the Radius	10,000000
So is the sine of LD $66^{\circ} 00'$	9,960730
	19,960730
To the Tangent of the Angle FLD $52^{\circ} 32'$ equal to the Arch SL.	9,884544

To

To find the Angle LFD.

FD is the mean, and the side LD, and Angle F are extremes adjacent; therefore,

As the Tangent of LD $66^{\circ} 00'$	10,551417
Is to the Radius	10,000000
So is the sine of DF $50^{\circ} 00'$	9,84254
	19,884254
To the Co-tangent of the Angle LFD $71^{\circ} 10'$ equal to At.	9,532837

To find the side LF.

LF is the mean, and the sides LD, DF are extremes disjunct, and the mean is sought; therefore,

As the Radius	10,000000
Is to the Co-sine of LD $66^{\circ} 00'$	9,609313
So is the Co-sine of DF $50^{\circ} 00'$	9,808067
To the Co-sine of LF $74^{\circ} 51'$ equal to Lr.	19,417380

Proposition 2.

2. Two Places both in the same Parallel of Latitude, the Latitude and their Difference of Longitude being given, to find the Great Circle Distance between them, and the Angles of Position.

Admit two Places in the Parallel of  $50^{\circ} 00'$  Differing in Longitude  $60^{\circ} 00'$ .

Geometrically.

Having described the Circle ABCD, and drawn the Diameters AC, BD at rightangles one to the other, prick  $60^{\circ} 00'$  the Difference of Longitude from D to L, and draw LPl, and at rightangles thereto OPR. Then prick the Latitude  $50^{\circ} 00'$  from D to E, and laying a Ruler over CE, find the point F, through which describe the Parallel of Latitude FZN. Afterwards bisect the Angle LPD, draw the oblique line MPg, and at rightangles thereto GPH. Lastly, by two intersections as was shewed in the last Proposition, find the center g, and describe the Arch GZGH. ABCD represents the Equinoctial, P the Pole thereof, APC, LPl, BPD, GPH Meridians, Z one of the Places,











the point  $z$ . Draw the obscure line  $zG$ , and at right Angles to  $zG$  draw  $Gg$ , which being produced, will concur with the line  $LI$  produced in  $b$ . Lastly, through the three points  $zFb$ , describe the Arch  $bzF$ , which will represent the great Circle passing over both places.

To measure the Arch  $zF$  the great Circle distance, you must first find the Pole thereof thus.

Draw the line  $RPK$ , and at right Angles thereto draw also  $MPaN$ . Then laying a Ruler over  $K$  and  $a$  mark  $s$ , and lay  $sN$  from  $R$  to  $t$ , a Ruler over  $K$  and  $t$  will find  $p$  the pole of the Arch  $Rz$   $aK$ . Lastly, lay the Ruler over  $p$ , and both  $z$  and  $F$ , making in the Limb the marks  $v$  and  $w$ , and the Arch  $vw$  is the measure of  $zF$  the great Circle distance.

To measure the Angles of Position  $PzF$ ,  $zFP$ .

Lay a Ruler over  $p$  and  $z$ , and find the point  $x$ , then is  $xG$  the measure of the Angle  $PzF$ . Again the Ruler laid over  $p$  and  $F$  finds the point  $k$ , and  $kC$  is the measure of the Angle  $zFP$ .

$Ns$  is the greatest Latitude the Arch passes. And  $LN$  is the Longitude from  $z$  of the greatest Latitude.

To find the Latitude this Arch shall pass through at every five or ten Degrees of Longitude, &c. from either place.

Prick ten Degrees from  $D$  to  $10$ , and from  $10$  to  $20$ , and from  $20$  to  $30$ , &c. to  $L$ , and draw the lines  $10 \lambda P$ ,  $20 \delta P$ ,  $30 \theta P$ , &c. Then take the extent between  $D$  and  $C$ , or  $D$  and  $A$ , and prick it from  $10$  to  $1$ , and from  $20$  to  $2$ , and from  $30$  to  $3$ , &c. Then laying a Ruler over  $1$  and  $\lambda$  find the point  $i$ , so is  $i10$  the Latitude at ten Degrees Longitude from  $F$ , lay the Ruler over  $2$ ,  $\delta$ , it finds the point  $m$ , and  $m20$  is the Latitude at twenty degrees Longitude from  $F$ , &c.

Here I might have shewed the measuring of the Angles of Position, at each five or ten Degrees difference of Longitude, and the distance that must be Sailed in altering each five or ten Degrees Longitude, and how to have found the difference of Longitude, and Angle of Position at each Degree, or half Degree difference of Latitude, or the difference of Longitude and Latitude, and distance made in altering the Angle of Position a quarter or half a point, but that we have been two large already.

The Projection here used is not the easiest to delineate, or most convenient to measure from the distances, Latitudes and Angles, but considering that the chief use of this Circular Sailing is only to exercise Youth in Spherical Triangles, I have chosen that Projection which might represent the Triangles best, and make the thing plainest to view, other ways they may find in Mr. Philips Geometrical Scaman, and Mr. Collins Plain Scale, &c.

Arith.

Arithmetically.

To calculate the great Circle Distance  $zF$ .

In the Oblique Triangle  $zPF$  is given the side  $zP$   $48^{\circ} 10'$ , the Complement of the Latitude of Cape Cod, and the side  $FP$   $39^{\circ} 50'$  the Co-latitude of the Lizard with the comprehended Angle  $zPF$   $58^{\circ}$  the difference of Longitude, to find the side  $zF$ .

The easiest way to work this is by the Verfed lines; thus,

2) $58^{\circ} 00'$	The Log. sine of $48^{\circ} 10'$	9,8722076
$29^{\circ} 00'$	The Log. sine of $39^{\circ} 50'$	9,8065579
	The double of the Log. sine of $29^{\circ} 00'$	19,3711424
	The natural sine against	39,0499075
	Is 1123361 which doubled is	2246722

$48^{\circ} 10'$	The Nat. Verfed sine of $8^{\circ} 20'$ the difference	} 105584
$39^{\circ} 50'$	of the sides is	
$8^{\circ} 20'$	The Verfed sine of $40^{\circ} 7'$ the	} 2352306
	the distance sought.	

To find the Angles of Position.

In the Spherical Triangle  $zPF$  are given,  $zP$   $48^{\circ} 10'$  the Complement of the Latitude of the Cape, the side  $zF$   $40^{\circ} 7'$  the distance, and the Angle  $zPF$   $58^{\circ} 00'$  the difference of Longitude, to find the Angle  $PFz$ .

As the sine of the distance $zF$ $40^{\circ} 7'$	9,8091192
Is to the sine of its opposite Angle $58^{\circ} 00'$	9,9284205
So is the sine of the side $zP$ $48^{\circ} 10'$	9,8722076
	19,8006281
To the sine of its opposite Angle $PFz$ $78^{\circ} 42'$	9,9915089

Then for the Angle  $PzF$ ; say,

As the sine of the side $zF$ $40^{\circ} 7'$	9,8091192
Is to the sine of $58^{\circ} 00'$ the opposite Angle	9,9284205
So is the sine of $FP$ $39^{\circ} 50'$	9,8065575
	19,7349780
To the sine of its opposite Angle $57^{\circ} 28'$	9,9258588

To



To find  $P a$  the Complement of the greatest Latitude this circle shall pass through.

In the Rightangled Triangle  $\triangle P a$ , Rightangled at  $a$ , are given the side  $\angle P 48^\circ 10'$ , and the Angle  $\angle P \alpha$ , to find the side  $P a$ ; thus,

As the Radius	10,000000
Is to the sine of $\angle P 48^\circ 10'$	9,8722076
So is the sine of the Angle $\angle P \alpha 57^\circ 28'$	9,9258588
To the sine of the side $P a 38^\circ 55'$ the Complement of } the greatest Latitude.	9,7980664

Afterwards find the Angle  $\angle P a$ ; thus,

As the Radius	10,000000
Is to the Tangent of $P a 38^\circ 55'$	9,9070773
So is the Co-tangent of $\angle P 48^\circ 10'$	9,9518961
To the co-sine the Angle $\angle P a 43^\circ 43'$ which being taken } from the Angle $\angle P F$ leaves the Angle $\angle F P a$ .	89,859734

To find the Latitude of this Arch, at each five or ten Degrees difference of Longitude from  $\alpha$ , or the Lizard, and also the position.

From the Angle  $\angle P a$  take ten Degrees, and there remains the Angle  $\beta P a$ , then in the Rightangled Spherical Triangle  $\triangle \beta P a$  Rightangled at  $a$  are given the Angle  $\beta P a$ , and side  $P a$ , to find the side  $\beta P$  the Complement of the Latitude, and the Angle  $\angle \beta P a$  the position.

If it were required to find the Longitude and Latitude of this Arch, at each quarter point alteration of the course.

Either by adding or subtracting according as the Case requires, successively  $\frac{1}{4}$  point from the Angle  $\angle P \alpha$ , find the Angles  $\angle \beta P a$ ,  $\angle \gamma P a$ , &c. and then in the Rightangled Triangle  $\triangle \beta P a$ , are given the side  $P a$ , and Angle  $\angle \beta P a$ , to find the side  $\beta P$  the Complement of the Latitude, and Angle  $\angle \beta P a$  the Longitude from the Perpendicular, which being compared with the Angle  $\angle P a$ , or  $\angle F P a$  will give the Longitude from either  $\alpha$  or  $F$ .

But if it were required to find the Angle of position and Longitude, at each half Degree or Degree of Latitude from either  $\alpha$  or  $F$ .

By subtracting or adding (as the Case shall require,)  $30'$  or a Degree to the side  $\angle P$  find the side  $\angle \beta$ , then in the Rightangled Triangle  $\triangle \beta P a$ , will be

be given the sides  $P \beta$ , and  $P a$  to find the Angle  $\angle \beta P a$ , and  $\angle P \beta a$ . Here I might shew how, after you have calculated the Latitudes of the Arch at each ten, five, or single Degree of Longitude, to make prick on the Mercators Chart, and to trace a Curve through them, representing the Arch of the Great Circle, &c. But I have too much swell'd the Volume already.

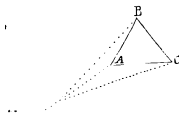
How to find where Currents are, and which way they set, and their rate of Driving, or Drift.

A good way to discover the great and most notable Currents, is by keeping an exact account of your way both outward, and homeward, according to your dead reckoning; being very curious in observing the way your ship makes by the Log-line, for it's not your correct account but your dead reckoning that is here to assist you. Therefore you must be careful to try how the Ship goes by it when you Sail near the Meridian, how she's drawn from her course, as again when she's steered directly East or West, take good notice if she alter her Latitude. As for those guessings by Rippings of the water and driving of froath, &c. along the shore when in sight of it, they can stand a man but in little stead. But the most usual and useful way of observing a Current is thus;

When there's a smooth Sea and not much wind, heave out the Boat taking into her three or four hands, a Compass, Log-line, and half-minute Glas, with a line or small warp of above an hundred Fathoms long, to the end of which line fasten a Triangular piece of board as the board  $ABC$ , and to one of the Angles fasten a good weight of Lead to sink it, some use instead of this board a Kettle tied by the bail. When you are off from the Ship, cast over your board or Kettle letting it sink at least 60 Fathom, and if you have line enough let it go 100 or 120 Fathom, then be- laying the line fast about her stem, it will bring her up and make her ride as if at an Anchor.

Then cast over your Log, turn up the Glas, and as you veer out the Log-line, set the drift of the Log with your Compass, so shall you know whether there be any Current or not; and if any how it sets, and the rate of driving, remembering to add always to the drift, if the line she ride by be sixty Fathom  $\frac{1}{3}$  part, if the line be 80 Fathom  $\frac{1}{4}$ , if an hundred

Fathom





Fathom the  $\frac{1}{2}$  *th* part, &c. of the drift more for the drift of the Boat: for tho the Boat seem to ride or lie still, yet she's found by experience to drive the mean time, but whether these allowances be the very truth I shall not much contend, they are delivered as agreeing with experience, and therefore may be used till farther experience better informs. Yet note that the bigger the weight and board is that the Boat is to be rid by, the less will be her drift.

*Of Lee-way.*

That you may be the better able to judge of a Ships *Lee-way*, always when you are by a wind and have Land in sight just on head, take notice as you keep the Ship steered on the point the Land bore on, how she slides away to *Lee-ward*, and the Land appears still more and more to windward, for by such kind of Observations taking notice of the Sail abroad, streis of wind, Ships trim, and growth of the Sea, the Judgment may be so strengthened that a man shall rarely fail in giving a pretty true allowance.

If the Land in sight be not right on head, yet by taking notice of the point it was on at first, and how it weathers in keeping the same course, you have the same advantage.

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F I N I S.

THE  
DOCTRINE  
OF THE  
SPHERE;  
*Grounded on the Motion of the*  
EARTH,  
And the Antient  
PYTHAGOREAN or COPERNICAN  
SYSTEM OF THE  
WORLD.

---

IN TWO PARTS.

---

L O N D O N:

Printed by *A. Godbid* and *J. Playford*, in the Year 1680.





T H E  
P R E F A C E.



H A T the Reader is like to meet with in the following Treatise, the Contents will inform him, what occasioned the writing of it I have intimated in the first *Section*; I have farther to add, that I thought I could not perform any piece of Service, which might more justly deserve acceptance, or be more usefull to the Ingenious Student of *Astronomy* than this, wherein I have shewed him how all the Diurnal Appearances of the Sun and Stars are naturally made, and how laying aside all *those Old Projections* of the *Sphere*, which falsly suppose the Earths *Stability*, they may be represented, and the Problems concerning them answered by *New ones*, groundd on that true System of the World, which



## THE PREFACE.

supposes the Annual and Diurnal Motions of the Earth, proposed first by *Pythagoras*, asserted by *Copernicus*, demonstrated by *Kepler*, and as most agreeable to reason and experience approved and entertained by the ablest *Astronomers* of our Times.

Hence I have given it the Name of the *Doctrine of the Sphere*, wherein if my Reader shall think I have answered but few of those many Problems that may be proposed, I must tell him, that though I have handled only the most ordinary and useful, yet if (as I suppose) he understands the Nature of Projections, and the Resolution of *Spherical Triangles*; he will readily apprehend how other Circles may be drawn in that I have described, and more Triangles formed, whence answers may be given to any Problem concerning the *Phainomena* of the Sun or Stars, as easily as by any of the *Ptolemaick* Projections hitherto used and Taught.

And least what I have writ should prove useles to him for want of such a perfect knowledge in *Trigonometry*, I have laid down the Analysis or Canon, whereby every particular Problem is answered in words at length, for I know very well there are a sort of diligent and curious Men in the World, who tho they may not at first apprehend the reason of a Rule, yet having frequent occasion to employ it, may at length make themselves Masters of it, and to such works of this Nature prove generally the most usefull.

For whose sake I have followed the same plain Method in the *Second Part*, where I have Taught how to find within what space on the Earth the Solar Eclipse is visible, and where the principal *Phases* appear, by Calculation; as also how all the requisites of the same

Folio C

## THE PREFACE.

Eclipse may be found, for any given place, without the Calculation of *Parallaxes*; which useful Invention having never appeared in Publick before, I find myself obliged to give the following account of its Original, that I may not hereafter be accused of injustice to two of my singular kind Friends, the admirably Ingenious Sir *Christopher Wren*, (Master Surveyor of His *Majesties* Buildings) and our Southern *Tycho*, Mr *Edmond Halley*.

It was in the *Winter* of the year 1676. that I light upon this Method; The Autumn before some spots had appeared in the Sun, and then I was observing a Compact one that made more than two entire Revolutions before it was wholly extinct; Examining my Observations to find the Reason of their different Appearances, I collected from them, that the spots adhered to his Superficies, and that they were carried round his Center once in 25 days and a quarter, the Northern half of that Axis on which this Revolution was performed, being inclined about 8 Deg. to the plane of the Ecliptick, betwixt the 12<sup>th</sup> and 18<sup>th</sup> Degrees of *Virgo*, which being concluded, I found that allowing what alterations must necessarily happen in their Appearances, by reason of the Earths Diurnal Progress in her Orbit, all my Observations would be represented as nearly as I could expect. And now having seen how the Poles, Axis, Equator, and Parallels in the Sun altered their Appearances to the Eye placed on the Earth, according as she changed her place in her Orbit, this put me upon considering how the Axis of the Earth, and the several Paths, or Parallels imagined on it, would appear from the Sun, and how the Diurnal *Phainomena* would



## THE PREFACE.

would be represented by an *Orthographical* Projection of our Globe, on a Plane standing at Right-Angles to the Ecliptick, and the Line connecting the Centers of the Sun and Earth: Here I found what I have delivered in the first *Section* of the Second Part of this Treatise, viz. how the Parallaxes of Altitude, Longitude, and Latitude, were made, and given by Construction, and upon a little farther Consideration, how the Times of any Appearance of a Solar Eclipse, the parts then darkned, with the Inclinations of the Cusps might be determined, without any Calculation of them, by the help of such a Projection. Much pleased with this discovery, I immediately constructed an Eclipse I had observed at Derby, Octob. 25. 1668. and with a brief Description of the Method transmitted it to my kind Friend, and then Living Patron Sir *Jonas Moore*, by whom it was Communicated to the Royal Society at one of their Meetings; It hap'ned Sir *Christopher Wren* was there present, who having viewed the Figure only, told him, that himself had known the same Method 16 years ago, and to assure him of it, sent him soon after a like Projection neatly drawn on Pastboard, and fitted with several Ingenious contrivances of Numbers and Scales for the Construction of Solar Eclipses in our Latitude. This Sir *Jonas* brought down to me, then Labouring under some Distempers, to *Greenwich*, whereby I was satisfied that the honour of the first Discovery of this useful invention was absolutely due to Sir *Christopher Wren*, whom of all Mortals I believe to have been the first, that knew how to find the Times of the Beginning, Middle, Digits then darkned, Inclination of the Cusps at any Phasis, and End of a Solar Eclipse, without the Calculation of Parallaxes.

In

## THE PREFACE.

In some Discourse I had with Mr. *Halley*, before he went to observe the Southern Constellations at *St. Helena*, he Mentioned the Construction of Eclipses as possible, but out of a tender Affection to his own Inventions, or for what other Reason I know not, he was pleased to conceal his Method both from me, who then thought it scarce possible, and, for ought I can understand, from all others: Nor is it to be wondred at, that three of us should make this discovery severally, and without any Intimation of the Method from each other; For to me it seems very unlikely, that any one who admits the Motion of the Earth, and apprehends how the Moon passing betwixt the Sun and it, Eclipses some part of him to all those People who lie under its passage, should ever miss of it. But we might rather admire, (had I not intimated the Reason of it in the fifth *Section* of the Second Part) that the acute Wit of the Sagacious *Kepler* should overlook it, when he had discovered the Method of finding by Calculation within what spaces on our Globe the Solar Eclipse is bounded, and where the principal Phases of it would appear.

I had almost finished what I have here delivered concerning the Construction of Eclipses, when it was intimated to me by my kind and Ingenious Friend Mr. *Perkins*, that there was little extant in the *English* Tongue concerning the general Method of Calculation aforementioned, and that therefore I might do well to explain it. I considered then that this might be performed more easily than is Taught by the first famous Inventer, and without his Nonagesimary Table. Waving therefore my first intent, which was not to engage my self in any thing, that had been expressly handled by others



## THE PREFACE.

others before me; I thought it necessary to impose this farther task on my self, and accordingly wrote the precepts relating to that Subject, after, tho for Method sake, they are inserted before the Construction of the Solar Eclipse.

In the year 1670. I first published Predictions of the Moons Appulses to Fixed Stars, which I continued Eight years after successively, first in the *Philosophical Transactions*, after in the *Royal Almanack*, proposing them as an useful and the most practicable expedient for finding the *Longitude*, or difference of Meridians betwixt any two places, by reason both of their frequency, and that a single Person might obtain what ever is required in Observations of them with a small *Apparatus* of Instruments, but the Calculation of Parallaxes required in their Application caused them to be less regarded then I hoped they would have been; I have therefore shewn here how this tedious labour may be avoided, and the Occultation or Emerision of a Star from the Moon, or the Time of its visible Conjunction with her Center, and distance then from her next Limb may be found by Construction, as the *Phases* of a Solar Eclipse; and the difference of Meridians betwixt two distant places, by Observations of the same Appulse made at each; and now the main difficulty being removed, I would again recommend this Method to the Study and Practice of the Ingenious *Astronomer* and *Navigator*.

Whom I advise to make himself well acquainted with the first part of this following Work, if he intends thoroughly to understand the second, wherein the Method of Constructing Eclipses and Appulses is Taught. And to carry this Notion along with him, which I forgot to insert in his proper place, *That by the true distance of the Sun or a Star from the Vertex, I mean an Arch in the Earths*

## THE PREFACE.

*Earth's superficies intercepted betwixt two Lines produced from its Center, the one to the station of the Observer, or Vertex, the other to the Sun or Star.* Something may after appear difficult, especially to such Young Artists, as this piece is properly design'd to instruct, though I have endeavoured to be as plain as was possible; but where there are such able Masters as Mr. Perkins to explicate them, some little difficulties will be found rather an advantage, than otherways to the Student.

The aforementioned Predictions of Appulses gave occasion to my first acquaintance with Sir *Jonas Moore*, who well apprehending their use, and that good Observations of the Moons Motions constantly continued for some years, and an accurate Catalogue of the Fixed Stars were required, before this easy Method was to be applyed, was pleased to recommend me for that Work to his MAJESTY, who has so far encouraged it by his Liberal allowance, that we need not doubt but what is wanting may be obtained in reasonable Time. And now Sir *Jonas* having left a Book of *Navigation* in the Press, by reason of his sudden Decease, unperfect; I thought I could not at present better answer the Engagements I lie under to my Royal, and most Gracious Master, than by imparting to the Publick an Invention, which through his Favour and Princely Care may become of ample use to it, in a piece designed by the Author for his peculiar service. In doing of which I hope I may be allowed to have satisfied the interest of that debt of Gratitude I owe his Memory, and that the discharge of the Principal will be Respited, till such time as Providence shall enable me with a more proper occasion, which I hope may be e're long.



# THE CONTENTS.

## PART I.

**T**HAT the Pythagorean System of the World, is both elder and more rational, than any hitherto proposed; Arguments for it drawn from the vast Magnitude of the heavenly bodies, and the Rotation of the Planet Jupiter about his Axis; the Fundamentals of that Hypothesis laid down. Sect. 1.  
An Explanation of these Fundamentals, and some Terms. Sect. 2.

A Stereographical Projection of the Globe, or rather a Sphere or Rete close encompassing the Earth, grounded on these Fundamentals, is taught and described; what is meant by the Sun's place in the Ecliptick. Sect. 3.

How the Sun's place being given; his distance from the North-Pole of the Globe, the Rectification, his Right Ascension, and the Angle of the Meridian and Ecliptic at his Center are formed, represented in this Projection, and found by Calculation. Sect. 4.

How the Sun's Distance from the Vertex, and Azimuth at the hour of 6 are made, represented, and found by Calculation, his, and the Path's Distance from the Pole being given. Sect. 5.

How the Sun's Distance from the Vertex when due East and West, and the Time from Noon when he is so, are represented and found by Calculation, the same things being given. Sect. 6.

How the Amplitudes and Ascensional Differences are found, represented, and from the same Data Calculated. Sect. 7.

How the Sun's Meridional Distance from the Vertex may be found, his and the Path's Distance from the Pole being given. Sect. 8.

How to lay down any hour Circle in the Projection; to find the Sun's Distance from the Vertex at any hour by Calculation, his and the Path's Distance from the Pole being given. Sect. 9.

Or his Distance from the Vertex and Pole, with the Latitude of the Place being given to find the hour from Noon. Sect. 10.

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How

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How the Point of the Ecliptick in the Meridian with its Distance from the Vertex, the Nonagesime, or highest Point of the Ecliptick, with its Distance from the Vertex are formed in the Projection, and how they may be found by Calculation, at any given time in a given Latitude. Sect. 13.

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**A**N Orthographical Projection of the Globe, Sphere, or Rete, on a Plane touching the Moon's Orbit, at Right-Angles to the Line Connecting the Centers of the Earth, and Sun, or given Star, by infinite straight Lines proceeding from either to the Rete or Sphere is Taught, and Described; and the Moons Parallaxes in Altitude, Longitude and Latitude, determin'd by it only. Sect. 1.

The Breadth of the Semidiameter of the Disk, Penumbra, and Earth's shadow demonstrated, how the Eclipse of the Sun is made. Sect. 2.

How the true Places of the Sun and Moon, her Latitude, Herary Motion, Horizontal Semidiameters, and Parallaxes may be found by Calculation, by Tables annexed to this Treatise fitted to the Meridian of London, with Examples, the Author discovers the greatest Error of the said Tables. Sect. 3.

How by the said Tables to find the Times of the Acan and True Conjunctions or Oppositions of the Luminaries, as also of the Principal Phases of a Solar Eclipse under the Meridian of London, with the Longitudes of the Places from it, and their Latitudes where the said Phases shall appear, that is,

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2. Where it Ends in his Vertex, as he Rises.
3. Where he Rises Centrally Eclipsed.
4. Where he Sets Centrally Eclipsed.
5. Where the Eclipse Ends in the lowest Point of the Rising Sun.
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8. Where the Sun's lower is just touched by the Moons upper Limb in the Merid.
9. Where his upper is just touched by her lower Limb in the Meridian.
10. Where the Sun is Centrally Eclipsed in the Nonagesime, without the help of any Nonagesimary Table, exemplified in the Eclipse of the Sun hapning July the 2<sup>d</sup> 1684.

The Reason and Demonstration of the said Calculus; A Time at London given, to find the place where the Sun shall then appear Centrally Eclipsed, and Time at that place. Sect. 4.

The Reason and Demonstration of the said Calculus; A Time at London given, to find the place where the Sun shall then appear Centrally Eclipsed, and Time at that place. Sect. 5.

To



To find the Beginning and visible Conjunction of the Luminaries, Digits then Darkned, Inclination of the Cusps, End of the Eclipse, or Time when any possible Number of Digits shall be Darkned, Geometrically, by Scale and Compasses without farther Calculation; These Appearances determined by Construction in the said Eclipse at London, Aleppo, and Jamaica; that the Difference of Meridians betwixt any two places may be found by two Accurate Observations of the same Solar Eclipse at the said places.

SECT. 6.

To find the Time of the true Conjunction of the Moon, and any Star by the said Tables. Of the visible, and Distance of the Star then from the Moons next Limb; or if she cover it, of its Occultation and Emergence from her by Construction, or with Scale and Compasses only; That if the Theory of the Moon, and places of the Fixed Stars were accurately restored, Observations of Appulses would be the best and readiest Expedient for finding of the Longitude; That through His MAJESTIES Liberality and Favour both may be expected in reasonable Time; this Method therefore proposed to the Ingenious Astronomer and Seaman.

SECT. 7.

To find the Beginning, Middle, Digits then Darkned, and End of a Lunar Eclipse, either by Calculation or Construction; Example of an Eclipse to happen August 18. 1681. How to find the Difference of Meridians betwixt two places, where the same Appearance of a Lunar Eclipse hath been carefully observed, with an Example.

SECT. 8.

The remoteness of my habitation from the Press, has been the principal action of the following *ERRATA*, which the Reader is advised to Correct before he proceed any further.

Page 1. Line 19. for *Contignation*, read *Conignation*. p. 2. l. 23. for *Chartes*, read *Cartes*. p. 3. l. 15. for *Prtex*, read *Prtex*. l. 26. for *Declination*, read *Delineation*. p. 4. l. 45. for *Pe*, read *PC*. p. 5. l. 15. for *qTAM*, read *qTm*. l. 28. for the place, read that place. p. 10. l. 12. for *c*, *o*, read *c*, *o*. p. 11. l. 1. for *s*, *o* P, read *s*, *o* P. l. 10. for Chapter, read *Salion*. p. 17. l. 5. for  $\frac{1}{2}$  *c*, *s*, read  $\frac{1}{2}$  *c*, *s*. p. 18. l. 32. for *me*, read *ne*. p. 20. l. 51. put the Comma after *e*. l. 34. for *N*, read *N*. p. 24. l. 5. for *Copernicans*, read by the *Copernicans*. p. 27. l. 7. for *Phases*, read *Phases*. p. 30. l. 1. for *H*, read *r*. l. 5. for *H*, read *H*. p. 31. l. 31. for *T*, read *T*. p. 32. l. 8. for *Oct*, read *Oct*. p. 35. l. 5. for *Added*, read *Added*, or. p. 40. l. 39. for *Solar shadow*, read *Solar*. of the *Jealous*. p. 45. l. 25. Put out the Comma after *Diameter*. l. 32. for *happens*, read *appears*. p. 46. l. 5. for *miles*, read *i. miles*. p. 47. l. 15. for *Disk*, read *Disk* when *see*. p. 48. l. 10. for *that* *Lat*, read *the* *Lat*. p. 50. l. 1. for the Latitude, read that Latitude. p. 58. l. 34. for *Lat*, read *e*. p. 59. l. 1. for *s*, read *s*. p. 72. l. 14. after *Parallax* add, *the* *Suns*. p. 74. l. 41. for *of* *Greenwich*, read at *Greenwich*.

Errors to be amended in the Tables. Page 80. against Feb. 2. for 1 2 31 25, read 1 2 31 35. p. 81. against Aug. 4. f. 7 c2 33 55, f. 7 c2 53 59. p. 86. against Feb. 12. f. 2 16 47. r. 2 16 37. and against Feb. 13. f. 2 19 c8, r. 2 19 45. p. 88. against May 19. f. 1 01 38 c8, r. 1 01 31 c8. and against May 15. f. 15 c2 34, r. 15 c2 24. and against May 11. f. 6 56 18, r. 6 56 14. p. 90. 4th Column after *Octob.* 28. put in 29 30 31. and against 30. for 11 c2 25 35, r. 11 c2 26 51. p. 94. against 29. Deg. f. 59783, r. 49783. and against 30. f. 55429, r. 49429. p. 97. against 5. 27. f. 0 49 30, r. 0 49 40. p. 104. against year 1. f. 6 23 31 29, r. 6 24 35 29. and against 2 days f. 24 22 53, r. 0 24 22 53.

THE



# THE DOCTRINE OF THE SPHERE.

## SECTION I.

Those who have conversed with Antiquity will easily allow the Pythagorean System of the World, lately revived by Copernicus, to have been Composed long before the Aristotelian; which though it had the Fortune to be more generally entertained, and to be adorned with very specious Explications by Ptolemy and his Followers, will force who ever shall go about to defend it, on such Assertions, as no ingenious man could ever conceive to be reasonable: For what person who has been so far acquainted with Astronomical Demonstrations, as to understand how vastly bigger then our Earth, not only the Sun, but some of the Planets also are, how immensely distant from us the fixed Stars are placed, and that some of them are probably bigger than the Sun it self? What man I say, thus informed, could ever conceive that all this great Contignation should be thrown about so slender a Ball as our Earth is.

B

compa-



compared with them, once in Four and twenty Hours? which the *Aristotelians* are forced to affirm. And how could it sink into the conception of a considerate man, that Nature or the unrestrained Architect of the Heavens should contrive *Epicycles* and contrary Motions to carry about the same Body, as they are likewise obliged to assert, when whatever is to be performed by them, might much more easily be effected by one continual progressive Motion of each Planet in a simple Line, as is abundantly proved in the Works of the Learned *Kepler*, and by the near agreement of his Tables with Celestial Observations, whilst the Planets places calculated from the best Numbers extant, grounded on the *Ptolemaick Hypothesis*, are found as wide and different from their observed Positions, as that *System* is from the *Copernican*?

The Noble *Tycho* proposed a third *System*, which as a Mean betwixt these, he thought might find the easier entertainment in the World: In this he admitted the Diurnal Rotation of the Earth about her *Axis*, whereby he avoided the imputation of that absurd Opinion, That the Sun, and with him all the Planets and fixed Stars were carried round her once a day; but the Sun and all the other Planets, save the Moon, moving round him, he supposed carried about the Earth once in a year. By this contrivance he conceived he attributed less Motion to the Earth than the *Copernicans*; and that nevertheless the appearances of the Planets would be represented, as in that *Hypothesis*: But if we may admit the Philosophy of the very ingenious *De Chavert*, it will be found, the Motion he allows the Earth is not less, but as much or more than the *Copernicans* require; and it seems little less difficult to conceive, that the vast Bodies of the Sun and Planets should be carried about it Annually, than Diurnally. However this Opinion has found but very few Followers, those who with *Aristotle* and his Disciples deny the Motion of the Earth, being unwilling to grant so much, as the noble Restorer of *Astronomy* required; and those who, with *Pythagoras* and his Followers the *Copernicans*, admit it, thinking it no less necessary to assert the Annual, than the Diurnal.

But the great and many Discoveries which have been made in the Heavens by the means of the *Telescope*, invented some few years after the decease of this Famous and never enough commended Great Person, have put an end to the Controverſie in the opinion of all ingenious and unprejudiced Judgments, by affording us near as many Arguments for the Earths Motion, as they are in Number. It would require an intire Volume to give an account of all, and what may be inferred from them: I am obliged to brevity, and shall therefore mention no more but the following. The Planet  $\pi$  is allowed by all Astronomers to be carried round the Heavens once in Twelve years, though he be very considerably larger than our Globe of Earth; and when nearest, five times more remote than it from the Sun: This Planet nevertheless is found by undoubted Observations, to turn about his own *Axis* once in some little less than Ten Hours, which I conceive so plain an Argument, both for the Annual and Diurnal Motion of the Earth, that the *Copernicans* need not

not seek any other, till their Antagonists shall produce a better for its stability.

How the Annual appearances of the Planets, their accelerate and retarded Motions, the augmentation and decrease of their visible Magnitudes, together with their Stations, and Retrogradations, are formed in the *Pythagorean* or *Copernican System*, has been abundantly shewed us by those many Learned Persons, who have framed Astronomical Tables on it, for calculating the Planets Places in the Heavens: But how the Diurnal are made out, none that I know of, hath fully informed us. Having therefore obliged my self by promise to the Relations of my deceased kind Friend, the great Encourager of my Studies, and the Author of the foregoing Work, to write an Explication of the *Phænomena* of the *Globe*, which was wanting in it: I shall ground it on that oldest and true *System*, which asserts the Sun to be placed in the Center of our *Vertex*, and all the Planetary Motions (having none proper to himself, besides a Rotation about his own *Axis* once in 25 days 9 hours nearly) and then,

1. That the Earth is carried round the Sun in a large Path, betwixt the Orbs of  $\delta$  and  $\eta$  once in a year.
2. That besides this Annual Motion, she turns round her own *Axis* once in 24 hours.
3. That the said *Axis* is constantly inclined to the Plane of the Orb at the same Angle, and keeps in all parts of the same Revolution, nearly parallel to it self.

These Assertions being the ground on which the following Discourses are founded, it will be convenient to explicate them by a Plane Declination; in doing of which, I shall also take occasion to explain some terms, whereof I shall make frequent use hereafter.

## SECTION II.

IN the uppermost of the two first Figures, let  $\odot$  represent the Sun placed near the Center of the Annual Orb ABCD, in the Periphery of which the Earths Center is carried round him once a year, according to the Succession of the Signs. The Ancients, and all before the Sagacious *Kepler*, supposed this a perfect *Circle*, but he proves it to be an *Ellipsis*, the remotest end of whose longer or transverse Diameter, is Eight Signs, and nearly as many Degrees elongated from the first Star of  $\gamma$ , and having the Sun in one of its focal Points.

Through  $\odot$  the Sun draws the Line  $\gamma \odot \pi$ , this I call the *Equinoctial Colure*; and at right Angles to it, also through the Sun  $\odot \omega$ , this I term the *Solstitial Colure*.

On the Centers  $e$  where these Lines intersect the Annual Orb, describe the four lesser Circles *d o t e*: these may represent the places of the Earths Globe,



Globe, on its four Cardinal Points; and if through  $e$  in each of these, the Lines  $d r$ , be drawn at right Angles to  $\odot e$ , these shall determine the illuminate part of the Disk  $d i r$ , from the obscure  $d o r$ ; wherefore I term the Lines  $d e r$ , the *Horizon of the Disk*.

If the plane of the Annual Orb ABCD, be supposed produced from the Sun infinitely every way, it will describe amongst the fixed Stars that Line we call the *Ecliptick*: And if in any place of the Orb, the Eye be supposed, somewhere in the inferior Hemisphere of the Earth, perpendicular to the *Ecliptick*, over her Center, then shall the utmost Circle of the Earths superior Hemisphere  $d o r i$ , lye in the same plane; and therefore I call it the *Ecliptick on the Earths Globe*, or, when I have no occasion to consider the Annual Orb, simply the *Ecliptick*; and its Center  $e$ , the *Center of the Ecliptick*.

To the Eye thus placed, the Northern Pole of the Globe, or the upper Extremity of that Axis, about which her diurnal Revolutions are made, will appear at  $P 23^{\circ} 29'$  distant from the Pole of the *Ecliptick*, to which if it be joined by the Line  $P e$ , this shall represent the constant distance of the two Poles, or the inclination of the Axes of the Globe and *Ecliptick* to each other; we may call it the *Line of the Direction of the Earths Axis*.

Let this Line be produced each way till it intersect the *Ecliptick* on both sides; so have you that Line in the Disk, I call the *Solstitial Colure*; because when ever the direct Rays proceeding from the Sun's towards the Earth's Center, run parallel to this Line, that is, when the Earths Center shall be found in the *Great Solstitial Colure*  $\odot \odot y$  before described, the longest or shortest Days are made in all places on it.

This *Line of Direction P e* is found allways parallel to the *Great Solstitial Colure*  $\odot \odot y$ , and nearly to it self where ever the Earth is found in her Orbit, during the space of one Annual Revolution.

That Line which stands at right Angles to the Line of direction on the Center  $e$ , we may call the *Earths Equinoctial Colure*; because it keeps always parallel to the great Equinoctial Colure before described, and when ever the Suns Centrall Rays incide directly parallel to it, the Days and Nights are equal in all places: And this also happens when the Earths Center arrives at the Points, where the *Great Equinoctial Colure* intersects the Orbit.

The Inclination of the Axis will be best apprehended by the under Figure, in which the Line CDCC, may represent the great Orb, viewed by the Eye from an infinite distance, some little elevated above its plane  $\Upsilon \odot \approx y$ , the Earths positions in it on the four Cardinal points,  $e$  the Pole of the *Ecliptick*,  $e d$  its Axis, always perpendicular to the great Orb, over the Earths Center, P the North Pole of the World,  $P m$  its Axis, about which the diurnal revolutions are made from West to East, keeping in all parts and places of the Orbit during one revolution, nearly parallel to its self; the Angle of its inclination to the Axis of the *Ecliptick P e* being constantly  $23^{\circ} 29'$ , and for ought we can collect from the ancientest Celestial observations, remaining in all Ages invariable.

Every

Every Point in the Globe as it turns round upon its Axis describes a Circle in the Disk about the next Pole, which I call the *Path of the Vertex*, considering the said Point as Vertical to the Earths Center: its uses being the same with that we call the Zenith, or Vertex, in the *Ptolemaick* projections.

Imagin a great Circle compassing the Earth equally distant from both its Poles, this shall be the *Equator*, the distance of any place from it the *Latitude of that Place*, and therefore the *Semidiameter of the Path* equal to the *Complement of the Latitude*.

If a Circle be imagined to pass through any place in the Earths superficies, and the two Poles, on which it turns, that Circle shall be the *Meridian of that place*; and that part of it which lies from the said place towards the North Pole, will be the *North part of the Meridian*; toward the South Pole, the *South Part*.

That Point in the Earths Periphery opposite to the Sun, or lying in a straight Line produced through the Centers of the Sun and Earth, I call the *Suns place in the Ecliptick*. And now seeing we shall have no farther use of the great Orb at present, I shall wave the mention of it; and when I shall have shewed how the Meridian, and Path of any Vertex in the Globe may be projected, the Eye being supposed in the Southern Pole of the *Ecliptick*; I shall next shew how from this Point, Spherical Triangles will be formed, wherein there will be sufficient given for determining the usual requisites of the Sphere, by the known Resolutions of Trigonometry.

### SECTION III.

THE Meridians in those lesser projections of the Globe, which are placed in the Periphery of the Annual Orb in the first Figure, are described as the hour Circles in that Stereographical projection of the Sphere on the Plane of the Horizon, where the Latitude is equal to the Complement of the Distance of the two Poles of the Globe and *Ecliptick*; that is thus, make the Semidiameter of the Earths Disk equal to the Tangent of  $45^{\circ}$  Degrees, or Semitangent of  $90^{\circ}$ , and having drawn the Solstitial Colure, set off in it the Tangent of  $11^{\circ} 44' \frac{1}{2}$ , or Semitangent of  $23^{\circ} 29'$ , the distance of the Poles of the Globe and the *Ecliptick*, from the Center  $e$  to  $P$ ; that shall be the place of the Pole of the Globe.

Take the Tangent of  $66^{\circ} 31'$ , the Complement of the distance of the two Poles, and set it off likewise in the Solstitial Colure produced the contrary way, without the Disk, from  $e$  to  $T$ ; this shall be the Center of the first Meridian.

All the Meridians on the Earth pass through its Poles, extend therefore the Compasses from  $T$  to  $P$ , and through it strike the Arch  $\Upsilon P \approx$  in the third Figure; this shall represent the said first Meridian.

To



To find the Centers of all the rest, through T draw  $qTw$  at right Angles to the Solstitial Colure produced, and making TP the Radius of a Tangent Line, therewith divide the said Line both ways from T.

Fig. 3.

Count 15, 30, 45, 60, 75 Degrees in the said Line both ways from T, so have you the Centers of ten other Meridians, upon each of which, if you set one Foot of the Compasses, and extending the other to the Pole P, therewith describe Circles through it, these shall represent so many Meridians, each one hour distant from other, or the Hour-circles, the Earth being in the first Point of  $\Upsilon$  or  $\varpi$ , and viewing the Sun in the opposite Point.

The last of these  $\varpi P \Upsilon$  coincides with the Solstitial Colure, and is a straight Line, its Semidiameter the Tangent of 90 Degrees being infinite.

Every place or Point on the Globe, as I said before, describes a Circle about its Axis, which I call the *Path of the Vertex*: Let it be now required to delineate the Line, that London carried round the Axis describes on the Plane of the Ecliptick, to the Eye placed in its Southern Pole.

The distance of London from the Pole of the World is  $38^{\circ} 29'$ , and of the Pole of the World from the Pole of the Ecliptick  $23^{\circ} 29'$ : Let now in the third Figure  $\Upsilon \varpi \varpi \Upsilon$  represent the Periphery or Diske of the Earth lying in the Plane of the Ecliptick,  $e$  the Pole of the Ecliptick,  $\varpi P \Upsilon$  the Solstitial Colure,  $\Upsilon e \varpi$  the Equinoctial Colure, P the Pole of the Globe, set off in it according to the former directions.

To the distance of the Poles  $P e 23^{\circ} 29'$ , add  $38^{\circ} 29'$ , the distance of London from the North Pole of the Globe, the Sum  $61^{\circ} 58'$  is the greatest distance of London from the Pole of the Ecliptick.

Make the Radius of the Diske equal to the Tangent of 45 Degrees, or Semitangent of  $90^{\circ}$ ; and from the same Line of Tangents, set off the Tangent  $30^{\circ} 59'$ , or Semitangent of  $61^{\circ} 58'$  from  $e$  the Pole of the Ecliptick, towards  $\varpi$  to  $m$ , in that Point the Path shall cut the Colure; or counting the said  $61^{\circ} 58'$ , from  $\Upsilon$  towards  $\varpi$  to M, in the Ecliptick, lay a Ruler over the opposite Point  $\varpi$  and this Point M, it will cut the Colure in  $m$ , where the Path shall likewise intersect it.

Subtract the distance of the two Poles  $e P 23^{\circ} 29'$ , from the Complement of the Latitude  $38^{\circ} 29'$ , the Difference  $15^{\circ} 00'$ , is the nearest approach of the Path of the Vertex to the Pole of the Ecliptick.

From the forementioned Line of Semitangents, set off the said  $15^{\circ} 00'$  from  $e$  towards  $\Upsilon$ , to  $x$ , or counting the said distance from  $\Upsilon$  towards  $\varpi$  to X, lay a Ruler over X and  $\varpi$ , it will cut the Solstitial Colure in the said Point  $x$ , where it is intersected by the Path.

The Middle betwixt these Points  $m$  and  $x$ , shall be the Center, upon which if you strike a Circle through them, it shall be that Line I call the *Path of the Vertex*, or which London would appear to describe on the Plane of the Ecliptick, to the Eye placed in the Southern Pole, as the Earth turns round, if the Globe were diaphanous.

After

After this manner were the Paths described in the small Projections placed in the Periphery of the first Figure, of which the remotest represents one half of the Equator, or of the Paths of such places as lie under it, that within this, the Northern Tropick, or the intire Path of such places as lie in the Latitude of  $23^{\circ} 29'$  North: the next within this is the Path of London, or of any place equally distant from the North Pole of the Globe: the innermost, of such places as lie  $23^{\circ} 29'$  distant from the said Pole, which therefore we may call the *Arctic Circle*.

Whereby it will be easily conceived, why under the Equator the Days are equal at all times of the year; why the Days at the same time of the year are not of the same length in all places, why within the Arctic Circle they are sometimes longer than 24 hours, and at the opposite times of the year the Nights as long; but when the Earth transits the first Points of  $\varpi$  and  $\Upsilon$ , the Days and Nights are in all places equal.

For the Sun illuminates but one half of the Earths Globe by his Central Rays, and if the Earth be supposed at  $\varpi$  or  $\Upsilon$ , the Horizon of the Diske *red* coincides with the Solstitial Colure; and of all the Paths which can be projected within the Ecliptick, on the Globe, according to the foregoing precepts, the one half will fall in the illuminate, the other in the obscure part of the Diske. Now whilst the Vertex is traversing the illuminate part, it sees the Sun, and we call it *Day*; whilst it travels through the obscure, we see him not, tis *Night* to us; and since in both these positions of the Globe, the obscure parts of all the Paths, or the *Nocturnal Arches*, will be equal to the illuminate, or *Diurnal Arches*, the days must of necessity be equal to the Nights in all places.

Conceive the Globe to have moved from  $\varpi$  to  $\Upsilon$ , the Line of Direction, (keeping its parallelism to its self, and the great Solstitial Colure) now coincides with it, and the Rays of the Sun illuminating the Hemisphere; and the Horizon of the Diske stands at right Angles to it, on the Pole of the Ecliptick  $e$ : Here all places betwixt the two Poles of the Globe, and Ecliptick, or within the Arctic Circle, are illuminated in their whole Revolutions. Wherefore the Vertices see the Sun longer than 24 hours, more or less according as they are less or more distant from the Pole of the Globe, but those which lie under the Arctic Circle touch the Horizon of the Diske; and therefore at this time see the Sun, not only in the South, but also in the North part of the Meridian, 90 Degrees from the Vertex, or precisely in the Horizon, and as soon as he is past it, view him rising again.

All the Paths, without this, intersect the Horizon of the Diske; where the Day is made so much longer than the Night, as the part of the Path lying in the *Illuminate Hemisphere*, is more than that part of it which lies in the *obscure*:  $v z l$  represents the Path of London, in which the Vertex cuts the Horizon of the Diske, some little more than 8 hours before it transits the Meridian, or Line passing from the Pole to the Sun, and tis so long again ere it pass the Horizon into the obscure Hemisphere; thereby shewing the Day to be something longer than 16 hours, and therefore the Night at this time scarce eight.

Whilst



Whilst the Earth runs from  $\omega$  by  $\psi$  to  $\gamma$ , the *Northern Pole* will be always in the illuminate part of the *Diske*, thereby shewing that it is continual Day all that time under the said Pole, but whilst she runs from  $\gamma$  by  $\omega$  to  $\omega$ , it will lie in the obscure part, thereby shewing it continually Night in the same place; the South Pole in the mean time passing in the illuminate *Diske*, and enjoying the Day, as it did the Night continually whilst the North Pole was illuminate: So that under the Poles, the whole year consists but of one long Day, and Night.

When the Earth is at  $\omega$ , whence the Sun appears in  $\psi$ , the length of the Night will be equal to the length of the Day when the Earth was on the opposite Point; for the *Nocturnal Arch*, or obscure part of the Path, is here equal to the illuminate, or *Diurnal*, when the Globe was at  $\psi$ , and the illuminate here no more than the obscure in that place.

When the Earth is at  $\psi$ , the *Tropical Path* will just touch the *Ecliptick* in the Meridian, or that point of the illuminate *Diske*, which is directly opposite to the Sun, thereby shewing, that when ever the Earth arrives at that Point of her Orbit, the Meridional Sun will be vertical to all places in that Latitude of  $23^{\circ} 26'$  North, the length of the Day here appears by the Projection; for the illuminate part of the Path betwixt the Horizon and Meridian being something less than 7 hours, the intire Day must be something less than its double, or 14 hours, and therefore the Night above 10 hours.

But to those People who live upon the Equator, the one half of the Path will always fall in the illuminate part of the *Diske*, the other in the obscure; to whom therefore at all times of the year, the Days and Nights will be equal.

How the Paths lie that have the same Latitude South of the Equator, will be easily seen, if the first Figure be held before a Looking Glass, and its Picture viewed in it; or they may be projected *in plano*, if  $\omega$  be wrote where  $\psi$  is,  $\gamma$  where  $\omega$ , &c. in the great Orb, and the Pole of the World laid down on the contrary side, or to the right hand, from the Pole of the *Ecliptick*: I shall not need therefore to repeat any directions for this purpose, but only to shew how such further Lines as shall be found necessary for my business in hand, may be described, and how the common requisites of the Sphere may be investigated by them.

#### SECTION IV.

THE first thing supposed to be known in all Problems concerning the diurnal *Phænomena*, is the distance betwixt the two Poles of the Globe and *Ecliptick*; this I have before proposed  $23^{\circ} 29'$ . The next is the *Sun's* place, or the Longitude of the Point in the Earths *Diske* opposite to him, from the next Equinoctial Point. And these being given, the requisites demanded are of two sorts; General,

or



or Particular, the General are such as are the same to all the inhabitants of the Globe, at the same time, as

1. The distance of the Suns place from the North Pole of the Globe.
2. The right Ascension of the said place.
3. The Angle which the Meridian passing through it makes with the Ecliptick.

The Particular are such as are different at the same time in different Latitudes, such are the Amplitudes, and Ascensional Differences, &c. which require the knowledg of the  $\odot$ 's distance from the Pole, to limit them. I shall therefore first shew how the General requisites may be represented and determined, supposing the  $\odot$ 's place in 15 Degrees of  $\varpi$ , or 45 Degrees distant from the first Point of  $\gamma$ .

In the third Figure, let  $\gamma \varpi \alpha \psi$  represent the Ecliptick,  $e$  its Pole, Fig. 3.  $\varpi e \psi$  the Solstitial,  $\gamma e \alpha$  the Equinoctial Colure,  $P$  the North Pole of the Globe,  $\gamma P \alpha$  the first Meridian described, and  $q T a u$ , the Tangent Line passing through its Center, divided according to the Prescriptions of the foregoing Chapter.

Count 45 Degrees, the  $\odot$ 's distance from the Equinoctial, from  $\gamma$  towards  $\varpi$  to  $\odot$ , through which and the Pole of the Ecliptick  $e$ , draw the Line of the Sun's Longitude  $\odot e n$ , producing it till it intersect the Tangent Line in  $q$ .

Through  $e$  draw  $H e r$ , at right Angles to  $\odot e n$ , this shall be the Horizon of the Disk to this place of the Sun, beyond which produce it likewise, till it intersect the Tangent Line in  $w$ .

Setting one foot of the Compasses on  $w$ , extend the other to the Pole  $P$ , with this extent you may strike the Arch  $n P \odot$ , which shall intersect the Ecliptick on both sides, with the Line of Longitude in  $\odot$  and  $n$ , this shall be the Proper Meridian to the place of the Sun.

In like manner on the Center  $q$ , with the distance  $P q$ , you may strike the Arch  $H P r$ , which passing through the Pole shall intersect the Horizon of the Disk on both sides, where it cuts the Ecliptick; this shall cut the Proper Meridian at right Angles in the Pole, and is therefore the Six a Clock Hour-circle to that place of the Sun.

Conceive both the Colures, the First, and Proper Meridian, the Hour-circle of Six, together with the Path of the Vertex, and in General all the Lines hereafter to be described as a Fixed Rete, close investing the Earth whilst the turns round within them.

And now betwixt the Proper Meridian, the Ecliptick, and Solstitial Colure, we have formed the Spherical Triangle  $\varpi P \odot$ , right Angled at  $\varpi$ , wherein we have given  $\odot \varpi$ , the Complement of  $\gamma \odot$  the Sun's distance from the Equinoctial  $45^\circ 00'$ ;  $\varpi P$ , the Complement of  $P e$ , the distance of the Poles of the Globe and Ecliptick  $66^\circ 31'$ ; with the Angle at  $\varpi$  Right, to find, 1.  $P \odot$  the Sun's distance from the Pole, 2.  $\varpi P \odot$ , the Complement of  $\odot P \gamma$ , his right Ascension from  $\gamma$ , and 3.  $P \odot \varpi$ , the Angle of the Meridian passing by the Sun with the Ecliptick. For the first, or  $P \odot$ , by the demonstrated properties of Spherical Triangles, it will hold,

C

R



R .  $\epsilon$ s,  $\odot \mathcal{S} :: \epsilon s, \mathcal{S} P . \epsilon s, P \odot$ , or,

	$^{\circ}$	$'$	$''$	Log.	
As the Radius,	90	00	00	10,000000	
To the Sine of the two Poles Distance;	S.	23	29	00	9,600409
So the Sine of the $\odot$ 's Longitude from the Equinox.	45	00	00	9,849485	
To the Co-sine of his Distance from the next Pole:	73	38	03	9,449894	

Whose Complement  $P \mathcal{I}$ ,  $16^{\circ} 21' 57''$ , is the Distance of the North Pole from the Horizon of the Disk, or the Reflection equal to the  $\odot$ 's Declination in the Ptolemaick System.

The  $\odot$ 's right Ascension is that Angle at the Pole, which the proper Meridian  $\odot P$  forms with the first  $\Upsilon P$ , its Complement  $\odot P \mathcal{S}$  will be found in the aforementioned Triangle, by this proportion,

R .  $\epsilon$ s,  $\mathcal{S} P :: \epsilon s \mathcal{S} \odot . \epsilon s \odot P \mathcal{S}$ , wherefore it will hold,

As the Radius,	S.	90	00	00	10,000000
To the Co-sine of the Distance of the two Poles;	23	29	00	9,962453	
So the Tangent of the $\odot$ 's Longitude from the next Equinoctial Point,	45	00	00	10,000000	
To the Tangent of his right Ascension from the said Point :	42	31	35	9,962453	

If the Sun had appeared in the middle of  $\mathcal{S}$ , where he is equally distant from the first Point of  $\Upsilon$ , this Arch subtracted from 360, the right Ascension of the last Point of the Ecliptick, had given his right Ascension there  $317^{\circ} 28' 25''$ .

If he had appeared as far remote from the opposite Equinoctial Point, either in the middle of  $\mathcal{Q}$  or  $m$ , this Arch subtracted from 180 Degrees, the right Ascension of the opposite Point, had given  $137^{\circ} 28' 25''$  his right Ascension in the middle of  $\mathcal{Q}$ , added to 180, it would make  $222^{\circ} 31' 35''$ , the same in the middle of  $m$ .

After this manner by the right Ascensions calculated only to one Quadrant of the Ecliptick, the same may be made out to every Degree of the whole.

For finding the third of the General Requisites, or the Angle  $P \odot \mathcal{S}$ , which the proper Meridian makes with the Ecliptick, in the same Triangle we may say

5  $\odot R$

$\mathcal{S} \odot P . R :: t, \mathcal{S} P . t \mathcal{S} \odot P$  or,

As the Co-sine of the $\odot$ 's Longitude from $\Upsilon$ or $\mathcal{S}$ ,	45	00	00	9,849485
To a Radius;	90	00	00	10,000000
So the Co-tangent of the two Poles Distance,	23	29	00	10,362044
To the Tangent of the Angle of the Meridian and Ecliptick,	72	55	20	10,512559

## SECTION V.

Before any other requisites can be investigated, the Path of the Vertex Fig. 4 or place to which they are required must be described, which may be done according to the directions of the third Chapter; this for London will be in the third and fifth Figure the Circle  $x f m g$ , by whose intersections with the fix a Clock Hour-circle  $k a$ , and the Points  $\odot n$  strike two Arches of Circles, then to find the two first particular requisites, or,

The Suns distance from the Vertex at the hour of fix,  
The Suns Azimuth at the hour of fix,

In the Spherical Triangles  $P \odot k$ ,  $P \odot a$ , right Angled at  $P$ , are given  $P k = P a$ , the distance of the Pole from the Path, or the Complement of the Latitude  $38^{\circ} 30'$ ;  $P \odot$  the distance of the Sun from the Pole, found before  $73^{\circ} 38' 03''$ ; to find  $\odot k$ , or  $\odot a$ , the distance demanded, with  $P k \odot$  or  $P a \odot$ , the Azimuth of the Sun from the North at the said hour; for the side  $\odot k$  you may say,

R .  $\epsilon s P \odot :: \epsilon s P k . \epsilon s \odot k$ , or,

As the Radius,	S.	90	00	00	10,000000
To the Co-sine of the Latitude;	51	30	00	9,794149	
So the Sine of the Reflection,	16	21	57	9,449894	
To the Co-sine of the Suns Distance from the Vertex.	79	53	52	8,924403	

And for the  $\odot$ 's Azimuth at fix, or the Angle  $\odot k P$ ,

S,  $k P . R :: t, \odot P . t, \odot k P$ , or,

As the Co-sine of the Latitude,	51	30	00	9,794149	
To the Radius;	S.	90	00	00	10,000000
So the Tangent of the $\odot$ 's Distance from the Pole,	73	38	03	10,532143	
To the Tan. of his Azimuth from the North Merid.	79	38	23	10,137994	
	C 2			For	



For in what part of the Path soever the Vertex is found, that part of the Hour-Circle intercepted betwixt it and the Pole, is the *North part of the Meridian* in all North Latitudes; And therefore the Angle  $\angle Pk\odot$ , formed betwixt it and the Line passing from the Vertex to the Sun, shall be his *Azimuth from the North Meridian*.

## SECTION VI.

Therefore in what part of the Path soever it happens, that the Meridian shall be found to cut the Line passing from the Vertex to the Sun at right Angles, he appears due East, or West, or, as the *Ptolemaicks* would phrase it, on the Prime Vertical.

Fig. 4.

Let now two Arches of Circles  $\odot b n$ ,  $\odot l n$ , be strook so, as they may pass through the two intersections of the Line of Longitude, and the Ecliptick  $\odot n$ , and but just touch the Path on each side it; the Points of Contingence at  $b$  and  $l$ , shall be the places in the Path from whence Hour-Circles strook through the Pole, shall intersect the Circles passing by the Sun at right Angles, in which therefore he shall appear due East or West; and now we have formed another pair of Triangles, (see the 4 Figure)  $P l \odot P b \odot$ , in which we have sufficient given to determin

The Sun's distance from the Vertex when due East or West, and,

The time from Noon when he shall be so:

For in the said Triangles are given the Hypothenuſa  $\odot P$ , the Sun's distance from the Pole of the Globe as before  $73^{\circ} 38' 03''$ : the distance of the Pole from the Path  $P b$ , or  $P l$   $38^{\circ} 30' 00''$ : with the right Angles at  $b$  and  $l$ , to find  $\odot b$ , or  $\odot l$  the distance desired, or  $\odot P b = \odot P l$ , when he shall appear as required; for the first it will hold,

$$cs Pb . R :: cs \odot P . cs b \odot, \text{ or,}$$

As the Sine of the Latitude,	51 30 00	9,893544
To a Radius;	90 00 00	10,000000
So the Sine of the Reflection,	16 21 57	9,449894
To the Co-sine of the Sun's Distance from the Vertex when due East or West.	68 53 50	9,336350

And for the latter,

$$t, \odot P . t, P b :: R . cs \odot P b, \text{ or,}$$

As the Tangent of the $\odot$ Distance from the Pole,	73 38 03	10,532143
To the Co-Tangent of the Latitude;	51 30 00	9,900665
So is the Radius,	09 00 00	10,000000
To the Co-sine of the hour from Noon, when the Sun is due East or West.	76 29 28	9,368462

$$\text{Which is} = 05 05 58$$

S E C T.

## SECTION VII.

THE Motion of the Earths Rotation about its Axis, is as hath been said from West to East, and therefore the Sun is then said to *Rise*, when the Vertex passes that Point in the Path at  $a$ , where it cuts the Horizon of the Disk; to *Climinate*, when it crosses the Meridian betwixt him and the Pole at  $d$ ; and to *Set* when it passes over the other intersection of the Path and Horizon at  $g$ : Let the Arches of a pair of Hour-Circles be strook through the said intersection of the Path and Horizon, as likewise two others, through  $\odot n$ , and the said two Points; so shall there be two Triangles formed on each side the Meridian; that is,  $\odot P a, \odot P i$ , on the Oriental or ascending side,  $\odot P g, i P g$  on the occidental, in either of which we may find sufficient given, for determining the Sun's Azimuth, Rising or Setting, and the time he Rises or Sets from Noon: For in the larger Triangles  $\odot P g, \odot P a$ , are known,  $\odot P$  the Sun's distance from the Pole,  $P a = P g$ , the distance of the Pole from the Vertex, with the sides  $\odot a, \odot g$  Quadrants; to find  $P a$  or  $P g$  the Sun's Azimuth, in this case from the North Rising or Setting; and  $\odot P a$  or  $\odot P g$ , the time before or after Noon: But in this case because the Angles  $\odot P a, \odot P g$ , are obtuse, it may be more convenient to use the lesser Triangles, in which are given  $P i$ , the Reflection,  $P a = P g$ , as before, and the Angles at  $i$  right, to find  $P g i$ , or  $P a i$  (the Complements of  $\odot g i$  and  $\odot a i$ ) the Sun's Amplitudes Rising or Setting from the East or West: and  $i P a = i P g$ , the time of his Rising after, or Setting before Midnight; I shall make use of the oriental of these lesser Triangles, in which it will hold,

$$S, P g . R :: t, P i . s P g i, \text{ or,}$$

As the Co-sine of the Latitude,	51 30 00	9,794149
To the Radius;	S. 90 00 00	10,000000
So the Sine of the Reflection,	16 21 57	9,449894
To the Sine of the Amplitude.	26 54 45	9,655745

Whose Complement to a Quadrant  $63^{\circ} 05' 15''$  is the Sun's Azimuth, in this case from the North, but when the Pole is in the obscure Hemisphere, from the South Meridian, in his Rising or Setting.

For the Ascensional Difference, say,

$$t, P g . R :: t, P i . cs P g i, \text{ or,}$$

As the Co-Tangent of the Latitude,	51 30 00	9,900665
To the Tangent of the Reflection;	26 21 57	9,467856
So the Radius,	S. 90 00 00	10,000000
To the Sine of the Ascensional Difference	20 15 49	9,567251

Whole



Whole Complement  $69^{\circ} 44' 11''$  converted into time, gives the Suns Rising  $4h. 38' 57''$ , and therefore that time of his Setting at  $7h. 21' 03''$  Afternoon.

## SECTION VIII.

**T**HE Meridional Distance of the Sun from the Vertex, may be found only by comparing the Suns distance from the Pole of the Globe, with the distance of the Vertex from the same Pole: For the lesser of these Subtracted from the greater, will leave the Suns Meridional Distance from the Vertex.

But Note, that if the Suns Distance from the Pole, be less than the distance of the Path from it; whence the Vertex passes the Meridian, he will appear betwixt the Pole and it; that is, to the North of the Vertex in Northern, and to the South in Southern Latitudes.

But if the Suns distance from the Pole be bigger than the Paths distance from it, he crosses the Meridian to the South of the Vertex, in Northern Latitudes, and to the North in Southern.

And if the Sum of the Suns, and Paths distance from the Pole be less than  $90^{\circ}$  Degrees, he shall appear twice upon the Meridian in 24 hours, once above, and again after 12 hours beneath the Pole, the Difference of them being his distance from the Vertex to the South in Northern, to the North in Southern Latitudes; but their Sum, his remotest distance from the Vertex to the South, in Southern Latitudes; and to the North in Northern which frequently happens in those places, that lie betwixt the Arctick and Antarctick Circles, and their Poles.

Hence the Rules are easily made for finding the Latitude, the Suns distance from either of the Poles, and his Meridional distance from the Vertex being given: but this I suppose has been already shewn. If the Reader finds it otherways, or think me deficient in this Point, it may excuse me, when I have informed him, that I could not be permitted the sight of what has been already Printed, upon which account it is I forbear least I should only do what has been already done, and therefore needless.

Fig. 3.

In my third Figure, if according to these Rules, from the Suns distance from the Vertex  $\odot P 73^{\circ} 38' 03''$ , you subtract the distance of the Path from the Pole  $33^{\circ} 30' 00''$ , the residue  $39^{\circ} 08' 03''$ , shall be  $\odot d$ , the Suns Meridional distance from the Vertex at that time.

S E C T.

## SECTION IX.

**T**HE Suns distance from the Pole, together with the hour from Fig. 3. Noon being given, to find his distance from the Vertex in any given Latitude.

Let the hour proposed be Four before Noon, or Eight in the Morning, and the Suns distance from the Pole as before.

Having made  $P T$  the Radius of a Tangent Line, and therewith divided the Line  $q T w$  both ways from  $T$ , the Points  $q$  and  $w$  will be found to fall  $42^{\frac{1}{2}}$  Degrees of the same, on each side  $T$ .

The Center of the proper Meridian is at  $w$ , Count therefore  $60$  Degrees (= to 4 hours) in the divided Tangent Line from  $w$  towards  $q$ , the Center of the six a Clock Hour-Circle, these shall terminate at  $y$ , and there is the Center of that Hour-Circle; which if setting one Foot of the Compasses on  $y$ , you strike through  $P$ , it shall form an Angle of  $60$  Degrees with the Meridian, and the Point  $8$ , where it intersects the Path, shall be that place, the Vertex shall pass, at 8 a Clock in the Morning, or 4 hours before Noon.

Let the Arch of a Circle  $8 \odot$ , be struck through this Point and the Suns place, so as it may also pass through his opposite place  $n$ ; then to find what is required, in the Oblique Angled Triangle  $P \odot 8$ , are given  $\odot P 8$ , the hour or Angle at the Pole  $60^{\circ} 00' 00''$ , the distance of the Pole, and Path  $P 8, 38^{\circ} 30' 00''$ , with  $P \odot$  the distance of the Sun from the Pole  $73^{\circ} 38' 03''$ , to find  $\odot 8$  the required distance of the Vertex from the Sun: which will be gotten by the second Case of Oblique Spherical Triangles, for,

As the Radius,	S. 90 00 00	10,000000
To the Co-sine of the hour from Noon;	60 00 00	9,698070
So the Tangent of the Poles Distance from the Vertex,	38 30 00	9,900605
To the Tangent of first Segment.	21 41 19	9,959975

Which, because the Angle  $\odot P 8$  is acute, the hour proposed being less than Six hours from Noon, subtracted from the Suns distance from the Pole  $73^{\circ} 38' 03''$ , leaves the second Base or Segment  $51^{\circ} 56' 44''$ .

	Again,	
As the Co-sine of the first Segment,	21 41 19	Ar. Co. 9,031883
To the Co-sine of the second;	51 56 44	9,789870
So the Sine of the Latitude,	51 30 00	9,893544
To the Co-sine of the $\odot^s$ Distance from the Vertex.	58 43 26	9,715302

Note, that when the hour proposed is more than Six from Noon, the Perpendicular falls without the Triangle, and then you must add the Suns distance from the Pole, to the first Segment, to get the second.

S E C T.



## SECTION X.

THE converse of the preceding propositions is of more frequent use in *Astronomy*, and therefore I shall next shew how, The Latitude of the place, the Suns distance from the Pole, with his observed distance from the Vertex, being given, to find the Hour from Noon.

Fig. 3.

In the aforementioned Triangle  $\odot P 8$ , let  $\odot P$  represent the Suns distance from the Pole  $73^{\circ} 33' 03''$ ,  $P 8$ , the distance of the Pole from the Vertex, or Complement of the Latitude  $38^{\circ} 30' 00''$ , and  $\odot 8$  his distance from the Vertex before Noon,  $58^{\circ} 43' 26''$ ; we have three sides of an Oblique Angled Spherical Triangle given, and the Angle at  $P$  required; which may be obtained by the 11 Case of such Oblique Angled Triangles: Wherefore add the three *data* together, and from half their Sum subtract the Suns distance from the Vertex, reserving the difference, then say,

As the Radius,

To the Sine of the Suns Distance from the Pole;

So is the Co-sine of the Latitude,

To a fourth Sine.

And Again,

As the fourth Sine,

To the Sine of half the Sum of the given sides;

So is the Sine of the Difference reserved,

To a seventh Sine.

To which if you add the Radius, half that Sum will be the Co-sine of half the hour from Noon. I proposed

The Suns Distance from the Pole $P \odot$	73	38	03
The Complement of the Latitude $P 8$	38	30	00
The Suns Distance from the Vertex $\odot 8$	58	43	26
Sum	170	51	29
$\frac{1}{2}$ Sum	85	25	44 $\frac{1}{2}$
Subtract $\odot 8$	58	43	26
Difference	26	42	18 $\frac{1}{2}$

$R = S$ ,	90	00	00	10,000000
$\odot P S$ ,	73	38	03	9,982037
$P 8 S$ ,	38	30	00	9,794149
$S$ ,	4th. Arch			9,776186

Fourth

Fourth Arch <i>Ar. Co.</i>	0,223814
$S, \frac{1}{2}$ Sum	85 25 44 $\frac{1}{2}$ 9,998616
$S$ , Diff.	26 42 18 $\frac{1}{2}$ 9,652632
$\frac{1}{2}$ Sine $\div R$	9,875062
$\frac{1}{2}$ <i>cs</i>	30 00 00 9,937531

Doubled  $60^{\circ} 00' 00'' = 4$  hours, the time from Noon, or Eight in the Morning, at which the Suns distance from the Vertex, was found  $58^{\circ} 43' 26''$ , in the work of the last proceeding Case.

## SECTION XI.

THE Suns distance from the Pole, his distance from the Vertex, and the Latitude being given, if his Azimuth shall be required:

The case is the same with the preceding, for in the same Triangle  $\odot P 8$ ; are given the three sides  $P \odot$ ,  $P 8$ ,  $\odot 8$ , as before, only whereas we then enquired the Angle at the Pole  $P$ , we must now seek the Angle at the Vertex  $8$ , for that is the Suns Azimuth from the North part of the Meridian.

Add therefore as before the Suns distance from the Pole, his distance from the Vertex, and the Complement of the Latitude together, and from half that Sum subtract the Suns distance from the Pole, then say:

As the Radius,

To the sine of the Suns Distance from the Vertex;

So the Co-sine of the Latitude,

To a fourth sine.

And Again,

As that fourth sine,

To the sine of the half Sum;

So the sine of the Difference,

To a seventh sine.

To which if you add the Radius, half that Sum will be the Co-sine of half the Suns Azimuth from the North.

Let now the *data* be the same as in the last case, and the Suns Azimuth or the Angle at  $8$ , enquired.

D

The



The Complement of the Latitude P 8 is	38	30	00
The Suns Distance from the Vertex $\odot$ 8	58	43	26
From the Pole P $\odot$	73	38	03
Sum	150	51	29
$\frac{1}{2}$ Sum	85	25	44 $\frac{1}{2}$
The Suns distance from the Pole	73	38	03
Subtracted leaves the Difference	11	47	41 $\frac{1}{2}$
Rad. S,	50	00	00
8 $\odot$ , S,	58	43	26
P 8, S,	38	30	00
Fourth sine	9,725950		
Fourth sine	Ar. Comp.	0,274050	
$\frac{1}{2}$ Sum S,	85	25	44 $\frac{1}{2}$
Diff. S,	11	47	41 $\frac{1}{2}$
Z + R	19,583164		
$\frac{1}{2} = \text{cs}$	51	46	05
	9,791532		

Doubled 103 32 10 the Suns Azimuth from the North Meridian, or the Angle at 8 required, its Complement to a Semicircle 76 27 50", his Azimuth from the South.

## SECTION XII.

IF the end of the Twilight in the Evening, or the first dawn of the Day in the Morning, were required, it must be considered; that the Daylight reaches to the Horizon, when the Sun is 16 Degrees beneath it; or as the *Copernicans* had rather express it, the Vertex sees the light of the Sun until it be 16 Degrees distant from the Horizon of the Disk, in the obscure Hemisphere of the Earth. Count therefore 16 Degrees in the Periphery of the Ecliptick, from each of its intersections with the Horizon of the Disk, into the obscure Hemisphere; or from H to  $\gamma$ , and from  $r$  to  $e$ , then laying a Ruler over  $\gamma r$ , mark the Point  $x$  where it intersects the Line of the Suns Longitude.

The Tangent of 74 Degrees (the Complement of 16) to the Radius  $e \gamma$ , shall be the Semidiameter of a Circle, that shall pass through these three Points; of which if you strike the Arch  $\gamma me$  it shall be the *Parallel* of and *Twilight*, the Point  $\zeta$ , wherein it intersects the occidental part of the Path, shall be that place the Vertex transits, when the Twilight ends in the Evening.

Strike

## Sect. 12.

## of the SPHERE.

Strike the Arch of a Circle through this Point  $\zeta$ , so as it may also pass through the Sun, and his opposite place at  $n$ ; through the said Point and the Pole P, strike also the Arch of an Hour-Circle  $\zeta P$ , so have you formed the oblique Angled Triangle  $P \zeta \odot$ , in which are given  $P \zeta$  the Complement of the Latitude 38° 30',  $P \odot$  the Suns distance from the Pole 73° 38' 03", and  $\odot \zeta$ , the Suns distance from the Parallel, to find the Angle at P, or the hour from Noon, when the Twilight ends, which may be obtained by the 11 case of Spherical oblique Angled Triangles, thus,

Add together the Suns distance from the Pole, his distance from the Parallel, and the Complement of the Latitude; from the half of the Sum subtract the Suns distance from the Parallel, reserving the difference. Then say,

As the Radius,  
To the Co-sine of the Latitude;  
So is the sine of the Suns Distance from the Pole,  
To a fourth sine.

And Again,

As that fourth sine,  
To the sine of half the Sum of the sides;  
So is the sine of the Difference, reserved,  
To a seventh sine.

To which add the Radius; half the Sum shall be the Co-sine of half the hour from Noon.

For Example.

When the Suns Distance from the Pole is	73	38	03
Complement of the Latitude	38	30	00
The Parallel from the Sun	106	00	00
Sum	218	08	03
$\frac{1}{2}$ Sum	109	04	01 $\frac{1}{2}$
$\odot \zeta$ Sub.	106	00	00
Difference	3	04	01 $\frac{1}{2}$
S,	90	00	00
P $\zeta$ S,	38	30	00
P $\odot$ S,	73	38	02
S,	4th. Arch	9,776186	

D 2

Fourth



Fourth Arch,	<i>Ar. Comp.</i>	0,223814
$\frac{1}{2}$ Sum S,	109 04 01 $\frac{1}{2}$	9,975495
Difference 8,	3 04 01 $\frac{1}{2}$	8,728396
Z + Radius,		18,927705
$\frac{1}{2}$ <i>cs</i> ,	73 05 02	9,463852

Doubled makes 146 10 04 equal to 9 h. 44' 40", at which time the Twilight ends, and it becomes perfectly dark. Subtract these from 12 hours, the remainder 2 h. 15' 20", is the time of the first Day-break in the Morning, the Sun being in the same place in the Ecliptick; Note that where the Path cuts not the Parallel of Twilight, tis no perfect darkness at Midnight, but Twilight only lighter, or darker, as the Path approaches nearer the Parallel.

## SECTION XIII.

**I**N the Calculation of Solar Eclipses, and the Moon's Transits over fixed Stars, it is usually required to know what Point of the Ecliptick Culminates in the Meridian, what is the highest Point of it, and the nearest Distance of each of these from the Vertex, and what is the Angle which the Vertical Circle makes with the Ecliptick, in any Point of it, at any given time. These are difficultly shewn in the Ptolemaick Projections, readily and easily in ours; thereby proving that the most ingenious of human inventions, are far less facile than the ordinary performances of Truth and Nature: I shall therefore next shew how each of these may be represented in the true System of the World, and calculated.

Let the Sun's place be as before proposed, and the forementioned requisites demanded to 2 h. Afternoon.

The Center of the proper Meridian is at w, Count 30 Degrees answering to 2 hours in the Tangent Line divided as before directed, from w to the right hand, an Hour-Circle struck with one Point of the Compasses set on the Point so found in the Tangent Line, through the Pole P, shall cut the Path in the Point  $\theta$ , which the Vertex shall traverse at 2 hours after Noon, the Ecliptick upon the Point C on the Meridian, and a Line produced through the Pole, *e* and the intersection of the Path, and this Arch at  $\theta$ , shall intersect the Ecliptick in the Nonagesime degree, or Point nearest the Vertex at N, C N being the distance of the Nonagesime degree from the Meridian, N its distance from the Vertex, and C  $\theta$  the distance of the Point on the Meridian from the Vertex.

To

To define these by Calculation.

In the Triangle C  $\theta$  P are given,  $\theta$  P, the Complement of  $\gamma$  P  $\theta$ , the right Ascension of the Midheaven or Point of the Ecliptick in the Meridian 17° 28' 25", P  $\theta$  as before 66° 31', and the right Angle at  $\theta$ , to find  $\theta$  C the Complement of  $\gamma$  C, the Longitude of the Midheaven from the first Point of the Ecliptick, and P C, the distance of the Midheaven from the Vertex, we may say, therefore,

R . *t*,  $\theta$  P C :: *s*, P  $\theta$  . *t* P C, that is,

As the Radius,	S. 90 00 00	10,000000
To the Co-tangent of the right Ascension of the Midheaven;	72 31 35	9,498024
So the sine of the Distance of the Pole and Tropick,	66 31 00	9,962453
To the Co-tangent of the Longitude of the Midheaven from the next Equinoctial Point.	73 53 45	9,460477

Therefore the Midheaven is  $\pi$  13° 53' 45"; for P C it will hold,

\* R . *cs*,  $\theta$  P C :: *t*,  $\theta$  P . *t* C P, or,

As the Radius,	S. 90 00 00	10,000000
To the Tangent of the Distance of the two Poles;	23 29 00	9,637956
So the sine of the right Ascension of the Midheaven,	72 31 35	9,979453
To the Co-tangent of its Distance from the next Pole.	67 29 24	9,617439

From which if according to the directions of the Eighth Section, we take away P  $\theta$  38° 30', the distance of the Pole from the Vertex, the remainder  $\theta$  C shall be the distance of the Midheaven from the Vertex, 28° 59' 24".

To find N  $\theta$ , the Complement of  $\gamma$  N, the Longitude of the Nonagesime, with N  $\theta$  its distance from the Vertex; in the Oblique Angled Triangle, P  $\theta$   $\theta$ , are given P  $\theta$  the distance of the two Poles 23° 29', P  $\theta$  the Complement of the Latitude, or Semidiameter of the Path 38° 30', with the included Angle  $\theta$  P  $\theta$ , the difference of the right Ascensions of the Midheaven, and first Point of  $\gamma$  162° 31' 35", to find the Angle P  $\theta$   $\theta$  =  $\theta$  N, the Longitude of the Nonagesime from the first Point of  $\theta$ , with  $\theta$  N, its distance from the Vertex, which may be obtained by the Second and Tenth Cases of Oblique Angled Spherical Triangles, for,

As



As the Radius,	90 00 00	10,000000
To the Co-tangent of the Latitude;	51 30 00	9,900605
So the sine of the right Ascension of the Midheaven	72 31 35	9,979+83
counted from $\gamma$ or $\pi$ ,		
To the Tangent of the first Segment.	37 11 20	9,880038

If the Angle  $\epsilon P\theta$  be obtuse, as in this Case, the Sum of the first Segment and the distance of the two Poles; but if it be acute, their difference, shall be the second Segment.

In this Case therefore the second Segment will be  $60^\circ 40' 20''$ .

Say Again,

As the sine of the second Segment;	60 40 20	Ar.C.0,059567
To the sine of the first;	37 11 20	9,781356
So the Co-sine of the right Ascension of the Midheaven from $\gamma$ or $\pi$ ,	62 31 35	9,498024
To the Co-sine of its Longitude.	77 41 18	9,338947

Therefore the Nonagesime  $\pi$   $17^\circ 41' 18''$ , for its distance from the Vertex, say,

As the Co-sine of the first Segment,	37 11 20	Ar.C.0,098734
To the Co-sine of the second Segment;	60 40 20	9,893544
So the Co-sine of the Latitude,	51 30 00	0,550023
To the sine of its Vertical Distance.	28 45 43	0,682301

Whose Complement  $61^\circ 14' 17''$ , is its Distance from the Horizon.

If it be demanded, what Angle the Circle passing from the Vertex to the Sun, makes with the Ecliptick at his Center, strike a Circle through the Sun, his opposite place  $n$ , and the Vertex; So shall you form the Triangle  $\theta N \odot$ , in which are given  $N \odot$  the Suns distance from the Nonagesime  $32^\circ 41' 18''$ ,  $N\theta$  the distance of the Nonagesime from the Vertex, and the Angle at  $N$  right, to find the Parallacltick, or required Angle, you may say therefore,

$$S, N \odot . R :: t, N \theta . t N \odot \theta, \pi,$$

As the sine of the $\odot$ Distance from the Nonagesime,	32 41 18	9,732449
To the Radius;	90 00 00	10,000000
So the Tangent of the Distance from the Vertex	28 45 43	9,739485
To the Tangent of the Parallacltick Angle.	45 27 31	10,007036

But

But if the Parallacltick Angle at the Moon, or some Star that has Latitude from the Ecliptick, be demanded; it will require some farther labour to investigate it. Let the time proposed, and consequently the Nonagesime Degree, and the distance of the Vertex from the Pole be as before found, and let the Parallacltick Angle at *Pollux*, whose Longitude is  $18^\circ 47' 30''$ , distance from the Pole of the Ecliptick  $83^\circ 21' 30''$ , be demanded: Let  $\ast$  represent the place of *Pollux*, the Arch  $NV$  equal to the Angle  $\theta \epsilon \ast$ , the difference of the Longitude of *Pollux* and the Nonagesime, shall be  $31^\circ 06' 12''$ : Strike the Arch of a great Circle  $\ast \theta$  from the Vertex to *Pollux*, so have you formed the Oblique Angled Spherical Triangle,  $\ast P \theta$ , in which are known  $\epsilon \theta$ , the distance of the Vertex from the Pole of the Ecliptick  $61^\circ 14' 17''$ , with  $\epsilon \ast$  the distance of *Pollux* from the Pole of the Ecliptick  $83^\circ 21' 30''$ , and the Angle  $\theta \epsilon \ast$  as before; to find the Angle  $\epsilon \ast \theta$ , the Complement of the Parallacltick Angle, with  $\theta \ast$  the distance of the Star from the Vertex, which will be given by the second and tenth Cases of Oblique Angled Spherical Triangles, by which it will hold:

As the Radius,	90 00 00	10,000000
To the Co-sine of the $\ast$ Distance from the Nonagesime;	31 06 12	9,932594
So the Tangent of the Distance of the Vertex from the Pole of the Ecliptick,	61 14 17	10,260515
To the Tangent of the first Segment.	57 20 17	10,193109

The difference betwixt the first Segment, and the Stars distance from the Pole of the Ecliptick, shall be the second Segment in this Case  $26^\circ 01' 13''$ .

Say Again,

As the sine of the second Segment,	26 01 13	Ar.C.0,357843
To the sine of the first;	57 20 17	9,925245
So is the Tangent of the $\ast$ Distance from the Nonagesime Degree,	31 06 12	9,780546
To the Co-tangent of the Parallacltick Angle.	40 49 02	10,063634

And for the Stars distance from the Vertex,

As the Co-sine of the first Segment,	57 20 17	Ar.C.0,267863
To the Co-sine of the second Segment;	26 01 13	9,955385
So the Co-sine of the Distance of the Vertex from the Pole of the Ecliptick,	61 14 17	9,682316
To the Co-sine of the $\ast$ Distance from the Vertex.	36 45 04	9,903764

SECT.



## SECTION XIV.

However large the Diameter of the Earths Annual Orb may appear to be, collated with her own Diameter, yet if it be compared with the vast distance at which the fixed Stars are placed, the Angle it subtends becomes almost insensible. So that in what part forever of her Orbit the Earth is found, she is yet conceived by Copernicans as in the Center of the starry Sphere; and then lines produced from her Center to each Star shall design their places in that Rete, which we before imagined to invest its superficies; and their Longitudes and right Ascensions, will be determined by their respect to the Equinoctial Point, and Colure; their Latitudes by their distances from the Ecliptick; and their Declinations, by the like distances from the Circle bisecting the Globe, equally distant from both its Poles, called the *Equator*.

The distances and positions of the fixed Stars one from another, have been found the same in all Ages; so that it is probable they are subject to no Motion, but what appears in them by reason of the continual recess of the Earths Equinoctial Points; the manner and reason whereof, will be conceived by the first Figure; In which view the Earth at  $\oplus$ , its Motion round its Axis is from West to East, or from  $d$  by  $i$  to  $t$  in the illuminate part of the Globe, or that next the Sun. But the Motion of the Ætherial Matter is also from West to East, or from  $a$  to  $g$  directly contrary to this in the same illuminate part of the Globe, and that too something stronger than in the remoter or obscure part; by reason the parts near the Sun are swifter moved than the more remote; thence it proceeds that the *Line of Direction*, or Plane connecting the Poles  $t$   $P$   $e$   $d$ , is reflected and born back contrary to the Earths, and *Vortex Motion*, 50 Seconds Annually. So that whereas about the beginning of *Nabonassar's Era*, it cut the Ecliptick, and consequently made the Solstice, near the Cloudy place in  $\oplus$ , it is now carried back to the Heel of *Castor*, and about 250 years hence, it will make the Solstice when the Earth passes under *Propus*.

That Point of the Orbit, where when the Earth arrives, the Line of direction, or Solstitial Colure, coincides with the Horizon of the Diske, and the North Pole, passing out of the obscure, begins to enter the illuminate part of the Globe, is the place where the vernal Equinox is made, and the Sun enters the first Point of  $\gamma$ . This Point about the time of *Nabonassar*, was at  $N$ , but since by the continual impression of the Ætherial matter, and its renitency to the Earths Motion, tis reflected equally with the Solstitial Colure, which is altered from *nea* to *red* receding continually, so that if the Earth continue some Ages longer, the Equinoctials may happen under those Stars, near which the Solstices were celebrated at the Creation.

Hence

Hence it is that the places of the Equinoxes receding from the fixed Stars, they seem to move slowly, but equally forward from the Equinoxes, about one Degree in 72 years; those which appeared near the Equinoctial Points, or some few Degrees in Antecedence, as *Spica*  $\mu$  did in the time of *Hipparchus*, being now found near 20 Degrees in consequence of them.

But though the Longitudes of the Stars alter yearly, yet may their places once determined to a known year, be made out to any other, past or to come, by the sole Subtraction or Addition of so many times 50 Seconds from or to the given Longitude, as there are years betwixt that to which the place of the Star given is rectified, and at which it is demanded. Their Latitudes vary not, but their right Ascensions and Declinations depending on these, are continually changing, and that not regularly, but unequally, more or less according to the distances of each Star from the Pole of the Ecliptick, and the Colures. It will be therefore requisite to shew how from the given Longitude and Latitude of a Star, its right Ascension and Declination may be Calculated.

Let the Star proposed be *Pollux*, whose place to this year 1680. is stated  $\oplus$   $18^{\circ} 47'$ , and let its place, right Ascension, and Declination, be required to the year 1800. or 120 years hence.

To its given place 1680,	$\oplus$ 18 47 30
Add the Motion for 120 years future;	1 40 00
It makes the Stars place to the year 1800, in	$\oplus$ 20 27 30
Its constant Distance from the Pole of the Ecliptick being.	} 83 21 30

Let  $\star$  represent the place of *Pollux* on the Globe,  $e \star$  his distance from the Pole of the Ecliptick  $83^{\circ} 21' 30''$ ; and  $P e \star$  his Longitude from the Solstitial Colures  $20^{\circ} 27' 30''$ ,  $P e$ , the distance of the two Poles  $23^{\circ} 29'$ ; we have here two sides of an Oblique Angled Spherical Triangle given, with the Angle betwixt them, to find the third side, and the Angle at  $P$ , which will be got by the Second and Tenth Cases of such Triangles, by these proportions.

As the Radius,	$S$ . 90 00 00	10,000000
To the Tangent of the Stars Distance from the Pole of the Ecliptick;	} 83 21 30	10,933894
So the Co-sine of its Longitude from the Solstitial Colure,	} 20 27 30	9,971708
To the Tangent of the first Segment.	82 54 56	10,905599

When the Stars place is in the first six Signs of the Ecliptick, as in this Case, the difference betwixt the first Segment, and the distance betwixt the two Poles, shall be the second Segment; otherways their Sum shall make it.

E

The



The second Segment therefore in Pollux,  $59^{\circ} 25' 56''$ .

Say Again,

As the sine of the second Segment,	59	25	56	Ar.C.o,064983	
To the sine of the first Segment;	82	54	56	9,996672	
So the Tangent of the Stars Longitude from the	}	20	27	30	9,571774
next Solstitial Colure,					
To the Tangent of its right Ascension from the	}	23	15	57	9,633429
same Colure.					

The right Ascension of the Colure is  $90^{\circ}$ ; therefore of Pollux to the year 1800. will be  $113^{\circ} 15' 57''$ . For its distance from the Pole of the Globe, say,

As the Co-sine of the first Segment,	82	54	56	Ar.C.o,908924	
To the Co-sine of the second Segment;	59	25	56	9,706339	
So the Co-sine of the Stars Distance from the Pole of	}	83	21	30	9,063181
the Ecliptick,		28	29	04	9,678444
To the sine of its Declination.					

Whose Complement  $61^{\circ} 30' 56''$ , is its Distance from the North Pole of the Globe.

If the Angle  $P * e$ , or the visible inclination of the Axis of the Globe to the Axis of the Ecliptick be demanded, it will hold,

As the sine of the Stars Distance from the Pole	}	83	21	30	Ar.C.o,002925
of the Ecliptick,		23	15	57	9,596595
To the sine of its right Ascension from the Colure;					
So the sine of the Distance of the Poles,					9,600409
To the sine of the Inclination.					09 07 04 9,199929

I might here proceed to shew how several other requisites in the Sphæra would be formed and represented in this Projection, but it will be convenient to leave something imperfect, to exercise the Ingenuity of the Student; who if he thoroughly understand the preceding discourse, will readily find places wherein any other Problem will be determined. I shall therefore close this part, and in the following I shall shew how by a like, but Orthographical Projection of the Globe, the Moons Appulses to the Sun or Stars may be constructed, and all the Appearances of an Eclipse, Occultation or Transit represented to the Eye for several Latitudes in one Figure; which will be of great use to the Ingenious Astronomer, Traveller, and Seaman, and was never to be expected from any Hypothesis, that did not admit the Motion of the Earth.

T H E



If both these shall be of the same Denomination, that is both to be added or both to be subtracted, their Sum, but if otherways, their Difference shall be the *Absolute Equation of Time*, which according to the Quality of the greater part ought to have been added or subtracted from the apparent time, if given, that so the Calculation might have been fitted to the Mean, as the Numbers require.

But since the Equation of Days could not be found without the Mean Anomalie and Suns place, these being attained we must seek a Correction. Enter therefore the Seventeenth Table with the Mean Anomalie, and against it in the Column entituled the *Earths true horary Motion*, take out the true hourly Motion of the Earth, then say,

As one hour or 60 Minutes, to the hourly Motion: So the absolute Equation of time, to the Proportional Correction.

Which if the Absolute Equation of Days were Additional, added to, otherways subtracted from the Suns place first found, gives his true place to the time proposed.

The following Example will explain these precepts; Let it be required to find the Suns true place in the year 1668; *October* the 25th. at 1 h. 5' 30", apparent time under the Meridian of *London*.

The year proposed is Leap-year, therefore I take the Mean Motion belonging to the 26th. of *October*, for the 25th. and the Calculation stands as follows.

	Mean Motion.				Perihelion.			
	s	o	'	"	s	o	'	"
1661	09	20	25	46	03	06	35	00
7	11	29	18	48			5	50
<i>October</i> 25th. Bissext.	09	24	42	30				41
1 Hour			2	28	03	06	41	31
5 Minutes				12	07	14	29	45
30 Seconds				1	04	07	48	14
Mean Motion	07	14	29	45	With the Earths Mean Ano. sub. 6' 8"			
Equation subtracted			1	32	Suns place			
Suns place	07	12	57	44	Absolute Equation of Days sub. 15 59			
Parts proport. sub.				40	Suns horary Motion			
Suns correct place	07	12	57	04	Parts proportional subtract			

To Calculate the Moons true place at all times.

1. To the given time get the Suns true place and Equation of Days, according to the preceding directions, this added to, or subtracted from the apparent time, gives the true mean time.



2. In the Seventh Table seek the given year, if you find it not, write down the next less therein, with the Residue of years to the given, the Month, and day together, with the hour, Minute, and Seconds; and the several Mean Motions, and places of the Apogee and Node against them, as in the following Example.

3. Collect the Sum of the Moons Mean Motions, as also of her Apogee severally, but for her Node, draw a Line under the Radical place to the year first found, and adding the Motions under it into one Sum, subtract that from the Radical place, to have you the Mean Motions of the Moon, her Apogee, and Node.

4. With the Suns Mean Anomalie enter the Tenth Table, Entitled *A Table of Physical Parts*; and thence take out the Physical parts, standing against it, then according to their Title added to or subtracted from the Moons Mean Motion, give her *Mean Motion correct*.

5. From the Suns true place subtract the Mean Motion of the Apogee, the Residue I call the *Annual Argument*; with which entering the Eleventh Table take thence the Equation of the Apogee; this according to its Title added to or subtracted from the *Mean* place of the Apogee gives the true: In the same Table also with the Annual Argument take out the *Excentricitie*, which if it be less than the Mean (55237) subtract from it, if bigger take the Mean out of it, and note the difference.

6. From the Mean Motion of the Moon correct, subtract the true place of the Apogee, the remainder is the *Mean Anomalie*; with which entering the Twelfth Table Entitled, *A Table of the Equations of the Moons Center*, take the Equation answering to it under the middle *Excentricitie*, as also, if the true *Excentricitie* were more than the Mean, under the greatest, if less, under the least; Note their difference, then say, As 11617  $\frac{1}{2}$ , to this difference: So the difference of the middle and true *Excentricities*, to the part proportional. This if the true *Excentricitie* were greater than the middle, added to the Equation found under it, otherways subtracted from it, leaves the *true Equation of the Orbit*, which according to its Title, added to, or subtracted from the Moons correct mean Motion, gives her *Equated place*.

7. From the Moons *Equated place*, subtract the Suns; and with the difference in the Thirteenth Table, find the *Variation*, this according to its Title added to, or subtracted from the Moon's *Equated place*, leaves her *true place in her Orbit*.

8. From the Suns true place subtract the Mean Motion of the Node, the remainder is the *distance of the Sun from the Node*, with which entering the Fourteenth Table, take out the *Equation of the Node*, this according to its Title added to, or subtracted from its Mean Motion, makes its *true place*. In the same Table also find the *inclination of the Limit above 5 degrees*, or the greatest Latitude of the Moons Orbit at that time.

9. From the Moons true place in her Orbit, subtract the true place of the Node, what remains is the *Argument of Latitude*, with which entering the Sixteenth Table find the *Reduction with the Excess*; then say, As 18°, to the Excess; So the inclination of the Limit, or Excess of the Moons greatest Latitude

*Latitude above 5 Degrees, to the part proportional*; which added to the simple *Reduction* makes the true, and this according to its Title added to, or subtracted from the Moons true place in her Orbit, gives her *true place in the Ecliptick*.

10. For her true Latitude, enter the Fifteenth Table with the Argument of Latitude, and therein find the Moons simple Latitude, with the Excess or Increment, when the Inclination of its Orbit is 5° 18'; then say, As 18' is to the Increment; So the Excess or Inclination of the Orbit above 5 Degrees, to the part Proportional; which added to her simple Latitude, makes the true.

Or having the Argument of Latitude, and the Inclination of the Moons Orbit; the Reduction and her present Latitude may be found perhaps more easily by these proportions.

As the Radius,  
To the Co-sine of the Inclination of her Orbit;  
So the Tangent of the Argument of Latitude,  
To the Tangent of her Longitude from the Node in the Ecliptick;

Whole difference from the Argument of Latitude shall be the Reduction, which if the Argument of Latitude were in the first or third Quadrants, subtracted, otherways added to the Moons place in her Orbit, makes her place in the Ecliptick. For her Latitude,

As the Radius,  
To the sine of the true Inclination of her Orbit;  
So the sine of the Argument of Latitude,  
To the sine of her true Latitude.

To find the Moons Horizontal Parallax, and Semidiameter at all times, with her true horary Motion at the Conjunction with or Opposition to the Sun.

In the Seventeenth Table you have given the Moons true horary Motions in Eclipses, with her Horizontal Parallaxes, and Semidiameters, under the least and greatest Excentricities, to every 6 Degrees of Mean Anomaly, noted in the outside Columns of the Table, by the sixth precept foregoing you may find the Excentricitie, from which subtract the least, and note their difference.

Then if the Moons true horary Motion were demanded, enter the said Table with the Mean Anomaly, and in the Columns of horary Motions take out the horary Motions answering to it under each Excentricitie; note their difference, then say, As 23235, (the difference of the least and greatest Excentricities) to the difference of the horary Motions found; So the difference noted betwixt the present and least Excentricitie to the part proportional; which if the horary Motion under the least Excentricitie, were less than that found under the greater, added to the Motion under the least, otherways subtracted from it, makes the hourly Motion of the Moon from the Sun, at the time of the Conjunction or opposition. After the same manner would the Horizontal Parallax, and Semidiameter be obtained, if demanded, and therefore I need not give any farther directions for finding them. To



To explain these precepts by an Example, let it be proposed to find the Moons true place and Latitude, her Horizontal Parallax and Semidiameter, in the present year 1680. on the 22th. of December, at 6 h. 30<sup>m</sup> time apparent Afternoon under the Meridian of London.

The Suns Mean Anomaly will then be  $6^{\circ} 5^{\circ} 7' \frac{1}{2}$ ; his true correct place  $12^{\circ} 09' 35''$ ; therefore the Equation of time  $4' 57''$  to be added to the apparent, which makes the true Mean time 6 h. 34' 57" p m; to which according to the preceding Directions I collect the Mean Motions, and Equations, as follows,

	Mean Motion.	Apoge.	Node Retrog.	
	s o i "	s o i "	s o i "	
1661	01 18 10 14	5 00 21 51	6 21 04 47	Radical place of the Node.
December 19	11 21 00 07	1 23 03 29	0 07 27 20	
22 <sup>B</sup>	2 58 22	09 46 22	18 54 19	
h. 6	3 17 39	1 40	4	
34	18 40	10	5	
" 57	31	3 03 13 32	0 26 22 32	Motion of the $\Omega$ from the Radix.
Mean Motion	02 06 45 33	9 12 09 35	5 24 42 15	$\Omega$ true place.
Physical parts sub	1 03	08 55 03	Annual Argument.	
Mean Motion Cor.	02 06 44 30	10 50 32	Equat. of the Apoge add.	
Apoge	08 14 04 04	8 14 04 04	True place of the Apoge.	
Mean Anomaly	05 22 40 26	Ex. 57678	Equat. under the	Greatest Excen. 01 03 52
Equation subtract	54 22	M. Ex. 55237		Mean Excenter 00 51 51
Equation place	02 05 05 05	Dir. 2441		Part propo. add 00 02 31
Suns	9 12 09 35			Absolute Equat. 00 54 22
from the Sun	04 23 40 33	$\Omega$ Mean pla.	5 24 42 15	R.C.S. 5 01 36 9,995327
Variation subtract	36 16	Suns	9 12 09 35	t. 71 29 22 10,475214
from the Orb	02 05 13 52	from the $\Omega$	3 17 27 20	t. 71 25 22 10,473541
Node	05 23 44 30	Equat. $\Omega$ sub.	57 45	Red. sub. 4 00
Argument of Lat.	05 11 29 22	$\Omega$ true place	5 23 44 30	R.S. 5 01 36 8,942600
Reduction Subtra.	4 00	In. of the Orb	5 01 36	s. 71 29 22 9,976930
place in the Eclip	05 09 52			s. 4 45 58 8,919530
Latitude South	04 45 5			
Moons Horiz. Paral	61 31	Hence the M. true place is $\Pi$ 5 09 52		
Horizontal Semid.	16 4	Latitude South 4 45 58		

The place of the Bulls South Eye is at this time  $\Pi$   $5^{\circ} 19'$ , its Latitude South  $5^{\circ} 30'$ : So that the Moon may cover it in several places of the Earth, how the application to it will appear in our or any other Horizon I shall shew hereafter; at present it will be necessary to direct you how to find the time of the true Conjunctions or Oppositions of the Luminaries, and to Construct their Eclipses; after which, the Construction of Appulses will be easie.

S E C T.

## SECTION IV.

To find the time of the Mean Conjunction or Opposition of the Sun and Moon.

**T**O the Year and Month in which the Mean Conjunction or Opposition of the Luminaries is required, in the Twentieth Table, Entitled, *A Table of the Mean Motions of the Moon from the Sun*, Collect the middle Motions of the Moon from the Sun; take the Complement of this to 12 Signes, and from it or the Opposition (which if required, may be made by the Addition of 6 Signes to it) continually subtracting the nearest lesser Mean Motions, the answerable Days, Hours, Minutes, and Seconds; will shew the time of the Mean Conjunction or Opposition of the Sun and Moon.

For Example.

I desire to know the time of the Mean Conjunction or New Moon which will happen in July 1684.

	Moon from the Sun.			
	s	o	i	"
1681	08	11	09	13
3	00	28	52	07
July	01	16	31	32
Motion of the $\Omega$ from the Sun	10	26	32	52
Complement	01	03	27	08
Days 2	00	24	22	53
Hours 17	00	09	04	15
	00	08	38	06
Minutes 51	00	00	26	09
	00	00	25	54
Seconds 29	00	00	00	15

Therefore the Mean time of the Mean Conjunction of the Luminaries in July 1684. will happen July the first at 17 h. 51' 29" Afternoon, for the given year is Leap-year.

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To find the time of the true Conjunction or Opposition of the Sun or Moon.

1. To the time of the *Mean Conjunction* or *Opposition* Calculate the true Longitude of the Sun from the Vernal Equinox, and of the Moon in her Orbit by the Directions of the last foregoing Section: If these be found exactly the same, or Opposite, the times of the *Mean and true Conjunction and Opposition are the same*, but if, as commonly it happens, they differ, then,

2. Note the difference, and with the Mean Anomalies of the Sun and Moon, (the Moons being first Corrected by the Addition or Subtraction of about half so much as she wants of, or is past the  $\odot$  or  $\oslash$ ) enter the Seventeenth Table, Entitled, *A Table of the Moons true hourly Motions*, &c. and in the second Column take out the Earths, by the third and fourth, get the Moons true hourly Motions, subtract the Earths from the Moons,

Then say,

*As the Difference of the true hourly Motions,  
Is to one Hour, or 60 Minutes of time;  
So is the Moons Distance from the  $\odot$  or  $\oslash$  of the Sun,  
To the Interval of time betwixt the Mean and true  $\odot$  or  $\oslash$ , which is always less than 14 Hours.*

If the Moon were found to want of the *Conjunction* or *Opposition* of the Sun, the Interval added, but if she was past either of them, subtracted from the time of the Mean  $\odot$  or  $\oslash$ , makes the *Mean or equal time of the true*; to which time again for greater certainty, compute the true places of the Sun, and  $\textcircled{M}$  in her Orbit, with the Moons Latitude, and the exact Mean time of the true  $\odot$  or  $\oslash$ , being found.

3. With the Suns Mean Anomalie, and true place, enter the first and second Tables, and thence take the *Equation of Natural days* according to the precepts of the last Section; this, if it were to have been added to the Apparent time, subtracted here; but if to have been subtracted, added to the Mean time of the true  $\odot$  or  $\oslash$ , makes the Apparent time of either in the Moons Orbit.

4. Enter the Nineteenth Table with the Moons true hourly Motion from the Earth, in the head, and the Argument of Latitude in the side, against them in the common Area you have the time of Reduction, which according to its Title added to, or subtracted from the Apparent time of the  $\odot$  or  $\oslash$  in the Orbit, leaves the Apparent time of the *nearest approach of the Moons Center, to the Center of the Disk in Solar shadow in Lunar Eclipses*.

But if the same contrary to its Title be added to, or subtracted from the Apparent time of the true  $\odot$  or  $\oslash$  in the Orbit, it makes the Apparent time of the true Conjunction or Opposition in the Ecliptick.

Example.

Example.

1684. The Mean Conjunction of the Sun and Moon? <sup>h m s</sup>  
July the first . . . . . } 17 51 29

The Earths Mean Anomalie then . . . . . } 00 14 03 37  
The Annual Argument . . . . . } 02 23 51 16  
The Moons Mean Anomalie . . . . . } 02 20 14 44

The Suns true place . . . . . } 20 30 50  
The Moons in her Orbit . . . . . } 16 00 46  
The Moon short of the Conjunction . . . . . } 00 04 30 04

The  $\textcircled{M}$ s hourly Motion (to  $2^{\circ} 22^{\frac{1}{2}}$  of Anom.) . . . . . } 33 00  
Suns true hourly Motion . . . . . } 02 23  
 $\textcircled{M}$ s true hourly Motion from the Sun . . . . . } 30 37

Interval add . . . . . } <sup>h m s</sup> 08 48 46  
Mean time of the true Conjunction in the }  
Orbit, July the second . . . . . } 02 46 15

At which time,

The Suns true place is . . . . . } 20 51 52  
The Moons Mean Anomalie . . . . . } 02 26 11 50  
The Excentricitie . . . . . } 43 862

The Moons true place . . . . . } 20 51 52  
The true place of the  $\oslash$  . . . . . } 16 30 24

The Argument of Latitude . . . . . } 04 21 28  
The Moons true hourly Motion . . . . . } 00 33 18  
The Sun's  $2' 23''$ : The Moons from the Sun . . . . . } 00 30 55

The Equation of days to be subtracted here <sup>h m s</sup> . . . . . } 00 04 57  
Therefore the apparent time of the  $\odot$  in? . . . . . } 02 35 18  
the Orbit at . . . . . }  
Time of Reduction subtracted . . . . . } 00 02 11

The apparent time of the nearest approach of }  
the Moon to the Center of the Disk . . . . . } 02 33 07  
But of the Ecliptical  $\odot$  with the Sun . . . . . } 02 37 29

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And



And the nearest distance of the Moons Center from the Center }  
 of the Disk in her passage over it, equal to her Latitude at }  
 the time of her Conjunction in the Orbit . . . . . } 22 46

The Moons Horizontal Parallax was then . . . . . 57 44  
 The Suns subtracted from it . . . . . 60 10  
 Leaves the Semidiameter of the Disk . . . . . 57 34

The Moons Horizontal Semidiameter . . . . . 15 40  
 The Suns . . . . . 15 50  
 The Semidiameter of the Penumbra . . . . . 31 30

The Angle of the Moons way with the Ecliptick  $5^{\circ} 41'$ , this is equal to the Angle which the Perpendicular to her way formes with the Axis of the Ecliptick; and if the Argument of Latitude be more than 9 Signes or less than 3, the said Perpendicular lies to the left hand, if more to the right from the Axis of the Ecliptick.

*To Calculate the times of the principal appearances of a Solar Eclipse under the Meridian of LONDON.*

1. To the Semidiameter of the Disk add the Semidiameter of the Penumbra, if the Moons Latitude at the time of the true  $\oslash$  in the Orbit be less than this Sum, the Sun will appear Eclipsed somewhere on the Earth, otherwise, not.

And if the said Latitude be less than the Semidiameter of the Disk, the Eclipse will be Central in some places of the Earth, otherwise, no where.

Subtract the Semidiameter of the Penumbra from the Semidiameter of the Disk, if the Moons Latitude at the time of the Conjunction be less than this Residue, the intire Penumbra will fall within the Limb of the Disk otherwise not.

2. Convert this difference, the Semidiameter of the Disk, and the Sum above got, severally into Seconds:

Then say,

*As the Radius,  
 To the Moons Latitude in Seconds;  
 So the Sum of the Semidiameters in Seconds,  
 To the Co-sine of the first Angle of Incidence.*

And, *So is the Semidiameter of the Disk,  
 To the Co-sine of the second Angle of Incidence;  
 And, So is the Difference of the said Semidiameters,  
 To the Co-sine of the third Angle of Incidence.*

The

The first Angle of Incidence subtends the Motion of Semiduration of all manner of Eclipses on the Earth; the second the Motion of Semiduration of Central Eclipses; and the last the Motion of Semiduration of the entire Penumbra within the Disk.

Say Again,

*As the Radius,  
 To the sine of the first Angle of Incidence;  
 So the Sum of the Semidiameters of the Disk and Penumbra,  
 To the Motion of Semiduration of the whole Eclipses of all sorts.*

And, *So the Semidiameter of the Disk,  
 To the Motion of Semiduration of Total Eclipses.*

And Again,

*So the difference of the Semidiameter of the Penumbra and Disk,  
 To the Motion of the Semiduration of the Penumbra within the Disk, or Semimora.*

3. To Convert these Motions into time, say,

*As the Moons hourly Motion from the Sun,  
 To one hour;  
 So the Motion of any Semiduration,  
 To the time answering it.*

Which subtracted from, or added to the time of the middle Eclipse; or the nearest approach of the Centers of the Moon and Disk, gives the time under the Meridian of our Tables, when the answerable appearances begin or end in other places of the Earth.

In the first Section of this part you were taught how to find the Angle which the Axis of the Earth formes with the Axis of the Ecliptick; and to know on which hand from the Axis of the Ecliptick it lay in the Projection; how to know on which side the said Axis the Perpendicular to the Moons way lies, you have been shewed before: Note now,

If the Axis of the Globe, and the Perpendicular to the Moons way be both to the same hand (that is, both to the right, or both to the left from the Axis of the Ecliptick) their difference, but if otherways (that is one on the right, and the other on the left) their Sum shall be the Angle, which the Moons Path over the Disk formes with a Parallel to the Equator: This for brevity, wanting a better Term, I call the Angle of Direction.

Which if the inclination of the Axis of the Globe, be less to the right hand or more to the left, than the Inclination of the Perpendicular to the Moons way, to the Axis of the Ecliptick; or if the Axis of the Globe

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lying



lying on the left, the Perpendicular fall on the right hand the said Axis of the Ecliptick, the Angle of Direction shall be Affirmative; but if the said Inclination be left to the left hand, or more to the right, than the Inclination of the Perpendicular; or if the Perpendicular lying on the left, the Axis of the Globe fall on the right hand the Axis of the Ecliptick, the said Angle of Direction will be Negative: Mind these Cautions, then say,

As the Radius,

To the Tangent of the Angle of Direction;

So the nearest distance of the Centers of the Moon, and Penumbra at the middle of the Eclipses.

To the Motion between the Axis of the Globe, and the place of the Moons nearest approach to the Center of the Disk.

Find the time answering to this Motion, as you did the time of the Semiduration before; If the Angle of Direction were Negative, this subtracted; If Affirmative, added to the Apparent time of the middle, gives the Apparent time at London, when the Meridional Sun shall be Centrally Eclipsed elsewhere.

Example.

The Semidiameter of the Disk	00	57	34
The Semidiameter of the Penumbra	00	31	30
Their Sum	01	29	04
Their Difference	00	26	04

The first Angle of Incidence	75	11	00
The second	66	42	00
The third	29	08	40

The Motion of Semiduration	01	26	06
Of Semi-centralitie	00	52	52
Of Semi-mora	00	12	41
From the Axis to the nearest approach	00	01	14

Hence the time of the Semiduration of all manner of Eclipses in the Earths Disk } 02 47 06

The time of the Semiduration of all the Central Eclipses in the Earth } 01 42 36

The time of the Semi-mora, or the Semiduration of the whole Penumbra within the Disk } 00 24 38

The time from the transit by the Axis to the middle } 00 02 24

By

By Subtracting and adding these severally (all save the last, which is only to be subtracted) to 2<sup>h</sup> 33' 00" the time of the middle, or nearest approach of the Moon to the Center of the Disk, I Collect the times at London, when,

The Penumbra first touches the Disk and the Eclipse first of all begins in the Earth } 11 46 01 In the Morning.

The Center of the Penumbra enters the Disk and the Central Eclipses begin } 00 50 31 Afternoon.

The Mora begins, or the Penumbra is now first wholly within the Disk } 02 08 29

The Meridional Sun Centrally Eclipsed } 02 30 43

The Nonagesimal Sun Centrally Eclipsed } 02 37 29

The Mora ends, or the Penumbra begins first to Emerge from the Disk } 02 57 45

The Central Eclipses end in the Earth and the Center of the Penumbra passes off the Disk } 04 15 43

The Penumbra passeth off the Disk, and all Eclipses ended in all places of the Earth } 05 20 13

After they have continued in passing over the Earth } 05 34 12

At that place where the Penumbra first enters into the Disk, the Sun appears beginning to be Eclipsed in the Supreme Point of his Vertical Diameter; where the Center of the Penumbra enters it, he appears Centrally Eclipsed in his Rising; and the Eclipse ends as he Riseth in the lowest Point of his Vertical Diameter, in that Point of the Earth where the Penumbra is first totally Immersed within it: where the Line of the Moons way intersects the Axis of the Globe he is Centrally Eclipsed in the Meridian; and where it passeth the Axis of the Ecliptick in the Nonagesimal degree.

Where the Penumbra first begins to Emerge from the Disk, the Eclipse is beginning in the lower Extremitie of his Vertical Diameter as he sets; where it Cuts the Disk again he happens Centrally Eclipsed in his setting; and where it wholly leaves the Disk, the Eclipse ends in the upper Extremitie of his Vertical Diameter as he passeth the Horizon.

¶ To



*To determin the Latitudes of those places on the Globe, and their Longitudes from London, where any of those appearances happen.*

If the Angle of Direction be Negative, subtract it from, otherways add it to the Angles of Incidence, the Residue shall be the Amplitudes of those Paths in the Horizon of the Disk, which the Penumbra touches in its first Entrance, when its Center enters, and when tis first totally within: Add the same Angle to the Angles of Incidence when Negative, subtract it when Affirmative, makes the Amplitudes of those Paths in the Horizon of the Disk, whereon the Penumbra first begins to Emerge from the Disk, where its Center Emerges, and where it last touches it as it passeth off.

Say Then,

*As the Radius,  
To the sine of the Suns distance from the Pole;  
So the Co-sine of the Amplitude of any Path,  
To the Co-sine of its Latitude.*

Which if the Amplitude of the Path be less than 90 Degrees, is North of the Equator, otherways, South:

Say Again,

*As the Co-sine of the Suns distance from the Pole,  
To a Radius;  
So the Tangent of the Amplitude of any Path,  
To the Tangent of the hour of Sun Rise, or Sun Set in that Latitude.*

Which if the Suns distance from the Pole be less than 90 Degrees and the Latitude North; or more than 90, and the Latitude South, is to be accounted from Midnight, otherways from Noon.

*But to find in what Latitude the Meridional Sun shall be Centrally Eclipsed.*

Say First,

*As the Co-sine of the Angle of Direction,  
To a Radius,  
So the Moons distance from the Center of the Disk in the middle of the Eclipse,  
To the distance in the Axis.*

And Again,

*As the Semidiameter of the Disk,  
To the sine of 90 Degrees;  
So the Distance of the Moons Center from the Center of the Disk, as she passeth over the Axis of the Globe,  
To the sine of the Arch of the Meridian betwixt the Sun and Vertex.*

Which

Which if the Moons Latitude at the  $\odot$  were North, subtracted from, if South added to the Suns distance from the Pole of the Globe, makes the distance of the Point on the Earth from the said Pole, of which, if less than 90 degrees, the Complement to 90 is the Latitude North; if more the excess shews the Latitude South.

And if the Arch of the Earth be more than the Suns distance from the Pole, the Pole it self is Eclipsed, and the Complement of the Latitude shall be their difference.

Take the Sum and difference of the Moons distance from the Center of the Disk, and the Semidiameter of the Penumbra, work by the same Proportion, and you will find the Arches of the Earth answering to them, and the places where the Meridional Sun was touched, either on his upper or under Limbe by the Moon as she passed by him.

If the place where the Moon shall be Centrally Eclipsed in the Nonagesime degree be required, having her distance from the Center of the Disk, she transits the Axis of the Ecliptick:

You may say again,

*As the Semidiameter of the Disk,  
To a Radius;  
So the Moons distance from the Center of the Disk in her transit,  
To the sine of the Suns distance from the Vertex in the Nonagesime.* Which obtained,

Say,

*As the Radius,  
To the Co-sine of the Inclination of the Axis of the Earths Globe to the Axis of the Ecliptick;  
So the Tangent of the Suns distance from the Vertex,  
To the Tangent of a fourth Arch, which taken from the Suns distance from the Pole leaves a fifth.*

Say Now,

*As the Co-sine of the fourth Arch,  
To the Co-sine of the fifth;  
So the Co-sine of the Suns distance from the Vertex,  
To the sine of the Latitude of the place.*

Say again,

*As the sine of a fifth Arch,  
To the sine of the fourth;  
So the Tangent of the Inclination of the Axes,  
To the Tangent of the hour from Noon when the Sun will be in the Nonagesime.*

Note,



Note, that if the Axis of the Globe be to the right hand from the Axis of the Ecliptick, the hour is before Noon, if to the left, Afternoon.

For Example.

The Inclination of the Axis of the Globe to the right hand from the Axis of the Ecliptick in the Disk	08 48 00
The Angle which the Perpendicular to the Moons way formes on the right hand with the Axis of the Ecliptick	05 41 00
Their difference the Angle of Direction Negative	03 07 00
Which therefore subtracted from the first Angle of Incidence	07 51 00
Leaves the Amplitude of that Path of that Vertex in the Horizon of the Disk, which the Penumbra first touches in its entrance	72 04 00
Hence the Latitude of that place	16 36 Nor.
The time of the Suns rising there	05 32 31
The time then at London	11 46 01
The Difference equal to the Difference of Meridians	06 13 30

And the place to the West of London, 93 22 1/2

Where the Eclipse first begins at Sun Rise, in which Latitude and Longitude from London, lies the Gulf of Honduras in America, where the Eclipse will begin in the Suns upper Limb as he Riseth.

The Angle of Direction	03 07 00
Contrary to its Title added to the Angle of Incidence	07 51 00
Makes the Amplitude of that Path in the Disk which the Penumbra last touches, when it leaves the Earth	78 18 00
Hence the Latitude of that Point	10 51 60.
The time of the Suns set there	06 17 39
The hour at London then Afternoon	05 20 13
The difference equal to the difference of Meridians	00 57 26
Therefore the place to the East of London	14 21 30

Under

Under which Position lies Zanfara in Egypt, whereabouts the Eclipse will be seen ending in the supreme part of the Suns Vertical Diameter, as *where the Eclipse last ends at Sun Set.*

The second Angle of Incidence is	66 42 00
The Angle of Direction Subtract	03 07 00
The Amplitude of that Path which the Center of the Penumbra touches, when it enters the Disk	63 35 00

Hence the Latitude of the place 24 23 Nor.

The time of the Suns Rise in that Latitude	05 18 05
The time at London then Afternoon	00 50 31
The Difference of Meridians	07 32 26

Therefore the place to the West of London 113 06 30

Which position agrees with New Spain in America, where the Sun will be Centrally Eclipsed at his Rising. *Where the Sun Rises Centrally Eclipsed.*

The Sum of the second Angle of Incidence and Direction make the Amplitude of that Path which the Center of the Penumbra last touches, when it leaves the Disk	69 49 00
The Latitude therefore of that Point North	18 40 00

The time of Sun Set in that Latitude	06 31 11
The time then at London Afternoon	04 15 43
The Difference of Meridians	02 15 28

The place therefore to the East of London 33 52 00

Under which Position lie the Southern parts of Egypt, where the Sun Sets centrally Eclipsed. *Where the Sun Sets Centrally Eclipsed.*

The Difference of the Angle of Direction, and third Angle of Incidence, makes the Amplitude of the Path of that Vertex in the Horizon of the Disk, which the Penumbra last touches when tis Totally immerfed in it, 26° 01'

Hence the Latitude of that Point 56 30

Time of Sun Rise in that Latitude at	03 30 39
Time then at London Afternoon	02 08 29
The Difference of Meridians	10 37 50

And the place to the West of London 159 27 1/2 The

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Where the Eclipse ends at Sun Rise. The place under the Latitude and Longitude from *London*, falls in the Western Ocean, to the West of the *Streight of Anian*, (if any such) and there the Eclipse ends at Sun Rise, in the lowest Point of his Vertical Diameter, this is the most Western place that sees the Eclipse.

The Sum of the Angle of Direction and the third Angle of Incidence makes the Amplitude of the Path of that Vertex whereon the Penumbra first begins to Emerge from the Disk

Therefore the Latitude of that place . . . . . 51 43

The time of Sun Set there . . . . . 08 02 12  
The hour then at *London* Afternoon . . . . . 02 57 45  
The Difference of Meridians betwixt *London* and it . . . . . 05 04 27

Therefore the place to the East of *London* . . . . . 76 07

Where the Eclipse begins at Sun Set. Under which Position on the Globe lie the Southern parts of *Caracathay*, where the Eclipse begins in the lowest Point of the Suns Vertical Diameter, as he Sets, this is the most Eastern of all those places where any part of the Eclipse of the Sun is seen.

The distance of the Penumbra from the Center of the Disk in the place where the Path intersects the Axis  
The Arch in the Meridian of the Earth under it is  
The Suns distance from the Pole  
Their Difference, or the Complement of the Latitude  
Therefore the Latitude North

Time there is Noon, at *London* Afternoon . . . . . 02 30 43

So the place to the West of *London* . . . . . 37 41

Where the Sun is Centrally Eclipsed in the Meridian. And the Sun Centrally Eclipsed in the Western Ocean about the *Azores*, in the Meridian, or at Noon.

The Sum of the Semidiameter of the Penumbra and the distance of its Center from the Center of the Disk in its passage  
The Arch in the Meridian answering it  
Exceeds the Suns distance from the Pole

Where the Suns lower is just touched by the upper Limb in the Meridian. The Eclipse therefore extends beyond the Pole, and in the Latitude of 8° 44', the Moons upper Limb just touches the lower Limb of the Sun in the Northern Meridian.

The

The Semidiameter of the Penumbra exceeds the distance of the Moons Center, from the Center of the Disk in her passage over the Axis

The Arch of the Meridian answering it South of the Sun  
Added to the Suns distance from the Pole makes  
Therefore the Latitude North

Where under the same Meridian passing a little to the West of the *Azores*, where the Northern Limb of the Sun is just touched by the Moons Southern, South touches which place falls in the Western Ocean betwixt the Islands of *Cape Verde* the Suns Northern Limb in the Meridian.

The distance betwixt the Center of the Disk, and the place where the Moons Path intersects the Axis of the Ecliptick is  
The Arch of the Earths Globe under it

The time when the Center of the Moon passeth it  
Afternoon  
The time at *London* then Afternoon  
The Difference of Meridians

Therefore the place to the West of *London* . . . . . 34 27  
The Latitude of that place . . . . . 45 04

Where the Nonagesimal Sun is Centrally Eclipsed; that is something more Westerly than the place where he was Centrally Eclipsed in the Meridian.

Where the Sun is Centrally Eclipsed in the Nonagesimal or highest Point of the Ecliptick.

## SECTION V.

That the reason of the foregoing Calculus of the General Phases of a Solar Eclipse may be evident to the Ingenious Reader; I shall here shew how this may be represented by an easy Delineation in *Plano*.

Let  $\odot$  represent the Center of the Disk, take  $\odot B$  from a Scale of equal parts, or from the Line of Lines on a Sector, equal to its Semidiameter 57'34", and therewith setting one Foot of the Compasses on  $\odot$ , strike a Circle; this shall represent the Limb or Horizon of the Disk, projected on a Plane Co-incident with the Moons way, at right Angles with the Line Connecting the Centers of the Sun and Earth.

Through  $\odot$  draw the Diameter  $e \odot \pi$  continuing it both ways without the Disk. This shall be the Line I call the Axis of the Ecliptick, and the Point  $e$  where it intersects the upper part of the Limb of the Disk its Northern Pole.

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From the same Scale of equal parts, or the same Line of Lines on the Sector open to the same Angle, take off the Semidiameter of the Penumbra  $31' 30''$ , and set it off on the Axis of the Ecliptick from  $e$  to  $A$  and  $x$ , through which Points, with one Foot of the Compasses on the Center  $\odot$ , strike Circles; the Semidiameter of the Larger  $\odot A$  shall be  $01^{\circ} 26' 04''$  the Sun,  $\odot x$   $26' 04''$  the difference of the Semidiameters of the Disk and Penumbra.

The Inclination of the Perpendicular to the Moons way to the Axis of the Ecliptick, I have before determined  $05^{\circ} 41'$  on the right hand. Make therefore  $\odot e$  (the Semidiameter of the Disk) the Radius of a Line of Chords, and taking from the same, the Chord of the Inclination  $05^{\circ} 41'$ , set it off from  $e$  the Pole of the Ecliptick to  $z$  that way; from the Center  $\odot$  draw the Line  $\odot z$ , this shall be the said Perpendicular to the Moons way.

From the forementioned Scale of equal parts take  $22' 46''$ , the nearest distance of the Line of the Moons way from the Center of the Disk; which if North, as here, set it off in the said Line from  $\odot$  to  $m$  Northwards (otherways on the contrary (ide the Center towards A) through  $m$  draw the Line  $m f$  at right Angles to  $\odot z$ , this shall be the Line of the Moons way over the Disk, or the Path of the Penumbra.

To the Points  $n k r u q$  and  $f$ , where the Path of the Penumbra intersects the Circles before described, draw straight Lines from the Center  $\odot$ , producing  $\odot r$  and  $\odot n$  till they reach the Limb of the Disk in  $r$  and  $s$ , so have you in the Antecedent Limb of the Disk, First the Point  $n$ , the place of the Moons Center, when the Penumbra first touches the Limb of the Disk in  $u$ , whence the Rising Sun appears beginning to be first Eclipsed in the supreme Point of his Vertical Diameter: Secondly the Point  $k$ , where the Center of the Penumbra enters the Disk, and the Sun appears Centrally Eclipsed in his Rising: Thirdly  $r$ , the place of the Moons Center, when the Penumbra is got wholly within the Disk, and  $r$  the place in it where the Eclipse at that time ends, in the lowest Point of the Suns Vertical Diameter, as he Riset: Fourthly  $n$  the Point under which the Sun is Centrally Eclipsed in the Nonagesime, or totally if the Suns Semidiameter be less than the Moons. And in the Consequent Semi-Circle; Fifthly  $v$  the place of the Moons Center when the Penumbra begins to Emerge from the Disk, and  $s$  the Point in the Disk where it Emerges, and whence the Eclipse appears beginning in the Suns lowest Limb, as he Sets: Sixthly  $q$ , where the Center of the Penumbra Emerges from the Disk, and the Sun appears Centrally Eclipsed in his Setting: Seventhly  $f$ , the place of the Moons Center when the Penumbra leaves the Disk; and  $g$  the Point whereon it Emerges, the Eclipse ending there in the Vertical Point of the Setting Sun.

And now we have formed three pair of Triangles: First,  $m \odot n = m \odot f$ , in which is given  $\odot n = \odot f$ , the Sum of the Semidiameters of the Penumbra and Disk, and  $\odot m$  the nearest distance of the Path of the Penumbra from the Center of the Disk, and the Angle at  $m$  right; to find  $m \odot n = m \odot f$  the first Angle of Incidence, with  $mn = mf$  the Motion of the Semidiameter of all manner of Eclipses, which will be easily obtained by the forementioned proportions.

Secondly,

Secondly, In the Triangles  $m k \odot = m g \odot$ , are given  $\odot k = \odot g$  the Semidiameter of the Disk, with  $m \odot$  as before, to find  $m k \odot$  the second Angle of Incidence equal to  $m g \odot$ ; and  $m k = m g$  the Motion of the Semidiameter of Central Eclipses.

Thirdly, In the Triangles  $m v \odot = m t \odot$ , are known  $\odot t = \odot v$ , the Difference of the Semidiameters of the Disk and Penumbra with  $\odot m$  as before; whence  $m t \odot = m v \odot$ , the third Angle of Incidence;  $m t = m v$  = the Motion of Semidiameters will be easily had; which Arches  $m i = m f$ ,  $m k = m g$ ,  $m t = m v$ , being turned into time, and the times answering them subtracted from and added to the middle of the Eclipse, or the Moment the Center of the Penumbra is at  $m$ , gives the several times when the said Center shall be at  $n k t v q f$ ; or the times of general Phases of the Eclipse belonging to those places at London.

Or the time when the Center of the Penumbra shall arrive at the said Points, may be otherways Mechanically investigated thus. The middle of the Eclipse, or the time when the Moons Center will be at  $m$ , happens at  $33' 07''$  past two a Clock Afternoon: Say, As 1 Hour or 60 Minutes, to  $30' 55''$  the hourly Motion of the Moon from the Sun: So is  $33' 07''$  the time more than 2 Hours Afternoon, to  $17' 02''$  the Motion from 2 a Clock to the middle.

From the same Scale wherewith you laid off the Semidiameter of the Disk  $57' 28''$ , take  $17' 02''$  of the same parts betwixt your Compasses, and setting one Foot on  $m$ , with the other make a Point in the Line of the Moons way on the Right-hand; this shall be the place of the Center of the Penumbra at 2 a Clock Afternoon at London, and is therefore noted here with the Number II.

The hourly Motion of the Moon from the Sun, is  $30' 55''$ , take therefore from the same Scale of equal parts  $30' 55''$  betwixt your Compasses, and setting one Foot on II, with the other make Points on each side it in the Line of the Moons way; these shall shew the place of her Center in it at the hours of I and III: And if from these Points you farther set off the said extent, in the said Line you may thereby find the place of the Moon in the same Line for every hour, whilst the Penumbra shall touch the Disk: Divide the space betwixt every hour into 60 parts, to have you the place of the  $v$  Center in the Line of her way to every single Minute of time.

After this manner was the Line of the Moons way drawn and divided in the Eighth Figure, whereby the times when the Moons Center comes upon any of the forementioned Points, will be found the same as by Calculation.

The Angle  $m \odot n$  is equal to the Arch  $z b$ ,  $m \odot k$  to  $z k$ , and  $m \odot t$  to  $z r$ ; to each of which the Arch  $z c$  (which according to Kepler is not more than  $5^{\circ} 18'$ ) in the Case before us being added, makes the Arches  $e b$ ,  $e k$ ,  $e r$ , but subtracted from them gives  $e g$ ,  $e f$ ,  $e s$  the Altitudes of the Nonagesime Degree in those places at San Rile or Sun Set; with which and the Suns true place or the opposite Point, as the Case happens, that Ingenious Person entering his Nonagesimary Table finds the Latitude of the Points



*b k r s q g*, and thence the right Ascension of the Midheaven at the time of the Sun Rising or Setting in those places, whose difference from the right Ascension of the Midheaven when the Penumbra is on any of the said Points under the Meridian of his Tables, gives the Longitude of those places thence, to the East if it were more, to the West if less than the right Ascension of the Midheaven at the place to which his Number are fitted.

It was I conceive the greatest success which the diligent Endeavours of this famous Person met with in Correcting of the Planetary Motions, that caused him to employ the greatest part of his time and pains about them; so that having found how the usual Imaginary Circles of the Sphere might be projected in the Copernican System, and all the Diurnal Appearances of the Sun and Stars salv'd by them; he contented himself to shew this, and never enquired how they were Naturally formed, and might be more easily represented without the help of any such Fictitious Circles; as I have before shewn; else he had never mist of a better Method, whereby without the help of any Nonagesimal Table, the Latitudes and Longitudes of those places on the Earth from the Meridian of his Tables, where the principal Appearances of a Solar Eclipse shall happen might be investigated, and which I shall here shew.

The Inclination of the Earths Axis to the Axis of the Ecliptick, I have already found in the first Section of this part  $8^{\circ} 48'$  on the right hand; set off accordingly  $8^{\circ} 48'$  in the Limb of the Disk, from  $e$  the Pole of the Ecliptick on the right hand to  $i$ , and by the Point so found draw the Line  $i \odot a$  through the Center of the Ecliptick, this shall be the Axis of the Earth projected in it.

The Inclination of the Perpendicular to the Moons way to the Axis of the Ecliptick, I have before determined  $5^{\circ} 41'$  to the same hand equal to the Arch  $e z$  which taken away from  $e i$ , leaves  $z i$  equal to  $z \odot i$  the Angle of Direction  $3^{\circ} 07'$ .

Which according to the Cautions of the Preceding Section is Negative, and therefore subtracted from the Arch  $z b$  leaves  $i b$  the Amplitude of that Path in the Horizon of the Disk whence the Eclipse is seen beginning in the Vertical Point of the Rising Sun; from  $z k$ , leaves  $i k$  the Amplitude of that Path whence the Eclipse is seen Central at Sun Rise; but taken from  $z r$ , the Residue  $i r$  will be the Amplitude of that, wherein the Eclipse ends in the lowest Point of the Rising Sun.

But if on the Contrary the Arch  $z n$  be added to  $z s$ , it makes  $i s$  the Amplitude of the Path, whence the Eclipse is seen beginning in the lowest Limb of the Setting Sun; to  $z q$  it gives  $i q$ , the like Amplitude of the Path of that Vertex, in which the Eclipse appears Central at Sun-set; but added to  $z g$ , the Sum  $i g$  will be the Amplitude of that Path, in which the Eclipse ends in the highest Point of the Suns upper Limb as he Sets.

In the same Seventh Figure let  $P$  represent the North Pole of the Globe, whose place in the Axis is determin'd by the directions of the first Section; from which Imagin Hour-circles drawn to *b k r s q g* in the Disk; the Angles which those Hour-circles shall form with the proper Meridian an  $\odot P$ , shall

be

be the hours at which the Sun rises or sets in any of those Paths, and the Arch of any Meridian betwixt the Pole and any of the said Points shall be the distance of the Path from the Pole, or the Complement of the Latitude of the place upon that Point. Let  $B$  in the Eighth Figure represent any of the said Points, and let the Hour-circle  $P B$  be drawn; In the Right-angled Triangle  $P B i$  are given,  $P i$  the Complement of the Suns distance from the Pole equal to the Reflection;  $i B$  the Amplitude of the Path, and the Angle at  $i$  right, whence either  $P B$  the Distance of the Path from the Pole, or  $B P i$  the hour of Sun rise or set will be found by the known Resolutions of Right-angled Triangles; which last whether it be to be Numbered from Noon or Midnight, the cautions of the last Section teach.

To find the place where the Sun will be Centrally Eclipsed in the Meridian: In the small Triangle  $m \odot p$  are given  $m \odot$  as before,  $m \odot p$  the Angle of Direction, with the Right-angle at  $m$ , whence the Arch  $m p$  intercepted betwixt the Earths Axis, and the Perpendicular to the Moons way, and consequently the time betwixt the Meridional Eclipse, and the middle will be found, as also  $\odot p$ , and the Arch of the Globe under it; Say, As  $i \odot :: 90^{\circ} :: \odot p$ : to the sine of the Arch of the Earths Globe under it; which in this Case subtracted from  $\odot P$  leaves  $P B$ , the Complement of that Latitude, under which the Sun is Centrally Eclipsed in the Meridian.

The Semidiameter of the Penumbra is  $31' 30''$ ;  $\odot p$   $22' 48''$  added to it makes  $54' 18''$ ; subtracted from it leaves  $8' 42''$ , which converted into Arches on the Earth by the foregoing Ratiocination, and those added to, and subtracted from the Suns Distance from the Pole  $\odot P$ , makes the Complements of those Latitudes, wherein the Suns under and upper Limb are only touched by the  $\delta$  in her Transit, as in the Example.

But if the Time when, and the place where the Moon shall appear totally Eclipsed in the Nonagesime Degree be required, in the Triangle  $N m \odot$  Right-angled at  $\odot$ , are known the Angle  $N \odot m$  which the Perpendicular to the Moons Path makes with the Axis of the Ecliptick, and the Angle at  $m$  right, whence the Motion betwixt the middle, and the Transit of the Axis of the Ecliptick  $N m$ , will be easily found, together with  $N \odot$ , and the Arch of the Earths Periphery under it.

Imagin an Arch of an Hour-circle  $P N$  strook through the Pole and this Point  $N$ , then in the Oblique-angled Triangle  $N P \odot$  are known the Arch  $N \odot$ , the Distance of the Nonagesimal Sun from the Vertex,  $\odot P$  the Suns Distance from the Pole, with the Angle  $\odot N P$  the Inclination of the Axis of the Globe to the Axis of the Ecliptick, whence  $N P$  the Complement of the Latitude, or the distance of the Vertex, where the Sun is Centrally Eclipsed in the Nonagesime, from the said Pole; together with the Angle  $N P \odot$ , or the hour (Afternoon in this Case) when the Sun shall be in the Nonagesime will be had.

After the same manner it might easily be determin'd under what Latitudes and Longitudes from the Meridian of our Tables, the Suns upper or under Limb should be only touched by the Moons in the Nonagesime Degree, or more Points might be found on the Globe; through which a Line drawn

shews



shews all the places where the Eclipse would appear Central, or the greatest nearly of any given Number of Digits.

If it were required to know the Longitude of that place from London, and its Latitude, where the Sun shall be Centrally Eclipsed, when 'tis here two hours Afternoon, the time proposed is  $33^{\circ} 07''$  before the middle of the Eclipse at London: Say then, As 1 Hour to  $30^{\circ} 53''$  the hourly Motion: So  $33^{\circ} 07''$  to  $17^{\circ} 02''$ , the Motion from 2 Hours Afternoon, to the middle, or from 11 to m.

To II draw the straight Line  $\odot$  II; then in the Triangle  $m \odot$  II, are given  $m \odot$  and  $m$  II, whence the Angle  $m \odot$  II will be found  $36^{\circ} 48'$ ; and  $\odot$  II  $28' 26''$ ; but the Arch of the Earths Periphery under it  $29^{\circ} 36'$ , the Distance of the Vertex under that Point from the Sun.

From the Pole P, let the Arch of an Hour-circle be drawn through II, so in the Oblique-angled Spherical Triangle  $\odot$  P II are known,  $\odot$  P the Suns Distance from the Pole  $65^{\circ} 08'$ , which  $\odot$  II the Suns Distance from the Vertex  $29^{\circ} 36'$ , and the Angle Interjacent P  $\odot$  II  $36^{\circ} 48''$ , whence P II the Complement of the Latitude will be found  $46^{\circ} 18'$ ; therefore the Latitude of that Point  $43^{\circ} 42'$  North.

But the Angle  $\odot$  P II, or the hour before Noon  $24^{\circ} 09^{\frac{1}{2}} = 1^{\text{h}} 36' 38''$ , the true time therefore at that place will be  $10^{\text{h}} 23' 22''$  in the Morning, which taken from 2 hours Afternoon leaves  $3^{\text{h}} 36' 38'' = 54^{\text{m}} 09^{\frac{1}{2}}$ , the Longitude of that place to the West from London.

## SECTION VI.

**T**O determin the Apparent Time of the beginning or end of Solar Eclipse, the Time when the Sun shall be Eclipsed to any possible Number of Digits, the Inclination of the Culps of the Eclipse, and the Time of the visible Conjunction of the Luminaries in any given Latitude.

In the first Section of this part, I have shewed how the Path of any Vertex may be described in the Disk, and for an Example, I have delineated the Path of the Vertex of London, at the time of this Eclipse of the Sun in the Eighth Figure which is the Ellipsis *dmf*.

In the foregoing or Fifth Section I have shewed how the Line of the Moons way, or Path of the Penumbra may be drawn and divided, which is also done according to the precepts there delivered, in the said Figure Eight.

In the same Figure I have drawn two other Paths, the middle LEO for the Latitude of  $36^{\circ} 03'$  North, which will fit Aleppo and all other places under that Latitude; the other IAB for the Latitude of  $17^{\circ} 30'$  North, under which lies the Island of Jamaica, where I desire to know at what time the Beginning of this Eclipse, the visible Conjunction of the Luminaries, and the End of it will happen.

Take

Take betwixt your Compasses the Semidiameter of the Penumbra  $31' 30''$ , from a Scale of such equal parts as the Semidiameter of the Disk was let off or measured by, that is  $57^{\frac{1}{2}}$ , and carrying one Foot along the Line of the Moons way from the right hand to the left, find a Point in it, upon which if that Foot be let the other turn'd about shall Cut the same hour in the Path of the Vertex that this stands upon: The Point in the Path upon which the fixed Foot then stands shall shew the time of the beginning of the Eclipse.

Carry on the same Foot of your Compasses still more to the left hand, and find another Point in the Line of the Moons way, whereon if you fix one Point of your Compasses, the other shall cut the same hour in the Path of the Vertex which this stands upon in the Line of the Moons way, the Point on which your Compasses stand shall shew the Minute the Eclipse ends, if the Scheme admit Minute Divisions.

By the help of a Square of which one side may be apply'd and carried close along the Ecliptick  $\gamma$  H, another Point may be found in the Path of the Vertex, whence a Line drawn by the Perpendicular edge of the Square, shall cut the same time in the Line of the Moons way, it marks in the said Path of the Vertex; this shall be the time of the visible Conjunction of the Luminaries.

Thus carrying the Semidiameter of the Penumbra betwixt my Compasses with one Foot in the Line of the Moons way, I find that when it comes to  $\alpha$  at 8' after 11 hours, the other if turn'd about will cut the same time in the Path of the Vertex at  $\beta$ , this therefore is the time of the beginning of the Eclipse at London.

Draw the Line  $\alpha \beta$ , and from  $\odot$  the Line  $\odot \beta$ , this shall represent the Vertical Circle; and the Angle  $\odot \beta \alpha$  which these two Lines form shall be the Angle which the Vertical Circle shall make with the Line connecting the Centers of the Sun and Moon at the beginning of the Eclipse.

If the Compasses be kept at the same extent, and one Point carried forward in the Path of the Penumbra, when it comes to  $\gamma$  at  $26^{\frac{1}{2}}$  past III, the other Point turn'd about will cut the same hour in the Path of the Vertex at  $\epsilon$ , wherefore the Eclipse then ends at London.

Draw  $\gamma \epsilon$ , and from the Center of the Disk  $\odot \epsilon$ , the Angle  $\odot \epsilon \gamma$  shall be that which the Vertical Circle shall form with the Line connecting the Center of the Luminaries, at the end of the Eclipse.

And if the edge of a true Square be carried close along the Line H  $\gamma$ , when the Perpendicular side cuts the Path of the Penumbra in  $\beta$  at 21 after III, it also cuts the same hour in the Path of the Vertex at  $\epsilon$ , this therefore is the time of the visible Conjunction,  $\epsilon$  the place of the Vertex or the Suns Center,  $\beta$  the Moons place in her Orbit.

Take the Semidiameter of the Sun from the same Scale, whereby you laid off the Semidiameter of the Disk, betwixt your Compasses, and therewith on the Center  $\epsilon$  describe a Circle, this shall represent the Sun, and with the Moons Semidiameter betwixt your Compasses taken from the same Scale, on the Center  $\beta$  describe another Circle, this shall cut off from the



former so much as the Sun shall be Eclipsed at the time of the visible Conjunction.

From  $\odot$  draw the Line  $\odot s \zeta$ , this shall represent the Vertical Circle,  $\zeta$  the Vertical Point in the Sun, whereby the position of the Culps of the Eclipse in respect of the Perpendicular through the Suns Center, are plainly and easily obtained.

Produce  $\zeta s$  till it intersect the Moons Limb in  $\theta$ , then shall  $\theta \theta$  the greatest distance of the Limbs of the Sun and Moon, be the parts Eclipsed, which if the Suns Diameter be divided into 12 equal parts shall be equal to  $7\frac{1}{2}$  of them, and so many are the Digits Eclipsed at the greatest Obscuration nearly.

Hence at London,

	h.	m.
The beginning of the Eclipse July 2 <sup>d</sup> 1684. at $\odot$	02	08 Afternoon,
The visible Conjunction of the Luminaries $\odot$	03	21 Digits then $7\frac{1}{2}$ ;
The end . . . . .	04	26 $\frac{1}{2}$ .

And the position of these Appearances in respect of the Vertical Circle passing the Suns Center, as in the Ninth Figure.

If it were required to know at what time the Eclipse shall begin and end at *Aleppo*; the Arch of the Ellipsis  $L E O$  is the Path of that place, and the Path of the Penumbra is the same for all places of the Earth.

But the Times will be to be Numbered differently in it, according to the Difference of the Meridian of any place from *London*, for if the place given lie to the East, the hours in the Moons Path will be to be reckoned so much more; if to the West so much less, as is the difference of Meridians.

*Aleppo* is usual accounted  $02^h 20'$  to the East of *London*, the middle therefore which at *London* will be  $2^h 33' 07''$  Afternoon, shall be  $04^h 53' 07''$  Afternoon at *Aleppo*; and all the hours marked in the Path will be accounted  $03^h 20'$  more than they are noted, with the large Figures.

Wherefore on the upper side of the Line of the Moons way, I have noted in small Figures the place of her Center in the Path at every hour; so that hence it will be easy to find her place in the Path to any Minute required.

And now carrying the Semidiameter of the Penumbra, betwixt my Compasses along the Line of her way; I find that when one Foot comes to  $\lambda$  at  $05^h 10'$  reckoned for *Aleppo*, the other will cut the same hour in the Path of the Vertex at  $\pi$ , this therefore I pronounce the time of the beginning of the Eclipse there.

And when the same carried on comes to  $\pi$  at  $6^h 17\frac{1}{2}'$ , there a Line drawn Parallel to the Axis of the Ecliptick, or Perpendicular to the Ecliptick itself will cut the same hour in the Path of the Vertex at  $\pi$ ; this therefore is the time of the visible Conjunction of the Luminaries, the distance of their Centers then  $\pi \theta$ .

Carrying the same Foot of the Compasses at the same extent forward along the Line of the Moons way, I find that when at  $07^h 08'$  the same Foot

Foot stands upon  $s$ , the other cuts the same hour in the Path of the Vertex where it intersects the Limb of the Disk, this therefore I conclude the end of the Eclipse, just at Sun-set.

Therefore at Aleppo,

	h.	m.
The beginning of the Eclipse . . . . .	05	19 $\frac{1}{2}$ Afternoon,
Visible Conjunction . . . . .	06	17 $\frac{1}{2}$ Digits then 7;
End at Sun-set . . . . .	07	08.

And the bearing of each of these Appearances as in the Tenth Figure.

If the time of these Phases at *Jamaica* be demanded the Arch of the Ellipsis  $I A B$  represents the Path of that place, whose Meridian is accounted 5 hours to the West of ours, so that when 'tis Noon with us, 'tis to the Inhabitants there only 7 a Clock in the Morning: and the middle of the Eclipse, which with us is at  $2^h 33'$  Afternoon, to them will be at  $9^h 33'$  before Noon; Wherefore on the under side of the Line of the Moons way, I have noted the hours 5 less than at *London*, so that the Divisions Numbered by them 'tween the place of the Moons Center to any given time during the Eclipse at *Jamaica*.

Let the Semidiameter of the Penumbra be carried along this Line as in the foregoing Examples, the standing Foot being at  $\mu$  upon  $6^h 55\frac{1}{2}'$  in the Path of the Penumbra, the other at  $\nu$  will cut the same hour in the Path of the Vertex; a Line drawn from  $\sigma$  at  $08^h 05'$  will cut the same hour in the Path of the Vertex at  $\tau$ , the distance of the Centers of the  $\odot$  and  $\nu$  at that time being  $\sigma \nu$ : And if with the Compasses at the former extent we seek another Point in the Line of the Moons way, whereon if one Foot standing, the other turn'd about will cut the same time in the Path of the Vertex; we shall find it at  $\xi$  at  $08^h 59'$ , and the place of the Vertex at  $\phi$ .

Wherefore at Jamaica,

	h.	m.
The beginning at . . . . .	06	55 in the Morning,
The visible Conjunction . . . . .	08	05 Digits then $4\frac{1}{2}$ ;
The End . . . . .	08	59.

And the position of these appearances as in the Eleventh Figure.

If it be required at what time any possible Number of Minutes or Digits, shall be Eclipsed in the Suns Antecedent or Consequent Limb at any Place; Let the Suns Diameter be accordingly divided into Minutes or Digits, and subtracting or Cutting off the parts required to be Eclipsed from the Semidiameter of the Penumbra, take the remaining part of it betwixt your Compasses, and carrying it along the Line of the Moons way find the first Point in it, on which placing the one Foot, the other turn'd about will Cut the same hour the fixed Foot stands upon; the hour and Minute in the Path on which the fixed Foot stands shall be the time of that



Obscuration. If for Example it were demanded at what time 3 Digits, or one fourth part of the Suns Diameter, should be Eclipsed in his Antecedent Limb at *London*; cutting off  $\frac{1}{4}$  of the Suns Semidiameter from the Semidiameter of the Penumbra, and carrying the rest as directed, I find it  $2^h 29^m \frac{1}{2}$  in the Line of the Moons way, when the one Point of the Compasses standing on that Time, the other will cut the same accounted in the Path of the Vertex; and therefore this shall be the time of that Eclipse in the Suns Antecedent Limb at *London*.

Whence we have a very ready way given for finding the Difference of Meridians betwixt any two places, whose Latitudes are known, from the like Observation of the same Solar Eclipse, which will not be difficult if the time and quantity of the Eclipse observed under the Meridian of the Tables, shall happen to be the same the Calculus and Construction shews; for suppose the Eclipse shall happen as it is predicted at *London*; but at *Jamaica* the end shall appear at  $9^h 20^m$  in the Morning; the place of the Vertex in the Path of *Jamaica* at that time will be found at *v*, take the Semidiameter of the Penumbra betwixt the Compasses and setting one Foot on *v*, with the other strike an Arch cross the Line of the Moons way at *e*, this cuts it  $2^h 4^m$  Afternoon at *London*; which shall be  $9^h 20^m$  in the Morning at *Jamaica*, therefore the difference of Meridians betwixt *Jamaica* and *London* (if it shall so happen) will be the difference of these Times, that is only 4 h. 44'.

But if the Time at *London* shall be found different from what the Calculation has given, and the Digits Eclipsed more or less than it represents, the Latitude of the Path *OM* must be made more or less accordingly; till the Digits Eclipsed at the visible Conjunction shall be found the same with what the Observation requires.

For the Semidiameter of the Disk, the Suns, and Moons, with their hourly Motions are found by Experience so nearly agreeable to Observation, that they will admit of little or no alteration, the sensible defects of our Tables are only in the Moons Latitude and place, of which the first being correct, the latter may also be easily amended.

For the Latitude of any place being given, and the time of the beginning, end, or any Phases of an Eclipse, the place of the Vertex in the Disk at that time may be laid down by the Method of the first Section.

The Semidiameter of the Penumbra, or the parts of it not Eclipsed, if some Appearance were given, may be made by taking the parts deficient from the Semidiameter of the Penumbra.

Then taking it or the remaining parts betwixt your Compasses, set one foot on the Point of the Vertex, and turning the other about make a stroke through the Line of the Moons way, the Point there Cut shall be the place of the Moons Center at that time, whence the Line of the Moons way may be divided.

And then the time of any Appearance, in a distant place whose Latitude is known, being given, the difference of Meridians betwixt that, and the Meridian of the Tables, or any other known place will be easily found, as the difference of Meridians betwixt *Jamaica* and *London*: The Method I confess requires much Caution, but if duly Considered, it will be easily understood, and put in practice by the Ingenious observer.

S E C T.

## SECTION VII.

**A**s the beginning, Digits obscured, and end of a Solar Eclipse; So also the Occultation of any Fixed Star by the Moon, its Emergence from her, or the distance of her Center from it when not covered by her, at the time of their Elliptical Conjunction, may be determined by Construction; only, remembering what I have before intimated, that by reason both the Parallaxes and Semidiameters of the fixed Stars are small and almost insensible, the Moons Horizontal Parallax shall be the Semidiameter of the Disk; and her Semidiameter, the Semidiameter of the Penumbra.

And for the Construction of these as of Solar Eclipses will be required.

1. The true time of the Elliptical Conjunction of the Moon and Star.
2. The Angle of the Moons way with the Ecliptick, or which the Axis of her Orbit forms with the Axis of the Ecliptick.
3. The difference of the true Latitudes of the Moons Center; and the Star to which she applies at the time of the Elliptical Conjunction.
4. The Stars Right Ascension and distance from the Pole of the Globe.
5. The Inclination of the Axis of the Earths Globe, to the Axis of the Ecliptick in the Disk.

1. To find the first in any given Year and Month; make the Mean Motions of the Moon to that Year and Month, by the help of the Table of the Moons mean Motions, which subtract from the true Longitude of the Star at the given Time, from the Residue subtract the next lesser middle Motion under the Month of *January* in the Eighth Table; and from what remains, the next lesser middle Motions found in the Ninth Table continually till nothing be left; the Days, Hours, Minutes and Seconds standing against the middle Motions, so subtracted, shall be the true time of the Mean Conjunction of the Moon and Star.

2. To this Time calculate the Moons true place in the Ecliptick by the Directions of the Third Section, which if it happen to be the same with the Stars, the time of the Mean and True Conjunction are the same, but if, as commonly, they differ; then,

Note the difference, and if the Moons true place be found short of the Stars, add; if past, subtract about twice as many Hours and Minutes, to or from the time of the Mean Conjunction, as the is Degrees and Minutes short or past the Star; and to the time thus made Calculate her true Longitude in the Ecliptick, betwixt which, and the Stars true place note the Difference:

Then you may say,

- As the differences of the places of the Moon Calculated to these two times;  
To the difference of the said times;  
So the difference betwixt the place of the Moon and the Star last Calculated;  
To the interval of time betwixt the last Calculation, and the time of the true Conjunction.*

A F.



If the Moons place found by the last Calculation were less than the Stars, add the interval to; if more, subtract it from the Time to which the last Calculation was made; that Sum or Difference shall be the true equal Time of the Conjunction of the Moon and Star; which by the Equation of Days may be Converted into the Apparent.

But this Method being tedious, I have most commonly made use of another, which besides that it is more Expeditious, will be found to have some other Conveniencies in it above the preceding.

The Moons true places Calculated either from Tycho's, or Kepler's Numbers I find to agree much better with my own, than any other; From these the places of the Moon are given in *Eichstadius* or *Heckers Ephemerides* for years past; in *Argolus's* for years to come till 1700.

Entering therefore the Ephemerides of that Month in which you desire to know at what time the Moon will be in Conjunction with any Star, you will readily see on what Day her places at Noon will be next less and more than the Stars, the difference betwixt those two places at Noon are her Diurnal Motion. Subtract her place at Noon next less than the Stars, from its true place, to have you their difference:

Say Then,

*As the Diurnal Motion, to this difference,*

*So are 24 hours or one day;*

*To the time of the Conjunction of the Moon and Star, Afternoon, under the Meridian of the Ephemerides.*

The Meridian of *Rome*, to which *Argolus's* Ephemerides are fitted, lies 1 hour nearly to the East of *London*; therefore from the time thus obtained subtract one hour, to have you the time of the Conjunction of the Moon and Star under the Meridian of *London*.

To which if you Calculate the Moons true place by the Tables herewith published, as also to 2 hours either before, or after, as you judge most Convenient, you will have the Moons Motion in 2 hours given, by which and the difference of hers and the Stars true Longitudes at either of the times, you may find the true time of their Conjunction. To get her Latitude at which time,

In the Calculation of the Moons place you will have given the Inclination of her Orbit to the Ecliptick, with the true place of her Node.

Subtract the place of the Node from the Longitude of the Star, the Residue is the Argument of Latitude:

Say Then,

*As the Radius,*

*To the Tangent of Inclination of her Orbit;*

*So the Sine of the Argument of Latitude,*

*To the Tangent of the Moons true Latitude at the time of the true Conjunction.*

Which

Which if the Argument of Latitude be less than 6 Signes is North, if more South.

And if the Moons Latitude at the time of the true Conjunction be more to the North, or less to the South than the Stars, the Moons Center in her transit by the Star passeth as much to the North of it, as is their difference, but if otherways, as much to the South:

Again,

*As the Radius,*

*To the Sine of the Inclination of the Orbit;*

*So the Co-sine of the Argument of Latitude,*

*To the sine of the Angle of the Moons way with the Ecliptick.*

Or which the Axis of her Orbit formes with the Ecliptick, from which it lies to the Right-hand, when the Argument of Latitude is more than 9 Signes, or under 3; but to the left when the said Argument is more than 3 Signes, or less than 9.

The Longitudes of the Stars from the first Point of  $\gamma$  with its Latitude being given, its distance from the Pole and Right Ascension may be got by the Directions of the 14 Section of the First Part, or more easily, and exact enough for our purpose, by the Tables of Declination and Right Ascension Printed herewith, from the beginning to page 37, which being obtained it will hold.

*As the Co-sine of the Stars Latitude,*

*To the Co-sine of its Right Ascension from the next Equinoctial Point;*

*So the sine of the distance of the Poles of the Globe and Ecliptick,*

*To the sine of the Inclination of the Earths Axis to the Ecliptick.*

Which if the Longitude of the Star be in  $\gamma \pi \times \gamma \delta \pi$  is to the Left, if in any of the other 6 Signes to the Right-hand from the Axis of the Ecliptick.

As in the Construction of the Solar Eclipse, the Plane upon which the Projection was drawn was supposed to stand at Right angles to the Line Connecting the Centers of the Sun and Earth, coincident with the Moons Orbit; so in the Stellar Eclipse we must suppose it to coincide with the Moons way at Right angles to the Line Connecting the Centers of the Earth and Star, and that Lines produced from the Star to infinite Points in the Horizon of the Earths Disk, her Axis, the Axis of the Ecliptick, and the Path of any Vertex, will project them all in the same Plane.

Having shewn before how this projection may be represented and delineated in *Figure*, I shall not need here to repeat any directions concerning it, but seeing the Path of the Vertex, and Line of the Moons way over the Disk may be divided several ways; I shall only teach one, which in my opinion seems the most convenient for our purpose.

When



When the Vertex passeth the Axis of the Globe projected in the Disk, the Star Transits the Meridian; I call *that time the Sidereal Noon*, and mark the intersection with  $\circ$ ; the hours on each side it projected in the Path I number by their distances from it: 1, 2, 3, 4, 5, 6, &c. as in the Twelfth Figure, those on the Right-hand being *Negative*, and shewing the Star short of the Meridian; those on the Left *Affirmative*, and shewing it past.

Having got the Apparent time of the true Ecliptical Conjunction, turn it into Degrees and Minutes; get the Suns Right Ascension at the same time. Add these together, the Sum shall be the Right Ascension of the Midheaven, which if it be less than the Stars Right Ascension subtracted from it, leaves an Arch, which turn'd into time gives *the time before the Sidereal Noon*, at which the Moons Center shall Transit the Axis of the Ecliptick.

But if the Right Ascension of the Midheaven be greater than the Stars, subtract this from that, the Residue converted into time, will give *the Sidereal hour Afternoon of the said Transit*.

Diminish the Moons true horary Motion by the 365<sup>th</sup> part of it self, the Residue is the *Sidereal horary Motion of the Moon*:

Say Then,

*As 1 Hour or 60 Minutes,*

*To the Sidereal horary Motion;*

*So the Minutes and Seconds above any hour, at which the Ecliptical Conjunction happens,*

*To the Motion answering it.*

Take this Motion betwixt your Compasses from the Scale of Minutes or equal parts, and setting one Foot on that Point where the Line of the Moons way intersects the Axis of the Ecliptick, with the other make a Point on the said Line; if the time of the Conjunction were before the Sidereal Noon, on the Left-hand; if after it, on the Right; this shall be the place of the Moons Center at the said hour.

Take the Moons Sidereal horary Motion betwixt your Compasses from the said Scale of Minutes, and setting one Foot on the Point last made, transfer the distance in the said Line to and fro, making as many more Points at the said Distance from each other as you shall find convenient, these shall be the places of the Moons Center at other hours: Divide each hour space into 60 equal parts, to have you the place of the Moons Center to every Minute of the Sidereal hour, which if the time of the Ecliptical Conjunction were before the Sidereal Noon, are to be Numbred successively from the Left-hand to the Right, as in the Twelfth Figure; but if after it, the contrary way, or from the Right-hand to the Left.

Taking the Semidiameter of the Moon betwixt your Compasses from the Scale of Minutes, carry one Point along the Line of the Moons way, till the other turn'd about will first cut the same time in the Path of the Vertex,

Vertex, if before the Sidereal Noon in the hours on the Right-hand the Axis of the Globe, if after it, on the Left; the Point on which the fixed Foot then stands, shall be the place of the Moons Center, and shall shew the Sidereal hour from Noon at which the Star shall be covered by the Moon.

In like manner carrying the Foot of the Compasses, forward or from the Right-hand to the Left, find another Point in the said Line, on which one Foot of the Compasses being set, the other turn'd about will cut the same hour in the Path of the Vertex, this shall be the place of the Moons Center and Sidereal hour from Noon at which she shall uncover the Star, or of its Emerision from her.

Subtract the Suns Right Ascension from the Stars, the remainder turn'd into time, shall give the time of the Stars Culmination, or when it Transits the Meridian.

If the Sidereal hour of the Stars Occultation or Emerision were before the Sidereal Noon, subtract it from the time of the Stars Culmination; if it were after, add them together, so have you the true times of the Stars Occultation and Emerision.

But if the time of the visible Conjunction of the Moons Center and the Star, or some other, which she shall not cover, be required, find a Point in the Line of the Moons way, whence a Line drawn Parallel to the Axis of the Ecliptick, shall cut the same hour in the Path of the Vertex that it touches in the Line of her way, this shall be the Sidereal hour of the visible Conjunction; whence the Solar may be derived as before directed.

Take the Moons Semidiameter betwixt your Compasses from the Scale of Minutes, and setting one Foot on the Point so found in the Line of her way, with the other describe a Circle, this shall represent her Disk, and the distance of the nearest part of it from the Vertex at that time measured on the Scale of equal Parts or Minutes, will shew how many Minutes the Moons next Limb will be distant from the Star at the time of the visible Conjunction.

The following Example will make these directions easily understood.

If it be required to know at what time the Moon will be in Conjunction with *Aldebaran*, or the Southern Eye of the Bull, in *December* this instant Year, 1680.

The place of the Star will be then  $\pi$   $5^{\circ} 19' 20''$ , its Latitude South  $5^{\circ} 30'$ ; And by the Ephemerides the Moon will be in the same Longitude on the 22 of *December*, at  $6^h 30'$  Afternoon at *London*.

The Moons true place then by my Tables $\pi$	05 09 32
but at 2 hours after, or at $8^h 30'$ in $\pi$	06 24 28
Therefore the Moons true Motion in 2 hours	01 14 56
and her true horary Motion	00 37 28
Moons place at 6 Hours 30 Minutes in Antecedence of the Star	00 09 48

K

There



Therefore the Apparent Time of the Ecliptical Conjunction at *London*,  
6<sup>h</sup> 45' 42" Afternoon.

	s	o	'	"
The Inclination of the Moons Orbit then	00	05	01	49
The true place of the Node	05	23	44	00
The Argument of Latitude	08	11	25	20

Therefore,

The Inclination of the Axis of the Moons Orbit?				
to the Axis of the Ecliptick on the left hand $z e$ .	01	36	00	
The Moons Latitude South	04	46	03	
Less than the Stars	00	44	07	

Fig. 12.

The Inclination of the Axis of the Ecliptick to the	0	'	"
Axis of the Globe on the left hand, $e i$ .	09	57	30
The Stars distance from the North Pole of the Globe	74	11	30
Difference of it and the Complement of the Latitude	35	39	00
Sum of it and the said Comp. $112^{\circ} 4'$ , Comp. to $180^{\circ}$	67	16	30

Time of the $\odot$ 6 <sup>h</sup> 45' 42", converted into deg. and min. makes	101	25	30
Sun then in $\psi$ $12^{\circ} 10' \frac{1}{2}$ ; his Right Ascension	283	15	00
The Right Ascension of the Midheaven, Subtract	24	40	30
The Right Ascension of <i>Aldebaran</i>	64	24	30
The Sidereal hour of the Conjunction, before the Sidereal Noon	39	44	00
Or in time 2 <sup>h</sup> 38' 56".			

The Right Ascension of the Sun  $283^{\circ} 15'$  Subtracted from the Right Ascension of the Star  $64^{\circ} 24' \frac{1}{2}$ , leaves  $141^{\circ} 09' \frac{1}{2}$ , which converted into Time gives 9<sup>h</sup> 44' 38", the time of its Culmination or Southing.

The Moons Sidereal horary Motion	37	19
Her Motion in 38' 56" of Time	24	13

To be laid off in the Line of the Moons way from its interfection with the Axis of the Ecliptick to the left hand.

In

In the Twelfth Figure, having drawn the Semicircle  $r e H$ , let it represent one half of the Earths Disk,  $e *$  the Axis of the Ecliptick; from  $e$  set off  $e z$  on the Left-hand =  $1^{\circ} 36'$ , and  $e i$   $9^{\circ} 57' \frac{1}{2}$ : draw the Line  $* z$ , it shall represent the Axis of the Moons Orbit in the Disk, and  $* i$  the Axis of the Globe.

If making  $* i$  the Radius of a Line of Sines, you take the Sine of  $35^{\circ} 39'$ , and let it off in the Axis of the Globe from  $* to o$ , and the Sine of  $67^{\circ} 16' \frac{1}{2}$  from  $* to m$ , the middle betwixt these Points  $C$  will be the Center of the Ellipsis representing the Path, and  $C o = C m$  its Conjugate Semidiameter.

Through  $C$  strike a Line at Right-angles to the Axis of the Globe, and therein let off the Sine of  $58^{\circ} 32'$  the Complement of the Latitude, from  $C$  both ways; this shall be the Conjugate Semidiameter of the Ellipsis representing the said Path of the *Observatory*, which may now be described, and the hour Points laid down in it, as in the Projection for the Eclipse, but the hours numbered as was last directed.

The Moons Horizontal Parallax will be  $61' 31''$ , her Horizontal Semidiameter  $16' 41''$ : Make a Scale of such equal parts, as that  $* i$  the Radius of the Disk may be  $61 \frac{2}{3}$ , (such a one I have drawn under the Twelfth Figure) take there from  $44 \frac{2}{3}$ , the Moons Latitude from the Star to the North, and set it off in the Axis of the Ecliptick from  $* to N$ , through which Point draw the Line  $+ N 1$  at Right-angles to  $* z$ , this shall be the Line of the Moons way.

The Moon passeth the Axis of the Ecliptick, or will be in Conjunction with the Star  $38' 56''$  more than 2 hours before the Star will pass the Meridian; the Moons Sidereal Motion in that time is  $24' \frac{1}{2}$ ; taking therefore  $24' \frac{1}{2}$  from the Scale of Minutes betwixt your Compasses, and setting one Foot on  $N$  the interfection of the Moons way, and the Axis of the Ecliptick, transfer the said distance in the Line of the Moons way, (because the Conjunction happens before the Culmination of the Star) on the Left-hand, 't shall give the place of the Moons Center 2 hours before the Sidereal Noon, or the Culmination of the Star.

From the same Scale of Minutes taking  $37 \frac{1}{2}$  the Moons Sidereal horary Motion, and setting one Foot of the Compasses on 2, with the other make Points in the said Line, and carrying the said Extent from 3 on the Right-hand, it gives the Point 4; so have we got the Place of the Moons Center at 4, 3, 2, and 1 hours before the Star Transits the Meridian.

Dividing the spaces betwixt each of these into 60 equal parts, as in the Figure, we have the place of the Moons Center to every single Sidereal Minute of the Intermediate Time.

Taking the Moons Semidiameter betwixt your Compasses, and carrying one Foot along the Line of the Moons way thus divided; when it comes to  $\alpha$  at  $3^h 44' \frac{1}{2}$ , the other Foot turn'd about will cut the same time in the Path of the Vertex; this therefore is the time before the Culmination of the Star, at which it will be covered by the Moons preceding Limb; and carrying the said Foot unto  $\beta$  at  $2^h 40' \frac{1}{4}$  the other turn'd about again cuts the same

K 2

hour



hour in the Path of the Vertex, and therefore the Emerſion of the Star will be  $2^h 40^m \frac{1}{2}$  before it croſs the Meridian.

If now from  $9^h 44^m \frac{1}{2}$  the time of the Stars Culmination, we ſubſtract  $3^h 44^m \frac{1}{2}$  the Reſidue  $6^m$  will be the time of the Stars Occultation; and if from the ſaid time of Culmination we take away  $2^h 40^m \frac{1}{2}$ , it leaves  $7^h 04^m \frac{1}{2}$  the true time of the Stars Emerſion from the Moon.

To  $\gamma$ , the place of the Vertex at the time of the Stars Occultation, let  $\gamma\delta$  be drawn, and through the Moons Center  $\epsilon$  a Parallel to it;  $\epsilon\gamma$  ſhall be the diſtance of the Star from the loweſt Point of the Moons Periphery at the time of its Occultation, equal to  $\epsilon\gamma$  in the Thirteenth Figure; and if in like manner we draw  $\ast\delta$  from the Center of the Projection to the place of the Vertex at the Stars Emerſion from the Moon, and through her Center  $\zeta$  a Parallel to it, then will  $\zeta\delta$  be the diſtance of the Star from the loweſt Point of the Moons Periphery at its Emerſion, equal to  $\ast\delta$  in the Thirteenth Figure, in which theſe Appearances are repreſented in reſpect of the Vertical  $\pi$  paſſing by the Moons Center.

If the Times of the Occultation and Emerſion were required at ſome other place, whoſe Latitude and Difference of Meridians from London are known: Firſt the Path of the Vertex muſt be drawn, then the hours numbered in the Line of the Moons way, if the place lie to the Eaſt of London muſt be accounted ſo much leſs if the Star be ſhort of the Meridian, ſo much more if paſt it, as the difference of Meridians really is: But if the place lie to the Weſt of London, then ſo much more whiſt the Star is ſhort of the Meridian, ſo much leſs when paſt, as is the ſaid difference of Meridians.

And the time of the Occultation and Emerſion of the Star, will be eaſily found by the Method before preſcribed and employ'd.

Or the Difference of Meridians betwixt any two places whoſe Latitudes are known, may be inveſtigated by the obſerved Occultation or Emerſion of the  $\odot$  from the Moons Limb, or its diſtances and Poſitions from her at both places, the times being carefully noted, by the Method ſuggeſted before in the deſcription of the Solar Eclipse, nor is it neceſſary that the obſerved times of the ſame Appearance at both places ſhould be known; For if the time of the Stars Occultation or Emerſion at one place were accurately obſerved, at the other a diſtance and Poſition of the Star, the difference of Meridians may thence be determin'd as eaſily as if the Occultation and Emerſion were obſerved at both places, by the Method ſuggeſted in the deſcription of the Solar Eclipse.

And had we ſuch Lunar Numbers as would ſhew us the Moons true place to half a Minute, or the 12th. part of a Degree, we needed not doubt but that by this Method the Difference of Meridians betwixt the place to which the ſaid Numbers ſhould be fitted, and any other, where ſome Appearance of an Appulſe of the Moon to any known fixed Star ſhould be obſerved, might be readily obtained by one only accurate obſervation; For the places of the fixed Stars I have hopes may be rectified to that exactneſs; The Work, by His MAJESTIES Princely Care for the Improvement of NAVIGATION, being ſomewhile ſince begun and carried on as far as the

the Time and the Obſervers Accommodations would permit; Nor is it to be feared, but that the Motions of the Moon may be rectified to as great exactneſs by the means of thoſe many Lunar Obſervations, which have been frequently made at the Obſervatory by the ſame Perſon, and by others elſewhere, to far greater exactneſs than could formerly be hoped for, and that without omitting any opportunity when the ſeaſon permitted, except when the Obſervers have been prevented by infirmities or indiſpenſable occaſions.

I have Numbered above 200 Fixed Stars in Tycho's Catalogue that lie in the Moons way, and may all of them be Eclipsed by her in one Revolution of her Node; The Greenwich Obſervations make above 300: There can ſcarce happen 2 Nights together, but ſome or other of them will be Eclipsed in one place or other of the Earth. Theſe Appulſes ſeem therefore one of the beſt expedients that can be propounded for the diſcovery of the LONGITUDE, and ſurely ſince we have found and Taught to eaſy a way to Conſtruct them, and that too perfectly Geometrical, thoſe who are ſo urgent upon the *Aſtronomer* for a good Method to find it, will not think much to be at the pains to Learn and Underſtand this, ſeeing it may be pracliſ'd by one Obſerver if accommodated with convenient Inſtruments; And I hope alſo that thoſe Ingenious Perſons who have employ'd their pains and Studies to correct the *Old*, or find a better Theory of the Moons Motions, will be hereby encouraged to proſecute their uſeful Endeavours, conſidering both the facility of this Method, the Benefit is thence like to accrue to Mankind, and the Reputation and Credit to themſelves and their Memories.

## SECTION VIII.

HAving ſhewn in the preceding Sections how to find the places on the Earth, and Times there, where any of the principal Phases of a Solar Eclipse ſhall appear, by Calculation; as alſo how the Times of any Appearance of a Solar Eclipse or Stellar may be determin'd in any given Latitude and Longitude by Conſtruction; It remains now, that I ſhew how the Times of the Principal Appearances and quantity of any Lunar Eclipse may alſo be found.

In the Fourth Section of this part I have taught how to find the Mean Time of the Mean oppoſition of the Luminaries, the Apparent Time of the True, their places then, and hourly Motions, their Horizontal Parallaxes and Semidiameters, with the neareſt diſtance of the Moons Center from the Center of the Disk, and ſhadow, in her paſſage over either; I ſhall not need here therefore to repeat the directions how to find them; admit them known, and then,

Add the Moons Horizontal Parallax and the Sins (which I ſuppoſe always 10) together, from which Sum ſubtract the Sins Semidiameter, the remainder ſhall be the Semidiameter of the Earths ſhadow.

Add.







*At which Time,*

	s	°	'	"
The Mean Anomaly of the Earth is	02	01	02	12
The Suns true place	12	06	14	48
The Annual Argument	08	06	21	16
The Moons Mean Anomaly	11	10	51	26
Her true place in her Orbit	X	06	14	48
Her true hourly Motion 32' 01", from the Earth	00	00	29	36

Argument of Latitude	05	24	13	04
----------------------	----	----	----	----

	h	'	"
Time of Reduction	00	03	04
Mean Time of the ☿ in the Ecliptick	15	13	40
Mean time of the middle of Eclipse	15	19	48

Equation of Days subtract from the Mean time	00	00	28
Apparent time of the middle of the Eclipse	15	19	20

	°	'	"
Moons Horizontal Parallax	00	56	47
Suns Semidiameter subtracted	00	15	58

Semidiameter of the shadow	00	40	49
Moons Semidiameter	00	15	25

Their Sum	00	56	14
The Moons Latitude North subtract	00	30	12

The parts deficient	00	26	02
Digits Eclipsed 10 Digits 8'			

Angle of Incidence	57	31	00
Motion of Semiduration	00	47	26

	h	'	"
Time of Semiduration	01	36	09

There

*In Eclipse of the Moon  
1681 August the 19<sup>th</sup> in the Morning.*

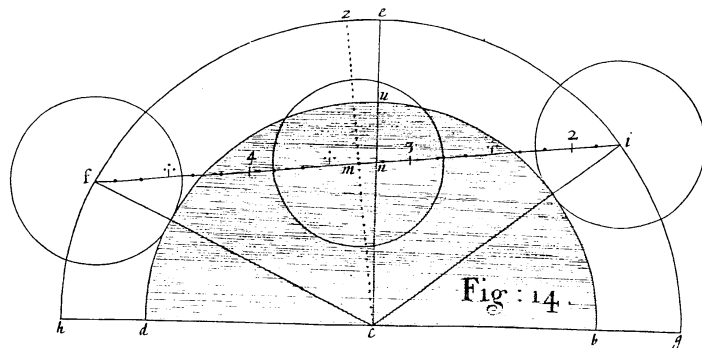


Fig: 14

10 20 30 40 50

*A Scale of Minutes.*

*between page 72 and 73. the Doctrine of the Sphere.*



Therefore,

	h	'	"	
The beginning of the Eclipse at	1	43	11	After the Midnight fol-
Ecliptical $\odot$ of the $\odot$ and $\text{D}$ . . .	3	13	12	lowing the Eighteenth
Middle or greatest Obscuration . .	3	19	20	of <i>August</i> , or the 19th.
End . . . . .	4	55	26	Day in the Morning.
Total duration . . . . .	3	12	18	

The Times of any Appearance of a Lunar Eclipse may be found by Construction, as the Times of the general Phases of the Solar were before, and the directions given for the Protraction of that will likewise serve for the Delineation of this. For Example, if it were required to represent *in Plano* the Lunar Eclipse, of which I have now found the Times of the principal Phases by Calculation; Having made a Scale of Minutes or equal parts for your purpose, take thence the Sum of the Semidiameters of the Moon and shadow  $56^{\frac{2}{3}}$ , and drawing first a straight Line  $bcg$ , which may represent an Arch of the Ecliptick, upon Paper; chuse therein a Center  $c$ , and setting one Foot of the Compasses thereon, with the other describe a Semicircle  $bxeg$  (if the Moon have North Latitude) above, if South, beneath the Line; but if her Latitude be not more than 5 Minutes, an entire Circle; in the Periphery of this the Moons Center shall be found at the Beginning and End of the Eclipse.

Taking from the same Scale the Semidiameter of the shadow  $40^{\frac{2}{3}}$  betwixt your Compasses, set one Foot on the Center  $c$ , and with the other describe the Semicircle  $dub$ , this shall represent half the shadow.

From  $c$  raise the Line  $ce$  Perpendicular to the Ecliptick  $dg$ , and then making  $ce$  the Radius of a Line of Chords, take the Chord of  $05^{\circ} 41'$  (the Angle which the Perpendicular to the Moons way makes with the Ecliptick) and setting it off from  $e$  to  $z$ , draw the Line  $zc$ , this shall be the said Perpendicular.

From the Scale of Minutes take  $30^{\frac{1}{2}}$  betwixt your Compasses, and transfer them in the Line  $cz$ , from  $c$  to  $m$ , through  $m$  draw the Line  $imf$  at Right-angles to  $zc$ , this shall be the Line of the Moons way, and the Points  $i, m$ , and  $f$ , the places of her Center at the Beginning, Middle, and End of the Eclipse.

From the Center  $c$  draw the Lines  $ci$  and  $cf$ , the Angle  $mci = mcf$  formed hereby shall be the Angle of Incidence.



The middle of the Eclipse happens  $19^{\circ} 20'$  after 3 in the Morning, the Moons horary Motion from the Earth is  $29' 36''$ ; therefore in  $19^{\circ} 20'$ , her Motion from the Earth  $09^{\circ} 32''$ ; take therefore  $09^{\circ} 32''$  from the Scale of Minutes betwixt your Compasses, and setting one Foot on  $m$ , with the other make a mark on the Line of the Moons way on the Left-hand, this shall be the place of the Moons Center at 3 hours after Midnight, or in the Morning.

Taking from the same Scale  $29^{\circ} 24'$  the Moons hourly Motion from the Earth, set it off in the said Line from 3. on both sides, it gives you the Points 2 and 4, or the place of the Moons Center at 2 and 4 a Clock in the Morning.

And if the spaces betwixt these be divided into 60 parts, and the Residue of the Line till it touch the utmost Circle, in the same manner, the Minutes there cut shall shew the Beginning and End of the Eclipse.

In the Figure I have divided the Line of the Moons way onely to every 10 Minutes, it being sufficient for the Explication of the Method; which I esteem far more troublesome than a Calculation, and therefore should rather perswade the use of the Pen, than the Compasses to determin the Appearances of Lunar Eclipses.

In the Calculation of which, as also of the Principal Phases of the Solar, I must acquaint my Reader, that tho I have employ'd the Line of the Moons way, and that which connects her Center with the Center of the Disk, or shadow, at their nearest distance, as if they were perfect freight Lines, yet are they really small Arches of great Circles, whose Curvities are so little, that their difference from freight Lines is imperceptible, and the Error, that is caused by my using them as such, altogether inconsiderable.

The difference of Meridians betwixt any two places on the Earths Globe, may be readily obtained by the observation of the same Appearance of a Lunar Eclipse, or the Occultation or Emerision of the same Spot from the Earths shadow accurately noted at both places, for the difference of the observed Times shall be the difference of Meridians betwixt those two places in Time, of which that shall be to the East from the other, where the Noted time is the most from Noon: For Example in the Year 1678, October the 19th. Old-Style, the end of a Lunar Eclipse was accurately Noted at His *MAJESTIES* Observatory at Greenwich at  $10^h 10' 38''$  Afternoon; but at *Paris* at  $10^h 20'$ ; wherefore the difference of Meridians betwixt the Observatories of Greenwich and Paris by this Observation should be  $9' 22''$  of Time: We observed likewise in the same Eclipse that the Spot called *Byzantium* by *Hevelius* was first covered by the shadow of Greenwich at  $7^h 09' 14''$ , but at *Paris* its Occultation was Noted at  $7^h 18' 28''$ , whence the difference is found onely  $9' 14''$ , or  $2^{\circ} 16'$ , and so much we have determin'd the difference of Meridians betwixt the Observatories of *Paris* and *Greenwich*, by comparing 22 several Appearances carefully observed in the same Eclipse at both places.

As by Lunar Eclipses, so also by the Eclipses of *Jupiters* Satellits, the difference of the observed Moments of the Occultation or Emerision of a Satellit from his shadow noted carefully in two distant places will be the difference of Meridians betwixt those two places in Time; But I cannot hope that this Method shall prove of much use to the Ingenious *Sea-man*, because the Observations require long Telescopes which in a Ship will hardly be manageable. Nor can we expect to find the difference of Meridians by one only Observation of a Satellit Eclipse, as we have hopes we may by a Lunar, by reason that as yet the inequalities in their Motions, and the time required for the Transmission of Light from the Planet to our Earth are unknown; Nay their Mean Motions are scarce so exactly stated, but that we may justly suspect them erroneous; Ommitting these therefore, the best Method for the discovery of the Longitude will be in my opinion by the Moons *Appulses* to, or observed distances from fixed Stars, upon which account I would recommend the Improvement and Correction of her Theory, with the *Daltrine* and *Construccion* of *Appulses*, to the Study of the Ingenious Astronomer and Sea-men.



ASTRONOMICAL  
**TABLES**  
For finding the true places of  
**LUMINARIES,**  
AND THEIR  
**ECLIPSES,**  
AT ALL TIMES.

J. Mathefin à Sole Fundes.



## TABLE

I.

II.

*The Equations of the Apparent Time.*

Sign.	Subtract from the Apparent, if the Suns Mean Anomaly be,						Subtra. from the Apparent.					
	0	1	2	3	4	5	0	1	2	3	4	5
0	00	3	46	34	7	40	6	42	3	54	30	
10	08	3	53	6	38	7	40	6	38	3	47	29
20	16	3	59	6	42	7	40	6	34	3	40	28
30	23	4	06	6	46	7	40	6	35	3	33	27
40	31	4	13	6	49	7	39	6	26	3	25	26
50	39	4	19	6	53	7	39	6	21	3	18	25
60	47	4	26	6	57	7	38	6	17	3	11	24
70	55	4	32	7	00	7	38	6	12	3	03	23
80	03	4	38	7	03	7	37	6	07	2	56	22
90	10	4	45	7	06	7	36	6	02	2	48	21
100	18	4	51	7	09	7	34	5	57	2	40	20
110	26	4	57	7	12	7	33	5	52	2	33	19
120	34	5	03	7	14	7	32	5	46	2	25	18
130	41	5	09	7	17	7	30	5	41	2	17	17
140	49	5	15	7	19	7	28	5	36	2	09	16
150	57	5	20	7	22	7	26	5	30	2	01	15
160	04	5	26	7	24	7	24	5	24	1	53	14
170	12	5	32	7	26	7	22	5	18	1	45	13
180	19	5	37	7	28	7	20	5	12	1	37	12
190	27	5	42	7	30	7	18	5	06	1	29	11
200	34	5	48	7	31	7	15	5	00	1	21	10
210	42	5	53	7	33	7	12	4	54	1	13	9
220	49	5	58	7	34	7	10	4	48	1	05	8
230	56	6	03	7	35	7	07	4	41	0	57	7
240	03	6	07	7	36	7	04	4	35	0	49	6
250	11	6	12	7	37	7	00	4	28	0	41	5
260	18	6	17	7	38	6	57	4	22	0	33	4
270	25	6	21	7	39	6	54	4	15	0	24	3
280	32	6	26	7	40	6	50	4	08	0	16	2
290	39	6	30	7	40	6	46	4	01	0	08	1
300	46	6	34	7	40	6	42	3	54	0	00	0
	11	10	9	8	7	6						
Add to the Apparent Time.												

## TABLE III.

*A TABLE of the Earths Mean Motions, the place of her Perihelion, and the recess of the Equinoxes from the first \* of v.*

Years of Christ current.	Mean Motion of the Earth from the Equinox.	The Perihelion from the vernal Equinox.	Common Years.	Mean Motion for Compleat Years.	The Perihelion and fixt Stars.
1	9 07 55 51	2 13 31 40	1	11 29 45 40	00 00 00 50
1501	9 19 13 29	3 04 21 40	2	11 29 31 20	00 00 01 40
1581	9 19 49 38	3 05 28 20	3	11 29 17 00	00 00 02 30
1601	9 19 58 40	3 05 45 00	4	00 00 01 48	00 00 03 20
1621	9 20 07 42	3 06 01 40	5	11 29 47 28	00 00 04 10
1641	9 20 16 44	3 06 18 20	6	11 29 33 08	00 00 05 00
1661	9 20 25 46	3 06 35 00	7	11 29 18 48	00 00 05 50
1681	9 20 34 48	3 06 51 40	8	00 00 03 36	00 00 06 40
82	9 20 20 28	3 06 52 30	9	11 29 49 16	00 00 07 30
83	9 20 06 08	3 06 53 20	10	11 29 34 56	00 00 08 20
84	9 19 51 48	3 06 54 10	11	11 29 20 36	00 00 09 10
85	9 20 36 36	3 06 55 00	12	00 00 05 25	00 00 10 00
86	9 20 22 16	3 06 55 50	13	11 29 51 05	00 00 10 50
87	9 20 07 56	3 06 56 40	14	11 29 36 45	00 00 11 40
88	9 19 53 36	3 06 57 30	15	11 29 22 25	00 00 12 30
89	9 20 38 25	3 06 58 20	16	00 00 07 13	00 00 13 20
90	9 20 24 05	3 06 59 10	17	11 29 52 53	00 00 14 10
91	9 20 09 45	3 07 00 00	18	11 29 38 33	00 00 15 00
92	9 19 55 25	3 07 00 50	19	11 29 24 13	00 00 15 50
93	9 20 39 13	3 07 01 40	20	00 00 09 02	00 00 16 40
94	9 20 25 53	3 07 02 30	40	00 00 18 04	00 00 33 20
95	9 20 11 33	3 07 03 20	60	00 00 27 06	00 00 50 00
96	9 19 57 13	3 07 04 10	80	00 00 36 08	00 01 06 40
97	9 20 42 02	3 07 05 00	100	00 00 45 10	00 01 23 20
98	9 20 27 42	3 07 05 50	200	00 01 30 21	00 02 46 40
99	9 20 13 22	3 07 06 40	300	00 02 15 31	00 04 10 00
1700	9 19 59 02	3 07 07 30	400	00 03 00 42	00 05 33 20
1701	9 20 43 50	3 07 08 20	500	00 03 45 52	00 06 56 40
1721	9 20 52 53	3 07 25 00	600	00 04 31 03	00 08 20 00
1741	9 21 01 54	3 07 41 40	700	00 05 16 13	00 09 43 20
1761	9 21 10 56	3 07 58 20	800	00 06 01 24	00 11 06 40
1781	9 21 19 58	3 08 15 00	900	00 06 46 34	00 12 29 00
1801	9 21 29 01	3 08 31 40	1000	00 07 31 45	00 13 53 20
			2000	00 15 03 30	00 27 46 40
			3000	00 22 35 15	00 41 40 40
			4000	01 00 07 01	00 55 33 20
			5000	01 07 38 46	00 09 26 40



### TABLE IV.

### A TABLE of the Earths Mean Motions

January.				February.				March.				April.			
Earth's Mean Motion.	M	P.		Earth's Mean Motion.	M	P.		Earth's Mean Motion.	M	P.		Earth's Mean Motion.	M	P.	
" S O F " "				" S O F " "				" S O F " "				" S O F " "			
10 00 59 08	00	1	01 32 27	04	1	29 08 20	08	2	29 41 38	12	3	29 41 38	12	3	29 41 38
20 01 58 17	00	1	02 31 25	05	2	00 07 28	08	3	00 40 46	13	3	00 40 46	13	3	00 40 46
30 02 57 25	00	1	03 30 43	05	2	01 06 36	08	3	01 39 55	13	3	01 39 55	13	3	01 39 55
40 03 56 33	01	1	04 29 52	05	2	02 05 43	09	3	02 39 03	13	3	02 39 03	13	3	02 39 03
50 04 55 42	01	1	05 29 00	05	2	03 04 53	09	3	03 38 11	13	3	03 38 11	13	3	03 38 11
60 05 54 50	01	1	06 28 08	05	2	04 04 01	09	3	04 37 20	13	3	04 37 20	13	3	04 37 20
70 06 53 58	01	1	07 27 16	05	2	05 03 10	09	3	05 36 27	13	3	05 36 27	13	3	05 36 27
80 07 53 07	01	1	08 26 25	05	2	06 02 18	09	3	06 35 36	13	3	06 35 36	13	3	06 35 36
90 08 52 15	01	1	09 25 33	06	2	07 01 26	09	3	07 34 45	13	3	07 34 45	13	3	07 34 45
100 09 51 23	01	1	10 24 41	06	2	08 00 35	09	3	08 33 53	14	3	08 33 53	14	3	08 33 53
110 10 50 32	02	1	11 23 50	06	2	08 59 43	10	3	09 33 01	14	3	09 33 01	14	3	09 33 01
120 11 49 40	02	1	12 22 58	06	2	09 58 51	10	3	10 32 10	14	3	10 32 10	14	3	10 32 10
130 12 48 48	02	1	13 22 06	06	2	10 58 00	10	3	11 31 18	14	3	11 31 18	14	3	11 31 18
140 13 47 57	02	1	14 21 15	06	2	11 57 08	10	3	12 30 26	14	3	12 30 26	14	3	12 30 26
150 14 47 05	02	1	15 20 23	06	2	12 56 16	10	3	13 29 34	14	3	13 29 34	14	3	13 29 34
160 15 46 13	02	1	16 19 31	05	2	13 55 25	0	3	14 28 43	14	3	14 28 43	14	3	14 28 43
170 16 45 22	02	1	17 18 40	07	2	14 54 33	10	3	15 27 51	15	3	15 27 51	15	3	15 27 51
180 17 44 30	02	1	18 17 48	07	2	15 53 41	11	3	16 27 05	15	3	16 27 05	15	3	16 27 05
190 18 43 38	03	1	19 16 56	07	2	16 52 50	11	3	17 26 08	15	3	17 26 08	15	3	17 26 08
200 19 42 47	03	1	20 16 04	07	2	17 51 58	11	3	18 25 16	15	3	18 25 16	15	3	18 25 16
210 20 41 55	04	1	21 15 13	07	2	18 51 06	11	3	19 24 24	15	3	19 24 24	15	3	19 24 24
220 21 41 03	04	1	22 14 21	07	2	19 50 15	11	3	20 23 33	15	3	20 23 33	15	3	20 23 33
230 22 40 12	04	1	23 13 30	07	2	20 49 23	11	3	21 22 41	15	3	21 22 41	15	3	21 22 41
240 23 39 20	04	1	24 12 38	08	2	21 48 31	11	3	22 21 49	16	3	22 21 49	16	3	22 21 49
250 24 38 28	04	1	25 11 46	08	2	22 47 40	11	3	23 20 58	16	3	23 20 58	16	3	23 20 58
260 25 37 37	04	1	26 10 55	08	2	23 46 48	12	3	24 20 06	16	3	24 20 06	16	3	24 20 06
270 26 36 45	04	1	27 10 03	08	2	24 45 56	12	3	25 19 14	16	3	25 19 14	16	3	25 19 14
280 27 35 53	04	1	28 09 11	08	2	25 45 05	12	3	26 18 23	16	3	26 18 23	16	3	26 18 23
290 28 35 02	04	1			2	26 44 13	12	3	27 17 31	16	3	27 17 31	16	3	27 17 31
300 29 34 10	04	1			2	27 43 21	12	3	28 16 39	16	3	28 16 39	16	3	28 16 39
310 00 33 18	04	1			2	28 42 30	12	3							

*to every Day in the Year.*

May.				June.				July.				August.							
Days	Earth's Motion.	Mean P.		Earth's Motion.	Mean P.			Earth's Motion.	Mean P.			Earth's Motion.	Mean P.						
	s	o	f	u	u			s	o	f	u	u	s	o	f	u	u		
13	29	15	48	17	4	29	49	06	21	5	29	23	16	25	6	29	56	34	29
24	00	14	56	17	5	00	48	14	21	6	00	22	24	25	7	00	55	42	29
34	01	14	04	17	5	01	47	23	21	6	01	21	32	25	7	01	54	51	29
44	02	13	13	17	5	02	46	31	21	6	02	20	40	25	7	02	53	59	30
54	03	12	21	17	5	03	45	39	21	6	03	19	49	25	7	03	53	07	30
64	04	11	29	17	5	04	44	48	21	6	04	18	57	26	7	04	52	16	30
74	05	10	38	17	5	05	43	56	22	6	05	18	06	26	7	05	51	24	30
84	06	09	46	17	5	06	43	04	22	6	06	17	14	26	7	06	50	32	30
94	07	08	54	18	5	07	42	13	22	6	07	16	22	26	7	07	49	41	30
104	08	08	03	18	5	08	41	21	22	6	08	15	31	26	7	08	48	49	30
114	09	07	11	18	5	09	40	29	22	6	09	14	39	26	7	09	47	57	31
124	10	06	19	18	5	10	39	38	22	6	10	13	47	26	7	10	47	06	31
134	11	05	28	18	5	11	38	46	22	6	11	12	56	27	7	11	46	14	31
144	12	04	36	18	5	12	37	54	23	6	12	12	04	27	7	12	45	22	31
154	13	03	44	18	5	13	37	03	23	6	13	11	12	27	7	13	44	31	31
164	14	02	53	19	5	14	36	11	23	6	14	10	21	27	7	14	43	39	31
174	15	02	01	19	5	15	35	19	23	6	15	09	29	27	7	15	42	47	31
184	16	01	09	19	5	16	34	28	23	6	16	08	37	27	7	16	41	56	31
194	17	00	18	19	5	17	33	36	23	6	17	07	46	27	7	17	41	04	32
204	17	59	26	15	5	18	32	44	23	6	18	06	54	28	7	18	40	12	32
214	18	58	34	15	5	19	31	53	24	6	19	06	02	28	7	19	39	21	32
224	19	57	42	19	5	20	31	01	24	6	20	05	11	28	7	20	38	29	32
234	20	56	51	20	5	21	30	09	24	6	21	04	19	28	7	21	37	37	32
244	21	55	59	20	5	22	29	18	24	6	22	03	27	28	7	22	36	46	32
254	22	55	0	20	5	23	28	26	24	6	23	02	36	28	7	23	35	54	32
264	23	54	16	20	5	24	27	33	24	6	24	01	44	28	7	24	35	02	33
274	24	53	24	20	5	25	26	41	24	6	25	00	52	28	7	25	34	11	33
284	25	52	33	20	5	26	25	51	24	6	26	00	01	29	7	26	33	19	33
294	26	51	41	20	5	27	24	58	25	6	26	59	09	29	7	27	32	27	33
304	27	50	49	21	5	28	24	06	25	6	27	58	17	29	7	28	31	36	33
314	28	49	58	21						6	28	57	26	29	7	29	30	44	33

N



A TABLE of the Earths Mean Motions.

Days	Septemb.				M	October.				M	November.				M	December.				M
	Earth's Mean Motion.					Earth's Mean Motion.					Earth's Mean Motion.					Earth's Mean Motion.				
1	00 29 52	35				00 04 02	38				10 00 37	20	42			11 00 11	30	46		
2	01 29 01	34				01 03 10	38				10 01 36	29	42			11 01 10	38	46		
3	02 28 09	34				02 02 19	38				10 02 35	37	42			11 02 09	47	46		
4	03 27 17	34				03 01 27	38				10 03 34	45	42			11 03 08	53	46		
5	04 26 36	34				04 00 35	38				10 04 33	54	42			11 04 08	03	46		
6	05 25 34	34				04 59 44	38				10 05 33	02	42			11 05 07	12	47		
7	06 24 42	34				05 58 52	38				10 06 32	10	43			11 06 06	20	47		
8	07 23 51	34				06 58 00	38				10 07 31	19	43			11 07 05	28	47		
9	08 22 59	35				07 57 08	39				10 08 30	27	43			11 08 04	37	47		
10	09 22 07	35				08 56 17	35				10 09 29	35	43			11 09 03	45	47		
11	10 21 16	35				09 55 25	39				10 10 28	44	43			11 10 02	53	47		
12	11 20 24	35				10 54 34	39				10 11 27	52	43			11 11 02	02	47		
13	12 19 32	35				11 53 42	39				10 12 27	00	43			11 12 01	10	48		
14	13 18 41	35				12 52 50	39				10 13 26	09	44			11 13 00	18	48		
15	14 17 49	35				13 51 59	39				10 14 25	17	44			11 13 59	27	48		
16	15 16 57	36				14 51 07	40				10 15 24	25	44			11 14 58	35	48		
17	16 16 05	36				15 50 15	40				10 16 23	34	44			11 15 57	43	48		
18	17 15 14	36				16 49 24	40				10 17 22	42	44			11 16 56	52	48		
19	18 14 22	36				17 48 32	40				10 18 21	50	44			11 17 56	00	48		
20	19 13 30	36				18 47 40	40				10 19 20	58	44			11 18 55	08	48		
21	20 12 39	36				19 46 49	40				10 20 20	07	44			11 19 54	17	49		
22	21 11 47	36				20 45 57	40				10 21 19	15	45			11 20 53	25	49		
23	22 10 55	36				21 45 05	40				10 22 18	24	45			11 21 52	33	49		
24	23 10 04	37				22 44 14	41				10 23 17	32	45			11 22 51	42	49		
25	24 09 12	37				23 43 22	41				10 24 16	40	45			11 23 50	50	49		
26	25 08 20	37				24 42 30	41				10 25 15	49	45			11 24 49	58	49		
27	26 07 29	37				25 41 38	41				10 26 14	57	45			11 25 49	07	49		
28	27 06 37	37				26 40 47	41				10 27 14	05	45			11 26 48	15	49		
29	28 05 45	37				27 39 55	41				10 28 13	13	46			11 27 47	23	50		
30	29 04 54	37				28 39 04	41				10 29 12	22	46			11 28 46	31	50		
31						29 38 12	42									11 29 45	40	50		

In the Leap-year after February add a Day to the given time, and its Motion to the Motions Collected.

A TABLE of the Earths Mean Motions to Hours, and Parts of an Hour.

H.	°	'	"		H.	°	'	"
0	0	00	00		30	1	13	55
1	0	02	28		31	1	16	23
2	0	04	56		32	1	18	51
3	0	07	24		33	1	21	19
4	0	09	51		34	1	23	47
5	0	12	19		35	1	26	14
6	0	14	47		36	1	28	42
7	0	17	15		37	1	31	10
8	0	19	43		38	1	33	38
9	0	22	11		39	1	36	06
10	0	24	38		40	1	38	34
11	0	27	06		41	1	41	02
12	0	29	34		42	1	43	29
13	0	32	02		43	1	45	57
14	0	34	30		44	1	48	25
15	0	36	58		45	1	50	53
16	0	39	25		46	1	53	21
17	0	41	53		47	1	55	49
18	0	44	21		48	1	58	16
19	0	46	49		49	2	00	44
20	0	49	17		50	2	03	12
21	0	51	45		51	2	05	40
22	0	54	13		52	2	08	08
23	0	56	40		53	2	10	36
24	0	59	08		54	2	13	03
25	1	01	36		55	2	15	31
26	1	04	04		56	2	17	59
27	1	06	32		57	2	20	27
28	1	09	00		58	2	25	55
29	1	11	27		59	2	22	23
30	1	13	55		60	2	25	50



A TABLE of the Equations of the Earths Orbit.

Subtract.										
Sign. 0	1	2	3	4	5					
0 0 00 00	0 56 28	1 38 33	1 54 59	1 40 37	0 58 33	30				
1 0 01 57	0 58 11	1 39 33	1 54 59	1 39 37	0 56 46	29				
2 0 03 55	0 59 52	1 40 31	1 55 00	1 38 35	0 54 59	28				
3 0 05 53	1 01 33	1 41 28	1 54 57	1 37 32	0 53 11	27				
4 0 07 51	1 03 12	1 42 24	1 54 52	1 36 27	0 51 22	26				
5 0 09 49	1 04 50	1 43 17	1 54 45	1 35 19	0 49 31	25				
6 0 11 47	1 06 27	1 44 09	1 54 36	1 34 10	0 47 40	24				
7 0 13 44	1 08 03	1 44 58	1 54 25	1 32 59	0 45 48	23				
8 0 15 40	1 09 38	1 45 46	1 54 12	1 31 47	0 43 55	22				
9 0 17 37	1 11 12	1 46 31	1 53 57	1 30 32	0 42 01	21				
10 0 19 34	1 12 45	1 47 16	1 53 38	1 29 16	0 40 06	20				
11 0 21 30	1 14 16	1 47 58	1 53 18	1 27 58	0 38 11	19				
12 0 23 25	1 15 46	1 48 38	1 52 57	1 26 39	0 36 14	18				
13 0 25 21	1 17 14	1 49 17	1 52 34	1 25 18	0 34 17	17				
14 0 27 16	1 18 42	1 49 53	1 52 08	1 23 55	0 32 20	16				
15 0 29 10	1 20 08	1 50 27	1 51 40	1 22 31	0 30 22	15				
16 0 31 04	1 21 32	1 50 59	1 51 09	1 21 05	0 28 23	14				
17 0 32 57	1 22 55	1 51 29	1 50 37	1 19 38	0 26 24	13				
18 0 34 50	1 24 16	1 51 58	1 50 03	1 18 08	0 24 24	12				
19 0 36 43	1 25 37	1 52 24	1 49 28	1 16 38	0 22 23	11				
20 0 38 35	1 26 56	1 52 48	1 48 50	1 15 06	0 20 22	10				
21 0 40 25	1 28 12	1 53 11	1 48 09	1 13 32	0 18 21	9				
22 0 42 15	1 29 27	1 53 31	1 47 27	1 11 57	0 16 20	8				
23 0 44 05	1 30 41	1 53 49	1 46 43	1 10 22	0 14 19	7				
24 0 45 54	1 31 53	1 54 06	1 45 56	1 08 44	0 12 16	6				
25 0 47 42	1 33 04	1 54 19	1 45 08	1 07 05	0 10 14	5				
26 0 49 28	1 34 12	1 54 31	1 44 18	1 05 25	0 08 12	4				
27 0 51 15	1 35 20	1 54 41	1 43 25	1 03 44	0 06 09	3				
28 0 53 00	1 36 26	1 54 50	1 42 31	1 02 01	0 04 06	2				
29 0 54 44	1 37 30	1 54 55	1 41 35	1 00 18	0 02 03	1				
30 0 56 28	1 38 33	1 54 59	1 40 37	0 58 33	0 00 00	0				
Sign. 11	10	9	8	7	6					
Add.										

A TABLE of the Mean Motions of the Moon, her Apogee and Node.

Years of Civil	Moons Motion from the vernal Equinox.	Motion of the Apogee from the Equinox.	Motion of the Node from the Equinox.	Com. Years Comp	Moons Mean Motion.	Mean Motion of the Apogee.	Mean Motion of the Node.
	S O P H	S O P H	S O P H		S O P H	S O P H	S O P H
1501	02 02 30 22	09 12 11 51	08 28 33 16		104 09 23 03	01 10 39 50	00 19 59 43
1502	01 29 40 22	03 29 41 51	01 25 46 34		2 08 18 46 05	02 21 19 39	01 08 39 26
1503	07 23 55 18	04 15 01 51	10 08 25 40		3 00 28 09 08	04 01 59 29	01 27 59 09
1504	00 07 29 02	07 18 51 51	09 11 35 27		4 05 20 42 45	05 12 46 00	02 17 22 03
1505	21 04 21 02 46	10 22 41 51	08 14 45 15		5 10 00 05 47	06 23 25 50	03 06 41 46
1506	41 09 04 36 30	11 26 31 51	07 17 35 01		6 02 09 25 49	08 04 05 39	03 26 01 29
1507	61 01 18 10 14	05 00 21 51	06 21 04 47		7 06 18 51 52	09 14 45 29	04 15 21 12
1508	81 06 01 43 58	08 04 11 51	05 24 14 33		8 11 11 25 29	10 25 32 00	05 04 44 05
1509	10 11 07 01	09 14 51 41	05 04 14 50		9 03 20 48 32	00 06 11 50	05 24 03 48
1510	32 20 30 03	10 25 31 30	04 15 35 07		10 08 00 11 34	01 16 51 39	06 13 23 32
1511	06 29 53 06	00 06 11 20	03 26 15 22		11 00 09 34 37	02 27 31 29	07 02 43 15
1512	11 22 26 43	01 16 57 51	03 06 52 30		12 05 02 18 15	04 08 18 00	07 22 06 08
1513	01 49 45	02 27 37 40	02 18 32 47		13 09 11 31 17	05 18 57 50	08 11 25 51
1514	08 11 12 47	04 08 17 30	01 28 13 04		14 01 20 54 20	06 29 37 39	09 00 45 34
1515	00 19 35 50	05 18 57 20	01 08 53 21		15 06 00 17 22	08 10 17 29	09 20 05 17
1516	05 13 09 27	06 29 43 51	00 19 30 28		16 10 22 51 00	09 21 04 00	10 09 28 11
1517	09 22 32 30	08 10 23 41	00 00 10 45		17 03 02 14 02	11 01 43 50	10 28 47 54
1518	01 01 55 32	09 21 03 30	11 10 51 01		18 07 11 37 04	00 12 23 39	11 18 07 30
1519	11 18 35 11	01 01 43 20	10 22 31 18		19 11 21 00 07	01 23 03 29	00 07 27 20
1520	11 04 02 13	10 12 29 51	10 02 08 25		20 04 13 33 46	03 03 50 00	00 26 50 13
1521	03 12 14 15	01 23 09 41	09 12 48 42		40 08 27 07 28	06 07 40 03	01 23 40 27
1522	07 22 38 18	03 03 49 30	08 23 28 58		60 01 10 41 12	09 11 30 03	02 20 30 40
1523	00 02 01 20	04 14 29 20	08 04 09 16		80 05 24 14 56	00 15 20 08	03 17 20 54
1524	04 24 34 58	05 25 15 51	07 14 46 22		100 01 07 48 40	03 19 10 00	04 14 11 07
1525	08 09 03 58 00	07 05 55 41	06 25 27 39		200 08 15 37 26	07 08 20 00	08 28 12 13
1526	09 01 13 21 02	08 17 05 30	06 06 07 56		300 06 23 26 00	10 27 30 00	01 12 33 20
1527	05 22 44 05	09 27 15 20 25	05 16 47 15		400 05 01 14 40	02 16 40 00	05 26 44 27
1528	10 15 17 44 11	08 01 51 04	27 24 25		500 03 09 03 20	06 05 50 00	10 10 55 33
1529	02 28 51 26	02 11 51 51	04 00 34 08		600 01 16 52 00	09 25 00 00	02 25 06 40
1530	07 12 25 10	05 15 41 51	03 03 43 55		700 11 24 40 40	01 14 10 00	07 09 17 47
1531	11 25 58 54	08 19 31 51	02 06 53 41		800 10 02 29 20	05 03 20 00	11 23 28 53
1532	04 09 32 38	11 23 21 51	01 10 03 28		900 08 10 18 00	08 22 30 00	04 07 40 00
1533	08 23 06 22	02 27 11 51	00 13 13 14		1000 06 13 06 40	00 11 40 00	05 21 51 07
1534	01 06 13 20	03 20 00 23	00 05 13 42 14		2000 01 06 13 20	00 23 00 05	05 13 42 14
1535	03 24 20 00	01 05 00 00	02 05 33 27		3000 02 24 20 00	01 05 00 00	02 05 33 27
1536	00 12 26 40	01 16 40 00	10 17 24 21		4000 02 12 26 40	01 16 40 00	10 17 24 21
1537	00 00 00 00	00 33 20 01	28 20 00		5000 00 00 00 00	00 33 20 01	28 20 00 00



A TABLE of the Mean Motions of the Moon,

January.							February.						
Days.	Moons Mean Motion.			Apoge.		Node Retrogr.	Days.	Moons Mean Motion.			Apoge.		Node Retrogr.
	S	O	P	H	M			S	O	P	H	M	
1	00	13	10	35	0	06	41	02	01	38	41	3	33
2	00	26	21	10	0	13	22	0	06	21	20	2	06
3	01	09	31	45	0	20	03	0	09	32	1	44	58
4	01	22	42	20	0	26	44	0	12	43	1	43	01
5	02	05	52	55	0	33	25	0	15	53	2	54	23
6	02	19	03	30	0	40	06	0	19	04	3	07	19
7	03	02	14	05	0	46	48	0	22	14	4	00	22
8	03	15	24	40	0	53	29	0	25	25	5	03	54
9	03	28	35	15	0	00	10	0	28	36	6	07	06
10	04	11	45	50	1	06	51	0	31	46	7	10	16
11	04	24	56	25	1	13	32	0	34	57	8	13	27
12	05	08	07	00	1	20	13	0	38	08	9	16	47
13	05	21	17	33	1	26	54	0	41	18	10	19	08
14	06	04	28	10	1	33	35	0	44	29	11	22	59
15	06	17	38	45	1	40	16	0	47	40	12	26	09
16	07	00	49	20	1	46	57	0	50	50	13	29	20
17	07	13	59	55	1	53	38	0	54	01	14	32	30
18	07	27	10	30	2	00	19	0	57	11	15	35	41
19	08	10	21	05	2	07	00	1	00	22	16	38	52
20	08	23	31	40	2	13	41	1	03	33	17	42	02
21	09	06	42	15	2	20	28	1	06	43	18	45	13
22	09	19	52	50	2	27	01	1	09	54	19	48	23
23	10	03	03	25	2	33	45	1	13	05	20	51	34
24	10	16	14	00	2	40	26	1	16	16	21	54	45
25	10	29	24	35	2	47	07	1	19	26	22	57	55
26	11	12	35	10	2	53	48	1	22	37	23	01	06
27	11	25	45	45	0	00	29	1	25	47	24	04	16
28	00	08	56	20	0	07	10	1	28	58	25	07	27
29	00	22	06	55	3	13	51	1	32	09	26	10	37
30	01	05	17	31	3	20	32	1	35	15	27	13	47
31	01	18	28	06	3	27	13	1	38	30	28	16	58

her Apoge, and Node, to every Day in the Year.

March.							April.						
Days.	Moons Mean Motion.			Apoge.		Node Retrogr.	Days.	Moons Mean Motion.			Apoge.		Node Retrogr.
	S	O	P	H	M			S	O	P	H	M	
1	02	10	35	01	06	41	04	03	10	38	10	08	17
2	02	23	45	36	06	47	45	03	13	49	10	14	58
3	03	06	56	11	06	54	26	03	16	59	10	21	39
4	03	20	06	46	07	01	07	03	20	10	10	28	20
5	04	03	17	21	07	07	48	03	23	20	10	35	02
6	04	16	27	56	07	14	29	03	26	31	10	41	43
7	04	29	38	31	07	21	11	03	29	42	10	48	24
8	05	12	49	06	07	27	52	03	32	52	10	55	05
9	05	25	59	41	07	34	33	03	36	03	11	01	46
10	06	09	10	16	07	41	14	03	39	14	11	08	27
11	06	22	20	51	07	47	55	03	42	25	11	15	08
12	07	05	31	26	07	54	36	03	45	36	11	21	49
13	07	18	42	01	08	01	17	03	48	46	11	28	30
14	08	01	52	36	08	07	58	03	51	56	11	35	11
15	08	15	03	11	08	14	39	03	55	07	11	41	52
16	08	28	13	46	08	21	20	03	58	18	11	48	33
17	09	11	24	21	08	28	01	04	01	28	11	55	14
18	09	24	34	56	8	34	42	04	04	39	12	01	55
19	10	07	45	31	8	41	23	04	07	49	12	08	36
20	10	20	56	07	8	48	04	04	11	00	12	15	18
21	11	04	06	42	8	54	45	04	14	11	12	21	59
22	11	17	17	17	9	01	27	04	17	22	12	28	40
23	00	00	27	52	9	08	08	04	20	32	12	35	21
24	00	13	38	27	9	14	49	04	23	43	12	42	06
25	00	26	49	02	9	21	30	04	26	53	12	48	13
26	01	09	59	37	9	28	11	04	30	04	12	55	24
27	01	23	10	12	9	34	52	04	33	15	13	02	03
28	02	06	20	47	9	41	33	04	36	25	13	08	14
29	02	19	31	22	9	48	14	04	39	36	13	15	27
30	02	41	57	09	9	54	55	04	42	47	13	22	06
31	03	15	52	32	10	01	36	04	45	58	13	28	17



A TABLE of the Mean Motions of the Moon,

May.												June.														
Days.	Moons Mean Motion.				Apoge.				Node Retrogr.				Days.	Moons Mean Motion.				Apoge.				Node Retrogr.				
	S	O	F	H	S	O	F	H	S	O	F	H		S	O	F	H	S	O	F	H					
1	05	04	20	37	13	28	49	06	24	27			1	06	22	48	43	16	56	03	08	02	56			
2	05	17	31	12	13	35	30	06	27	38			2	07	05	59	18	17	02	44	08	06	07			
3	06	00	41	47	13	42	11	06	30	48			3	07	19	09	53	17	09	25	08	09	18			
4	06	13	52	22	13	48	52	06	33	59			4	08	02	20	28	17	16	06	08	12	29			
5	06	27	02	57	13	55	34	06	37	10			5	08	15	31	03	17	22	47	08	15	39			
6	07	10	13	32	14	02	56	06	40	20			6	08	28	41	38	17	29	28	08	18	50			
7	07	23	24	07	14	08	56	06	43	31			7	09	11	52	13	17	36	09	08	22	00			
8	08	06	34	42	14	15	37	06	46	41			8	09	25	02	48	17	42	50	08	25	11			
9	08	19	45	17	14	22	18	06	49	52			9	10	08	13	23	17	49	31	08	28	22			
10	09	02	55	53	14	28	59	06	53	03			10	10	21	23	58	17	56	12	08	31	32			
11	09	16	06	27	14	35	40	06	56	18			11	11	04	34	33	18	02	53	08	34	43			
12	09	29	17	03	14	42	21	06	59	24			12	11	17	45	08	18	09	34	08	37	54			
13	10	12	27	38	14	49	02	07	02	34			13	00	00	55	43	18	16	15	08	41	05			
14	10	25	38	13	14	55	43	07	05	45			14	00	14	06	18	18	22	56	08	44	16			
15	11	08	48	48	15	02	34	07	08	50			15	00	27	16	53	18	29	37	08	47	26			
16	11	21	59	23	15	09	05	07	12	06			16	01	10	27	28	18	36	19	08	50	37			
17	00	05	09	58	15	15	46	07	15	17			17	01	23	38	03	18	43	00	08	53	47			
18	00	18	20	33	15	22	28	07	18	27			18	02	06	48	38	18	49	41	08	56	58			
19	01	01	38	08	15	29	09	07	21	38			19	02	19	59	13	18	56	22	09	00	09			
20	01	14	41	43	15	35	50	07	24	49			20	03	03	09	48	19	03	03	09	03	19			
21	01	27	52	18	15	42	31	07	28	00			21	03	16	20	23	19	09	44	09	06	30			
22	02	11	02	53	15	49	12	07	31	10			22	03	29	30	58	19	16	25	09	09	40			
23	02	24	13	28	15	55	53	07	34	21			23	04	12	41	33	19	23	06	09	12	51			
24	03	07	24	03	16	02	34	07	37	32			24	04	25	52	08	19	29	47	09	16	02			
25	03	20	34	38	16	09	15	07	40	43			25	05	09	02	43	19	36	28	09	19	12			
26	04	03	45	13	16	15	56	07	43	53			26	05	22	13	18	19	43	09	09	22	23			
27	04	16	55	48	16	22	37	07	47	04			27	06	05	23	53	19	49	50	09	25	34			
28	05	00	06	23	16	29	18	07	50	14			28	06	18	34	28	19	56	31	09	28	45			
29	05	13	16	58	16	35	59	07	53	25			29	07	01	45	04	20	03	12	09	31	55			
30	05	26	27	33	16	42	40	07	56	36			30	07	14	55	39	20	09	54	09	35	06			
31	06	09	38	08	16	49	21	07	59	46																

her Apoge, and Node, to every Day in the Year.

July.												August.														
Days.	Moons Mean Motion.				Apoge.				Node Retrogr.				Days.	Moons Mean Motion.				Apoge.				Node Retrogr.				
	S	O	F	H	S	O	F	H	S	O	F	H		S	O	F	H	S	O	F	H	S	O	F	H	
1	07	28	06	14	20	16	38	9	38	15			1	09	16	34	19	23	43	47	11	16	47			
2	08	11	16	49	20	23	16	9	41	27			2	09	29	44	54	23	50	28	11	19	58			
3	08	24	27	24	20	29	57	9	44	37			3	10	12	55	25	23	57	09	11	23	08			
4	09	07	37	59	20	36	38	9	47	47			4	10	26	06	04	24	03	51	11	26	19			
5	09	20	48	34	20	43	11	9	50	59			5	11	09	16	39	24	10	32	11	29	29			
6	10	03	59	09	20	50	00	9	54	09			6	11	22	27	14	24	17	13	11	32	40			
7	10	17	09	44	20	56	41	9	57	20			7	00	35	37	49	24	21	54	11	35	51			
8	11	00	20	19	21	03	22	10	00	30			8	00	18	48	24	24	30	35	11	39	02			
9	11	13	30	54	21	10	03	10	03	41			9	01	01	58	59	24	37	16	11	42	12			
10	11	26	41	29	21	16	44	10	06	51			10	01	15	09	34	24	43	57	11	45	23			
11	00	09	52	04	21	23	25	10	10	02			11	1	28	20	09	24	50	38	11	48	33			
12	00	23	02	39	21	30	06	10	13	13			12	02	11	30	44	24	57	19	11	51	44			
13	01	06	13	14	21	36	47	10	16	24			13	02	24	41	19	25	04	00	11	54	54			
14	01	19	23	49	21	43	28	10	19	35			14	03	07	51	54	25	10	42	11	58	05			
15	02	02	34	24	21	50	09	10	22	45			15	03	21	02	29	25	17	23	12	01	15			
16	02	15	44	59	21	56	52	10	25	56			16	04	04	13	04	25	24	04	12	04	26			
17	02	28	55	34	22	03	32	10	29	06			17	04	17	23	40	25	30	45	12	07	36			
18	03	12	06	09	22	10	13	10	32	17			18	05	00	34	15	25	37	26	12	10	47			
19	03	25	16	44	22	16	54	10	35	28			19	05	13	44	50	25	44	07	12	13	58			
20	04	08	27	19	22	23	35	10	38	39			20	05	26	55	25	25	50	48	12	17	08			
21	04	21	37	54	22	30	15	10	41	49			21	06	10	06	00	25	57	25	12	20	19			
22	05	04	48	21	22	36	50	10	45	00			22	06	23	16	35	26	04	10	12	23	29			
23	05	17	59	04	22	43	3	10	48	11			23	07	06	27	10	26	10	51	12	26	40			
24	06	01	09	30	22	50	10	10	51	21			24	07	19	37	45	26	17	32	12	29	51			
25	06	14	20	14	22	57	00	10	54	32			25	08	02	48	20	26	24	13	13	33	01			
26	06	27	30	49	23	03	41	10	57	42			26	08	15	59	55	26	30	53	12	36	12			
27	07	10	41	2	23	10	22	11	00	53			27	08	29	09	30	26	37	30	12	39	23			
28	7	23	51	59	23	17	03	11	04	03			28	09	12	20	05	26	44	17	12	42	34			
29	8	07	02	34	23	23	44	11	07	14			29	09	25	30	40	26	50	58	12	45	44			
30	8	20	13	9	23	30	23	11	10	25			30	10	08	41	06	26	57	36	12	48	54			
31	9	03	23	44	3	37	06	11	13	36			31	10	2	51	06	27	44	36	12	52	04			



A TABLE of the Mean Motions of the Moon,

September.				October.			
Days.	Moons Mean Motion.	Apoge.	Node Retrogr.	Days.	Moons Mean Motion.	Apoge.	Node Retrogr.
1	11 05 02 25	0 27 11 01	12 55 16	1	10 10 19 55	0 00 31 33	14 30 35
2	11 18 13 00	0 27 17 42	12 58 27	2	20 23 30 30	0 00 38 14	14 33 46
3	00 01 23 35	0 27 24 23	13 01 37	3	30 06 41 05	0 00 44 55	14 36 56
4	00 14 34 10	0 27 31 04	13 04 45	4	40 19 51 45	0 00 51 30	14 40 07
5	00 27 44 45	0 27 37 45	13 07 58	5	50 03 02 15	0 00 58 17	14 43 17
6	01 10 55 20	0 27 44 26	13 11 09	6	60 16 12 50	0 01 04 58	14 46 28
7	01 24 05 55	0 27 51 07	13 14 20	7	70 29 23 26	0 01 11 39	14 49 39
8	02 07 16 30	0 27 57 48	13 17 31	8	80 12 34 01	0 01 18 20	14 52 50
9	02 20 27 05	0 28 04 29	13 20 41	9	90 25 44 36	0 01 25 02	14 56 00
10	03 03 37 40	0 28 11 11	13 23 52	10	100 4 08 55	0 01 31 43	14 59 11
11	03 16 48 15	0 28 17 52	13 27 03	11	110 4 22 05 46	0 01 38 24	15 02 21
12	03 29 58 50	0 28 24 33	13 30 14	12	120 5 05 16 21	0 01 45 05	15 05 32
13	04 13 09 25	0 28 31 14	13 33 24	13	130 5 18 26 56	0 01 51 46	15 08 43
14	04 26 20 00	0 28 37 55	13 36 35	14	140 6 01 37 31	0 01 58 27	15 11 53
15	05 09 30 35	0 28 44 36	13 39 45	15	150 6 14 48 06	0 02 05 08	15 15 04
16	05 22 41 10	0 28 51 17	13 42 56	16	160 6 27 58 41	0 02 11 49	15 18 15
17	06 05 51 45	0 28 57 58	13 46 07	17	170 7 11 09 16	0 02 18 30	15 21 26
18	06 19 02 20	0 29 04 39	13 49 17	18	180 7 24 19 51	0 02 25 11	15 24 36
19	07 02 12 55	0 29 11 20	13 52 27	19	190 8 07 30 26	0 02 31 52	15 27 47
20	07 15 23 30	0 29 18 01	13 55 37	20	200 8 20 41 01	0 02 38 33	15 30 57
21	07 28 34 05	0 29 24 42	13 58 47	21	210 9 03 51 36	0 02 45 14	15 34 08
22	08 11 44 40	0 29 31 23	14 02 00	22	220 9 17 02 11	0 02 51 55	15 37 19
23	08 24 55 15	0 29 38 04	14 05 10	23	230 10 00 12 46	0 02 58 36	15 40 29
24	09 08 05 50	0 29 44 45	14 08 21	24	240 10 13 23 21	0 03 05 17	15 43 40
25	09 21 16 25	0 29 51 27	14 11 31	25	250 10 26 33 56	0 03 11 58	15 46 50
26	10 04 27 00	0 29 58 08	14 14 42	26	260 11 09 44 31	0 03 18 39	15 50 01
27	10 17 37 35	0 00 04 49	14 17 53	27	270 11 22 55 06	0 03 25 20	15 53 12
28	11 00 48 10	0 00 11 30	14 21 03	28	280 06 05 41	0 03 32 02	15 56 22
29	11 13 58 45	0 00 18 11	14 24 14	29	00 19 16 16	0 03 38 43	15 59 33
30	11 27 09 20	0 00 24 52	14 27 24	30	11 02 26 51	0 03 45 24	16 02 43
					01 15 37 26	0 03 52 05	16 05 54

her Apoge, and Node, to every Day in the Year.

November.				December.			
Days.	Moons Mean Motion.	Apoge.	Node Retrogr.	Days.	Moons Mean Motion.	Apoge.	Node Retrogr.
1	01 28 48 01	0 03 58 46	16 09 05	1	03 04 05 32	0 07 19 18	17 44 25
2	02 11 58 36	0 04 05 27	16 2 15	2	03 17 16 07	0 07 25 59	17 47 35
3	02 25 03 11	0 04 12 08	16 15 26	3	04 00 26 42	0 07 32 40	17 50 46
4	03 08 19 46	0 04 18 49	16 18 37	4	04 13 37 17	0 07 39 21	17 53 56
5	03 21 30 21	0 04 25 30	16 21 48	5	04 26 47 52	0 07 46 02	17 57 07
6	04 04 40 56	0 04 32 11	16 24 59	6	05 09 58 27	0 07 52 43	18 00 18
7	04 17 51 31	0 04 38 53	16 28 09	7	05 23 09 02	0 07 59 24	18 03 28
8	05 01 02 06	0 04 45 34	16 31 20	8	06 06 19 37	0 08 06 06	18 06 39
9	05 14 12 41	0 04 52 15	16 34 30	9	06 19 30 12	0 08 12 47	18 09 49
10	05 27 23 16	0 04 58 56	16 37 41	10	07 02 40 47	0 08 19 28	18 13 00
11	06 10 33 51	0 05 05 37	16 40 52	11	07 15 51 22	0 08 26 09	18 16 11
12	06 23 44 26	0 05 12 18	16 44 02	12	07 29 01 57	0 08 32 50	18 19 21
13	06 36 55 01	0 05 18 59	16 47 13	13	08 12 12 32	0 08 39 31	18 22 32
14	07 20 05 36	0 05 25 40	16 50 23	14	08 25 23 07	0 08 46 12	18 25 42
15	08 03 16 11	0 05 32 21	16 53 34	15	09 08 33 42	0 08 52 53	18 28 53
16	08 16 26 46	0 05 39 02	16 56 45	16	09 21 44 17	0 08 59 34	18 32 04
17	08 29 37 21	0 05 45 43	16 59 55	17	10 04 54 52	0 09 06 15	18 35 15
18	09 12 47 56	0 05 52 24	17 03 06	18	10 18 05 27	0 09 12 56	18 38 25
19	09 25 58 31	0 05 59 05	17 06 16	19	11 01 16 02	0 09 19 38	18 41 36
20	10 09 09 06	0 05 05 46	17 09 27	20	11 14 26 37	0 09 26 19	18 44 47
21	10 22 19 41	0 06 12 27	17 12 38	21	11 27 37 12	0 09 33 00	18 47 58
22	11 05 30 16	0 06 19 09	17 15 49	22	12 00 47 47	0 09 39 41	18 51 09
23	11 18 40 51	0 06 25 50	17 18 59	23	12 13 58 22	0 09 46 22	18 54 19
24	12 01 51 26	0 06 32 31	17 22 10	24	01 07 08 57	0 09 53 03	18 57 30
25	12 15 02 01	0 06 39 12	17 25 21	25	01 20 19 32	0 09 59 44	19 00 41
26	12 28 12 37	0 06 45 53	17 28 32	26	02 03 30 07	0 10 06 25	19 03 51
27	11 11 23 12	0 06 52 34	17 31 42	27	02 16 40 42	0 10 13 06	19 07 02
28	01 24 33 47	0 06 59 15	17 34 53	28	02 29 51 17	0 10 19 47	19 10 12
29	02 07 44 22	0 07 05 56	17 38 03	29	03 13 01 52	0 10 26 28	19 13 23
30	02 20 54 57	0 07 12 37	17 41 14	30	03 26 12 27	0 10 33 09	19 16 34
					03 39 23 02	0 10 39 50	19 19 45



TABLE IX.

*A TABLE of the Moons Mean Motions to Hours and Parts of an Hour.*

H.	0	1	2	3	4	5	6	7	8	9	H.	0	1	2	3	4	5	6	7	8	9
0	0	0	0	0	0	0	0	0	0	0	30	16	28	14							
1	0	32	56	0	17	0	c8				31	17	01	10		8	38	4	06		
2	1	05	53	0	33	0	16				32	17	34	07		8	54	4	14		
3	1	38	49	0	50	0	24				33	13	07	03		9	11	4	22		
4	2	11	46	1	67	0	32				34	13	39	59		9	28	4	30		
5	2	44	42	1	24	0	40				35	12	12	55		9	45	4	38		
6	3	17	39	1	40	0	48				36	19	45	52		10	02	4	46		
7	3	50	35	1	57	0	56				37	20	18	48		10	19	4	54		
8	4	23	32	2	14	1	04				38	20	51	45		10	36	5	02		
9	4	56	28	2	30	1	12				39	21	24	41		10	52	5	10		
10	5	29	25	2	47	1	19				40	21	57	38		11	08	5	18		
11	6	02	21	3	04	1	27				41	22	30	34		11	25	5	26		
12	6	35	18	3	21	1	35				42	23	03	31		11	42	5	34		
13	7	08	14	3	37	1	43				43	23	36	27		11	59	5	42		
14	7	41	10	3	54	1	51				44	24	09	24		12	16	5	50		
15	8	14	07	4	11	1	59				45	24	42	20		12	32	5	58		
16	8	47	03	4	27	2	07				46	25	15	17		12	48	6	06		
17	9	20	00	4	44	2	15				47	25	48	13		13	05	6	14		
18	9	52	56	5	01	2	23				48	26	21	10		13	22	6	22		
19	10	25	53	5	18	2	31				49	26	54	06		13	39	6	30		
20	10	58	49	5	34	2	39				50	27	27	03		13	56	6	38		
21	11	31	46	5	51	2	47				51	27	59	59		14	13	6	46		
22	12	04	42	6	08	2	55				52	28	32	56		14	30	6	54		
23	12	37	39	6	24	3	03				53	29	05	52		14	46	7	01		
24	13	10	35	6	41	3	11				54	29	38	49		15	02	7	08		
25	13	43	32	6	58	3	19				55	30	11	45		15	19	7	16		
26	14	16	28	7	15	3	27				56	30	44	42		15	36	7	24		
27	14	49	24	7	31	3	34				57	31	17	38		15	53	7	32		
28	15	22	21	7	48	3	42				58	31	50	34		16	10	7	40		
29	15	55	17	8	05	3	50				59	32	23	31		16	26	7	48		
30	16	28	14	8	21	3	58				60	32	56	27		16	43	7	56		
For the																					

In the Leap-year after *February* add a Day to the given time, and its Motions to the Motions Collected.

*A TABLE of Physical Parts, to be added to or subtracted from the Moons Mean Motion, according to the Suns Mean Anomaly.*

		Add.								
		0	1	2	3	4	5			
		1	2	3	4	5	6	7	8	9
0	0 00	5 36	9 51	11 30	10 04	5 51	30			
1	0 12	5 47	9 57	11 30	9 58	5 40	29			
2	0 23	5 58	10 03	11 30	9 51	5 30	28			
3	0 35	6 09	10 09	11 30	9 45	5 19	27			
4	0 47	6 19	10 14	11 29	9 39	5 08	26			
5	0 59	6 29	10 19	11 28	9 32	4 57	25			
6	1 10	6 39	10 25	11 27	9 25	4 46	24			
7	1 22	6 48	10 30	11 26	9 18	4 35	23			
8	1 33	6 58	10 34	11 25	9 11	4 23	22			
9	1 45	7 07	10 39	11 24	9 03	4 12	21			
10	1 56	7 16	10 43	11 22	8 55	4 00	20			
11	2 08	7 25	10 48	11 20	8 48	3 49	19			
12	2 19	7 34	10 52	11 18	8 40	3 37	18			
13	2 31	7 43	10 56	11 15	8 32	3 25	17			
14	2 42	7 52	10 59	11 13	8 23	3 14	16			
15	2 54	8 01	11 02	11 10	8 15	3 02	15			
16	3 05	8 09	11 06	11 07	8 06	2 50	14			
17	3 16	8 17	11 09	11 04	7 58	2 38	13			
18	3 27	8 25	11 12	11 00	7 49	2 26	12			
19	3 39	8 33	11 14	10 57	7 40	2 14	11			
20	3 50	8 41	11 17	10 53	7 30	2 02	10			
21	4 01	8 49	11 19	10 50	7 21	1 50	9			
22	4 12	8 57	11 21	10 45	7 12	1 38	8			
23	4 22	9 04	11 23	10 40	7 02	1 26	7			
24	4 33	9 11	11 24	10 35	6 52	1 13	6			
25	4 44	9 18	11 26	10 31	6 42	1 01	5			
26	4 55	9 25	11 27	10 26	6 32	0 49	4			
27	5 05	9 32	11 28	10 20	6 22	0 37	3			
28	5 16	9 38	11 29	10 15	6 12	0 24	2			
29	5 26	9 45	11 29	10 09	6 02	0 12	1			
30	5 36	9 51	11 30	10 04	5 51	0 00	0			
		11	10	9	8	7	6			
Subtract.										



The Equations of the Moons Apoge and the Excentricities of her Orbit, in such Parts as the Radius is, 1000000.

Add the Equations of the Apoge.					
Sign 0	Excen.	Sign 1	Excen.	Sign 2	Excen.
0 0 00 00	Parts.	0 0 00 00	Parts.	0 0 00 00	Parts.
0 0 00 00	66854	09 07 14	61045	11 08 55	49429
1 0 20 21	66847	09 20 52	60691	10 59 45	49082
2 0 40 42	66826	09 34 01	60330	10 49 35	48741
3 1 01 01	66791	09 46 40	59962	10 38 22	48408
4 1 21 17	66741	09 58 49	59589	10 26 07	48085
5 1 41 30	66678	10 10 24	59210	10 12 50	47769
6 2 01 40	66600	10 21 29	58827	09 58 31	47463
7 2 21 44	66509	10 31 58	58439	09 43 10	47167
8 2 41 42	66404	10 41 50	58047	09 26 48	46880
9 3 01 34	66286	10 51 08	57652	09 09 24	46604
10 3 21 18	66154	10 59 48	57254	08 51 00	46337
11 3 40 54	66008	11 07 47	56854	08 31 36	46082
12 4 00 21	65850	11 15 07	56451	08 11 14	45838
13 4 19 38	65679	11 21 45	56047	07 49 55	45606
14 4 38 44	65495	11 27 40	55642	07 27 40	45385
15 4 57 38	65298	11 32 51	55237	07 04 31	45176
16 5 16 20	65083	11 37 17	54832	06 40 30	44979
17 5 34 49	64863	11 40 55	54427	06 15 40	44795
18 5 53 02	64636	11 43 47	54023	05 50 02	44624
19 6 11 01	64392	11 45 49	53620	05 23 39	44466
20 6 28 43	64137	11 47 01	53220	04 56 34	44320
21 6 46 03	63870	11 47 22	52822	04 28 51	44188
22 7 03 15	63594	11 46 50	52427	04 00 32	44070
23 7 20 03	63307	11 45 24	52035	03 31 40	43965
24 7 36 30	63011	11 43 04	51647	03 02 20	43874
25 7 52 36	62705	11 39 47	51264	02 32 26	43796
26 8 08 20	62389	11 35 34	50885	02 02 30	43733
27 8 23 41	62066	11 30 23	50512	01 32 08	43683
28 8 38 38	61733	11 24 14	50144	01 01 30	43648
29 8 53 08	61392	11 17 05	59783	00 30 45	43627
30 9 07 14	61045	11 08 55	59429	00 00 00	43619
Sign 5		Sign 4		Sign 9	
11		10		9	

Subtract, &c.

A TABLE of the Equations of the Moons Center.

Subtract.					
Sign 0.	Sign 1.	Sign 2.	Sign 3.	Sign 4.	Sign 5.
Least Exc.	Middle.	Greatest.	Least Exc.	Middle.	Greatest.
43619	55237	66854	43619	55237	66854
0 0 00 00	0 0 00 00	0 0 00 00	0 0 00 00	0 0 00 00	0 0 00 00
0 0 00 00	0 0 00 00	0 0 00 00	2 23 08	2 59 04	3 34 08
1 0 04 58	0 06 12	0 07 24	2 27 32	3 04 33	3 40 43
2 0 09 56	0 12 24	0 14 48	2 31 50	3 10 00	3 47 15
3 0 14 53	0 18 35	0 22 12	2 36 07	3 15 23	3 53 43
4 0 19 50	0 24 47	0 29 36	2 40 22	3 20 44	4 00 08
5 0 24 48	0 30 58	0 36 58	2 44 35	3 26 01	4 06 30
6 0 29 44	0 37 09	0 44 20	2 48 48	3 31 16	4 12 47
7 0 34 39	0 43 19	0 51 42	2 52 53	3 36 27	4 19 01
8 0 39 34	0 49 27	0 59 04	2 56 54	3 41 35	4 25 12
9 0 44 30	0 55 36	1 06 25	3 00 58	3 46 39	4 31 18
10 0 49 25	1 01 43	1 13 45	3 04 55	3 51 39	4 37 20
11 0 54 19	1 07 51	1 21 02	3 08 53	3 56 36	4 43 18
12 0 59 13	1 13 57	1 28 18	3 12 46	4 01 30	4 49 12
13 1 04 04	1 20 02	1 35 34	3 16 35	4 06 20	4 55 01
14 1 08 56	1 26 05	1 42 49	3 20 22	4 11 06	5 00 46
15 1 13 45	1 32 07	1 50 02	3 24 05	4 15 47	5 06 26
16 1 18 33	1 38 08	1 57 13	3 27 44	4 20 24	5 12 01
17 1 23 20	1 44 08	2 04 23	3 31 20	4 24 58	5 17 32
18 1 28 06	1 50 06	2 11 31	3 34 53	4 29 28	5 22 59
19 1 32 50	1 56 02	2 18 37	3 38 22	4 33 53	5 28 20
20 1 37 32	2 01 56	2 25 41	3 41 47	4 38 14	5 33 36
21 1 42 13	2 07 49	2 32 43	3 45 09	4 42 31	5 38 47
22 1 46 53	2 13 39	2 39 43	3 48 28	4 46 43	5 43 53
23 1 51 33	2 19 27	2 46 40	3 51 43	4 50 50	5 48 53
24 1 56 09	2 25 14	2 53 35	3 54 54	4 54 53	5 53 48
25 2 00 45	2 30 58	3 00 28	3 58 03	4 58 55	5 58 38
26 2 05 18	2 36 41	3 07 18	4 01 06	5 02 43	6 03 21
27 2 09 49	2 42 21	3 14 05	4 04 05	5 06 32	6 07 59
28 2 14 18	2 47 58	3 20 49	4 07 00	5 10 15	6 12 31
29 2 18 44	2 53 32	3 27 30	4 09 51	5 13 54	6 16 58
30 2 23 08	2 59 04	3 34 08	4 12 40	5 17 27	6 21 18
Sign 11.			Sign 10.		

Add.



A TABLE of the Equations of the Moons Center.

Subtract.																		
Mens. Hourly	Sign 2.						Sign 3.								Mens. Hourly			
	Least Exc		Middle.		Greatest.		Least Exc		Middle.		Greatest.							
	43619	55327	66854	43619	55327	66854												
	o	i	"	o	i	"	o	i	"	o	i	"	o	i	"			
0	4	12	40	5	17	27	6	21	18	4	59	30	6	18	59	7	38	17
1	+	15	18	5	20	54	6	25	32	4	59	48	6	19	23	7	38	52
2	+	17	56	5	24	17	6	29	39	4	59	56	6	19	40	7	39	20
3	4	20	28	5	27	35	6	33	40	4	59	59	6	19	50	7	39	40
4	4	23	00	5	30	47	6	37	36	4	59	58	6	19	54	7	39	51
5	+	25	24	5	33	53	6	41	25	4	59	49	6	10	51	7	39	53
6	+	27	44	5	36	54	6	45	08	4	59	36	6	19	40	7	39	47
7	4	30	00	5	39	49	6	48	44	4	59	20	6	19	23	7	39	33
8	4	32	12	5	42	39	6	52	14	4	58	53	6	18	57	7	39	09
9	+	34	19	5	45	24	6	55	36	4	58	24	6	18	25	7	38	37
10	+	36	21	5	48	02	6	58	52	4	57	48	6	17	46	7	37	58
11	+	38	18	5	50	33	7	02	01	4	57	06	6	17	00	7	37	09
12	+	40	12	5	53	02	7	05	03	4	56	19	6	16	08	7	36	12
13	+	41	58	5	55	22	7	07	57	4	55	27	6	15	08	7	35	06
14	4	43	41	5	57	36	7	10	45	4	54	30	6	14	00	7	33	52
15	4	45	19	5	59	44	7	13	25	4	53	27	6	12	46	7	32	29
16	4	46	53	6	01	46	7	15	56	4	52	19	6	11	25	7	30	57
17	4	48	22	6	03	42	7	18	21	4	51	03	6	09	56	7	29	17
18	+	49	44	6	05	31	7	20	42	4	49	45	6	08	20	7	27	28
19	+	51	02	6	07	15	7	22	53	4	48	21	6	06	37	7	25	30
20	4	52	15	6	08	52	7	24	56	4	46	51	6	04	48	7	23	23
21	4	53	22	6	10	23	7	26	52	4	45	16	6	02	51	7	21	08
22	4	54	23	6	11	46	7	28	36	4	43	34	6	00	48	7	18	44
23	4	55	20	6	13	03	7	30	26	4	41	44	5	58	37	7	16	12
24	4	56	12	6	14	14	7	31	52	4	39	56	5	56	19	7	13	30
25	4	56	59	6	15	19	7	33	16	4	37	58	5	53	54	7	10	40
26	4	57	38	6	16	17	7	34	32	4	35	56	5	51	23	7	07	42
27	4	58	14	6	17	08	7	35	47	4	33	47	5	48	43	7	04	35
28	4	58	45	6	17	52	7	36	41	4	31	33	5	45	57	7	01	19
29	4	59	10	6	18	29	7	37	34	4	29	13	5	43	04	6	57	55
30	4	59	30	6	18	59	7	38	17	4	26	43	5	40	05	6	54	23
Sign 9.							Sign 8.											
Add.																		

A TABLE of the Equations of the Moons Center.

Subtract.																			
Mean Abundancy	Signs 4.						Signs 5.						Mean Abundancy						
	Least Exc		Middle.		Greatest.		Least Exc		Middle.		Greatest.								
	43619		55237		66854		43619		55237		66854								
	o	i	u	o	i	u	o	i	u	o	i	u							
	4	26	49	5	40	05	6	54	23	2	37	10	3	21	48	4	07	29	30
1	4	24	19	5	37	00	6	50	42	2	32	27	3	15	48	4	00	10	29
2	4	21	43	5	33	46	6	46	52	2	27	42	3	09	44	3	52	45	28
3	4	19	01	5	30	25	6	42	54	2	22	54	3	03	36	3	45	14	27
4	4	16	14	5	26	57	6	38	48	2	18	03	2	57	24	3	37	39	26
5	4	13	22	5	23	24	6	34	34	2	13	09	2	51	06	3	29	59	25
6	4	10	25	5	19	43	6	30	11	2	08	13	2	44	43	3	22	14	24
7	4	07	24	5	15	53	6	25	40	2	03	14	2	38	20	3	14	24	23
8	4	04	18	5	12	06	6	21	01	1	58	12	2	31	55	3	06	30	22
9	4	01	08	5	08	07	6	16	14	1	53	07	2	25	24	2	58	21	21
10	3	57	53	5	04	00	6	11	20	1	48	01	2	18	50	2	50	20	20
11	3	54	32	4	59	48	6	06	16	1	42	52	2	12	13	2	42	23	19
12	3	51	07	4	55	30	6	01	06	1	37	41	2	05	32	2	34	11	18
13	3	47	38	4	51	06	5	55	49	1	32	27	1	58	49	2	25	53	17
14	3	44	04	4	46	36	5	50	21	1	27	11	1	52	05	2	17	41	16
15	3	40	27	4	42	00	5	44	48	1	21	54	1	45	17	2	09	21	15
16	3	36	43	4	37	17	5	39	06	1	16	35	1	38	26	2	00	50	14
17	3	32	55	4	32	27	5	33	17	1	11	14	1	31	33	1	52	31	13
18	3	29	02	4	27	32	5	27	22	1	05	55	1	24	38	1	44	01	12
19	3	25	05	4	22	33	5	21	19	1	00	27	1	17	42	1	35	29	11
20	3	21	04	4	17	28	5	15	09	0	55	02	1	10	44	1	26	53	10
21	3	16	59	4	12	17	5	08	52	0	49	34	1	03	43	1	18	19	9
22	3	12	48	4	07	01	5	02	28	0	44	07	0	56	42	1	09	42	8
23	3	08	34	4	01	40	4	55	58	0	38	37	0	49	30	1	01	03	7
24	3	04	16	3	56	13	4	49	21	0	33	08	0	42	36	0	52	22	6
25	2	59	53	3	50	40	4	42	38	0	27	38	0	35	30	0	43	40	5
26	2	55	27	3	45	03	4	35	48	0	22	08	0	28	25	0	34	57	4
27	2	50	58	3	39	21	4	28	52	0	16	37	0	21	19	0	26	13	3
28	2	46	26	3	33	34	4	21	49	0	11	04	0	14	13	0	17	29	2
29	2	41	50	3	27	43	4	14	41	0	05	32	0	07	07	0	08	45	1
30	2	37	10	3	21	48	4	07	29	0	00	00	0	00	00	0	00	00	0
Signs 7							Signs 6												
Add.																			



A TABLE of the Variation.						
	Add.					
	Sign 6		Sign 7		Sign 8	
	°	'	°	'	°	'
0	00	00	32	54	32	54
1	01	20	33	33	32	13
2	02	39	34	09	31	30
3	03	59	34	42	30	45
4	05	18	35	13	29	57
5	06	36	35	42	28	07
6	07	54	36	09	28	14
7	09	11	36	32	27	20
8	10	28	36	52	26	24
9	11	44	37	10	25	26
10	13	00	37	25	24	25
11	14	14	37	38	23	23
12	15	27	37	48	22	20
13	16	40	37	55	21	15
14	17	51	37	59	20	08
15	19	00	38	00	19	00
16	20	03	37	59	17	51
17	21	15	37	55	16	40
18	22	20	37	48	15	27
19	23	23	37	38	14	14
20	24	25	37	25	13	00
21	25	26	37	10	11	44
22	26	24	36	52	10	28
23	27	20	36	32	09	11
24	28	14	36	09	07	54
25	29	07	35	42	06	36
26	29	57	35	13	05	18
27	30	45	34	42	03	59
28	31	30	34	09	02	39
29	32	13	33	33	01	20
30	32	54	32	54	00	00
	Sign 11		Sign 10		Sign 9	
	5		4		3	
Subtract.						

A Table of the Equati. of the Node, and Inclinations of the Limit about 5 Deg.																			
Equation of the $\Omega$ Add.																			
$\circ$ $\frac{1}{2}$ $\frac{3}{4}$ diff.	Signs $\frac{0}{6}$					Signs $\frac{1}{7}$					Signs $\frac{2}{8}$					$\circ$ $\frac{1}{2}$ $\frac{3}{4}$ diff.			
	Equati. $\Omega$		Inc. Lim			Equati. $\Omega$		Inc. Lim			Equati. $\Omega$		Inc. Lim						
	$\circ$	$\frac{1}{2}$	$\frac{3}{4}$	$\frac{1}{2}$	$\frac{3}{4}$	$\circ$	$\frac{1}{2}$	$\frac{3}{4}$	$\frac{1}{2}$	$\frac{3}{4}$	$\circ$	$\frac{1}{2}$	$\frac{3}{4}$	$\frac{1}{2}$	$\frac{3}{4}$				
0	00	00	18	00		1	25	12	13	30		1	26	50	04	30	30		
1	03	28	18	00		1	27	00	13	14		1	25	01	04	14	29		
2	06	56	17	59		1	28	37	12	57		1	23	06	03	59	28		
3	10	23	17	59		1	30	04	12	40		1	21	06	03	45	27		
4	13	49	17	55		1	31	22	12	23		1	19	03	03	28	26		
5	17	11	17	52		1	32	30	12	05		1	16	56	03	13	25		
6	20	31	17	48		1	33	34	11	47		1	14	44	02	59	24		
7	23	48	17	43		1	34	34	11	29		1	12	26	02	45	23		
8	27	02	17	38		1	35	31	11	11		1	10	02	02	32	22		
9	30	13	17	34		1	36	25	10	53		1	07	31	02	19	21		
10	33	22	17	28		1	37	15	10	34		1	04	53	02	06	20		
11	36	29	17	21		1	37	59	10	14		1	02	09	01	54	19		
12	39	34	17	13		1	38	37	09	55		1	59	19	01	43	18		
13	42	37	17	05		1	39	09	09	37		1	56	23	01	32	17		
14	45	38	16	57		1	39	33	09	18		1	53	21	01	22	16		
15	48	37	16	48		1	39	46	09	00		1	50	15	01	12	15		
16	51	33	16	38		1	39	34	03	42		1	47	06	01	03	14		
17	54	27	16	28		1	39	11	08	23		1	43	56	00	55	13		
18	57	17	16	17		1	38	41	08	05		1	40	44	00	47	12		
19	00	06	16	06		1	38	05	07	46		1	37	29	00	39	11		
20	02	51	15	54		1	37	23	07	26		1	34	12	00	32	10		
21	05	31	15	41		1	36	34	07	07		1	30	53	00	26	9		
22	08	04	15	28		1	35	46	06	49		1	27	32	00	22	8		
23	10	29	15	15		1	34	56	06	31		1	24	09	00	17	7		
24	12	45	15	01		1	34	03	06	13		1	20	44	00	12	6		
25	15	01	14	47		1	33	06	05	55		1	17	18	00	08	5		
26	17	08	14	32		1	32	03	05	37		1	13	51	00	05	4		
27	19	12	14	17		1	31	00	05	20		1	10	24	00	03	3		
28	21	14	14	01		1	29	47	05	03		1	06	57	00	01	2		
29	23	14	13	46		1	28	24	04	46		1	03	29	00	00	1		
30	25	12	13	30		1	26	50	04	30		1	00	00	00	00	0		
Signs $\frac{5}{11}$					Signs $\frac{4}{10}$					Signs $\frac{3}{9}$									
Equation of the Node Subtract.																			



A TABLE of the Moons simple Latitude, to the least Inclination of her Orbit 5 Degrees, with the parts to be added when 'tis 5°18'.

Arg. of Lat.	Sign 0 Nor. 6 Sou.			Increm. or parts to be added.	Sign 1 Nor. 7 Sou.			Increm. or parts to be added.	Sign 2 Nor. 8 Sou.			Increm. or parts to be added.	Arg. of Lat.			
	D <sup>r</sup> Latitude.				D <sup>r</sup> Latitude.				D <sup>r</sup> Latitude.							
	°	'	"		°	'	"		°	'	"					
0	0	00	00	0	00	00	00	00	0	19	44	15	36	30		
1	0	05	14	0	19	29	51	9	16	4	22	18	15	43	20	
2	0	10	28	0	37	2	38	50	9	32	4	24	49	15	54	28
3	0	15	42	0	56	2	43	15	9	48	4	27	14	16	02	27
4	0	20	55	1	15	2	47	37	10	03	4	29	34	16	11	26
5	0	26	08	1	34	2	51	56	10	19	4	31	50	16	19	25
6	0	31	20	1	53	2	56	11	10	34	4	34	06	16	27	24
7	0	36	32	2	11	3	00	24	10	49	4	36	06	16	34	23
8	0	41	43	2	30	3	04	33	11	04	4	38	06	16	42	22
9	0	46	53	2	49	3	08	39	11	19	4	40	02	16	49	21
10	0	52	02	3	08	3	12	42	11	34	4	41	52	16	55	20
11	0	57	10	3	26	3	16	41	11	48	4	43	37	17	01	19
12	1	02	18	3	45	3	20	36	12	02	4	45	17	17	07	18
13	1	07	24	4	03	3	24	38	12	16	4	46	52	17	12	17
14	1	12	29	4	21	3	28	16	12	30	4	48	21	17	18	16
15	1	17	33	4	39	3	32	00	12	44	4	49	45	17	23	15
16	1	22	36	4	57	3	35	40	12	56	4	51	04	17	28	14
17	1	27	37	5	15	3	39	17	13	09	4	52	18	17	33	13
18	1	32	36	5	33	3	42	49	13	22	4	53	26	17	37	12
19	1	37	34	5	51	3	46	17	13	35	4	54	18	17	40	11
20	1	42	29	6	09	3	49	42	13	47	4	55	26	17	44	10
21	1	47	23	6	27	3	53	02	13	59	4	56	18	17	47	9
22	1	52	16	6	45	3	56	17	14	11	4	57	04	17	50	8
23	1	57	06	7	02	3	59	29	14	23	4	57	45	17	52	7
24	2	01	54	7	19	4	02	36	14	34	4	58	21	17	54	6
25	2	06	39	7	36	4	05	39	14	45	4	58	51	17	56	5
26	2	11	23	7	53	4	08	37	14	56	4	59	16	17	58	4
27	2	16	04	8	09	4	11	30	15	06	4	59	35	17	59	3
28	2	20	42	8	26	4	14	19	15	17	4	59	49	17	59	2
29	2	25	18	8	43	4	17	47	15	26	4	59	57	18	00	1
30	2	29	51	9	00	4	19	44	15	36	5	00	00	18	00	0
	Sign 5 Nor. 11 Sou.					Sign 4 Nor. 10 Sou.					Sign 3 Nor. 9 Sou.					

A TABLE of the Reduction when the Inclination of the Orbit is 5 Degrees, with the excess when it is 5°18'.

Arg. of Lat.	Sign <sup>0</sup> Sub. 6 Reduction			Ex- cess.	Sign <sup>1</sup> Sub. 7 Reduction	Ex- cess.	Sign <sup>2</sup> Sub. 8 Reduction	Ex- cess.	Arg. of Lat.			
	"	"	"									
0	0	00	02		5	40	42		5	41	42	30
1	0	14	02		5	47	43		5	34	41	29
2	0	27	04		5	53	44		5	26	40	28
3	0	41	06		5	59	45		5	18	39	27
4	0	55	08		6	04	46		5	10	38	26
5	1	08	09		6	09	46		5	02	37	25
6	1	22	11		6	14	46		4	53	36	24
7	1	35	12		6	18	47		4	43	35	23
8	1	48	13		6	21	47		4	34	34	22
9	2	01	15		6	24	47		4	23	33	21
10	2	14	17		6	27	48		4	13	31	20
11	2	27	19		6	29	48		4	02	30	19
12	2	40	20		6	31	48		3	51	29	18
13	2	52	22		6	32	48		3	40	28	17
14	3	04	23		6	33	49		3	29	26	16
15	3	16	24		6	33	49		3	17	24	15
16	3	28	26		6	33	49		3	05	23	14
17	3	40	28		6	32	49		2	53	22	13
18	3	51	29		6	31	49		2	40	20	12
19	4	02	30		6	29	48		2	28	19	11
20	4	12	31		6	27	48		2	15	17	10
21	4	23	33		6	25	47		2	02	15	9
22	4	33	34		6	22	47		1	49	13	8
23	4	44	35		6	18	47		1	35	12	7
24	4	52	36		6	14	46		1	22	11	6
25	4	01	37		6	10	46		1	08	9	5
26	5	09	38		6	05	46		0	55	8	4
27	5	18	39		6	00	45		0	41	6	3
28	5	26	40		5	54	44		0	27	4	2
29	5	33	41		5	47	43		0	14	2	1
30	5	40	42		5	41	42		0	00	0	0
	Sign 5 11				Sign 4 10				Sign 3 9			

Add.

Add.



A Table of the Moons true horary Motion in Eclipses, her horizontal Semidiameters, and Parallaxes, under her least and greatest Eccentricities, with the Suns true hourly Motions and Semidiameters.

Mean Anomaly.	Earth's true hourly Moti.	Sun's Semi- diameter.	Moons true hourly Moti. Excentricity.	Moons hori- zontal Paral. Excentricity.	Moons hori- zontal Semidi. Excentricity.	Mean Anomaly.
			4362   6685	4362   6685	4362   6685	
s "	" "	" "	" "	" "	" "	s "
0 00	2 23 15 50	30 51 29 30	55 35 54 23	15 04 14 45	12 00	
06	2 23 15 50	30 52 29 31	55 35 54 23	15 05 14 45	24	
12	2 23 15 50	30 52 29 33	55 38 54 26	15 05 14 46	18	
18	2 23 15 50	30 52 29 39	55 43 54 31	15 06 14 47	12	
24	2 23 15 51	31 03 29 47	55 48 54 38	15 08 14 49	06	
1 00	2 23 15 52	31 10 29 57	55 54 54 47	15 16 14 52	11 00	
06	2 24 15 53	31 19 30 09	56 01 54 58	15 12 14 55	24	
12	2 24 15 54	31 29 30 22	56 09 55 11	15 14 14 58	18	
18	2 24 15 55	31 40 30 37	56 19 55 25	15 16 15 02	12	
24	2 25 15 56	31 52 30 55	56 30 55 41	15 19 15 06	06	
2 00	2 25 15 58	32 06 31 15	56 42 55 58	15 23 15 11	10 00	
06	2 26 15 59	32 21 31 36	56 56 56 17	15 27 15 16	24	
12	2 26 16 01	32 36 31 59	57 10 56 37	15 30 15 21	18	
18	2 27 16 02	32 54 32 24	57 25 56 59	15 34 15 27	12	
24	2 27 16 04	33 11 32 50	57 39 57 22	15 38 15 34	06	
3 00	2 28 16 06	33 29 33 18	57 54 57 48	15 42 15 40	9 00	
06	2 28 16 08	33 47 33 47	58 10 58 10	15 47 15 46	24	
12	2 29 16 09	34 07 34 15	58 27 58 35	15 51 15 53	18	
18	2 29 16 11	34 26 34 43	58 43 59 01	15 55 16 01	12	
24	2 30 16 13	34 45 35 12	58 58 59 28	16 00 16 07	06	
4 00	2 30 16 14	35 03 35 42	59 13 59 48	16 04 16 14	8 00	
06	2 31 16 15	35 20 36 16	59 28 50 12	16 08 16 20	24	
12	2 31 16 17	35 36 36 36	59 43 50 35	16 12 16 26	18	
18	2 32 16 19	35 51 37 01	59 56 50 56	16 16 16 32	12	
24	2 32 16 20	36 05 37 24	60 07 51 14	16 19 16 37	06	
5 00	2 32 16 21	36 17 37 45	60 16 51 30	16 21 16 41	7 00	
06	2 33 16 21	36 27 38 02	60 24 51 44	16 23 16 45	24	
12	2 33 16 22	36 34 38 15	60 30 51 55	16 25 16 48	18	
18	2 33 16 22	36 39 38 25	60 35 52 03	16 26 16 50	12	
24	2 33 16 23	36 43 38 31	60 38 52 08	16 27 16 51	06	
6 00	2 33 16 23	36 44 38 32	60 39 52 10	16 27 16 52	6 00	

A TABLE of the Angle which the true Motion of the Moon from the Sun, makes with the Ecliptick in the  $\odot$  and  $\odot$ .

Arg. of Latitu.	The true hourly Motion of the Moon from the Sun.												Arg. of Latitu.
Sig. 0	27'	28'	29'	30'	31'	32'	33'	34'	35'	36'			Sig. 11
Sig. 6	0	0	0	0	0	0	0	0	0	0			Sig. 5
gr. 0	5 46 5 45	5 44 5 43	5 42 5 41	5 40 5 39	5 38 5 37	5 36 5 35	5 34 5 33	5 32 5 31	5 30 5 29	5 28 5 27			gr. 30
1	5 46 5 45	5 44 5 43	5 42 5 41	5 40 5 39	5 38 5 37	5 36 5 35	5 34 5 33	5 32 5 31	5 30 5 29	5 28 5 27			29
2	5 46 5 45	5 44 5 43	5 42 5 41	5 40 5 39	5 38 5 37	5 36 5 35	5 34 5 33	5 32 5 31	5 30 5 29	5 28 5 27			28
3	5 46 5 45	5 44 5 43	5 42 5 41	5 40 5 39	5 38 5 37	5 36 5 35	5 34 5 33	5 32 5 31	5 30 5 29	5 28 5 27			27
4	5 45 5 44	5 43 5 42	5 41 5 40	5 39 5 38	5 37 5 36	5 35 5 34	5 33 5 32	5 31 5 30	5 29 5 28	5 27 5 26			26
5	5 45 5 44	5 43 5 42	5 41 5 40	5 39 5 38	5 37 5 36	5 35 5 34	5 33 5 32	5 31 5 30	5 29 5 28	5 27 5 26			25
6	5 44 5 43	5 42 5 41	5 40 5 39	5 38 5 37	5 36 5 35	5 34 5 33	5 32 5 31	5 30 5 29	5 28 5 27	5 26 5 25			24
7	5 44 5 43	5 42 5 41	5 40 5 39	5 38 5 37	5 36 5 35	5 34 5 33	5 32 5 31	5 30 5 29	5 28 5 27	5 26 5 25			23
8	5 43 5 42	5 41 5 40	5 39 5 38	5 37 5 36	5 35 5 34	5 33 5 32	5 31 5 30	5 29 5 28	5 27 5 26	5 25 5 24			22
9	5 42 5 41	5 40 5 39	5 38 5 37	5 36 5 35	5 34 5 33	5 32 5 31	5 30 5 29	5 28 5 27	5 26 5 25	5 24 5 23			21
10	5 41 5 40	5 39 5 38	5 37 5 36	5 35 5 34	5 33 5 32	5 31 5 30	5 29 5 28	5 27 5 26	5 25 5 24	5 23 5 22			20
11	5 40 5 39	5 38 5 37	5 36 5 35	5 34 5 33	5 32 5 31	5 30 5 29	5 28 5 27	5 26 5 25	5 24 5 23	5 22 5 21			19
12	5 39 5 38	5 37 5 36	5 35 5 34	5 33 5 32	5 31 5 30	5 29 5 28	5 27 5 26	5 25 5 24	5 23 5 22	5 21 5 20			18

TABLE XIX.

A TABLE of the time of Reduction, or betwixt the true  $\odot$  or  $\odot$  of the Luminaries, and the nearest Approach of their Centers.

Arg. of Latitu.	Subtract from the time of the true $\odot$ or $\odot$ in the Orbit.												Arg. of Latitu.
Sig. 0	27'	28'	29'	30'	31'	32'	33'	34'	35'	36'			Sig. 5
Sig. 6	0	0	0	0	0	0	0	0	0	0			Sig. 11
gr. 0	0 00 0 00	0 00 0 00	0 00 0 00	0 00 0 00	0 00 0 00	0 00 0 00	0 00 0 00	0 00 0 00	0 00 0 00	0 00 0 00			gr. 30
1	0 35 0 34	0 33 0 31	0 30 0 28	0 27 0 26	0 24 0 23	0 21 0 20	0 18 0 17	0 15 0 14	0 12 0 11	0 09 0 08			29
2	1 10 1 07	1 05 1 03	1 00 0 58	0 55 0 51	0 50 0 47	0 45 0 42	0 40 0 37	0 35 0 32	0 30 0 27	0 25 0 22			28
3	2 45 1 41	1 37 1 34	1 30 1 27	1 25 1 22	1 20 1 17	1 15 1 12	1 10 1 07	1 05 1 02	1 00 0 57	0 55 0 52			27
4	2 20 2 15	2 10 2 05	2 05 2 00	1 56 1 53	1 51 1 47	1 46 1 42	1 41 1 37	1 36 1 32	1 31 1 27	1 26 1 22			26
5	2 55 2 48	2 42 2 36	2 30 2 25	2 21 2 12	2 12 2 03	2 03 1 54	1 54 1 45	1 45 1 36	1 36 1 27	1 27 1 18			25
6	3 29 3 21	3 14 3 07	3 00 2 54	2 48 2 43	2 43 2 38	2 38 2 33	2 33 2 28	2 28 2 23	2 23 2 18	2 18 2 13			24
7	4 04 3 54	3 46 3 38	3 30 3 23	3 16 3 10	3 04 2 58	2 52 2 45	2 40 2 33	2 28 2 21	2 16 2 09	2 04 1 57			23
8	4 38 4 27	4 17 4 03	3 59 3 51	3 43 3 36	3 29 3 23	3 17 3 10	3 04 2 57	2 52 2 45	2 40 2 33	2 28 2 21			22
9	5 11 4 59	4 48 4 38	4 28 4 19	4 04 3 54	3 47 3 40	3 34 3 27	3 21 3 14	3 08 3 01	2 56 2 49	2 43 2 36			21
10	5 44 5 31	5 19 5 07	4 56 4 46	4 34 4 28	4 14 4 07	3 56 3 49	3 38 3 31	3 25 3 18	3 12 3 05	2 59 2 52			20
11	6 17 6 03	5 49 5 37	5 25 5 14	5 03 4 53	4 44 4 37	4 26 4 19	4 08 4 01	3 55 3 48	3 42 3 35	3 29 3 22			19
12	6 50 6 34	6 19 6 06	5 58 5 41	5 29 5 19	5 09 4 59	4 49 4 42	4 31 4 24	4 13 4 06	3 55 3 48	3 42 3 35			18

Add to the time of the true  $\odot$  or  $\odot$  of the Sun and Moon in her Orbit.



A TABLE of the Mean Motions of the Moon from the Sun.

Current Y.	The Mean Motion of the ☾ from the ☉.	Complete Years.	The Mean Motion of the ☾ from the ☉.	Days.	The Mean Motion of the ☾ from the ☉.	M.Motion	M.Motion
s o i u	s o i u	s o i u	s o i u	s o i u	s o i u	H. o i u	H. o i u
1501	06 23 31 29	1	04 09 37 23	1	00 12 11 27	1 00 30 29 31	5 44 47
1502	04 10 26 36	2	08 19 14 45	2	01 24 22 53	2 01 00 57 32	16 15 16
1503	10 04 05 33	3	10 28 52 07	3	01 06 34 20	3 01 31 26 33	16 45 44
1601	02 17 30 17	4	05 20 40 57	4	01 18 45 47	4 02 01 54 34	17 16 13
1621	27 00 55 01	5	10 00 18 20	5	02 00 57 13	5 02 32 23 35	17 46 42
1641	11 14 19 45	6	02 09 55 42	6	02 13 08 40	6 03 02 54 36	18 17 10
1661	03 27 44 29	7	06 19 33 04	7	02 25 20 07	7 03 33 20 37	18 47 39
1681	08 11 09 13	8	11 11 21 54	8	03 07 31 33	8 04 03 49 38	19 18 07
1701	00 24 33 57	9	03 20 59 17	9	03 19 43 00	9 04 34 18 39	19 48 36
1721	05 07 58 41	10	08 00 36 39	10	04 01 54 27	10 05 04 46 40	20 19 05
1741	09 21 23 25	11	00 10 14 01	11	04 14 05 53	11 06 35 15 41	20 49 33
1761	02 04 48 09	12	05 02 02 50	12	04 26 17 20	12 06 05 45 42	21 20 02
1781	06 18 12 54	13	09 11 40 13	13	05 08 28 47	13 06 36 12 43	21 50 31
1801	11 01 37 38	14	01 21 17 35	14	05 20 40 13	14 07 06 41 44	22 20 59
1901	09 08 41 18	15	06 00 54 57	15	06 02 51 40	15 07 37 09 55	22 51 28
2001	07 15 44 59	16	10 22 43 47	16	06 15 03 07	16 08 07 35 46	23 21 56
Complete Julian Y.	Motion of the ☾ from the ☉.	17	03 02 21 10	17	06 27 14 33	17 08 38 09 47	23 52 25
	s o i u	18	07 11 58 32	18	07 09 26 00	18 09 08 35 48	24 22 54
		19	11 21 35 54	19	07 21 37 27	19 09 39 04 49	24 53 22
		20	04 13 24 44	20	08 03 48 53	20 10 09 32 50	25 23 51
2004	13 24 44	Months.	Motion of the ☾ from the ☉.	21	08 16 00 20	21 10 40 01 51	25 54 19
4003	26 49 28		s o i u	22	08 28 11 47	22 11 10 50 52	26 24 48
6001	10 14 12			23	09 10 23 13	23 11 40 58 53	26 55 17
8005	23 38 56			24	09 22 34 40	24 12 11 27 55	27 25 45
1001	07 03 40	Jan.	00 00 00 00	25	10 04 46 07	25 12 41 55 55	27 56 13
20008	14 07 21	Feb.	00 17 54 47	26	10 16 57 33	26 13 12 24 56	28 26 43
30006	21 11 01	Mar.	11 29 15 14	27	10 29 09 00	27 13 42 53 57	28 57 11
40004	28 14 42	Apr.	00 17 10 02	28	11 11 20 27	28 14 13 21 58	29 27 40
50003	05 18 22	May.	00 22 53 22	29	11 23 31 53	29 14 43 50 59	29 58 08
60001	12 22 03	June.	01 10 48 10	30	00 05 43 20	30 15 14 19 00	30 28 37
70011	19 25 43	July.	01 16 31 32	31	00 17 54 47		
80009	26 29 24	Aug.	02 04 26 18	32	01 00 06 13		
90008	03 33 04	Sep.	02 21 21 06				
100006	10 36 45	Oct.	02 28 04 27				
200000	21 13 30	Nov.	03 15 59 14				
300007	01 50 15	Dec.	03 21 42 34				
400001	12 27 00						
500007	23 03 45						

In the Leap-year add a Day to the Time, and a Days Motion to the Motion Collected.

## ARITHMETICK

IN

SPECIES,

OR,

ALGEBRA.

LIB. IV.



Printed at LONDON, by Anne Godbid,  
and John Playford, 1680.

A





ARITHMETICK in SPECIES,

O R

# ALGEBRA,

*Teacheth an Universal Method of Resolving  
all difficult Questions, both in Arithmetick  
and Geometry.*

CHAP. I.

§ 1. Notation.

1. **D**esign all Quantities with Letters, but when any Quantity is taken more than once, prefix its Number, as  $5a$ ,  $7c$ , &c. stands for  $a$  taken five times,  $c$  seven times, or seven times  $c$ , &c. And these prefixed Quantities, whether Numbers, or Letters, denoting some known Quantities, are called *Coefficients*, or *Fellow-factors*.

A 2

2. If



2. If a Letter have no prefix Number or Coefficient, then such a Quantity stands for it self once, and is understood to have 1 for its Prefix or Coefficient.

3. All Quantities expressed by Numbers (as in Vulgar Arithmetick) not having any Letter or Character annexed to them, are called *Absolute Numbers*.

4. A Root and the Powers resulting from the Root are called *Cosicks Quantities*, or *Powers*.

5. The *Indices* are the Terms of an Arithmetical Progression proceeding in the Natural Order of Numbers, as 1, 2, 3, &c. as the *Cosicks* go in a Geometrical, from a Root to a Square, and from a Square to a Cube, &c.

6. The Sum of any two Exponents or Indices, is an *Index* shewing what Power will be produced by the Multiplication of those Powers one in another, which answer to the Indices that were added together.

7. The *Difference* of any two Indices sheweth what Power will be produced by the Division of those Powers one by another, which answer to the Indices that were subtracted.

8. All *Magnitudes* that are under any Power are called *Parodical* to the Power.

9. For distinction, note all Schemes with the Capital or great Letters, and work all *Algebraick* Operations with the small.

10. Numbers prefix to any Quantity shew how often it's to be taken, but set at the head of a Quantity, then shew a Power or Degree of that Quantity.

11. The Sign still belongs to the Quantity following, or to the right hand of it. If a Quantity have no Sign before it, 'tis understood to have the Sign  $+$ .

12. Quantities expressed by Letters are either *Simple* or *Compound*. *Simple* Quantities are such as are expressed either by a single Letter, or by more joyned together like Letters in a Word, as  $a$ ,  $b$ ,  $a$ , &c. *Compound* Quantities consist of two or more simple Quantities joyned together with Signs, as  $b + a$ , &c.

Every one of these four Signs  $+$ ,  $-$ ,  $\infty$ ,  $\times$ , may sometimes have reference to the *Compound* Quantity that followeth the Sign, and hath a Line drawn over every Member, as  $y - r \infty a$ ,  $b - y + x$ , &c.

13. Like Quantities or *Species* are such which are expressed by the same Letters under the same Power, as  $a$  &  $a$ ,  $b$  &  $b$ ,  $c^2$  &  $c^2$ , &c.

14. Unlike Quantities are those which are expressed by different Letters, or by the same Letters under different Powers, as  $a$  &  $b$ ,  $b^2$  &  $b^3$ , &c.

The

The TABLE.

7	6	5	4	3	2	1	0	1	2	3	4	5	6	7	8	Indices:
128	64	32	16	8	4	2	0	$\frac{1}{2}$	$\frac{1}{4}$	$\frac{1}{8}$	$\frac{1}{16}$	$\frac{1}{32}$	$\frac{1}{64}$	$\frac{1}{128}$		Cosf. Pow.
QC S QRC Q R 0								R Q C QRS QC								Ought.
Acc Aqc Aqq Ac Aq A 0								A Aq Ac Aqq Aqc Acc								Har.
&c. aaaa aaa aa a 0								a aa aaa &c.								
$a^7$	$a^6$	$a^5$	$a^4$	$a^3$	$a^2$	$a$	0	$a$	$a^2$	$a^3$	$a^4$	$a^5$	$a^6$	$a^7$		Des Char.
2 Surfolids.	Cubick Cubes.	Surfolids, or Square of Cubes.	Biquadrant.	Cube.	Square.	Root.	Absol. Numbers.	Root.	Square.	Cube.	Biquadrant.	Surfolids.	Cubick Cube.			

The Signs for the more short and quick expressing Words and Operations in Species.

$+$	The Sign of Affirmation or Addition.	$::$	The Sign of Disjunct, Proportion, or Symbol of the Golden Rule.
$-$	The Sign of Negation or Subtraction.	$:::$	Continual Proportion.
$\times$	The Sign of Multiplication.	$=$	The Sign of Equality.
$\infty$	The Sign of Involution.	$>$	Greater than, but some use $>$ .
$\odot$	The Sign of Completion.	$<$	Lesser than, but some use $<$ .
$\div$	The Sign of Division.	$\infty$	Evolution, but some use $\infty$ .
$\sim$	Signifieth the Difference of two Quantities is to be taken, when it's not known which is the greater.	$^{\circ}$	The defect of a Degree.
		$\sqrt{\phantom{x}}$	The Radical Sign, or Sign of Irrationality.
		$\sqrt[3]{\phantom{x}}$	The Sign of an Universal Root.

§ 2. Addition.

When the Quantities to be added, or Species by which they are expressed, are alike, and have like Signs; first add the prefixed Numbers together, and set their common Sign to the left hand thereof. But if the Signs be unlike, subtract the lesser prefixed Number from the greater, and



and to the left hand of the Remainder, prefix the Sign of the Letter wherein the Excess lieth: then to the right hand of that Sum or Difference annex the Letter or Letters, fo is this new Quantity the Sum. But when the Quantities to be added be unlike, write them down one after another in a Rank with their Signs.

	1	2a	a	-a	-a	5b	a	3	-5	b <sup>3</sup>	-7bye
	2	-2a	a	3a	-a	-3b	b	-2	-7	5b <sup>3</sup>	2bye
1-2	3	0	2a	2a	-2a	2b	b -a	1	-12	6b <sup>3</sup>	-5bye

	1	a -b	a-b	a-b	8y	-xc	n	-7n <sup>2</sup>
	2	a -b	a-b	a -b	3y	+5xc	-2a <sup>2</sup>	b -5n <sup>3</sup>
1-2	3	2a+2b	2a-2b	2a	11y	-4xc	-2a <sup>2</sup>	b -n -5n <sup>3</sup> -7n <sup>2</sup>

## § 3. Subtraction.

First change, or imagin to be changed, all the Signs of the Quantities to be subtracted; then add or collect into one Sum by Addition all the Quantities, as well those from which the subtraction was to be made, as the other that were to be subducted; and that Collection or Sum is the Remains or Difference sought.

	1	4a	5a	a	5	-5	-9	a	5a	4a	b <sup>2</sup>
	2	a	-2a	b	-3	3	-7	a	2a	-3a	b <sup>3</sup>
1-2	3	3a	7a	a-b	8	-8	-2	0	3a	7a	b <sup>2</sup> -b <sup>3</sup>
2-3	4	4a	5a	a	5	-5	-9	a	5a	4a	b <sup>2</sup>

	1	a -b	a-b	a -b	a-b	5a <sup>2</sup>	-7 -3y	5c -8b
	2	a-b	a-b	a -b	a -b	3a <sup>2</sup>	+9-2x	6c -b
1-2	3	2b	0	0	-2b	2a <sup>2</sup>	-16+3y+2x	-1c -7b
2-3	4	a -b	a-b	a -b	a-b	5a <sup>2</sup>	-7 -3y	5c -8b

## § 4. Multi-

## § 4. Multiplication.

First Multiply the prefix Numbers together, and connex or joyn the Product and both or all the Letters to be multiplied without any Signs between them; and note, that if the Signs of the Quantities to be multiplied be alike, then the sign of Affirmation is to be prefixed to the Product; But if they be unlike, then the Sign of Negation.

Sometimes in long Compounds, and some other particular Cases, it's necessary to omit the Operation, and joyn or let together the Quantities with the Sign  $\times$  or  $Int$  between them, drawing a conjugating Line over each compound Quantity, as  $a|-b \times r-l$ .

	1	a	3a	ae	a-e	b -1	a	a <sup>2</sup>	aa
	2	e	2e	ae	b	a	a	a	aa
1 x 2	3	ae	6ae	a <sup>2</sup> e <sup>2</sup>	ba-be	ba -a	a <sup>2</sup>	a <sup>3</sup>	aaa

	4	-5y <sup>2</sup>	75	-9	n <sup>5</sup>	a-b	7le	a -e -n
	5	-3y	-3	-7	n <sup>3</sup>	a	-5ry	z
4 x 5	6	15y <sup>2</sup> y	-225	63	n <sup>8</sup>	a <sup>2</sup> -ba	-35lery	az -ez -nz

	7	7e <sup>4</sup>	n -2ma
	8	-3a <sup>3</sup>	-5b
7 x 8	9	-21e <sup>4</sup> a <sup>3</sup>	-5nb

	10	a -e	a -e	a-e
	11	a-e	a -e	a-e
		-ac-e <sup>2</sup>	ac -e <sup>2</sup>	-ac -e <sup>2</sup>
		a <sup>2</sup>  -ae	a <sup>2</sup> -ac	a <sup>2</sup>  -ae
10 x 11		a <sup>2</sup> -e <sup>2</sup>	a <sup>2</sup> -2ac -e <sup>2</sup>	a <sup>2</sup> -2ac -e <sup>2</sup>



③  $a - e$  Root.

$$\begin{array}{r} a - e \\ -ae + e^2 \\ \hline a^2 - ae \end{array}$$

$a^2 - 2ae + e^2$  Square.

$$\begin{array}{r} a - e \\ -a^2e + 2ae^2 - e^3 \\ \hline a^3 - 2a^2e + ae^2 \end{array}$$

$$\begin{array}{r} a^3 - 3a^2e + 3ae^2 - e^3 \end{array}$$

Cube.

③  $a + e$  Root.

$$\begin{array}{r} a + e \\ ae + e^2 \\ \hline a^2 + ae \end{array}$$

$a^2 + 2ae + e^2$  Square.

$$\begin{array}{r} a + e \\ -a^2e + 2ae^2 - e^3 \\ \hline a^3 - 2a^2e + ae^2 \end{array}$$

$$\begin{array}{r} a^3 - 3a^2e + 3ae^2 - e^3 \end{array}$$

Cube.

Hence may be noted, that the Powers of a Residual Root differ from the like Powers from a Binomial only in Sign, and that in each Power of a Residual the Signs prefix to the parts of the Power are alternately  $-$  and  $+$ , viz. the first  $-$ , the second  $+$  &c. Farther, that all the parts or Members of any Power raised from a Binomial or Residual Root, taken together without unity are in continual Proportion.

Again we may note, that admitting  $a$  and  $e$  to be the two parts of a Line or Number, the Sum of the Squares of the said two parts, more the double Rectangle, is equal to the Square of the whole Number; But the Sum of the Squares of the said parts, less the double Rectangle, equals the Square of the Difference of those parts.

The Difference of the Squares of the said parts equals the Product of their Sum and Difference. The Square of their Difference taken from the Sum of their Squares, the Remainder shall be the double Rectangle; or thus, the double Rectangle, more the Square of the Difference, is equal to the Sum of their Squares. The Square of the Difference, less the Quadruple Rectangle, is equal to the Square of their Sum.

The Product of the Difference and Sum added to twice the Rectangle more the double Square of the lesser, makes the Square of their Sum. The Square of the Sum, less the Difference of the Squares, equals the double Rectangle, more the double Square of the lesser Number.

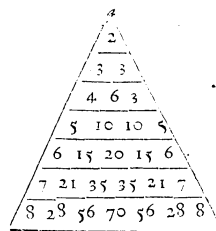
The Square of the Sum, less the double Rectangle, equals the Sum of the Squares.

A Table

A Table of Powers made by the former method of Multiplication, and may thereby be continued at pleasure.

	$a^2$	$a^3$	$a^4$	$a^5$	$a^6$	
$a$	$2ae$	$3a^2e$	$4a^3e$	$5a^4e$	$6a^5e$	
$e$	$e^2$	$3a^2e^2$	$6a^3e^2$	$10a^4e^2$	$15a^5e^2$	$\delta c$
		$e^3$	$4a^3e^3$	$10a^4e^3$	$15a^5e^3$	
			$e^4$	$5a^4e^4$	$6a^5e^4$	
				$e^5$	$e^6$	

The Powers of any Binomial or Residual Root may be thus raised without continual multiplication. Set down all the Parabolic Degrees under the highest Power to each part of the Root, then join them together, prefixing the Unity as in this small Table, which is made and continued by Arithmetical Progression on either side in form of a Triangle, and adding up every two Numbers above for middle or Intermediats under.



¶ 5. The Composition or Genesis of Powers in Numbers from a Binomial Root.

Set the Numbers of the given Root so much distant, that there may be room for the Rectangles; then take the first Number to the left-hand for  $a$ , and the next to it for  $e$ , and work according to the Table for that Power; setting down all the Parts in their due places, add them, and the Sum is the Power of them two Figures; then take the two left-hand Figures of the Root for  $a$ , and the next for  $e$ , and work according to the tenor of the Table, &c.

B

③



[illegible]

9.	3.	6.	4.	3.	5.	
216	...					$a^3$
432	...					$3a^2e$
288	...					$3ae^2$
	64					$e^3$
262	144	...				$a^3$
368	64	...				$3a^2e$
172	8	...				$3ae^2$
	27					$e^3$
265	847	707	...			$a^3$
620	1135	5				$3a^2e$
	482	25				$3ae^2$
		125				$e^3$
266	468	362	875			

The Cube defined.

¶ 6. *Division.*

**D**ivision undoth that which Multiplication composeth or doth ; Therefore take such a Quantity for the Quotient, as being multiplied by the Divisor, the Product may equal the Dividend ; which is done by observing the order of Multiplication, and considering whether the Dividend be composed of the Divisor for one Factor ; for then the other shall be the Quotient : And note, that if the Signs of the Divisor and Dividend be unlike, the Quotient will be negative ; but if like, the Quotient will be affirmative. If the Dividend be not so composed, then set the Dividend over the Divisor in form of a Fraction.

$$b) \quad ba(a^2 - 1)$$
$$\begin{array}{r}
 b) \quad ba \quad (a \qquad 3a^2) \quad 6a^3 \quad (2a \qquad a^3) \quad a^7 \quad (a^4 \qquad a) \quad ae \quad (e \\
 \hline
 a^2) \quad da^3 \quad (da \qquad b) \quad ay \quad \left( \frac{ay}{b} \qquad -3b \right) \quad 9b \quad (-; \qquad 2b-y) \quad 3a \quad \left( \frac{3ax}{2b-y} \right. \\
 \hline
 a-e) \quad ba-be \quad (b \qquad c) \quad bc \div c \quad (b \div 1 \qquad c \div y) \quad c^2 \div c^2 y \quad (c^2 \\
 \hline
 b) \quad zb \div -ab \quad (z \div -a \qquad 5r^2) \quad by-ry \quad \left( \frac{by-ry}{5r^2} \qquad -5b^2 \right) \quad 5rb^2 - 5yb^2 \quad (-rb \div -y) \\
 \begin{array}{r}
 zb \\
 \hline
 0 \div ab \\
 ab \\
 \hline
 0
 \end{array}
 \qquad
 \begin{array}{r}
 5rb^2 - 5yb^2 \\
 \hline
 0 - 5yb^2 \\
 0
 \end{array}
 \end{array}$$

B 2

CHAF.





## CHAP. II.

## FRACTIONS.

## § 1. Abbreviation.

When an Integer is to be prefixed Fraction-wise, give it an *U* for its Denominator.

**I**F the Numerator and Denominator be both Simple Quantities, strike out all the Letters that are alike, both in the Numerator, and Denominator, abbreviating the prefix Numbers (if any) as in Vulgar Arithmetick.

$$\text{Abr. } \frac{acr}{aby} \text{ fa. } \frac{r}{y} \quad \frac{abr}{ady} \text{ fa. } \frac{br}{dy} \quad \frac{byur}{yur} \text{ fa. } \frac{b}{r}$$

$$\text{Abr. } \frac{56ec}{4be-16ze} \text{ fa. } \frac{9e}{b-4z} \quad \frac{12ab-8ay}{16az} \text{ fa. } \frac{3b-2y}{4z}$$

2. If the Numerator and Denominator be Compound Quantities, find a Quantity which will divide both the Numerator and Denominator without leaving any Remains, by which Quantity abridge the Fraction given.

$$\text{Abr. } \frac{an-bn}{a^2-2bas-b^2} \text{ fa. } \frac{n}{a-b} \text{ the common Divisor, by which the Fraction being abridged becomes } \frac{n}{a-b}.$$

2. *Ex.*

## Chap. 2.

## or ALGEBRA.

## § 2. Reduction.

1. **T**O Reduce an Integer to a Fraction of a given Denominator, multiply the Integer and given Denominator together, for a new Numerator, which being set over the Denominator, shall form a Fraction desired.

$$z \text{ reduced to the Denominator } y \text{ fa. } \frac{zy}{y}.$$

$$r+f \text{ reduced to the Denominator } b \text{ is } \frac{br+bf}{b}.$$

2. To find the smallest Quantity that can be divided by two or more given Quantities severally without a Remainder.

If the given Quantities be in their least Terms, multiply them together, and that Product is the Quantity that will answer the demand.

But if they be not in their least Terms, reduce them (by abbreviation) to their least Terms, and setting them Fraction-wise multiply cross, and that Product is the Quantity sought.

3. To Reduce Integers and Fractions to Improper Fractions, multiply the Integral Parts by the Denominator of the Fraction, and to the Sum add the Numerator, which Sum is the new Numerator.

$$b + \frac{y}{a} \text{ makes } \frac{ba+y}{a}.$$

4. To reduce an Improper Fraction to an Integer and Fraction, divide the Numerator by the Denominator; thus:

$$\frac{be+cer}{c} \text{ makes } b + \frac{cer}{c}.$$

5. To reduce Fractions of divers Denominations to one Denomination.

Multiply the Numerator of each Fraction into all the Denominators, except its own, so the Products made by that continual Multiplication shall be new Numerators, and multiply all the Denominators together for a new Denominator.

$$\frac{ac}{b} \text{ and } \frac{br}{a} \text{ reduced, make } \frac{a^2c}{ba} \text{, } \frac{br}{ba}.$$

$$\frac{e}{r}, \frac{y}{z}, \frac{ceg}{h} \text{ reduced } \frac{exb}{h}, \frac{ryb}{rxz}, \frac{2rxeg}{x..b}.$$

§ 3. *Subst.*



§ 3. Addition and Subtraction of Fractions.

If the Fractions be of one Denomination, add or subtract their Numerators, and set the Sum or Remains as a new Numerator over the Common Denominator; but if they be of divers Denominations, reduce them first to one Denomination, and then add or subtract them.

Add  $\frac{ly}{r}$  to  $\frac{sr}{t}$ , reduced they are  $\frac{tly + sr^2}{tr}$ , and the Sum  $\frac{tly + sr^2}{tr}$

Take  $\frac{br - a}{f}$  from  $\frac{r^3y}{2b}$ , reduced they are  $\frac{2b^2r - 2ba}{2bf}$   $\frac{r^3yf}{2bf^2}$  and the Difference  $\frac{r^3yf - 2b^2r - 2ba}{2bf^2}$ .

§ 4. Multiplication of Fractions.

Multiply the Numerators together for a new Numerator, and the Denominators for a new Denominator, which new Fraction shall be the Product.

Mult.  $a$  by  $\frac{5}{a}$  Product  $\frac{5a}{a}$ .  $\frac{5y^2}{c}$  by  $\frac{r}{7d}$  Product  $\frac{5y^2r}{7cd}$

Mult.  $\frac{3b}{2y}$  by  $\frac{fr}{ab}$  Product  $\frac{3bfr}{2yba}$  or  $\frac{3fr}{2ya}$

§ 5. Division.

Multiply cross-wise the Numerator of the Divisor by the Denominator of the Dividend for a new Denominator, and the Numerator of the Dividend by the Denominator of the Divisor for a new Numerator; but when the Fractions are of the same Denomination, divide the Numerators by each other, casting away the Denominators.

$\frac{b}{a}$   $\frac{r}{a}$   $\left(\frac{r}{b} \frac{y}{2}\right)$   $\frac{5}{z}$   $\left(\frac{10}{yz} \frac{2}{3}\right)$   $\frac{r}{y}$   $\left(\frac{3r}{2y} 7\right)$   $\frac{r^2b}{a}$   $\left(\frac{r^2b}{7a}\right)$

$\frac{ab}{y}$   $3zb$   $\left(\frac{3yzb}{ab} \frac{f^2 - r}{5y}\right)$   $\frac{g^2b}{r-f}$   $\left(\frac{5yg^2b}{f^2r - r^2 - f^3 - f^4}\right)$

CHAP.



CHAP. III.

Evolution, or Extraction of Roots of Simple Species.

Divide the Index of the Quantity, out of which the Extraction is to be made, by the Index of the Power to be Extracted, and the Quotient is the Index of the Root; as to Extract the Square Root of a Quantity, divide the Index by 2; if the Cube Root, by 3, &c. and deal with the prefix Numbers as in Vulgar Arithmetick. But if the Root cannot be Extracted, prefix to the Quantity out of which the Extraction was to be made, the  $\sqrt{\phantom{x}}$  with the Index of the Power before it, hence ariseth Surds.

To extract a Root out of a Fraction, first Extract the Root of the Numerator, and then of the Denominator, which new Fraction is the Root desired. But if the intended Root cannot be extracted out of either Numerator or Denominator, prefix the Radical Sign.

1	1	$a^4$	$216c^3$	$36yy$	$81gg$	$8fff$	$a^2b^2$	$\frac{a^2b}{cc}$
1	2	$a^2$	$\sqrt{216c^3}$	$6y$	$9g$	$2\sqrt{2fff}$	$ab$	$\frac{a\sqrt{b}}{c}$
1	3	$\sqrt[3]{(3)a^4}$	$6c$	$\sqrt[3]{(3)36y^2}$	$3\sqrt[3]{(3)3g^2}$	$2f$	$\sqrt[3]{(3)a^2b^2}$	$\sqrt[3]{(3)\frac{a^2b}{cc}}$
1	4	$a$	$\sqrt[4]{(4)216c^3}$	$\sqrt[4]{6y}$	$3\sqrt[4]{g}$	$\sqrt[4]{(4)8fff}$	$\sqrt[4]{ab}$	$\sqrt[4]{(4)\frac{a^2b}{cc}}$

§ 11. The



§ 1. The Analysis, or Extraction of Roots out of Numbers.

**D**istinguish the given Number with Points, according to the Number of Means or Rectangles, between the two Diagonal Powers in the Table. Then out of the Figures of the first Point, or first set of Figures towards the left hand, take the greatest Root of the kind to be Extracted that is in them, which Root call  $a$ , then  $a$  being rightly ordered according to the Table, makes a Divisor, by which divide, and the Quotient is the second Figure of the Root  $e$ ; so  $a$  and  $e$  rightly compoed according to the Table, produce the Sum to be subtraced, or *Gnomon*. Then to find another Figure of the Root, take the two Figures of the Root already found for a new Value of  $a$ , which compoed according to the Table, make a new Divisor; by which divide, and the Quotient is a new Value of  $e$ ; which  $a$  and  $e$  ordered according to the Table, make the *Gnomon*, or *Ablatium*, which must be subtraced. Then take the three Figures of the Root already found, for a new Value of  $a$ , which compoed into a Divisor, &c.

If the Number doth not divide off, but something remain, set so many Punctations of Cyphers for that kind, as shall be judged needful, and continue the Extraction therewith.

If the Numbers propounded be a Fraction or mixed Number, reduce it to a Decimal, and then Extract the Root thereof, as before.

⊙ 2. 682 | 7315 (2612

4		$a^2$
28		Refol.
4		$2a$ Divisor.
24		$2ae$
36		$e^2$
276		Ablat.
673		Refol.
52		$2a$ Divisor.
52		$2ae$
1		$e^2$
521		Ablat.
15215		Refolv.
522		Divisor.
104		$2ae$
1		$e^2$
1		Ablat.

⊙ 3. 15625 (25

8		$a^2$
7625		Refolvend.
12		$3a^2$
6		$3a$
126		Divisor.
60		$3ae$
150		$3ae^2$
125		$e^3$
7625		Subducend.
1000		

⊙ 4.

⊙ 4.	39525	6871	(141
1			$a^2$
29525			Refol.
4			$4a^3$
6			$6a^2$
4			$4a$
4640			Divisor.
16			$4a^3e$
96			$6a^2e^2$
256			$4ae^3$
256			$e^4$
28416			Subducend.
1109		6871	Refol.
1097		6	$4a^3$
1176		6	$6a^2$
56		4	$4a$
1109		416	Divisor.
1097		6	$4a^3e$
1176		6	$6a^2e^2$
56		4	$4ae^3$
1		1	$e^4$
1109		4161	Subduc.
		2710	Rem.

§ 2. Surds.

**A**LL Quantities that have not a Radical Sign prefix are called Rational, whether they be Integers or Fractions; but if any Root be desired out of any Quantity, and cannot be Extracted perfectly, that Quantity is called Surd, and hath the Sign of the desired Root prefix.

G

CHAP.





## CHAP. IV.

## E Q U A T I O N.

§ 1. *An Equation is a mutual comparing of equal Quantities, or Things.*

**W**hen a Question is propounded, in the first place the meaning of it must be clearly comprehended; which that you may do, when any Arithmetical Question (wherein Numbers are mixt or confounded with material things, as Men, Money, Time, &c.) is propounded, separate the same from such things, and see how it will stand, or be propounded in the pure consideration of Numbers.

2. Then design, note, or express all the Quantities in the Question, as well unknown as known, with Letters; the known with great Letters, and the unknown with small; or the known with the Letters in the first part of the Alphabet, and the unknown with those of the Latter end, as *TZ*, &c. forming them into Equations; (but when diverse Quantities are granted to be equal, they may be expressed by the same Letter;) which Equations must be ordered, disposed, and moulded, according to the import of the Problem or Question, till all the unknown Quantities vanish but one.

3. And note, that (in a Question so stated) if the unknown Symbols or Letters be more than the number of Equations, nor mutually depending upon one another, the Question is not fully limited, but is capable of innumerable Answers. A Problem hath a certain determinable number of Answers, when the Equations, no ways depending one upon another, are as many just as the Quantities unknown or sought.

To prescribe Rules which may hold in all cases, for the raising off all the unknown Quantities but one, is a difficult, if not impossible, work; yet here shall be inserted three Rules, which are so comprehensive, that

few

few Questions will fall without them, and those that do, an Ingenious person will soon discover the way to proceed by their due intermixture.

## Rule I.

**VV**hen the same Quantity is found in two several Equations, with equal prefixes, if their Signs be like subtract them, but if unlike add them.

## Rule II.

**VV**hen the same Quantity is found in two several Equations, with unequal prefixes; multiply the first Equation by the prefix, to the said Quantity in the second Equation, and the second Equation by the prefix to the said Quantity in the first; then will the prefixes to the said Quantity be the same in both Equations, and so fall under the first Rule, for farther clearing. Lastly, if there be more such Equations by repeating the former work; expell the same Quantity out of them also.

## Rule III.

**I**f neither of the two Rules above will take place, by Chap. 4. § 2. following, bring the Quantity you first intended to banish to one side of the first Equation alone, making the Equation stand between it and the other; then in the place of that Quantity substitute its equal, through all the Equations, so shall they be cleared of that; afterwards bring by Transposition a second Letter to stand alone on one side of one of the Equations as before, substituting the other side of that Equation every where, throughout all the other Equations, in the Room of this second Letter to be taken away, so proceeding with the third, fourth &c. till all the unknown be taken away, save one.

Then for as much as every Problem when thus brought to one single Equation, hath yet the known Quantities interwoven or mixed with that unknown; the next work will be to clear it of all superfluous Quantities, and to separate the known, from the unknown. (keeping still an Equality) that at length the Equation may remain in the fewest and simplest termes, so ordered, that the known Quantities may make one side of the Equation and the unknown the other, which Operation fits the Equation for Reduction, and is called Reduction.



§ 2. By Addition and Subtraction.

**V**Hen known Quantities be joyned or linked with unknown, in one side of an Equation, transfer Terms from one side of the Equations to the other, changing their Signs. This Operation it self is called *Transposition*.

$$\begin{array}{l} 1 - A^2 \\ 2 - DB \end{array} \left| \begin{array}{l} 1 \mid DA - DC = A^2 + b^2 - DB + dc \\ 2 \mid DA - DC - A^2 = b^2 - DB + dc \\ 3 \mid DA - DC - A^2 - DB = b^2 - dc \end{array} \right| \begin{array}{l} 1 - ac \\ 2 - RC = n - ac \end{array}$$

$$\begin{array}{l} 1 - A^2 \\ 2 - a^2 \end{array} \left| \begin{array}{l} 1 \mid a^2 - \sqrt{5} B^2 = ry - A^2 \\ 2 \mid A^2 - a^2 - \sqrt{5} B^2 = ry \\ 3 \mid A^2 - \sqrt{5} B^2 = ry - A^2 \end{array} \right| \begin{array}{l} 1 - A^2 \\ 2 - y^2 \end{array} \left| \begin{array}{l} 1 \mid y^2 + 5 A^2 = A^2 + rr \\ 2 \mid y^2 + 4 A^2 = rr \\ 3 \mid 4 A^2 = rr - y^2 \end{array} \right|$$

§ 3. By Multiplication.

**I**F the Quantity sought, or any Degree or Power thereof be in a Fraction, reduce, as in Reduction of Fractions (*viz.* by cros multiplying) the parts thereof to one Denomination; that omitting that common Denominator, the Equation may be expressed by the Numerators only.

$$1 \times a - r \left| \begin{array}{l} 1 \mid a = \frac{D^2}{a-r} \\ 2 \mid a^2 - ar = D^2 \end{array} \right| 1 \times b \left| \begin{array}{l} 1 \mid a + c = \frac{Aa}{b} \\ 2 \mid ba + bc = Aa \end{array} \right|$$

$$1 \times nc \left| \begin{array}{l} 1 \mid \frac{3vv}{c} = \frac{B^2}{n} \\ 2 \mid 3vvv = B^2 C \end{array} \right| 1 \times e^2 - nc + N^2 \left| \begin{array}{l} 1 \mid \frac{e^3}{e^2 - nc + N^2} = \frac{rA}{1} \\ 2 \mid e^3 = rAc^2 - rAnc + rAN^2 \end{array} \right|$$

*To clear an Equation of the Radical Sign.* When there is an Equation between Homogencal Surds, cast away the Radical Sign, and let the Equation stand in Rational Quantities.

When

When one part of an Equation is a Surd Quantity, and the other a Rational, multiply the Rational part either Quadratically, or Cubically, &c. according to the Index of the Radical Sign, and cast away the Radical Sign from the other part.

$$1 \oplus 2 \left| \begin{array}{l} 1 \mid b + r = \sqrt{c} \\ 2 \mid b^2 + 2br - r^2 = c \end{array} \right| \begin{array}{l} \sqrt{c} : ac - n = c \\ ac - n = c^2 \end{array}$$

§ 4. By Division.

**I**F the known Quantity be found in each Member of an Equation, divide the whole Equation by the least Degree of the unknown Quantity, which shall clear one Member or Term thereof from the unknown Quantity.

$$1 \div a \left| \begin{array}{l} 1 \mid Ba^2 - 15 Ra = a \\ 2 \mid Ba - 15 R = 1 \end{array} \right| \begin{array}{l} a^3 - Xa^2 = C^2 a \\ a^2 - Xa = C^2 \end{array}$$

If the highest Power of the unknown Quantity be multiplied in a known, divide the Equation by that known Quantity, thereby clearing the highest Power of the unknown from all the known Quantities.

$$1 \div B \left| \begin{array}{l} 1 \mid Ba^3 - 3Ra = N \\ 2 \mid a^3 - \frac{3Ra}{B} = \frac{N}{B} \end{array} \right| 1 \div 5 \left| \begin{array}{l} 1 \mid Da^2 - 5a^2 = B - 18 \\ 2 \mid \frac{Da^2}{5} - a^2 = \frac{B - 18}{5} \end{array} \right|$$

§ 5. To convert Analogies into Equations.

**I**F four Quantities be Proportional, the Product of the Extreams is equal to the Product of the Means.

If three Quantities be Proportional, the Product of the Extreams is equal to the Square of the Mean.

$$\begin{array}{l} 7 \times \frac{ab}{7} \\ a \times b \\ 2, 3 \end{array} \left| \begin{array}{l} 1 \mid 7 : a :: b : \frac{ab}{7} \\ 2 \mid ab \\ 3 \mid ab \\ 4 \mid ab = ab \end{array} \right| \begin{array}{l} a \times d \\ b \times c \\ 2, 3 \end{array} \left| \begin{array}{l} 1 \mid a : b :: c : d \\ 2 \mid ad \\ 3 \mid bc \\ 4 \mid ad = bc \end{array} \right|$$

$I \times 4$



	1	$n$
	2	$r$
	3	$al$
	4	$y$
	5	$n \cdot r :: al \cdot y$
1 x 4	6	$ny$
2 x 3	7	$ral$
6, 7	8	

§ 6. To convert Equations into Analogies.

IF the Rectangle of two Quantities be equal to the Rectangle or Product of two other; say, *As* either of the Factors in one side of the Equation, *Is* to either of the Factors in the other part: *So* is the other Factor in the last part, *To* the other Factor in the first part.

1	$ba=an$	$rl=ny$	$\frac{ry}{b}=a.$
2	$b \cdot n :: a \cdot a$	$r \cdot n :: y \cdot l$	$b \cdot r :: y \cdot a$

§ 7. The Order in which those Reductions are to be used, in Clearing and Trimming an Equation.

1. IF there be any Fractions in an Equation, let them be cleared of their Denominators by § 3. Chap. 4. also by the same; let the Surd Character be taken away, if there be any.

2. If the unknown Quantity be found in all the Terms, you must clear as many of the Terms of it as may be, by § 4. Chap. 4. but if all the Terms may be cleared, that Equation is Identical and vain, and may be resolved by any Number whatever.

3. If several like terms be distributed, let them be gathered into one Term by the prescription of their Signs and known Factors, placing the highest Power of the unknown Quantity first (most finitely) and the rest of the inferior Powers, or Parodical Degrees, succeeding in their order, the Absolute possessing the other side of the Equation, by § 2. Chap. 4.

4. If there be a known Factor in the now first Term, or highest Power of the unknown, let it be cleared by § 4. Chap. 4.

Equations thus cleared and reduced are either Pure and Simple, or Admixed and Compound.

Pure and Simple Equations are such whose unknown part or side is a Simple Root or Power.

An Admixed, or Compound Equation, is that wherein there are two or more differing Degrees or Powers of the unknown Quantity.

CHAP.



CHAP. V.

Questions producing a Simple Equation.

1. A Certain Man goeth 29 Miles a day, another followeth him from the same place, but setteth forth 7 days after, and goeth 36½ Miles each day. In how many days will the last overtake the first?

	1	$B=203=29 \times 7$	
	2	$C=29$	
	3	$D=36\frac{1}{2}$	
	4	$y?$	$\frac{1}{2}y$
4 x 3	5	$yD$	$29y$
4 x 2	6	$yC$	$29y + 203$
6 + 1	7	$yC + B$	$29y + 203 = \frac{1}{2}y$
7, 5	8	$yC + B = yD$	$\frac{1}{2}y - 29y = 203$
8 - yC	9	$yD - yC = B$	$y = \frac{203}{7.5}$
9 ÷ D - C	10	$y = \frac{B}{D - C}$	

2. A certain Man finding divers Poor People at his door, gave each of them 3 d. and had 6 d. remaining in his pocket; but if he would have given them 4 d. each, he must have wanted 2 d. How many Poor were there?

		$d.$	
	1	$B=5$	
	2	$C=6$	
	3	$D=4$	
	4	$H=2$	
	5	$y=?$	
1 x 5	6	$By$	$3y$
6 x 2	7	$By + C$	$3y + 6$
3 + 5	8	$Dy$	$4y$
8 - 4	9	$Dy - H$	$4y - 2$
7, 9	10	$Dy - H = By + C$	$4y - 2 = 3y + 6$
10 - By + H	11	$Dy - By = C + H$	$4y - 3y = 8$
11 ÷ D - B	12	$y = \frac{C + H}{D - B}$	$y = 8.$

3. The



3. The Sum of two Numbers  $S$ , 84 and their Difference  $D$ , 39: what are the Numbers?

Rule 1.	$y = ?$	1	$y - z = S$	$y - z = 84$
	$z = ?$	2	$y - z = D$	$y - z = 39$
	$1 + 2$	3	$2y = D + S$	$2y = 123$
	$3 \div 2$	4	$y = \frac{D+S}{2}$	$y = 61\frac{1}{2}$
	$1 - 2$	5	$2z = S - D$	$2z = 45$
	$5 \div 2$	6	$z = \frac{S-D}{2}$	$z = 22\frac{1}{2}$

4. The Sum of two Numbers  $S$  (9) and quintuple product  $\frac{5}{4}P$  (100) given, to find the Numbers?

Rule 2.	$y ?$	1	$y - z = S$	$y - z = 9$
	$z ?$	2	$\frac{5}{4}yz = \frac{5}{4}P$	$\frac{5}{4}yz = 100$
	$2 \div \frac{5}{4}$	3	$yz = P$	$yz = 20$
	$1 \times y$	4	$y^2 + yz = Sy$	$y^2 + yz = 9y$
	$4 - 3$	5	$y^2 = Sy - P$	$y^2 = 9y - 20$
	$5 - y^2$	6	$Sy - y^2 = P$	$9y - y^2 = 20$

Which happening to be an affected Equation, the Solution must be omitted till a fit place.

5. There be two Numbers whose difference is  $D$  7, with this property, that if the lesser be multiplied by  $B$  2, and  $C$  (3) added to the Product, the Sum may equal the greater multiplied by  $F$  6 and  $V$  1 added to that Product? what be the Numbers?

Rule 3.	$y = ?$	1	$y - z = D$	$y - z = 7$
	$z = ?$	2	$zB + C = yF + V$	$2z + 3 = 6y + 1$
	$1 - z$	3	$y - D + z$	$y = 7 + z$
	$3 \times F$	4	$FD - Fz$	$4z$
	2. <i>aliter</i>	5	$zB - C = FD - Fz + V$	$2z + 3 = 4z + 6z$
	$5 - Fz$	6	$zB - Fz + C = FD - V$	$3 = 4z + 4z$
	$6 - C$	7	$zB - Fz = FD + V - C$	$3 - 4z = 4z \text{ or } -4z = 4z$
	$7 \div B - F$	8	$z = \frac{FD + V - C}{B - F}$	$\frac{-4z}{4} = -10 = z?$
	1. $z - D$	9	$y - D = z$	$y - 7 = z$
	$9 \times B$	10	$By - BD$	$2y - 14$
	2. <i>aliter</i>	11	$By - BD + C = yF + V$	$2y - 11 = 6y + 1$
	$11 - yF$	12	$By - yF - BD + C = V$	$2y - 6y - 11 = 1$
	$12 - C + BD$	13	$By - yF = V - BD - C$	$-4y = 12$
		14	$y = \frac{V - BD - C}{B - F}$	$y = \frac{12}{-4} = -3?$

THE SIX

## FIRST BOOKS

OF



## Euclid's Elements.



Printed at LONDON, by Anne Godbid,  
and John Playford, 1680.

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THE





THE  
FIRST BOOK  
OF  
Euclid's Elements.

DEFINITIONS.

1. **A** *Point* is that which hath no Parts.
2. A *Line* is length without breadth.
3. The ends, or limits of a *Line*, are Points.
4. A *Right-Line* is that which lieth evenly between its terminating Points.
5. A *Superficies* is that which hath only length and breadth.
6. The extreames, or limits of a *Superficies*, are Lines.
7. A *Plain-Superficies* is that which lieth evenly betwixt its Lines.
8. A *Plain-Angle* is the Inclination of two Lines one to the other, the one touching the other in the same Plain, yet not lying in the same *Grait* Line.
9. If the Lines which contain the Angle be Right-Lines, it is called a *Right-lined Angle*.



10. When a Right-Line  $AB$  standing on a Right-Line  $CD$ , makes the Angles on either side thereof, viz.  $ABC$ ,  $ABD$ , equal, then they are *Right-Angles*; and the Right-Line  $AB$  which standeth upon the other is a Perpendicular to that on which it stands,  $CD$ . The mark for the Perpendicular is  $\perp$ , and for a Right-angle  $\angle$ .

An *Angle* is marked commonly either with one Letter, which is set at the Angular Point, or with three; the middlemost whereof shews the Angular Point; and the other Letters the Lines that make that Angle: As the Angle which the Right-Lines  $AB$ ,  $CB$ , make at  $B$ , is called  $CBA$ , or  $ABC$ , or  $B$ , omitting the Letters  $A$  and  $C$ .

11. An *Obtuse-Angle* is that which is greater than a Right-Angle, as  $EBC$ .

12. An *Acute-Angle* is that which is less than a Right-Angle, as  $EBD$ , and its Character shall be  $\angle$ , which is also used for the word *Angle*, when the kind is undetermined.

13. A *Limit*, or *Term*, is the end of any thing.

14. A *Figure* is that which is contained under one or more Terms.

15. A *Circle* is a plain Figure contained under one Line, which is called a *Circumference*, unto which all the Lines  $DA$ ,  $DE$ ,  $DC$ , drawn from one Point within the Figure, are equal one to the other.

16. And that Point is called the *Center of the Circle*, the Character for a Circle is  $\circ$ .

17. A *Diameter of a Circle* is a Right-Line  $AB$ , drawn through the Center thereof  $D$ , and terminated on either side by the Circumference  $A$  and  $B$ , and it divides the Circle into two equal parts.

18. A *Semicircle* is a Figure contained under the Diameter  $AB$ , and that part of the Circumference  $ADB$ , which is cut off by the Diameter.

19. *Right-lined Figures* are such as are contained under Right Lines.

20. *Three Sided*, or *Trilateral Figures* are such as are contained under three Right-Lines.

21. *Four Sided*, or *Quadrilateral Figures*, are such as are contained under four Right-Lines.

22. *Many Sided Figures*, or *Multilaterals*, are such as are contained under more Right-Lines than four.

23. Of *Trilateral Figures*, that is an *Equilateral  $\Delta$* , which hath three equal Sides, as the  $\Delta A$ .

24. An *Isosceles* is a  $\Delta$  which hath only two Sides equal, as the  $\Delta B$ .

25. *Scalenum* is a  $\Delta$  whose three Sides are all unequal, as  $C$ .

26. Of these *Trilateral Figures*, a *Right-Angled  $\Delta$*  is that which hath one Right  $\angle$ .

27. An *Amblygonium*, or *Obtuse-Angled  $\Delta$* , is that which hath one Obtuse  $\angle$ .

28. An *Oxygonium*, or *Acute-Angled  $\Delta$* , is that which hath three Acute  $\angle$ s.

■ An *Equiangular Figure* is that whereof all the  $\angle$ s are equal. The same is to be understood of *Equilateral*s.

31. Of

29. Of *Quadrilateral*, or four sided *Figures*, a *Square* is that whose sides are equal, and  $\angle$ s *Right*; as  $ABCD$ .

30. A *Figure* on the one part longer, or an *Oblong*, is that which hath *Right  $\angle$ s*, but not equal sides; as  $ABCD$ .

31. A *Rhombus*, or *Diamond-Figure*, is that which hath Four equal sides, but not  $\angle$ s: as  $A$ .

32. A *Rhomboides* is that whose opposite sides and opposite  $\angle$ s are equal; but hath neither equal sides nor  $\angle$ s; as  $B$ .

33. All other *Quadrilateral Figures* besides these, are called *Trapezia*, as the *Figure C*.

34. *Parallel* or *Equidistant Right-Lines*, are such, as being on the same plain, if *Infinitely produced*, would never meet; as  $A$ , and  $B$ . And their mark is  $\parallel$ .

35. A *Parallelogram* is a *Quadrilateral Figure*, whose opposite Sides are *Parallel*; as the  $\square$ ,  $\square$ ,  $\square$ ,  $\square$ . *Square*, *Oblong*, *Rhombus*, and *Rhomb*; and its Character is  $\square$ .

36. When in a  $\square$   $ABED$  are drawn the *Diameter* (or rather *Diagonal*)  $DB$ , and two Lines  $HK$ ,  $CF$  *Parallel* to the Sides, cutting the *Diameter* in one and the same Point  $G$ , so that the  $\square$  be divided by them into Four  $\square$ s; those two  $AG$ ,  $GE$ , through which the *Diameter* passes not, are called the *Complements* of those standing about the *Diameter*; viz. of  $HF$ , and  $CK$ .

Whatever is proposed to be either done or demonstrated is called a *Proposition*; and is either *Problem* or *Theorem*.

A *Problem*, is somewhat proposed to be done or effected.

A *Theorem*, is somewhat proposed to be Demonstrated.

A *Corollary*, is some consequent Truth gained from a preceeding Demonstration.

A *Lemma* is the Demonstration of some Premise, whereby the proof of the thing about, becomes the shorter.

An *Axiome*, is that which is self evident, and is Comprehensible at the first proposing to all.

#### Postulates or Petitions.

1. From any point  $A$ , to any point  $B$ , to draw a Right-Line  $AB$ .
2. To produce a *Finite* Right-Line,  $AB$  strait forth continually.
3. Upon any Center, and at any Distance or Extent, to Describe a Circle.

#### Axioms.

1. Things equal to the same, are also equal one to the other; As  $a=b=c=d=f$ ; Therefore  $a=f$ , and consequently all  $a, b, c, d, f$ , are equal one to the other.
2. If to equal things, equal things be added, the wholes will be equal.

3. If



3. If from equal things, equal things be taken away, the remains will be equal.

4. If to unequal things, equal things be added, the wholes will be unequal.

5. If from unequal things, equal things be taken, the Remainders will be unequal.

6. Things which are double to the same thing, are equal one to the other. Understand the same of Triple, Quadruple, &c.

7. Things which are half one and the same thing, are equal one to the other. Understand the same of Subtriple, Subquadruple, &c.

8. Things which agree together, are equal one to the other.

The converse of this *Axiom* is true in Right-Lines and  $\angle^s$ , but not in *Figures*, unless they be like.

*Magnitudes* are said to agree, when the parts of the one being apply'd to the parts of the other they fill up an equal place.

9. Every whole is greater than it's part.

10. All Right  $\angle^s$  are equal between themselves.

11. Two Right-Lines cannot have one and the same Segment (or part) common to them both.

12. Two Right-Lines meeting in the same point, if they be both produced, shall necessarily cut one the other in that Point.

13. If a Right-Line  $BA$  falling on two Right-Lines  $AD, CB$ , make the Internal  $\angle^s$  on the same Side,  $BAD + ABC, \rightarrow 2 \angle^s$ , those two Right-Lines produced shall meet on that Side, wherethe  $\angle^s$  are  $\rightarrow 2 \angle^s$ .

14. Two Right-Lines do not contain a Space.

15. Every whole is equal to all its parts taken together.

The Citation in the Margent, understand thus, if there be two Numbers, the first shews the Proposition, the second the Book.

*Ax.* is for Axiom, *Post.* Postulate, *Def.* Definition, *Sch.* Scholium, *Cor.* Corollary. Also note, that  $WW D$ , stands for, which was to be Demonstrated, and  $WW D n$ , which was to be done. Further note, that *Pro.* stands for Proof; *Præ.* for Preparation; and *Præ.* for Praxis.

### Prop. I.

Problem 1.

Upon a finite Right-Line given,  $AB$ , to describe an equilateral  $\Delta, ACB$ .

(a) 3 *post.*  
(b) 1 *post.*  
(c) 15 *def.*  
(d) 4. 1. *ax.*  
(e) 23 *def.*

ON the Centers  $A$  and  $B$ , with the extent  $AB$  or  $BA$ , <sup>a</sup> describe two  $\bigcirc^s$  cutting each other in the point  $C$ : from whence <sup>b</sup> draw the two Right-Lines  $CA, CB$ . Then is  $AC = AB = BC^d = AC$ , <sup>e</sup> Wherefore the  $\Delta ACB$  is Equilateral.  $WW D n$ .

Scholium.

Scholium.

After the same manner may be described upon the Line  $AB$  an Isosceles  $\Delta$ , if the Semidiameters of the equal  $\bigcirc^s$  be taken greater or lesser than the line  $AB$ .

### Prop. II.

At a point given,  $A$ , to make a Right-Line,  $AG$ , equal to a given Right-Line,  $BC$ . Problem 2.

ON the Center  $C$ , with the Extent  $CB$ , <sup>a</sup> describe the  $\bigcirc CBE$ ; <sup>b</sup> joyn  $AC$ ; upon which <sup>c</sup> make the Equilateral  $\Delta A'DC$ . <sup>d</sup> Produce  $DC$  to  $E$ . On the Center  $D$ , with the Extent  $DE$ , describe the  $\bigcirc DEH$ ; and let  $DA^e$  be produced to the point  $G$ . Then  $AG = CB$ .  
For  $DG^f = DE$ , and  $DA^g = DC$ . Wherefore  $AG^h = CE^i = BC^k = AG$ .  $WW D n$ . The falling of the point  $A$ , within or without the Line  $BC$  varies the Case; yet the Construction and Demonstration continue the same.

(a) 3 *post.*  
(b) 1 *post.*  
(c) 1. 1.  
(d) 2 *post.*  
(e) 2 *post.*  
(f) 15 *def.*  
(g) *conf.*  
(h) 3 *ax.*  
(i) 15 *def.*  
(k) 1 *ax.*

Scholium.

This, and the preceding Problem might be performed much easier, mechanically with a pair of Compasses; but that will answer to no postulate, as intimated by *Proclus*.

### Prop. III.

Two unequal Right-Lines,  $A$  and  $BC$ , being given, to take from the greater,  $BC$ , the Right-Line  $BE$ , equal to the lesser  $A$ . Problem 3.

TO the point  $B$  <sup>a</sup> draw the Right-Line  $BD = A$ . The  $\bigcirc$  Described on the Center  $B$  with the Extent  $BD$  shall cut off  $BE^b = BD^c = A^d = BE$ .  $WW D n$ .

(a) 2. 1.  
(b) 15 *def.*  
(c) *conf.*  
(d) 1 *ax.*

Prop. IV.



## Prop. IV.

Theorem 1. If two  $\Delta^s$   $BAC$ ,  $EDF$ , have two sides of the one equal to two sides of the other, that is,  $AB$  to  $DE$  and  $AC$  to  $DF$  and the  $\angle^s$  contained by these sides, viz.  $A$  and  $D$  equal: they shall have the base  $BC$  equal to the base  $EF$ ; and the  $\Delta BAC = \Delta EDF$ ; and the remaining  $\angle^s$  of the one shall be equal to those remaining of the other, each to its correspondent, that is,  $B$  to  $E$ , and  $C$  to  $F$  according to the equal subtending sides.

Pro. The side  $AB$  is put equal to the side  $DE$ , and the side  $AC$  to  $DF$ , and the  $\angle A$  to  $\angle D$ : Therefore if they be apply'd one upon the other<sup>a</sup> they will have the same terms and agree, the basis  $BC$  to the basis  $EF$ . And consequently the whole  $\Delta^b$  shall agree, and be equal to the whole  $\Delta$  on which it's placed, that is  $\Delta EDF$  to  $\Delta BAC$ ,  $WW^D$ .

(a) hyp.

(b) 14 ax.

## Prop. V.

Theorem 2. The  $\angle^s$   $ABC$ ,  $ACB$ , at the base of an Isosceles  $\Delta ABC$ , are equal: and if the equal sides  $AB$ ,  $AC$  be produced, the  $\angle^s$   $CBD$ ,  $BCE$  under the base, shall be equal.

- (a) 3 1.  
(b) 1 Pp.  
(c) hyp.  
(d) confr.  
(e) 4 1.  
(f) 3 ax.  
(g) 4 1.  
(h) before.  
(i) 3 ax.

Prepar.<sup>a</sup> Take  $AE = AD$ ; and<sup>b</sup> joyn  $CD$  and  $BE$ .  
Pro. Because, in the  $\Delta^s$   $ACD$ ,  $ABE$ ,  $AB^c = AC$ , and  $AE^d = AD$ , and the  $\angle A$  common to both, <sup>e</sup> therefore is the  $\angle ABE = \angle ACD$ , and the  $\angle AEB^c = \angle ADC$ , and the base  $BE^c = CD$ ; also  $EC^f = DB$ . Therefore also in the  $\Delta^s$   $BEC$ ,  $BDC$  shall be the  $\angle ECB = \angle DCB$ .  $WW^D$ . By like reason is the  $\angle EBC = \angle DCB$ , but the  $\angle ABE^h = \angle ACD$ ; therefore the  $\angle ABC^i = \angle ACB$ ,  $WW^D$ .

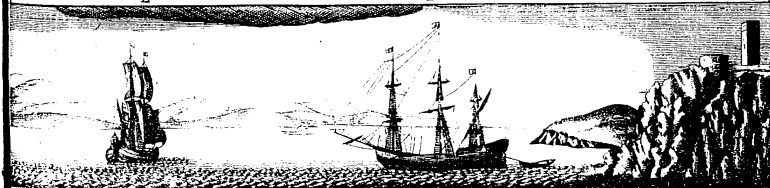
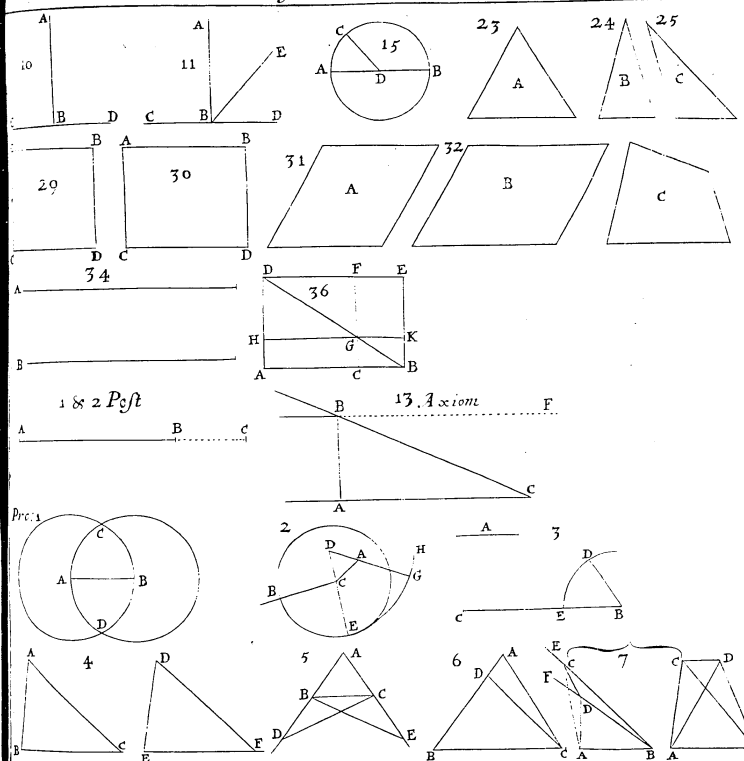
Cenol.

Thales Autor  
hujus Pro.

Every Equilateral  $\Delta$  is also Equiangular.

## Prop. VI.

First Booke of Euclide.  
Definitions





## Prop. VI.

Theorem 3.

If two  $\angle$ 's,  $\angle ABC$ ,  $\angle ACB$ , of a  $\triangle ABC$ , be equal, the sides,  $AB$ ,  $AC$ , subtending these equal  $\angle$ 's, shall also be equal one to the other.

**Prep.** **I** F the sides be not equal, let one be longer than the other, suppose <sup>(a)</sup>  $BA < CA$ , <sup>(b)</sup> make  $BD = CA$ , and <sup>(c)</sup> draw the line  $CD$ . <sup>(d)</sup> In the  $\triangle BDC$ ,  $ACB$ , because  $BD = CA$ , and the side  $BC$  is common, and the  $\angle DBC = \angle ACB$ , the  $\triangle BDC = \triangle ACB$  <sup>(e)</sup> shall be equal the one to the other, a part to the whole <sup>(f)</sup> which is impossible. <sup>(g)</sup>

Corol.

Every Equiangular  $\triangle$  is also Equilateral.

## Prop. VII

Theorem 4.

Upon the same Right-Line  $AB$ , two Right-Lines being drawn  $AC$ ,  $BC$ , two other Right-Lines  $AD$ ,  $BD$ , equal to the former, each to each (viz.  $AD = AC$ , and  $BD = BC$ ) cannot be drawn from the same points  $A$ ,  $B$ , on the same side, to several points, as  $C$  and  $D$ , but only to  $C$ .

**Pro** 1. **Cafe.** **I** F the point  $D$  be in the Line  $AC$ ; it's evident that  $AD$  is <sup>(a)</sup> not equal to  $AC$ . <sup>(b)</sup>

2. **Cafe.** If the point  $D$  be within the  $\triangle ACB$ , then draw  $CD$ , and produce  $EDF$ , and  $BCE$ . Now if it must be  $AD = AC$ , then the  $\angle ADC = \angle ACD$ ; <sup>(c)</sup> as also, because  $BD = BC$ , the  $\angle FDC = \angle BCD$ ; therefore the  $\angle FDC = \angle ACD$  also the  $\angle ECD = \angle ACD$ . <sup>(d)</sup> Which is impossible. <sup>(e)</sup>

3. **Cafe.** If  $D$  be without the  $\triangle ACB$ , join  $CD$ . Again, the  $\angle ACD = \angle ADC$ , and the  $\angle BCD = \angle BDC$ , <sup>(f)</sup> Therefore the  $\angle ACD = \angle BDC$ , *scil.* the  $\angle ADC = \angle BDC$  a part to the whole. Which is impossible. Therefore  $\&c$ .

E

Prop. VIII.



## Prop. VIII.

Theorem 5. If two  $\triangle^s$  ABC, DEF, have two sides of the one equal to two sides of the other, viz.  $AB = DE$ , and  $AC = DF$ , and the bases equal,  $BC = EF$ ; then the  $\angle^s$  contained under the equal Right-Lines shall be equal, viz.  $A$  to  $D$ .

(a) hyp. Pro. **B**ecause  $BC = EF$ , if the base  $BC$  be laid on the base  $EF$ , <sup>b</sup> they shall agree; therefore whereas  $AB = DE$ , and  $AC = DF$ , the point  $A$  <sup>a</sup> will fall on  $D$ , and to the sides of the  $\angle^s$   $A$  and  $D$  are coincident; <sup>c</sup> wherefore those  $\angle^s$  are equal.  $WW Dn$ .  
(b) 8 ax.  
(c) hyp.  
(d) 7. 1.  
(e) 5 ax.

Corol.

(F) 4. 1. 1.  $\triangle^s$  mutually equilateral are also mutually <sup>e</sup> Equiangular.  
2.  $\triangle^s$  mutually equilateral <sup>e</sup> are equal one to the other.

## Prop. IX.

Problem. 4. To divide a Right-Lined  $\angle$  given BAC into two equal parts.

(a) 3. 1. Pro. **M**ake  $AD = AE$ , drawing  $DE$ ; on which <sup>b</sup> make an equilateral  $\triangle DFE$ . So drawing the Right-Line  $AF$ ; it shall bisect the  $\angle$  as required.

(c) conftr. Pro. For  $AD = AE$ , and the side  $AF$  is common, and the base  $DF = FE$ . <sup>d</sup> Therefore the  $\angle DAF = EAF$ .  $WW Dn$ .  
(d) 8. 1.

Corol.

Hence it appears how an  $\angle$  may be cut into any equal parts in a Geometrical progression as 4, 8, 16, &c. viz. By a continual Subsection of each part again. But the method of dividing  $\angle^s$  into other parts by a Scale and Compasses, is as yet unknown.

## Prop. X.

Problem 5. To divide a Right-Line given GH into two equal parts.

(a) 1. 1. Pro. **U**pon  $GH$  <sup>a</sup> make an equilateral  $\triangle GAH$ , and bisect the  $\angle A$  with the Right-Line  $AF$ . That Line shall also bisect the given Line  $GH$ .  
(c) conftr. Pro. For  $GA = HA$ , and  $AI$  is common, and the  $\angle GAI = HAI$ , therefore <sup>d</sup>  $GI = IH$ .  $WW Dn$ .  
(d) 4. 1.

Prop. XI.

## Prop. XI.

Problem 6.

From a point I, in a given Right-Line DF, to raise a Right-Line IA at Right  $\angle^s$ .

Pro. **T**ake on either side of the point I an equal space viz.  $DI = IE$ , <sup>(a) 3. 1.</sup> and on  $DE$  <sup>b</sup> make an equilateral  $\triangle DAE$ , then draw  $AI$ , <sup>(b) 1. 1.</sup> and it will be the Perpendicular required. <sup>(c) conftr.</sup>

Pro. For  $DI = IE$ , and  $DA = AE$ , and  $AI$  is common. <sup>(d) 23 def.</sup> Therefore the  $\angle AID = AIE$ , <sup>(e) 8. 1.</sup> and consequently right: Whence  $AI$  must be a  $\perp$ .  $WW Dn$ . <sup>(f) 10 def.</sup>

## Prop. XII.

Problem 7.

Upon an infinite Right-Line given DE, from a given point A without it, to let fall a Perpendicular Right-Line AI.

Pro. **O**N the center A, <sup>a</sup> describe a Circle cutting DE, the given Right-Line in the points D and E. Then <sup>b</sup> bisect DE in I drawing  $AI$ , which will be the  $\perp$  required. <sup>(a) 3 post.</sup> <sup>(b) 10. 1.</sup>

Pro. Draw  $AD, AE$ . Then the  $\triangle AID, AIE$ , are mutually <sup>c</sup> equilateral. <sup>(c) conftr.</sup> Therefore the  $\angle DIA = EIA$ , and consequently right. <sup>(d) 8. 1.</sup> Wherefore  $AI$  is a  $\perp$ .  $WW Dn$ . <sup>(e) 10 def.</sup>

## Prop. XIII.

Theorem 6.

When a Right-Line EB standing upon a Right-Line CD makes  $\angle^s$ ; these  $\angle^s$  shall be either 2  $\perp^s$ , or together equal to 2  $\perp^s$ .

Pro. **I**F the  $\angle^s$   $EBD$  and  $EBC$  be equal, <sup>a</sup> they are 2  $\perp^s$ ; if unequal, <sup>(a) 10 def.</sup> from the point B <sup>b</sup> raise  $BA \perp$ . Because the  $\angle EBC = \perp$  <sup>(b) 11. 1.</sup>  $ABE$ , and the  $\angle EBD = \perp - ABE$ , therefore shall be  $EBC + EBD = 2 \perp^s + ABE - ABE = 2 \perp^s$ .  $WW Dn$ . <sup>(c) 15 ax.</sup> <sup>(d) 3 ax.</sup> <sup>(e) 2 ax.</sup>

Corol.

1. If one  $\angle EBD$  be right, the other  $EBC$  is also right; if one acute, the other is obtuse; and the contrary.
2. If more Right-Lines than one stand upon the same Right-Line at the same point, the  $\angle^s$  shall be equal to 2  $\perp^s$ .
3. Two Right-Lines cutting each other make  $\angle^s = 4 \perp^s$ .
4. All the  $\angle^s$  about one point = 4  $\perp^s$ . by Corol. 2.

F 2

Prop.



Theorem 7.

## Prop. XIV.

If to any Right-Line DE, and point therein C, two Right-Lines, DC, CE, be drawn from contrary sides, making the  $\angle$  ACD  $\perp$  ACE, = 2  $\angle$ s, the lines DC, CE, shall make one straight Line.

(a) 13. 1. *Pro.* IF not; let DC, CE, make one Right-Line; then shall the  $\angle$  ACD  
(b) *bif.*  $\perp$  ACE = 2  $\angle$ s = ACD  $\perp$  ACE, which is  $\angle$  absurd.  
(c) 9. ax.

Theorem 8.

## Prop. XV.

If two Right-Lines AB, CD, mutually cut one the other, the opposite  $\angle$ s are equal viz. AED = CEB, or AEC = DEB.

(a) 13. 1. *Pro.* FOR the  $\angle$  AED  $\perp$  DEB = CEB  $\perp$  DEB = 2  $\angle$ s,  $\therefore$  there-  
(b) 3. ax. fore CEB = AED.

Theorem 9.

## Prop. XVI.

One side BA of a  $\triangle$  ABC being produced, the outward  $\angle$  EAC will be greater than either of the inward opposite  $\angle$ s C or B,

(a) 10. 1. *Pro.* L Et the Right-Line BG,  $\perp$  bisect the side AC,  $\therefore$  produce FG = FB,  
(b) 1. *Post.* and draw AG.

(b) 3. 1. *Pro.* Because AF = CF, and FG = FB, and  $\angle$  AFG =  $\angle$   
(c) *constr.* CFB;  $\therefore$  also shall the  $\angle$  GAF =  $\angle$  BCF, and consequently  
(d) 4. 1. the whole external  $\angle$  EAC  $\perp$  ACB the internal opposite.

Also if the side AB be bisected in I, the same shall follow, and be proved the External  $\angle$  DAB =  $\angle$  ABC.

(e) 15. 1. Lastly, seeing the  $\angle$  EAC =  $\angle$  DAB:  $\therefore$  shall be the External  $\angle$   
(f) 9. ax. EAC  $\perp$   $\angle$  C or B either of the Internal opposite. WWD.

Theorem 10.

## Prop. XVII.

Two  $\angle$ s of any  $\triangle$  ABC, which way soever they are taken, are less than 2  $\angle$ s.

(a) 13. 1. *Pro.* Rduce B C. Because the  $\angle$  ACD  $\perp$  ACB = 2  $\angle$ s, and the  
(b) 16. 1.  $\angle$  ACD  $\perp$  A,  $\therefore$  therefore A  $\perp$  ACB = 2  $\angle$ s. After the same  
(c) 4. ax. manner is the  $\angle$  B  $\perp$  ACB = 2  $\angle$ s. The side AB being produced, the  
 $\angle$  A  $\perp$  B will be in like manner demonstrated less than 2  $\angle$ s. WWD.

Corol.

Corol.

1. In every  $\triangle$  where one  $\angle$  is either right or obtuse, the two other are acute.

2. All the  $\angle$ s of an equilateral  $\triangle$ , and the 2  $\angle$ s of an Isosceles that are upon the base, are acute.

3. If a Right-Line AE make unequal  $\angle$ s with another Right-Line D, viz. one acute AED, the other AEC obtuse, a Perpendicular AD, let fall from any point A, to the other line CD, shall fall on that side the acute  $\angle$  is.

For if AC, drawn on the side of the obtuse  $\angle$  be a  $\perp$ , then in the  $\triangle$  AEC shall  $\angle$  AEC  $\perp$  ACE = 2  $\angle$ s. \*Which is contrary to the precedent (\*) 17. 1. Prop.

## Prop. XVIII.

Theorem 11.

The greatest side AC of every  $\triangle$  ABC subtends the greatest  $\angle$  ABC.

*Pro.* FROM AC  $\perp$  take away AD = AB, and joyn BD.  $\therefore$  Therefore (a) 3. 1.  
is the  $\angle$  ADB = ABD. But ADE  $\perp$  C;  $\therefore$  therefore the (b) 5. 1.  
whole  $\angle$  ABC  $\perp$  C. After the same manner, shall be ABC  $\perp$  A. (c) 16. 1.  
WWD. (d) 9. ex.

## Prop. XIX.

Theorem 12.

In every  $\triangle$  ABC, under the greatest  $\angle$  A, is subtended the greatest side BC.

*Pro.* FOR if it be admitted AB = BC, then will the  $\angle$  A = C, which (a) 5. 1.  
is contrary to the Hypoth. If AB  $\perp$  BC, then shall be the (b) 18. 1.  
 $\angle$  C  $\perp$  A, which is also against the Hypoth. Wherefore BC  $\perp$  AB.  
After the same manner BC  $\perp$  AC. WWD.

Note, This is but the Converse of the last Proposition, and therefore might have been omitted.

## Prop. XX.

Theorem 13.

Of every  $\triangle$  ABC two sides BA, AC, any way taken, are greater than the side that remains BC.

*Pro.* Rduce the line AB,  $\perp$  and take AD = AC, and draw DC,  $\therefore$  then (a) 3. 1.  
shall the  $\angle$  D = ACD,  $\therefore$  therefore is the whole  $\angle$  BCD  $\perp$  D; (b) 5. 1.  
 $\therefore$  therefore BD ( $\perp$  BA  $\perp$  AC)  $\perp$  BC. WWD. (c) 9. ax.  
(d) 19. 1.  
(e) *constr.*

Prop. 2 ax.



Theorem 14.

Prop. XXI.

If from the extreampoints of one side  $BC$ , of a  $\triangle ABC$ , two Right-Lines  $BD$ ,  $CD$ , be drawn to any point within the  $\triangle$ , then are both those two Lines shorter than the two other sides of the  $\triangle$ ,  $BA$ ,  $CA$ ; but do contain a greater  $\angle$ , that is, the  $\angle D < \angle A$ .

- (a) 20. 1. *Pro.* **P**roduce  $BD$  to  $E$ . Then  $CE + ED < CD$ , and making  $BD$  common to both,  $BD + EC + DE < CD + BD$ . Again,  $BA + AE < BE$ ,  $^b$  therefore  $BA + AC < BE + EC$ . Wherefore  
(b) 4 *ax.*  $BA + AC < BD + DC$ . 2. the  $\angle BDC < \angle DEC < \angle A$ . Therefore the  $\angle BDC < \angle A$ . *WW D.*

Problem 8.

Prop. XXII.

To make a  $\triangle FKG$  of three Right-Lines  $FK$ ,  $FG$ ,  $GK$ , which shall be equal to three Right-Lines given  $A$ ,  $B$ ,  $C$ . Of which it's necessary that any two taken together be longer than the third.

- (a) 3. 1. *Pro.* **O**N the infinite Right-Line  $DE$ ,  $^a$  take  $DF$ ,  $FG$ ,  $GH$  equal to the given lines  $A$ ,  $B$ ,  $C$ ; Then if from the  $^b$  centers  $F$  and  $G$ , with the extents  $FD$  and  $GH$ , two  $^c$  be described, cutting each other in  $K$ , and the Right-Lines  $KF$ ,  $KG$  be drawn, the  $\triangle FKG$  shall be made,  $^c$  whole sides  $FK$ ,  $FG$ ,  $GK$  are equal to the three lines  $DF$ ,  $FG$ ,  $GH$ ,  $^d$  that is, to the three lines given  $A$ ,  $B$ ,  $C$ . *WW Dn.*

Problem 9.

Prop. XXIII.

At a point  $C$ , in a Right-Line given  $AB$ , to make a Right-Lined  $\angle GCB$ , equal to a given Right-Lined  $\angle DEF$ .

- (a) 1 *post.* *Pro.* **D**raw the Right-Line  $DF$  cutting the sides of the given  $\angle$  any ways.  
(b) 3. 1. *Pro.*  $^b$  Make  $CG = ED$ ; and on  $CG$   $^c$  make a  $\triangle CGB$ ,  
(c) 22. 1. having equal sides to the former  $EDF$ , so that  $CB = EF$ , and  $GB = DF$ ;  
(d) 8. 1. then will  $\angle C = \angle E$ . *WW Dn.*

Prop.

Prop. XXIV.

Theorem 15.

If 2  $\triangle$ 's  $ABC$ ,  $DEF$ , have two sides of the one equal to two sides of the other, viz.  $AB = DE$ , and  $AC = DF$ , and the  $\angle A = \angle E$   $^b$   $\angle D$  contained under the equal Right-Lines, they shall also have the base  $BC = EF$  the other base.

*Pra.* **M**ake the  $\angle EDG = \angle A$ , and the side  $DG = DF$ ;  $^b$   $AC$ ; (a) 23. 1. and joyn  $EG$ , and  $FG$ . (b) 3. 1.

*Pro.* 1. *Cafe.* If  $EG$  fall above  $EF$ ; Because  $AB = DE$ , and  $AC = DG$  and the  $\angle A = \angle EDG$ ,  $^b$  therefore is  $BC = EG$ . But because  $DF = DG$ ,  $^c$  therefore is the  $\angle DFG = DGF$ ;  $^d$  therefore is the  $\angle DFG = EGF$ , and consequently the whole  $\angle EFG = EGF$ ,  $^e$  wherefore  $EG = BC$ .  $^f$   $EF$ . (c) *hyp.*  
(d) *hyp.*  
(e) *conf.*  
(f) 4. 1.

2. *Cafe.* If the base  $EF$  fall in the same place with  $EG$ ,  $^g$  it's evident that  $EG = BC$ .  $^h$   $EF$ . (g) 5. 1.  
(h) 9 *ax.*  
(i) 9 *ax.*

3. *Cafe.* If  $EG$  fall below  $EF$ , then because  $DG + GE = DF + FE$ , (m) 21. 1. if from both there be taken  $DG = DF$ , the remains  $EG (BC) = EF$ . (n) 5 *ax.*  
*WW D.*

Prop. XXV.

Theorem 16.

If 2  $\triangle$ 's  $ABC$ ,  $DEF$ , have two sides of the one equal to two of the other; that is,  $AB = DE$ , and  $AC = DF$ , and the bases  $BC = FE$ , they shall also have the  $\angle$ 's contained under the equal Right-Lines one greater than the other viz.  $\angle A < \angle D$ .

*Pro.* **F**or if the  $\angle A = \angle D$ ,  $^a$  then is the base  $BC = EF$ , which is contrary to the Hypothesis. If the  $\angle A > \angle D$ , then  $^b$  will  $BC > EF$ , which is also against the Hypothesis. Therefore  $BC < EF$ .  $^c$   $WW D.$  (a) 4. 1.  
(b) 24. 1.

Prop. XXVI.

Theorem 17.

If two  $\triangle$ 's  $BAC$ ,  $EDG$ , have 2  $\angle$ 's of the one  $B$ ,  $C$ , equal to 2  $\angle$ 's of the other  $E$ ,  $D$ ,  $G$ , each to his correspondent  $\angle$ , and have also one side of the one equal to one side of the other, either that side which lieth betwixt the equal  $\angle$ 's, or that which is subtended under one of the equal  $\angle$ 's; the other sides also of the one shall be equal to the other sides of the other, each to his correspondent side, and the other  $\angle$  of the one shall be equal to the other  $\angle$  of the other.

*Pro. Hyp.* 1. **L**et  $BC = EG$ , which are the sides interjacent of the equal  $\angle$ 's. Then shall  $BA = ED$ , and  $AC = DG$ , and the  $\angle A = \angle D$ . For if  $ED < BA$ , then  $^a$  make  $EH = BA$ , and draw  $GH$ . (a) 3. 1.  
*Bécause*



- (b) *suppos.* Because  $AB^b = HE$ , and  $BC^c = EG$ , and the  $\angle B^e = E$ , therefore shall the  $\angle EGH^d = C^e = DGE$ ,<sup>1</sup> which is absurd. In like manner let  $AC = DG$ , then will the  $\angle A = EDG$ .  
 (c) *hyp.*  
 (d) 4. 1.  
 (e) *hyp.*  
 (f) 9. ax.  
 (g) *hyp.*  
 (h) *suppos.*  
 (i) 4. 1.  
 (j) *hyp.*  
 (k) 4. 1.  
 (l) *hyp.*  
 (m) 16. 1.  
 Thales. Milesius. *WW D.*

Theorem 18.

## Prop. XXVII.

If a Right-Line EF falling upon two Right-Lines AB, CD, make the alternate  $\angle AGH = DHG$ , then are the Right-Lines AB, CD parallel.

- (a) 16. 1. *Pro.* If not, produce them till they meet in I, and then shall the outward  $\angle AGH^a = GHD$  the internal opposite, to which it was by Hyp. equal. Which is repugnant.

Theorem 19.

## Prop. XXVIII.

If a Right-Line EF falling upon two Right-Lines AB, CD, make the outward  $\angle$  of the one line AGE =  $\angle$  CHG the inward, and opposite of the other on the same side, or make the inward  $\angle$  on the same side viz.  $AGH + CHG = 2 \angle$ , then are the Right-Lines AB, CD parallel.

- (a) 15. 1. *Pro. Hyp. 1.* Because by Hyp. the  $\angle AGE = CHG$ ,<sup>a</sup> therefore are  
 (b) 27. 1. the alternate  $\angle BGH = CHG$ :<sup>b</sup> and therefore AB  
 || CD.  
 (a) 13. 1. *Hyp. 2.* Because by Hyp. the  $\angle AGH + CHG = 2 \angle$ ,<sup>a</sup> =  $AGH$   
 (b) 3. ax. +  $BGH$ ,<sup>b</sup> is  $CHG = BGH$ ; and therefore AB, || CD. *WW D.*  
 (c) 27. 1.

Theorem 20.

## Prop. XXIX.

If a Right-Line EF, fall upon two parallels AB, CD, it will make the alternate  $\angle$  BGH and GHC equal one to the other, and the outward  $\angle EGB$  equal to the inward opposite  $\angle$  on the same side EHD, as also the inward  $\angle$  on the same side AGH, CHG, equal to  $2 \angle$ .

- (a) 13. 1. *Pro. Part. 1.* The  $\angle DHG + GHC = 2 \angle$ : also  $DHG + BGH$   
 (b) 28. 1. =  $2 \angle$ :<sup>b</sup> and taking from each the common  $\angle DHG$ ,  
 (c) 3. ax. there shall remain  $BGH = GHC$ .

Part. 2

Part. 2. The  $\angle EGB + BGH = 2 \angle$ :<sup>a</sup> and  $BGH + GHD = (d)$  13. 1.  $2 \angle$ :<sup>s</sup>, and taking from each the common  $\angle BGH$ , there shall remain (e) 28. 1.  $EGB = GHD$ .

Part. 3. The Right-Lines AB, CD are parallels by the Hyp.<sup>f</sup> and cannot (f) 34. def. meet, therefore the inward  $\angle$  on the same side both towards A and B are equal to  $2 \angle$ . *WW D.*

Corol.

Every  $\square$ , having one  $\angle$ , is a Right-Angled  $\square$ , and hath all the rest of the  $\angle$ s right.

## Prop. XXX.

Theorem 21.

Right-Lines (AB, CD) parallel to one and the same Right-Line EF, are also parallel the one to the other.

- Pro.* Draw GI cutting the three Right-Lines given any ways.  
*Pro.* Then because AB, || EF will the  $\angle AGI^a = EHI$ , also (a) 29. 1.  
 because CD, || EF, will the  $\angle EHI^b = DIG$ ,<sup>b</sup> Therefore the  $\angle AGI$  (b) 1. ax.  
 =  $DIG$ ,<sup>c</sup> whence will be AB || CD. *WW D.* (c) 27. 1.

## Prop. XXXI.

Problem 10.

From a point given A, to draw a Right-Line AE, parallel to a Right-Line given, BC.

- Pro.* From the point A draw a Right-Line AD to any point of the given Right-Line; with which at the point thereof A make an  $\angle DAE$  (a) 23. 1.  
 =  $ADC$ ,<sup>b</sup> then will be AE || BC. *WW D.* (b) 27. 1.

## Prop. XXXII.

Theorem 22.

Of any  $\triangle ABC$  one side BC being produced, the outward  $\angle$  ACE, shall be equal to the two inward opposite  $\angle$ s A, B, and the three inward  $\angle$ s of the  $\triangle$ , A, B, ACB shall be equal to  $2 \angle$ .

- Pro.* From C draw CD || BA. Then is the  $\angle A^b = ACD$ , and (a) 31. 1.  
 the  $\angle B^b = DCE$ . Therefore A + B =  $ACD + DCE$  (b) 29. 1.  
 = ACE. *WW D.* (c) 2. ax.  
 Also ACE + ACB =  $2 \angle$ :<sup>c</sup> therefore A + B + ACB =  $2 \angle$ .  
*WW D.* (d) 15. ax.  
 (e) 13. 1.  
 (f) 1. ax.  
 Pythagoras  
 Samius.

F

Corol.



Corol.

1. The 3  $\angle$ s of any Right-Lined  $\Delta$  together, are equal to the 3  $\angle$ s of any other Right-Lined  $\Delta$  taken. Whence,
2. If in one Right-Lined  $\Delta$ , 2  $\angle$ s (taken severally, or together) = 2  $\angle$ s of another Right-Lined  $\Delta$  (10 taken) then shall their remaining  $\angle$ s be also equal. Likewise, if 2  $\Delta$ s have one  $\angle$  of the one equal to one of the other, then is the sum of the remaining  $\angle$ s of the one  $\Delta$ , equal to the sum of the remaining  $\angle$ s of the other.
3. If one  $\angle$  of a Right-Lined  $\Delta$  be Right, the other two together are equal to a Right. Also, that  $\angle$  of a Right-Lined  $\Delta$  which is equal to the other 2  $\angle$ s is itself a  $\angle$ .
4. In an Isosceles, when the equal sides include a  $\angle$ , the other two upon the base are each of them  $\frac{1}{2}$   $\angle$ .
5. An  $\angle$  of an Equilateral  $\Delta$  is  $\frac{1}{3}$   $\angle$ . For  $\frac{1}{3}$  of 2  $\angle$ s =  $\frac{2}{3}$   $\angle$ .

Scol.

Every Right-Lined Figure may be divided into so many  $\Delta$ s, as it contains sides less two, and the  $\angle$ s of the  $\Delta$ s shall make up the  $\angle$ s of the Figure. Hence.

All the  $\angle$ s of a Right-Lined Figure together, make twice as many  $\angle$ s, bating four, as the Figure hath sides; and consequently all Right-Lined Figures, of the same species have the sums of their  $\angle$ s equal.

Theorem 21.

Prop. XXXIII.

If two equal and parallel lines  $AB$ ,  $CD$  be joyned together with two other Right-Lines  $AC$ ,  $BD$ , then are those lines also equal and parallel.

Pro. Draw the Right-Line  $DA$ . Now because  $AB$ , and  $CD$  are parallel, and the  $\angle DAB = ADC$ ; and also by Hyp.  $AB = CD$ , and the side  $AD$  common, therefore is  $AC = DB$ , and the  $\angle CAD = ADB$ . <sup>c</sup> Whence also  $AC \parallel DB$ .

- (a) 29. 1.  
(b) 4. 1.  
(c) 27. 1.

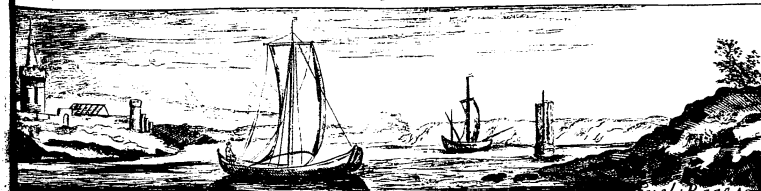
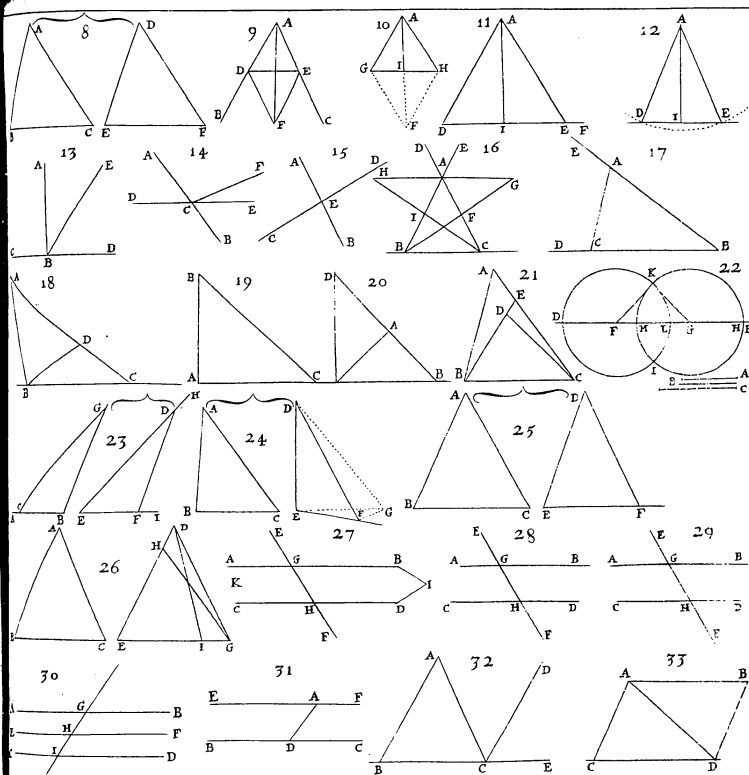
Theorem 24.

Prop. XXXIV.

In Parallelograms as  $ABCD$ , the opposite sides are equal viz.  $AB = CD$ , and  $AC = BD$ , as also the opposite  $\angle$ s,  $A = D$ , and  $B = C$ , and the Diameter  $AD$ , bisects the same.

Pro.  $AB \parallel CD$  <sup>b</sup> therefore the  $\angle BAD = CDA$ , and because also  $AC \parallel BD$  <sup>b</sup> therefore is the  $\angle CAD = ADB$  <sup>c</sup> therefore the

- (a) hyp.  
(b) 29. 1.  
(c) 2. ax.





the whole  $\angle BAC = BDC$ . After the same manner is  $B = C$ . Also because the alternate  $\angle EAD = ADC$ , and  $CAD = ADE$ , <sup>d</sup> therefore is  $AC = BD$ , and  $AB = CD$ , and also the  $\triangle ABD = \triangle ACD$ . *WW'D.* (d) 26. 1.

*Schol.*

1. It's only the Parallelogram space, or area that is bisected or divided into two equal parts by the Diagonal  $AD$ , and not the  $\angle$ 's, unless where the sides be all equal as in the  $\square$  and  $\diamond$ ; in the  $\square$  and  $\square$ , the  $\angle$ 's are cut unqually, because of the inequality of the adjacent Sides.

2. Every Four sided Figure,  $ABDC$ , having the opposite  $\angle$ 's equal, is a  $\square$ .

Hence may be also learnt another Method, how to draw a parallel  $CD$ , to a Right-Line given  $AB$ , that shall pass through a point assigned  $C$ .

Take in the Line  $AB$ , two points  $E, F$ . And with the Extent  $EC$ , setting one Foot in  $F$ , sweep the Arch  $RS$ , then with the Extent  $EF$ , setting one Foot in  $C$ , cross the said Arch in  $D$ : lastly, draw  $CD$ , and it shall be a parallel to  $AB$ , and pass through  $C$ .

Prop. XXXV.

Theorem 25.

*Parallelograms, DA, ED, standing on the same base DC, and between the same parallels AB, CD; are equal one to the other.*

*Pro 1. Case.*  $AE = CD = EB$ , and  $AC = ED$ ; also the  $\angle CAE$  <sup>(a)</sup> 34. 1.  $= DEB$ . therefore the  $\triangle CAE = \triangle DEB$ , <sup>(c)</sup> 29. 1. also put the  $\triangle ECD$  common to both, then will the  $\square AECD = CEED$ . <sup>(e)</sup> 4. 1. *WW'D.* <sup>(f)</sup> 2. ax. <sup>(g)</sup> 3. ax.

2. *Case.*  $AE = FB$  as before, <sup>(h)</sup> 34. 1. then taking from both the common segment  $FE$ , there remains  $AF = EB$ . Because  $AC = ED$ , the  $\angle$  <sup>(i)</sup> 29. 1.  $A = E$ , and consequently <sup>(k)</sup> 4. 1. the  $\triangle FAC = \triangle BED$ , to both which adding Trapezium  $EFC D$  the  $\square AECD = FBCE$ . <sup>(m)</sup> 2. ax. *WW'D.* <sup>(p)</sup> 2. ax.

3. *Case.* Again,  $AE = CD = FB$ ; therefore  $AF = EB$ . And forasmuch as  $AC = ED$ , the  $\angle E = A$ ; and consequently the  $\triangle ACF$  <sup>(q)</sup> 34. 1.  $= \triangle EDB$ . Lastly if from both there be taken the common  $\triangle EGF$ , the remaining Trapezium,  $ACGE = FGDB$ , to which if you add the common  $\triangle CGD$ , then shall the  $\square AD = DF$ . *WW'D.* <sup>(r)</sup> 29. 1. <sup>(t)</sup> 4. 1.



Schol.

Hence, the Area of any  $\square$ , is found by multiplying the Perpendicular height thereof by the base. As admit  $AB$ , be 4 Foot, and  $BC = 3$ ; then  $4 \times 3 = 12$  the Area, or number of square Feet (represented by the several squares in the Scheme) in that Parallelogram.

Theorem 26.

Prop. XXXVI.

*Parallelograms AE, HD upon equal bases CE, FD, and betwixt the same Parallels AB, CD, are equal one to the other.*

(a) 34. 1. *Pro.* **D** Draw  $CH$ , and  $EB$  which will be equal and Parallel, and consequently  $CB$  be a  $\square$ , whence the  $\square CG = CB = HD$ .  
(b) 35. 1. *WW'D.*

Theorem 27.

Prop. XXXVII.

*$\Delta^s$  ACD, FCD upon the same base CD, and between the same Parallels AB, CD, are equal one to the other.*

(a) 31. 1. *Pro.* **T** Hrough  $D$ , draw  $DE \parallel CA$ , and  $DB \parallel CF$ . Then is the  $\square AD = \square CB$ , and consequently their halves, the  $\Delta ACD = \Delta FCD$ . *WW'D.*  
(b) 35. 1.  
(c) 34. 1.  
(d) 7. ax.

Theorem 28.

Prop. XXXVIII.

*$\Delta^s$  ACE, BFD upon equal bases CE, FD, and between the same Parallels AB, CD are equal one to the other.*

(a) 31. 1. *Pro.* **D** Draw  $EG \parallel AC$ , and  $FH \parallel BD$ . Then will the  $\square CG = \square HD$ , and the  $\Delta ACE = \frac{1}{2} \square CG = \frac{1}{2} \square HD = \Delta BFD$ .  
(b) 35. 1.  
(c) 34. 1.  
(d) 7. ax. *WW'D.*

Schol.

1. If the base  $CE$ , be greater than  $FD$ , then is the  $\Delta ACE > BFD$ , and the contrary.

2. Also a Right-Line, being drawn from the vertical  $\angle$  of any Right-lined  $\Delta$  to the base, shall divide the Area according to the base, as if it bisect the base, the  $\Delta$  shall be divided in respect of Area, into two equal parts &c.

Prop.

Prop. XXXIX.

Theorem 29.

*Equal  $\Delta^s$  BCA, BCD upon the same base BC, and on the same side, are also between the same Parallels AD, BC.*

*Pro.* **I** F not, draw  $AE \parallel BC$ , and joyn  $CE$ . Then is the  $\Delta CBE = C$   $\Delta BCA = C$   $\Delta BCD$ , which is absurd. (a) 37. 1. (b) hyp. (c) 9. ax.

Prop. XL.

Theorem 30.

*Equal  $\Delta^s$  BCA, EFD upon equal bases BC, EF, and on the same side, are also betwixt the same Parallels.*

*Pro.* **I** F not, draw  $AH \parallel BF$ , and joyn  $FH$ . Then is the  $\Delta EFH = \Delta BCA = \Delta EFD$ , which is absurd. The like will follow for  $AG$ . (a) 33. 1. (b) hyp. (c) 9. ax.

Prop. XLI.

Theorem 31.

*If a  $\square$  AECD, have the same base CD with the  $\Delta$  FCD, and be between the same Parallels AF, CD: then is the  $\square$  double to the  $\Delta$ .*

*Pro.* **D** Draw  $AD$ . Then is the  $\Delta ACD = \Delta FCD$ . Therefore is the  $\square CE = 2 \Delta ACD = 2 \Delta FCD$ . *WW'D.* (a) 37. 1. (b) 34. 1. (c) 6. ax.

Corol.

Hence, is the Area of a  $\Delta$  found by multiplying the  $\perp$  in the  $\frac{1}{2}$  base, or the whole base in the  $\frac{1}{2}$   $\perp$ . As admit, the height or  $\perp$  be 6 and the  $\frac{1}{2}$  base 5; then  $6 \times 5 = 30$  the Area, or  $10 \times 3 = 30$  the Area.

Prop. XLII.

Problem 11.

*To make a  $\square$  FC, equal to a  $\Delta$  given ABC, in an  $\angle$  equal to a Right-lined  $\angle$  given D.*

*Pro.* **T** Hrough  $A$ , draw  $AG \parallel BC$ , and bisect the base  $BC$  in  $E$ , make the  $\angle BCG = D$ , and draw  $EF \parallel CG$ , which resolves the Problem. (a) 31. 1. (b) 10. 1. (c) 23. 1. (d) 38. 1. (e) 41. 1.

*Pro.* For  $AE$  being drawn, the  $\angle ECG = D$  by constr. and the  $\Delta BAC = 2 \Delta AEC = \square ECGF$ . *WW'D.*

Prop.



Theorem 32.

Prop. XLIII.

In every  $\square ABCD$ , the complements  $DG, GB$  of the  $\square H E, F I$ , which stand about the Diameter, are equal one to the other.

- Pro.** For the  $\triangle ACD = \triangle ACB$ , and the  $\triangle AGH = \triangle AGE$ , and the  $\triangle GCF = \triangle GCI$ , and  $\triangle AGE + \triangle GCI = \triangle AGH + \triangle GCF$ .  
 Therefore  $\triangle ACD - \triangle AGH + \triangle GCF = \triangle DGB = \triangle ACB - \triangle AGE + \triangle GCI = \triangle GCB$ , and consequently the  $\triangle DGB = \triangle GCB$ . *WW Dn.*

Problem 12.

Prop. XLIV.

To a Right-Line given  $F$ , to make a  $\square CM$ , at a Right-Lined  $\angle$  given  $D$ , equal to a given  $\triangle ABC$ .

- Pro.** Make a  $\square CG = \triangle ABC$ , having its  $\angle GEC = D$ . Produce  $EC$  till  $CK =$  the given Line  $F$ , through  $K$  draw  $MI \parallel CH$ , meeting  $GH$  produced in  $I$ , then from  $I$  draw by  $C$  the diameter  $IC$  meeting, (when produced,)  $GE$  in  $L$ , through  $L$  draw  $LM \parallel EK$ , which let  $HC$  produced meet at  $N$ , then shall  $CM$  be the  $\square$  required.  
**Pro.** For the  $\square CM = \square CG = \triangle ABC$ , and the  $\angle CNM = \angle HCK = \angle GEC = D$ . *WW Dn.*

Problem 13.

Prop. XLV.

Upon a Right-Line given  $FG$ , to make a  $\square FL$ , equal to a Right-Lined Figure given  $AC$ , at a Right-Lined  $\angle$  given  $E$ .

- Pro.** Reduce the given Right-Lined Figure into  $\triangle BAD, BCD$ , then make a  $\square FH = \triangle BAD$  and having an  $\angle F = E$ ,  $FI$  being produced, make on  $HI$  the  $\square IL = \triangle BCD$ . Then is the  $\square FL = FH + IL = AC$ . *WW Dn.*

SchoL.

Hence is conspicuous a method of Reducing Figures, to  $\square$  of equal bases or heights.

Problem 14.

Prop. XLVI.

Upon a Right-Line given  $AB$ , to describe a Square  $ABCD$ .

- Pro.** ON  $A$  and  $B$ , Raife 2  $\perp^s AC, BD$ , each equal to the given Line  $AB$ ; then joyn  $CD$ , and the thing required is done.

Pro.

**Pro.** For, seeing the  $\angle A + B = 2 \perp^s$ , therefore  $\triangle AC \parallel BD$ , and they are also equal, therefore the Figure  $AD$ , is a Right-Angled Equilateral  $\square$ , and consequently a Square. *WW Dn.*

After the same manner may an Oblong, or a long Square be described, with two given Lines.

Prop. XLVII.

Theorem 33.

In any Right-Angled  $\triangle BAC$ , the Square  $BD$ , which is made of the side  $BC$ , that subtends the  $\angle BAC$ , is equal to both the Squares  $BG, CH$ , which are made of the sides  $AB, AC$ , containing the  $\angle$ .

- Pro.** Joyn  $AE$ , and  $AD$ ; and draw  $AL \parallel BE$ , also draw  $BI$  and  $CF$ .  
**Pro.** Because the  $\angle DCB = \angle ICA$ , and the  $\angle ACB$  common, the  $\angle ACD = \angle ICE$ . Also because  $AC = CI$ , and  $CD = BC$ ; therefore is the  $\triangle ACD = \triangle ICE$ . But the  $\square CL = 2 \triangle ACD$ , and the  $\square CH = 2 \triangle ICE$ , (for  $HAB$  is a Right-Line,) therefore is the  $\square CL = \square CH$ . By like reason is  $2 \triangle ABE = \square BL = 2 \triangle FBC = \square BG$ , and consequently  $\square BL = \square BG$ . Therefore is the whole  $\square BD = \square CL + \square BL = \square CH + \square BG$ . *WW Dn.*

SchoL.

Hence we have a method of Adding, and Subtracting Squares, which shall be farther illustrated in the two Problems following.

Problem I.

Andr. Tacquet.

To make a Square equal to any Number of given Squares.

- Pro.** Let  $a, b, c$ , be the sides of the three  $\square$ s. Make the  $\angle ABC$ , laying  $a$  from  $B$  to  $C$ , and  $b$  from  $B$  to  $D$  and draw  $DC$ , then is  $DCq = BCq - BDq = a^2 - b^2$ . Then transfer  $DC$  from  $B$  to  $E$ , and lay  $C$  from  $B$  to  $F$ , drawing  $EF$ , then is  $FEq = BEq (DCq) - BFq (c^2) = a^2 + b^2 - c^2$ . *WW Dn.*

Problem II.

To make a  $\square$  equal to the difference of 2  $\square$ s given.

- Pro.** Let  $a, b$  be the sides of the 2  $\square$ s given. Draw the indeterminate line  $AD$ , then transfer  $a$  from  $A$  to  $B$ , and  $b$  from  $B$  to  $C$ , and with the extent  $AB$  from the Center  $B$ , describe a  $\circ$ ; and from the point  $C$ , raise the  $\perp CE$ , cutting the circumference in  $E$ ; lastly, draw  $BE$ . Then is  $BEq = BAq = a^2 = BCq (b^2) - ECq$ . Therefore  $BAq - BCq = a^2 - b^2 = ECq$ . *WW Dn.*

Problem III.



## Problem III.

Any two sides of a Right-Angled  $\triangle a, b, c$  being given to find the third.

IF the two sides containing the  $\perp$  be given, viz.  $a, b$ : then  $a^2 + b^2 = c^2$ , and  $\sqrt{a^2 + b^2} = c$ . In Numbers thus, let  $a = 9, b = 12$ , then  $a^2 = 81$ , and  $b^2 = 144$ , and  $a^2 + b^2 = 225$ . And  $\sqrt{a^2 + b^2} = 15 = c$ . But if the side  $c$ , subtending the  $\perp$  be one of the sides given, then  $c^2 - b^2 = a^2$ , and  $\sqrt{c^2 - b^2} = a$ . In Numbers thus,  $c^2 = 225, b^2 = 144$ , and  $c^2 - b^2 = 81$ , also  $\sqrt{c^2 - b^2} = 9 = a$ . *WW Dn.*

And Note, that the Numbers 3, 4, and 5 (to which we may add all their multiples and powers) are called Pythagoric Numbers, and do completely constitute Right-Angled  $\triangle$ s if put for sides.

Theorem 38.

## Prop. XLVIII.

If the Square made upon one side  $BC$ , of a  $\triangle CAB$ , be equal to the Squares made on the other side of the  $\triangle$ ,  $AB, AC$ , then the  $\angle CAB$  contained under the other two sides  $AB, AC$  is a  $\perp$ .

*Præ.* FROM the point  $A$ , draw  $AD = AC$ , so that  $AD \perp AB$ , and join  $DB$ .

*Pro.* Then because  $\angle DAB$  is  $\perp$ ,  $DB^2 = AB^2 + AD^2$ , and because  $\angle CBQ = \angle CAQ + \angle ABQ$ ,  $c$  therefore  $CB = BD$ . And to the  $\triangle$ s  $CAB$ , and  $ADB$  are mutually Equilateral, and also  $\angle$ s correspondent to the equal sides equal. But  $\angle DAB$  is  $\perp$ , therefore  $\angle CAB$  shall also be  $\perp$ . *WW D.*

The most notable and useful Propositions of this Book are the, 4, 5, 6, 13, 15, 18, 19, 20, 26, 29, 31, 32, 36, 37, 38, 41, 47.

THE



THE  
SECOND BOOK  
OF  
Euclid's Elements.

## DEFINITIONS.

1. Every Right-Angled  $\square ABCD$ , is said to be contained under two Right-Lines  $AB, BD$  comprehending a  $\perp$ .  
But for ease sake we express  $\square CA, AB$ , or  $\square CAB$  or  $\square AD$  or  $CA \times AB$ , (or by marking each side with a single letter)  $a, b$ , still understanding thereby the rectangle or oblong, contained under the Right-Lines  $CA, AB$  set at Right-Angles.

2. In every  $\square AD$ , any one of those  $\square$ s which are about the Diameter, together with its two complements, is called a Gnomon, as the  $\square GE + \square AC + \square EH$  or  $ABH$  is a Gnomon; as also  $FH + \square AC + \square CD$  or  $GLE$  is a Gnomon.

G

Very



Very easie Equations, arising by comparing of two unequal Quantities or Numbers: whereby most of the Propositions of the Second Book are invented, found out and wrought, fit to exercise the young Student withall. Let the Quantities be  $m$  (7),  $n$  (3), the sum  $z$  (10), Difference  $x$  (4)

The Reason.	Num- bers of Equa- tions.	In Species	In Numbers.	The Reason.	Num- bers of Equa- tions.	In Species.
	1	$z = m + n$	$10 = 7 + 3$	$1 \times b$	18	$zb = bm + bn$ (1 Prop.)
	2	$x = m - n$	$4 = 7 - 3$	$1 \times z$	19	$z^2 = zm + zn$ (2 Prop.)
$1 - n$	3	$m = z - n$	$7 = 10 - 3$	$1 \times m$	20	$zm = m^2 + mn$ } (3 Prop.)
$1 - m$	4	$n = z - m$	$3 = 10 - 7$	$1 \times n$	21	$zn = n^2 + mn$ }
$2 + n$	5	$m = x + n$	$7 = 4 + 3$	1. Q.	22	$z^2 = m^2 + 2mn + n^2$ (4 Prop.)
$2 - n$	6	$n = m - x$	$3 = 7 - 4$	2. Q.	23	$x^2 = m^2 - 2mn + n^2$
$2 - x$	7	$2m = z + x$	$14 = 10 + 4$	$7 \times 8$	24	$4mn = z^2 - x^2$
$1 - 2$	8	$2n = z - x$	$6 = 10 - 4$	$24 \frac{7}{8}$	25	$mn = \frac{z^2 - x^2}{4}$
$7 \frac{2}{2}$	9	$m = \frac{z + x}{2}$	$7 = \frac{10 + 4}{2}$	$25 \frac{7}{2}$	26	$mn + \frac{x^2}{4} = \frac{z^2}{4}$ (5 Prop.)
$8 \frac{2}{2}$	10	$n = \frac{z - x}{2}$	$3 = \frac{10 - 4}{2}$	$1 \times 2$	27	$zx = m^2 - n^2$
$7 - x$	11	$z = 2m - x$	$10 = 14 - 4$	$27 \frac{1}{2}$	28	$zx + n^2 = m^2$ (6 Prop.)
$7 - z$	12	$x = 2m - z$	$4 = 14 - 10$	3. Q.	29	$m^2 = z^2 - 2zn + n^2$
$8 - x$	13	$z = 2n + x$	$10 = 6 + 4$	$29 + 2zn$	30	$2zn + m^2 = z^2 + n^2$ (7 Prop.)
$13 - 2x$	14	$x = z - 2n$	$4 = 10 - 6$	$24 + x^2$	31	$4mn + x^2 = z^2$ (8 Prop.)
$2 \times x$	15	$x^2 = xm - xn$	$16 = 28 - 12$	$22 + 23$	32	$z^2 - x^2 = 2m^2 + 2n^2$ (10 Prop.)
$5 \times 4$	16	$mn = z^2 + mn - zm - zn$		$32 \frac{2}{2}$	33	$\frac{z^2 - x^2}{2} = m^2 + n^2$ (9 Prop.)
5. Q.	17	$m^2 = x^2 + 2xn + n^2$				and so infinitely.

The 16 Equation, and so to the 33 will prove true if put into Numbers as the former were.

Prop.



Prop. I.

Theorem 1

If two Right-Lines  $b$ , and  $AB$  be given, and one of them  $AB$  divided into as many parts as you please; the  $\square$  comprehended under the whole  $b$ , and divided line  $AB$ , shall be equal to all the  $\square$   $CE$ ,  $EH$ ,  $FD$  contained under the whole line  $b$ , and the several segments  $AE$ ,  $EF$ ,  $FB$ .

**Pr.** From the points  $A, B$ , raise  $AC, BD$ ,  $\perp$  to  $AB$ , making  $AC =$  (a) 11. 1.  
 $BD = b$ , and join  $CD$ , then draw through the points  $E$  and  $F$ , (b) 30. 1.  
 $EH \parallel AC$ , producing them till they meet with the Line  $CD$ . (c) 31. 1.  
**Pro.** So is  $\square CB$  a  $\square$ , under  $AC (=b)$  and  $AB$ , and is  $\square$  equal to the (d) 15 ax. 1.  
 $\square CA + EH + HB$ . *WW'D.* (e) 34. 1.

In Numbers thus,

Let  $b = 3$ , and  $AB = 10$ , which 10 divide into  $2 = AE$ ,  $3 = EF$ , and  $5 = FB$ . Then will  $10 \times 3 = 30 = 3 \times 2 + 3 \times 3 + 3 \times 5$ .

The 18 Equation,  $z b = m b + n b$ , in words thus, if two Right-Lines  $z$  and  $b$  be given, and if one  $z$  be divided into two parts (or as many as you please)  $m + n$ , the Rectangle of those two lines  $z b$  is equal to the Parallel Rectangles  $m b + n b$ , made of the line  $b$  and the Segment of  $z$ , viz.  $m$  and  $n$ .

Prop. II.

Theorem 2.

If a Right-Line  $AB$ , be divided any wise in  $C$  and  $D$ , the Rectangles  $EC$ ,  $GD$ ,  $HB$ , comprehended under the whole line  $AE$ , ( $= AB$ ) and each of the Segments  $AC$ ,  $CD$ ,  $BD$ , are equal to the Square  $AE$ , which is made of the whole line  $AB$ . That is,  $AB \times AC + AB \times CD + AB \times DB = AB \times q$ .

**Pr.** ON  $AB$  make the  $\square EB$ , and through  $C$  and  $D$  let be drawn  $CG$ , (a) 46. 1.  
and  $DH \parallel AE$ ; also let  $CG = DH = AE$ . Then shall the (b) 31. 10.  
 $\square EC = AE (= AB) \times AC$ , the  $\square GD = CG (= AB) \times CD$ , and (c) 3. 1.  
the  $\square HB = DH (= AB) \times DB$ . Therefore  $\square EC + \square GD + \square HB = AB \times q$ . *WW'D.* (d) 29 def. 1.

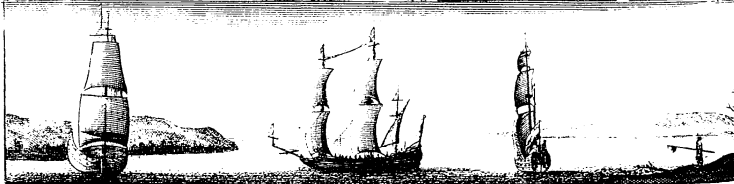
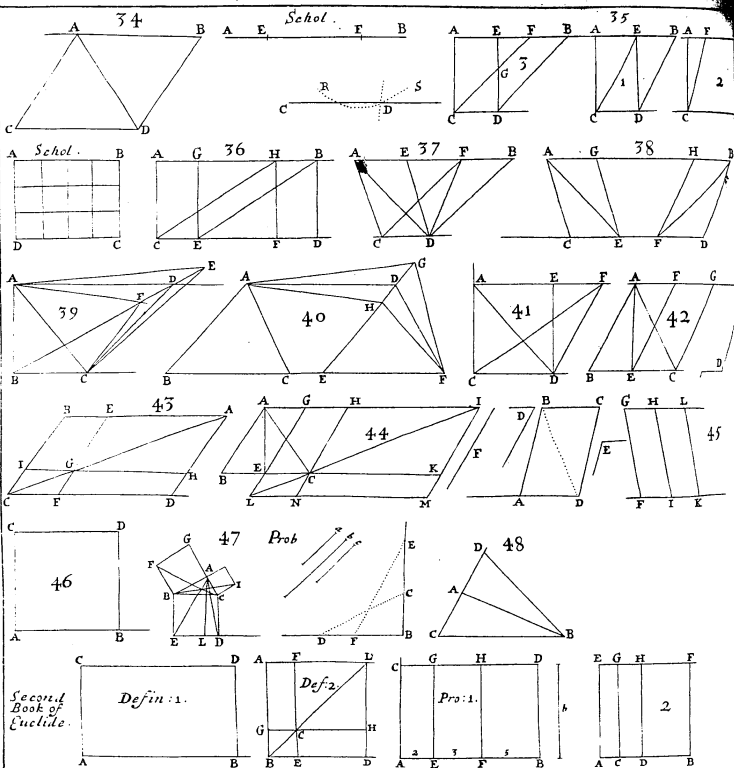
In Numbers.

Let  $AB = 10$ ,  $AC = 2$ ,  $CD = 3$ ,  $DB = 5$ . Then  $10 \times 5 + 10 \times 3 + 10 \times 2 = 10 \times 10 = 100$ .

The 19 Equation,  $z^2 = z m + z n$ , in words, the Square of any line is equal to the Rectangle of that line and its parts.

G 2

Prop.





Theorem 3.

## Prop. III.

If a Right-Line AB, be cut any wise in E, the Rectangle CB, comprehended under the whole line AB, and one segment AC = AE, is equal to the Rectangle FB, contained under BE, FE (= AE) and the square CE, which is described on the segment AE. That is,  $AB \times AE = EB \times AE + AE^2$ .

**Pro.** Let AB, be divided in E, then on the points A, E, B raise AC, EF, BD  $\perp$  AB, and make AC = EF = BD = AE, also draw CD  $\parallel$  AB. Then because AC = AE, the  $\square AD = AB \times AE$ . Again, because FE = AE, therefore the  $\square FB = BE \times AE$ . Lastly, because AC = EF = AE, the  $\square AF$  is a Square, and the  $\square AF = \square FB + \square AD$ . *WWVD.*

In Numbers.

Let AB = 10, AE = 7, and EB = 3. Then  $7 \times 7 + 7 \times 3 = 7 \times 10 = 70$ .

The 20 and 21 Equations,  $zm = m^2 + mn$  &c. in words, the Rectangle under the whole line z, and one of its parts m, is equal to the Square of one part  $m^2$  and the  $\square$  of the part mn.

Theorem 4.

## Prop. IV.

If a Right-Line AB be cut any wise in C, the Square AE, which is made of the whole line AB, shall be equal to the Squares HF, CK, which are described on the segment AC, CB, and to double the  $\square$  contained under the segment AC CB, *sci.* the  $\square$  AG, GE. That is,  $AB^2 = AC^2 + CB^2 + 2AC \times CB$ .

**Pro.** IN the  $\triangle ABD$ , because AD = AB, therefore the  $\angle ADB = \angle ABD = \frac{1}{2} \angle$ . The same may be said of the  $\triangle EBD$ . Also in the  $\triangle FDG$ , the  $\angle DFG = \angle$ , and  $FDG = FGD = \frac{1}{2} \angle$ , therefore  $DF = FG = DH = HG$ , and the  $\square FH$  is a  $\square$ . For the same reason shall the  $\square CK$  be a  $\square$ . Therefore HF, CK are the  $\square$ 's of the segment AC (= HG), CB. Again, seeing CG = GK = CB, and FG = GH = AC the  $\square AG, GE$  are contained under the segments AC, CB. And lastly, the  $\square AE = \square HF + \square CK + \square AG + \square GE$ , or  $AB^2 = AC^2 + CB^2 + 2AC \times CB$ . *WWVD.*

Corol.

The  $\square$  about the Diameter of a  $\square$  are  $\square$ 's

Li

In Numbers.

Let AB = 6, AC = 4, and CB = 2. Then  $AB^2 = 36$ ,  $AC^2 = 16$ ,  $CB^2 = 4$ , and  $AC \times CB = 8$ , and lastly,  $36 = 16 + 4 + 2 \times 8 (= 16)$ .

Or Thus.

$\square AE = 36$ ,  $\square HF = 16$ ,  $\square CK = 4$ ,  $\square AG = 8$ ,  $\square GE = 8$ . Then  $\square 36 = \square 16 + \square 4 + 8 + 8$ .

The 22 Equation,  $z^2 = m^2 + 2mn + n^2$ , in words, the Square of the whole line, is equal to both the Squares made of the segment, and twice their  $\square$ .

## Prop. V.

Theorem 5.

If a Right-Line AB, be cut into equal parts in C, and unequal in D, the Rectangle LD, under the unequal parts AD, DG (= DB) together with the Square HF, which is made of the intermediate distance of the sections CD, is equal to the Square of the half line CB. That is,  $CB^2 = AD \times DB + DC^2$ .

**Pro.** ON CB make the  $\square CI$ , and draw its diameter EB, also through  $\square D$  draw  $DF \parallel BI$ ; and taking  $BK = DB$ , draw likewise through K the line  $KL \parallel AB$ , also  $AL \parallel BK$ . **Pro.** The  $\square CG = \square GI$ , and putting the  $\square DK$  common, the  $\square CK = \square DI$ . But  $AH = CK = DI$ . If therefore CG be put common,  $\square AG = \square IG$ . Wherefore seeing the Gnomon  $IGC + \square HF = \square CI$ , the  $\square AG + \square HF = \square CI$ . *WWVD.*

In Numbers.

Let AB = 10, AC = CB = 5, AD = 7, DB = 3. Then  $7 \times 3 + 2 \times 2 = 5 \times 5$ , that is,  $21 + 4 = 25$ .

The 26 Equation,  $mn + \frac{x^2}{4} = \frac{z^2}{4}$ . That is, in words, the Rectangle of the unequal segments, together with the Square of the half difference, is equal to the Square of half the sum; now to prove that the intermediate distance CD is equal  $\frac{x}{2}$ , the 13 Equation proves  $z = 2n + x$ . The half whereof is  $\frac{z}{2} = n + \frac{x}{2}$ , now  $DB = n$ , Therefore  $CD = \frac{x}{2}$ .

Prop.



Theorem 6.

Prop. VI.

If a Right-Line AB, be divided into two equal parts in C, and another Right-Line BD, added to the same directly in one Right-Line, the Rectangle AI, comprehended under the whole AB, more the augment BD, and the augment DI (=BD,) together with the Square of the half KH (=CB) viz. KG, is equal to the Square CE made on CD = CB + BD, taken as one line. That is,  $\overline{AD} \times \overline{DB} + \overline{CB}q = \overline{CD}q$ .

- (a) 46. 1. *Pro.* ON the Right-Line CD<sup>a</sup> make the  $\square$  CE, through B, draw BG  
(b) 31. 1.  $\parallel$  DE, and taking DI = DB draw through I, IL  $\parallel$  DA, and  
also AL  $\parallel$  DI.  
(c) 36. 1. *Pro.* The  $\square$  LC =  $\square$  KB =  $\square$  HE, and putting CHBI common, the  
(d) 45. 1. Gnomon EHC = AI. But EHC +  $\square$  KG =  $\square$  CE: Therefore  $\square$  AI  
(e) 15 ax. +  $\square$  KG =  $\square$  CE. WWD.

In Numbers.

Let AB = 10, AC = CB 5, BD = 2, AB + BD = 12, CB + BD = 7.  
Then  $12 \times 2 + 5 \times 5 = 7 \times 7$ , that is,  $24 + 25 = 49$ .

Corol.

If 3 Right-Lines BD, CB + BD, AB + BD, be in arithmetical proportion, then the Rectangle under the extremes, together with the Square of the difference, is equal to the Square of the middle term. that is,  $\overline{AD} \times (\overline{AB} + \overline{BD}) \times \overline{CB} + \overline{BD} + \overline{BC}q = \overline{CD} \times \overline{CD} = \overline{CB} + \overline{BD}$ .

The 28 Equation,  $zx + n^2 = m^2$ , putting CD = m, AC = z, and BD = n, in words, it will make this proposition.

Theorem 7.

Prop. VII

If a Right-Line AB, be cut any wise in C, the Squares of the whole line, together with the Square of one of the segments CB, is equal to the double Rectangle under the whole line AB, and the said segment CB, together with the Square made of the other segment AC. That is,  $\overline{AB}q + \overline{CB}q = 2 \overline{AB} \times \overline{CB} + \overline{AC}q$ .

- (a) 46. 1. *Pro.* ON AB<sup>a</sup> make the  $\square$  AE, and taking BM = CB, draw CL  $\parallel$  BE,  
(b) 2 ax. and MK  $\parallel$  AB, and produce BE to G, so that EG = BM, and  
(c) *constr.* MG = BE and complicate the  $\square$  EF.  
(d) 15 ax. 1. *Pro.* Then,  $\square$  AE +  $\square$  EF =  $\square$  AM + MF + KL. WWD.

In

In Numbers.

Let AB = 10, AC = 7, CB = 3, and ABq = 100, CBq = 9,  
ACq = 49, AB  $\times$  CB = 30. Then  $100 + 9 = 30 \times 2 + 49$ .  
The 30 Equation  $2zn + m^2 = z^2 + n^2$ , in words, &c.

Prop. VIII.

Theorem 8.

If a Right-Line b be cut any wise into two parts, the quadruple Rectangle under the whole line b, and one of the segments z, together with the Square of the other segment y, is equal to the Square of the whole line b, and segment z, taken as one line.

- |   |   |              |
|---|---|--------------|
| 1 | That is, $4bz + y^2 = \overline{b+z}$ .               | (a) 7. 2.    |
| 2 | For $2bz + y^2 = b^2 + z^2$ .                         |              |
| 3 | $2bz = b^2 + z^2 - y^2$ .                             |              |
| 4 | $4bz = b^2 + z^2 - y^2 + 2bz$ .                       | (b) 3 ax. 1. |
| 5 | $4bz + y^2 = b^2 + z^2 + 2bz = \overline{b+z}$ . WWD. | (c) 2 ax. 1. |

In Numbers.

Let b = 10, y = 7, z = 3, then bz = 30, and 4bz = 120, b<sup>2</sup> = 100,  
y<sup>2</sup> = 49, z<sup>2</sup> = 9, 2bz = 60, lastly,  $120 + 49 = 100 + 9 + 60 = 169 =$   
 $10 + 3 \times 10 + 3$ .

The 31 Equation,  $4mn + x^2 = z^2$ , in words, &c.

Prop. IX.

Theorem 9.

If a Right-Line AB, be cut into unequal parts in D, and equal in C, then are the Squares of the unequal parts AD, DB together, double to the square of the half-line AC, and to the Square of the difference CD. that is,  $\overline{AD}q + \overline{DB}q = 2 \overline{AC}q + \overline{CD}q$ .

*Pro.* From C, raise CE  $\perp$ , and = CA = CB, and draw EA, EB, also through D, draw DF  $\parallel$  CE, and through F, GF  $\parallel$  CD, and lastly, join AF.

*Pro.* The  $\triangle ACE$  is an  $\triangle$  Isosceles, therefore the  $\angle A = \angle B = \angle C$ . (a) *constr.*  
Also in the  $\triangle BCE$ , for the same reason, the  $\angle B = \angle C = \angle E$ ; therefore (b) 5. 1.  
the whole  $\angle AEB$  is  $\angle$ . in the  $\triangle EGF$ , the  $\angle G = \angle E = \angle C$ ; therefore (c) 32. 1.  
therefore the  $\angle E = \angle F = \angle C$ , and consequently,  $GE = GF$ . Whence (d) 29. 1.  
 $GF = CD = GE$ , and by like reason shall  $DF = DB$ . Now  $AFq =$  (e) 6. 1.  
 $ADq + DFq (= DBq)$ ; again  $AFq = AEq + EFq$ . But  $AEq =$  (f) 34. 1.  
 $ACq + CEq = 2ACq$ . And  $EFq = EGq + GFq = 2GFq =$  (g) 47. 1.  
 $2CDq$ . Wherefore  $\overline{AD}q + \overline{DB}q = 2 \overline{AC}q + \overline{CD}q$ . WWD.

In



In Numbers.

Let  $AD = 7$ ,  $DB = 3$ ,  $AC = 5$ , and  $CD = AD - AC = 2$ ,  $ADq = 49$ ,  $DBq = 9$ ,  $ACq = 25$ ,  $CDq = 4$ . Then  $49 + 9 = 58 \times 2 + 4 \times 2$ , that is,  $49 + 9 = 50 + 8 = 58$ .

The 33 Equation,  $\frac{z^2 + x^2}{2} = m^2 + n^2$ , in words, &c.

Prop. X.

Theorem 10.

If a Right-Line AB, be cut into two equal parts in C, and another line BO, be added in a Right-Line with the same, then is the Square of the whole line and augment taken as one line, together with the Square of the said augment BO, double of the Square of the half CB, and augment BO, taken as one line. That is,  $AOq + BOq = 2BCq + 2COq$ .

Pro. From C, raise  $CE \perp$  and  $= AC$ , and draw  $AE, EB$ ; also through E, draw  $EF \parallel CO$ , and through O,  $OF \parallel CE$ , produce FO, till it meet EB produced in G, and draw AG.

Pro. In the  $\Delta s ACE, ECB$ ,  $AC = EC = CB$ , also in the  $\Delta s EFG$  and  $BOG$ ,  $FE = FG$ , and  $BO = OG$ , and consequently the  $\angle FEG = FGE = GBO = \frac{1}{2} \angle$ , and the  $\angle BEC = EBC = CE A = EAC = \frac{1}{2} \angle$ . Then  $AGq = AOq + OGq (= BOq)$ , and  $AGq = AEq + EGq$ . But  $AEq = 2ACq$ , and  $EGq = 2EFq = 2FGq$ . Therefore  $AOq + BOq = 2ACq + 2COq$ . WWD.

In Numbers.

Let  $AB = 10$ ,  $AC = CB = 5$ ,  $BO = 3$ ,  $AO = BA + BO = 13$ ,  $CO = 8$ ,  $ABq = 100$ ,  $BOq = 9$ ,  $AB \times BO = 30$ , Then  $169 + 9 = 8 \times 8 \times 2 + 5 \times 5 \times 2 = 178$ .

The 32 Equation,  $z^2 + x^2 = 2m^2 + 2n^2$ , in words, &c.

Problem 1.

Prop. XI.

To cut a Right-Line given AB in G, so that the Rectangle under the whole line AB, and one of the segment BG, shall be equal to the Square of the other segment AG.

Pro. Upon AB describe the  $\square AC$ . Bisection the sides AD in E, and draw EB, the line EA being produced, make  $EF = EB$ , on AF make the  $\square AH$ , extending the side GH to I, then is the  $\square AH = AB \times BG$ .

Pro.

Pro. For  $\square FI = EAq = EFq = EBq = BAq = EAq$ . (c) 6. 3. therefore  $\square FI = BAq = \square AC$ . Then take away the common  $\square AI$ , and there remains  $AH = GC$ , that is,  $AGq = AB \times BG = \square GC$ . (d) 47. 1. WW D.

Scheil.

This Prop. \* cannot be performed by Numbers.

Prop. XII.

Theorem 11.

In obtuse angled  $\Delta s ABC$ , the Square of the side AC, subtending the obtuse  $\angle B$ , is greater than the Squares of the sides BC, BA containing the obtuse  $\angle$ , by a double Rectangle under the side BC, and segment of the continued Base BD, taken without the  $\Delta$  from the point on which the Perpendicular AD falls, to the obtuse  $\angle B$ . That is,  $CAq = CBq + ABq + 2CB \times BD$ .

1-1-DAq | 1 Pro.  $CAq = CBq + ABq + 2CB \times BD$ . (a) 4. 2.  
2 | 2  $CBq + DAq = DBq + BCq + 2DB \times BC + ADq$ . (b) 47. 1.  
3 | 3 But  $ACq = CDq + DAq$ .  
4 | 4  $ACq = DBq + BCq + 2DB \times BC + ADq$ .  
5 | 5 And  $ABq = BDq + DAq$ .  
6 | 6 Therefore  $ACq = CBq + ABq + 2CB \times BD$ . (c) 5. 26.  
7 | 7 And consequently  $ACq = CBq + ABq + 2CB \times BD$ . WW D.

Or thus Lettering the Scheme as in the Margin.

1 |  $b^2 = c^2 + d^2 + 2cy$ , or  $b^2 = c^2 + d^2 + 2cy$ . (a) 47. 1.  
2 |  $b^2 = c^2 + z^2$ . (b) 4. 2.  
3 | But  $s^2 = y^2 + 2yc + c^2$ .  
4 |  $b^2 = y^2 + 2yc + c^2 + z^2$ .  
5 |  $d^2 = y^2 + z^2$ .  
6 |  $b^2 - d^2 = 2yc + c^2$ .  
7 |  $b^2 = d^2 + c^2 + 2yc$ . WW D.

In Numbers.

Let  $b = 10$ ,  $d = 7$ ,  $c = 5$ ,  $y = 2.6$ ; then is,  $b^2 = 100$ ,  $d^2 = 49$ ,  $c^2 = 25$ ,  $y = 6.76$ ,  $2cy = 26$ , and  $d^2 + c^2 = 49 + 25 = 74$ . And lastly,  $100 = 74 + 49 + 26$ .

H

Scheil.



Schol.

Hence, the sides of any obtuse angled  $\triangle$  being known, the segment  $y$  intercepted between the  $\perp$   $z$  and the obtuse  $\angle$ , as also the  $\perp$  it self  $z$  may

(e) 47. 1. easily be found, thus  $\frac{b^2 - c^2 + d^2}{2c} = y$ , then  $c \sqrt{d^2 - y^2} = z$ . Thus ex-

plained with the former Numbers,  $100 - 25 + 49 = 26$ , then  $\frac{26}{5} = 2.6 = y$ .  
Also  $49 - 6.76 = 42.24$ , and  $\sqrt{42.24} = z$ .

Theorem 12.

Prop. XIII.

In an acute angled  $\triangle ABC$ , the Square of the side  $AB$  subtending the acute  $\angle C$ , is less than the Squares of the sides  $AC$ ,  $CB$  comprehending the acute  $\angle$ , by a double Rectangle under one of the sides containing (viz.  $BC$  on which the  $\perp$  falls) and the line  $DC$ , taken within the  $\triangle$  from the  $\perp$  to the acute  $\angle C$ . That is,  $BAq = ACq + CBq$  by  $2BC \times CD$ , or  $BAq + 2BC \times CD = ACq + CBq$ .

(a) 7. 2. 1  $\vdash ADq$  | 1  $\vdash Pro$   $BCq + DCq + DAq = BDq + ADq + 2BC \times CD$ .  
(b) 47. 1. 2  $\vdash ADq$  | 2  $\vdash BCq + DCq + DAq = BDq + ADq + 2BC \times CD$ .  
(c) 47. 1. 3  $\vdash ADq$  | 3  $\vdash DCq + DAq = ACq$ .  
4  $\vdash BDq + ADq = BAq$ .  
2, 3. 5  $\vdash BCq + ACq = BDq + ADq + 2BC \times CD$ .  
5, 4. 6  $\vdash BCq + ACq = BAq + 2BC \times CD$ .  $WW D$ .

Or thus, marking the Scheme as in the Margin.

(a) 7. 2. 1  $\vdash p^2$  | 1  $\vdash d^2 + y^2 = z^2 + 2dy$ .  
(b) 47. 1. 2  $\vdash p^2$  | 2  $\vdash d^2 + y^2 + p^2 = z^2 + p^2 + 2dy$ .  
3  $\vdash y^2 + p^2 = c^2$ .  
4  $\vdash z^2 + p^2 = b^2$ .  
2, 3. 5  $\vdash d^2 + c^2 = z^2 + p^2 + 2dy$ .  
5, 4. 6  $\vdash d^2 + c^2 = b^2 + 2dy$ .  $WW D$ .

In Numbers,

Let  $b = 13$ ,  $c = 15$ ,  $d = 14$ , and  $y = 9$ , and  $b^2 = 169$ ,  $c^2 = 225$ ,  $d^2 = 196$ ,  
 $2dy = 252$ , then  $196 + 225 = 169 + 252 = 421$ .

Corol.

Corol.

Hence, the sides of an acute angled  $\triangle$  being known, the segment intercepted between the acute  $\angle$  and  $\perp$  and as also the  $\perp$  may easily be found; thus,  $\frac{c^2 + d^2 - b^2}{2d} = y$ , then  $c \sqrt{c^2 - y^2} = p$ .

Prop. XIV.

Problem 2.

To make a Square  $ML$ , equal to a Right-Lined Figure given  $A$ .

*Pro.* Make the  $\square EC = A$ , and producing  $DC$ , make  $CF = CB$ , (a) 45. 1.  
Bisect  $DF$  in  $G$ , and with the extent  $GF = GD$  from  $G$  de- (b) 10. 1.  
scribe the Circle  $FHD$ , producing  $CB$  till it touch the Circumference in (c) 46. 1.  
 $H$ . Then shall  $CHq = \square ML = A$ . (d) *constr.*  
*Pro.* For let  $GH$  be drawn. Then is  $A^d = EC^d = DC \times CF^e = GFq$  (e) 5. 2. 3  
 $- GCq^f = HCq^d = ML$ .  $WW D$  (f) 47. 1. 6

The most useful Prop. of this Book are the 4, 5, 6, 12, 13 and 14.

H 2

THE





THE  
THIRD BOOK  
OF  
Euclid's Elements.

DEFINITIONS.

1. Equal  $\circ$ 's  $AB, BC$  are such whose diameters are equal: or from whole centers  $D$  and  $E$ , Right-lines drawn  $DF, EG$  are equal.

2. A Right-line  $AC$  is said to touch a  $\circ$ , when touching the same, suppose in  $E$ , and being produced, it cutteth it not.

3. Circles are said, to touch one the other, which touch, but cut not one the other.

4. In a  $\circ$  Right-lines  $CK, AB$  are said to be equally distant from the center, when Perpendiculars  $DE, DF$  drawn from the center  $D$ , to them are equal; and that line  $GH$  is said to be farther distant from it; on whom the greater Perpendicular  $DI$  falls.

5. A segment of a Circle  $ACB$  is a Figure contained under a Right-line  $AB$ , and a portion of the Circumference of a Circle  $ACB$ .

6. An

6. An  $\angle$  of a segment  $CAB$ , is that  $\angle$  which is contained under a Right-line  $AB$ , and an Arch of a Circle  $CA$ .

7. An  $\angle ABC$ , is said to be in a segment  $ABC$ , when in the Circumference thereof some point  $B$  is taken, and from it Right-lines  $AB, CB$ , drawn to the ends of the Right-line  $AC$ , which is the base of the segment, then the  $\angle ABC$ , contained under the adjoynd lines  $AB, CB$ , is said to be an  $\angle$  in a segment.

8. But when the Right-lines  $AE, AD$ , comprehending the  $\angle DAB$ , do receive any periphery of the Circle  $BCD$ , then the  $\angle DAB$  is said to stand upon that periphery.

9. A sector of a Circle is when an  $\angle BAC$ , is set at the center  $A$  of that Circle; viz. that Figure  $BAC$ , comprehended under the Right-lines  $BA, AC$  containing the  $\angle$ , and the part of the Circumference received by them  $BC$ .

10. Like segments of a Circle are  $ABC, DEF$ , which conclude equal  $\angle$ 's  $BAC, EDF$ , or, in whom the  $\angle$ 's  $CBA, FED$  are equal.

Prop. I.

Problem 1.

To find the center  $F$ , of a circle given,  $ABC$ .

*Præ.* Draw  $AC$ , which bisect in  $E$ , and on  $E$  raise  $BD \perp AC$ , (a) 10. 1.  
and bisect it in  $F$ ; the point  $F$ , shall be the center. (b) 11. 1.

*Pro.* If not, let  $G$  a point without  $BD$ , be the center (for it cannot be in the line  $BD$ , seeing that cannot be divided equally in any point but  $F$ ;) let the lines  $GA, GC, GE$  be drawn.

Now  $\angle GA = GC$ , and  $AE = EC$  by constr. and  $GE$  is common; (c) 15 def. 1.  
therefore the  $\angle GEA = GEC = \angle$ , (d) 8. 1.  
therefore the  $\angle GEC = FEC$ . (e) 10 def. 1.  
(f) 10 ax.  
(g) 9 ax.  
Which is absurd.

Corol.

If a Right-line bisect at Right-angles, another Right-line in a Circle; the center shall be in the bisecting line.

Prop. II.

Theorem 1.

If in the circumference of a Circle  $ABC$ , any two points  $A$  and  $C$  be taken, the Right-line  $AC$ , which joyns those two points shall fall within the Circle.

*Pro.* If not, let it fall without and  $ADC$ , be a Right-line. (a) 1. 2.  
Having found the center  $E$ , draw  $EA, EC, ED$ ; and let  $ED$  cut the periphery in  $B$ .

Now



- (b) 15 def. 1. Now because in the Right-lined  $\triangle EADC$ ,  $EA = EC$ , the  $\angle EADC = \angle ECD$ . But the outward  $\angle ADE = \angle DCE = \angle EAD$ . Therefore  $EB = AE = ED$ , the part than the whole, which is absurd.  
 (c) 5. 1.  
 (d) 16. 1.  
 (e) 19. 1. Therefore the Right-line from  $A$  to  $C$ , cannot fall without but within the Circle.  $WW'D$ .

Corol.

If a Right-line touch a Circle, so that it cut it not, it touches but in one point.

Theorem 2.

Prop. III.

If in a Circle  $CBD$ , a Right-line  $CE$ , drawn through the center  $A$ , bisect any other line  $BD$  not drawn through the center, it shall also cut it at Right  $\angle$ : and if it cut it at Right-angles it shall also bisect the same.

- (a) hyp.  
 (b) 15 def. 1. **Pro.** From the Center  $A$  let  $BA$ ,  $DA$  be drawn.  
 (c) 8. 1. **Pro. 1.** Because  $BF = FD$ , and  $BA = AD$ , and  $EA$  is common: the  $\angle AFB = \angle AFD = \angle L$ .  $WW'D$ .  
 (d) 10 def. 1. **Pro. 2.** Because  $AFD = AFB$ , and the  $\angle ABF = \angle ADF$ , and  
 (e) hyp.  $AF$  common; therefore is  $BF = FD = \frac{1}{2} BD$ .  $WW'D$ .  
 (f) 5. 1.  
 (g) 26. 1.

Corol.

In any Equilateral or Isosceles  $\triangle$ , if a line drawn from the vertex bisect the base, that line is Perpendicular to it. And on the contrary, a Perpendicular drawn from the vertex bisects the base.

Theorem 3.

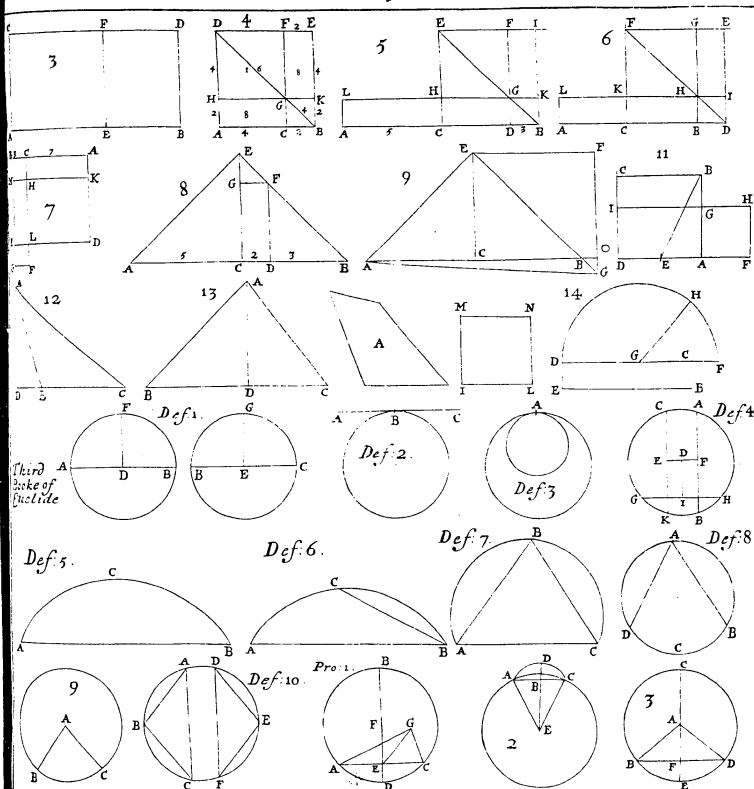
Prop. IV.

If in a Circle  $ADB$ , two Right-lines  $AB$ ,  $CD$  cut through one the other, yet neither of them pass through the Center  $F$ , then neither of those lines are divided into equal parts.

**Pro.** For if one line only pass through the Center, its manifest that it cannot be bisected by the other.

If neither of them pass through the Center, then from the Center  $F$  draw  $FE$ , now if  $AB$ ,  $CD$ , were both bisected in  $E$ , the  $\angle FEB = \angle FEC = \angle L$ . Which is absurd.

Prop.





## Prop. V.

Theorem 4.

If two  $O$ 's, DCB, ECB cut one the other, they shall not have the same Center A.

Pro. **I**f they have then  $AB^2 = AD^2 = AE^2$ . <sup>(a) 15 def. 1.</sup> Which is absurd. <sup>(b) 9 ax.</sup>

## Prop. VI.

Theorem 5.

If 2  $O$ 's, AB, CB inwardly touch one the other in B, they have not one and the same Center D.

**I**f they have, then  $DA^2 = DB^2 = CD^2$ . <sup>(a) 15. def. 1.</sup> Which is absurd. <sup>(b) 9 ax.</sup>

## Prop. VII.

Theorem 6.

If in AB, the Diameter of a  $O$ , some point G be taken, which is not the Center of the  $O$ , and from that point certain Right-lines GC, GD, GE fall on the  $O$ , the greatest line shall be that GA in which is the Center F; the least the remainder of the same line GB. And of all the other lines, the line GC nearest to that which was drawn through the center, is always greater than any line DG more remote; and only two lines are equal GE, GH, which fall upon the  $O$  from the same point, on each side of the least GB, or of the greatest GA.

Pro. **F**rom the Center F draw FC, FD, FE; and <sup>a</sup> make the  $\angle$  <sup>(a) 23. 1.</sup>  $\angle BFH = BFE$ .

Pro. 1.  $GF \perp FC (= GA)^b \perp GC$ .  $WWD$ .

2.  $FC = FD$  and  $FG$  is common, also the  $\angle GFC^a \perp GFD$ ; <sup>(b) 27. 1.</sup> <sup>(c) 15 def. 1.</sup> <sup>(d) 9 ax.</sup> therefore  $GC \perp GD$ . <sup>(e) 24. 1.</sup>

3.  $FB = FE^c \rightarrow GE \perp GF$  and  $FG$  common. Therefore  $FB = FE$ . <sup>(f) 20. 1.</sup> <sup>(g) 5 ax.</sup>

4.  $FE = FH$ , and  $FG$  is common, also the  $\angle BFH^b = BFE$ ; therefore is  $GE = GH$ . But that its impossible for any other line GD from the point G, to equal GE or GH hath been already proved.  $WW'D$ . <sup>(h) 11. 1.</sup> <sup>(i) 11. 1.</sup> <sup>(k) 4. 1.</sup>

Prop.



Theorem 7.

Prop. VIII.

If some point A be taken without a  $\bigcirc$ , and from that point be drawn certain Right-lines AF, AG, AH to the  $\bigcirc$ , and of those one AH be drawn through the center L, and the other any wise; of all these lines that fall on the concave of the circumference, that is the greatest AH which is drawn through the center; and of the others, that which is nearest to the line passing through the center, is greater than that which is remoter. But of all these lines that fall on the convex part of the  $\bigcirc$ , the least is that AB which is drawn from the point A to the Diameter BH; and of the others, that which is nearest to the least, is less than that which is farther distant, and from that point there can be only two equal Right-lines AI, AE drawn, which shall fall on the circumference on each side of the least line AB, or of the greatest AH.

Pro. From the center L, draw the Right-lines LG, LF, LE, LC, LI and make the  $\angle ALE = \angle ALI$ .

Pro. 1.  $AH = AL + LG = AG$ .

2.  $LG = LF$ , and AL is common, also the  $\angle ALG = \angle ALF$ ; therefore  $AG = AF$ .

3.  $LA = LC + CA$ , and  $LB = LC$ , if I take this latter from the there remains  $AB = AC$ .

4.  $AC + CL = AE + LE$ , and  $CL = EL$ , therefore  $AC =$  former AE.

5.  $LI = LE$ , and AL is common, also the  $\angle ALE = \angle ALI$ ; therefore  $AIL = AEL$ . But that no other line could be drawn equal to these, was proved before. Therefore *c.c.* *WW'D.*

Theorem 8.

Prop. IX.

If in a Circle BCD a point be taken, and from that point more than two equal Right-lines AB, AC, AD, drawn to the circumference, then is that point A, the center of the  $\bigcirc$ .

Pro. For if from no point without the centre can more than two equal Right-lines be drawn to the circumference. Therefore A is the centre. *WW'D.*

Prop.

Prop. X.

Theorem 9.

A Circle, AEF cannot cut another Circle FDC in more than two points.

Pro. If it can let it in AEC, From the center G draw GA, GC, GE, (a) 1. 3. now because  $GA = GC = GE$  touch the circumference of both (b) 9. 3. Circles, the point G shall be the center of both  $\bigcirc$ 's. Which is absurd. (c) 5. 3.

Prop. XI.

Theorem 10.

If 2  $\bigcirc$ 's, ABC, AED, touch one the other inwardly, in A, and their centers be taken G, F; a Right-line FA joining their centres and produced, shall cut the Circumference in A, the point of contact of the Circles.

Pro. If not, let the Right-line FG produced cut the Circles in some other point viz. D. And from the center G, of the  $\bigcirc$  ABC let GA be drawn to the point of contact, as also FD. Now seeing  $FD = FA$ , and  $GD + GF = FD$ , its also  $GD + GF = FA$ , and taking (a) 20. 1. away the common part FG, the remainder  $GA = GD$ , But  $GA = GB$ , therefore  $GB = GD$ , viz. the part than the whole. Which is absurd. (b) 15. def. 1. (c) 7. 3. (d) 9. ax. 1.

Prop. XII.

Theorem 11.

If 2  $\bigcirc$ 's, ABC, EBD touch one the other outwardly in B, the Right-line which joins their centers shall pass through the point of contact.

Pro. If not; let FG conjoin their centres, and let FB, GB be drawn. Then  $BF + BG = FG$ . But  $BF = FC$ , and  $BG = GD$ , therefore (a) 20. 1.  $FC + GD = FC + CD + GD$ , a part than the whole. Which is absurd. (b) 15. def. 1.

Prop. XIII.

Theorem 12.

One  $\bigcirc$  cannot touch another  $\bigcirc$ , in more points than one, whether it be inwardly or outwardly.

If it can, let them touch in both the points A and C. But then their centers must be in the line conjoining the points of contact, yet (a) 11 & 12. 3. not both the same or in the same point. Therefore there shall be two centers in that line, as G and H, which is impossible, seeing the line can be bisected but in one point only. (b) 6. 3.

I

Prop.



Theorem 13.

Prop. XIV.

In a  $O$ ,  $ABC$ , equal Right-lines  $AB$ ,  $DC$  are equally distant from the center  $E$ : and Right-lines which are equally distant from the center, are equal among themselves.

**Pro.** From the center  $E$ , draw  $EF \perp AB$ , and  $EG \perp CD$ , which will bisect the lines  $AB$ ,  $CD$ , also join  $EA$ ,  $ED$ .  
 (a) 3. 3.  $Pro. 1.$   $AB = DC$ , therefore  $AF = DG$ . But also  $EA = ED$ ,  
 (b) 7. 4. therefore  $FE = EG$ . And consequently  $AB$ ,  $CD$  are equally distant from the center.  
 (c) 47. 1.  $Pro. 2.$   $EF = EG$ . Therefore  $AF = DG$  and consequently  $AB = DC$ .  
 (d) 4. def. 3.  $EG = DG$ . Therefore  $AF = GD$  and consequently  $AB = DC$ .  
 (e) 6. ax.  $WW D.$

Theorem 14.

Prop. XV.

In a  $O$ ,  $ABCD$ , the greatest line is  $AF$  the Diameter; and of all other lines, that line  $BE$  which is nearest to the center  $G$ , is greater than any remoter line  $CD$ .

(a) 20. 1.  $Pro. 1.$  Draw  $GB$ ,  $GE$ , then in the  $\triangle GBE$ ,  $GB + GE > BE$ ,  
 But  $GB + GE = AF$ , therefore  $AF > BE$ .  $WW D.$   
 (b) 24. 1.  $Pro. 2.$  Draw  $GC$ ,  $GD$ , then  $GC + GD = GB + GE$ . But the  $\angle$   
 $BGE < \angle CGD$ , therefore the side  $BE < CD$ .  $WW D.$

Theorem 15.

Prop. XVI.

A line  $EF$  drawn from the extrem point of the Diameter  $AC$ , at  $L$  to the said Diameter, shall fall without the  $O$ ,  $ABC$ ; and between the same Right-line  $EF$  and the circumference, cannot be drawn another line  $AB$ . And the  $\angle$  of the semicircle  $DAGB$ , shall be greater than any Right-lined angle  $\angle$ ; and the remaining  $\angle$  without the circumference,  $EAGB$  is less than any Right-lined  $\angle$ .

**Pro. 1.** From the center  $D$  to any point  $F$ , in the Right-line  $FE$  draw the Right-line  $DHF$ . Then in the Right-angled  $\triangle DHE$ ,  
 (a) 19. 1.  $DF > (DA =) DH$ , and seeing  $H$  is in the circumference,  $F$  will be without.  $WW D.$

Pro.

**Pro. 2.** Draw  $DK \perp AB$ , then in the Right-angled  $\triangle DKA$ ,  $DA < b DK$ , but the point  $A$  is in the circumference, therefore  $K$ , and (b) 19. 1. consequently the whole line  $AB$ , shall be within the Circle.  $WW D.$

**Pro. 3.** To constitute an  $\angle$  greater than the  $\angle DAGB$ , there must be a Right-line drawn between the Right-line  $EA$ , and the periphery  $AB$ , which hath been proved already impossible; and therefore  $c$ .

**Pro. 4.** So also to constitute a Right-lined  $\angle$  less than the  $\angle$  of contact  $EAGB$ , there must be drawn a Right-line between  $AE$  and the periphery  $AB$ , which hath been proved also impossible.

Corol.

A Right-line drawn from the extremity of the Diameter of a  $O$ , and at  $L$ , is a tangent to the said  $O$ .

Prop. XVII.

Problem 2.

From a point given  $A$ , to draw a Right-line  $AC$ , which shall touch a  $O$  given  $BCD$ .

**Pro.** With the extent  $AD$ , from the center  $D$ , describe the Circle  $AE$ , and draw  $DA$ , also on  $B$  raise  $BE \perp AD$ . Then draw  $DE$ , and  $AC$  which will be a tangent to the  $O$   $BCD$ .

**Pro.** For  $DB = DC$ , and  $DE = DA$ , and the  $\angle D$  is common; (a) 15. def. 1. therefore the  $\angle ACD = \angle EDB = L$ . Therefore  $AC$  touches the  $O$  (b) 4. 1. in  $C$ .  $WW D.$  (c) 16. 3.

Prop. XVIII.

Theorem 16.

If any Right-line  $AB$  touch a  $O$   $DCE$ , and from the centre  $D$ , to the point of contact  $C$ , a Right-line  $DC$  be drawn: that line  $DC$  shall be a Perpendicular to the tangent  $AB$ .

If you deny it, let some other line  $DB$  be drawn from the centre  $D$ , Perpendicular to  $AB$ , then seeing the  $\angle B$  is a  $L$ , shall be the  $\angle C$  (a) 17. 1.  $\angle L$ ; therefore the side  $DC = DB$ . Which is absurd. (b) 19. 1. (c) 9. ax.

Prop. XIX.

Theorem 17.

If a Right-line  $AB$  touch a  $O$ ,  $GCE$ , and from the point of contact  $C$ , a Right-line  $EC$  be drawn at Right-angles to the tangent  $AB$ , the center of the  $O$  shall be in the said line  $EC$ .

**Pro.** If it be denied, let the center be somewhere else as in  $F$ ; and from  $F$  to the point of contact, let  $FC$  be drawn. Then shall  $FC \perp AB$ ; (a) 18. 3. and consequently  $FCB = L = DCB$ . Which is absurd. (b) 9. ax.

I 2

Prop.



Theorem 18.

Prop. XX.

In a  $\circ$ , DFGA, the  $\angle$  BEC at the center is double of the  $\angle$  BAC at the circumference, when the same arch BC is the base of the  $\angle$ s.

**Pro.** **T**his *Pro.* admits of a triple variety. 1. Draw the Diameter AEF, and let the Right-lines BA, AC include BE, EC; then  $\angle EAB = \angle EAC$ ; therefore the  $\angle$  BEA =  $\angle$  EAC; but the  $\angle$  BEF =  $\angle$  EAB +  $\angle$  EAC =  $2\angle$  BAC, likewise the  $\angle$  CEF =  $2\angle$  CAF; therefore the whole  $\angle$  BEC =  $2\angle$  BAC. *WW'D.*  
2. But admit DG, DB which do not include the Right-lines EG, EB; then seeing  $ED = EB$ , the  $\angle$  EDB =  $\angle$  EBD, and  $\angle$  GEB =  $\angle$  EDB +  $\angle$  EBD =  $2\angle$  GDB. *WW'D.*  
3. Lastly, admitting the  $\angle$  to intersect as BEC, BDC; now the  $\angle$  GEC =  $2\angle$  GDC. But the  $\angle$  GEB =  $2\angle$  GDB, therefore the remaining  $\angle$  BEC =  $2\angle$  BDC. *WW'D.*

Theorem 19.

Prop. XXI.

In a  $\circ$ , ADCB, the  $\angle$ s BAC, BDC which are on the same segment, are equal one to the other.

(a) 20. 3. **Pro.** **F**or the  $\angle$  BEC =  $2\angle$  BAC =  $2\angle$  BDC, therefore the  $\angle$  BAC =  $\angle$  BDC. *WW'D.*  
(b) 1. *ax.*

Theorem 20.

Prop. XXII.

The opposite  $\angle$ s DCB, DAB of a quadrilateral figure ABCD, described in a  $\circ$ , are equal to  $2\angle$ s.

(a) 21. 3. **Pro.** **D**raw the Diagonals AC, DB: then the  $\angle$  ADB =  $\angle$  ACB, also the  $\angle$  BAC =  $\angle$  BDC, therefore the whole  $\angle$  ADC =  $\angle$  BAC +  $\angle$  BDC; but the  $\angle$ s BEA +  $\angle$  BAC +  $\angle$  BDC =  $2\angle$  BEC; therefore the  $\angle$  ADC =  $2\angle$  BEC. *WW'D.*  
(b) 32. 1.

Corol.

A Circle cannot be described about a Rhombus, because the opposite  $\angle$ s are greater than  $2\angle$ s.

Prop.

Prop. XXIII.

Theorem 21.

Two like and unequal segments of a  $\circ$ , DIF, DEF cannot be set on the same Right-line DF, and the same side thereof.

**I**f they be like segments draw the lines ED, EF, and ID; then the  $\angle$  DIF =  $\angle$  DEF. (a) 10. def. 3. (b) 16. 1. Which is absurd.

Prop. XXIV.

Theorem 22.

Like segments of  $\circ$ s upon equal Right-Lines AB, DF are equal one to the other.

**Pro.** **L**et AB be placed on DF, then they shall agree; if not the one must either wholly fall without or within the other, which is absurd, or part without and part within; and so one  $\circ$  cut another in more than two points, which is also absurd. Therefore the segment ACB = DEF. *WW'D.* (a) 8. ax. (b) 23. 3. (c) 10. 3. (d) 8. ax. 1.

Prop. XXV.

Problem 3.

A segment of a  $\circ$ , ABD being given, to describe the whole  $\circ$ , whereof that is the segment.

**Pro.** **F**rom any three points in the Arch, draw two Right-lines in the segment, as AB, BD which bisect with the  $\perp$  CE, CF, which  $\perp$  CE, CF shall cut one the other in C the center.

*Pro.* For the centre is in both CE and CF, therefore it must be in the common point C. *WW'D.* (a) 1. 3.

Schol.

Hence three points being given, its easie to find the center of a Circle that shall pass through them.

Prop. XXVI.

Theorem 23.

In equal  $\circ$ s ABC, DEF, equal  $\angle$ s G and H, B and E stand upon equal parts of the circumference AC, DF; whether those  $\angle$ s be made at the centers G and H, or at the circumferences B, E.

**Pro.** **B**ecause the  $\circ$ s are equal, GA = DH, and GC = HF; and the  $\angle$  G =  $\angle$  H; therefore AC = DF. Also the  $\angle$  B =  $\frac{1}{2}\angle$  G, and  $\frac{1}{2}\angle$  H =  $\frac{1}{2}\angle$  E; therefore the segments ABC, DEF are like, and consequently equal. Therefore also the remaining segment AC = DF. *WW'D.* (a) 10. 3. (b) 16. 1. (c) 10. 3. (d) 8. ax. 1.



Theorem 24.

Prop. XXVII.

In equal  $\odot^s$   $ABI$ ,  $DEF$ , the  $\angle^s$  standing upon equal parts of the circumference  $AI$ ,  $DF$  are equal one to the other, whether they be constituted at the centers  $G$  and  $H$ , or at the circumference  $B$  and  $E$ .

- (a) 26. 3.  
(b) hyp.  
(c) 9 ax.

For if it be possible, let be one of the  $\angle^s$   $AGC = DHF$ , and make  $AGI = DHF$ ; then is the Arch  $AI = DF = AC$ . Which is absurd.

Theorem 25.

Prop. XXVIII.

In equal  $\odot^s$   $ABC$ ,  $DEF$  equal Right-lines  $AC$ ,  $DF$  cut off equal parts of the circumference, the greatest  $ABC$  equal to the greatest  $DEF$ , and the least, to the least.

- (a) 8. 1.  
(b) 26. 3.  
(c) 3 ax.

Pro. From the centers  $G$  and  $H$  draw  $GA$ ,  $GC$  and  $HD$ ,  $HF$ : then because the  $\triangle AGC = \triangle DHF$ ; the  $\angle G = \angle H$ , and consequently the Arch  $AC = DF$ , and the remaining Arch  $ABC = DEF$ .  $WW'D$ .

Theorem 26.

Prop. XXIX.

In equal  $\odot^s$   $ABC$ ,  $DEF$ , equal Right-lines  $AC$ ,  $DF$  subtend equal peripheries,  $ABC$ ,  $DEF$ .

- (a) hyp.  
(b) 27. 3.  
(c) 4. 1.

Pro. Draw  $GA$ ,  $GC$ , and  $HD$ ,  $HF$ . Because  $GA = HD$  and  $GC = HF$ , and (because the Arch  $AC = DF$ ) the  $\angle G = \angle H$ , therefore is the base  $AC = DF$ .  $WW'D$ .

This and the 3 preceeding Prop. may be understood also of the same  $\odot$ .

Problem. 4.

Prop. XXX.

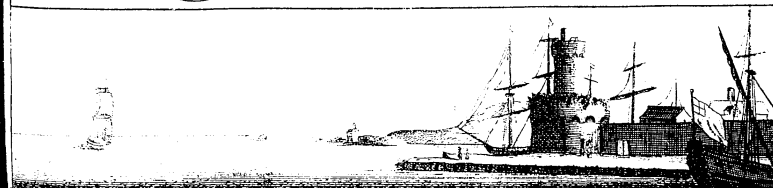
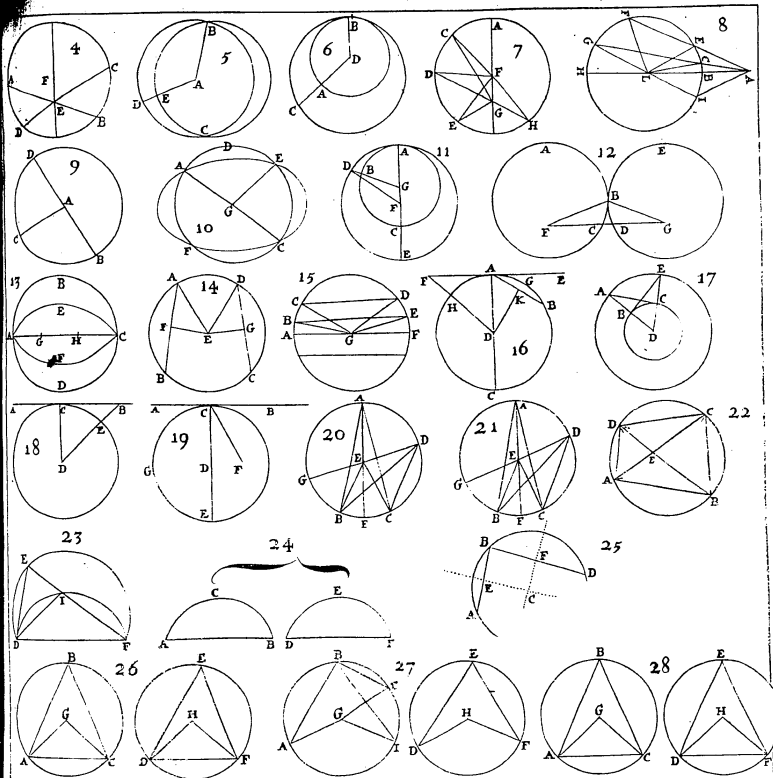
To cut a Periphery given  $ABC$ , into two equal parts

- (a) 10. 1.  
(b) conf.  
(c) 10 ax.  
(d) 4. 1.  
(e) 28. 3.

Pro. Draw the Right-line  $AC$ , and bisect it in  $D$ , with the  $\perp BD$  which shall bisect the Arch in  $B$ .

Pro. For  $AB$ ,  $CB$  being drawn, the side  $DB$  is common, and  $AD = DC$ , and the  $\angle ADB = \angle CDB$ . Therefore  $AB = BC$ ; and the Arch  $AB = BC$ .  $WW'D$ .

Prop.





## Prop. XXXI.

Theorem 27.

In a  $\bigcirc$ , ABEC the  $\angle ABC$  which is in the semicircle, is a Right  $\angle$ ; but the  $\angle$  which is the greater segment BAC is  $\supset \angle$ , and the  $\angle$  which is in the lesser segment BEC  $\subset \angle$ : Moreover the  $\angle CBA$  of the greater segment is greater than a  $\angle$ ; and the  $\angle EBC$  of the lesser segment is less than a  $\angle$ .

Pro. 1. Draw  $DA$ ,  $DB$ , and  $DC$ ; then the  $\angle DAB = \angle DBA$ : (a) 5. 1.  
 also the  $\angle DCB = \angle DBC$ , therefore the whole  $\angle ABC$  (b) 32. 1.  
 $= \angle A + \angle DCB = \angle FBC = \angle$ , and consequently the  $\angle ABC$  (c) 13. 1.  
 $= \angle$ . (d) 1 ax.

Pro. 2. The  $\angle ABC$  is  $\angle$ : therefore the  $\angle$  in the greater segment viz.  $BAC \supset \angle$ . (e) 32. 1.

Pro. 3. Make the Quadrilateral ABEC, then the  $\angle A \supset \angle$ , therefore the  $\angle$  in the lesser segment *scilicet*  $BE C \subset \angle$ . (f) 31. 1.  
 (g) 22. 3.

Pro. 4. The  $\angle$  contained under the Right-line  $CB$ , and Arch  $AB$  is  $\subset \angle ABC$ .

Pro. 5. But the  $\angle$  made by the Right-line  $CB$ , and lesser Arch  $EB$ , is less than the  $\angle FBC$ . *WW D*. (h) 9 ax.

Schol.

Thales did it first.

In any Right-lined Right-angled  $\angle$ , if the Hypothenufe be bisected, that point shall be the center of a  $\bigcirc$ , passing through the 3 angular points.

## Prop. XXXII.

Theorem 28.

If a Right-line  $AB$  touch a Circle,  $CHEG$ , and from the point of contact  $C$ , be drawn a Right-line  $CD$ , or  $EC$ , cutting the  $\bigcirc$ , the  $\angle$ s which it makes with the tangent line  $AB$ , are equal to those  $\angle$ s which are made in the alternate segments of the  $\bigcirc$ . That is the  $\angle ACE = \angle G$ , and the  $\angle BCE = \angle H$ .

Pro. Draw  $DC \perp AB$ , then the  $\angle ACD = \angle DEC = \angle ECD$  (a) 31. 3.  
 $+ \angle EDC$ . But the  $\angle BCE + \angle ECD = \angle$ : then taking away (b) 32. 1.  
 the common  $\angle ECD$ , the remaining  $\angle BCE = \angle EDC = \angle CHE$ , there- (c) 27. 3.  
 fore the  $\angle BCE = \angle CHE$ . Again, being in the Quadrilateral  $DG$ , the (d) 22. 3.  
 $\angle$ s  $\angle EDC + \angle EGC = 2 \angle = \angle ACE + \angle ECB$ , and the  $\angle CDE =$  (e) 13. 1.  
 $\angle BCE$  shall the remaining  $\angle G = \angle ACE$ . *WW D*. (f) 32. 3.

Prop.



Problem 5.

Prop. XXXIII.

Upon a Right-line AB, to describe a segment of a  $\circ$ , which shall contain an  $\angle$  equal to a Right-lined  $\angle$  given C.

- (a) 23. 1. *Pr<sup>a</sup>*. Make the  $\angle BAD = C$ . Through the point A draw  $AE \perp DH$ . At one end of the given line AB, make an  $\angle ABF = BAF$ , one side whereof may cut AE in F; with the extent AF, from the center F describe a  $\circ$ , and it shall pass through B, and AIB shall be the segment required.
- (b) cor. 16. 3. *Pro*. For  $HD \perp AE$ , and so  $HD^b$  touches the  $\circ$  which AB cuts, and therefore the  $\angle AIB^c = BAD^d = C$ . *WW Dn*.
- (c) 32. 3. *confr.*

Problem 6.

Prop. XXXIV.

From a  $\circ$  given ABC, to cut off a segment CBA containing an  $\angle B$ , equal to a Right-lined  $\angle$  given D.

- (a) 17. 3. *Pr<sup>a</sup>*. Draw the tangent EF, touching the given  $\circ$  in A, and make the  $\angle CAE = D$ , the segment ABC, shall contain an  $\angle B = CAE^d = D$ . *WW D*.
- (b) 23. 1.
- (c) 32. 3.
- (d) *confr.*

Theorem 29.

Prop. XXXV.

If in a  $\circ$ , AD BC two Right-lines AB, CD cut each other, the Rect-angle comprehended under the segments AE, EB of the one, shall be equal to the Rect-angle under the segments of the other, CE, ED. That is  $AE \times EB = CE \times ED$ .

*Pro*. 1. If they cut one the other in the center, the thing is evident of it self.

- Pro*. 2. If one line CD, pass through the center F, and bisect the other AB, in E; draw FB. Now CD is cut equally in F, and unequally in E, therefore  $CE \times ED = EFq^a = FDq = FBq^b = FBq^c = FEq + EBq$ . Therefore  $CE \times ED = FEq + FBq^b = FBq^c = FEq + EBq$ . Therefore  $CE \times ED = EBq$ . *WW D*.

- Pro*. 3. Let CD pass by the Center F, but not dividing the Right-line AB, equally in E; draw FB and make  $FG \perp$  to AB. Then the  $AE \times EB = ED + EFq = FDq$  or  $FBq$ . Again  $AE \times EB = GEq = G Bq$ . Add  $GFq$ . Now whereas  $FBq = FGq + GBq$ , the  $AE \times EB = GEq + GFq = FBq$ , that is, to the  $CE \times ED$  and to the Square of FE. Therefore whereas  $FEq = GFq + GEq$ , if from one be taken FE and from the other EGq and GFq, there remains  $CE \times ED = AE \times EB$ . *WW D*.

Pro.

4. If neither of the lines pass by the Center, and yet cut one the other, let GH be drawn through E by the Center F; Now whereas  $CE \times ED = HE \times EG$ , and that by the same Reason the  $AE \times EB = GE \times HF$ , therefore  $CE \times ED = AE \times EB$ . *WW D*. (e) p. 3. p. b. recq.

Prop. XXXVI.

Theorem 30.

If there be taken some point A without a Circle FBE, and from that point there fall two Right-lines to the Circle, one of which AB divides the Circle, and the other AF toucheth it, the Rect-angle contained under the whole line dividing AB and its part CA without, taken between the Convex part C and point A, is equal to the square of the touching Line AF.

*Pro*. 1. Let the line AB pass by the Center D, drawing DF, the Right-line BC is bisected in D, and the part CA is added. The  $AB \times AC = DCq = DAq$ . But  $DAq = DFq + FAq$ , and  $DFq = DCq$ ; take  $DCq$  away, rests  $AB \times AC = FAq$ . (a) c. 2. (b) 47. 1. (c) 18. 3. (d) 6. 2.

*Pro*. 2. If the Right-line AE pass not by the Center D, draw  $DG \perp$  to AE, it will cut IE into halves in G; therefore  $AE \times AI = GIq = GAq$ , and adding  $DGq$ , then  $AE \times AI = GIq + DGq = DAq + DGq$ , but  $GIq + DGq = DIq = DFq$ ; therefore  $AE \times AI = DFq = GAq + DGq = DAq = DFq + FAq$ , and taking away  $DFq$  from both sides it leaves  $AE \times AI = FAq$ . *WW D*.

*Corol*. 1. Hence it followeth, that if from any point without a Circle, there be drawn many lines to cut the Circle, the  $\square$  comprehended under every of those lines and the parts without the Circle, are equal to one another.

*Corol*. 2. Two Right-lines, drawn from the same point without and touching the Circle, are equal.

*Corol*. 3. And from the same point there can be drawn but two lines to touch the Circle.

Prop. XXXVII.

Theorem 31.

If without the Circle FHE any point A be taken, and from the same two lines AF and AB fall, so that one AB cut it and another AF fall upon it, so that the  $AB \times AC = AFq$ ; the line AF shall touch the Circle.

*Pro*. 2. Draw the Tangent AH, and from H the Right-line DH. Now whereas  $AHq = AB \times AC = FAq$ , the lines AH and AF shall be equal, and  $FD = DH$ , and the base AD common, therefore the  $\angle DFA = \angle DHA$ , and because  $\angle AHD = \angle AFD = \angle A$ , therefore AF shall touch the Circle per. *Corol*. 16. 3. *WW D*. (a) 17. 3. (b) 38. 2. (c) 8. 1. (d) 18. 3.

The most noted Prop. of this Book are the 20, 22, 31, 35, and 36.

K

THE





THE  
FOURTH BOOK  
OF  
Euclid's Elements.

DEFINITIONS.

1. A Right-lined figure is said to be inscribed in a Right-lined figure, when every one of the  $\angle$ s of the inscribed figure, touch every one of the sides of the figure wherein it is inscribed.

So the  $\triangle ABC$ , is inscribed in the  $\triangle DEF$ : because the  $\angle$ s  $A, B, C$  touch the sides  $DE, EF, DF$ .

2. In like manner a figure is said to be described about a figure, when every one of the sides of the figure circumscribed touch every one of the  $\angle$ s of the figure about which it is circumscribed.

So the  $\triangle DEF$ , is properly said to be described about the  $\triangle ABC$ .

3. A Right-lined figure is said to be inscribed in a  $\bigcirc$ , when all the  $\angle$ s of that figure which is inscribed do touch the circumference of the  $\bigcirc$ .

4. A Right-lined figure is said to be described about a  $\bigcirc$ , when all the sides of the figure which is circumscribed, touch the periphery of the  $\bigcirc$ .

5. Likewise:

5. Likewise a  $\bigcirc$  is said to be inscribed in a Right-lined figure, when the periphery of the  $\bigcirc$  touches all the sides of the figure in which it is inscribed.

6. A Circle is said to be described about a figure, when the periphery of the  $\bigcirc$  touches all the  $\angle$ s of the figure which it circumscribes.

7. A Right-line is said to be coapted or applied in a  $\bigcirc$ , when the extremes thereof fall upon the circumference.

So  $AB$ , is rightly said to be apply'd in the  $\bigcirc$ , and not  $CD$ .

Prop. I.

Problem 1.

In a  $\bigcirc$  given  $ABC$ , to apply a Right-line  $AB$ , equal to a Right-line given  $D$ , which doth not exceed the  $\bigcirc$ 's diameter  $BC$ .

Præ. **V** With the extent  $BE = D$ , <sup>a</sup> from the center  $B$  describe a  $\bigcirc$  (a) *prop. 3. 1.* cutting the given  $\bigcirc$  in  $A$ . Draw  $BA$ , then is  $BA$  <sup>b</sup>  $= BE$  (b) *15. 1.* <sup>c</sup>  $= D$ . *WW D n.* (c) *constr.*

Prop. II.

Problem 2.

In a  $\bigcirc$  given  $ABC$ , to describe a  $\triangle ABC$ , equiangular to a  $\triangle$  given  $DEF$ .

Præ. **D** Draw the tangent  $GH$ , touching the  $\bigcirc$  given in  $A$ , and make (a) *17. 3.* <sup>b</sup> the  $\angle HAC = \angle E$ , and  $GAB = F$ , also join  $BC$ , and the (b) *23. 1.* thing required is done. (c) *32. 3.*

Pro. For the  $\angle B^c = HAC^d = E$ , and the  $\angle C^e = GAB^d = F$ ; (d) *constr.* <sup>e</sup> Whence also the  $\angle BAC = D$ . Therefore the  $\triangle ABC$  inscribed in the  $\bigcirc$ , is equiangular to  $DEF$ . *WW D n.* (e) *23. 1.*

Prop. III.

Problem 3.

About a  $\bigcirc$  given  $BCE$ , to describe a  $\triangle LM\bigcirc$  equiangular to a  $\triangle$  given  $DFA$ .

Præ. **P** Produce the side  $AF$  of the given  $\triangle$  to  $G$  and  $H$ ; and at the center  $I$ , <sup>a</sup> make an  $\angle CIB = \angle DFH$ , and  $EIB = DAG$ . (a) *23. 1.* Then to the points  $E, B, C$ , <sup>b</sup> let 3 touch lines be drawn as  $M\bigcirc, ML, L\bigcirc$ , (b) *17. 3.* and the thing is done: That the Right-lines  $M\bigcirc, ML, L\bigcirc$  will meet and (c) *13. 3.* make a  $\triangle$  is evident, <sup>c</sup> because (the  $\angle$ s  $LEI, LBI$  being right; the (c) *11. 4.* Right-line  $BE$  being drawn,) the  $\angle$ s  $LEB, LBE$  will be less than 2  $\angle$ s. (d) *32. 1.* And seeing the  $\angle EIB + L^e = 2 \angle s^f = DAG$ , <sup>e</sup>  $\angle DAF$ , and  $EIB$  (d) *13. 1.* <sup>f</sup>  $= DAG$ ; <sup>g</sup> therefore the  $\angle L = DAF$ . By like reason the  $\angle M = (g) *constr.*$   $DF A$ , <sup>h</sup> therefore also the  $\angle \bigcirc = D$ . And therefore the  $\triangle LM\bigcirc$  described about the  $\bigcirc$  is equiangular to  $AFD$ , the given  $\triangle$ . *WW D n.* (h) *3. 1.*

K 2

Prop



Problem 4.

Prop. IV.

In a  $\triangle$  given  $ABC$ , to describe a  $\circ$ ,  $EFG$ .

- (a) 2. 1.  
(b) 12. 1.  
(c) *confr.*  
(d) 10. ax.  
(e) 26. 1.

*Pro.* Bisect the  $\angle$ 's  $B$  and  $C$ , with the Right-lines  $BD$ ,  $CD$ , meeting in the point  $D$ ,<sup>b</sup> and draw the Perpendiculars  $DE$ ,  $DF$ ,  $DG$ . A  $\circ$  described with the extent  $DG$  from the center  $D$ , will pass through  $F$  and  $E$  also, and touch the 3 sides of the  $\triangle$ .

*Pro.* For the  $\angle DBE^c = DBF$ ; and the  $\angle DEB^d = DFB$ ; and the side  $DB$  common, <sup>e</sup> therefore  $DE = DF$ , and for the same reasons  $BF = DF$ . Therefore the  $\circ$  passeth through the 3 points  $E$ ,  $F$ ,  $G$ . And because the  $\angle$ 's  $E$ ,  $F$ ,  $G$ , are right, it also touches all the sides of the  $\triangle$ . *WWDN.*

*Schol.*

Hence, the sides of a  $\triangle$  being known, their segments which are made by the points of contact of the inscribed  $\circ$  may be found; thus. Let  $AB$  be 12,  $BC$  16,  $AC$  18. Then shall  $AB \perp BC = 28$ . From which subtract  $AC$  18,  $= AE \perp FC$ , and there shall remain  $10 = BE \perp BF$ . And therefore  $BE$  or  $BF = 5$ ; and consequently  $FC$  or  $CG = 11$ ,  $GA$ , or  $AE = 7$ .

Problem 5.

Prop. V.

About a  $\triangle$  given  $ABC$ , to describe a Circle.

- (a) 10 & 11. 1.

*Pro.* Bisect any two sides  $AB$ ,  $BC$ , with Perpendiculars  $ED$ ,  $FD$ , meeting in the point  $D$ , this point  $D$  shall be the center of the  $\circ$ , from which with the extent  $BD$ , the circle may be described circumscribing the  $\triangle$  given.

- (b) *confr.*

- (c) 4. 1.

*Pro.* Draw the Right-lines  $DB$ ,  $DA$ ,  $DC$ . Then because  $BE = EA$ , and  $DE$  is common and the  $\angle$ 's at  $E$  right, shall  $AD^c = DB$ . After the same manner is proved  $DB^c = DC$ , therefore  $\odot^c$ . *WWDN.*

*Corol.*

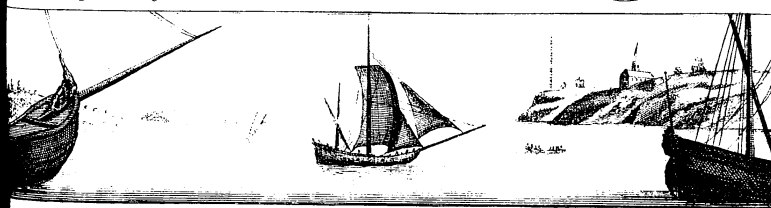
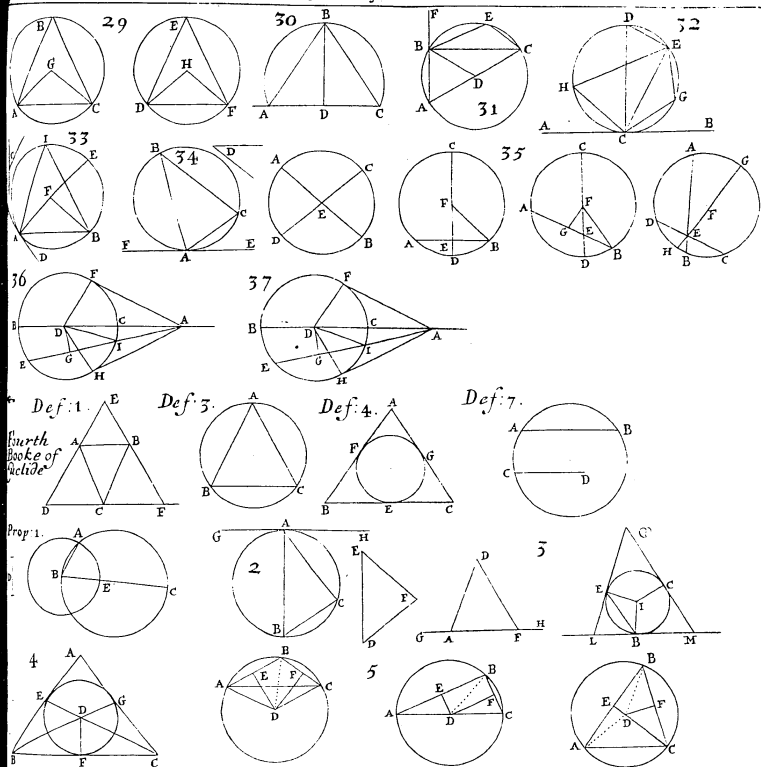
- (d) 21. 3.

<sup>d</sup> Hence, if a  $\triangle$  be acute angled, the center shall fall within the  $\triangle$ ; if Right-angled, in the side opposite to the right  $\angle$ , and if obtuse angled, without the  $\triangle$ .

*Schol.*

By this method also may a  $\circ$  be described, that shall pass through 3 points given, not lying in a straight line.

*Prop.*





## Prop. VI.

Problem 6.

*In a given Circle ABC, to inscribe a Square.*

*Præ.* Draw the Diameters  $AC, BD$ , cutting each other at Right-angles <sup>(a)</sup> 11. 1. in the center  $E$ , then drawing also the Right-lines  $AB, BC, CD, DA$ . The thing required is done.

*Pro.* Because the  $\angle$ s at the center  $E$  are right, <sup>a</sup> the Arches and <sup>b</sup> subtences  $AB, BC, CD, DA$  are equal; therefore is the figure  $ABCD$  equilateral, and all the  $\angle$ s in semicircles, and so <sup>c</sup> right. Therefore  $AB$  <sup>(a)</sup> 26. 3. <sup>(b)</sup> 29. 3. <sup>(c)</sup> 31. 3.  $CD$  shall be a Square inscribed in a  $\bigcirc$ . *WW'Dn.*

## Prop. VII.

Problem 7.

*About a  $\bigcirc$  given, to describe a Square.*

*Præ.* Draw the Diameters  $AC, BD$ , cutting one the other at right  $\angle$ s <sup>(a)</sup> 11. 1. in the center  $E$ ; then through the extremes of these Diameters, <sup>a</sup> draw the  $\perp$ s or tangents  $FG, FI, IH, GH$ , these produced till they <sup>(g)</sup> 17. 3. meet in the points,  $F, G, H, I$ , shall constitute the required  $\square$ .

*Pro.* Because <sup>b</sup> the  $\angle$ s at  $E$  are  $\perp$ s, as also those at  $A, B, C, D$ , <sup>(b)</sup> 18. 3. <sup>(c)</sup> 28. 1. therefore the Right-lines  $FG, BD, HI$ , are parallel, and also  $FI, AC$  <sup>(d)</sup> 34. 1.  $GH$ , are parallel, <sup>d</sup> and therefore  $FGIH$  is a Right-angled parallelogram. <sup>(e)</sup> 15 def. 1. And because  $FG$  <sup>a</sup>  $HI$  <sup>d</sup>  $DB$  <sup>c</sup>  $CA$  <sup>d</sup>  $GH$  <sup>d</sup>  $FI$ , it's also equilateral, and consequently a Square. *WW'Dn.* <sup>(f)</sup> 25 def. 1.

*Schol.*

The Square circumscribing a  $\bigcirc$ , is double the Square inscribed in the same  $\bigcirc$ . For  $BA, AD$  (the sides of an inscribed  $\square$ ) being drawn, the  $\square$  <sup>(g)</sup> 41. 1.  $BG = 2BAD$ , and  $BH = 2BCD$ .

## Prop. VIII.

Problem 8.

*In a Square given, to describe a Circle.*

*Præ.* Bisect the sides of the given Square in  $A, B, C, D$ , and draw  $AC, BD$ , cutting one the other in  $E$ , from which as center with the extent  $EA$  if a  $\bigcirc$  be described, the Problem is answer'd.

*Pro.* Because  $AE, IC$ , are parallel and equal,  $EG, HI$ , as also  $AC, FI$  are parallel and equal, and likewise  $AC, HG$ , therefore  $FE, EI, EH, EG$  are  $\square$ s. And because  $BF = FA = AE = EB = EC = ED$ , therefore shall  $E$  be the center, from which with the extent  $EA$  a  $\bigcirc$  being described, shall touch all the points  $ABCD$ , and consequently all the sides of the Square. *WW'Dn.*

*Prop.*



Problem 9.

Prop. IX.

*About a given Square, to describe a Circle.*

**Præ.** Draw the diameters  $AC, BD$ , cutting one the other in  $E$ . From the center  $E$ , through  $A$  describe a  $\bigcirc$ , which shall answer the Problem.

(a) 4 cor. 32.1. **Pro.** For the  $\angle ABD = BAC = \frac{1}{2} \angle$ , <sup>b</sup> therefore  $AE = EB$ .  
(b) 6. 1. After the same manner is  $AE = ED = EC$ . The  $\bigcirc$  therefore described from the center  $E$  passes through  $A, B, C, D$ , the  $\angle$ s of the  $\square$  given.  $WW'Dn$ .

Problem 10.

Prop. X.

*To make an Isosceles  $\triangle ABD$ , having each  $\angle$  at the base  $B$  and  $D$ , double to the remaining  $\angle A$ .*

(a) 11. 2. **Præ.** Take any Right-line  $AB$ , and divide it <sup>a</sup> fo in  $C$ , that  $AB \times BC = AC^2$ . Then from the center  $A$ , through  $B$ , describe a  $\bigcirc$ , in which  
(b) 1. 4. let be <sup>b</sup> applied  $BD = AC$ , and joyn  $AD$ . I say  $ABD$  is the  $\triangle$  required:  
(c) 5. 4. Which is thus proved.  
(d) 37. 3. **Pro.** Draw  $DC$ , and through the points  $ADC$  <sup>c</sup> describe a  $\bigcirc$ . Now  
(e) 32. 3. seeing  $AB \times BC = CA^2 = BD^2$ , <sup>d</sup> it's evident, that  $BD$  touches the circle  
(f) 2. ax.  $ACD$  which  $DC$  cutteth; <sup>e</sup> therefore is the  $\angle BDC = A$ , and therefore  
(g) 32. 1. also the  $\angle BDC - \angle CDA^f = A - \angle CDA^g = BCD$ . But  $BDC - \angle CDA = BDA^h = CBD$ ; <sup>k</sup> therefore the  $\angle BCD = CBD$ , and therefore  
(h) 5. 1.  $DC^i = DB = AC$ , <sup>n</sup> seeing the  $\angle CDA = A = BDC$ ; therefore  
(i) 1. ax.  $ADB = 2A = ABD$ .  $WW'Dn$ .  
(m) 10. 1.   
(n) 5. 1.

Corol.

Seeing all the 3  $\angle A, B, D$ , together make 2  $\angle$ s, it is evident that  $A$  is  $\frac{2}{3}$  of 2  $\angle$ s.

Prop. XI.

*In a  $\bigcirc$  given  $EHFGI$ , to describe a Pentagone Figure equilateral and equiangular.*

(a) 10. 4. **Præ.** Make an Isosceles  $\triangle$ , having each  $\angle$  at the base double to  
(b) 2. 4. that at the vertex, <sup>b</sup> and inscribe one equiangular thereto  
(c) 9. 1. in the  $\bigcirc$  given  $EHFG$ . <sup>c</sup> Biseñ the  $\angle$ s at the base with the lines  $IF, HG$ , and lastly, joyn these 5 points  $E, H, F, G, I$ , with so many Right-lines, and the thing required is done.

Pro.

**Pro.** Seeing by the construction the  $\angle EFG, FGH, HGE, JFG, EFI$ , are equal; <sup>a</sup> the Arches and their subtended lines  $FG, FH, HE, EI, IG$ , are equal. (d) 26. 3. Then the Arch  $EH = FG$ . Therefore if  $HF$  be put common, the Arch  $EHF = HFG$ ; and to the other segment  $FG = IE = GI = EH$ : <sup>b</sup> therefore the  $\angle EHF = HFG$ , and the same may be said of the rest. Therefore is the inscribed Pentagone both equilateral and equiangular.  $WW'Dn$ . (e) 29. 3. (f) 27. 3.

Corol.

Each  $\angle$  of an equilateral and equiangular Pentagone, is equal to  $\frac{1}{5}$  of 2  $\angle$ s, or  $\frac{2}{5}$  of one  $\angle$ .

Prop. XII.

Problem 11.

*About a  $\bigcirc$  given  $ABCD$ , to describe an equilateral and equiangular Pentagone  $GHIKL$ .*

**Præ.** IN the  $\bigcirc$  given <sup>a</sup> inscribe a Pentagone  $CB AED$ ; and from the center <sup>a</sup> 11. 4.  $F$  draw the Right-lines  $FA, FB$ , &c. and to those points  $C, B, A, E, D$ ; draw so many touch lines, which meeting in the points  $G, H, I, K, L$ , shall complet the Pentagone required.

**Pro.** Because  $HA, HB$ , from the same point  $H$  <sup>b</sup> touch the  $\bigcirc$ , <sup>c</sup> therefore is  $HA = HB$ , and <sup>d</sup> therefore the  $\angle AFH = HFB$ , therefore the  $\angle AFB = 2HFA$ . After the same manner is the  $\angle BFI = IFB$ , and consequently the  $\angle BFC = 2BFI$ . <sup>e</sup> But the  $\angle AFB = CFB$ , <sup>f</sup> therefore the  $\angle HFB = BFI$ . But also the  $\angle FBI^g = FBH^h$ ; and the side  $FB$  is common, <sup>i</sup> therefore  $IB = BH = HA = AG$ , &c. <sup>j</sup> Therefore the sides  $IH = GH = GL = LK = KI$ , the  $\angle$ s also are equal, because double of the equal  $\angle$ s  $BHF, BIF$ . Therefore the Pentagone is both equilateral and equiangular.  $WW'Dn$ . (b) cor. 16. 3. (c) 2 cor. 36. 3. (d) 8. 1. (e) 27. 5. (f) 7. 4. (g) 19. 2. (h) 26. 1. (i) 2. ax.

Corol.

Hence, if any equilateral and equiangular figure be inscribed in a Circle, and at the extremes of the semidiameters be raised  $\perp$ s to the said diameters, these  $\perp$ s shall constitute another figure of as many equal sides, and equal  $\angle$ s circumscribed about the  $\bigcirc$ .

Prop.



Problem 13.

Prop. XIII

*In an equilateral and equiangular Pentagon given, to inscribe a Circle.*

(a) 9. 1. *Præ.* Bisect two  $\angle$ s  $BAE, ABC$ , with the Right-lines  $AF, BF$ , meeting in the point  $F$ . From  $F$  draw the Perpendiculars  $FG, FH, FI$  &c. Then a  $\bigcirc$  described from the center  $F$ , with the extent  $FG$  will touch all the sides of the Pentagon.

(c) *confr.* *Pro.* Because, in the  $\triangle$ s  $ABF, FBC$ , the side  $BA = BC$ , and  $BF$  is common, and the  $\angle ABF = CBF$ ; Therefore is the  $\angle BAF = BCF$ , and  $AF = CF$ . But the  $\angle BAF = \frac{1}{2} BAE = BCF = \frac{1}{2} BCD$ . Therefore the  $\angle FCB = \frac{1}{2} BCD$ . After the same manner are all the other  $\angle$ s bisected. Because the  $\angle FGB = FLB$ , and the  $\angle GBF = FBL$ , and the side  $FB$  common; <sup>a</sup> therefore is  $FG = FL$ . In like manner are all the lines  $FK, FI, FH$ , equal. Therefore a  $\bigcirc$  described from the center  $F$ , with the extent  $FG$ , passes through the points  $H, I, K, L$ , and touches the <sup>b</sup> sides of the Pentagon, because the  $\angle$ s at those points are right. *WW'D n.*

Corol.

Hence, if any two nearest  $\angle$ s of an equilateral and equiangular figure be bisected, and from the point in which those bisecting lines meet, be drawn Right-lines to the remaining  $\angle$ s of the figure, all the  $\angle$ s of the figure shall be bisected.

Schol.

By the same method shall a  $\bigcirc$  be inscribed, in any equilateral and equiangular figure.

Problem 14.

Prop. XIV.

*About a Pentagon given, which is both equilateral and equiangular to describe a Circle.*

*Præ.* Bisect any two  $\angle$ s of the Pentagon, as  $A$  and  $E$ , with the Right-lines  $AF, FE$ , meeting in the point  $F$ ; the  $\bigcirc$  described from the center  $F$ , through  $A$ , shall be described about the Pentagon.

(a) 13. 4. *Pro.* Let  $FD, FC, FB$ , be drawn. <sup>a</sup> Then the  $\angle$ s  $D, C, B$ , are bisected; and therefore  $FA = FB = FC = FD = FE$ . Therefore the  $\bigcirc$  described from the center  $F$ , &c. shall circumscribe the Pentagon. *WW'D n.*

Schol.

By the same method shall a  $\bigcirc$  be described, about any equilateral equiangular figure.

Prop.

Prop. XV.

Problem 15.

*In a given Circle to inscribe an Hexagon (or six sided figure) equilateral and equiangular.*

*Præ.* Draw the diameter  $AD$ ; from  $D$  with the extent  $DG$  describe a  $\bigcirc$  cutting the  $\bigcirc$  given in the points  $C$  and  $E$ . Draw the diameters  $CF, EB$ , and join  $AB, BC, CD, DE, EF, FA$ , and it's done. *Pro.* The Right-lines  $GC = GD = CD = DE$ ; therefore the  $\triangle DGC$  is equilateral, and <sup>b</sup> consequently equiangular. Then the  $\angle CGD = \frac{1}{2}$  of  $2 \angle$ s  $= DGE = AGF = AGB$ . And seeing  $CGE = EGF = 2 \angle$ s shall  $EGF = \frac{1}{2}$  of  $2 \angle$ s. Therefore the <sup>c</sup> arcs and <sup>d</sup> subtenses  $AB, BC$  &c. are equal, therefore the Hexagon is equilateral; and also equiangular <sup>e</sup> seeing the  $\angle$ s of it stand upon equal arcs.

Corol.

1. The side of an Hexagon inscribed in a  $\bigcirc$  is equal to the semi-diameter.

Schol.

1. Hereby an equilateral  $\triangle$  may easily be described in a Circle viz. by drawing  $AC, AE, CE$ .

2. To make a true Hexagon upon a Right-line given  $CD$ . <sup>a</sup> Make an equilateral  $\triangle CGD$ , upon the given line  $CD$ , describing a  $\bigcirc$  with the extent  $CG$  from the center  $G$ . That  $\bigcirc$  shall contain the Hexagon required. *Ans. T. 4. 1.*

Prop. XVI.

Problem 16.

*In a given Circle to inscribe a Quindecagon (or fifteen sided figure) equilateral and equiangular.*

*Præ.* Inscribe in the given  $\bigcirc$  an equilateral Pentagon  $A E F G H$ , and also an equilateral  $\triangle ABC$ , then is  $BF$  the side of the Quindecagon required. *(a) 11. 4. (b) 2. 4.*

*Pro.* For the arch  $AB$  is  $\frac{1}{5}$  of that periphery, whereof  $AF$  is  $\frac{2}{5}$  or  $\frac{4}{5}$ . Therefore the remaining part  $BF$  is  $\frac{1}{5}$  of the periphery; and therefore the Quindecagon, whose side is  $BF$ , is equilateral, but it is equiangular also, <sup>a</sup> because all the  $\angle$ s insit on equal arcs, whereof every one is  $\frac{1}{5}$  of the whole circumference, Therefore &c. *(c) confr. (d) 27. 3.*

Schol.



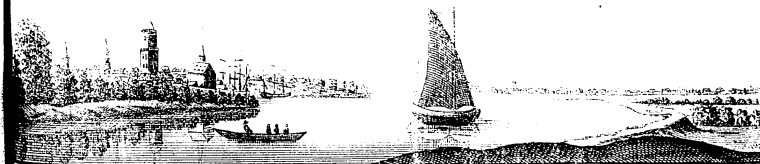
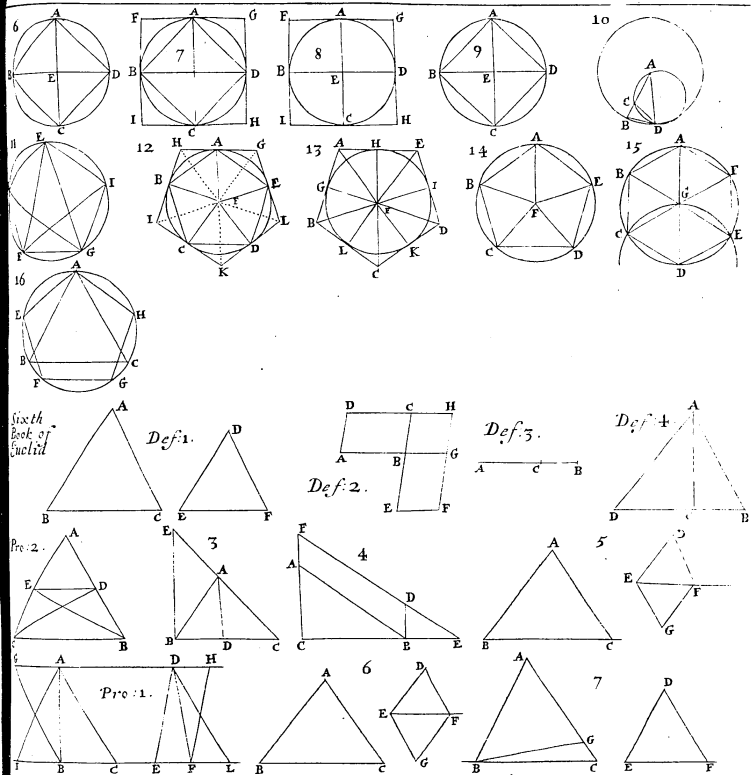
*Schol.*

A Circle is Gemoetrically divided into parts.  $\left\{ \begin{array}{l} 4, 8, 16, \&c. \text{ by } 6, 4, \text{ and } 9, 1. \\ 3, 6, 12, \&c. \text{ by } 15, 4, \text{ and } 9, 1. \\ 5, 10, 20, \&c. \text{ by } 11, 4, \text{ and } 9, 1. \\ 15, 30, 60, \&c. \text{ by } 16, 4, \text{ and } 9, 1. \end{array} \right.$

To divide the circumference into any other parts, is yet unknown; wherefore in the construction of ordinate figures, we are forced to have recourse to mechanick artifices.

THE

4<sup>th</sup> Book.







THE  
FIFTH BOOK  
OF  
Euclid's Elements.

DEFINITIONS.

1. **A** *Part*, is a Magnitude of a Magnitude, a less of a greater, when the less measureth the greater.  
 2. *Multiplex* is a greater, when the lesser measureth the greater.  
 3. *Ratio*, (or Rate) is the mutual habitude of two Magnitudes of the same kind each to other, according to quantity.

In every Ratio, that quantity which is referred to another quantity, is called the antecedent of the Ratio; and that to which the other is referred is called the consequent of the Ratio, as in the Ratio 6 to 3, 6 is the antecedent and 3 the consequent.

Note, The quantity of any Ratio, is known by dividing the antecedent by the consequent; as the Ratio of 12 to 5, is expressed by  $\frac{12}{5}$ ; or the quantity of the Ratio, of  $a$  to  $b$ , is  $\frac{a}{b}$ . Wherefore often for brevity sake we

1. 2.

denote



denote the quantities of Ratios thus;  $\frac{a}{b} <$ , or  $=$ , or  $> \frac{c}{d}$ , that is, the Ratio of  $a$  to  $b$ , is greater, equal, or less, than the Ratio of  $c$  to  $d$ .

4. *Proportion* is a Similitude of Ratios.

That which is here termed proportion, is more rightly called proportionality or Analogy; for proportion commonly denotes no more than the Ratio between two Magnitudes.

5. Those numbers are said to have a Ratio betwixt them, which being multiplied may exceed one the other.

6. *Magnitudes*, are said to be in the same Ratio, the first  $a$  to the second  $b$ , and the third  $c$  to the fourth  $d$ , when the equimultiples  $g$  and  $h$ , of the first  $a$ , and the third  $c$  compared with the equimultiples  $k$ ,  $l$  of the second  $b$ , and the fourth  $d$ ; according to any multiplication whatever, either both together  $g$ ,  $h$  are less than  $k$ ,  $l$ , both together, or equal taken together; or exceeding one the other together if those be taken  $g$ ,  $k$ , and  $h$ ,  $l$ , which answer one to the other. That is, compare the multiplex of the first, with the multiplex of the second, and the multiplex of the third with that of the fourth; and see, whether as often as the multiplex of the first contains or is contained by the multiplex of the second, so often the multiplex of the third contains or is contained by the multiplex of the fourth; for if it be so, then are those 4 quantities in the same Ratio, otherwise not. Thus, seeing  $k$  30 contains  $g$  12, as often as  $l$  50 contains  $h$  20, viz.  $2\frac{1}{2}$ ,  $a$ ,  $b$ , and  $c$ ,  $d$ , or 5, 6, and 5, 10, are in the same Ratio. The note of identity of Ratio is ::, as in the former

example,  $a : b :: c : d$ , but sometimes it's expressed  $\frac{a}{b} = \frac{c}{d}$ .

7. Magnitudes that have the same Ratio, are called *Proportionals*.

8. When of equimultiples,  $g$ , the multiplex of the first  $a$ , exceeds  $k$  the multiplex of the second  $b$ , but  $h$ , the multiplex of the third  $c$ , exceed not  $l$ , the multiplex of the fourth  $d$ , then the first  $a$ , to the second  $b$ , has a greater Ratio; then the third  $c$ , to the fourth  $d$ .

If  $\frac{a}{b} < \frac{c}{d}$ , it is not necessary from this Definition that  $g$ , should always exceed  $k$ ; when  $h$  is less than  $l$ , but it is granted that this may be.

9. *Proportionality* consists in three terms at least. Whereof the second supplies the place of two.

10. When three Magnitudes  $a$ ,  $b$ ,  $c$ , are proportional, the first  $a$ , shall have a *duplicate Ratio*, to the third  $c$ , of that it hath to the second  $b$ : But when 4 Magnitudes  $a$ ,  $b$ ,  $c$ ,  $d$ , are proportional, the first  $a$ , shall have a *triplicate Ratio*, to the fourth  $d$ , of what it had to the second  $b$ ; and so always one more in order, as the proportion shall be extended.

Duplicate

Duplicate Ratio is thus expressed,  $\frac{a}{c} = \frac{a^2}{d}$ . And triplicate Ratio thus;

$\frac{a}{c} = \frac{a^3}{d}$ . That is the Ratio of  $a$  to  $c$ , is triple of the Ratio of  $a$  to  $d$ .

11. Magnitudes of a like Ratio, are antecedents to antecedents; and consequents to consequents; as if  $a : b :: c : d$ .  $a$  and  $c$ , and  $b$  and  $d$ , are homologous or Magnitudes of a like Ratio.

In the 6 following Definitions, names are given to the 6 ways of arguing, used by Mathematicians, which will be demonstrated in their places in this Book.

12. *Alternate Proportion* is the comparing of antecedent to antecedent, and consequent to consequent. As if  $a : b :: c : d$ , then alternately it's  $a : c :: b : d$ . By 16, 5.

13. *Inverse Ratio*, is when the consequent is taken as the antecedent, and so compared to the antecedent as the consequent; as  $a : b :: c : d$ . Therefore generally  $b : a :: d : c$ , by Cor. 4, 5.

14. *Compound Ratio*, is when the antecedent and consequent taken both as one, are compared to the consequent it self; as  $a : b :: c : d$ . Therefore by composition  $a + b : b :: c + d : d$ , by 18, 5.

15. *Divided Ratio*, is when the excess wherein the antecedent exceeds the consequent, is compared to the consequent. As  $a : b :: c : d$ . Therefore by Division  $a - b : b :: c - d : d$ , by 17, 5.

16. *Converse Ratio*, is when the antecedent is compared to the excess, wherein the antecedent exceeds the consequent. As  $a : b :: c : d$ . Therefore by converse Ratio,  $a : a - b :: c : c - d$ , by Cor. 19, 5.

17. *Proportion of equality* is where there are taken more Magnitudes than two in one order, and also as many Magnitudes in another order, comparing two to two being in the same Ratio; it cometh to pass that as in the first order of Magnitudes, the first is to the last, so in the second order of Magnitudes is the first to the last. Or thus; it is a comparison of the extremes together, the means being omitted.

18. *Ordinate Proportionality* is, when, as the antecedent is to the consequent, so is the antecedent to the consequent, and as the consequent is to any other, so is the consequent to any other. As  $a : b :: d : e$ , also  $b : c :: e : f$ , it shall be also  $a : c :: d : f$ , by 22, 5.

19. *Inordinate Proportion* is, when 3 Magnitudes being put, and others also, which are equal to these in Multitude, as in the first Magnitudes the antecedent is to the consequent; so in the second Magnitudes is the antecedent to the consequent: and as in the first Magnitudes the consequent is to any other, so in the second Magnitudes any other thing to the antecedent. As  $a : b :: f : g$ , also  $b : c :: e : f$ , it shall be true in ordinate proportion,  $a : c :: e : g$ , by 23, 5.

20. Any number of Magnitudes being put; the proportion of the first to the last, is compounded of the proportions of the first to the second, the second to the third, and the third to the fourth &c. till the proportion arith.

Arith.



## Axiome.

Magnitudes equimultiples to the same multiplex, are also equimultiples betwixt themselves.

Theorem 1.

Prop. I.

3 1 3 1 If there be a number of Magnitudes howmany soever a, c,  
a. e. c. f. equimultiples to a like number of Magnitudes e, f, each  
6 2 to other; how multiplex one Magnitude a, is to one e,  
g. h. so multiples are all the Magnitudes a + c to all the  
other Magnitudes e + f. That is, because a to e, and  
(e) 2 5 def. c to f, are equimultiples. If a and c be joyned in g, and  
likewise e and f in h, how multiplex a shall be of e, and c of f.  
So multiplex shall g be of h.

Pro. **B**ecause as well g, as h, are augmented by an equal number of containing and contained parts.

Theorem 2.

Prop. II.

6 3 4 2 If the first a be equimultiplex to the second b, as the  
a. b. c. d. third c is to the fourth d; and if the fifth e be  
9 6 15 10 equimultiplex to the second b, as the sixth f is to the  
c. f. g. h. fourth d; then shall the first compounded with the  
fifth (g) be equimultiplex to the second c, as the third  
compounded with the sixth (h) is to the fourth d.

Pro. <sup>(a) b p.</sup> **T**he second b and fourth d, are contained alike numbers of times  
in their multiples a and e, viz. twice, and likewise the same  
second b and fourth d, are contained alike numbers of times in their other  
multiples c and f, viz. thrice. <sup>(b) 1. 5</sup> Therefore they shall also be contained  
alike number of times in the compound multiples, that is, if it be made  
that a + e = g, and likewise f + c = h; then as g contains b five times,  
so shall h contain d five times.

Prop.

Prop. III.

Theorem 3.

4 2 6 3 If the first a be equimultiplex to the second b, and the  
a. b. c. d. third c of the fourth d, and there be taken e and f  
8 12 equimultiples of the first and third, then will each  
e. f. of the Magnitudes taken be alike equimultiplex of  
both, the one e to the second b, the other f to the  
fourth d.

Pro. **L**et b and d, be contained alike number of times in each of these (a) 1. 4.  
a and c; <sup>2</sup> then they shall also be contained an equal number of  
times in any the multiples of a and c as e and f.

Theorem 4.

Prop. IV.

4 2 6 3 If the first a, have the same Ratio to the second b,  
a. b. c. d. as the third c to the fourth d; then also e and g,  
8 6 12 9 the equimultiples of the first a and the third c,  
e. f. g. h. shall have the same Ratio to f and h; the equi-  
16 12 24 18 multiples of the second b and the fourth d, ac-  
l. m. k. n. cording to any Multiplication, if so taken as they  
answer each one the other.

**T**ake l and k the equimultiples of e and g; and also m and n the <sup>(a) 3. 5.</sup>  
equimultiples of f and h. <sup>(b) b p.</sup> Then is l as multiplex of a, as k of c;  
<sup>2</sup> and also m is as multiplex of b, as n of d. Therefore whereas it is a . b  
<sup>b</sup> :: c . d; according to the sixth definition, if l be =, =, = m, then  
consequently, after the same manner is k =, =, = n. Therefore when  
l and k are taken as multiples of e and g, as m and n of f and h, then will  
it be by the 7 def. e . f :: g . h. WW'D.

Corol.

From hence is wont to be demonstrated the proof of inverse (or con-  
verse) Ratio.

For because a . b :: c . d, therefore if e =, =, = f, then is <sup>(c) 2 def. 5.</sup>  
like-  
wise g =, =, = h; therefore it's evident that if f =, =, = e, then is <sup>(d) 6 def. 5.</sup>  
b =, =, = g; <sup>a</sup> therefore b . a :: d . c. WW'D.

Prop.



Theorem 5.

Prop. V.

e, 4. f, 2. If a Magnitude a, be as multiplex of a Magnitude b,  
c, 8. d, 4. as part taken from the one c, of a part taken from  
a, 12. b. 6. the other d; the residue of the one c, shall be as  
g, 4. multiplex of the residue of the other f, as the whole  
a is of the whole b.

(a) 1. 5.  
(b) 6 ax. 1.  
(c) 2 ex. 1.

Take any other g, which shall be as multiplex to f, as a is of b, or  
as the part taken away c is of the part d. Therefore g-|-c is as  
multiplex of d-|-f; as the one c of the one d, that is, as a of b. Therefore  
g-|-c<sup>h</sup> = a; and so c that was common being taken away, there remains  
g = c.

Theorem 6.

Prop. VI.

g 2, h 3, | g 8, h 12,  
c 10, f 15, | c 4, f 6,  
a 12, b 18, | a 12, b 18,  
c 2, d 3, | c 2, d 3,

If two Magnitudes a and b, be equi-  
multiples of two Magnitudes c, d;  
and some Magnitudes e, f, equimulti-  
ples of the same c, d, be taken away,  
then the residues g, h, are either e-  
qual to these Magnitudes c, d or else  
the equimultiples of them.

(a) Hyp.  
(b) 5. 5.

Pro. C and d, are contained an equal number of times in a and b, and  
also in some of their parts e, f; therefore they shall also be con-  
tained an equal number of times in the residues g and h. Therefore the  
residues, are either equal or equimultiples. WW'D.

Theorem 7.

Prop. VII.

24 8 24 Equal Magnitudes a and a, have to the same Magni-  
d. f. c. tude b, the same proportion or Ratio. And one and the  
a. a. same Magnitude b hath the same Ratio, to equal  
12 b. 12 Magnitudes a and a.  
A

(a) 6 ax. 1.  
(b) 6 def. 5.

Pro. Take d and e, equimultiples of the equal Magnitudes a and a,  
and f any wise multiplex of b; then is d = e. Wherefore if  
d = e, = f; then also e will be = f. Therefore a : b :: a : b.  
and by inversion b : a :: b : a. WW'D.

Schoi.

Schoi.

If instead of the multiplex f, two equi-multiples be taken, it shall  
be the same way proved that equal Magnitudes have the same Ratio, to  
other Magnitudes that are equal between themselves.

Prop. VIII.

Theorem 8.

16 8 5 Of unequal Magnitudes a, b, the greater a hath a greater  
a. b. c. Ratio to the same third c, than the lesser b; and the  
6 4 8 same third c hath a greater Ratio to the lesser b, than  
d. e. f. to the greater a.  
32 16 20

Pro. Take d and e, equimultiples of the said a, b, and also f a  
multiplex of c, greater than e but less than d, (which will easily  
happen, if both e and d = e be taken greater than c.) It is manifest from 8  
def. 5. That  $\frac{a}{c} < \frac{b}{c}$ , and  $\frac{e}{a} > \frac{c}{b}$ . WW'D.

Prop. IX.

Theorem 9.

a. b. c. Magnitudes which to one and the same Magnitude have  
15 15 4 the same Ratio, are equal one to the other. And if  
a Magnitude have the same Ratio to other Magnitudes  
those Magnitudes are equal one to the other.

Hyp. 1. If a : c :: b : c, then a = b; For let a be <, or > c, then is (a) 8. 5.  
 $\frac{a}{c} < \frac{b}{c}$  or  $\frac{a}{c} > \frac{b}{c}$ . Which is contrary to the Hyp.

Hyp. 2. If c : b :: c : a; then a = b. For let a be < b, then (b) 8. 5.  
 $\frac{c}{b} < \frac{c}{a}$ . Which is against the Hyp.

Prop. X.

Theorem 10.

16 8 4 Of Magnitudes having Ratio to the same Magnitude,  
a, b, c, that which hath the greater Ratio, is the greater Mag-  
nitude; and that Magnitude to which the same bears  
a greater Ratio, is the lesser Magnitude.

Hyp. 1. If  $\frac{a}{c} < \frac{b}{c}$ , then a < b. For if a = b, then a : c :: b : c. which (a) 7. 5.  
is contrary to the Hyp. If a > b, then is  $\frac{a}{c} > \frac{b}{c}$ . Which is (b) 8. 5.  
also against the Hyp.

M

Hyp. 2.



Hyp. 2. If  $\frac{c}{b} = \frac{c}{a}$ ; then  $b = a$ . For if  $b = a$ , its against the Hyp. (c) 7. 5. for it will follow that  $c : b :: c : a$ . If you say  $b < a$ , then is  $\frac{c}{a} < \frac{c}{b}$  (d) 5. 5. Which is also against the Hyp.

Theorem 11.

Prop. XI.

a, 9. c, 6. c, 12. Ratio's which are one and the same to any third, b, 6. f, 4. d, 8. are also the same one to another.

**T**his Proposition is clear enough from Ax. 1. 1. For if  $\frac{a}{b} = \frac{c}{f} = \frac{c}{d}$   $\frac{a}{b}$  will equal  $\frac{c}{d}$ .

Theorem 12.

Prop. XII.

8 6 12 9  
g. k. h. l. If any numbers of Magnitudes a, b, c, d, be proportional; as one of the antecedents a is to one of the consequents b, so are all the antecedents e, to all the consequents f.

**Pro.** Take the equimultiples of the antecedents g, h, and of the Consequents k, l. Because that as multiplex as one g is of one a, so multiples are g, h, of a, c; and likewise as multiplex as one k is of one b, so multiples are all k, l, of b, d. Moreover because  $a : b :: b : c$ , if  $g = a$ , then will  $b = c$ , and so if  $g < a$ , then will  $b < c$ , in like manner will  $h = b$ , then will  $l = d$ , and so if  $h < b$ , then will  $l < d$ . Wherefore  $a : b :: a : c$ ,  $b : d$ . *WW D.*

Corol.

From hence, if like proportionals be added to like proportionals, the wholes shall be proportional.

Theorem 13.

Prop. XIII.

12 8 6 4 10 12  
g. k. h. l. p. m. If the first a have the same Ratio to the second b, that the third c to the fourth d; and if the third c have a greater proportion to the fourth d, then the fifth e to the sixth f, then also shall the first a have a greater proportion to the second b, than the fifth e to the sixth f.

**T**ake g, h, p, equimultiples of a, c, e, and k, l, m, equimultiples of b, d, f. Now because that  $a : b :: c : d$ , if  $h = b$ , then is  $g = k$ , but because  $\frac{a}{b} < \frac{c}{d}$ , it may be that  $h < b$ , and yet  $p$  not  $= m$ , Therefore  $\frac{a}{b} < \frac{c}{d}$ . *WW D.*

Prop.

Schol.

If  $\frac{c}{d} > \frac{c}{f}$ , then also is  $\frac{a}{b} > \frac{c}{f}$ . Also, if  $\frac{a}{b} < \frac{c}{d} < \frac{c}{f}$ , then is  $\frac{a}{b} < \frac{c}{f}$ . And if  $\frac{a}{b} > \frac{c}{d} > \frac{c}{f}$ , then is  $\frac{a}{b} > \frac{c}{f}$ .

Prop. XIV.

Theorem 14.

If the first a have the same Ratio to the second b, that the third c hath to the fourth d; and if the first a be greater than the third c, then shall the second b be greater than the fourth d. But if the first a be equal to the third c, then the second b shall be equal to the fourth d, but if a be lesser, than is b also lesser.

**L**et  $a < c$ , then  $\frac{a}{b} < \frac{c}{b}$ , but  $\frac{a}{b} = \frac{c}{d}$ ; Therefore  $\frac{c}{d} < \frac{c}{b}$ , Therefore  $b < d$ . By the like way of argument, If  $a > c$ , then is  $b > d$ . But if a be equal to c, then  $c : b :: c : d$ , therefore  $b = d$ . *WW D.*

Prop. XV.

Theorem 15.

c, 25 d, 35 Parts a and b are in the same Ratio, with their like a, 5 b, 7 multiplex c and d, if taken correspondently. ( $c : d :: a : b$ )

**L**et a be part of c, and b of d, c shall contain a so often as d contains b. And because one of the antecedents a is to one consequent b, so are all the antecedents c, to all the consequents d. Therefore  $c : d :: a : b$ . *WW D.*

Prop. XVI.

Theorem 16.

e 16, f 20, If 4 Magnitudes a, b, c, d, be proportional, they a 8, b 10, also shall be alternately proportional. ( $a : c :: b : d$ ) c 4, d 5, g 8, h 10,

**Pro.** Take e and f equimultiples, of a and b, also g and h equimultiples of c and d. Therefore  $e : f :: a : b :: c : d :: g : h$ . Wherefore if  $e = g$ , then likewise is  $f = h$ , therefore  $a : c :: b : d$ . *WW D.*

M 2

Schol.



Schol.

Alternate Ratio has place only then when the quantities are of the same kind. For heterogeneous quantities are not compared together.

Theorem 17.

## Prop. XVII.

*a* 16. *c* 12. *c* 6. *f* 2. If Magnitudes compounded be proportional, they shall also be proportional when divided. That is, if it be  $a : d :: b : f$ , it shall be also  $c : d :: e : f$ .

(a) 4 def. 5. *Pro.*  $A$  and  $b$  are proportionals, therefore of their parts  $d$  and  $f$ , they contain alike number in a like Ratio; therefore if these parts be taken from each of their respective wholes, the remainders  $c$  and  $e$  shall also contain their parts alike numbers of times: therefore it shall be as  $c : d :: e : f$ . *WW D.*

Theorem 18.

## Prop. XVIII.

*a* 16. *c* 12. *c* 6. *f* 2. If Magnitudes divided be proportional, the same also being compounded shall be proportional. That is, if it be  $d : c :: f : e$ , it shall also be  $a : d :: b : f$ .

*Pro.* The parts  $c, e$  contain parts  $d, f$  in a like Ratio; therefore if these be added to them, the wholes  $a, b$ , also shall contain their parts  $d, f$  in a like Ratio. *WW D.*

Theorem 19.

## Prop. XIX.

*a* 16. *d* 4. *f* 2. If the whole  $a$ , be to the whole  $b$ , as the part taken away  $d$ , is to the part taken away  $f$ , then shall the residue  $c$  be to the residue  $e$ , as the whole  $a$  is to the whole  $b$ .

(a) 16. 5. *Pro.* Seeing  $a, b, d, f$  are proportionals; it shall be  $b : f :: a : d$ . Therefore it shall be as  $f : e :: d : c$ , and lastly as  $f : d :: e : c$ , that is as  $a : b :: c : e$ . *WW D.*

Corol.

If like proportionals be subtracted from like proportionals, the residues shall be proportional.

2 Hence is converse Ratio demonstrat.

Let  $a : c :: b : e$ , then  $a : d :: b : f$ . For by permutation  $a : b :: c : e$ ; therefore  $a : b :: d : f$ , whence again by permutation  $a : d :: b : f$ . *WW D.*

Prop.

## Prop. XX.

Theorem 20.

12 9 6 If there be 3 Magnitudes  $a, b, c$ , and others  $d, e, f$ , equal to those in number which being taken two and two in each order are in the same Ratio, and if of equality the first  $a$  be greater than the third  $c$ ; then shall the fourth  $d$  be greater than the sixth  $f$ . But if the first  $a$  be equal to the third  $c$ , then the fourth  $d$  is so to the sixth  $f$ ; and if  $a$  be less than  $c$ , so  $d$  is less than  $f$ .

1. *Hyp.*  $L$  Et  $a < c$ . Because  $a : f :: b : c$  by inversion it shall be  $f : e :: c : b$ . But  $\frac{c}{b} > \frac{a}{b}$ . Therefore  $\frac{f}{e} > \frac{a}{b}$  or  $\frac{d}{c}$  there-fore  $d < f$ . *WW D.*  
2. *Hyp.* By the same way of argument if  $a = c$ , it will appear that  $d = f$ .  
3. *Hyp.* If  $a = c$ . Because  $f : e :: c : b :: a : b :: d : c$ ; there-fore  $d = f$ . *WW D.*

## Prop. XXI.

Theorem 21.

18 12 4 If there be 3 Magnitudes  $a, b, c$ , and others  $d, e, f$ , equal to them in number, which taken two and two are in the same Ratio; and their proportions inordinate ( $a : b :: e : f$ , and  $b : c :: d : e$ ) and if of equality, the first  $a$  be greater than the third  $c$ ; then is the fourth  $d$  greater than the sixth  $f$ ; but if the first be equal to the third, then is the fourth equal to the sixth; if less, so is the other likewise.

1. *Hyp.*  $I$  F  $a < c$ ; then because  $a : e :: b : c$ , therefore inversely  $e : d :: c : b$ , but  $\frac{c}{b} > \frac{a}{b}$ ; therefore  $\frac{e}{d} > \frac{a}{b}$  that is  $\frac{e}{f} > \frac{a}{c}$  therefore  $d < f$ .  
2. *Hyp.* By the like argument if  $a = c$ , then is  $d = f$ .  
3. *Hyp.* If  $a = c$ ; then because  $e : d :: c : b :: a : b :: e : f$ , therefore is  $d = f$ . *WW D.*

Prop.



Theorem 22.

Prop. XXII.

12 9 6. 8 6 4 If there be any number of Magnitudes  
 a. b. c. d. e. f. a, b, c, and others equal to them in num-  
 24 18 12 16 12 8 ber d, e, f, which taken two and two are  
 g. h. k. l. m. n. in the same Ratio, (a . b :: d . e and  
 b . c :: e . f) they shall be in the same  
 Ratio also by equality, (a . c :: d . f.)

Pre. Take g, h, k, equimultiples of a, b, c, and l, m, n, equimulti-  
 plices of d, e, f.

(a) hyp.

(b) 4. 5.

(c) 20. 5.

(d) 6. def. 5.

Pro. Because a . b :: d . e; <sup>b</sup> therefore g . h :: l . m, and in like  
 manner h . k :: m . n, therefore, if g =, =, k, <sup>c</sup> then is l =, =, n,  
<sup>d</sup> therefore a . c :: d . f.

Theorem 23.

Prop. XXIII.

18 12 4 If there be 3 Magnitudes a, b, c, and others d, e, f,  
 a. b. c. equal to them in number, which taken two and two are  
 27 9 6 in the same Ratio and their proportionality inordinate  
 d. c. f. (a . b :: c . f, and b . c :: d . e) they shall be  
 in the same Ratio also by equality, (that is  
 c :: d . f.)

(a) 21. 5.

(b) 15. 5.

(c) 17. def. 5.

(d) 6. def. 5.

Pro. IF a =, =, c; d shall be =, =, f. <sup>b</sup> And the same will  
 hold in their equimultiples. Therefore of <sup>c</sup> equality <sup>d</sup> in the  
 same Ratio that a is to c, shall d be to f, that is, a . c :: d . f.  
 WW D.

Corol.

\* 22 &amp; 23 5.

\* 20. def. 5.

\* Ratio's compounded of the same Ratio's, are amongst themselves  
 the same; also the same parts of the same Ratio's, are among themselves  
 the same.

Prop.

Prop. XXIV.

Theorem 24.

4 2 6 If the first Magnitude a have the same Ratio to the  
 a. b. c. second b, which the third c, hath to the fourth d;  
 3 10 15 and if the fifth e have the same Ratio to the second b,  
 d. c. f. which the sixth f hath to the fourth d, then shall the  
 14 21 first compounded with the fifth (g) have the same Ratio  
 g. h. to the second b, which the third compounded with the  
 sixth (h) hath to the fourth d.

Pro. <sup>a</sup> B is such part of either a or e, as d is of either c or f. <sup>b</sup> There-  
 fore also shall b be such a part of the compound g, as d is of the  
 compound h. WW D.

Prop. XXV.

Theorem 25.

12 4 9 3 If 4 Magnitudes be proportional (a . b :: c . d)  
 a. b. c. d. the greatest a, and the least d, shall be greater than  
 e. 3 f. 1 the remaining two b, c.

Pro. FROM a 12 take e 9, and there will remain e 3. Also from b 4, take  
 d 3, and there will remain f 1. Now because it is a . b :: c . d,  
 it shall also be by division a . b :: e . f. But a = b, therefore also e = f.  
 Therefore (the compound of e + e viz.) a + d = b + f ( = d + f ) + e.  
 WW D.

Prop. XXVI.

Theorem 26.

8 4 5 3 If the first a have a greater proportion to the second b;  
 a. b. c. d. than the third c, to the fourth d; then contrarywise,  
 by conversion, the second shall have a less proportion  
 to the first, than the fourth to the third.

THIS and the other eight propositions remaining, seeing they are  
 not Euclid's, we shall no otherwise demonstrate then by referring  
 to the propositions of Euclid beforegoing in which they are virtually  
 contained.

This Prop. is contained in the 4th, and 10th, of the 5th.

Prop.



Theorem 27.

Prop. XXVII.

8 4 5 3 If the first a have a greater proportion to the second b,  
a. b. c. d. than the third c to the fourth d; then alternately  
the first a shall have a greater proportion to the third  
c, than the second b to the fourth d.

This is contained in the 16th, of the 5th.

Theorem 28.

Prop. XXVIII.

8 4 5 3 If the first a have a greater proportion to the second b,  
a. b. c. d. than the third c to the fourth d, then the first a com-  
pounded with the second b, shall have a greater pro-  
c. 12 f. 8 portion to the second b, than the third c compounded  
with the fourth d, to the fourth d.

This is contained in the 18th Prop. of the 5th.

Theorem 29.

Prop. XXIX.

8 4 5 3 If the first a compounded with the second b, have a  
a. b. c. d. greater proportion to the second b, then the third c  
c. 12 f. 8 compounded with the fourth d hath to the fourth d;  
then by division the first a shall have a greater pro-  
portion to the second b, than the third c to the fourth d.

This is contained in the 17th of the 5th.

Theorem 30.

Prop. XXX.

8 4 5 3 If the first a compounded with the second b, have a  
a. b. c. d. greater proportion to the second b, then the third  
c. 12 f. 8 c compounded with the fourth d hath to the fourth d,  
then by converse Ratio shall the first a compounded  
with the second b have a lesser Ratio to the first a, than the third  
c compounded with the fourth d shall have to the third c.

This is contained in the 19th of the 5th.

Prop.

Prop. XXXI.

Theorem 31.

16 8 4 9 5 3 If there be three Magnitudes a, b, c, and others  
a' b. c. d. e. f. also d, e, f, equal to them in number, and if  
there be a greater proportion of the first of  
the former a to the second b, than there is of the first of the last d  
to their second e, (that is,  $\frac{a}{b} < \frac{d}{e}$ ;) and there be also a greater  
proportion of the second of the first Magnitudes b, to the third c,  
than there is of the second of the last Magnitudes e, to their third f,  
(that is,  $\frac{b}{c} < \frac{e}{f}$ .) Then by equality also shall the Ratio of the  
first of the former Magnitudes a to the third c, be greater than  
the Ratio of the first of the last Magnitudes d, to the third f,  
(that is,  $\frac{a}{c} < \frac{d}{f}$ .)

This is contained in Prop. 20th and 21th.

Prop. XXXII.

Theorem 32.

16 8 5 If there be 3 Magnitudes a, b, c, and others d, e, f,  
a. b. c. equal to them in number and there be a greater pro-  
9 6 4 portion of the first of the former Magnitudes a, to the  
d. e. f. second b, than there is of the second of the latter e, to  
the third f, (that is,  $\frac{a}{b} < \frac{e}{f}$ ;) and also the Ratio of the  
second of the former b, to the third c, be greater than the Ratio of  
the first of the later d, to the second e, (that is,  $\frac{b}{c} < \frac{d}{e}$ ;) then by equa-  
lity also shall the proportion of the first of the former a, to the third  
c, be greater than that of the first of the latter d, to the third f,  
(that is,  $\frac{a}{c} < \frac{d}{e}$ .)

This is contained in the 21th and 23th Prop. of the 5th.

N

Prop.



Theorem 33.

Prop. XXXIII.

12 6

- a. b. If the proportion of the whole  $a$  to the whole  $b$ , be greater  
 4. 3 than the proportion of the part taken away  $c$ , to the part  
 c. d. taken away  $d$ ; then shall also the Ratio of the remainder  
 8. 3  $e$  to that of  $f$ , be greater than that of the whole  $a$  to the  
 e. f. whole  $b$ .

This is contained in the 18th.

Theorem 34.

Prop. XXXIV.

- 12 8 4 6 5 3 If there be any number of Magnitudes  $a, b, c$ ,  
 a. b. c. d. e. f. and others  $d, e, f$ , equal to them in number;  
 and the proportion of the first of the former  
 to the first of the latter, be greater then that of the second to the  
 second, and that greater than the proportion of the third to the  
 third, and so forward; all the former Magnitudes together shall  
 have a greater Ratio to all the latter together, than all the former  
 omitting the first, shall have to all the latter, omitting the first;  
 but less than that of the first of the former to the first of the latter;  
 and lastly greater than that of the last of the former, to the last of the  
 latter.

This being of no use in the following demonstrations, we pass as the  
 other 7 foregoing.

The most notable Prop. of this Book are the 15, 16, 17, 18.

THE



THE  
 SIXTH BOOK  
 OF  
 Euclid's Elements.

DEFINITIONS.

1. **L**ike Right-lined figures are such, whose several  $\angle$ 's are equal one to the other, and also their sides about the equal  $\angle$ 's proportional; as  $ABC, DEF$ . For,  
 The  $\angle B = E$ , and  $AB : BC :: DE : EF$ .  
 Also the  $\angle A = D$ , and  $BA : AC :: ED : DF$ .  
 Lastly, the  $\angle C = F$ , and  $BC : CA :: EF : FD$ .
2. Reciprocal figures are, when in either figure the terms are the antecedents and consequents of Ratio's  
 As the  $\square^s BD, BF$ : for  $AB : BC :: EB : BG$ .
3. A Right-line  $AB$ , is said to be cut according to extreme and mean proportion, when, as the whole  $AB$ , is to the greater segment  $AC$ , so is the greater segment  $AC$ , to the lesser  $CB$ . ( $AB : CA :: CA : CB$ .)
4. The Altitude of any figure, is a perpendicular line  $AC$ , drawn from the top  $A$  to the base  $BD$ .

N 2

c. 24



5. A Ratio, is said to be compounded of two Ratio's, when the quantities of the Ratio's being multiplied the one into the other, do produce any Ratio.

As the Ratio of  $a$  to  $c$ , is compounded of the Ratio's of  $a$  to  $b$  and of  $b$  to  $c$ .

(a) 20. def. 5. For  $\frac{a}{b} \cdot \frac{b}{c} = \frac{a}{c}$ .  
(b) 15. 5.

Theorem 1.

Prop. I.

Triangles  $ABC$ ,  $DEF$ , and Parallelograms  $CG$ ,  $DF$ , which have the same height, are in proportion one to the other, as their bases  $BC$ ,  $EF$ .

(a) 3. 1. \* Take  $BI = BC$ , and  $FL = EF$ , and draw  $AI$ ,  $DL$ .  
(b) 33. 1. The  $\triangle ABC = ABI$ , and also  $DEF = DFL$ . Therefore the  $\triangle AIC$  is as multiplex of the  $\triangle ABC$ , as the base  $IC$  is of the base  $BC$ ; and the  $\triangle DEL$  as multiplex of the  $\triangle DEF$ , as the base  $EL$  is of  $EF$ . But if  $IC = EL$ , then is the  $\triangle AIC = \triangle DEL$ ; and therefore  $BC \cdot EF :: \triangle ABC \cdot DEF :: CG \cdot EF$ .  $WW'D$ .  
(c) 36. 3°. 1.  
(d) 6 def. 5.  
(e) 41. 15. 5.

Schol.

Triangles and  $\square$ 's whose bases are equal, are in such proportion as their altitudes.

Theorem 2.

Prop. II.

If to one side  $CB$  of a  $\triangle ABC$ , be drawn a parallel Right-line  $ED$ , the same shall cut the sides  $(AC, AB)$  of the  $\triangle$  proportionally. And if the sides of the  $\triangle$  be proportionally cut, then a Right-line  $ED$ , joining the points of section, shall be parallel to the remaining side of the  $\triangle CB$ .

(a) 37. 1. Hyp. 1. Because the  $\triangle DEB = DEC$ , therefore shall be the  $\triangle ADE$   
(b) 7. 5.  $\triangle DBE :: ADE \cdot ECD$ . But the  $\triangle ADE \cdot DBE ::$   
(c) 1. 6.  $\triangle AD \cdot DB$ , and the  $\triangle ADE \cdot DEC :: AE \cdot EC$ , therefore  $AD$   
(d) 11. 5.  $\cdot DB :: AE \cdot EC$ .  
(e) 1. 6. Hyp. 2. Because  $AD \cdot DB :: AE \cdot EC$ , that is, as the  $\triangle ADE$ ,  
(f) 9. 5.  $DBE :: ADE \cdot ECD$ ; therefore is the  $\triangle DBE = ECD$ ; therefore  $DE \parallel BC$ .  $WW'D$ .  
(g) 39. 1.

Schol.

If there be drawn many parallels to one side of any  $\triangle$ , then all the segments of the other sides shall be proportional.

Prop.

Prop. III.

Theorem 3.

If an  $\angle A$ , of a  $\triangle ABC$  be bisected, and the Right-line  $AD$ , that bisects the  $\angle$ , cut the base  $BC$  also; then shall the segments of the base  $BD$ ,  $DC$ , have the same Ratio that the other sides of the  $\triangle BA$ ,  $AC$  have, and if the segments of the base  $BD$ ,  $DC$  have the same Ratio, that the other sides of the  $\triangle$  have  $BA$ ,  $AC$ , then a Right-line  $AD$ , drawn from the top  $A$  to the section  $D$ , shall bisect that  $\angle A$  of the  $\triangle$ .

Præ. Produce  $AC$ , and make  $AE = AB$ , and draw  $EB$ .

Hyp. 1. Because  $AE = AB$ , therefore is the  $\angle ABE = E$ .  
(a) 5. 1.  $\frac{1}{2} BAC = DAB$ ; therefore  $DAB = E$ . Wherefore  $CA \cdot AE$   
(b) 32. 1.  $(AB) :: CD \cdot DB$ .  
(c) 4. hyp.  
(d) 27. 1.  
(e) 26. 1.  
(f) 29. 1.  
(g) 1. 4x.  
Hyp. 2. Because  $CA \cdot AB (AE) :: CD \cdot DB$ , is  $DAB \parallel E$ ; and therefore is the  $\angle CAD = E$ ; and the  $\angle DAB = ABE = E$ . Therefore the  $\angle CAD = DAB$ . Wherefore the  $\angle CAB$  is bisected.  $WW'D$ .

Prop. IV.

Theorem 4.

Of equiangular  $\triangle$ 's  $ACB$ ,  $DBE$ , the sides are proportional which are about the equal  $\angle$ 's  $C$  and  $B$  (that is,  $AC \cdot CB :: DB \cdot BE$ .) and the sides  $BA$ ,  $ED$ , which are subtended under the equal  $\angle$ 's  $C$  and  $B$ , are homologous, or of like Ratio.

Præ. Set the side  $CB$ , in a direct line to the side  $BE$ , and produce  $CA$  and  $ED$ , till they meet.  
(a) 32. 1. Pro. Because the  $\angle C = EBD$ , shall  $CF \parallel BD$ . Also because the  
(b) 4. hyp.  $\angle CBA = BED$ , therefore is  $BA \parallel EF$ . Then is  $BAFD$  a  $\square$  and  
(c) 28. 1. therefore  $AF = BD$ , and  $AB = ED$ . Whence it's evident that  
(d) 34. 1.  $CA \cdot AF (BD) :: CB \cdot BE$ , by permutation therefore  $AC \cdot CB$   
(e) 2. 6.  $:: BD \cdot BE$ , also  $CB \cdot BE :: FD (A^E) \cdot DE$ , and thence by  
(f) 16. 5. permutation  $CB \cdot AB :: BE \cdot DE$ , therefore also by equality  $AC$   
(g) 22. 5.  $\cdot AB :: BD \cdot DE$ . Therefore  $Q.E.D.$

Corol.

Hence,  $AC \cdot BD :: CB \cdot BE :: AB \cdot DE$ .

Schol.

If in a  $\triangle FCE$ , there be drawn  $AB \parallel FE$  (one of the sides,) the  $\triangle ACB$  shall be like to the whole  $FCE$ .

Prop.



Theorem 5.

Prop. V.

If two  $\Delta^s$  ABC, DEF have their sides AB, BC, proportional to DE, EF, the  $\Delta^s$  are equiangular, and their  $\angle^s$  (viz. D, A, E, B; F, C) equal, under which are subtended the homologous sides.

**Pro.** Upon the line EF, and at the point E, <sup>a</sup> make the  $\angle FEG = B$ , and at F make the  $\angle EFG = C$ ; <sup>b</sup> whence the  $\angle G = A$ . Therefore  $GE : EF :: AB : BC :: DE : EF$ ; <sup>c</sup> and therefore  $GE = DE$ . Likewise  $GF : FE :: AC : CB :: DF : FE$ ; <sup>c</sup> therefore  $GF = DF$ . Therefore the  $\Delta^s$  DEF, GEF, are mutually equilateral. <sup>d</sup> Therefore the  $\angle D = G = A$ , and the  $\angle FED = FEG = B$ , and <sup>e</sup> consequently the  $\angle DFE = C$ . Therefore  $\Delta^s$  c.

Theorem 6.

Prop. VI.

If two  $\Delta^s$  ABC, DEF, have one  $\angle A$  equal to one  $\angle D$ , and the sides about the equal  $\angle^s$ , A, D, proportional, (BA . AC :: ED . DF) then those  $\Delta^s$  are equiangular, and have those  $\angle^s$  E, B; C, F, equal, under which are subtended the homologous sides BA, ED; AC, DF.

**Pro.** ON the Right-line EF make the  $\angle FEG = B$ , and  $EFG = C$ . **Pro.** <sup>a</sup> Then will the  $\angle G = A$ . Therefore  $AB . AC :: GE . GF :: DE . DF$ , <sup>a</sup> and therefore  $DE = GE$ , and  $DF = GF$ . But the  $\angle D = A = G$ ; therefore the  $\angle DEF = GEF = B$ , and consequently the  $\angle EFD = C$ . *WIV'D.*

Theorem 7.

Prop. VII.

If two  $\Delta^s$  ABC, DEF, have one  $\angle A$ , equal to one  $\angle D$ , and the sides about the other  $\angle^s$  ABC, E, proportional, (AB . BC :: DE . EF) and if they have both the remaining  $\angle^s$  C, F, either less or not less than a Right  $\angle$ ; then shall the  $\Delta^s$  ABC, DEF, be equiangular, and have those  $\angle^s$  equal about which the proportional sides are, viz. ABC, DEF.

**Pro.** Let C and F, be less than  $\angle$ , and let, if it can be, the  $\angle ABC = \angle FED$ , and make the  $\angle ABG = E$ . Then seeing the  $\angle A = D$ , <sup>a</sup> shall the  $\angle AGB = F$ . Therefore  $AB . BG :: DE . EF :: AB . BC$ ; <sup>c</sup> therefore  $BG = BC$ , <sup>d</sup> therefore the  $\angle BGC = BCG$ . <sup>e</sup> Therefore  $BGC = C$  is less than a  $\angle$ , and <sup>f</sup> consequently,  $AGB$  or  $F = \angle$ , which

which is against the Hyp. Again, let B and E be  $\angle$  also, then shall  $BG = BC$ , and <sup>a</sup> consequently the  $\angle BGC = BCG$ , and not less than  $\angle$ , <sup>(b)</sup>  $\angle$  <sup>c</sup> <sup>d</sup> <sup>e</sup> <sup>f</sup> <sup>g</sup> <sup>h</sup> <sup>i</sup> <sup>j</sup> <sup>k</sup> <sup>l</sup> <sup>m</sup> <sup>n</sup> <sup>o</sup> <sup>p</sup> <sup>q</sup> <sup>r</sup> <sup>s</sup> <sup>t</sup> <sup>u</sup> <sup>v</sup> <sup>w</sup> <sup>x</sup> <sup>y</sup> <sup>z</sup> <sup>aa</sup> <sup>ab</sup> <sup>ac</sup> <sup>ad</sup> <sup>ae</sup> <sup>af</sup> <sup>ag</sup> <sup>ah</sup> <sup>ai</sup> <sup>aj</sup> <sup>ak</sup> <sup>al</sup> <sup>am</sup> <sup>an</sup> <sup>ao</sup> <sup>ap</sup> <sup>aq</sup> <sup>ar</sup> <sup>as</sup> <sup>at</sup> <sup>au</sup> <sup>av</sup> <sup>aw</sup> <sup>ax</sup> <sup>ay</sup> <sup>az</sup> <sup>ba</sup> <sup>bb</sup> <sup>bc</sup> <sup>bd</sup> <sup>be</sup> <sup>bf</sup> <sup>bg</sup> <sup>bh</sup> <sup>bi</sup> <sup>bj</sup> <sup>bk</sup> <sup>bl</sup> <sup>bm</sup> <sup>bn</sup> <sup>bo</sup> <sup>bp</sup> <sup>bq</sup> <sup>br</sup> <sup>bs</sup> <sup>bt</sup> <sup>bu</sup> <sup>bv</sup> <sup>bw</sup> <sup>bx</sup> <sup>by</sup> <sup>bz</sup> <sup>ca</sup> <sup>cb</sup> <sup>cc</sup> <sup>cd</sup> <sup>ce</sup> <sup>cf</sup> <sup>cg</sup> <sup>ch</sup> <sup>ci</sup> <sup>cj</sup> <sup>ck</sup> <sup>cl</sup> <sup>cm</sup> <sup>cn</sup> <sup>co</sup> <sup>cp</sup> <sup>cq</sup> <sup>cr</sup> <sup>cs</sup> <sup>ct</sup> <sup>cu</sup> <sup>cv</sup> <sup>cw</sup> <sup>cx</sup> <sup>cy</sup> <sup>cz</sup> <sup>da</sup> <sup>db</sup> <sup>dc</sup> <sup>dd</sup> <sup>de</sup> <sup>df</sup> <sup>dg</sup> <sup>dh</sup> <sup>di</sup> <sup>dj</sup> <sup>dk</sup> <sup>dl</sup> <sup>dm</sup> <sup>dn</sup> <sup>do</sup> <sup>dp</sup> <sup>dq</sup> <sup>dr</sup> <sup>ds</sup> <sup>dt</sup> <sup>du</sup> <sup>dv</sup> <sup>dw</sup> <sup>dx</sup> <sup>dy</sup> <sup>dz</sup> <sup>ea</sup> <sup>eb</sup> <sup>ec</sup> <sup>ed</sup> <sup>ee</sup> <sup>ef</sup> <sup>eg</sup> <sup>eh</sup> <sup>ei</sup> <sup>ej</sup> <sup>ek</sup> <sup>el</sup> <sup>em</sup> <sup>en</sup> <sup>eo</sup> <sup>ep</sup> <sup>eq</sup> <sup>er</sup> <sup>es</sup> <sup>et</sup> <sup>eu</sup> <sup>ev</sup> <sup>ew</sup> <sup>ex</sup> <sup>ey</sup> <sup>ez</sup> <sup>fa</sup> <sup>fb</sup> <sup>fc</sup> <sup>fd</sup> <sup>fe</sup> <sup>ff</sup> <sup>fg</sup> <sup>fh</sup> <sup>fi</sup> <sup>fj</sup> <sup>fk</sup> <sup>fl</sup> <sup>fm</sup> <sup>fn</sup> <sup>fo</sup> <sup>fp</sup> <sup>fq</sup> <sup>fr</sup> <sup>fs</sup> <sup>ft</sup> <sup>fu</sup> <sup>fv</sup> <sup>fw</sup> <sup>fx</sup> <sup>fy</sup> <sup>fz</sup> <sup>ga</sup> <sup>gb</sup> <sup>gc</sup> <sup>gd</sup> <sup>ge</sup> <sup>gf</sup> <sup>gg</sup> <sup>gh</sup> <sup>gi</sup> <sup>gj</sup> <sup>gk</sup> <sup>gl</sup> <sup>gm</sup> <sup>gn</sup> <sup>go</sup> <sup>gp</sup> <sup>gq</sup> <sup>gr</sup> <sup>gs</sup> <sup>gt</sup> <sup>gu</sup> <sup>gv</sup> <sup>gw</sup> <sup>gx</sup> <sup>gy</sup> <sup>gz</sup> <sup>ha</sup> <sup>hb</sup> <sup>hc</sup> <sup>hd</sup> <sup>he</sup> <sup>hf</sup> <sup>hg</sup> <sup>hh</sup> <sup>hi</sup> <sup>hj</sup> <sup>hk</sup> <sup>hl</sup> <sup>hm</sup> <sup>hn</sup> <sup>ho</sup> <sup>hp</sup> <sup>hq</sup> <sup>hr</sup> <sup>hs</sup> <sup>ht</sup> <sup>hu</sup> <sup>hv</sup> <sup>hw</sup> <sup>hx</sup> <sup>hy</sup> <sup>hz</sup> <sup>ia</sup> <sup>ib</sup> <sup>ic</sup> <sup>id</sup> <sup>ie</sup> <sup>if</sup> <sup>ig</sup> <sup>ih</sup> <sup>ii</sup> <sup>ij</sup> <sup>ik</sup> <sup>il</sup> <sup>im</sup> <sup>in</sup> <sup>io</sup> <sup>ip</sup> <sup>iq</sup> <sup>ir</sup> <sup>is</sup> <sup>it</sup> <sup>iu</sup> <sup>iv</sup> <sup>iw</sup> <sup>ix</sup> <sup>iy</sup> <sup>iz</sup> <sup>ja</sup> <sup>jb</sup> <sup>jc</sup> <sup>jd</sup> <sup>je</sup> <sup>jf</sup> <sup>jj</sup> <sup>jh</sup> <sup>ji</sup> <sup>jj</sup> <sup>jk</sup> <sup>jl</sup> <sup>jm</sup> <sup>jn</sup> <sup>jo</sup> <sup>jp</sup> <sup>jq</sup> <sup>jr</sup> <sup>js</sup> <sup>jt</sup> <sup>ju</sup> <sup>jv</sup> <sup>jw</sup> <sup>jx</sup> <sup>ky</sup> <sup>kz</sup> <sup>la</sup> <sup>lb</sup> <sup>lc</sup> <sup>ld</sup> <sup>le</sup> <sup>lf</sup> <sup>lg</sup> <sup>lh</sup> <sup>li</sup> <sup>lj</sup> <sup>lk</sup> <sup>ll</sup> <sup>lm</sup> <sup>ln</sup> <sup>lo</sup> <sup>lp</sup> <sup>lq</sup> <sup>lr</sup> <sup>ls</sup> <sup>lt</sup> <sup>lu</sup> <sup>lv</sup> <sup>lw</sup> <sup>lx</sup> <sup>ly</sup> <sup>lz</sup> <sup>ma</sup> <sup>mb</sup> <sup>mc</sup> <sup>md</sup> <sup>me</sup> <sup>mf</sup> <sup>mg</sup> <sup>mh</sup> <sup>mi</sup> <sup>mj</sup> <sup>mk</sup> <sup>ml</sup> <sup>mm</sup> <sup>mn</sup> <sup>mo</sup> <sup>mp</sup> <sup>mq</sup> <sup>mr</sup> <sup>ms</sup> <sup>mt</sup> <sup>mu</sup> <sup>mv</sup> <sup>mw</sup> <sup>mx</sup> <sup>my</sup> <sup>mz</sup> <sup>na</sup> <sup>nb</sup> <sup>nc</sup> <sup>nd</sup> <sup>ne</sup> <sup>nf</sup> <sup>ng</sup> <sup>nh</sup> <sup>ni</sup> <sup>nj</sup> <sup>nk</sup> <sup>nl</sup> <sup>nm</sup> <sup>nn</sup> <sup>no</sup> <sup>np</sup> <sup>nq</sup> <sup>nr</sup> <sup>ns</sup> <sup>nt</sup> <sup>nu</sup> <sup>nv</sup> <sup>nw</sup> <sup>nx</sup> <sup>ny</sup> <sup>nz</sup> <sup>oa</sup> <sup>ob</sup> <sup>oc</sup> <sup>od</sup> <sup>oe</sup> <sup>of</sup> <sup>og</sup> <sup>oh</sup> <sup>oi</sup> <sup>oj</sup> <sup>ok</sup> <sup>ol</sup> <sup>om</sup> <sup>on</sup> <sup>oo</sup> <sup>op</sup> <sup>oq</sup> <sup>or</sup> <sup>os</sup> <sup>ot</sup> <sup>ou</sup> <sup>ov</sup> <sup>ow</sup> <sup>ox</sup> <sup>oy</sup> <sup>oz</sup> <sup>pa</sup> <sup>pb</sup> <sup>pc</sup> <sup>pd</sup> <sup>pe</sup> <sup>pf</sup> <sup>pg</sup> <sup>ph</sup> <sup>pi</sup> <sup>pj</sup> <sup>pk</sup> <sup>pl</sup> <sup>pm</sup> <sup>pn</sup> <sup>po</sup> <sup>pp</sup> <sup>pq</sup> <sup>pr</sup> <sup>ps</sup> <sup>pt</sup> <sup>pu</sup> <sup>pv</sup> <sup>pw</sup> <sup>px</sup> <sup>py</sup> <sup>pz</sup> <sup>qa</sup> 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<sup>su</sup> <sup>sv</sup> <sup>sw</sup> <sup>sx</sup> <sup>sy</sup> <sup>sz</sup> <sup>ta</sup> <sup>tb</sup> <sup>tc</sup> <sup>td</sup> <sup>te</sup> <sup>tf</sup> <sup>tg</sup> <sup>th</sup> <sup>ti</sup> <sup>tj</sup> <sup>tk</sup> <sup>tl</sup> <sup>tm</sup> <sup>tn</sup> <sup>to</sup> <sup>tp</sup>  <sup>tq</sup> <sup>tr</sup> <sup>ts</sup> <sup>tu</sup> <sup>tv</sup> <sup>tw</sup> <sup>tx</sup> <sup>ty</sup> <sup>tz</sup> <sup>ua</sup> <sup>ub</sup> <sup>uc</sup> <sup>ud</sup> <sup>ue</sup> <sup>uf</sup> <sup>ug</sup> <sup>uh</sup> <sup>ui</sup> <sup>uj</sup> <sup>uk</sup> <sup>ul</sup> <sup>um</sup> <sup>un</sup> <sup>uo</sup> <sup>up</sup> <sup>uq</sup> <sup>ur</sup> <sup>us</sup> <sup>ut</sup> <sup>uu</sup> <sup>uv</sup> <sup>uw</sup> <sup>ux</sup> <sup>uy</sup> <sup>uz</sup> <sup>va</sup> <sup>vb</sup> <sup>vc</sup> <sup>vd</sup> <sup>ve</sup> <sup>vf</sup> <sup>vg</sup> <sup>vh</sup> <sup>vi</sup> <sup>vj</sup> <sup>vk</sup> <sup>vl</sup> <sup>vm</sup> <sup>vn</sup> 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<sup>ca</sup> <sup>cb</sup> <sup>cc</sup> <sup>cd</sup> <sup>ce</sup> <sup>cf</sup> <sup>cg</sup> <sup>ch</sup> <sup>ci</sup> <sup>cj</sup> <sup>ck</sup> <sup>cl</sup> <sup>cm</sup> <sup>cn</sup> <sup>co</sup> <sup>cp</sup> <sup>cq</sup> <sup>cr</sup> <sup>cs</sup> <sup>ct</sup> <sup>cu</sup> <sup>cv</sup> <sup>cw</sup> <sup>cx</sup> <sup>cy</sup> <sup>cz</sup> <sup>da</sup> <sup>db</sup> <sup>dc</sup> <sup>dd</sup> <sup>de</sup> <sup>df</sup> <sup>dg</sup> <sup>dh</sup> <sup>di</sup> <sup>dj</sup> <sup>dk</sup> <sup>dl</sup> <sup>dm</sup> <sup>dn</sup> <sup>do</sup> <sup>dp</sup> <sup>dq</sup> <sup>dr</sup> <sup>ds</sup> <sup>dt</sup> <sup>du</sup> <sup>dv</sup> <sup>dw</sup> <sup>dx</sup> <sup>dy</sup> <sup>dz</sup> <sup>ea</sup> <sup>eb</sup> <sup>ec</sup> <sup>ed</sup> <sup>ee</sup> <sup>ef</sup> <sup>eg</sup> <sup>eh</sup> <sup>ei</sup> <sup>ej</sup> <sup>ek</sup> <sup>el</sup> <sup>em</sup> <sup>en</sup> <sup>eo</sup> <sup>ep</sup> <sup>eq</sup> <sup>er</sup> <sup>es</sup> 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<sup>we</sup> <sup>wf</sup> <sup>wg</sup> <sup>wh</sup> <sup>wi</sup> <sup>wj</sup> <sup>wk</sup> <sup>wl</sup> <sup>wm</sup> <sup>wn</sup> <sup>wo</sup> <sup>wp</sup> <sup>wq</sup> <sup>wr</sup> <sup>ws</sup> <sup>wt</sup> <sup>wu</sup> <sup>wv</sup> <sup>ww</sup> <sup>wx</sup> <sup>wy</sup> <sup>wz</sup> <sup>xa</sup> <sup>xb</sup> <sup>xc</sup> <sup>xd</sup> <sup>xe</sup> <sup>xf</sup> <sup>yg</sup> <sup>yh</sup> <sup>yi</sup> <sup>yj</sup> <sup>yk</sup> <sup>yl</sup> <sup>ym</sup> <sup>yn</sup> <sup>yo</sup> <sup>yp</sup> <sup>yq</sup> <sup>yr</sup> <sup>ys</sup> <sup>yt</sup> <sup>yu</sup> <sup>yv</sup> <sup>yw</sup> <sup>yx</sup> <sup>yy</sup> <sup>yz</sup> <sup>za</sup> <sup>zb</sup> <sup>zc</sup> <sup>zd</sup> <sup>ze</sup> <sup>zf</sup> <sup>zg</sup> <sup>zh</sup> <sup>zi</sup> <sup>zj</sup> <sup>zk</sup> <sup>zl</sup> <sup>zm</sup> <sup>zn</sup> <sup>zo</sup> <sup>zp</sup> <sup>zq</sup> <sup>zr</sup> <sup>zs</sup> <sup>zt</sup> <sup>zu</sup> <sup>zv</sup> <sup>zw</sup> <sup>zx</sup> <sup>zy</sup> <sup>zz</sup>



- (a) 31. 1.  
(b) 2. 6.  
(c) 34. 1 & 7-5.

*Pro.* For let  $DH$  be drawn <sup>a</sup>parallel to  $AB$ . Then  $AD \cdot DE ::$   
<sup>b</sup> $AF \cdot FG$ , and  $DE \cdot EC :: DI \cdot IH ::$  <sup>c</sup> $EG \cdot GB$ . *WW'D n.*

*Schol.*

Hence is learnt with any extent of the compasses, to cut a Right-line given into as many equal parts as you please. As admit, I would divide the Right-line  $AG$  into 6 equal parts. Draw an infinite line  $AR$ , and another  $GH$ , parallel thereto; then take any extent in the Compasses, and lay it off 5 times from  $A$  to  $N, O, P, Q, R$ ; and also 5 times from  $G$ , viz. to  $M, L, K, I, H$ ; (always one less than are required in  $AG$ ;) and draw  $HN, IO, KP, LQ, MR$ ; these lines so drawn shall cut the Right-line given  $AG$  into 6 parts, as required.

Problem 3.

Prop. XI.

Two Right-lines  $AB, BC$ , being given, to find a third proportional.

*Pro.* **V**ith the two given lines make the Right-angle  $ABC$ , also another Right-angle  $ACD$ , by raising  $CD \perp AC$ , and extending it till it meet  $AB$  protracted in  $D$ . Then it's evident by cor. 8. 6. that  $BC$  is a mean proportional, and consequently,  $AB \cdot BC :: BC \cdot BD$ . *WW'D n.*

Problem 4.

Prop. XII.

Three Right-lines  $AB, BC, AD$ , being given, to find a fourth proportional  $DE$ .

*Pro.* **O**f the lines  $AB, BC$  (placed in a direct line) and  $AD$ , make an  $\angle DAC$ , and join  $BD$ , and lastly, draw  $CE \parallel BD$ , so shall  $DE$  be a fourth proportional required.

- (a) 2. 6.

*Pro.* For  $CE \parallel BD$ : <sup>a</sup>therefore  $AB \cdot BC :: AD \cdot DE$ . *WW'D n.*

Problem 5.

Prop. XIII.

Two Right lines  $AB, BC$ , being given, to find a mean proportional  $BD$ .

*Pro.* **P**lace  $AB, BC$ , in a direct line, and on the whole line  $AC$ , describe the semicircle  $ADC$ . On  $B$  raise the perpendicular  $BD$ , meeting with the periphery in  $D$ , so is  $BD$  the mean required.

- (a) 31. 3.  
(b) cor. 8. 6.

*Pro.* For letting  $AD, CD$ , be drawn, seeing from the <sup>a</sup> $\angle L$  of the Right-angled  $\triangle ADC$ , is drawn the perpendicular  $DB$ , <sup>b</sup>therefore  $AB \cdot BC :: BD \cdot BD$ . *WW'D n.*

*Corol.*

*Corol.*

A Right-line drawn from any point in the Circumference of a Circle Perpendicular to the diameter, is a mean proportional between the segments of the diameter.

Prop. XIV.

Theorem 9.

Equal  $\square$ 's  $BD, BF$ , having one  $\angle ABC$ , equal to one  $EBG$ , have the sides  $AB, BG, EB, BC$ ; which are about the equal  $\angle$ 's reciprocal: And these  $\square$ 's which have one  $\angle$  equal to one  $\angle$ , and the sides which are about the equal  $\angle$ 's reciprocal, are equal.

*Pro.* **L**et the sides  $AB, BG$ , about the equal  $\angle$ 's make one Right-line; <sup>(a) 15. 1.</sup> wherefore  $EB, BC$ , shall do the same. Let  $FG, DC$ , be produced till they meet. <sup>(b) 1. 6.</sup>  
<sup>(c) 7. 5.</sup> Hyp. 1.  $AB \cdot BG :: BD \cdot BH ::$  <sup>(d) 1. 6.</sup>  $BF \cdot BH ::$  <sup>(e) 11. 5.</sup>  $BE \cdot BC$ . <sup>(f) 1. 6.</sup>  
<sup>(g) hyp.</sup> Therefore  $\square$ 's. <sup>(h) 1. 6.</sup>  
Hyp. 2.  $BD \cdot BH ::$  <sup>(i) 1. 6.</sup>  $AB \cdot BG ::$  <sup>(j) 11. 5.</sup>  $BE \cdot BC ::$  <sup>(k) 11. 2 & 9-5.</sup>  $BF \cdot BH$ .  
<sup>\*</sup> Therefore the  $\square BD = BF$ . *WW'D.*

Prop. XV.

Theorem 10.

Equal  $\triangle$ 's  $ABC, DBE$ , having one  $\angle ABC$ , equal to one  $\angle DBE$ , their sides which are about the equal  $\angle$ 's are reciprocal ( $AB \cdot BE :: DB \cdot BC$ ) and these  $\triangle$ 's which have one  $\angle ABC$  equal to one  $\angle DBE$ , and have also the sides that are about the equal  $\angle$ 's reciprocal, are equal.

*Pro.* **L**et the sides  $CB, BD$ , which are about the equal  $\angle$ 's be set in a straight-line; <sup>(a) 15. 1.</sup> then  $ABE$  is also a Right-line. Let  $CE$  be drawn. <sup>(b) 1. 6.</sup>  
Hyp. 1.  $AB \cdot BE ::$  <sup>(c) 7. 5.</sup>  $\triangle ABC \cdot CBE ::$  <sup>(d) 11. 5.</sup>  $\triangle DBE \cdot CBE ::$  <sup>(e) hyp.</sup>  $DB \cdot BC ::$  <sup>(f) 11. 2 & 9-5.</sup>  $DBE$ .  
Hyp. 2.  $\triangle ABC \cdot CBE ::$  <sup>(g) 11. 5.</sup>  $AB \cdot BE ::$  <sup>(h) 11. 5.</sup>  $DB \cdot BC ::$  <sup>(i) 11. 2 & 9-5.</sup>  $DBE$ .  
<sup>\*</sup> Therefore the  $\triangle ABC = DBE$ . *WW'D.*

O

Prop.



Theorem 11.

Prop. XVI.

If 4 Right-lines A, G, F, B, be proportional, the Rectangle AC, comprehended under the extremes AB, BC, is equal to the Rectangle FG, comprehended under the means EF, FG. And if the Rectangle AC, comprehended under the extremes AB, BC, be equal to the Rectangle FG, comprehended under the means FE, EG, then are these 4 Right-lines proportional.

(a) 10 ax. 1. Hyp. 1. The  $\angle^s$  B and E are right, and  $\therefore$  consequently equal, and by hypothesis AB . EG :: FE . CB.  $\therefore$  therefore the  $\square$

(b) 14. 6. AC = FG.

(c) hyp.

(d) 14. 5.

Hyp. 2. The  $\square$  AC = FG, and the  $\angle$  B = E;  $\therefore$  therefore AB . EG :: EF . CR. WW'D.

Cor. I.

Hence, it's easie to reduce one Rectangle into another of a given length or breadth.

Proposition 12.

Prop. XVII.

If 3 Right-lines A, F, B, be proportional, the Rectangle AC, comprehended under the extremes AB, BC, is equal to the Square EG, made of the mean F. And if the Rectangle AC, comprehended under the extremes AB, BC, be equal to the Square EG, made of the mean F, then the three lines are proportional. Take GF = FE.

(a) exp.

(b) 10. 6.

(c) 25. 4. 1.

(d) hyp.

(e) 14. 5.

Hyp. 1. A B . FE ::  $\therefore$  FE (GF) . CB; therefore the  $\square$  AC = GE

Hyp. 2. The  $\square$  AC =  $\square$  EG = FE q.  $\therefore$  Therefore AB . FE :: FG (EF) . BC. WW'D.

Corol.

Let  $a \times b = c^2$ , then  $a . c :: c . b$ .

Problem 6.

Prop. XVIII.

Upon a Right-line given AB, to describe a Right-lined figure CD EFG, like and a like situate to a Right-lined figure given ABHIK.

(a) 23. 1.

Resolve the Right-lined figure given into  $\Delta^s$ , by drawing CF, DF.  $\therefore$  Make the  $\angle$  IAB = FCD,  $\therefore$  and the  $\angle$  IBA = FDC,  $\therefore$  and the  $\angle$  IBH = FDE, and BIH = DFE, also IAK = FCG, and AIK = CFG. Then shall ABHIK be the Right-lined figure sought. Pro.

Pro. For seeing the  $\angle$  IAB = FCD, and IBA = FDC; shall the  $\angle$  AIB = CFD, and because IBH = FDE, and BIH = DFE, shall BHI = DEF; also because IAK = FCG, and AIK = CFG, shall AKI = CGF. And because IAB = FCD, and IAK = FCG, shall the whole BAK = DCG; and because ABI = FCD, and IBH = FDE, shall ABH = CDE; and lastly, because HIB = EFD, and BIA = DFC, and AIK = CFG, shall HIK = EFG. The Polygons therefore are mutually equiangular. And because the  $\Delta^s$  are equiangular, therefore AB . BH :: CD . DE; and BA . KI :: GC . GF, &c.  $\therefore$  whence by equality KA . AB :: GC . CD, &c.  $\therefore$  therefore also like situate. WW'D.

Prop. XIX.

Theorem 13.

Like  $\Delta^s$  ABC, DEF, are in duplicate Ratio of their homologous sides.

If the  $\Delta^s$  be equal it's evident without farther demonstration. But when unequal, its thus, demonstrated.

Make BC . EF :: EF . BG, and let AG be drawn. Then because AB . DE :: BC . EF :: EF . BG, and the  $\angle$  B = E,  $\therefore$  therefore is the  $\Delta$  ABG = DEF. But the  $\Delta$  ABC . ABG :: BC . BG, and  $\frac{BC}{ABG} = \frac{BC^2}{EF^2}$ ; therefore  $\frac{ABC}{ABG}$  that is  $\frac{ABC}{DEF} = \frac{BC^2}{EF^2}$  that is in a duplicate Ratio. WW'D.

Corol.

If three Right-lines a, b, c, be proportional, then as the first is to the third, so is a  $\Delta$  made upon the first a, to a  $\Delta$  like and a like described upon the second b: or so is a  $\Delta$  described upon the second b, to a  $\Delta$  like and a like described on the third c.

Prop. XX.

Theorem 14.

Like Polygons are divided into equal  $\Delta^s$ , both equal in number and homologous to the wholes: and the Polygons have a double Ratio one to the other, of what one homologous side hath to the other homologous side.

Pro. 1. The  $\angle$  K = G, and KI . KA :: FG . GC;  $\therefore$  therefore the  $\Delta^s$  IKA, and FGC are equiangular. After the same manner are the  $\Delta^s$  IHB, FED, like. Therefore seeing the  $\angle$  KAI = GCF,  $\therefore$



(c) *Hyp.*  
 (d) 3 *ax. 1.*  
 (e) 32. 1.  
 (f) 19. 6.

and the  $\triangle IBH^b = FDE$ , and the whole  $\angle KAB = \angle GCD$ , and  $ABH^c = CDE$ , the remaining  $\angle IAB^d = FCD$ , and  $IBA = FDC$ ; and consequently  $AIB^e = CFD$ . Therefore the  $\triangle AIB, CFD$  are like, therefore  $\angle c$ .

2. Because the  $\triangle KAI, GCF$  are like, <sup>f</sup> therefore is  $\frac{KAI}{GCF} = \frac{KA^2}{GC^2}$ .

For the same reason is  $\frac{AIB}{CFD} = \frac{AB^2}{CD^2}$ ; lastly  $\frac{RHI}{DEF} = \frac{BH^2}{DE^2}$ . Now because that

(g) *Hyp.* 16. 5.  
 (h) *Schol.* 23. 5.  
 (i) 12. 5.

$KA \cdot GC^2 :: AB \cdot CD^2 :: BH \cdot DE^2$ ; <sup>h</sup> therefore is the  $\triangle KAI \cdot GCF :: ABI \cdot CFD :: BHI \cdot DEF$  <sup>i</sup>: the Polygon  $KABHI \cdot GCDEF :: KA^2$ .

*Corol.*

1. If 3 Right-lines be proportional; then as the first is to the third, so is a Polygon made upon the first, to a Polygon made upon the second, like and a like described, or so is a Polygon described upon the second to a Polygon made on the third, like and a like described.

By which is discovered a method of enlarging or diminishing, any Right-lined figure in a Ratio given: As if you would make a pentagone quintuple of that pentagone whereof  $AB$  is the side, then betwixt  $AB$ , and  $\frac{5}{2} AB$ , find a mean proportion, <sup>\*</sup> upon which make a pentagone like that given, and it shall be quintuple of the pentagone given.

2. If the homologous sides of like figures be known, then will the proportion of the figures be evident, *viz.* by finding a third proportional.

### Prop. XXI.

Theorem 15.

*Right-lined figures ABC, DEF, which are like to the same Right-lined figures GHI, are also like one to the other.*

(a) 1 *def.* 6. *Pro.* For the  $\angle A^2 = G^2 = D$ ; and the  $\angle C^2 = I^2 = F$ ; and the  $\angle B^2 = H^2 = E$ . Also  $BA \cdot BC :: GH \cdot HI :: DE \cdot EF$ , and  $BC \cdot CA :: HI \cdot IG :: EF \cdot FD$ , and  $BA \cdot AC :: HG \cdot GI :: ED \cdot DF$ . Therefore  $\triangle ABC, DEF$ , are like. *IVWD.*

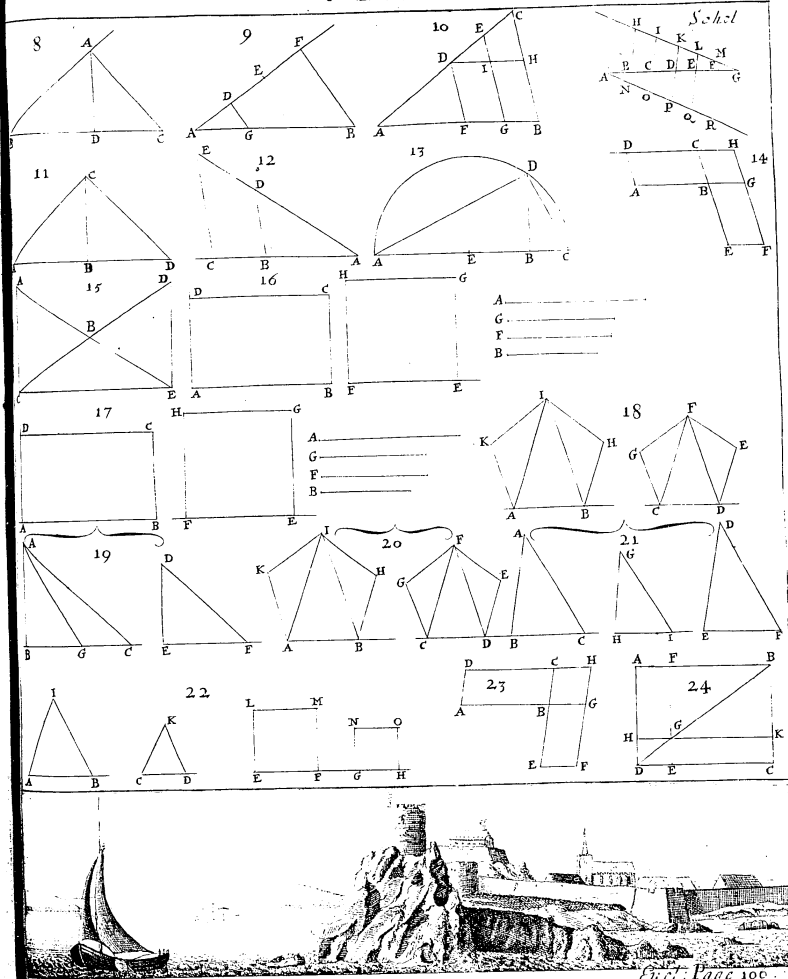
### Prop. XXII.

Theorem 16.

If 4 Right-lines  $AB, CD, EF, GH$ , be proportional: the Right-lined figures also  $ABI, CDK, EM$ , and  $NH$ , described upon them being like and alike situate, shall be proportional. And if the Right-lined figures described upon the lines, like and a like situate, be proportional, then the Right-lines also shall be proportional.

(a) 15. 6.  $H^{yp. 1.} \frac{AIB}{CDK} = \frac{AB^2}{CD^2} = \frac{EF^2}{GH^2} = \frac{EM}{GO}$ . <sup>b</sup> Therefore  $ABI, CDK :: EM, GO$ .

*Hyp. 2.*



*Geol. Page 100.*



Hyp. 2.  $\frac{AB^2}{CD} = \frac{ABI}{CDK} = \frac{EM}{GO} = \frac{EF^2}{GH}$ . Therefore  $AB \cdot CD :: EF$  <sup>(b) hyp.</sup> <sup>(c) 20. 6.</sup>  
 $GH$ .  $WW'D$ .

Prop. XXIII.

Theorem 17.

Equiangular  $\square$ s  $AC$ ,  $BF$ , have the Ratio one to the other, which is compounded of their sides  $AB$ , to  $BG$ , and  $EB$ , to  $EC$ .

Pre. **L** Et the sides about the equal  $\angle$ s  $B$ , be <sup>a</sup> set in a direct line, and let the  $\square$   $BH$ , be completed.

Pro. Then is the Ratio of  $AC$ , to  $BF$ , equal to the Ratio of <sup>a</sup>  $AC$ , to <sup>(a) sch. 15. 1</sup>  $BH$ , together with that of  $BH$ , to  $BF$ , as also to the Ratio of <sup>c</sup>  $AB$ , to <sup>(b) 20. def. 5.</sup>  $BH$ , <sup>(c) 1. 6.</sup> together with the Ratio of  $CB$ , to  $BE$ . That is,  $\frac{AC}{BF} = \frac{AC}{BH} + \frac{BH}{BF}$

$$= \frac{AB}{BG} + \frac{BC}{BE} \quad WW'D.$$

Corol.

1. Hence, and from 34. 1. Triangles which have one  $\angle$  equal, have a Ratio compounded of the Ratio's of the Right-lines containing the equal  $\angle$ .
2. All  $\square$ s and  $\square$ s have their Ratio one to the other, compounded of the Ratio's of base to base, and altitude to altitude. And after the same manner in  $\triangle$ s.

Prop. XXIV.

Theorem 18.

In every  $\square$   $AC$ , the  $\square$ s  $FK$ ,  $HE$ , which are about the diameter  $DE$ , are like to the whole, and also one to the other.

Pro. **S**eeing the  $\square$ s  $HE$ ,  $FK$ , have each of them one  $\angle$  common with the whole; <sup>a</sup> therefore they are equiangular to the whole, and also one <sup>(a) 29. 1.</sup> to the other.

Also both the  $\triangle$ s  $BAD$ ,  $GHD$ ,  $BFG$ , <sup>a</sup> and the  $\triangle$ s  $BCD$ ,  $GED$ ,  $BKG$ , are mutually equiangular; <sup>b</sup> therefore the sides are proportional, <sup>(b) 4. 6.</sup> and <sup>c</sup> consequently constitute  $\square$ s like to the whole, and also one to the other. <sup>(c) 1. def. 6.</sup>  
 $WW'D$ .

Prop. XXV.

Problem 7.

To a Right-lined figure given  $A$ , to describe another figure  $L$  like and alike situate, which also shall be equal to another Right-lined figure given  $B$ .

Pro. **O**N the side of the given figure  $AD$ , <sup>a</sup> make the Rect-angle  $CE = A$ ; <sup>(a) 45. 1.</sup> <sup>(b) 44. 1.</sup> Also upon  $DE$ , make the  $\square$   $DK = B$ ; Between  $C$ , and  $DG$ , <sup>(c) 13. 6.</sup> find a mean proportion  $DH = IN$ ; <sup>d</sup> upon  $IN$  make the figure  $L$ , like and in a like position to the Right-lined figure given  $A$ , then shall the Right-lined figure  $L = B$ , and be like the figure  $A$ .  $WW'D$ . <sup>(d) 18. 6.</sup> <sup>(e) cor. 20. 6.</sup> <sup>(f) 1. 6.</sup>

Pro. For  $A(CE) \cdot L :: CD \cdot DG :: CE \cdot DK$ . Therefore  $L = DK = B$ . <sup>(g) 14. 5.</sup> <sup>(h) const.</sup>  
 $WW'D$ . Prop.



Theorem 19.

Prop. XXVI.

If from a Parallelogram  $BD$ , be taken away another  $FG$ , like unto the whole, and in like manner set, having also an  $\angle FBG$ , common with it, then is that  $\square$  about the same diagonal  $BD$ , with the whole.

- (a) 24. 6.  
(b) 1 def. 6.  
(c) hyp.  
(d) 9. 5.  
(f) 9 ax.

If you deny  $BD$ , to be the common diagonal, let  $BHD$  be it, cutting  $G$  in  $H$ , and draw  $HE \parallel BG$ . Then are the  $\square^s GE, AC$ , like; <sup>b</sup> therefore  $BG \cdot GH :: BA \cdot AD :: GB \cdot IG$ , and <sup>d</sup> consequently  $GH = GI$ . <sup>e</sup> Which is absurd.

Theorem 20.

Prop. XXVII.

Of all  $\square^s AD, AG$ , applied to the same Right-line  $AB$ , and wanting in figure by  $\square^s CE, KI$  like and alike situate to the  $\square AD$ , described upon half  $AC$ , the greatest is that  $AD$ , which is applied to the half, being like to the defect  $KI$ . That is, let there be described on  $AC$ , the half of the line  $AB$ , a  $\square AD$ , so that it may want of the whole  $AE$ , a  $\square CE$ , equal and like to  $AD$ . Also to any other segment  $AK$ , let there be applied another  $\square AG$ , wanting so much as the  $\square KI$ , like to  $CE$ , that is standing about the diameter  $BGD$ . I say  $AG \supset AD$ .

- (a) 43. 1.  
(b) 2 ax.  
(c) 36. 1.  
(d) 2 ax.  
(e) 9 ax.

*Pro.* Because  $GE = GC$ , and  $KI$  added common, <sup>b</sup> thence is  $KE = CI$ . <sup>c</sup>  $CI = AM$ . add  $CG$  common, <sup>d</sup> then is  $AG =$  the Gnomon  $MBL$ . But the Gnomon  $MBL \supset CE (AD)$ . Therefore  $AG \supset AD$ . *WVD.*

Problem 3.

Prop. XXVIII.

Upon a Right-line given  $AB$ , to apply a  $\square AI$ , equal to a Right-lined figure given  $C$ , deficient by a  $\square ON$ , which is like to another  $\square$  given  $D$ . <sup>a</sup> But it's requisite that the Right-lined figure given  $C$ , whereunto the  $\square$  to be applied  $AI$ , must be equal, be not greater then the  $\square AF$ , which is upon the half-line. seeing the defects must be like, namely the defect of the  $\square AF$ , which is applied to the half-line, and the defect of the  $\square D$ , to be applied, whose defect is to be like to the  $\square$  given.

- (a) 18. 6.  
(b) sch. 45. 1.  
(c) 25. 6.

*Pro.* Bisect  $AB$  in  $E$ ; upon  $EB$ , <sup>a</sup> make the  $\square EG$ , like to the  $\square D$ ; and compleat the  $\square BH$ , and <sup>b</sup> let  $EG = C - P$ . <sup>c</sup> Make the  $\square QR = P$ , and like to the  $\square$  given  $D$ , or  $EG$ , draw the diameter  $FB$ ; make  $KF = PQ$ , and  $FL = PR$ ; through  $I$  and  $L$ , draw the parallels  $MN, LO$ . Then is the  $\square AI$ , that which was sought. *Pro.*

*Pro.* The  $\square^s D, EG, KL, QR, ON$ , are all <sup>d</sup> like one to the other, and the  $\square EG = \square QR - C = \square KL + C$ . <sup>e</sup> Wherefore  $C =$  the Gnomon  $KBL = AK + IG = AK + EI = AI$ . *WVD.*

- (d) *confr.* 24. 6.  
(e) *confr.* (f) 3 ax.  
(g) 2 ax.  
(h) 43. 1.

Prop. XXIX.

Problem 9.

Upon a Right-line given  $AB$ , to apply a  $\square$  equal to a Right-lined figure given  $C$ , exceeding by a  $\square PO$ , which shall be like to another  $\square$  given  $D$ .

*Pro.* Bisect  $AB$ , in  $E$ . Upon  $EB$ , <sup>a</sup> make an  $\square EC$ , like to  $D$  given. And <sup>b</sup> make the  $\square IK = EC - C$ , and like to  $D$  given, or  $EC$ . Make  $FEN = HI$ ; and  $FCM = KH$ . Through  $N$  and  $M$ , draw the  $\square^s MR, QR$ , and  $AMR$ , produce  $ABO, CBP$ . Draw the diameter  $FB$ . Then is  $AR$ , the  $\square$  required.

The  $\square^s D, IK, NM, EC$ , are <sup>d</sup> like; <sup>e</sup> therefore the  $\square PO$ , is like to the  $\square NM$ , or  $D$ . Also  $NM = IK = EC - C$ ; <sup>f</sup> therefore  $C =$  the Gnomon  $ERC$ . But  $AN = NB = BM$ ; <sup>g</sup> therefore  $C = AR$ . *WVD.*

Prop. XXX.

Problem 10.

To cut a terminate Right-line given  $AB$ , into  $G$ , according to extreme and mean Ratio. That is,  $AB \cdot AG :: AG \cdot GB$ .

*Pro.* Cut  $AB$ , in  $G$ , in such wise that  $AB \times BG = AG^2$ . <sup>a</sup> Then  $BA \cdot AG :: AG \cdot BG$ . *WVD.*

- (a) 11. 2.  
(b) 17. 2.

Prop. XXXI.

Theorem 21.

In a Right-angled  $\triangle BAC$ , any figure  $BD$ , described upon the side  $BC$ , subtending the Right-angle  $BAC$ , is equal to the figures  $BG, AI$ , described upon the sides  $BA, AC$ , containing the Right  $\angle$ , like and alike situate to the former  $BD$ .

*Pro.* The figures  $FA, AI, BD$ , are <sup>a</sup> like, <sup>b</sup> therefore in a duplicate Ratio of their sides. Also the Squares described on these sides or lines  $BA, AC, BC$ , are in a duplicate Ratio of their sides. Therefore seeing  $BAq - ACq = BCq$ , shall the figures  $FA - AI = BD$ . *WVD.*

Corol.

Hence, may be learned how to add or subtract any like figures, viz. by using the same method that was followed in adding and subtracting Squares. *Prop.*

Sch. 47. 1.



Theorem 21.

Prop. XXXII.

If 2  $\Delta^s$  ABC, DCE, having two sides AB, AC, proportional to two sides DC, DE, be so compounded or set together at one  $\angle$  ACD, that their homologous sides AB, DC; AC, DE, be parallel, then the remaining sides BC, CE, of these  $\Delta^s$  shall be found placed in one strait line.

- (A) 29. 1.  
(b) hyp.  
(c) 6. 6.  
(d) 2. ax.  
(e) 32. 1.  
(f) 1. ax.  
(g) 14. 1.

Pro. **T**he  $\angle A^s = ACD^s = D$ . And  $AB : AC :: DC : DE$ ,  
therefore the  $\angle B = DCE$ . Therefore the  $\angle B + A^s = ACE$ .  
But the  $\angle B + A + ACB^s = 2 \angle^s$ . Therefore the  $\angle ACE + ACB^s = 2 \angle^s$ ; therefore BCE, is a Right-line. *WW D.*

Theorem 22.

Prop. XXXIII.

In equal Circles ABCE, EFGL, the  $\angle^s$  A, E, D, H, have the same Ratio with their peripheries BC, FG, on which they insift, whether the  $\angle^s$  be at the centers D, H, or at the circumferences A, E, and in like sort are the sectors BDC, FHG, because described upon the centers.

Pro. **D**raw the Right-lines BC, FG; Make  $CI = CB$ , and  $GK = FG = KL$ , and joyn DI, HK, HL.

Pro. The arch  $BC^s = CI^s$ , also the arch  $FG = GK = KL$ ; therefore the  $\angle BDC = CDI$ , and the  $\angle FHG = GHK = KHL$ . Therefore the arch BI, is as multiplex of the arch BC, as the  $\angle BDI$ , is of the  $\angle BDC$ . And in like manner is the arch FL, as multiplex of the arch FG, as the  $\angle FHL$ , is of the  $\angle FHG$ . But if the arch  $BI = FL$ , then likewise is the  $\angle BDI = \angle FHL$ . Therefore is the arch  $BC : FG :: \frac{BDC}{2} : \frac{FHG}{2} :: A : E$ . *WW D.*

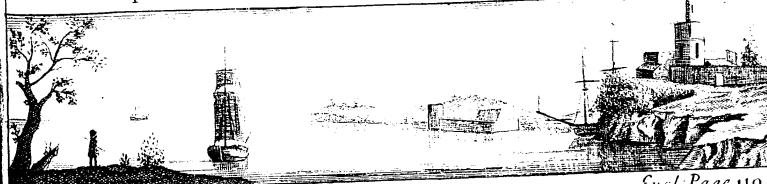
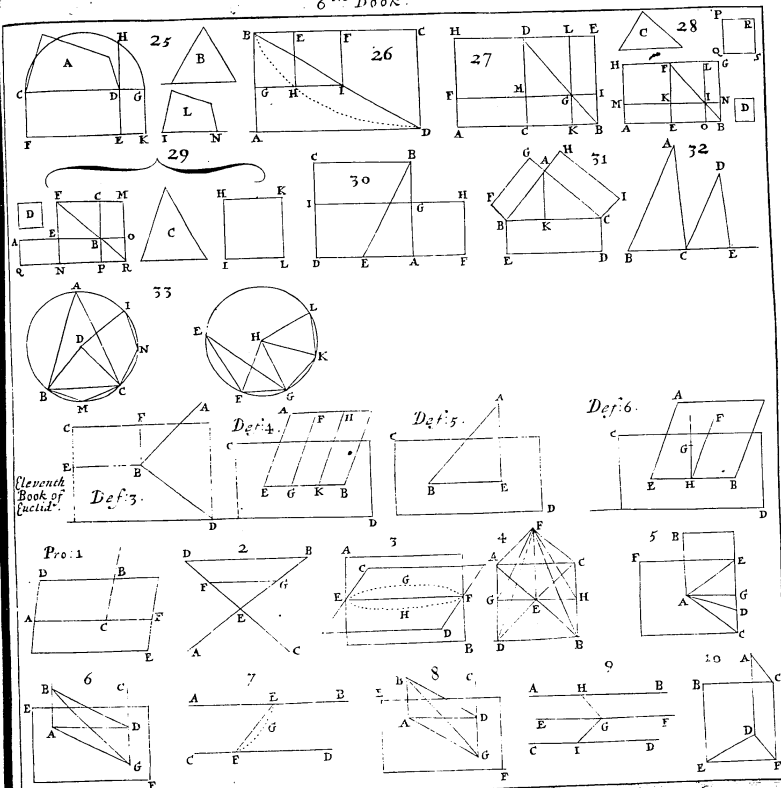
Secondly, the  $\angle BMC = CNT$ ; and therefore the segment  $BCM = CTN$ , also the  $\angle BDC = CDI$ ; wherefore the sector  $BDCM = CDIN$ . After the same manner are the sectors  $FHG = GHK = KHL$ . Therefore since accordingly as the arch  $BI = FL$ , so is likewise the sector  $BDI = FHL$ ; thence shall be the sector  $BDC : FHG ::$  the arch  $BC : FG$ . *WW D.*

- (a) 28. 3.  
(b) 27. 3.  
(c) 27. 3.  
(d) 6. def. 5.  
(e) 15. 5.  
(f) 20. 3.

- (g) 24. 3.  
(h) 4. 1.  
(k) 2. ax.

- (l) 6. def. 5.

Corol.

6<sup>th</sup> Book.



*Corol.*

1. As a sector is to a sector, so is  $\angle$  to  $\angle$ .
2. The  $\angle$  at the center is to 4  $\angle$ 's, as the arch on which it insits, to the whole circumference.
3. Arches of unequal  $O$ 's which subtend equal  $\angle$ 's, whether at the centers, or at the circumference, are like.
4. Two semidiameters cut off, like arches from concentrick Circumferences.

The most notable Prop. of this Book are the 1, 2, 3, 4, 5, 6, 8, 13, 14, 16, 19, 31.

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P

T H E

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THE  
ELEVENTH AND TWELFTH  
BOOKS

OF  
Euclid's Elements.

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Printed at LONDON, by *Anne Godbid*,  
and *John Playford*, 1680.





THE  
ELEVENTH BOOK  
OF  
Euclid's Elements.

DEFINITIONS.

1. **A** *Solid* is that which hath length, breadth, and thickness.
2. The *term*, or extreme, of a solid is a Superficies.
3. A *Right-line*  $AB$ , is perpendicular to a Plane  $CD$ , when it makes Right-angles  $ABD$ ,  $ABE$ ,  $ABF$ , with all the Right-lines  $BD$ ,  $BE$ ,  $BF$ , that touch it, and are drawn in the said Plane.
4. A *Plane*  $AB$ , is perpendicular to a Plane  $CD$ , when the Right-lines  $FG$ ,  $HK$ , drawn in one Plane  $AB$ , to the line of common section of the two Planes  $EB$ , and making Right-angles therewith, do also make Right-angles with the other Plane  $CD$ .
5. The *inclination* of a Right-line  $AB$ , to a Plane  $CD$ , is, when a perpendicular  $AE$ , is drawn from  $A$ , the highest point of that line  $AB$ , to the Plane  $CD$ , and another line  $EB$ , drawn from the point  $E$ , which the perpendicular  $AE$ , makes in the Plane  $CD$ , to the end  $B$ , of the said line  $AB$ , which is in the same Plane, whereby the angle is acute  $ABE$ , which is contained under the insisting line  $AB$ , and the line drawn in the Plane  $EB$ .
6. The



6. The inclination of a Plane  $AB$  to a Plane  $CD$ , is an acute angle  $FHG$  contained under the Right-lines  $FH, GH$ , which being drawn in either of the Planes  $AB, CD$  to the same point  $H$ , of the common section  $BE$ , make Right-angles  $FHB, GHB$ , with the common section  $BE$ .
7. Planes are said to be inclined to other Planes in the same manner, when the said angles of inclination are equal one to another.
8. Parallel Planes are those which being prolonged never meet.
9. Like solid figures are such as are contained under like Planes equal in number.
10. Equal and like solid figures are such as are contained under like Planes, equal both in multitude and magnitude.
11. A solid angle is the inclination of more than two Right-lines which touch one another, and are not in the same superficies.

Or thus ;

A solid angle is that which is contained under more than two Plane angles not being in the same superficies, but consisting all at one point.

12. A Pyramid is a solid figure comprehended under divers Planes (set upon one Plane, (which is the base of the Pyramid,) and gather together to one point.

13. A Prism is a solid figure contained under Planes, whereof the two opposite are equal, like and parallel ; but the others are parallelograms.

14. A Sphere is a solid figure made when the diameter of a semicircle abiding unmoved, the semicircle is turned round about, till it return to the same place from whence it began to be moved.

Corol.

Hence, all the rayes drawn from the center to the superficies of a Sphere, are equal amongst themselves.

15. The Axis of a Sphere, is that fixed Right-line, about which the semicircle is moved.

16. The Center of a Sphere, is the same point with that of the semicircle.

17. The Diameter of a Sphere, is a Right-line drawn through the center, and terminated on either side in the superficies of the sphere.

18. A Cone is a figure made, when one side of a rectangled triangle (*viz.* one of those that contain the Right-angle) remaining fixed, the triangle is turned round about till it return to the place from whence it first moved. And if the fixed Right-line be equal to the other which containeth the Right-angle, then the Cone is a rectangled Cone: but if it be less, it is an obtuse-angled Cone ; if greater, an acute angled Cone.

19. The Axis of a Cone is that fix'd line about which the triangle is moved.

20. The Base of a Cone is the circle, which is described by the Right-line moved about.

21. A

21. A Cylinder is a figure made by the moving round of a Right-angled parallelogram, one of the sides thereof, (namely which contains the Right-angle) abiding fix'd, till the parallelogram be turned about to the same place, where it began to move.

22. The Axis of a Cylinder is that quiescent Right-line, about which the parallelogram is turned.

23. And the Bases of a Cylinder are the circles which are described by the two opposite sides in their motion.

24. Like Cones and Cylinders, are they, both whose Axes and Diameters of their Bases are proportional.

25. A Cube is a solid figure contained under six equal Squares.

26. A Tetraedron is a solid figure contained under four equal and equilateral triangles.

27. An Octaedron is a solid figure contained under eight equal and equilateral triangles.

28. A Dodecaedron is a solid figure contained under twelve equal, equilateral and equiangular Pentagones.

29. An Icosaedron is a solid figure contained under twenty equal and equilateral triangles.

30. A Parallelepipedon is a solid figure contained under six quadrilateral figures, whereof those which are opposite are parallel.

31. A Solid figure is said to be inscribed in a solid figure, when all the angles of the figure inscribed are comprehended either within the angles, or in the sides, or in the planes of the figure wherein it is inscribed.

32. Likewise a Solid figure is then said to be circumscribed about a solid figure, when either the angles, or sides, or Planes of the circumscribed figure, touch all the angles of the figure which it contains.

Prop. I.

One part  $AC$ , of a Right-line, cannot be in a Plane superficies, and another part  $CB$ , elevated upward.

PRODUCE  $AC$ , in the Plane directly to  $F$ . If you conceive  $CB$ , to be drawn strait from  $AC$ , then two Right-lines  $AB, AF$ , have one common segment  $AC$ . <sup>(a) Which is impossible.</sup>

(a) IO AX. I.

Prop. II.

If two Right-lines  $AB, CD$ , cut one another, they are in the same Plane : And every Triangle  $DEB$ , is in one and the same Plane.

FOR imagine  $EFG$ , part of the triangle  $DEB$ , to be in one Plane, and the part  $DGB$ , to be in another ; then  $EF$ , part of the Right-line  $ED$  is in a Plane, and the other part elevated upwards. <sup>(a) Which is Absurd.</sup>  
There-



- (a) 1. 11. Therefore the triangle  $EDB$ , is in one and the same Plane; and so also are the Right-lines  $ED$ ,  $EB$ ; <sup>a</sup> wherefore the whole lines  $AB$ ,  $DC$ , are in one Plane. Which was to be demonstrated.

## Prop. III.

If two planes  $AB$ ,  $CD$ , cut one the other, their common section  $EF$ , is a Right-line.

- (a) 1. post. 1. IF  $EF$ , the common section be not a Right-line, <sup>a</sup> then in the plane  $AB$ , draw the Right-line  $EGF$ , <sup>a</sup> and in the plane  $CD$ , the Right-line  $EHF$ . Therefore two Right-lines  $EGF$ ,  $EHF$ , include a superficies. <sup>b</sup> Which is Absurd.

## Prop. IV.

If a Right-line  $EF$ , be at Right-angles erected upon two lines  $AB$ ,  $CD$ , cutting one the other, at the common section  $E$ ; it shall also be at Right-angles to the plane  $ACBD$ , drawn by the said lines.

- TAKE  $EA$ ,  $EC$ ,  $EB$ ,  $ED$ , equal one to the other, and joyn the Right-lines  $AC$ ,  $CB$ ,  $BD$ ,  $AD$ . Draw any Right-line  $GH$  through  $E$ , and joyn  $FA$ ,  $FC$ ,  $FD$ ,  $FB$ ,  $FG$ ,  $FH$ . Because  $AE$  is <sup>a</sup>  $= EB$ , and  $DE$  <sup>a</sup>  $= EC$ , and the angle  $AED$  <sup>b</sup>  $= CEB$ , <sup>c</sup> therefore  $AD$  is  $= CB$ , <sup>c</sup> and likewise  $AC$   $= DB$ . <sup>a</sup> Therefore  $AD$  is parallel to  $CB$ , <sup>a</sup> and  $AC$  to  $DB$ . <sup>c</sup> Wherefore the angle  $GAE$   $= EBH$ , and the angle  $AGE$   $= EHB$ . But also  $AE$   $= EB$ , <sup>b</sup> Therefore  $GE$   $= EH$ , <sup>b</sup> and  $AG$   $= BH$ . Whence by reason of the right angles, by the hyp. and so equal, at  $E$ , <sup>b</sup> the bases  $FA$ ,  $FC$ ,  $FB$ ,  $FD$ , are equal. Therefore the triangles  $ADF$ ,  $FBF$ , are equilateral one to another. <sup>a</sup> and thence the angle  $DAF$   $= BCF$ . Therefore in the triangles  $AGF$ ,  $FBH$ , the sides  $FG$ ,  $FH$ , are equal; and so by consequence the triangles  $FEH$ , and  $FEH$ , are mutually equilateral. <sup>m</sup> Therefore the angles  $FEH$ ,  $FEH$ , are equal, and <sup>a</sup> so Right-angles. In like manner,  $FE$ , makes Right-angles with all the lines drawn through  $E$ , in the plane  $ADBC$ , <sup>a</sup> and is therefore perpendicular to the said plane.

## Prop. V.

If a Right-line  $AB$ , be erected perpendicular to three Right-lines  $AC$ ,  $AD$ , touching one the other at the common section, those three lines are in the same plane.

- (a) 2. 11. FOR  $AC$ ,  $AD$ , <sup>a</sup> are in one plane  $FC$ ; <sup>a</sup> and  $AD$ ,  $AE$ , are in one plane  $BE$ . Which if you conceive to be several planes, then let their intersection <sup>b</sup> be the Right-line  $AG$ ; therefore because  $BA$  by the Hypoth. is per-

perpendicular to the Right-lines  $AC$ ,  $AD$ . And so to the plane  $FC$ , <sup>a</sup> it <sup>(c) 4. 11.</sup> is also perpendicular to the Right-line  $AG$ . Therefore (since <sup>a</sup> that  $AB$  <sup>(d) 5. def. 11.</sup> is in the same plane with  $AC$ ,  $AE$ ) the angles  $BAG$ ,  $BAE$ , are right angles, and consequently equal, the part and the whole. Which is Absurd.

## Prop. VI.

If two Right-lines  $AB$ ,  $DC$ , be erected perpendicular to one and the same plane  $EF$ , those Right-lines  $AB$ ,  $DC$ , are parallel one to the other.

DRAW  $AD$ , whereunto let  $DG$   $= AB$  be perpendicular in the plane  $EF$ , and joyn  $BD$ ,  $BG$ ,  $AG$ . Being in the triangles  $BAD$ ,  $ADG$ , the angles  $DAB$ ,  $ADG$  <sup>a</sup> are Right-angles, and  $AB$  <sup>b</sup>  $= DG$ , and  $AD$  <sup>(a) hyp.</sup> is common, <sup>c</sup> therefore  $BD$  is  $= AG$ . Whence in the triangles  $AGB$ ,  $BGD$ , equilateral one to the other, the angle  $BAG$  is <sup>a</sup>  $= BDG$ ; of <sup>(c) 4. 1.</sup> which being  $BAG$  is a Right-angle,  $B DG$  shall be so also. But the angle <sup>(d) 8. 1.</sup>  $GDC$  is supposed right, therefore the Right-line  $GD$  is perpendicular to the three lines  $DA$ ,  $DB$ ,  $CD$ . <sup>c</sup> Which are therefore in the same plane <sup>(e) 5. 11.</sup> wherein  $AB$  is. Wherefore since  $AB$  and  $CD$  are in the same plane, and <sup>(f) 2. 11.</sup> the internal angles  $BAD$ ,  $CD A$ , are Right-angles, <sup>a</sup>  $AB$  and  $CD$  shall <sup>(g) 28. 1.</sup> be parallels. *WW* to be Dem.

## Prop. VII.

If there be two parallel Right-lines  $AB$ ,  $CD$ , and any points  $E$ ,  $F$ , be taken in both of them, the line  $EF$ , which is joined at these points, is in the same plane with the parallels  $ABCD$ .

LET the plane in which  $AB$ ,  $CD$ , are, be cut by another plane at the points  $E$ ,  $F$ . Then if  $EF$  is not in the plane  $ABCD$ , it shall not be the common section. Therefore let  $EGF$  be the common section; which <sup>(a) 3. 11.</sup> <sup>(b) 14. ax. 1</sup> then is a Right-line. Therefore two Right-lines  $EF$ ,  $EGF$ , include a superficies. <sup>b</sup> Which is Absurd.

## Prop. VIII.

If there be two parallel Right-lines  $AB$ ,  $CD$ , whereof one  $AB$ , is perpendicular to a plane  $EF$ . Then the other  $CD$  shall be perpendicular to the same plane  $EF$ .

THE preparation and demonstration of the sixth of this Book being transferred hither; the angles  $GDA$ , and  $GDB$  are Right-angles: <sup>a</sup> there-



- (a) 4. 11. \* therefore  $GD$  is perpendicular to the plane, wherein are  $AD, DB$  (<sup>b</sup> in which also  $AB, CD$ , are.) <sup>c</sup> Therefore  $GD$  is perpendicular to  $CD$ . But the angle  $CDA$  is also <sup>a</sup> a Right-angle. <sup>e</sup> Therefore  $D$  is perpendicular to the plane  $EF$ . *W.W. to be Dem.*
- (b) 7. 11.  
(c) 3. def. 11.  
(d) 29. 1.  
(e) 4. 11.

## Prop. IX.

*Right-lines (AB, CD) which are parallel to the same Right-line EF, but not in the same plane with it, are also parallel one to the other.*

- I**N the plane of the parallels  $AB, EF$ , draw  $HG$  perpendicular to  $EF$ ; also in the plane of the parallels  $EF, CD$ , draw  $IG$  perpendicular to  $EF$ , <sup>a</sup> therefore  $EG$  is perpendicular to the plane wherein  $HG, GI$  are; and  $AH, CI$ , are perpendicular to the same plane. <sup>c</sup> Therefore  $AH$  and  $CI$  are parallels. *W.W. to be Dem.*
- (a) 4. 11.  
(b) 3. 11.  
(c) 6. 11.

## Prop. X.

*If two Right-lines AB, AC, touching one another be parallel to two other Right-lines ED, DF, touching one another, and not being in the same plane, those Right-lines contain equal angles, BAC, EDF.*

- L**et  $AB, AC, DE, DF$ , be equal one to the other, and draw  $AD, BC, EF, BE, CF$ . Being  $AB, DE$ , <sup>a</sup> are parallels and equal, <sup>b</sup> also  $BE, AD$ , are parallels and equal. In like manner  $CF, AD$ , are parallels and equal; <sup>c</sup> therefore also  $BE, FC$ , are parallels and equal. <sup>d</sup> Therefore  $BC, EF$  are equal. Wherefore since the triangles  $BAC, EDF$ , are of equal sides one to the other, the angles  $BAC, EDF$  <sup>e</sup> shall be equal. *W.W. to be Dem.*
- (a) hyp. and conctr.  
(b) 33. 1.  
(c) 2. 48. 1.  
(d) 36. 1.  
(e) 33. 1.  
(f) 8. 1.

## Prop. XI.

*From a Point given on high A, to draw a Right-line AI, perpendicular to a plane below BC.*

- I**N the plane  $BC$  draw any line  $DE$ ; to which from the point  $A$  <sup>a</sup> draw the perpendicular  $AF$ , and <sup>b</sup> likewise  $FH$  in the plane  $BC$ , cutting the said line  $DE$  at  $F$ ; <sup>c</sup> then let fall  $AI$  perpendicular to  $FH$ . Which  $AI$ , shall be perpendicular to the plane  $BC$ .
- (a) 12. 1.  
(b) 11. 1.

For

For through  $I$  <sup>c</sup> let  $KIL$ , be drawn parallel to  $DE$ . Because  $DE$  <sup>d</sup> is perpendicular to  $AF$ , and  $FH$ , <sup>e</sup> therefore  $DE$ , shall be perpendicular to the plane  $IFA$ . And so also  $KL$  <sup>f</sup> is perpendicular to the same plane. <sup>g</sup> Therefore the angle  $KIA$  is a Right-angle; but the angle  $AIF$  is also <sup>h</sup> a Right-angle. <sup>i</sup> Therefore  $AI$  is perpendicular to the plane  $BC$ . *W.W. to be Done.*

(c) 31. 1.  
(d) conctr.  
(e) 4. 11.  
(f) 8. 11.  
(g) 3. def. 11.  
(h) conctr.  
(i) 4. 11.

## Prop. XII.

*In a plane given BC, at a point given therein A, to erect a perpendicular line AF.*

**F**rom some point without the plane,  $D$ , <sup>a</sup> draw  $DE$  perpendicular to the said plane  $BC$ ; and joyning the points  $A, E$ , by a line  $AE$ , <sup>b</sup> draw  $AF$  parallel to  $DE$ . <sup>c</sup> It is apparent that  $AF$  is perpendicular to the plane  $BC$ . *W.W. to be Done.*

(a) 11. 11.  
(b) 31. 1.  
(c) 8. 11.

This and the preceding problem are practically performed by applying two Squares to the point given; as appears by 4. 11.

## Prop. XIII.

*At a point given C, in a plane given AB, two Right-lines CD, CE, cannot be erected perpendicular on the same side.*

**F**or both  $CD$ , and  $CE$ , <sup>a</sup> should then be perpendicular to the plane  $AB$ , and consequently parallels; which is repugnant to the definition of parallel lines.

(a) 6. 11.

## Prop. XIV.

*Planes CD, FE, to which the same Right-line AB, is perpendicular, are parallel.*

**I**F you deny this; then let the planes  $CD, FE$ , meet, so that their common section be the Right-line  $GH$ ; in which take any point  $I$ , draw to it the Right-lines  $IA, IB$ , in the said planes. Whereby in the triangle  $IAB$ , two angles  $IAB, IBA$  <sup>a</sup> are Right-angles. <sup>b</sup> Which is Absurd.

(a) hyp. and def. 11.  
(b) 17. 1.

Q2

Prop.



## Prop. XV.

If two Right-lines  $AB, AC$ , touching one another, be parallel to two other Right-lines  $DE, DF$ , touching one the other, and not being in the same plane with them, the planes  $BAC, EDF$ , drawn by those Right-lines, are parallel one to the other.

(a) 11. 11.  
(b) 31. 1.  
(c) 30. 1.  
(d) 3 def. 11.  
(e) 29. 1.  
(f) 4. 11.  
(g) *constr.*  
(h) 23. 11.

From  $A$  draw  $AG$ , perpendicular to the plane  $EF$ . And let  $GH, GI$ , be parallel to  $DE, DF$ ; these also shall be parallel to  $AB, AC$ . Therefore since the angles  $IGA, HGA$ , are Right-angles, also  $CAG, BAG$ , shall be Right-angles. Therefore  $GA$  is perpendicular to the plane  $BC$ ; but the same is perpendicular to the plane  $EF$ . Therefore the planes  $BC, EF$ , are parallel. *W. W. to be Dem.*

## Prop. XVI.

If two parallel planes  $AB, CD$ , be cut by some other plane  $HEIGF$ , their common sections  $EH, GF$ , are parallel one to the other.

(a) 1. 11.

For if they be conceived to be otherwise, being in the same plane that cuts them, they will meet somewhere, if produced; suppose in  $I$ ; wherefore since the whole lines  $HEI, FGI$ , are in the planes  $AD, CD$ , being produced, the planes also shall meet. *Contrary to the Hyp.*

## Prop. XVII.

If two Right-lines  $ALB, CMD$ , be cut by parallel planes  $EF, GH, IK$ ; they shall be cut proportionally, ( $AL : LB :: CM : MD$ .)

(a) 16 11.  
(b) 2. 6.

Let the Right-lines  $AC, BD$ , be drawn in the planes  $EF, IK$ ; as also  $AD$  passing through the plane  $GH$  in the point  $N$ . And join  $NL, LM$ ; the planes of the triangles  $ADC, ADB$ , make the sections  $BD, LN$ , and  $AC, NM$  parallels. Therefore  $AL : LB :: AN : ND :: CM : MD$ . *W. W. to be Dem.*

Prop.

## Prop. XVIII.

If a Right-line  $AB$ , be perpendicular to some plane  $CD$ , all the planes extended by that Right-line  $AB$  ( $EF$ , &c.) shall be perpendicular to the same plane  $CD$ .

Let there be some plane  $EF$  drawn by  $AB$ , making the section  $EG$  with the plane  $CD$ ; from some point whereof  $H$ , draw  $HI$  parallel to  $AB$ , in the plane  $EF$ ; then shall  $HI$  be perpendicular to the plane  $CD$ , and so likewise any other lines, that are perpendicular to  $EG$ ; therefore the plane  $EF$  is perpendicular to the plane  $CD$ ; and by the same reason any other planes drawn by  $AB$  shall be perpendicular to  $EF$ . *W. W. to be Dem.*

## Prop. XIX.

If two planes  $AB, CD$ , cutting one the other, be perpendicular to some plane  $GH$ , their line of common section  $EF$  shall be perpendicular to the same plane ( $GH$ .)

Because the planes  $AB, CD$ , are taken perpendicular to the plane  $GH$ , it appears by 4. def. 11. that out of the point  $F$  there may be drawn in both planes  $AB, CD$ , a perpendicular to the plane  $GH$ . Which shall be but one; and therefore the common section of the said planes. *W. W. to be Dem.*

## Prop. XX.

If a solid angle  $ABCD$ , be contained under three plane angles,  $BAD, DAC, BAC$ , any two of them howsoever taken are greater than the third.

If the three angles are equal, the assertion is evident; if unequal, then let the greatest be  $BAC$ ; from whence take away  $BAE = BAD$ , and make  $AD = AE$ ; and also draw  $BE, BD, DC$ . Because the side  $BA$  is common, and  $AD = AE$ ; and the angle  $BAE = BAD$ , thence is  $BE = BD$ . But  $BD = DC$  is  $BC$ ; therefore  $DC = EC$ . Wherefore since  $AD = AE$ , and the side  $AC$  is common, and  $DC = EC$ ; the angle  $CAD$  shall be  $CAE$ ; therefore the angle  $BAD = CAD = BAC$ . *W. W. to be Dem.*

Prop.



## Prop. XXI.

Every solid angle  $A$ , is contained under less angles than four plane Right-angles.

For let a plane any wise cutting the sides of the solid angle  $A$ , make a many-sided figure  $BCDE$ , and as many triangles  $ABC$ ,  $ACD$ ,  $ADE$ ,  $AEB$ . I denote all the angles of the Polygon by  $X$ ; and I term the sum of the angles at the bases of the triangles  $T$ . Wherefore  $X \vdash 4$  Right-ang.  $^a = T \vdash A$ : but being that (of the angles at  $B$ )  $^b$  the angle  $ABE \vdash ABC$  is  $\sqsubset CBE$ , and the same is true also of the angles at  $C$ , at  $D$ , and at  $E$ ,  $^c$  it is manifest that  $T$  is  $\sqsubset X$ . And consequently  $A$  shall be  $\sqsubset 4$  Right-angles. *W. W. to be Dem.*

(a) 32. 1. and  
Job. 32. 1.  
(b) 20. 11.  
(c) 5 ax. 1.

## Prop. XXII.

If there be three plane angles  $A$ ,  $B$ ,  $HCI$ , whereof two howsoever taken are greater than the third, and the Right-lines which contain them be equal  $AD$ ,  $AE$ ,  $FB$ , &c. then of the Right-lines  $DE$ ,  $FG$ ,  $HI$ , coupling those equal Right-lines together, it is possible to make a triangle.

A Triangle may be  $^a$  made of them, if any two be greater than the third: but they are so. For  $^b$  make the angle  $HCK = B$ , and  $CK = CH$ , and draw  $HK$ ,  $IK$ .  $^c$  Thence  $KH = FG$ ; and because the angle  $KCI \vdash A \vdash C$ . Therefore  $KI \vdash DE$ ; but  $KI \vdash HI \vdash KH$  ( $FG$ .) therefore  $DE \vdash HI \vdash FG$ . By the like argument any two may be proved greater than the third; and consequently  $^d$  it is possible to make a triangle of them. *W. W. to be Dem.*

(a) 22. 1.  
(b) 23. 1.  
(c) 4. 1.  
(d) hyp.  
(e) 24. 1.  
(f) 20. 1.

## Prop. XXIII.

To make a solid angle  $MHIK$ , of three plane angles  $A$ ,  $B$ ,  $C$ , whereof two howsoever taken are greater than the third.  $^*$  But it is necessary that those three angles be less than four Right-angles.

$^*$  21. 11.

Make  $AD$ ,  $AE$ ,  $BE$ ,  $BF$ ,  $CF$ ,  $CG$ , equal one to the other; and of the subtended lines  $DE$ ,  $EF$ ,  $FG$ , (that is, of the equal lines  $HI$ ,  $IK$ ,  $KH$ .)  $^a$  make the triangle  $HKI$ ; about which  $^b$  describe the circle  $LHKI$ .  $^c$  But because  $AD$  is  $\sqsubset HL$ ;  $^d$  let  $ADq$  be  $HLq \vdash LMq$ .  $^e$  And let  $LM$  be perpendicular to the plane of the circle  $LHKI$ ; and draw  $HM$ ,  $KM$ ,  $IM$ . Wherefore since the angle  $HLM$ ,  $^f$  is a Right-

(a) 22. 11. and  
21. 1.  
(b) 5. 4.  
\* See Clavius.  
(c) Job. 47. 1.  
(d) 12. 11.  
(e) 3. def. 11.

Right-angle,  $^f$  thence is  $MHq = HLq \vdash LMq = ADq$ . Therefore  $^g$   $MH = AD$ . By the same reason  $MK$ ,  $MI$ ,  $AD$ , (that is  $AE$ ,  $EB$ , &c.) are equal; therefore since  $HM = AD$ , and  $MI = AE$ , and  $DE = HI$ ,  $^h$  the angle  $A$  shall be  $= HMI$ ,  $^i$  as likewise the angle  $IMK = B$ ,  $^k$  and the angle  $HMK = C$ ; wherefore a solid angle is made at  $M$  of the three given plane angles. *W. W. to be Done.*  $AD$  is assumed to be  $\sqsubset HL$ . But this is manifest. For if  $AD$  be  $=$  or  $\vdash HL$ , then is the angle  $A =$   $^l$  or  $\sqsubset HLI$ . In like manner shall  $B$  be equal or  $\sqsubset HLK$ , and  $C =$  or  $\sqsubset KLI$ ; wherefore  $A \vdash B \vdash C$   $^m$  shall either equal or exceed four right angles, contrary to the Hypoth. therefore rather let  $AD$  be  $\sqsubset HL$ . *W. W. to be Dem.*

(f) 47. 1.  
(g) constr.  
(h) constr.  
(i) 5. 1.

(l) constr. and  
8. 1.  
(m) 21. 1.

$^n$  4 cor. 13.

## Prop. XXIV.

If a solid  $AB$  be contained under parallel planes, the opposit planes thereof ( $AG$ ,  $DB$ , &c.) are like and equal parallelograms.

The plane  $AC$  cutting the parallel planes  $AG$ ,  $DB$ ,  $^a$  makes the sections  $AH$ ,  $DC$ , parallels; and by the same reason  $AD$ ,  $HC$  are parallels. Therefore  $ADCH$  is a pgr. By the like argument the other planes of the parallelepipedon are  $^b$  pgrs. wherefore being  $AF$  is parallel to  $^c$   $HG$ , and  $AD$  to  $HC$ ,  $^d$  the angle  $FAD$  shall be  $= CGH$ ; therefore because  $AF = HG$ , and  $AD = HC$ , and so  $AF \cdot AD :: HG \cdot HC$ ; the triangles  $FAD$ ,  $GHC$ ,  $^e$  are like and  $^f$  equal; and consequently the pgrs.  $AE$ ,  $HB$ , are like and  $^g$  equal; and the same may be shewn of the rest opposit planes. Therefore, &c.

(a) 16. 11.  
(b) 35 def. 1.  
(c) 10. 11.  
(d) 34. 1.  
(e) 7. 5.  
(f) 6. 6.  
(g) 4. 1.  
(h) 6 ax. 1.

## Prop. XXV.

If a solid Parallelepipedon  $ABCD$ , be cut by a plane  $EF$ , parallel to the opposite planes  $AD$ ,  $BC$ ; then as the base  $AH$  is to the base  $BH$ , so shall solid  $AHD$  be to solid  $BHC$ .

Conceive the Parallelepipedon to be extended on either side; and take  $AI = AE$ , and  $BK = EB$ , and put the planes  $IQ$ ,  $KP$ , parallel to the planes  $AD$ ,  $BC$ ; then the pgrs.  $IM$ ,  $AH$ , and  $^a$   $DL$ ,  $DG$ , and  $IQ$ ,  $AD$ ,  $EF$ , &c. are  $^b$  like and equal;  $^c$  wherefore the Parallelepipedon  $AQ$  is  $= AF$ ; and by the same reason the Parallelepipedon  $BP$  is  $= BF$ ; therefore the solids  $IF$ ,  $EP$ , are as multiplex of the solids  $AF$ ,  $^d$   $EC$ , as the bases  $IH$ ,  $KH$ , are of the bases  $AH$ ,  $BH$ . And if the basis  $IH$  be  $\sqsubset$ ,  $=$ ,  $\vdash KH$ ,  $^e$  likewise shall the solid  $IE$  be  $\sqsubset$ ,  $=$ ,  $\vdash EP$ ,  $^f$  consequently  $AH \cdot BH :: AF \cdot EC$ . *W. W. to be Dem.*

(a) 36. 1. and  
1. def. 6.  
(b) 24. 11.  
(c) 10 def. 11.  
(d) 24. 11. and  
9. def. 11.  
(e) 6 def. 5.

The same may be accommodated to all sort of prisms, whence

Corol.



Carol.

If any prism whatsoever be cut by a plane parallel to the opposite planes, the section shall be a figure equal and like to the opposite planes.

## Prop. XXVI.

Upon a Right-line given  $AB$ , and at a point given in it  $A$ , to make a solid angle  $AHIL$  equal to a solid angle given  $CDEF$ .

- (a) 11. 11. **F**rom some point  $F$  draw  $FG$  perpendicular to the plane  $DCE$ , and draw the Right-lines  $DF$ ,  $FE$ ,  $EG$ ,  $GD$ ,  $CG$ . Make  $AH=CD$ , and the angle  $HAI=DCE$ , and  $AI=CE$ ; and in the plane  $HAI$  make the angle  $HAK=DCG$ , and  $AK=CG$ ; then erect  $KL$  perpendicular to the plane  $HAI$ , and let  $KL$  be  $=GF$ . And draw  $AL$ , then  $AHIL$  shall be a solid angle equal to that given  $CDEF$ . For the construction of this do's wholly resemble the framing of that, as may easily appear to any that examine it.

## Prop. XXVII.

Upon a Right-line given  $AB$ , to describe a Parallelepipedon  $AK$ , like, and in like manner situate, with a solid Parallelepipedon given  $CD$ .

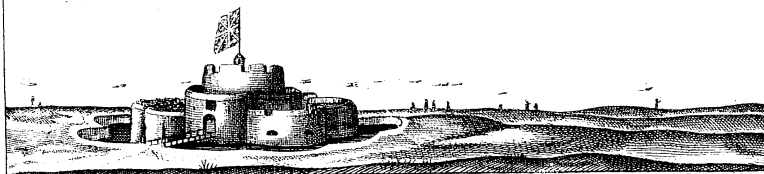
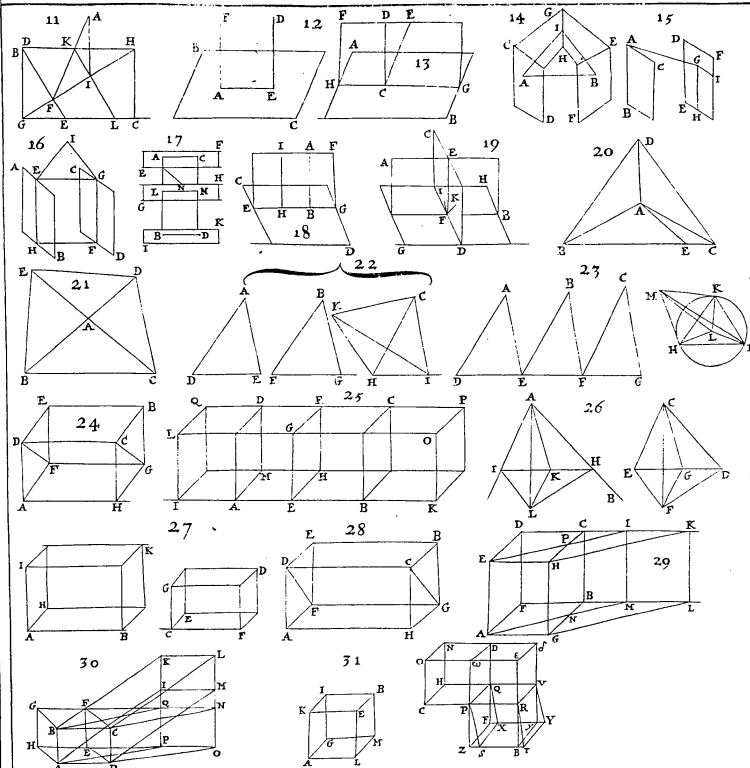
- O**F the plane angles,  $BAH$ ,  $HAI$ ,  $BAI$ , which are equal to  $FCE$ ,  $ECG$ ,  $FCG$ , make the solid angle  $A$  equal to the solid angle  $C$ . Also make  $FC:CE::BA:AH$ , and  $CE:CG::AH:AI$ , (whence of equality  $FC:CG::BA:AI$ ) and finish the Parallelepipedon  $AK$ , which shall be like to that which is given.

- For by the construction, the Pgr.  $BH$  is like to  $FE$ , and  $HJ$  to  $EG$ , and  $BI$  to  $FG$ , and so the opposites of these to the opposites of them: therefore the six planes of the solid  $AK$ , are like to the six planes of the solid  $CD$ , and consequently  $AK$ ,  $CD$ , are like solids. *W.W. to be Done.*

## Prop. XXVIII.

If a solid Parallelepipedon  $AB$ , be cut by a plane  $FGCD$ , drawn by the diagonal lines  $DF$ ,  $CG$ , of the opposite planes  $AE$ ,  $HB$ , that solid  $AB$ , shall be equally bisected by the plane  $FGCD$ .

- F**or because  $DC$ ,  $FG$ , are equal and parallels, the plane  $FGCD$ , is a Pgr. and being the Pgrs.  $AE$ ,  $HB$ , are equal and like, also the triangles  $AFD$ ,  $HGC$ ,  $CGB$ ,  $DFE$ ; are equal and like. But





But the Pgrs.  $AC$ ,  $AG$ , are equal and like to  $FB$  and  $FD$ ; therefore all the planes of the prism  $FGCDAH$ , are equal and like to all the planes of the prism  $FGCDEB$ , and consequently this prism is equal to that. (c) 9 def. 11. *W. W. to be Dem.*

## Prop. XXIX.

*Solid Parallelepipeds*  $AGHEFBCD$ ,  $AGHEMLKI$ , being constituted upon the same base  $AGHE$ , and \* in the same height, whose insisting lines  $AF$ ,  $AM$ , are placed in the same Right-lines  $AG$ ,  $FL$ , are equal one to the other.

\* i.e. between the Parallel planes  $AGHE$ ,  $EFLK$ , and so understand it in the foll.

For if from the equal prisms  $AFMEDI$ ,  $GBLHCK$ , the common prism  $NBMPCI$ , be taken away, and the solid  $AGNEHR$  be added, the Parallelepipeton  $AGHEFBCD$  shall be =  $AGHEMLKI$ . *W. W. to be Dem.*

(a) 10 def. 11. and 35. 1. (b) 3 and 7 ex. 1.

## Prop. XXX.

*Solid Parallelepipeds*  $ADBCHEFG$ ,  $ADCBIMLK$ , being constituted upon the same base  $ADBC$ , and in the same height, whose insisting lines  $AH$ ,  $AI$ , are not placed in the same Right-lines, are equal one to the other.

For produce the Right-lines  $HEO$ ,  $GFN$ , and  $LMO$ ,  $KIP$ ; and draw  $AP$ ,  $DO$ ,  $BQ$ ,  $CN$ ; then shall  $DC$ ,  $AB$ ,  $HG$ ,  $EF$ ,  $PQ$ ,  $ON$ , be as well equal and parallel one to the other as  $AD$ ,  $HE$ ,  $GF$ ,  $BC$ ,  $KL$ ,  $IM$ ,  $QN$ ,  $PO$ . Wherefore the Parallelepipeton  $ADCBPONQ$  shall be equal to either Parallelepipeton  $ADCBHEFG$ ,  $ADCBIMLK$ ; and consequently these two are equal one to the other. *W. W. to be Dem.*

(a) 34. 1. (b) 29. 11. (c) 1 ax. 1.

## Prop. XXXI.

*Solid Parallelepipeds*,  $ALEKGMBI$ ,  $CP\omega OHQDN$ , being constituted upon equal bases  $ALEK$ ,  $CP\omega O$ , and \* in the same height are equal one to the other.

\* by height understand the Perpendicular drawn from the plane of the base to the opposite plane.

First, let the Parallelepipeds  $AB$ ,  $CD$ , have the sides perpendicular to the bases; and at the side  $CP$  being produced, make the Pgr.  $PRTS$  equal and like to the Pgr.  $KELA$ ; and so the Parallelepipeton  $PRTS$  equal and like to the Parallelepipeton  $AB$ . Produce  $O\omega E$ ,  $ND\delta$ ,  $\omega PZ$ ,  $DQF$ ,  $ERB$ ,  $\delta V\gamma$ ,  $TSZ$ ,  $TXF$ ; and draw  $E\delta$ ,  $B\gamma$ ,  $ZF$ .

(a) 18. 6. (b) 27. 11. and 10 def. 11.



- (c) 30 def. 11. The planes  $O\epsilon\delta N$ ,  $CRVH$ ,  $ZTYF$ ;  $\epsilon$  are parallels one to the other;  
 (d) hyp. and  $\delta$  and the Pgrs.  $ALEK$ ,  $CD\omega O$ ,  $PRTS$ ,  $PRBZ$  are equal. There-  
 35. 1. fore since the Parallelepipedon  $CD\omega$   $PV\delta\omega$  :: Pgr.  $C\omega$  ( $PRBZ$ )  $P\epsilon\epsilon$  ::  
 (e) 25. 11. Parallelepipedon  $PRBZQV\gamma F$ .  $PV\delta\omega$ ; the Parallelepipedon  $CD$ ,  
 (f) 9. 5. 'shall be  $= TRBZQV\gamma F = PRVQSTYX^a = AB$ . *W.W. to be*  
 (g) 29. 11. *Dem.*  
 (h) *constr.*

But if the Parallelepipedons  $AB$ ,  $CD$ , have sides oblique to the base, then on the same bases, and in the same height place Parallelepipedons whose sides are perpendicular to the base.  $\epsilon$  They shall be equal to one another, and those that are oblique  $\epsilon$  whence, also the oblique Parallelepipedons  $AB$ ,  $CD$  are equal. *W.W. to be Dem.*

## Prop. XXXII.

*Solid Parallelepipedons*  $ABCD$ ,  $EFGH$ , of the same height, are one to the other, as their bases,  $AB$ ,  $EF$ .

- (a) 45. 1. **P**roduce  $EHI$ ,  $\epsilon$  and make the Pgr.  $FI = AB$ , and  $\epsilon$  compleat the  
 (b) 31. 1. Parallepp.  $FINM$ . It is clear that the Parallepp.  $FINM$ . ( $\epsilon$   $ABCD$ .)  
 (c) 31. 11.  $EFGH^a$  ::  $FI(AB)$   $EF$ . *W.W. to be Dem.*  
 (d) 25. 11.

## Prop. XXXIII.

*Like Solid Parallelepipedons*,  $ABCD$ ,  $EFGH$ , are in tripled proportion one to the other, of that in which their homologous sides, or of like proportion  $AI$ ,  $EK$ , are.

- (a) 3. 7. **P**roduce the Right-lines  $AIL$ ,  $DIO$ ,  $BIN$ , and  $\epsilon$  make  $IL$ ,  $IO$ ,  $IN$ ,  
 (b) 27. 11. equal to  $EK$ ,  $KH$ ,  $KF$ , and so the Parallepp.  $IXMT$  equal  
 (c) 31. 1. and like to the Parallepp.  $EFGH$ .  $\epsilon$  Let the Parallepps.  $IXPB$ ,  $DLTQ$   
 (d) hyp. be finished.  $\epsilon$  Then shall be  $AL$ .  $IL(EK)$  ::  $DI$ .  $IO(HK)$  ::  $BI$   
 (e) 1. 6.  $IN$ .  $KF$ ;  $\epsilon$  that is the Pgr.  $AD$ .  $DL$  ::  $DL$ .  $IX$  ::  $BO$ .  $IT$   
 (f) 32. 11.  $\epsilon$  i.e. the Parallepp.  $ABCD$ .  $DLQY$  ::  $DLQY$ .  $IXBP$  ::  $IXBP$   
 (g) *constr.*  $IXMT$  ( $\epsilon$   $EFGH$ ).  $\epsilon$  therefore the proportion of  $ABCD$  to  $EFGH$   
 (h) 10. def. 5, is triple of the proportion of  $ABCD$  to  $DLQY$ ,  $\epsilon$  or of  $AI$  to  $EK$ .  
 (k) 1. 6. *W.W. to be Dem.*

*Corol.*

Hence it appears, that if four Right-lines be continually proportional, as the first is to the fourth, so is a Parallelepipedon described on the first to a Parallelepipedon described on the second, being like and in like manner described.

Prop.

## Prop. XXXIV.

*In equal solid Parallelepipedons*  $ADCB$ ,  $EHGF$ , the bases and altitudes are reciprocal ( $AD$ .  $EH$  ::  $EG$ .  $AC$ .) And solid Parallelepipedons,  $ADCB$ ,  $EHGF$ , whose bases and altitudes are reciprocal, are equal.

**F**irst, let the sides  $CB$ ,  $GE$  be perpendicular to the bases; then if the altitudes of the solids are equal, the bases also shall be equal; and the thing is clear. But if the altitudes are unequal, from the greater  $EG$  take  $EI = AC$ , and at  $I^b$  draw the plane  $IK$  parallel to the base  $EH$ . Then,

1. Hyp.  $AD$ .  $EH$   $\epsilon$  :: Parallepp.  $ADCB$ .  $EHIK^a$  :: Parallepp.  $EHGF$ .  $EHIK^c$  ::  $GL$ .  $IL^c$  ::  $GE$ .  $IE$ . ( $\epsilon$   $AC$ .)  $\epsilon$  it is plain therefore that  $AD$ .  $EH$  ::  $GE$ .  $AC$ . *W.W. to be Dem.*  
 2. Hyp.  $ADCB$ .  $EHIK^b$  ::  $AD$ .  $EH^a$  ::  $EG$ .  $EI^1$  ::  $GL$ .  $LI^m$  :: Parallepp.  $EHGF$ .  $EHIK$ .  $\epsilon$  Wherefore the Parallelepipedon  $ADCB = EHGF$ . *W.W. to be Dem.*

Moreover, let the sides be oblique to the bases, and erect right Parallelepipedons upon the same bases in the same altitude; the oblique Parallepps shall be equal to them. Wherefore since by the first part, the bases and altitudes of those be reciprocal, the bases and altitudes of these also shall be reciprocal. *W.W. to be Dem.*

*Corol.*

*All that hath been demonstrated of Parallelepipedons in the 29, 30, 31, 32, 33, 34. Prop. does also agree to triangular prisms, which are half Parallelepipedons, as appears by Prop. 28. Therefore,*

1. Triangular prisms are of equal height with their bases.
2. If they have the same or equal bases, and the same altitude, they are equal.
3. If they be like, their proportion is treble to that of their sides of like proportion.
4. If they be equal, their bases and altitudes are reciprocal; and if their bases and altitudes be reciprocal, they are also equal.

R 2

Prop.



## Prop. XXXV.

if there be two plane angles BAC, EDF, equal, and from the points of those angles two Right-lines AG, DH, be elevated on high, containing equal angles with the lines first given, each to his correspondent angle (the angle GAB = HDE, and GAC = HDF.) and if in those elevated lines AG, DH, some points be taken, G, H; and from these points perpendicular lines GI, HK, drawn to the planes BAC, EDF, in which the angles first given are, and Right-lines AI, DK, be drawn to the angles first given from the points I, K, which are made by the perpendiculars in the planes; these Right-lines with the elevated lines, AG, DH, shall contain equal angles GAM, HDK.

**M**ake DH, AL, equal; and GI, LM parallels; and MC to AC, MB to AB, KF to DF, KE to DE, perpendicular; and draw the Right-lines BC, LB, LC, and EF, HF, HE; <sup>a</sup> and LM is perpendicular to the plane BAC; <sup>b</sup> wherefore the angles LMC, LMA, LMB; and by the same reason the angles HKF, HKD, HKE are Right-angles. Therefore ALq = LMq - AMq = LMq - CMq + ACq = LCq - ACq; <sup>a</sup> therefore the angle ACL is a Right-angle. Again ALq = LMq - MAq = LMq - BMq + BAq = BLq - BAq; <sup>a</sup> therefore the angle ABL is also a Right-angle. By the like inference the angles DFH, DEH, are Right-angles; <sup>c</sup> therefore AB = DE, <sup>d</sup> and BL = EH, <sup>e</sup> and AC = DF, and CL = FH; <sup>f</sup> wherefore also BC = EF, <sup>g</sup> and the angle ABC = DEF, <sup>g</sup> and the angle ACB = DFE; <sup>h</sup> whence the other Right angles CBM, BCM, are equal to the other FEK, FEH, <sup>i</sup> therefore CM = FK; <sup>j</sup> and so also AM = DK; therefore if from LAq = HDq be taken away AMq = DKq, <sup>k</sup> there remains LMq = HKq; wherefore the triangles LAM, HDK are equilateral one to the other; <sup>l</sup> therefore the angle LAM = HDK. W. W. to be Dem.

Corol.

Therefore, if there be two plane angles equal, from whose points equal Right-lines be elevated on high, containing equal angles with the lines first given, each to each; perpendiculars drawn from the extreme points of those elevated lines to the planes of the angles first given, are equal one to the other; viz. LM = HK.

Prop.

## Prop. XXXVI.

if there be three Right-lines DE, DG, DF, proportional, the solid parallelepipedon DH, made of them, is equal to the solid parallelepipedon IN, made of the middle line DG, (IL) which is also equilateral, and equiangular to the said parallep. DH.

**B**ecause DE . LK :: IL . DF; <sup>b</sup> the pgr. IK shall be = FE; <sup>(a) 6p.</sup> and by reason of the equality of the plane angles at E and I, and of <sup>(b) 14. 6.</sup> the lines G D, I M, also the altitudes of the Parallelepipedons are equal by the prec. Corol. <sup>c</sup> therefore the paralleps are equal one to the other. <sup>(c) 21. 11.</sup> W. W. to be Dem.

## Prop. XXXVII.

if there be four Right-lines A, B, C, D, proportional, the solid Parallelepipedons A, B, C, D, being like, and in like sort described from them, shall be proportional. And if the solid Parallelepipedons, being like and in like sort described, be proportional (A . B :: C . D.) Then those Right-lines A, B, C, D, shall be proportional.

**F**or the proportions of the paralleps. <sup>a</sup> are triple of those of the <sup>(a) 33. 11.</sup> lines; therefore if A . B :: C . D; <sup>b</sup> then shall the parallep. A . <sup>(b) 14. 6.</sup> parallep. B :: parallep. C . parallep. D; and so also contrarily.

## Prop. XXXVIII.

if a plane AB, be perpendicular to a plane AC, and a perpendicular line EF be drawn from a point E in one of the planes (AB) to the other plane AC, that perpendicular EF shall fall upon the common section of the planes AD.

**I**f it be possible, let F fall without the intersection AD, and in the <sup>(a) 12. 1.</sup> plane AC <sup>a</sup> draw FG perpendicular to AD, and join EG. The angle <sup>(b) 4. and 3.</sup> FGE <sup>b</sup> is a Right-angle, and EFG is supposed to be such also; therefore <sup>(c) 17. 1.</sup> two Right-angles are in the triangle EFG. <sup>c</sup> Which is absurd.

Prop



## Prop. XXXIX.

If the sides (AE, FC, AF, EC, and DH, GB, DG, HB) of the opposite planes AC, DB, of a solid Parallelepipedon AB, be divided into two equal parts, and planes, ILQO, PKMR, be drawn through their sections, the common section of the planes ST, and the diameter of the solid Parallelepipedon AB shall divide one the other into two equal parts.

(a) 34. 1. Draw the Right-lines SA, SC, TD, TB. Because <sup>a</sup> the sides DO, (b) 29. 1. OT are equal to the sides BQ, QT, <sup>b</sup> and the alternate angles (c) 4. 1. TOD, TQB, equal also, <sup>c</sup> the bases DT, TB, and the angles DTO, (d) sch. 15. 1. BTQ are equal; <sup>d</sup> therefore DTB is a Right-line; and so in like manner (e) 34. 1. is ASC. Moreover <sup>e</sup> as well AD is parallel and equal to FG <sup>e</sup> as FG (f) 5. 11. and 1. ax. to CB, and <sup>f</sup> thence AD is parallel and equal to CB; <sup>g</sup> and consequently (g) 33. 1. AC to DB; <sup>h</sup> wherefore AB and ST are in the same plane ABCD. (h) 7. 11. Therefore since the vertical angles AVS, BVT, and the alternate angles (i) 7. ax. 1. ASP, BTV are equal; <sup>k</sup> and AS = BT; therefore shall AV be = (l) 26. 1. BV, <sup>l</sup> and SV = VT. W.W. to be Dem.

Corol.

Hence in every Parallelepipedon all the diameters bisect one another in one point, V.

## Prop. XL.

If two prisms ABCFD, GHMLK, be of equal altitude, whereof one hath its base ABCE, a Parallelogram, and the other GHM a triangle; and if the Parallelogram ABCE, be double to the triangle GHM; these prisms ABCFD, GHMLK are equal.

(a) 31. 11. For if the parallepps. AN, GQ, be completed, <sup>a</sup> they shall be e- (b) 34. 1. and 7. ax. qual, because of the equality <sup>b</sup> of the bases AC, GP, and <sup>c</sup> of the (c) hyp. altitudes; <sup>d</sup> therefore also the prisms, <sup>e</sup> the halves thereof shall be equal. (d) 28. 11. W.W. to be Dem. (e) 7. ax. 1.

Schol.

Antr. Tasc. From the preceding demonstrations, the dimension of triangular prisms, and quadrangular, or parallelepipedons, is learnt; viz. by multiplying the altitude into the base.

As

As if the altitude be 10 foot, and the base 100 square foot (the base may be measured by sch. 35, 1. or by 41, 1.) then multiply 100 by 10, and 1000 cubic foot shall be produced for the solidity of the prism given.

For as a Rectangle, so also is a right Parallelepipedon produced of the altitude multiplied into the base. Therefore every Parallelepipedon is produced of the altitude multiplied into the base, as appears by 31. of this Book.

Moreover, since the whole Parallelepipedon is produced of the altitude drawn in to the base, the half thereof (that is, a triangular prism) shall be produced of the altitude drawn into half the base, namely the triangle.

An Adversisement.

Obs. That of those letters which denote a solid angle, the first is always at the point in which the angle is; but of those letters which denote a pyramid, the last is at the supreme point thereof.

Ex. gr. The solid angle ABCD is at the point A, and the supreme point of the pyramid BCDA is at the point A, and the base is the triangle BCD.

THE





THE  
TWELFTH BOOK  
OF  
Euclid's Elements.

PROPOSITION I.

Like polygonous figures  $ABCDE$ ,  $FGHIK$ , described in circles  $ABD$ ,  $FGI$ , are one to another, as the squares described of the diameters of the circles  $AL$ ,  $FM$ :

- (a) 1 def. 6.  
(b) 6. 6.  
(c) 21. 3.  
(d) 31. 3.  
(e) 32. 3.  
(f) cor. 4. 6.  
(g) 22. 6.

**D**raw  $AC$ ,  $BL$ ,  $FH$ ,  $GM$ . Because <sup>a</sup> the angle  $ABC = FGH$ , <sup>b</sup> and  $AB \cdot BC :: FG \cdot GH$ ; <sup>b</sup> therefore shall the angle  $ACB$  ( $\angle ALB$ ) be  $= FHG$  ( $\angle FMG$ .) but the angles  $ABL$ ,  $FGM$  <sup>c</sup> are right and so equal; <sup>c</sup> therefore the triangles  $ABL$ ,  $FGM$  are equiangular; <sup>d</sup> wherefore  $AB \cdot FG :: AL \cdot FM$ ; <sup>e</sup> therefore  $ABCDE \cdot FGHK :: ALq \cdot FMq$ .

Corol.

Corol.

Hence (because  $AB \cdot FG :: AL \cdot FM :: BC \cdot GH$ , &c.) the contents of like polygonous figures described in a circle are in <sup>b</sup> proportion as the diameters. (h) 1. 12. and 1. 5.

Prop. II.

Circles  $ABT$ ,  $EFN$ , are in proportion one to another, as the squares of their diameters  $AC$ ,  $EG$  are.

**S**uppose  $ACq \cdot EGq ::$  the circle  $ABT \cdot I$ . I say then  $I$  is equal to the circle  $EFN$ .  
For first, if it be possible, let  $I$  be less than the circle  $EFN$ , and let  $K$  be the excess or difference. Inscribe the Square  $EFGH$  in the circle  $EFN$ , <sup>a</sup> it being the half of a circumscribed square, and so greater than the semicircle. <sup>b</sup> Divide equally in two the arches  $EF$ ,  $FG$ ,  $GH$ ,  $HE$ , and at the points of the divisions join the Right-lines  $EL$ ,  $LF$ , &c. at  $L$  draw the tangent  $PQ$  (<sup>c</sup> which is parallel to  $EF$ ) and produce  $HEP$ ,  $GFQ$ ; then is the triangle  $ELF$  <sup>d</sup> the half of the Pgr.  $EPQF$ , and so greater than the half of the segment  $ELF$ ; and in like sort the rest of those triangles exceed the halves of the rest of the segments. And if the arches  $EL$ ,  $LF$ ,  $FM$ , &c. be again bisected, and the Right-lines joined, the triangles will likewise exceed the half of the segments. Wherefore if the square  $EFGH$  be taken from the circle  $EFN$ , and the triangles from the other segments, and this be done continually, at length <sup>e</sup> there will remain some magnitude less than  $K$ . Let us have gone so far, namely to the segments  $EL$ ,  $LF$ ,  $FM$ , &c. taken together less than  $K$ . Therefore  $I$  (the circle  $EFN - K$ )  $\supset$  the polyg.  $ELFMGNHO$  (the circle  $EFN$  - the segm.  $EL$ ,  $LF$ , &c.) In the circle  $ABT$  <sup>f</sup> conceive a like polygon  $AKBSCTDVF$  inscribed; therefore since  $AKBSCTDVF \cdot ELFMGNHO$  <sup>g</sup>  $:: ACq \cdot EGq$ ; the circle  $ABT \cdot I$ ; and the polyg.  $AKBSCTDVF$  <sup>h</sup>  $\supset$  the circle  $ABT$ . the polyg.  $ELFMGNHO$  <sup>i</sup> shall be  $\supset I$ ; but before,  $I$  was  $\supset ELFMGNHO$ , which is repugnant. (c) 1. 10. (f) 1. 12. (g) 30. 3. and 1. 11. (h) 1. 12. (i) 1. 12. (j) 1. 12. (k) 1. 12. (l) 1. 12. (m) 14. 5.

Again, if it be possible, let  $I$  be  $\supset$  the circle  $EFN$ . Therefore because  $ACq \cdot EGq :: ABT \cdot I$ ; and inversely  $I \cdot$  the circle  $ABT$  <sup>n</sup>  $:: EGq \cdot ACq$ ; suppose  $I \cdot$  the circle  $ABT ::$  the circle  $EFN \cdot K$ ; <sup>o</sup> therefore the circle  $ABT \supset K$ ; and  $EGq \cdot ACq ::$  the circle  $EFN \cdot K$ ; which is shewn to be repugnant. (n) 1. 12. (o) 1. 12. (p) 11. 5.

Therefore it must be concluded, that  $I =$  to the circle  $EFN$ .  $W. W.$  to be Dem.

S

Corol.



Corol.

Hence it follows, that as a circle is to a circle, so is a polygon described in one to a like polygon described in the other.

## Prop. III.

Every Pyramid  $ABDC$  having a triangular base, may be divided into two pyramids  $AEGH$ ,  $HIKC$ , equal, and like one to the other, having bases triangular, and like to the whole  $ABDC$ ; and into two equal prisms,  $BFG EIH$ ,  $EGDIHK$ ; which two prisms are greater than the half of the whole pyramid  $ABDC$ .

- D**ivide the sides of the pyramid into two parts at the points  $E, F, G, H, I, K$ ; and join the Right-lines  $EF, FG, GE, EI, IF, FK, KG, GH, HE$ . Because the sides of the pyramid are proportionally cut; <sup>(a)</sup> thence  $HI, AB$ ; and  $GF, AE$ ; and  $IF, DC$ ; and  $HG, DC$ , &c. are parallels; and consequently  $HI, FG$ ; and  $GH, FI$  are also parallels. Therefore it is apparent that the triangles  $ABD, AEG, EBF, FDG, HIK$ , <sup>(b)</sup> are equiangular; and that the four last are <sup>(c)</sup> equal: in like manner the triangles  $ACB, AHE, EIB, HIC, FGK$  are equiangular; and the four last are equal one to the other. Also the triangles  $BFI, FDK, IKC, EGH$ ; and lastly the triangles  $AHG, GDK, HKC, EFI$  are like and equal. Moreover the triangles,  $HIK$  to  $ADB$ , and  $EGH$  to  $BCD$ , and  $EFI$  to  $ADC$ , and  $FGK$  to  $ABC$ , <sup>(d)</sup> are parallel. From whence it evidently follows, first that the pyramids  $AEGH, HIKC$  are equal, and <sup>(e)</sup> like to the whole  $ABDC$ , and to one another. Next, that the solids  $BFG EIH, EGDIHK$  are prisms, and that of equal height, as being placed between the parallel planes  $ABD, HIK$ ; but the base  $BFG E$  is <sup>(f)</sup> double of the base  $FDG$ . <sup>(g)</sup> Wherefore the said prisms are equal; whereof the one  $BFG EIH$  is greater than the pyramid  $BEFI$ , that is, than  $AEGH$ , the whole than its part; and consequently the two prisms are greater than two pyramids, and so exceed the half of the whole pyramid  $ABDC$ . *W. W. to be Dem.*

Prop.

## Prop. IV.

If there be two Pyramids  $ABCD, EFGH$ , of the same altitude, having triangular bases  $ABC, EFG$ ; and either of them be divided into two pyramids ( $AILM, MNOD$ ; and  $EPRS, STVH$ ) equal one to the other and like to the whole, and into two equal prisms ( $IBKLMN, KLCNMO$ ; and  $PFQRST, QRGTSV$ ); and if in like manner either of these pyramids made by the former division be divided, and this be done continually; then as the base of one pyramid is to the base of the other pyramid, so are all the prisms which are in one pyramid, to all the prisms which are in the other pyramid, being equal in multitude.

**F**or (applying the construction of the precedent Prop.)  $BC \cdot KC :: FG \cdot GQ$ ; <sup>(a)</sup> therefore the triangle  $ABC$  is to the like triangle  $LKC$  as  $EFG$  is to the like  $RQG$ ; therefore by permutation  $ABC \cdot EFG :: LKC \cdot RQG$ ; <sup>(b)</sup> the prism  $KLCNMO \cdot QRGTSV$  (for these are of equal altitude) <sup>(c)</sup>  $IBKLMN \cdot PFQRST$ ; <sup>(d)</sup> wherefore the triangle,  $ABC \cdot EFG ::$  the prism  $KLCNMO - IBKLMN$ , the prism  $QRGTSV - PFQRST$ . *W. W. to be Dem.*

But if the pyramids  $MNOD, AILM$ ; and  $EPRS, STVH$ ; be further divided, in like manner the four new prisms made hereby shall be to the four produced before, as the bases  $MNO$  and  $ALI$  are to the bases  $STV$  and  $EPR$ ; that is, as  $LKC$  to  $RQG$ , or as  $ABC$  to  $EFG$ ; <sup>(e)</sup> wherefore all the prisms of the pyramid  $ABCD$  are to all the prisms of the pyramid  $EFGH$ , as the base  $ABC$  is to the base  $EFG$ . *W. W. to be Dem.*

## Prop. V.

Pyramids  $ABCD, EFGH$ , being under the same altitude, having triangular bases  $ABC, EFG$ , are one to another as their bases  $ABC, EFG$ , are.

**L**et the triangle  $ABC \cdot EFG :: ABCD \cdot X$ . I say  $X$  is equal to the pyramid  $EFGH$ . For if it be possible, let  $X$  be  $\neg EFGH$ ; and let the excess be  $T$ . Divide the pyramid  $EFGH$  into prisms and pyramids, and the other pyramids in like manner, <sup>(a)</sup> till the pyramids left  $EPRS, STVH$ , be less than the solid  $T$ . Therefore since the pyramid  $EFGH = X - T$ , it is manifest that the remaining prisms  $PFQRST, QRGTSV$  are greater than the solid  $X$ . Conceive the pyramid  $ABCD$  divided after the same manner; <sup>(b)</sup> then will be the prism  $IBKLMN - KLCNMO, PFQRST - QRGTSV :: ABC \cdot EFG$ ; <sup>(c)</sup> the pyr.  $ABCD \cdot X$ ; <sup>(d)</sup> therefore  $X \subset$  the prism  $PFQRST - QRGTSV$ ; which is contrary to that which was affirmed before.

S 2

Again,



Again, conceive  $X$  the pyr.  $EFGH$ , and make the pyr.  $EFGH$ .  
 (e) hyp. and  $\gamma :: X$  the pyr.  $ABCD :: EFG \cdot ABC$ . Because  $EFGH \perp$   
 cor. 4. 5.  $X$ ,  $\therefore$  thence  $\gamma \perp$  the pyr.  $ABCD$ , which is shewn before to be impossible.  
 (f) suppos.  
 (g) 14. 5.  $\therefore$  I conclude, that  $X$  is equal to the pyr.  $EFGH$ .  $W. W.$  to be  
 Dem.

## Prop. VI.

Pyramids  $ABCDEF$ ,  $GHIKLM$ , consisting under the same altitude, and having polygonous bases  $ABCDE$ ,  $GHIKL$ , are to one another as their bases  $ABCDE$ ,  $FHIKLM$  are.

Draw the Right-lines  $AC$ ,  $AD$ ,  $GI$ ,  $GK$ ; then is the base  $ABC$ .  
 $ACD ::$  the pyr.  $ABCF$ .  $ACDF$ ;  $\therefore$  therefore by composition,  
 $ABCF \cdot ACD ::$  the pyr.  $ABCF \cdot ACDF$ ;  $\therefore$  but also  $ACD$   
 $ADE ::$  the pyr.  $ACDF \cdot ADEF$ ;  $\therefore$  therefore of equality  $ABCF$   
 $ADE :: ABCDF \cdot ADEF$ ; and  $\therefore$  thence by composition  $ABCF$   
 $ADE ::$  the pyr.  $ABCF \cdot ADEF$ ; moreover  $ADE \cdot GKL$   
 $ADE ::$  the pyr.  $ADEF \cdot GKLM$ ; and, as before, and inversely  $GKL$   
 $GHIKL ::$  the pyr.  $GKLM \cdot GHIKLM$ ;  $\therefore$  therefore again of  
 equality  $ABCF \cdot GHIKL ::$  the pyr.  $ABCF \cdot GHIKLM$ .  
 $W. W.$  to be Dem.

If the bases have not sides of equal multitude, the demonstration will proceed thus. The base  $ABC \cdot GHI ::$  the pyr.  $ABCF \cdot GHIK$ ;  
 $\therefore$  and  $ACD \cdot GHI ::$  the pyr.  $ACDF \cdot GHIK$ ;  $\therefore$  therefore the base  
 $ABCD \cdot GHI ::$  the pyr.  $ABCF \cdot GHIK$ .  $\therefore$  Moreover the  
 base  $ADE \cdot GHI ::$  the pyr.  $ADEF \cdot GHIK$ ;  $\therefore$  therefore the base  
 $ABCDE \cdot GHI ::$  the pyr.  $ABCF \cdot GHIK$ .

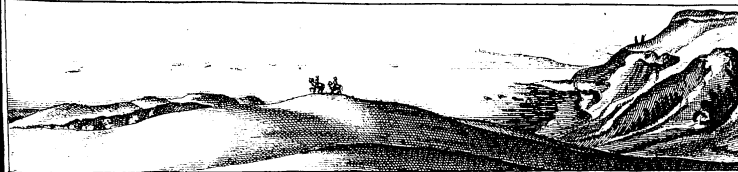
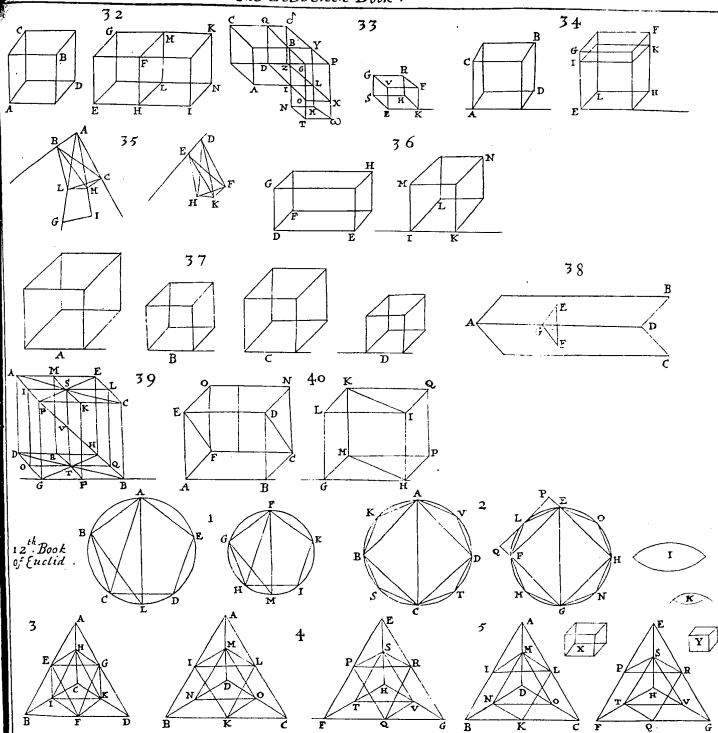
## Prop. VII.

Every prism,  $ABCDEF$ , having a triangular base, may be divided into three pyramids  $ACBF$ ,  $ACDF$ ,  $CDFE$ , equal one to the other, and having triangular bases.

Draw the diameters of the Parallelograms,  $AC$ ,  $CF$ ,  $FD$ : Then the triangle  $ACB$  is  $\triangle ACD$ ;  $\therefore$  therefore the pyramids of equal height  $ACBF$ ,  $ACDE$ , are equal. In like manner the pyr.  $DFAC$  is the pyr.  $DFEC$ ; but  $ACDF$  and  $DFAC$  are one and the same pyramid;  $\therefore$  therefore the three pyramids  $ACBF$ ,  $ACDF$ ,  $DFEC$ , into which the prism is divided, are equal one to the other.  $W. W.$  to be Dem.

Hence, every pyramid is the third part of the prism that has the same base and height with it; or every prism is treble of that pyramid that has the same base and height with it.

For





For resolve the polygonous prism  $ABCDEFGHIK$  into triangular prisms; and the pyramid  $ABCDEH$  into triangular pyramids; <sup>(a)</sup> then all the parts of the prism shall be treble to all the parts of the pyramid, <sup>(b)</sup> consequently the whole prism  $ABCDEFGHIK$  is treble to the whole pyramid  $ABCDEH$ . *W. W. to be Dem.*

## Prop. VIII.

*Like pyramids  $ABCD$ ,  $EFGH$ , which have triangular bases  $ABC$ ,  $EFG$ , are in triple proportion of that in which their sides of like proportion  $AC$ ,  $EG$  are.*

\* Compleat the Parallelepipedons  $ABICDMKL$ ,  $EFNGHQOP$ , <sup>(a)</sup> which <sup>(b)</sup> are like, and <sup>(c)</sup> sextuple of the pyramids  $ABCD$ ,  $EFGH$ ; <sup>(d)</sup> and therefore in the same proportion with them one to another, <sup>(e)</sup> that is, triple of that of the sides of like proportion, &c.

*Corol.*

Hence also, like polygonous pyramids have proportion tripled to that of the sides of like proportion; as may easily be proved by resolving the same into triangular pyramids.

## Prop. IX.

*See the prec. Scheme.*

*In equal pyramids  $ABCD$ ,  $EFGH$ , having triangular bases  $ABC$ ,  $EFG$ , the bases and altitudes are reciprocal; And pyramids having triangular bases, whose altitudes and bases are reciprocal, are equal.*

1. Hyp. **T**he compleated Parallelepipedons  $ABICDMKL$ ,  $EFNGHQOP$  are <sup>(a)</sup> sextuple of the equal pyramids  $ABCD$ ,  $EFGH$  (either of either) and so equal one to the other. Therefore the altitude <sup>(b)</sup>  $(H.)$  the alt.  $(D.)$  <sup>(c)</sup>  $ABIC$  .  $EFNG$  <sup>(d)</sup>  $ABC$  .  $EFG$ . *W. W. to be Dem.*

2. Hyp. The altitude  $(H.)$  the alt.  $(D.)$  <sup>(a)</sup>  $ABC$  .  $EFG$  <sup>(b)</sup>  $ABIC$  .  $EFNG$ ; <sup>(c)</sup> therefore the parallelepipedons  $ABICDMKL$ ,  $EFNGHQOP$  are equal; <sup>(d)</sup> consequently also the pyramids  $ABCD$ ,  $EFGH$ , being subsextuple of the same, are equal. *W. W. to be Dem.*

*The same is applicable to polygonous pyramids; for they may also in like manner be reduced to triangulars.*

*Corol.*



## Corol.

Whatever is demonstrated of pyramids in Prop. 6, 8, 9. do's likewise agree to any sort of prisms; seeing they are triple of the pyramids that have the same base and altitude with them. Therefore,

1. The proportion of prisms of equal altitude is the same with that of their bases.
2. The proportion of like prisms is triple of that of the sides of like proportion.
3. Equal prisms have their bases and altitudes reciprocal; and prisms which are so reciprocal, are equal.

## Scol.

From what is hitherto demonstrated the dimension of any prisms and pyramids may be collected.

- <sup>(a)</sup> 1. cor. 12. <sup>a</sup> The solidity of a prism is produced of the altitude multiplied into the base; <sup>b</sup> and therefore likewise that of a pyramid, of the third part of the altitude multiplied into the base.
- <sup>(b)</sup> 7. 12.

## Prop. X.

Every Cone is the third part of a Cylinder having the same base with it  $ABCD$ , and the altitude equal.

- See the second fig. of this Book. <sup>(a)</sup> 1. cor. 12. and sch. 4. and cor. 9. 12.
- <sup>(b)</sup> sch. 27. 3. and cor. 9. 12.
- <sup>(c)</sup> 5. ax. 1. <sup>(d)</sup> hyp. <sup>(e)</sup> cor. 7. 12.
- If you deny it, then first let such cylinder be more then triple to the cone, and let the excess be  $E$ . A prism described on a square in the circle  $ABCD$  <sup>a</sup> is subduple of a prism described upon a square about the circle, being equal to it and the cylinder in height. Therefore a prism upon the square  $ABCD$  exceeds the half of the cylinder; and likewise a prism upon the base  $AFB$ , of equal height to the cylinder, <sup>b</sup> is greater than the half of the segment of the cylinder  $AFB$ ; continue an equal bisection of the arches, and subtract the prisms till the remaining segments of the cylinder, namely at  $AF, FB$ , &c. become less than the solid  $E$ . Therefore the cyl. — segm.  $AF, FB$ , &c. (the prism on the base  $AFBGCHDI$ ) <sup>c</sup> is greater than the cylinder —  $E$  (<sup>d</sup> the triple of the cone;) therefore the pyramid, <sup>e</sup> a third part of the said prism (being placed on the same base, and of the same height) is greater than the cone of equal height on the base  $ABCD$  a circle, i. e. the part greater than the whole. Which is Absurd.

But

But if the cone be affirmed to be greater than the third part of the cylinder, then let the excess be  $E$ . Detract the pyramids from the cone, as you did in the first part the prisms from the cylinder, till some segments of the cone remain, conceive at  $AF, FB, BG$ , &c. less than the solid  $E$ . Therefore the cone —  $E$  (<sup>a</sup>  $\frac{1}{3}$  of the cylin.)  $\supset$  the pyr.  $AFBGCHDI$  (<sup>b</sup>) hyp. (the cone — segm.  $AF, FB$ , &c.) therefore the prism triple to the pyramid (*viz.* of equal height, and on the same base) is greater than the cylinder on the base  $ABCD$ , the part than the whole. Which is Absurd. Wherefore it must be granted, that the cylinder is equal to triple of the cone. *W. W. to be Dem.*

## Prop. XI.

Cylinders and Cones  $ABCDK$ ,  $EFGHM$ , being under the same altitude, are to one another as their bases  $ABCD$ ,  $EFGH$ , are.

Let the circle  $ABCD$ . the cir.  $EFGH$  :: the cone  $ABCDK$ .  $N$ . I say  $N$  is equal to the cone  $EFGHM$ .

For if it be possible, let  $N$  be  $\supset$  the cone  $EFGHM$ , and let the excess be  $O$ . The preparation and argumentation of the prec. Prop. being supposed; then shall  $O$  be greater than the segments of the cone  $EP, PF, FQ$ , &c. and so the solid  $N \supset$  the pyr.  $EPFQGRHSM$ . In the circle  $ABCD$  <sup>a</sup> make a like polygonous fig.  $ATBVCXDT$ . Because the pyr.  $ABPTK$ . the pyr.  $EFQSM$  <sup>b</sup> :: the polyg.  $ATBVT$ . the polyg.  $EPFQS$  <sup>c</sup> :: the cir.  $ABCD$ . the cir.  $EFGH$  <sup>d</sup> :: the cone  $ABCDK$ .  $N$  <sup>e</sup> thence the pyr.  $EPFQGRHSM$  shall be  $\supset N$ . Contrary to what was affirmed before. Again conceive  $N \sqsubset$  the cone  $EFGHM$ ; and make the cone  $EFGHM$ .  $O :: N$ . the cone  $ABCDK$  <sup>f</sup> :: the cir.  $EFGH$ .  $ABCD$ ; <sup>g</sup> therefore  $O \supset$  the cone  $ABCDK$ . Which is Absurd, as appears by what is shewn in the first part. Therefore rather admit  $ABCD$ .  $EFGH$  :: the cone  $ABCDK$ .  $EFGHM$ . *W. W. to be Dem.*

The same may be demonstrated of cylinders, if cylinders and prisms be conceived in the place of cones and pyramids. Therefore, &c.

## Scol.

Hence, is gathered the dimension of all sorts of cylinders and cones. The solidity of a Right cylinder is produced of the circular base (<sup>a</sup> the dimension whereof is to be learnt out of Archimedes) multiplied into the height, <sup>b</sup> whence in like manner that of every cylind.

Therefore the solidity of a cone is produced of the third part of the altitude multiplied in the base.

Prop.



## Prop. XXII.

Like Cones and Cylinders  $ABCDK$ ,  $EFGHM$ , are in triple proportion of that of the diameters  $TX$ ,  $PR$ , of their bases  $ABCD$ ,  $EFGH$ .

**L**et the cone  $A$  have to  $N$  triple proportion of  $TX$  to  $PR$ . I say  $N$  is = the cone  $EFGHM$ . For if it be possible let  $N$  be  $\neq$   $EFGHM$ ; and let the expts be  $O$ ; therefore,  $N \neq$  the pyr.  $EPFQGRHS$ . Let the axes of the cones be  $IK$ ,  $LM$ , and join the Right-lines  $VK$ ,  $CK$ ,  $VI$ ,  $CI$ , and  $QM$ ,  $GM$ ,  $QL$ ,  $GL$ . Because the cones are like, <sup>a</sup> thence  $VI \cdot IK :: QL \cdot LM$ ; but the angles  $VIK$ ,  $QLM$  are Right-angles; <sup>c</sup> therefore the triangles  $VIK$ ,  $QLM$  are equiangular. <sup>d</sup> whence  $VC \cdot VI :: QG \cdot QL$ ; also  $VI \cdot VK :: QL \cdot QM$ ; therefore of equality  $VC \cdot VK :: QG \cdot QM$ ; <sup>e</sup> moreover  $VK \cdot CK :: QM \cdot MG$ . Therefore again of equality  $VC \cdot CK :: QG \cdot GM$ ; <sup>f</sup> therefore the triangles  $VKG$ ,  $QMG$  are like: and by the same reason the other triangles of this pyramid are like to the other of that; <sup>g</sup> wherefore the pyramids themselves are like. <sup>h</sup> But they are in triple proportion of that of  $VC$  to  $QG$ ; <sup>i</sup> that is, of  $VI$  to  $RL$ ; <sup>j</sup> or  $TX$  to  $PR$ ; <sup>k</sup> therefore that of the pyr.  $AIRFCXYDK$ , the pyr.  $EPFQGRHSM$   $\neq$  the cone  $ABCDK$   $\cdot N$ ; <sup>l</sup> whence the pyr.  $EPFQGRHSM$   $\neq$   $N$ , which is repugnant to what was affirmed before.

Again, take  $N$  = the cone  $EFGHM$ ; make the cone  $EFGHM$ .  $O :: N$ , the cone  $ABCDK$   $o ::$  the pyr.  $EPRM$ .  $ATCK$   $o :: GQ$   $VC$  thrice  $o :: PR \cdot TX$  thrice; but  $O$  is  $\neq$   $ABCDK$ ; which was before shewn to be repugnant. Wherefore  $N$  = the cone  $EFGHM$ . <sup>W. W. to be Dem.</sup>

But forasmuch as what proportion soever cones have, also cylinders, being triple of them, have the same; therefore cylinder to cylinder shall have proportion triple of the diameters of the bases.

## Prop. XIII.

If a Cylinder  $ABCD$ , be divided by a plane  $EF$  parallel to the opposite planes  $BC$ ,  $AD$ , then as one Cylinder  $Aefd$  is to the other Cylinder  $EBCF$ , so is the axis  $GI$  to the axis  $Ih$ .

**T**he axis being produced, <sup>a</sup> take  $GK = GI$ , and  $HL = Ih = LM$ ; and conceive planes drawn at the points  $K$ ,  $L$ ,  $M$ , parallel to the circles  $AD$ ,  $BC$ ; <sup>b</sup> therefore the cylinder  $FD$  = the cyl.  $AN$ ; and the cyl.  $EC$  =  $BO$  =  $OP$ ; therefore the cylinder  $EN$  is as multiplex of the cylinder  $ED$ , as the axis  $IK$  is of the axis  $IG$ ; and in like manner the cylinder  $FP$  is as multiplex of the cylinder  $BE$ , as the axis  $IM$  is of the axis  $Ih$ ; but as  $IK$  is  $o :: IM$ , <sup>c</sup> so is the cylinder  $EN$  =  $o :: FP$ ; <sup>d</sup> therefore the cylinder  $Aefd$  . the cyl.  $EBCF$   $o :: GI \cdot Ih$ . <sup>W. W. to be Dem.</sup>

## Prop. XIV.

Cones  $AEB$ ,  $CFD$ , and Cylinders  $AH$ ,  $CK$ , consisting upon equal bases  $AB$ ,  $CD$ , are to one another as their altitudes  $ME$ ,  $NF$  are.

**T**he cylinder  $HA$ , and the axis  $EM$  being produced, take  $ML = FN$ ; and at the point  $L$  draw a plane parallel to the base  $AB$ , <sup>a</sup> then shall the cyl.  $AP$  be =  $CK$ ; <sup>b</sup> but the cyl.  $AH \cdot AP$   $(CK) :: ME \cdot ML$   $(NE)$ . <sup>WW to be Dem.</sup>

The same may be affirmed of cones subtriple of cylinders; <sup>\*</sup> as also of prisms, <sup>\*</sup> and pyramids. <sup>apply 9. and 7. 12.</sup>

## Prop. XV.

In equal cones  $BAC$ ,  $EDF$ , and Cylinders  $BH$ ,  $EK$ , the bases and altitudes are reciprocal  $(BC \cdot EF :: MD \cdot LA)$ : And cones and cylinders, whose bases and altitudes are reciprocal, are equal one to the other.

**I**f the altitudes be equal then the bases are equal too, and the thing is evident. If unequal, then take away  $MO = LA$ . <sup>(a) 14. 12. (b) cor. 1. (c) hyp. (d) 11. 12. (e) hyp. (f) 11. 12. (g) 11. 5. (h) 11. 12. (i) 9. 5.</sup>  
1. Hyp. Then is  $MD \cdot MO$   $(LA)$   $o ::$  cyl.  $EK \cdot (BH) EQ$ .  
<sup>a</sup>  $o ::$  the cir.  $BC \cdot EF$ . Which was to be Dem.  
2. Hyp.  $BC \cdot EF$   $o :: DM \cdot OM$   $(LA)$   $o ::$  the cyl.  $EK \cdot EQ$ . <sup>(b) 11. 12. (c) 9. 5.</sup> Therefore the cylind.  $EK = BH$ . Which was to be Dem.

The same argument may be used for cones.

## Prop. XVI.

Two unequal circles  $ABCG$ ,  $DEF$ , having the same center  $M$ , to inscribe in the greater circle  $ABCG$ , a polygonous figure of equal and even sides, which shall not touch the lesser circle  $DEF$ .

**T**hrough the center  $M$  draw the line  $AC$ , cutting the circle  $DEF$  in  $F$ , from whence raise a perpendicular  $FH$ ; <sup>a</sup> divide the semicircle  $ABC$  into two equal parts; and the half thereof  $BC$  also; and so do continually, till the arch  $IC$  become less than the arch  $HC$ , from  $I$  let fall the perpendicular  $IL$ . It is manifest that the arch  $IC$  measures the whole circle, and that the number of arches is even, and so that the subtended line  $IC$  is the side of the polygonon that may be inscribed without touching the lesser circle  $DEF$ . For  $HG$  touches the circle  $DEF$ , to which  $IK$  is parallel, and placed outwardly; <sup>b</sup> wherefore  $IK$  does not touch the circle  $DEF$ ; much less do  $CI$ ,  $CK$ , and the other sides of this polygonon more remote from the center. <sup>(a) 30. 3. (b) 1. 10. (c) sch. 16. 4. (d) cor. 16. 3. (e) 28. 1. (f) 34. def. 1.</sup>

<sup>W. W. to be Done.</sup>

Corol. Observe that  $IK$  touches not the circle  $DEF$ .

Prop.



## Prop. XVII.

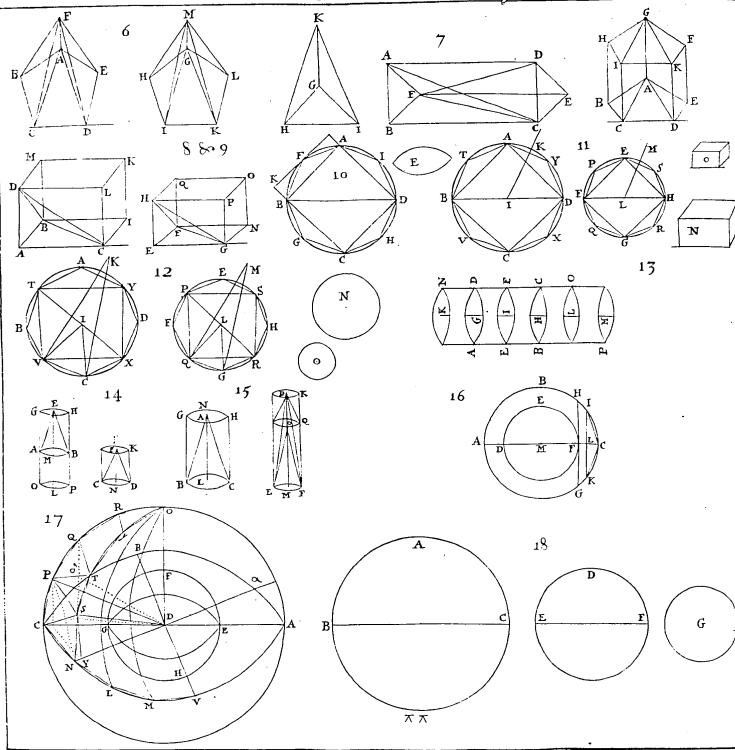
Two spheres  $ABCV$ ,  $EFGH$ , consisting about the same center  $D$ , being given, to inscribe a solid of many sides (or Polyedron) in the greater sphere  $ABCV$ , which shall not touch the superficies of the lesser sphere  $EFGH$ .

**L** Et both the spheres be cut by a plane passing by the center making the circles  $EFGH$ ,  $ABCV$ ; and the diameters  $AC$ ,  $BF$  drawn, cutting perpendicularly. In the circle  $ABCV$ , <sup>a</sup> inscribe the equilateral polygon  $VMLNC$ , &c. not touching the circle  $EFGH$ : then draw the diameter  $Na$ , and erect  $DO$  perpendicular to the plane  $ABC$ ; by  $DO$ , and by the diameters  $AC$ ,  $Na$ , conceive planes  $DOC$ ,  $DON$  erected, which shall be <sup>b</sup> perpendicular to the circle  $ABCV$ , and so in the superficies of the sphere make <sup>c</sup> the quadrants  $DOC$ ,  $DON$ . In which let the right lines  $CP$ ,  $PQ$ ,  $QR$ ,  $RO$ ,  $NS$ ,  $ST$ ,  $T\gamma$ ,  $\gamma O$ ; <sup>d</sup> be fitted, equal, and of equal multitude with  $CN$ ,  $NL$ , &c. make the same construction in the other quadrants  $OL$ ,  $OM$ , &c. and in the whole sphere. Then I say the thing required is done.

From the points  $P$ ,  $S$ , to the plane  $ABCV$  draw the perpendiculars  $PX$ ,  $ST$ , <sup>e</sup> which shall fall on the sections  $AC$ ,  $Na$ . Therefore because both <sup>f</sup> the Right-angles  $PXC$ ,  $STN$ , <sup>g</sup> and  $PCX$ ,  $SNT$  insiting on <sup>h</sup> equal circumferences, <sup>i</sup> are equal, the triangles also  $PXC$ ,  $SNT$  <sup>j</sup> are equiangular. Wherefore being  $PC = SN$ , <sup>k</sup> also is  $PX = ST$ , <sup>l</sup> and  $KC = TN$ ; <sup>m</sup> whence  $DX = DT$ ; <sup>n</sup> and therefore  $DX : XC :: DT : TN$ ; <sup>o</sup> therefore  $TX$ ,  $NC$  are parallels; but because  $PX$ ,  $ST$  are equal, and since being perpendicular to the same plane  $ABCV$ , they are also <sup>p</sup> parallels, <sup>q</sup> therefore  $TX$ ,  $SP$  shall be equal and parallels; <sup>r</sup> whence  $SP$ ,  $NC$ , are parallel one to the other; and so the <sup>s</sup> quadrilateral  $NCP S$ , and by the same reason  $SPQT$ ,  $TQRG$ , as also the <sup>t</sup> triangle  $\gamma RO$  are so many planes. In like manner the whole sphere may be shewn full of such quadrilaterals and triangles; wherefore the figure inscribed is a polyedron.

From the center  $D$  draw  $DZ$ , perpendicular to the plane  $NCP S$ ; and join  $ZN$ ,  $ZC$ ,  $ZS$ ,  $ZP$ . Because  $DN : NC :: DT : TX$ , thence  $NC$  is <sup>u</sup>  $\perp TX$  ( $SP$ ), and likewise  $SP = TQ$ , and  $TQ \perp \gamma R$ . And because the angles  $DZC$ ,  $DZN$ ,  $DZS$ ,  $DZP$ , <sup>v</sup> are right, and the sides  $DC$ ,  $DN$ ,  $DS$ ,  $DP$ , <sup>w</sup> equal, and  $DZ$  common, <sup>x</sup> thence  $ZC$ ,  $ZN$ ,  $ZS$ ,  $ZP$ , are equal one to the other; and consequently about the quadrilateral  $NCP S$ , <sup>y</sup> a circle may be described, in which (because  $NS$ ,  $NC$ ,  $CP$ , are <sup>z</sup> equal, and  $NC \perp SP$ )  $NC$  <sup>a</sup> subtends more then the quadrant, <sup>b</sup> therefore the ang.  $NZC$  at the center is obtuse. <sup>c</sup> Therefore  $N C q \perp Z \gamma q$  ( $Z C q \perp Z N q$ ). Let  $NI$  be drawn perpendicular to  $AC$ ; therefore since the angle  $ADN$  ( $\perp DNC \perp DCN$ ) <sup>d</sup> is obtuse, the half of it  $DCN$ , shall be greater then the half of a right angle; <sup>e</sup> and so that which remains





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remains of the right ang.  $CNI$  shall be less than it; whence  $IN \perp IC$ ; therefore  $NC \perp q$  ( $NI \perp q \rightarrow IC \perp q$ ) <sup>(n) 19. 1.</sup> therefore  $IN \perp ZC$ , and consequently  $DZ \perp DI$ , but the point  $I$  is <sup>(o) 47. 1.</sup> without the sphere  $EF GH$ , and so much more the point  $Z$ . Wherefore the plane  $NCP S$ , (whose next point to the center is  $Z$ ) does not touch the sphere  $EF GH$ . And if a perpendicular  $D\delta$  be drawn to the plane  $SPQT$ , the point  $\delta$ , and so also the plane  $SPQT$  is yet further removed from the center, which is also true of the other planes of the polyhedron. Therefore the polyhedron  $ORQPCN$ , &c. inscribed in the greater sphere, does not touch the lesser. *W. W. to be Dem.*

*Corol.* Hence it follows, that if in any other sphere a solid polyhedron, like to the above-said solid polyhedron be inscribed, the proportion of the polyhedron in one sphere to the polyhedron in the other is triple of that of the diameters of the spheres.

For if right-lines be drawn from the centers of the spheres to all the angles of the bases of the said polyhedrons, then the polyhedrons will be divided into pyramids equal in number and like: whose homologous sides are semidiameters of the spheres, as appears, if the lesser of these spheres be conceived described within the greater about the same center. For the right-lines drawn from the center of the sphere to the angles of the bases will agree one to the other by reason of the likeness of the bases; and so will like pyramids be made. Wherefore since every pyramid in one sphere, to every pyramid like it in the other sphere <sup>(a) cor. 5. 12.</sup> has proportion triple to that of the homologous sides, that is, of the semidiameters of the spheres; and <sup>(b) 12. 5.</sup> as one pyramid is to one pyramid, so all the pyramids, that is, the solid polyhedron composed of these, are to all the pyramids, that is, the solid polyhedron composed of the others; therefore the polyhedron of one sphere shall have to the polyhedron of the other sphere, proportion triple of that of the semidiameters, <sup>(c) 15. 5.</sup> and so of the diameters of the spheres.

Prop. XVIII.

Spheres  $BAC$ ,  $EDF$ , are in triple proportion one to the other of that in which their diameters  $BC$ ,  $EF$ , are.

Let the sphere  $BAC$  be to the sphere  $G$  in triple proportion of that of the diameter  $BC$  to the diameter  $EF$ , I say  $G = EDF$ . For if it be possible, let  $G$  be  $\neq EDF$ ; and conceive the sphere  $G$  concentric with  $EDF$ . In the sphere  $EDF$  inscribe a polyhedron not touching the sphere  $G$ , and a like polyhedron in the sphere  $BAC$ . These polyhedrons are in triple proportion of the diameters  $BC$ ,  $EF$ , that is, of the sphere  $BAC$  to  $G$ . Consequently the sphere  $G$  is greater than the polyhedron inscribed in the sphere  $EDF$ , the part then the whole. <sup>(a) 17. 12.</sup> <sup>(b) cor. 17. 12.</sup> <sup>(c) hyp.</sup> <sup>(d) 14. 5.</sup>

Again, if it be possible, let the sphere  $G$  be  $\neq EDF$ , and as the sphere  $EDF$  is to another sphere  $H$ , so let  $G$  be to  $BAC$ , that is, in triple proportion of the diameter  $EF$  to  $BC$ , therefore since  $BAC \perp H$ , we shall incur the absurdity of the first part, wherefore rather the sphere  $G = EDF$ . *W. W. to be Dem.*

*Corol.* Hence, As one sphere is to another sphere, so is a polyhedron described in that to a like polyhedron described in this.



THE  
DOCTRINE  
OF  
SURDS.

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Printed at LONDON, by *Anne Godbid,*  
and *John Playford,* 1680.





THE  
DOCTRINE  
OF  
SURDS.

CHAP. I.  
REDUCTION.

SECT. I.

*To reduce a Rational quantity to the forme of a Surd, which shall have the same Radical sign with any Surd prescribed.*

**I**nvolve (or multiply it *per se*) as often as there are Units in the Index of the assigned power, and prefix it's sign.

*The*



## The Operation in Species.

Reduce  $b$  to the same sign with

$$\sqrt{(3)}n^2.$$

$$\sqrt{(3)}b^1.$$

Reduce  $b-d$  to  $\sqrt{(2)}b-d$ .

$$\frac{-bd-1.d^2}{b^2-bd}$$

$$\sqrt{(2)}b-2bd-1.d^2$$

Reduce the Numerator of this Fraction  $\frac{a}{\sqrt{b}}$  to the sign  $\sqrt{b}$  the Denominator..

$$\frac{a}{a}$$

$$\frac{a}{\sqrt{a^2}}$$

Reduce the Denominator ( $5d$ ) of this Fraction  $\frac{\sqrt{(3)ac}}{5d}$  to the sign  $\sqrt{(3)ac}$  the Numerator.

$$\frac{5d}{5d}$$

$$\frac{25d^2}{5d}$$

$$\sqrt{(3)125d^3}$$

## The Operation in Numbers.

Reduce 6 to the sign  $\sqrt{(3)}12$ .

$$\frac{6}{36}$$

$$\frac{6}{\sqrt{(3)216}}$$

Reduce 5 to the sign  $\sqrt{7}$ .

$$\frac{5}{25}$$

$$\sqrt{25}$$

Reduce the Numerator 3 of this Fraction  $\frac{3}{\sqrt{7}}$  to the sign  $\sqrt{7}$ .

$$\frac{3}{3}$$

$$\frac{3}{\sqrt{9}}$$

Reduce the Denominator 7 of this Fraction  $\frac{\sqrt{(3)4}}{7}$  to the sign  $\sqrt{(3)4}$  the Numerator.

$$\frac{7}{7}$$

$$\frac{49}{7}$$

$$\sqrt{(3)343}$$

## SECT. II.

To reduce simple heterogeneous Surds, that is, such as are under different radical signs to homogeneous, or to such as may have a common radical line.

Divide the Indices of the proposed powers by their greatest common measure, multiplying the said Indices by each others quotients cross-wise, and before the Product set  $\sqrt{\quad}$  with its Index for the common radical line; then

then multiply the powers themselves alternately into the Species denominated by each others quotient.

Reduce  $\sqrt{a^2}$  and  $\sqrt{(4)}b^2$ .

$$\frac{2)\sqrt{a^2}}{1} \times \frac{\sqrt{(4)}b^2}{2}$$

$$\sqrt{(4)}b^2 \quad \sqrt{(4)}a^4$$

Reduce  $\sqrt{5}$  and  $\sqrt{(4)}7$ .

$$\frac{1)\sqrt{5}}{2} \times \frac{\sqrt{(4)}7}{4}$$

$$\sqrt{(8)}49 \quad \sqrt{(5)}625$$

## SECT. III.

To reduce a Surd to another more Simple when it may be done.

**VV**hen the power of a Surd quantity, the radical sign being omitted, can be divided just without any remainder, by a power which hath a rational Root of the same kind with that which is denoted by the said radical sign; divide the Surd quantity proposed by that rational Root, and prefix this Root before the Quotient; so have you a new Surd equal to the proposed, and in more simple terms.

But when a Square or Cube &c. by which the division necessary to such contraction is to be performed, cannot be readily discerned, first search out all the Divisors of the power of the Surd quantity proposed, and then see whether any of them be a Square or Cube &c. viz. such a power as the radical sign denotes, which if you find, you may use in the aforesaid manner, to free the Surd quantity in part from the radical line.

$\sqrt{48}a^2$  will be reduced to  $a\sqrt{48}$   
or  $2a\sqrt{12}$ , or  $4a\sqrt{3}$ .

$\sqrt{16}aab$  may be reduced to  
 $4a\sqrt{b}$ .

$\sqrt{(3)}cb^3r$  will become  
 $b\sqrt{(3)}cr$ .

$\frac{\sqrt{16}a^2b}{c}$  will become  
 $\frac{4a}{c}\sqrt{b}$ .

$\sqrt{72}$  may be reduced to  
 $6\sqrt{2}$ .

$\sqrt{75}$  may be reduced to  
 $5\sqrt{3}$ .

$\sqrt{(3)}72$  will become  
 $2\sqrt{(3)}9$ .

$\frac{\sqrt{75}}{2}$  will become  
 $\frac{5}{2}\sqrt{3}$ .



## SECT. IV.

*Of the Commensurability of Surds.*

Commensurable Surds are such as being reduced to their least terms, become true figurative quantities of their kind; and are therefore as a rational quantity to a rational.

## SECT. V.

*To try whether any Quantities proposed be commensurable or not.*

First, if they be of different kinds, reduce them to one kind; then divide them severally by their greatest common measure, and if the quotients be rational quantities, the Surds proposed are commensurable; but if the quotients be irrational they are incommensurable.

If two Surd quantities be divided by some common divisor, tho it be not the greatest, yet if there come forth rational quotients, those Surds are commensurable.

If Surd Fractions be proposed that have not a common denominator, reduce them to their smallest common denominator, and then try whether the new Surd numerators be commensurable or not, for if those be commensurable, the Surd Fractions first proposed are commensurable.

But if either the numerators or denominators of two Surd Fractions, or mixt numbers standing Fraction wise (the radical sign being neglected) be powers of that kind which is denoted by the radical sign, then they need no reduction, but try whether their numerators or denominators be commensurable or not; for if these be commensurable, the Surd Fraction proposed shall be also commensurable, as  $\sqrt{\frac{3}{2}}$  and  $\sqrt{\frac{2}{3}}$ .

## CHAP.



## CHAP. II.

*Multiplication of Simple Surds.*

1. IF the quantities to be multiplied be of the same kind, multiply them one by the other; and to the product præfix the common radical sign. But if they be heterogenous or of different kinds, reduce them first to one kind, and then multiply them.

Multi. by	$\sqrt{240}$ $\sqrt{15}$	$\sqrt{15}$ $\sqrt{26}$	$\sqrt{32}$ $\sqrt{48}$	$\sqrt{(3)7\frac{1}{2}}$ $\sqrt{(3)\frac{1}{2}}$	$\sqrt{(+)}15$ $\sqrt{(+)}7$	
Product	$\sqrt{3600}$	$\sqrt{390}$	$\sqrt{1536}$	$\sqrt{(3)5\frac{1}{2}}$	$\sqrt{(+)}105$	
Multi. by	$\sqrt{8}$ $\sqrt{(3)4}$	} that is {		$\sqrt{(6)5^{12}}$ $\sqrt{(6)16}$	$\sqrt{9}$ $\sqrt{(3)27}$	$\sqrt{(3)32}$ $2$
Product				$\sqrt{(6)8192}$	$\sqrt{(6)531441}$	$\sqrt{(3)256}$

2. When a Surd is to be multiplied by a rational quantity, it will be sometimes convenient only to connex them together, or prefix the rational quantity to the left hand of the Surd. As to multiply  $\sqrt{27}$  by 6 the product will be  $6\sqrt{27}$ , so 12 multiplied by  $\sqrt{(3)5}$ , the product will be  $12\sqrt{(3)5}$  &c.

3. When two rational quantities are thus prefix to two Surds of the same kind, multiply the rational part by the rational, and the Surd by the Surd, which products joined together, is the product required. As to multiply  $6\sqrt{(3)7}$  by  $5\sqrt{(3)3}$  the product will be  $30\sqrt{(3)21}$ , and  $\sqrt{(4)6}$  multiplied by  $3\sqrt{(4)7}$  will make  $3\sqrt{(4)42}$ ;  $5\sqrt{2}$  multiplied by  $4\sqrt{5}$  makes  $20\sqrt{10}$ .

4. When any Surd is to be multiplied in itself according to the index of its own power, cast away the radical sign, and take the quantity remaining for the product, which in this case will be always rational. As the Square of  $\sqrt{11}$  will be 11, the Cube of  $\sqrt{(3)17}$ , will be 17. Also  $2\sqrt{3}$  multiplied by  $8\sqrt{3}$  makes 48, and  $3\sqrt{5}$  multiplied by  $2\sqrt{5}$  makes 30 &c.

V 2

5. If



5. If a Surd whose index is a Compound number, be to be multiplied in it self according to the index of either of the compounding Species; the root of the other Species shall only be prefixt to the special quantity.

As to Square  $\sqrt{(4)} 12$ , the product will be  $\sqrt{12}$ , so the Square of  $\sqrt{(6)} 15$  will be  $\sqrt{(3)} 15$ , the biquadrat of  $\sqrt{5}$  will be  $25$ , the Cube of  $\sqrt{(6)} 64$ , will be  $\sqrt{64}$  or  $8$  &c.

## C H A P.



## C H A P. III.

## Division of Simple Surds.

1. IF the Surds be of the same kind divide one by the other, and to the quotient prefix the common radical sign, which new root is the quotient sought, but if they be not of the same kind first reduce them, and then divide.

Divide by	$\sqrt{576}$ $\sqrt{9}$	$\sqrt{256}$ $\sqrt{8}$	$\sqrt{(4)} 35$ $\sqrt{(4)} 5$	$9$ $\sqrt{(3)} 21$
Quot.	$\sqrt{64}$ or $8$	$\sqrt{32}$	$\sqrt{(4)} 7$	$\sqrt{(3)} \frac{3}{21}^2$ or $\sqrt{(3)} 34 \frac{2}{3}$
Divide by	$\sqrt{b}$ $\sqrt{a}$	$\sqrt{abdg}$ $\sqrt{ab}$	$\sqrt{bl}$ $l$	
Quot.	$\sqrt{\frac{b}{a}}$	$\sqrt{dg}$	$\sqrt{\frac{b}{l}}$	

2. When a rational quantity is to be divided by its Square Root, the Root will be the quotient. As  $ab$ , divided by  $\sqrt{ab}$  the quotient will be  $\sqrt{ab}$ , and  $50$  divided by  $\sqrt{50}$  the quotient will be  $\sqrt{50}$ , &c.

3. When a Surd with a prefixt rational quantity is to be divided by the same Surd, the quotient will be the said prefixt rational quantity. As  $5\sqrt{7}$  divided by  $\sqrt{7}$  gives  $5$  for the quotient, or  $5\sqrt{7}$  divided by  $5$  will give  $\sqrt{7}$  in the quotient, &c.

4. When the Dividend and Divisor, are two rational quantities prefixed severally to one common Surd; divide the rational part of the Dividend by the rational part of the Divisor, and the quotient sought is produced thereby. As  $8\sqrt{5}$  divided by  $2\sqrt{5}$  the quotient will be  $4$ ; also  $8\sqrt{(3)} 7$  divided by  $4\sqrt{(3)} 7$  gives  $2$  in the quotient.

5. When



5. When the Dividend and Divisor are two rational quantities prefix to two unequal Surds, divide the rational part of the Dividend by the rational part of the Divisor, and the Surd part by the Surd part, which two quotients connexed together make the quotient desired. As  $4\sqrt{13}$  divided by  $2\sqrt{26}$ , the quotient will be  $2\sqrt{\frac{13}{26}}$  or  $2\sqrt{\frac{1}{2}}$ . So  $4\sqrt{30}$  divided by  $2\sqrt{10}$  the quotient will be  $2\sqrt{3}$ . Also  $5\sqrt{(3)20}$  divided by  $3\sqrt{(3)4}$  the quotient will be  $\frac{5}{3}\sqrt{(3)5}$ , and  $5\sqrt{8}$  divided by  $\sqrt{8}$  gives 5 in the quotient, &c.

## C H A P.



## C H A P. IV.

*Addition and Subtraction of Surds, both Simple and Compound.*

**I**F the Surds proposed be not of one kind, reduce them to one kind; and then if they be commensurable multiply the Sum of the rational quantities by the common measure, and the product shall be the Sum of the Surds proposed; or multiply the difference of the rational parts by the common measure, and the product shall be the difference of the Surds proposed; or instead of multiplying, subjoin the rational part, to the Sum or difference of the rational parts.

*Example in Species.*

Admit  $\sqrt{8b^2}$  to be added to  $\sqrt{32b^2}$ , their greatest common measure will be  $\sqrt{8}$ , by which they'll be reduced to their least terms  $\sqrt{1b^2}$  and  $\sqrt{4}$ , that is  $1b$  and  $2b$  whose Sum  $3b$  Squared, makes  $9b^2$  and multiplied by  $\sqrt{8}$  the common measure makes  $\sqrt{72b^2}$  the Sum of the two given Surds. But if we take  $1b$  from  $2b$  the remains  $1b$  Squared is  $b^2$  which multiplied by  $\sqrt{8}$  the greatest common measure makes  $\sqrt{8b^2}$  the difference of the given Surds, which may otherwise be expressed thus according to the latter clause of the rule,  $3b\sqrt{8}$  the Sum,  $b\sqrt{8}$  the difference.

*Examples in Numbers.*

Admit  $\sqrt{8}$  and  $\sqrt{32}$  to be added, their greatest common measure is  $\sqrt{8}$ , by which they'll be brought to  $\sqrt{1}$  and  $\sqrt{4}$  or 1 and 4 whose Sum is 5 and difference 3, which Squared make 25 and 9, and being multiplied by  $\sqrt{8}$  the common measure, makes  $\sqrt{200}$  the Sum, or  $\sqrt{72}$  the difference, which may stand otherwise thus  $5\sqrt{8}$  the Sum,  $3\sqrt{8}$  the difference.

To add  $\sqrt{(3)81}$  to  $\sqrt{(3)192}$ , their greatest common measure is  $\sqrt{3}$ , and they in their least terms  $\sqrt{(3)27}$  and  $\sqrt{(3)64}$ , that is, 3, and 4, the Sum whereof is 7 and diff. 1, which being cubed make 343 and 1, and these multiplied in  $\sqrt{(3)}$  the common measure make  $\sqrt{(3)1225}$  for the Sum, and  $\sqrt{(3)3}$  the difference, or thus  $7\sqrt{(3)3}$  the Sum, and  $1\sqrt{(3)3}$  the difference.

But



2. But if the quantities to be added or subtracted be incommensurable, add and subtract them by the signs + and -; whence arise Surds Binomial and residual. Thus  $\sqrt{6}$  and  $\sqrt{7}$  their Sum is  $\sqrt{6} + \sqrt{7}$ , and difference  $\sqrt{7} - \sqrt{6}$ .

3. Incommensurable Square roots may be added or subtracted thus; To the Sum of the Squares of the given Surds, add their double rectangle, or subtract the said double rectangle from the Sum of the Squares, the Square root of the Sum or remainder is the Sum or difference of the Surds proposed.

As to find the Sum and difference of  $\sqrt{14}$  and  $\sqrt{12}$ , their Squares are 14 and 12 whose Sum is 26, and the double rectangle of  $\sqrt{14}$  and  $\sqrt{12}$  is  $2\sqrt{168}$ , and consequently  $\sqrt{26 - 2\sqrt{168}}$  is the Sum, and  $\sqrt{26 + 2\sqrt{168}}$  is the difference.

4. When two commensurable Surds proposed are Fractions, or mixt quantities, if they have not a common denominator, reduce them to a common denominator in the least terms; then to find out the rational parts, divide only the two new Numerators severally by their greatest common measure, and proceed as before. As to find the Sum or difference of  $\sqrt{\frac{2}{7}}$  and  $\sqrt{\frac{3}{5}}$ , reduced to a common denominator they will be  $\sqrt{\frac{2}{35}}$  and  $\sqrt{\frac{3}{35}}$  which divided by their common measure  $\sqrt{\frac{1}{35}}$ , brings them to  $\sqrt{\frac{2}{7}}$  and  $\sqrt{\frac{3}{5}}$  or  $6\sqrt{\frac{2}{7}}$  and  $5\sqrt{\frac{3}{5}}$  whose Sum is  $11\sqrt{\frac{2}{7}}$  or  $\sqrt{\frac{22}{7}}$ , and their difference  $1\sqrt{\frac{2}{7}}$ .

#### Examples in Compound Surds.

	$\sqrt{4} + \sqrt{8}$	$5 + \sqrt{32}$	$6 + \sqrt{18}$	$\sqrt{192} + 3$
	$\sqrt{5} - \sqrt{7}$	$4 + \sqrt{8}$	$5 + \sqrt{8}$	$\sqrt{75} - 3$
Sum	$\sqrt{5} + \sqrt{17}$	$9 + 6\sqrt{2}$	$11 + 5\sqrt{2}$	$13\sqrt{3}$
Diff.	$3 - \sqrt{5}$	$1 + 2\sqrt{2}$	$1 + \sqrt{2}$	$3\sqrt{3} + 6$
	$15 - 2\sqrt{2}$	$\sqrt{242} - 12$	$11\sqrt{2} + \sqrt{75}$	
	$7 + \sqrt{2}$	$-\sqrt{50} + 8$	$8\sqrt{3} + 8\sqrt{3}$	
Sum	$22 - \sqrt{2}$	$6\sqrt{2} - 4$	$11\sqrt{2} + 21\sqrt{3}$	
Diff.	$8 - 3\sqrt{2}$	$16\sqrt{2} - 20$	$11\sqrt{2} - 11\sqrt{3}$	

#### Multiplication of Compound Surds.

Observe the same method used in rational quantities.

Multiplicand	$b\sqrt{b^3} - aa$	$4 + \sqrt{7}$	$4 - \sqrt{3}$
Multiplior	$5b$	$3$	$2$
Product	$5b^2\sqrt{b^3} - 5a^2b$	$12 + \sqrt{63}$	$8 - \sqrt{12}$

Mul-

Multiplicand	$3d + \sqrt{bb}$	$\sqrt{2} + \sqrt{6}$	$\sqrt{7} - 2$
Multiplior	$\sqrt{bb}$	$\sqrt{8}$	$6$
Product	$3d\sqrt{b^2} + \sqrt{bb^2}$	$4 + \sqrt{48}$	$\sqrt{252} - 12$

Multiplicand	$\sqrt{bc} + \sqrt{c}$	$18 + \sqrt{54}$
Multiplior	$\sqrt{cn} - \sqrt{a}$	$6 - \sqrt{24}$
	$-\sqrt{bcn} - \sqrt{ac}$	$-18\sqrt{24} - \sqrt{1296}$
	$\sqrt{bc^2n} + \sqrt{c^2n}$	$108 + 6\sqrt{54}$
	$\sqrt{bc^2n} + \sqrt{c^2n} - \sqrt{bcn} - \sqrt{ac}$	$72 - 18\sqrt{6}$

If a Binomial be to be multiplied by its correspondent Residual, take the difference of the Squares of the Parts for the Product; for  $a + e \times a - e$  produceth  $a^2 - e^2$ .

Involution in Binomials and Residuals, is more easily performed by the Table of Powers, thus:

Because  $a + e \times 2 = a^2 + 2ae + e^2$ : Therefore to  $\odot 2$  any Binomial, take the Squares of the Parts, and twice their Product.

And to  $\odot 2$  any Residual, from the Sum of the Squares of the Parts, subtract a double Rectangle; because  $a - e \times a - e = a^2 - 2ae + e^2$ .

Thus may any Binomial, Trinomial, or Quadrinomial, &c. be involved as often as you please, by observing the result of so many rational Nomines so often involved.

Thus the Square of  $3 + \sqrt{6}$  is  $15 + 6\sqrt{6}$ ; the Square of  $a + \sqrt{b}$  is  $a^2 + b + 2a\sqrt{b}$ ; the Square of  $3 - \sqrt{6}$  is  $15 - 6\sqrt{6}$ ; of  $\sqrt{7} + \sqrt{4}$  is  $11 + 2\sqrt{28}$ ; of  $5 + \sqrt{3}$  is  $28 + 10\sqrt{3}$ ; and of  $4 - \sqrt{7}$  is  $23 - 8\sqrt{7}$ ; and the Cube of  $\sqrt{7} + \sqrt{5}$  is  $74 + 21\sqrt{35} + 15\sqrt{7}$ .





## CHAP. V.

*Division of Compound Surds.**Reduction necessary to precede Division.*

**I**F a Binomial, consisting of two Simple Square Roots, or of one Square Root and a Rational Quantity, be multiplied by its correspondent Residual, the Product will be a Rational Quantity.

If a Binomial, consisting of two Biquadratic Simple Roots, or of one Biquadratic Root and a Rational Quantity, be multiplied by its correspondent Residual, the Product will be a Residual, consisting of two Square Roots, or of one Square Root and a Rational Quantity, which being multiplied by its Binomial, as above, produceth a Rational Quantity.

If a Trinomial, consisting of three Simple Square Roots, be multiplied by the same Trinomial, having one of its Signs changed, the Product will be either a Binomial or Residual, which being multiplied by its correspondent Residual or Binomial, produceth a Quantity wholly Rational.

If a Quadrinomial, consisting of four Simple Square Roots, be multiplied by the same Quadrinomial, with two Signs changed, the Product will be a Trinomial, which may (by the Parag. above) be reduced to a Binomial, and that to a Quantity entirely Rational.

When a Binomial or Residual, consisting of two Simple Cubic or Biquadratic Roots, &c. or of one Cubic or Biquadratic Root, &c. and a Rational Quantity, is proposed for a divisor; find so many continual Proportionals in the proportion of the Parts of the Binomial or Residual proposed, as there be Unites in the Index of the Radical Sign, and such whole Radical Sign may be the same with that of the parts of the Binomial or Residual, but conjoined in the Binomial by +, and in the Proportionals by + and - alternately; or contrarily, in the Proportionals by - +, and in the Residual by + and -; the Product of the said Proportionals for connexed multiplied in the Binomial or Residual, will be a Quantity entirely Rational.

After

After the same manner may a Binomial or Residual, having 5 or 6, &c. for the Index of the common Radical Sign of the Roots, be reduced to a Quantity entirely Rational. And note, that when the Roots are of different kinds, they must first be reduced to a common Radical Sign.

If the Divisor be a Simple Quantity, divide each part of the Dividend by the Divisor, (according to the Directions in Division of *Simple Species*) and connex those particular Products together by their Signs: But if the Divisor be a Binomial, Trinomial, or Quadrinomial, &c. of such kind as before is specified, reduce the given Divisor to a new Divisor that may be a Simple Rational Quantity. Reduce also the given Dividend to a new Dividend, by multiplying the former by the same Quantities that were Multipliers, in reducing the given Divisor to a Rational Quantity; then divide the new Dividend by the new Divisor. But when the Divisor cannot be reduced to a Simple Rational Quantity, set the Dividend as a Numerator over the Divisor as a Denominator.

Thus  $12 + \sqrt{63}$  divided by 3, the Quotient is  $4 + \sqrt{7}$ ; and  $8 - \sqrt{12}$  divided by 2, the Quotient is  $4 - \sqrt{3}$ ;  $\sqrt{21} + \sqrt{15}$  divided by  $\sqrt{3}$ , the Quotient is  $\sqrt{7} + \sqrt{5}$ ;  $\sqrt{56} + \sqrt{24}$  divided by  $\sqrt{6}$ , the Quotient is  $\sqrt{9\frac{2}{3}} + 2$ ; and  $\sqrt{(3)28} - \sqrt{(3)14}$  divided by  $\sqrt{(3)7}$ , the Quotient is  $\sqrt{(3)4} - \sqrt{(3)2}$ .





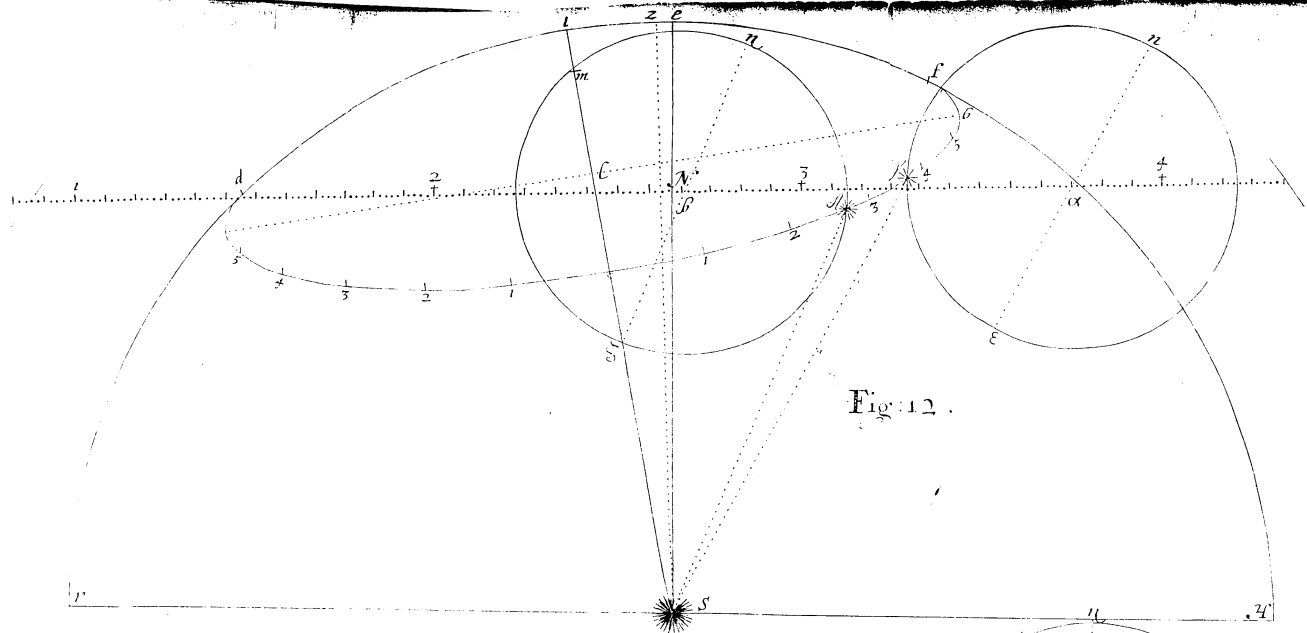
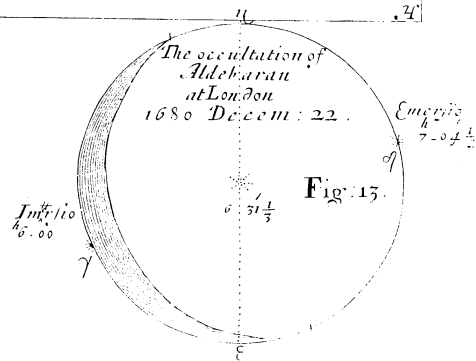


Fig: 12 .

7 Scale of Minutes



between page 66 and 67 the Doctrine of the Sphere .



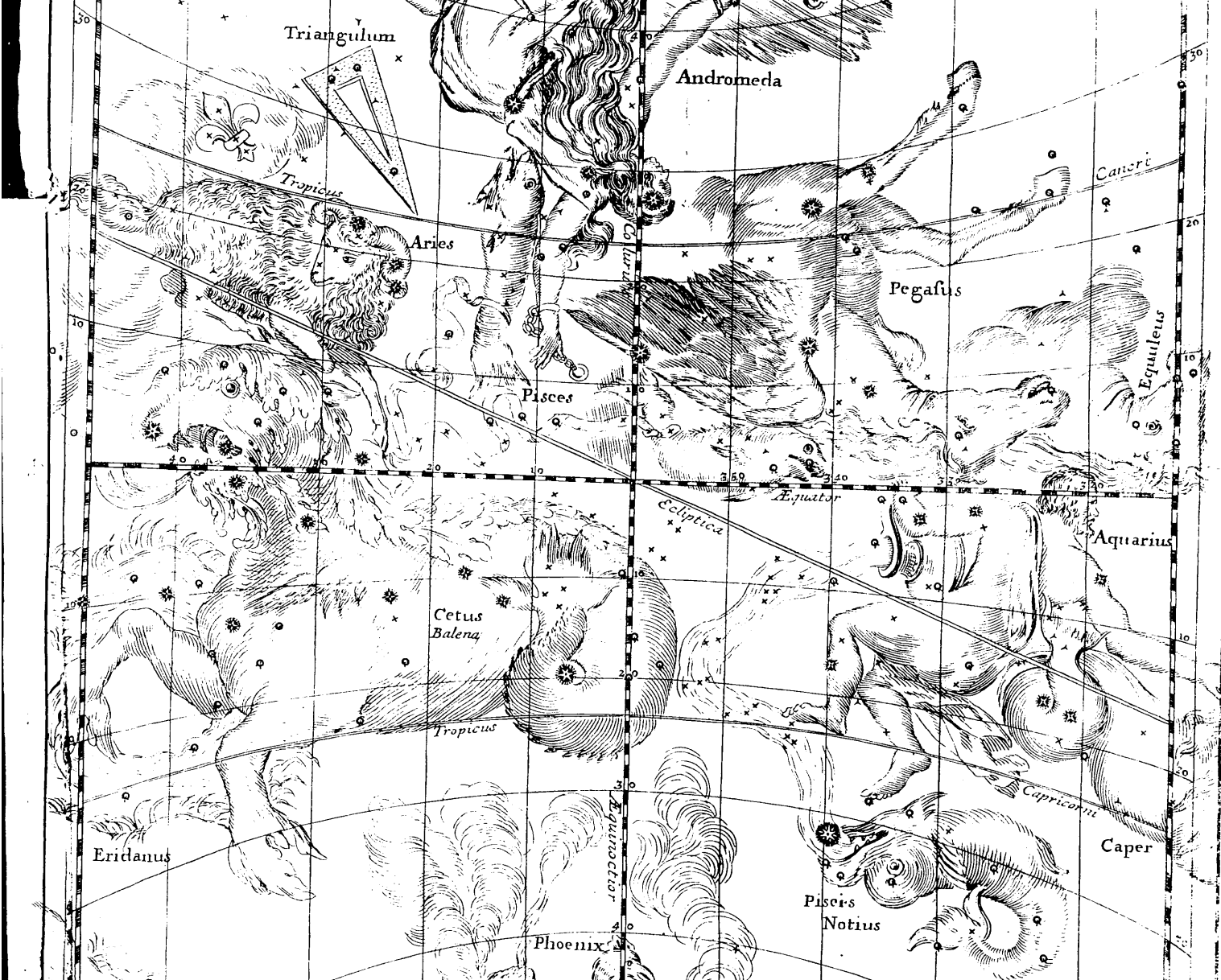
The occultation of  
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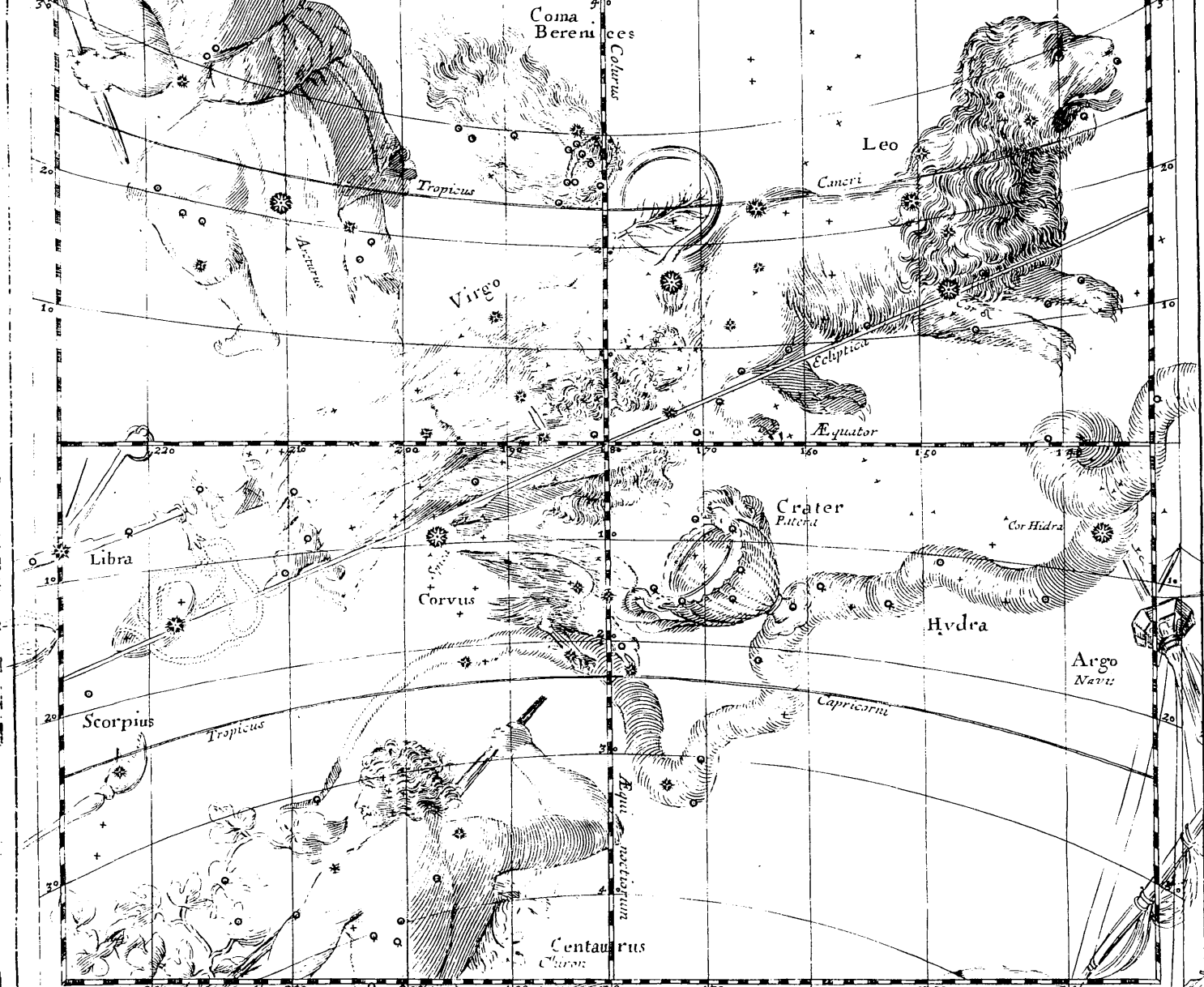








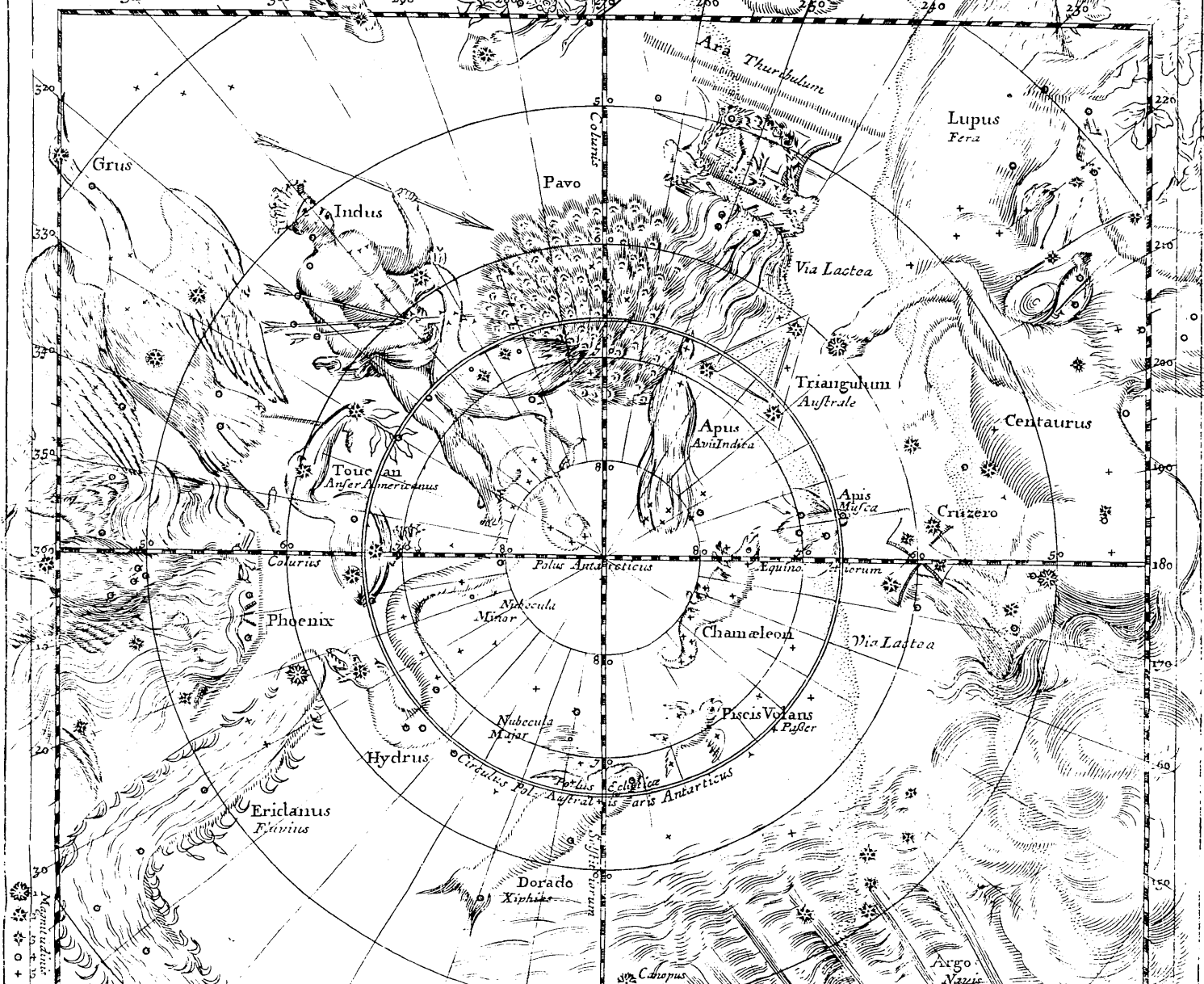














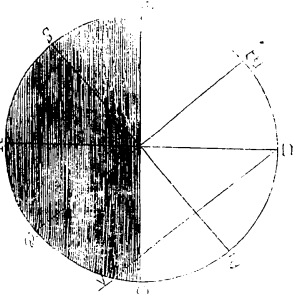


Fig. 1.

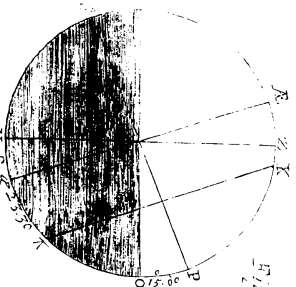


Fig. 2.

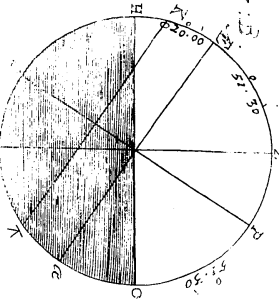


Fig. 3.

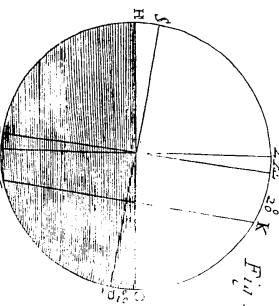


Fig. 4.

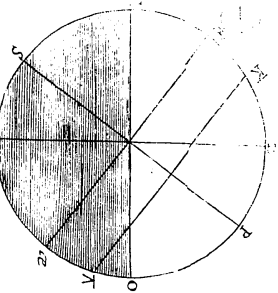


Fig. 5.

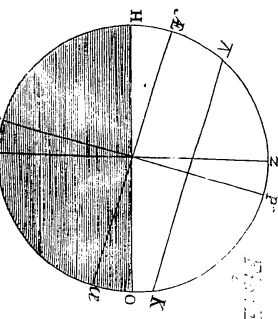
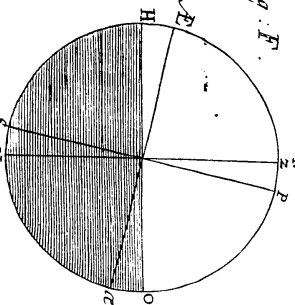


Fig. 6.



*H E Z PON* represents the Meridian, *E e* the Equinoctial, *K T* the Parallel of Declination, *HO* the Horizon, *SP* the Axis of the Equinoctial, *ZN* the Axis of the Horizon, and Prime vertical, *P* the North Pole, *S* the South Pole, *Z* the Zenith, *N* the Nadir, *H* the South point of the Horizon, *O* the North Point, *H K* or *OK* the Meridian, *Altitude*, *Z K* the Co-latitude or Zenith distance, *E K* the Declination, *Z . E* the Lat: = *O P* the Poles elevation.



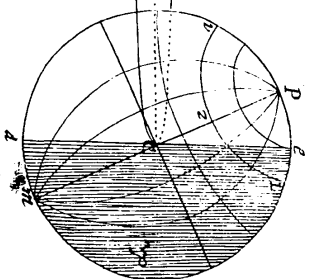
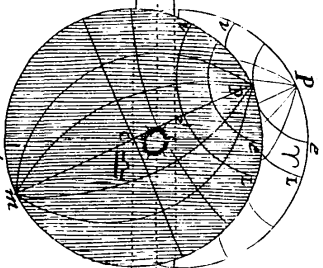
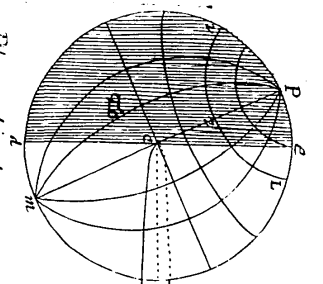
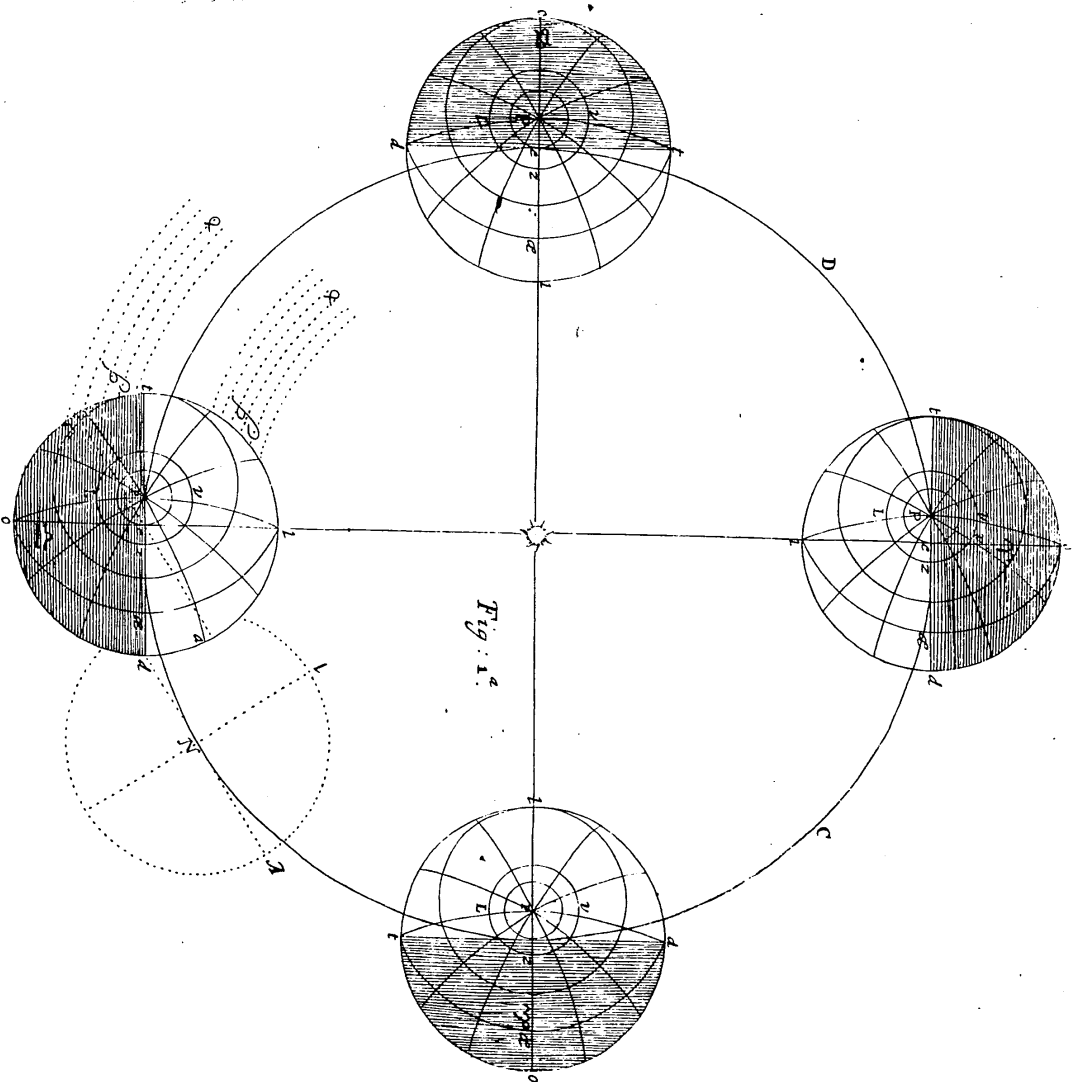
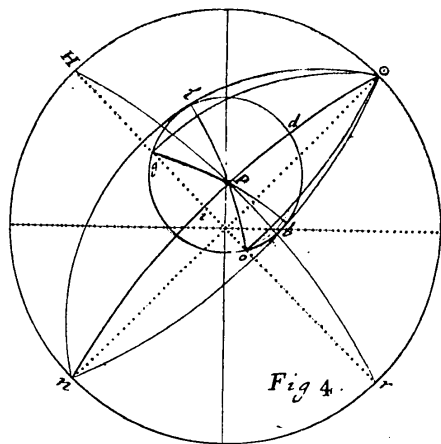
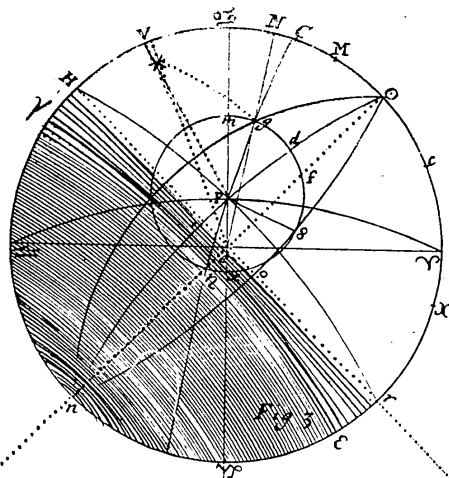
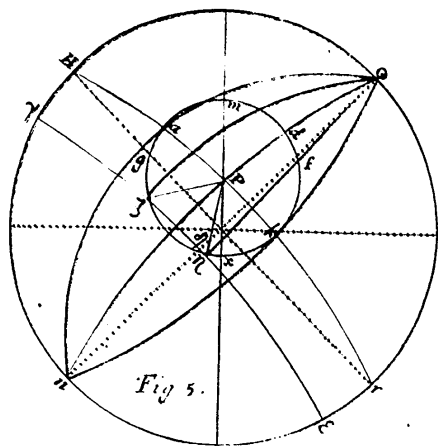


Fig. 2.

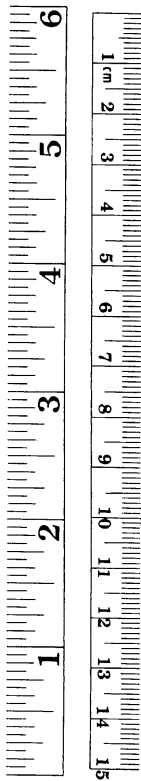
Place this between page 4 and 5 the Doctrine of the Sphere.





Place this between page 6 and 7 the Doctrine of the Sphere.





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# ASTRONOMICAL TABLES.

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# ASTRONOMICAL TABLES.

## Tables of Declination.

### North Latitude.

	0	1	2	3	4	5	6	7	8	9	
	D. M.	D. M.	D. M.	D. M.	D. M.	D. M.	D. M.	D. M.	D. M.	D. M.	
0	32	32	32	32	32	32	32	32	32	32	30
1	31	31	31	31	31	31	31	31	31	31	29
2	30	30	30	30	30	30	30	30	30	30	28
3	29	29	29	29	29	29	29	29	29	29	27
4	28	28	28	28	28	28	28	28	28	28	26
5	27	27	27	27	27	27	27	27	27	27	25
6	26	26	26	26	26	26	26	26	26	26	24
7	25	25	25	25	25	25	25	25	25	25	23
8	24	24	24	24	24	24	24	24	24	24	22
9	23	23	23	23	23	23	23	23	23	23	21
10	22	22	22	22	22	22	22	22	22	22	20
11	21	21	21	21	21	21	21	21	21	21	19
12	20	20	20	20	20	20	20	20	20	20	18
13	19	19	19	19	19	19	19	19	19	19	17
14	18	18	18	18	18	18	18	18	18	18	16
15	17	17	17	17	17	17	17	17	17	17	15
16	16	16	16	16	16	16	16	16	16	16	14
17	15	15	15	15	15	15	15	15	15	15	13
18	14	14	14	14	14	14	14	14	14	14	12
19	13	13	13	13	13	13	13	13	13	13	11
20	12	12	12	12	12	12	12	12	12	12	10
21	11	11	11	11	11	11	11	11	11	11	9
22	10	10	10	10	10	10	10	10	10	10	8
23	9	9	9	9	9	9	9	9	9	9	7
24	8	8	8	8	8	8	8	8	8	8	6
25	7	7	7	7	7	7	7	7	7	7	5
26	6	6	6	6	6	6	6	6	6	6	4
27	5	5	5	5	5	5	5	5	5	5	3
28	4	4	4	4	4	4	4	4	4	4	2
29	3	3	3	3	3	3	3	3	3	3	1
30	2	2	2	2	2	2	2	2	2	2	0

# ASTRONOMICAL TABLES.

## Tables of Declination.

### South Latitude.

	0	1	2	3	4	5	6	7	8	9	
	D. M.	D. M.	D. M.	D. M.	D. M.	D. M.	D. M.	D. M.	D. M.	D. M.	
0	32	32	32	32	32	32	32	32	32	32	30
1	31	31	31	31	31	31	31	31	31	31	29
2	30	30	30	30	30	30	30	30	30	30	28
3	29	29	29	29	29	29	29	29	29	29	27
4	28	28	28	28	28	28	28	28	28	28	26
5	27	27	27	27	27	27	27	27	27	27	25
6	26	26	26	26	26	26	26	26	26	26	24
7	25	25	25	25	25	25	25	25	25	25	23
8	24	24	24	24	24	24	24	24	24	24	22
9	23	23	23	23	23	23	23	23	23	23	21
10	22	22	22	22	22	22	22	22	22	22	20
11	21	21	21	21	21	21	21	21	21	21	19
12	20	20	20	20	20	20	20	20	20	20	18
13	19	19	19	19	19	19	19	19	19	19	17
14	18	18	18	18	18	18	18	18	18	18	16
15	17	17	17	17	17	17	17	17	17	17	15
16	16	16	16	16	16	16	16	16	16	16	14
17	15	15	15	15	15	15	15	15	15	15	13
18	14	14	14	14	14	14	14	14	14	14	12
19	13	13	13	13	13	13	13	13	13	13	11
20	12	12	12	12	12	12	12	12	12	12	10
21	11	11	11	11	11	11	11	11	11	11	9
22	10	10	10	10	10	10	10	10	10	10	8
23	9	9	9	9	9	9	9	9	9	9	7
24	8	8	8	8	8	8	8	8	8	8	6
25	7	7	7	7	7	7	7	7	7	7	5
26	6	6	6	6	6	6	6	6	6	6	4
27	5	5	5	5	5	5	5	5	5	5	3
28	4	4	4	4	4	4	4	4	4	4	2
29	3	3	3	3	3	3	3	3	3	3	1
30	2	2	2	2	2	2	2	2	2	2	0



## ASTRONOMICAL TABLES.

Tables of Declination.

North Latitude.

	0.		1.		2.		3.		4.		5.		6.		7.		8.		9.		
$\Delta$	D.	M.	D.	M.	D.	M.	D.	M.	D.	M.	D.	M.	D.	M.	D.	M.	D.	M.	D.	M.	
0	20	13	21	12	22	10	23	09	24	07	25	06	26	04	27	03	28	01	28	59	30
1	20	00	20	59	21	57	22	56	23	54	24	53	25	51	26	49	27	47	28	45	29
2	19	47	20	45	21	44	22	42	23	40	24	39	25	37	26	35	27	33	28	31	28
3	19	33	20	31	21	30	22	28	23	26	24	25	23	26	21	27	19	28	17	27	
4	19	19	20	17	21	16	22	14	23	12	24	11	25	09	26	07	27	05	28	03	26
5	19	05	20	03	21	02	22	00	23	58	23	56	24	54	25	52	26	50	27	48	25
6	18	50	19	49	20	47	21	45	22	43	23	41	24	39	25	37	26	35	27	33	24
7	18	35	19	34	20	32	21	29	22	27	23	25	24	23	25	21	26	19	27	17	23
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9	18	04	19	02	20	00	20	57	21	55	22	53	23	51	24	48	25	46	26	44	21
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29	11	52	12	48	13	44	14	40	15	36	16	33	17	29	18	25	19	21	20	17	1
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## ASTRONOMICAL TABLES.

Tables of Declination.

South Latitude.



	0		1		2		3		4		5		6		7		8		9	
$\Delta$	D.	M.	D.	M.	D.	M.	D.	M.	D.	M.	D.	M.	D.	M.	D.	M.	D.	M.	D.	M.
0	20	13	19	14	18	16	17	17	16	18	15	20	14	21	13	22	12	24	11	25
1	20	00	19	01	18	03	17	04	16	05	15	07	14	08	13	10	12	12	11	14
2	19	47	18	48	17	50	16	51	15	52	14	54	13	55	12	57	11	59	11	01
3	19	33	18	35	17	36	16	38	15	39	14	41	13	42	12	44	11	46	10	48
4	19	19	18	21	17	22	16	24	15	26	14	27	13	29	12	31	11	32	10	35
5	19	05	18	07	17	08	16	10	15	12	14	13	13	15	12	17	11	19	10	21
6	18	50	17	52	16	54	15	56	14	58	13	59	13	01	12	03	11	05	10	07
7	18	35	17	38	16	39	15	41	14	43	13	44	12	46	11	48	10	50	9	52
8	18	20	17	22	16	24	15	26	14	28	13	29	12	31	11	33	10	35	9	37
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10	17	48	16	50	15	52	14	54	13	56	12	58	12	01	11	03	10	05	9	07
11	17	32	16	34	15	36	14	38	13	40	12	42	11	45	10	48	9	49	8	51
12	17	15	16	17	15	20	14	22	13	24	12	26	11	29	10	31	9	31	8	35
13	16	56	16	00	15	03	14	05	13	08	12	10	11	13	10	15	9	17	8	20
14	16	41	15	43	14	46	13	48	12	51	11	53	10	56	9	58	9	01	8	03
15	16	24	15	26	14	28	13	31	12	34	11	36	10	39	9	41	8	44	7	46
16	16	06	15	08	14	11	13	14	12	17	11	19	10	22	9	24	8	27	7	30
17	15	48	14	50	13	53	12	56	11	59	11	01	10	04	9	07	8	10	7	14
18	15	29	14	32	13	35	12	38	11	41	10	43	9	46	8	49	7	52	6	55
19	15	11	14	14	13	17	12	20	11	23	10	25	9	28	8	31	7	34	6	37
20	14	52	13	55	12	58	12	01	11	04	10	07	9	10	8	13	7	16	6	19
21	14	33	13	36	12	39	11	42	10	45	9	48	8	51	7	54	6	57	5	60
22	14	14	13	17	12	20	11	23	10	26	9	29	8	32	7	35	6	38	5	41
23	13	54	12	58	12	01	11	04	10	07	9	10	8	13	7	16	6	19	5	22
24	13	34	12	38	11	41	10	44	9	48	8	51	7	54	6	57	6	00	5	03
25	13	14	12	18	11	21	10	24	9	28	8	31	7	35	6	38	5	41	4	44
26	12	54	11	59	11	01	10	04	9	08	8	11	7	15	6	18	5	22	4	05
27	12	33	11	36	10	39	9	43	8	47	7	50	6	54	5	57	5	01	4	04
28	12	13	11	17	10	20	9	24	8	28	7	31	6	35	5	38	4	42	3	46
29	11	52	10	56	10	00	9	04	8	07	7	11	6	15	5	17	4	22	3	26
30	11	31	10	35	9	38	8	42	7	46	6	50	5	54	4	57	4	01	3	05



## Tables of Declination.

## North Latitude.

	0	1	2	3	4	5	6	7	8	9	
D. M.	D. M.	D. M.	D. M.	D. M.	D. M.	D. M.	D. M.	D. M.	D. M.	D. M.	
0	11	31	12	27	13	22	14	10	15	16	11
1	11	09	12	05	13	01	13	57	14	53	16
2	10	48	11	45	12	41	13	36	14	32	15
3	10	26	11	23	12	19	13	14	14	10	15
4	10	05	11	01	11	57	12	52	13	48	14
5	9	43	10	39	11	35	12	30	13	26	14
6	9	21	10	17	11	13	12	08	13	04	14
7	8	58	9	55	10	51	11	46	12	42	13
8	8	36	9	32	10	28	11	23	12	19	13
9	8	13	9	10	10	06	11	01	11	56	12
10	7	51	8	47	9	42	10	38	11	33	12
11	7	28	8	23	9	18	10	14	11	09	12
12	7	05	8	00	9	55	10	46	11	42	13
13	6	42	7	37	8	32	9	28	10	23	11
14	6	19	7	14	8	09	9	05	10	00	10
15	5	56	6	52	7	47	8	42	9	37	10
16	5	33	6	29	7	24	8	19	9	14	10
17	5	09	6	05	7	00	8	55	9	46	10
18	4	46	5	42	6	37	7	32	8	27	9
19	4	22	5	18	6	13	7	08	8	03	9
20	3	58	4	54	5	49	6	44	7	39	8
21	3	35	4	30	5	25	6	20	7	15	8
22	3	11	4	07	5	02	6	57	7	02	7
23	2	47	3	43	4	38	5	33	6	28	7
24	2	24	3	19	4	14	5	09	6	04	6
25	2	00	3	55	4	50	5	45	6	40	5
26	1	36	2	31	3	26	4	21	5	16	4
27	1	12	2	07	3	02	4	57	5	52	3
28	0	48	1	43	2	38	3	33	4	28	2
29	0	24	1	19	2	14	3	09	4	04	1
30	0	00	0	55	1	50	2	45	3	40	0

## Tables of Declination.

## South Latitude.

	0	1	2	3	4	5	6	7	8	9	
D. M.	D. M.	D. M.	D. M.	D. M.	D. M.	D. M.	D. M.	D. M.	D. M.	D. M.	
0	11	31	10	35	9	39	8	43	7	46	6
1	11	09	10	14	9	18	8	22	7	25	6
2	10	48	9	53	8	57	8	01	7	04	6
3	10	26	9	31	8	35	7	39	6	43	5
4	10	05	9	09	8	14	7	18	6	22	5
5	9	43	8	47	7	52	6	56	5	04	4
6	9	21	8	25	7	30	6	34	5	38	4
7	8	58	8	03	7	07	6	11	5	15	4
8	8	36	7	40	6	44	5	49	4	53	3
9	8	13	7	17	6	21	5	26	4	30	3
10	7	51	6	55	5	59	5	04	4	08	3
11	7	28	6	32	5	37	4	41	3	46	2
12	7	05	6	09	5	14	4	18	3	23	2
13	6	42	5	46	4	51	3	55	3	00	2
14	6	19	5	23	4	28	3	32	2	37	1
15	5	56	5	01	4	06	3	10	2	15	1
16	5	33	4	38	3	43	2	57	1	52	0
17	5	09	4	14	3	19	2	24	1	29	0
18	4	46	3	51	2	56	2	01	1	05	0
19	4	22	3	27	2	32	1	57	0	41	0
20	3	58	3	03	2	08	1	13	0	18	0
21	3	35	2	29	1	44	0	49	0	06	0
22	3	11	2	16	1	21	0	26	0	29	0
23	2	47	1	52	0	57	0	02	0	53	0
24	2	24	1	29	0	33	0	22	1	17	2
25	2	00	1	05	0	09	0	46	1	41	2
26	1	36	0	41	0	15	1	10	2	05	3
27	1	12	0	17	0	33	1	33	2	29	3
28	0	48	0	07	1	23	1	57	2	52	3
29	0	24	0	31	1	37	2	21	3	16	4
30	0	00	0	55	1	50	2	45	3	40	4



# ASTRONOMICAL TABLES.

## Tables of Declination.

### North Latitude.

	0	1	2	3	4	5	6	7	8	9	
D. M.	D. M.	D. M.	D. M.	D. M.	D. M.	D. M.	D. M.	D. M.	D. M.	D. M.	
0	00	01	02	03	04	05	06	07	08	09	30
1	00	01	02	03	04	05	06	07	08	09	29
2	00	01	02	03	04	05	06	07	08	09	28
3	00	01	02	03	04	05	06	07	08	09	27
4	00	01	02	03	04	05	06	07	08	09	26
5	00	01	02	03	04	05	06	07	08	09	25
6	00	01	02	03	04	05	06	07	08	09	24
7	00	01	02	03	04	05	06	07	08	09	23
8	00	01	02	03	04	05	06	07	08	09	22
9	00	01	02	03	04	05	06	07	08	09	21
10	00	01	02	03	04	05	06	07	08	09	20
11	00	01	02	03	04	05	06	07	08	09	19
12	00	01	02	03	04	05	06	07	08	09	18
13	00	01	02	03	04	05	06	07	08	09	17
14	00	01	02	03	04	05	06	07	08	09	16
15	00	01	02	03	04	05	06	07	08	09	15
16	00	01	02	03	04	05	06	07	08	09	14
17	00	01	02	03	04	05	06	07	08	09	13
18	00	01	02	03	04	05	06	07	08	09	12
19	00	01	02	03	04	05	06	07	08	09	11
20	00	01	02	03	04	05	06	07	08	09	10
21	00	01	02	03	04	05	06	07	08	09	9
22	00	01	02	03	04	05	06	07	08	09	8
23	00	01	02	03	04	05	06	07	08	09	7
24	00	01	02	03	04	05	06	07	08	09	6
25	00	01	02	03	04	05	06	07	08	09	5
26	00	01	02	03	04	05	06	07	08	09	4
27	00	01	02	03	04	05	06	07	08	09	3
28	00	01	02	03	04	05	06	07	08	09	2
29	00	01	02	03	04	05	06	07	08	09	1
30	00	01	02	03	04	05	06	07	08	09	0

# ASTRONOMICAL TABLES.

9

## Tables of Declination.

### South Latitude.

	0	1	2	3	4	5	6	7	8	9	
D. M.	D. M.	D. M.	D. M.	D. M.	D. M.	D. M.	D. M.	D. M.	D. M.	D. M.	
0	00	01	02	03	04	05	06	07	08	09	30
1	00	01	02	03	04	05	06	07	08	09	29
2	00	01	02	03	04	05	06	07	08	09	28
3	00	01	02	03	04	05	06	07	08	09	27
4	00	01	02	03	04	05	06	07	08	09	26
5	00	01	02	03	04	05	06	07	08	09	25
6	00	01	02	03	04	05	06	07	08	09	24
7	00	01	02	03	04	05	06	07	08	09	23
8	00	01	02	03	04	05	06	07	08	09	22
9	00	01	02	03	04	05	06	07	08	09	21
10	00	01	02	03	04	05	06	07	08	09	20
11	00	01	02	03	04	05	06	07	08	09	19
12	00	01	02	03	04	05	06	07	08	09	18
13	00	01	02	03	04	05	06	07	08	09	17
14	00	01	02	03	04	05	06	07	08	09	16
15	00	01	02	03	04	05	06	07	08	09	15
16	00	01	02	03	04	05	06	07	08	09	14
17	00	01	02	03	04	05	06	07	08	09	13
18	00	01	02	03	04	05	06	07	08	09	12
19	00	01	02	03	04	05	06	07	08	09	11
20	00	01	02	03	04	05	06	07	08	09	10
21	00	01	02	03	04	05	06	07	08	09	9
22	00	01	02	03	04	05	06	07	08	09	8
23	00	01	02	03	04	05	06	07	08	09	7
24	00	01	02	03	04	05	06	07	08	09	6
25	00	01	02	03	04	05	06	07	08	09	5
26	00	01	02	03	04	05	06	07	08	09	4
27	00	01	02	03	04	05	06	07	08	09	3
28	00	01	02	03	04	05	06	07	08	09	2
29	00	01	02	03	04	05	06	07	08	09	1
30	00	01	02	03	04	05	06	07	08	09	0



## Tables of Declination.

## North Latitude.

	0		1		2		3		4		5		6		7		8		9	
m.	D.	M.	D.	M.	D.	M.	D.	M.	D.	M.	D.	M.	D.	M.	D.	M.	D.	M.	D.	M.
0	11	31	10	35	9	39	8	43	7	46	6	50	5	54	4	57	4	01	3	05
1	11	52	10	56	10	00	9	04	8	07	7	11	6	15	5	18	4	22	3	26
2	12	13	11	17	10	20	9	24	8	28	7	31	6	35	5	38	4	42	3	46
3	12	33	11	37	10	40	9	44	8	48	7	51	6	55	5	58	5	02	4	06
4	12	54	11	58	11	01	10	04	9	08	8	11	7	15	6	18	5	22	4	26
5	13	14	12	18	11	21	10	24	9	28	8	31	7	35	6	38	5	42	4	46
6	13	34	12	38	11	41	10	44	9	48	8	51	7	54	6	57	6	01	5	05
7	13	54	12	58	12	01	11	04	10	07	9	10	8	13	7	16	6	20	5	24
8	14	14	13	17	12	20	11	23	10	26	9	29	8	32	7	35	6	39	5	42
9	14	35	13	39	12	39	11	42	10	45	9	48	8	51	7	54	6	57	6	00
10	14	55	13	59	12	59	11	04	10	07	9	10	8	13	7	16	6	19	5	23
11	15	15	14	18	13	17	12	20	11	23	10	25	9	28	8	31	7	34	6	37
12	15	35	14	39	13	37	12	38	11	41	10	43	9	46	8	49	7	52	6	55
13	15	55	14	59	13	57	12	56	11	59	11	01	10	04	9	07	8	10	7	13
14	16	06	15	09	14	11	13	14	12	17	11	19	10	22	9	24	8	27	7	30
15	16	26	15	29	14	29	13	31	12	34	11	36	10	39	9	41	8	44	7	47
16	16	46	15	49	14	49	13	51	12	54	11	56	10	59	9	61	8	64	7	67
17	16	56	16	00	15	03	14	05	13	08	12	10	11	13	10	15	9	17	8	20
18	17	16	16	19	15	20	14	22	13	24	12	26	11	29	10	31	9	33	8	35
19	17	36	16	39	15	39	14	41	13	43	12	45	11	47	10	49	9	51	8	53
20	17	56	16	59	15	59	14	54	13	56	12	58	11	60	10	62	9	64	8	66
21	18	07	17	00	16	08	15	10	14	12	13	14	12	16	11	18	10	20	9	22
22	18	27	17	29	16	29	15	26	14	28	13	29	12	31	11	33	10	35	9	37
23	18	47	17	49	16	49	15	44	14	46	13	48	12	50	11	52	10	54	9	56
24	18	57	17	59	16	59	15	54	14	56	13	58	12	60	11	62	10	64	9	66
25	19	08	18	00	17	08	16	10	15	12	14	15	12	17	11	19	10	21	9	23
26	19	28	18	29	17	29	16	26	15	28	14	29	12	31	11	33	10	35	9	37
27	19	48	18	49	17	49	16	44	15	46	14	48	12	50	11	52	10	54	9	56
28	19	68	18	69	17	69	16	64	15	66	14	68	12	70	11	72	10	74	9	76
29	20	09	19	00	18	09	17	11	16	13	14	15	12	17	11	19	10	21	9	23
30	20	29	19	29	18	29	17	26	16	28	15	29	12	31	11	33	10	35	9	37

## Tables of Declination.

## South Latitude.

	0		1		2		3		4		5		6		7		8		9	
m.	D.	M.	D.	M.	D.	M.	D.	M.	D.	M.	D.	M.	D.	M.	D.	M.	D.	M.	D.	M.
0	11	31	12	27	13	23	14	19	15	15	16	11	17	07	18	03	18	55	19	54
1	11	52	12	48	13	44	14	40	15	36	16	33	17	29	18	25	19	21	20	16
2	12	13	13	09	14	05	15	01	15	57	16	54	17	50	18	46	19	42	20	37
3	12	33	13	29	14	25	15	21	16	18	17	14	18	10	19	06	20	02	20	57
4	12	54	13	50	14	46	15	42	16	39	17	35	18	31	19	27	20	24	21	19
5	13	14	14	11	15	07	16	03	17	00	17	56	18	52	19	49	20	45	21	40
6	13	34	14	31	15	27	16	24	17	20	18	17	19	13	20	10	21	05	22	01
7	13	54	14	51	15	47	16	44	17	40	18	37	19	33	20	30	21	26	22	21
8	14	14	15	11	16	07	17	04	18	00	18	57	19	53	20	50	21	46	22	42
9	14	35	15	30	16	26	17	23	18	20	19	17	20	15	21	10	22	05	23	02
10	14	55	15	49	16	45	17	42	18	39	19	36	20	33	21	30	22	26	23	22
11	15	15	16	08	17	04	18	01	18	58	19	55	20	52	21	49	22	45	23	42
12	15	35	16	26	17	23	18	20	19	17	20	14	21	11	22	08	23	05	24	02
13	15	55	16	45	17	42	18	39	19	36	20	33	21	30	22	27	23	24	21	17
14	16	06	17	03	18	00	18	57	19	54	20	52	21	49	22	46	23	43	24	40
15	16	26	17	21	18	18	19	15	20	12	21	10	22	07	23	04	24	01	24	58
16	16	46	17	38	18	36	19	33	20	30	21	48	22	25	23	22	24	19	25	16
17	16	56	17	55	18	53	19	51	20	48	21	46	22	43	23	40	24	37	25	34
18	17	16	18	12	19	10	20	08	21	05	22	03	23	00	23	57	24	53	25	52
19	17	36	18	29	19	27	20	25	21	23	22	20	23	17	24	14	25	12	26	10
20	17	56	18	46	19	44	20	41	21	39	22	37	23	34	24	31	25	26	24	20
21	18	07	19	02	20	00	20	57	21	55	22	53	23	51	24	48	25	46	26	44
22	18	27	19	18	20	16	21	13	22	11	23	09	24	07	25	05	26	03	27	01
23	18	47	19	34	20	32	21	29	22	27	23	25	24	23	25	21	26	19	27	17
24	18	57	19	49	20	47	21	45	22	43	23	41	24	39	25	37	26	35	27	33
25	19	08	20	03	21	02	22	00	22	58	23	56	24	54	25	52	26	50	27	48
26	19	28	20	17	21	16	22	14	23	12	24	11	25	09	26	07	27	05	28	03
27	19	48	20	31	21	30	22	28	23	20	24	25	23	26	21	27	19	28	17	15
28	19	68	20	45	21	44	22	42	23	40	24	39	25	37	26	35	27	33	28	31
29	20	09	20	59	21	47	22	56	23	54	24	53	25	51	26	49	27	47	28	45
30	20	29	21	12	22	10	23	09	24	07	25	06	26	04	27	03	28	01	29	00



ASTRONOMICAL TABLES.

## Tables of Declination.

North Latitude.

	0		1		2		3		4		5		6		7		8		9		
F.	D.	M.	D.	M.	D.	M.	D.	M.	D.	M.	D.	M.	D.	M.	D.	M.	D.	M.	D.	M.	
0	20	13	19	14	18	16	17	17	16	18	15	20	14	21	13	22	12	24	11	26	30
1	20	26	19	27	18	28	17	29	16	30	15	32	14	33	13	33	12	36	11	37	29
2	20	38	19	39	18	40	17	41	16	42	15	44	14	45	13	47	12	48	11	49	28
3	20	50	19	51	18	52	17	53	16	54	15	55	14	57	13	58	12	43	12	02	27
4	21	01	20	02	19	03	18	04	17	05	16	07	15	08	14	00	13	10	12	11	26
5	21	13	20	13	19	15	18	16	17	16	15	19	15	19	14	13	20	12	12	21	25
6	21	23	20	24	19	25	18	26	17	27	16	28	15	28	14	29	13	30	12	31	24
7	21	33	20	34	19	35	18	36	17	37	16	38	15	38	14	39	13	40	12	41	23
8	21	43	20	44	19	45	18	46	17	47	16	47	15	48	14	49	13	50	12	50	22
9	21	53	20	54	19	55	18	56	17	56	16	57	15	58	14	58	13	59	13	00	21
10	22	02	21	03	20	04	19	05	18	05	17	06	16	05	15	07	14	07	13	08	20
11	22	12	21	11	20	12	19	13	18	13	17	14	16	14	15	15	14	15	13	16	19
12	22	19	21	19	20	20	19	21	18	21	17	22	16	22	15	23	14	23	13	24	18
13	22	27	21	28	20	28	19	28	18	29	17	29	16	29	15	30	14	20	13	31	17
14	22	34	21	35	20	35	19	35	18	36	17	36	16	30	15	37	14	37	13	37	16
15	22	41	21	41	20	41	19	41	18	42	17	42	16	42	15	43	14	43	13	43	15
16	22	47	21	47	20	47	19	47	18	48	17	48	16	48	15	49	14	49	13	49	14
17	22	53	21	53	20	53	19	53	18	54	17	54	16	54	15	55	14	55	13	55	13
18	22	59	21	59	20	59	19	59	18	00	18	00	17	00	16	01	15	01	14	01	12
19	23	04	22	04	21	04	20	04	19	05	18	05	17	05	16	05	15	06	14	06	11
20	23	09	22	09	21	09	20	09	19	10	18	10	17	10	16	10	15	10	14	10	10
21	23	15	22	13	21	15	20	13	19	14	18	14	17	14	16	14	15	14	14	14	9
22	23	17	22	17	21	17	20	17	19	17	18	17	17	17	16	17	15	17	14	17	8
23	23	20	22	20	21	20	20	20	19												
24	23	23	22	23	21	23	20	23	19	23	18	23	17	23	16	23	15	23	14	23	6
25	23	26	22	26	21	26	20	26	19	26	18	26	17	26	16	26	15	26	14	26	5
26	23	28	22	28	21	28	20	28	19	28	18	28	17	28	16	28	15	28	14	28	4
27	23	30	22	30	21	30	20	30	19	30	18	30	17	30	16	30	15	30	14	30	3
28	23	31	22	31	21	31	20	31	19	31	18	31	17	31	16	31	15	31	14	31	2
29	23	31	22	31	21	31	20	31	19	31	18	31	17	31	16	31	15	31	14	31	1
30	23	31	22	32	21	32	20	32	19	31	18	32	17	32	16	32	15	32	14	32	C

### Tables of Declination.

*South Latitude,*

	0	1	2	3	4	5	6	7	8	9
<i>D.</i>	<i>M.</i>	<i>D.</i>	<i>M.</i>	<i>D.</i>	<i>M.</i>	<i>D.</i>	<i>M.</i>	<i>D.</i>	<i>M.</i>	<i>D.</i>
0	20	13	21	12	22	10	23	09	24	07
1	20	26	21	25	22	23	22	24	20	25
2	20	38	21	37	22	36	23	35	24	33
3	20	50	21	49	22	48	23	47	24	45
4	21	01	22	00	22	59	23	58	24	57
5	21	13	22	11	23	10	24	09	25	08
6	21	23	22	22	23	21	24	20	25	19
7	21	33	22	32	23	31	24	30	25	29
8	21	43	22	42	23	41	24	40	25	39
9	21	53	22	52	23	51	24	50	25	49
10	22	02	23	01	24	00	25	00	25	59
11	22	12	23	10	24	09	25	08	27	07
12	22	19	23	19	24	18	25	18	26	17
13	22	27	23	27	24	26	25	26	27	24
14	22	34	23	34	24	33	25	32	27	31
15	22	41	23	41	24	40	25	39	26	35
16	22	47	23	47	24	46	25	45	26	43
17	22	53	23	53	24	53	25	52	26	51
18	22	59	23	59	24	59	25	58	26	57
19	23	04	24	04	25	04	26	03	27	03
20	23	09	24	09	25	09	26	08	27	08
21	23	13	24	13	25	13	26	12	27	12
22	23	17	24	17	25	17	26	16	27	16
23	23	20	24	20	25	20	26	19	27	19
24	23	23	24	23	25	23	26	22	27	22
25	23	26	24	26	25	26	26	25	27	25
26	23	28	24	28	25	28	26	27	28	28
27	23	30	24	30	25	30	26	29	30	29
28	23	31	24	31	25	31	26	30	31	30
29	23	31	24	31	25	31	26	30	31	31
30	23	32	24	32	25	32	26	31	32	32



## Tables of Right Ascension.

North Latitude.

	0	1	2	3	4	5	6	7	8	9
$\gamma$	D. M.	D. M.	D. M.	D. M.	D. M.	D. M.	D. M.	D. M.	D. M.	D. M.
0	0 00	359 37	359 13	358 49	358 25	358 01	357 37	357 13	356 48	356 23
1	0 55	0 32	0 08	359 44	359 20	358 56	358 32	358 08	357 43	357 18
2	1 50	1 27	1 03	0 39	0 15	359 51	359 27	359 03	358 38	358 13
3	2 45	2 22	1 58	1 34	1 10	0 46	0 22	359 58	359 34	359 09
4	3 40	3 17	2 53	2 29	2 05	1 41	1 17	0 53	0 29	0 04
5	4 35	4 12	3 48	3 24	3 00	2 36	2 12	1 48	1 24	0 59
6	5 30	5 07	4 43	4 19	3 55	3 31	3 07	2 43	2 19	1 54
7	6 25	6 02	5 38	5 14	4 50	4 26	4 02	3 38	3 14	2 49
8	7 21	6 57	6 33	6 09	5 45	5 21	4 57	4 33	4 09	3 44
9	8 16	7 52	7 28	7 04	6 40	6 16	5 52	5 28	5 04	4 39
10	9 11	8 47	8 23	7 59	7 35	7 11	6 47	6 23	5 59	5 34
11	10 06	9 42	9 18	8 54	8 30	8 06	7 42	7 18	6 54	6 30
12	11 02	10 38	10 14	9 50	9 26	9 02	8 38	8 14	7 50	7 26
13	11 57	11 33	11 09	10 45	10 21	9 57	9 33	9 09	8 45	8 21
14	12 53	12 29	12 05	11 41	11 17	10 53	10 29	10 05	9 41	9 17
15	13 48	13 24	13 00	12 36	12 12	11 48	11 24	11 00	10 36	10 12
16	14 44	14 20	13 56	13 32	13 08	12 44	12 20	11 56	11 32	11 08
17	15 40	15 16	14 52	14 28	14 04	13 40	13 16	12 52	12 28	12 04
18	16 36	16 12	15 48	15 24	15 00	14 36	14 12	13 48	13 24	13 00
19	17 31	17 07	16 43	16 19	15 55	15 31	15 07	14 43	14 19	13 55
20	18 27	18 03	17 39	17 15	16 51	16 27	16 03	15 39	15 15	14 51
21	19 23	19 00	18 36	18 12	17 48	17 24	17 00	16 36	16 12	15 48
22	20 20	20 00	19 39	19 19	18 59	18 39	18 19	17 59	17 39	17 19
23	21 16	21 00	20 39	20 19	19 59	19 39	19 19	18 59	18 39	18 19
24	22 12	22 01	21 39	21 19	20 59	20 39	20 19	19 59	19 39	19 19
25	23 09	23 02	22 39	22 19	21 59	21 39	21 19	20 59	20 39	20 19
26	24 06	24 03	23 39	23 19	22 59	22 39	22 19	21 59	21 39	21 19
27	25 02	25 04	24 39	24 19	23 59	23 39	23 19	22 59	22 39	22 19
28	25 59	25 25	25 39	25 19	24 59	24 39	24 19	23 59	23 39	23 19
29	26 57	26 35	26 19	25 59	25 39	25 19	24 59	24 39	24 19	23 59
30	27 54	27 33	27 17	26 57	26 37	26 17	25 57	25 37	25 17	24 57

## Tables of Right Ascension.

South Latitude.

	0	1	2	3	4	5	6	7	8	9
$\gamma$	D. M.	D. M.	D. M.	D. M.	D. M.	D. M.	D. M.	D. M.	D. M.	D. M.
0	0 00	0 23	0 47	1 11	1 35	1 59	2 23	2 47	3 12	3 36
1	0 55	1 18	1 42	2 06	2 30	2 54	3 18	3 42	4 06	4 30
2	1 50	2 13	2 37	3 01	3 25	3 49	4 13	4 37	5 01	5 25
3	2 45	3 08	3 32	3 56	4 20	4 44	5 08	5 32	5 56	6 20
4	3 40	4 03	4 27	4 51	5 15	5 39	6 03	6 27	6 51	7 15
5	4 35	4 58	5 22	5 46	6 10	6 34	6 58	7 22	7 46	8 09
6	5 30	5 54	6 18	6 42	7 06	7 30	7 54	8 18	8 42	9 04
7	6 25	6 49	7 13	7 37	8 01	8 25	8 49	9 13	9 37	9 59
8	7 21	7 44	8 08	8 32	8 56	9 20	9 44	10 08	10 32	10 53
9	8 16	8 40	9 04	9 28	9 51	10 15	10 39	11 03	11 27	11 48
10	9 11	9 35	9 59	10 23	10 46	11 10	11 33	11 57	12 21	12 42
11	10 06	10 30	10 54	11 18	11 41	12 05	12 28	12 52	13 16	13 37
12	11 02	11 25	11 49	12 13	12 36	13 00	13 23	13 47	14 11	14 32
13	11 57	12 20	12 44	13 08	13 31	13 55	14 18	14 42	15 06	15 27
14	12 53	13 16	13 39	14 03	14 26	14 50	15 13	15 36	15 59	16 21
15	13 48	14 12	14 35	14 58	15 21	15 45	16 08	16 31	16 54	17 16
16	14 44	15 07	15 30	15 53	16 16	16 40	17 03	17 26	17 49	18 11
17	15 40	16 02	16 25	16 48	17 11	17 35	17 58	18 21	18 44	19 06
18	16 36	16 58	17 21	17 44	18 07	18 30	18 53	19 16	19 39	20 01
19	17 31	17 54	18 17	18 40	19 03	19 26	19 49	20 12	20 35	20 56
20	18 27	18 50	19 13	19 36	19 59	20 22	20 45	21 08	21 31	21 51
21	19 23	19 46	20 09	20 32	20 55	21 18	21 41	22 04	22 27	22 45
22	20 20	20 42	21 05	21 28	21 51	22 14	22 37	22 60	22 83	23 01
23	21 16	21 38	22 01	22 24	22 47	23 10	23 33	23 56	24 19	24 36
24	22 12	22 35	22 57	23 20	23 43	24 06	24 29	24 52	25 15	25 32
25	23 09	23 31	23 53	24 16	24 39	25 02	25 25	25 48	26 11	26 27
26	24 06	24 28	24 51	25 14	25 37	25 60	25 83	26 06	26 29	26 45
27	25 02	25 25	25 48	26 11	26 34	26 57	27 20	27 43	28 06	28 22
28	25 59	26 22	26 45	27 08	27 31	27 54	28 17	28 40	29 03	29 19
29	26 57	27 19	27 42	28 05	28 28	28 51	29 14	29 37	29 60	30 00
30	27 54	28 16	28 39	29 02	29 25	29 48	30 11	30 34	30 57	31 00



## Tables of Right Ascension.

## North Latitude.

	0	1	2	3	4	5	6	7	8	9
8	D. M.	D. M.	D. M.	D. M.	D. M.	D. M.	D. M.	D. M.	D. M.	D. M.
0	27	54	27	33	27	11	26	49	26	27
1	28	51	28	30	28	0	27	47	27	25
2	29	48	29	27	29	06	28	45	28	23
3	30	46	30	25	30	04	29	43	29	21
4	31	44	31	23	31	02	30	41	30	19
5	32	42	32	21	32	00	31	39	31	18
6	33	40	33	20	32	59	32	38	32	17
7	34	38	34	18	33	57	33	37	33	16
8	35	37	35	17	34	57	34	36	34	15
9	36	36	36	16	35	56	35	36	35	15
10	37	34	37	15	36	55	36	35	36	15
11	38	33	38	14	37	54	37	35	37	15
12	39	33	39	14	38	54	38	35	38	15
13	40	32	40	13	39	54	39	35	39	15
14	41	31	41	13	40	54	40	35	40	15
15	42	31	42	13	41	54	41	36	41	17
16	43	31	43	13	42	54	42	36	42	18
17	44	31	44	13	43	55	43	37	43	19
18	45	31	45	14	44	56	44	38	44	20
19	46	32	46	14	45	57	45	39	45	21
20	47	32	47	15	46	58	46	40	46	22
21	48	33	48	16	47	59	47	41	47	23
22	49	34	49	17	48	00	48	42	48	24
23	50	35	50	18	49	01	49	43	49	25
24	51	36	51	20	51	02	50	44	50	26
25	52	38	52	22	52	03	51	45	51	27
26	53	40	53	24	53	04	52	46	52	28
27	54	42	54	27	54	05	53	47	53	29
28	55	44	55	29	55	06	54	48	54	30
29	56	46	56	32	56	07	55	49	55	31
30	57	48	57	35	57	08	56	50	56	32

## Tables of Right Ascension.

## South Latitude.

	0	1	2	3	4	5	6	7	8	9
8	D. M.	D. M.	D. M.	D. M.	D. M.	D. M.	D. M.	D. M.	D. M.	D. M.
0	27	54	28	16	28	37	28	58	29	19
1	28	51	29	13	29	34	29	55	30	16
2	29	49	30	10	30	31	30	52	31	13
3	30	46	31	07	31	28	31	49	32	10
4	31	44	32	05	32	25	32	46	33	07
5	32	42	33	03	33	23	33	43	34	04
6	33	40	34	01	34	21	34	41	35	01
7	34	38	34	59	35	19	35	39	36	58
8	35	37	35	57	36	17	36	37	36	56
9	36	36	36	56	37	15	37	35	37	54
10	37	34	37	54	38	13	38	33	38	52
11	38	33	38	53	39	12	39	31	39	50
12	39	33	39	52	40	11	40	30	40	48
13	40	32	40	51	41	10	41	28	41	46
14	41	31	41	50	42	09	42	27	42	44
15	42	31	42	50	43	08	43	26	43	42
16	43	31	43	49	44	07	44	25	44	40
17	44	31	44	49	45	06	45	24	45	38
18	45	31	45	49	46	06	46	23	46	36
19	46	32	46	49	47	06	47	23	47	34
20	47	32	47	49	48	06	48	23	48	32
21	48	33	48	50	49	06	49	23	49	30
22	49	34	49	50	50	06	50	23	50	28
23	50	35	50	51	51	06	51	23	51	26
24	51	36	51	52	52	07	52	23	52	24
25	52	38	52	53	53	08	53	24	53	22
26	53	40	53	55	54	09	54	25	54	20
27	54	42	54	56	55	11	55	25	55	18
28	55	44	55	58	56	12	56	26	56	16
29	56	46	56	59	57	13	57	27	57	14
30	57	48	57	02	58	15	58	29	58	12



## Tables of Right Ascension.

North Latitude.

	0	1	2	3	4	5	6	7	8	9
π	D. M.	D. M.	D. M.	D. M.	D. M.	D. M.	D. M.	D. M.	D. M.	D. M.
0	57 48	57 35	57 21	57 07	56 53	56 38	56 23	56 08	55 53	55 38
1	58 51	58 38	58 24	58 10	57 57	57 42	57 28	57 13	56 59	56 44
2	59 53	59 41	59 27	59 14	59 01	58 47	58 33	58 19	58 05	57 50
3	60 56	60 44	60 31	60 18	60 05	59 52	59 38	59 25	59 11	58 57
4	61 59	61 47	61 35	61 22	61 10	60 57	60 44	60 31	60 17	60 04
5	63 03	62 51	62 39	62 27	62 15	62 02	61 50	61 37	61 24	61 11
6	64 06	63 55	63 43	63 32	63 20	63 08	62 56	62 44	62 31	62 18
7	65 09	64 59	64 47	64 36	64 25	64 13	64 02	63 50	63 38	63 25
8	66 13	66 03	65 52	65 42	65 30	65 19	65 08	64 56	64 45	64 33
9	67 17	67 07	66 56	66 45	66 34	66 23	66 12	66 01	65 50	65 41
10	68 21	68 11	68 02	67 52	67 42	67 31	67 21	67 10	67 00	66 49
11	69 25	69 16	69 07	68 57	68 48	68 38	68 28	68 18	68 08	67 57
12	70 29	70 21	70 12	70 03	69 54	69 45	69 35	69 26	69 16	69 05
13	71 34	71 26	71 17	71 09	71 00	70 51	70 42	70 33	70 24	70 14
14	72 38	72 31	72 22	72 15	72 06	71 58	71 49	71 41	71 32	71 23
15	73 43	73 36	73 28	73 21	73 13	73 05	72 57	72 49	72 41	72 32
16	74 47	74 41	74 33	74 27	74 19	74 12	74 04	73 57	73 49	73 41
17	75 52	75 46	75 39	75 33	75 26	75 19	75 12	75 05	74 57	74 50
18	76 57	76 51	76 45	76 39	76 33	76 27	76 20	76 14	76 07	76 00
19	78 02	77 56	77 51	77 45	77 40	77 34	77 28	77 22	77 16	77 09
20	79 07	79 02	78 57	78 52	78 47	78 42	78 36	78 30	78 24	78 18
21	80 12	80 08	80 03	80 00	79 55	79 50	79 45	79 40	79 34	79 28
22	81 17	81 13	81 09	81 05	81 01	80 56	80 52	80 48	80 43	80 37
23	82 22	82 18	82 15	82 11	82 08	82 04	82 00	81 57	81 53	81 47
24	83 28	83 24	83 21	83 18	83 15	83 11	83 09	83 06	83 02	82 57
25	84 33	84 30	84 27	84 24	84 21	84 18	84 15	84 12	84 09	84 07
26	85 38	85 35	85 32	85 29	85 26	85 23	85 20	85 17	85 14	85 11
27	86 44	86 41	86 38	86 35	86 32	86 29	86 26	86 23	86 20	86 17
28	87 49	87 46	87 43	87 40	87 37	87 34	87 31	87 28	87 25	87 22
29	88 55	88 52	88 49	88 46	88 43	88 40	88 37	88 34	88 31	88 28
30	90 00	90 00	90 00	90 00	90 00	90 00	90 00	90 00	90 00	90 00

## Tables of Right Ascension.

South Latitude.

	0	1	2	3	4	5	6	7	8	9
π	D. M.	D. M.	D. M.	D. M.	D. M.	D. M.	D. M.	D. M.	D. M.	D. M.
0	57 48	58 02	58 15	58 29	58 42	58 55	59 07	59 20	59 32	59 43
1	58 51	59 04	59 17	59 30	59 43	59 55	60 07	60 20	60 32	60 42
2	59 53	60 06	60 19	60 31	60 44	60 56	61 08	61 20	61 32	61 42
3	60 56	61 08	61 21	61 33	61 46	61 57	62 09	62 21	62 32	62 41
4	61 59	62 11	62 23	62 35	62 48	62 58	63 09	63 21	63 32	63 41
5	63 03	63 16	63 28	63 39	63 50	64 01	64 12	64 24	64 35	64 44
6	64 06	64 18	64 29	64 40	64 51	65 02	65 13	65 24	65 35	65 44
7	65 09	65 20	65 31	65 42	65 53	66 04	66 15	66 26	66 37	66 46
8	66 13	66 24	66 35	66 46	66 57	67 07	67 18	67 29	67 39	67 48
9	67 17	67 28	67 39	67 50	68 01	68 11	68 22	68 32	68 43	68 52
10	68 21	68 32	68 43	68 53	69 04	69 14	69 25	69 35	69 46	69 55
11	69 25	69 36	69 46	69 57	70 07	70 17	70 27	70 38	70 48	70 57
12	70 29	70 40	70 50	71 01	71 11	71 21	71 31	71 42	71 52	72 01
13	71 34	71 45	71 55	72 06	72 16	72 26	72 37	72 47	72 57	73 06
14	72 38	72 49	73 00	73 10	73 20	73 30	73 41	73 51	74 01	74 10
15	73 43	73 54	74 04	74 14	74 24	74 34	74 45	74 55	75 05	75 14
16	74 47	74 58	75 08	75 18	75 28	75 38	75 48	75 58	76 08	76 17
17	75 52	76 03	76 13	76 23	76 33	76 43	76 53	77 03	77 13	77 22
18	76 57	77 07	77 17	77 27	77 37	77 47	77 57	78 07	78 17	78 26
19	78 02	78 12	78 22	78 32	78 42	78 52	79 02	79 12	79 22	79 31
20	79 07	79 17	79 27	79 37	79 47	79 57	80 07	80 17	80 27	80 36
21	80 12	80 22	80 32	80 42	80 52	81 02	81 12	81 22	81 32	81 41
22	81 17	81 27	81 37	81 47	81 57	82 07	82 17	82 27	82 37	82 46
23	82 22	82 32	82 42	82 52	83 02	83 12	83 22	83 32	83 42	83 51
24	83 28	83 38	83 48	83 58	84 08	84 18	84 28	84 38	84 48	84 57
25	84 33	84 43	84 53	85 03	85 13	85 23	85 33	85 43	85 53	86 02
26	85 38	85 48	85 58	86 08	86 18	86 28	86 38	86 48	86 58	87 07
27	86 44	86 54	87 04	87 14	87 24	87 34	87 44	87 54	88 04	88 13
28	87 49	87 59	88 09	88 19	88 29	88 39	88 49	88 59	89 09	89 18
29	88 55	89 05	89 15	89 25	89 35	89 45	89 55	90 05	90 15	90 24
30	90 00	90 10	90 20	90 30	90 40	90 50	91 00	91 10	91 20	91 29



### Tables of Right Ascension.

North Latitude.

	0	1	2	3	4	5	6	7	8	9
Sec.	D. M.	D. M.	D. M.	D. M.	D. M.	D. M.	D. M.	D. M.	D. M.	D. M.
0	90 00	90 00	90 00	90 00	90 00	90 00	90 00	90 00	90 00	90 00
1	91 05	91 08	91 07	91 07	91 07	91 08	91 09	91 09	91 10	91 11
2	92 11	92 12	92 14	92 14	92 15	92 16	92 18	92 18	92 20	92 22
3	93 16	93 18	93 20	93 21	93 23	93 24	93 26	93 27	93 29	93 32
4	94 22	94 24	94 27	94 28	94 30	94 32	94 35	94 36	94 39	94 42
5	95 27	95 30	95 33	95 33	95 38	95 40	95 43	95 45	95 49	95 52
6	96 32	96 36	96 39	96 42	96 45	96 48	96 51	96 54	96 58	97 02
7	97 38	97 42	97 45	97 49	97 52	97 56	98 00	98 03	98 08	98 12
8	98 43	98 47	98 51	98 55	99 00	99 04	99 08	99 12	99 17	99 21
9	99 48	99 52	99 57	100 01	100 07	100 12	100 16	100 21	100 26	100 31
10	100 53	100 58	101 03	101 08	101 14	101 19	101 24	101 30	101 35	101 40
11	100 58	102 04	102 09	102 15	102 21	102 26	102 32	102 38	102 44	102 50
12	103 03	103 08	103 15	103 21	103 27	103 33	103 40	103 46	103 53	103 59
13	104 08	104 14	104 21	104 27	104 34	104 41	104 48	104 55	105 02	105 09
14	105 13	105 16	105 22	105 33	105 41	105 48	105 56	106 03	106 11	106 18
15	106 17	106 24	106 33	106 39	106 47	106 55	107 03	107 11	107 19	107 27
16	107 22	107 29	107 38	107 45	107 53	108 02	108 11	108 19	108 28	108 36
17	108 26	108 34	108 43	108 53	108 55	109 05	109 18	109 27	109 36	109 45
18	109 31	109 39	109 47	109 57	110 05	110 15	110 25	110 34	110 44	110 54
19	110 35	110 44	110 53	111 03	111 12	111 22	111 32	111 42	112 52	112 02
20	111 35	111 44	111 53	112 03	112 12	112 22	112 33	112 50	113 00	113 11
21	112 43	112 53	113 03	113 13	113 24	113 35	113 46	113 57	114 08	114 19
22	113 47	113 57	114 07	114 18	114 30	114 41	114 52	115 04	115 15	115 27
23	114 51	115 01	115 13	115 23	115 35	115 47	115 58	116 10	116 22	116 35
24	115 54	116 05	116 17	116 27	116 41	116 52	117 04	117 17	117 29	117 42
25	116 57	117 08	117 21	117 33	117 46	117 58	118 11	118 23	118 36	118 49
26	118 03	118 15	118 28	118 37	118 51	119 05	119 19	119 29	119 43	119 56
27	119 06	119 19	119 29	119 42	119 55	120 08	120 22	120 35	120 49	121 03
28	120 07	120 19	120 33	120 47	120 59	121 13	121 27	121 41	121 55	122 10
29	121 08	121 22	121 36	121 50	122 03	122 18	122 32	122 47	123 01	123 16
30	122 13	122 27	122 36	122 53	123 07	123 22	123 37	123 52	124 07	124 22

### Tables of Right Ascension.

*South Latitude*

	0	1	2	3	4	5	6	7	8	9
Σ	D. M.	D. M.	D. M.	D. M.	D. M.	D. M.	D. M.	D. M.	D. M.	D. M.
0	90 00	90 00	90 00	90 00	90 00	90 00	90 00	90 00	90 00	90 00
1	91 05	91 05	91 05	91 04	91 04	91 03	91 03	91 02	91 02	91 02
2	92 11	92 10	92 10	92 08	92 08	92 06	92 06	92 04	92 04	92 03
3	93 16	93 15	93 14	93 12	93 11	93 09	93 08	93 06	93 05	93 05
4	94 22	94 20	94 19	94 16	94 15	94 12	94 11	94 08	94 07	94 06
5	95 27	95 25	95 23	95 20	95 18	95 15	95 13	95 10	95 09	95 07
6	96 32	96 30	96 27	96 24	96 21	96 18	96 15	96 12	96 10	96 08
7	97 38	97 35	97 31	97 28	97 25	97 21	97 18	97 14	97 12	97 09
8	98 43	98 39	98 35	98 32	98 28	98 24	98 20	98 16	98 13	98 10
9	99 48	99 43	99 39	99 35	99 31	99 26	99 22	99 18	99 14	99 11
10	100 53	100 48	100 43	100 39	100 34	100 29	100 25	100 20	100 16	100 12
11	101 58	101 53	101 47	101 42	101 37	101 32	101 27	101 22	101 17	101 12
12	103 03	102 57	102 51	102 45	102 40	102 34	102 29	102 23	102 18	102 13
13	104 08	104 02	103 55	103 49	103 43	103 37	103 31	103 25	103 20	103 14
14	105 13	105 06	104 59	104 52	104 46	104 40	104 33	104 27	104 21	104 14
15	106 17	106 10	106 03	105 56	105 49	105 42	105 35	105 28	105 22	105 15
16	107 22	107 14	107 07	106 59	106 52	106 45	106 37	106 30	106 23	106 15
17	108 26	108 18	108 10	118 02	107 55	107 47	107 39	107 32	107 24	107 15
18	109 31	109 22	109 14	109 05	108 57	108 49	108 41	108 33	108 25	108 16
19	110 35	110 26	110 17	110 08	110 00	109 51	109 43	109 34	109 26	109 16
20	111 39	111 30	111 20	111 11	111 02	110 53	110 44	110 35	110 27	110 16
21	112 43	112 33	112 23	112 13	112 04	111 55	111 45	111 36	111 27	111 16
22	113 47	113 37	113 26	113 16	113 06	112 56	112 47	112 37	112 27	112 17
23	114 51	114 40	114 29	114 19	114 08	113 58	113 48	113 38	113 28	113 17
24	115 54	115 43	115 32	115 21	115 10	114 59	114 48	114 38	114 28	114 17
25	116 57	116 46	116 35	116 23	116 12	116 01	115 50	115 39	115 28	115 17
26	118 01	117 49	117 37	117 25	117 14	117 02	116 51	116 39	116 28	116 17
27	119 04	118 51	118 38	118 27	118 15	118 03	117 52	117 39	117 28	117 16
28	120 07	119 54	119 41	119 29	119 19	119 07	118 55	118 42	118 28	118 16
29	121 09	120 56	120 43	120 30	120 17	120 05	119 53	119 40	119 28	119 15
30	122 12	121 58	121 45	121 32	121 18	121 05	120 53	120 40	120 28	120 15



## Tables of Right Ascension.

North Latitude.

	0	1	2	3	4	5	6	7	8	9
Ω	D. M.	D. M.	D. M.	D. M.	D. M.	D. M.	D. M.	D. M.	D. M.	D. M.
0	122 12	122 25	122 39	122 53	123 07	123 22	123 37	123 52	124 07	124 22
1	123 14	123 28	123 42	123 57	124 11	124 26	124 42	124 57	125 12	125 28
2	124 16	124 31	124 45	125 00	125 15	125 30	125 46	126 02	126 17	126 33
3	125 18	125 33	125 48	126 03	126 18	126 34	126 50	127 06	127 22	127 38
4	126 20	126 36	126 51	127 06	127 22	127 38	127 54	128 11	128 27	128 43
5	127 22	127 38	127 54	128 09	128 25	128 42	128 58	129 15	129 32	129 48
6	128 24	128 40	128 56	129 12	129 28	129 45	130 02	130 19	130 36	130 53
7	129 25	129 42	129 58	130 14	130 31	130 48	131 05	131 23	131 40	131 58
8	130 26	130 43	131 01	131 16	131 33	131 51	132 08	132 26	132 44	133 02
9	131 27	131 44	132 01	132 18	132 35	132 53	133 11	133 29	133 47	134 06
10	132 28	132 45	133 02	133 20	133 37	133 55	134 14	134 32	134 50	135 09
11	133 28	133 46	134 03	134 21	134 39	134 57	135 16	135 35	135 53	136 12
12	134 29	134 47	135 04	135 22	135 40	135 59	136 18	136 37	136 56	137 15
13	135 29	135 47	136 05	136 23	136 41	137 00	137 20	137 39	137 58	138 17
14	136 29	136 47	137 06	137 24	137 42	138 01	138 21	138 41	139 00	139 20
15	137 29	137 47	138 06	138 24	138 43	139 02	139 22	139 42	140 02	140 22
16	138 29	138 47	139 06	139 25	139 44	140 03	140 24	140 44	141 04	141 24
17	139 28	139 47	140 06	140 25	140 45	141 04	141 25	141 45	142 06	142 26
18	140 28	140 46	141 06	141 25	141 45	142 05	142 26	142 46	143 07	143 27
19	141 27	141 46	142 06	142 25	142 45	143 06	143 27	143 47	144 08	144 28
20	142 26	142 45	143 05	143 25	143 45	144 06	144 27	144 48	145 09	145 29
21	143 25	143 44	144 04	144 24	144 45	145 06	145 27	145 48	146 09	146 30
22	144 24	144 43	145 03	145 24	145 45	146 06	146 27	146 48	147 09	147 31
23	145 23	145 42	146 02	146 23	146 44	147 05	147 27	147 48	148 09	148 31
24	146 20	146 40	147 01	147 22	147 43	148 04	148 26	148 48	149 10	149 31
25	147 18	147 39	148 00	148 21	148 42	149 03	149 25	149 47	150 10	150 31
26	148 16	148 37	148 58	149 19	149 41	150 02	150 24	150 46	151 08	151 31
27	149 14	149 35	149 56	150 17	150 38	151 01	151 23	151 45	152 08	152 31
28	150 11	150 32	150 54	151 15	151 37	151 59	152 22	152 44	153 07	153 29
29	151 09	151 30	151 52	152 13	152 35	152 57	153 20	153 43	154 06	154 28
30	152 06	152 27	152 49	153 11	153 33	153 55	154 18	154 42	155 04	155 27

## Tables of Right Ascension.

South Latitude.

	0	1	2	3	4	5	6	7	8	9
Ω	D. M.	D. M.	D. M.	D. M.	D. M.	D. M.	D. M.	D. M.	D. M.	D. M.
0	122 12	121 58	121 45	121 31	121 18	121 05	120 53	120 40	120 28	120 15
1	123 14	123 00	122 47	122 33	122 19	122 06	121 53	121 40	121 29	121 15
2	124 16	124 02	123 48	123 34	123 20	123 06	122 53	122 40	122 27	122 14
3	125 18	125 03	124 49	124 35	124 21	124 07	123 53	123 39	123 26	123 13
4	126 20	126 05	125 51	125 36	125 22	125 07	124 53	124 39	124 25	124 12
5	126 22	127 07	126 52	126 36	126 22	126 07	125 52	125 38	125 24	125 11
6	128 24	128 08	127 53	127 37	127 22	127 07	126 52	126 37	126 23	126 09
7	129 25	129 09	128 54	128 37	128 22	128 07	127 51	127 36	127 22	127 07
8	130 26	130 10	129 54	129 37	129 22	129 06	128 50	128 35	128 20	128 05
9	131 27	131 10	130 54	130 37	130 21	130 05	129 49	129 33	129 18	129 03
10	132 28	132 11	131 54	131 37	131 21	131 04	130 48	130 32	130 17	130 01
11	133 28	133 11	132 54	132 37	132 20	132 03	131 47	131 31	131 15	130 58
12	134 29	134 11	133 54	133 37	133 19	133 02	132 46	132 29	132 13	131 56
13	135 29	135 11	134 54	134 36	134 18	134 01	133 45	133 28	133 11	132 54
14	136 29	136 11	135 53	135 35	135 17	135 00	134 43	134 25	134 09	133 51
15	137 29	137 10	136 52	136 34	136 16	135 58	135 41	135 23	135 06	134 48
16	138 29	138 10	137 51	137 33	137 15	136 57	136 39	136 21	136 04	135 45
17	139 28	139 09	138 50	138 32	138 14	137 55	137 37	137 19	137 02	136 42
18	140 27	140 08	139 49	139 30	139 13	138 53	138 35	138 17	137 59	137 39
19	141 27	141 07	140 48	140 29	140 10	139 51	139 33	139 15	138 56	138 36
20	142 26	142 06	141 47	141 27	141 08	140 49	140 31	140 12	139 53	139 33
21	143 24	143 04	142 45	142 25	142 06	141 47	141 28	141 09	140 50	140 30
22	144 23	144 03	143 43	143 23	143 04	142 45	142 25	142 06	141 47	141 27
23	145 22	145 01	144 41	144 21	144 02	143 42	143 22	143 03	142 44	142 24
24	146 20	145 59	145 39	145 19	144 59	144 39	144 19	143 59	143 40	143 20
25	147 18	146 57	146 37	146 17	145 56	145 36	145 16	144 56	144 37	144 16
26	148 16	147 55	147 35	147 14	146 53	146 33	146 13	145 53	145 33	145 12
27	149 14	148 53	148 32	148 11	147 50	147 29	147 09	146 49	146 29	146 08
28	150 11	149 50	149 29	149 08	148 47	148 26	148 06	147 46	147 25	147 04
29	151 09	150 47	150 26	150 05	149 44	149 23	149 03	148 42	148 21	148 00
30	152 06	151 44	151 23	151 02	150 41	150 20	149 59	149 38	149 17	148 56



## Tables of Right Ascension.

North Latitude.

	0	1	2	3	4	5	6	7	8	9
度	D. M. D. M.	D. M. D. M.	D. M. D. M.	D. M. D. M.	D. M. D. M.	D. M. D. M.	D. M. D. M.	D. M. D. M.	D. M. D. M.	D. M. D. M.
0	152 06	152 27	152 49	153 11	153 33	153 55	154 18	154 41	155 04	155 27
1	153 04	153 25	153 47	154 09	154 31	154 53	155 16	155 39	156 03	156 26
2	154 01	154 22	154 44	155 06	155 29	155 51	156 14	156 37	157 01	157 25
3	154 58	155 19	155 41	156 03	156 26	156 49	157 12	157 35	157 59	158 23
4	155 54	156 16	156 39	157 01	157 24	157 47	158 10	158 33	158 57	159 21
5	156 51	157 13	157 36	157 58	158 21	158 44	159 08	159 31	159 55	160 19
6	157 48	158 10	158 33	158 55	159 18	159 41	160 05	160 28	160 52	161 16
7	158 44	159 07	159 30	159 51	160 15	160 38	161 02	161 25	161 49	162 13
8	159 40	160 04	160 27	160 49	161 12	161 35	161 59	162 22	162 46	163 10
9	160 37	161 00	161 23	161 45	162 09	162 32	162 56	163 19	163 43	164 07
10	161 33	161 56	162 19	162 42	163 06	163 29	163 53	164 16	164 40	165 04
11	162 29	162 52	163 15	163 38	164 02	164 25	164 49	165 13	165 37	166 01
12	163 25	163 50	164 11	164 34	164 58	165 21	165 45	166 09	166 33	166 58
13	164 20	164 44	165 07	165 30	165 54	166 18	166 42	167 06	167 30	167 54
14	165 16	165 40	166 03	166 26	166 50	167 14	167 38	168 02	168 26	168 50
15	166 12	166 35	166 59	167 22	167 46	168 10	168 34	168 58	169 22	169 46
16	167 07	167 31	167 55	168 18	168 42	169 06	169 30	169 54	170 18	170 42
17	168 03	168 27	168 51	169 14	169 38	170 02	170 26	170 50	171 14	171 38
18	168 58	169 23	169 46	170 09	170 33	170 57	171 21	171 45	172 09	172 34
19	169 54	170 18	170 42	171 05	171 29	171 53	172 17	172 41	173 05	173 30
20	170 49	171 13	171 37	172 01	172 25	172 49	173 13	173 37	174 01	174 25
21	171 44	172 08	172 32	172 56	173 20	173 44	174 08	174 32	174 56	175 21
22	172 39	173 03	173 27	173 51	174 15	174 39	175 03	175 27	175 51	176 16
23	173 35	173 59	174 22	174 46	175 10	175 34	175 58	176 22	176 46	177 12
24	174 30	174 53	175 17	175 41	176 05	176 29	176 53	177 17	177 41	178 07
25	175 25	175 48	176 12	176 36	176 60	177 24	177 48	178 12	178 36	179 02
26	176 20	176 43	177 07	177 31	177 56	178 19	178 43	179 07	179 31	179 57
27	177 15	177 38	178 02	178 26	178 50	179 14	179 38	180 02	180 26	180 52
28	178 10	178 33	178 57	179 21	179 45	180 09	180 33	180 57	181 21	181 47
29	179 05	179 28	179 52	180 16	180 40	181 04	181 28	181 52	182 17	182 42
30	180 00	180 23	180 47	181 11	181 35	181 59	182 23	182 47	183 12	183 37

## Tables of Right Ascension.

South Latitude.

	0	1	2	3	4	5	6	7	8	9
度	D. M. D. M.	D. M. D. M.	D. M. D. M.	D. M. D. M.	D. M. D. M.	D. M. D. M.	D. M. D. M.	D. M. D. M.	D. M. D. M.	D. M. D. M.
0	152 06	151 44	151 23	151 02	150 41	150 20	149 59	149 38	149 17	148 56
1	153 04	152 41	152 20	151 59	151 38	151 16	150 55	150 34	150 13	149 52
2	154 01	153 38	153 17	152 55	152 34	152 12	151 51	151 30	151 09	150 48
3	154 58	154 35	154 13	153 52	153 30	153 08	152 47	152 25	152 04	151 43
4	155 54	155 32	155 10	154 48	154 26	154 04	153 43	153 21	153 00	152 38
5	156 51	156 29	156 07	155 44	155 22	155 00	154 39	154 17	153 55	153 33
6	157 48	157 25	157 03	156 40	156 18	155 56	155 34	155 12	154 50	154 28
7	158 44	158 22	157 59	157 36	157 14	156 52	156 30	156 08	155 46	155 23
8	159 40	159 18	158 55	158 32	158 10	157 48	157 26	157 03	156 41	156 18
9	160 37	160 14	159 51	159 28	159 06	158 43	158 21	157 58	157 36	157 13
10	161 33	161 10	160 47	160 24	160 02	159 39	159 17	158 54	158 31	158 08
11	162 29	162 06	161 43	161 20	160 58	160 35	160 12	159 49	159 26	159 03
12	163 25	163 02	162 39	162 16	161 53	161 30	161 07	160 44	160 21	159 58
13	164 20	163 58	163 35	163 12	162 49	162 26	162 02	161 39	161 16	160 53
14	165 16	164 53	164 30	164 07	163 44	163 20	162 57	162 34	162 11	161 48
15	166 12	165 48	165 25	165 02	164 39	164 15	163 52	163 29	163 06	162 43
16	167 07	166 44	166 21	165 57	165 34	165 10	164 47	164 24	164 01	163 38
17	168 03	167 40	167 17	166 52	166 29	166 05	165 42	165 19	164 56	164 33
18	168 58	168 35	168 12	167 47	167 24	167 00	166 37	166 13	165 50	165 28
19	169 54	169 31	169 08	168 43	168 19	167 55	167 32	167 08	166 46	166 23
20	170 49	170 26	170 02	169 38	169 14	168 50	168 27	168 03	167 41	167 17
21	171 44	171 21	170 57	170 33	170 09	169 45	169 22	168 58	168 35	168 12
22	172 39	172 16	171 52	171 28	171 04	170 40	170 17	169 53	169 30	169 07
23	173 35	173 11	172 47	172 23	171 59	171 35	171 12	170 48	170 25	170 01
24	174 30	174 06	173 42	173 18	172 54	172 30	172 07	171 43	171 20	170 56
25	175 25	175 02	174 38	174 14	173 50	173 26	173 02	172 38	172 15	171 51
26	176 20	175 57	175 33	175 09	174 45	174 21	173 57	173 33	173 10	172 45
27	177 15	176 52	176 28	176 04	175 40	175 16	174 52	174 28	174 04	173 40
28	178 10	177 47	177 23	176 59	176 35	176 11	175 47	175 23	174 59	174 34
29	179 05	178 42	178 18	177 54	177 30	177 06	176 42	176 18	175 54	175 29
30	180 00	179 37	179 13	178 49	178 25	178 01	177 37	177 13	176 49	176 24



## Tables of Right Ascension.

North Latitude.

	0	1	2	3	4	5	6	7	8	9
$\alpha$	D. M.	D. M.	D. M.	D. M.	D. M.	D. M.	D. M.	D. M.	D. M.	D. M.
0	180 05	180 23	180 47	181 11	181 35	181 59	182 23	182 47	183 12	183 37
1	180 55	181 18	181 42	182 06	182 30	182 54	183 18	183 42	184 06	184 31
2	181 50	182 13	182 37	183 01	183 25	183 49	184 13	184 37	185 01	185 25
3	182 45	183 08	183 32	183 56	184 20	184 44	185 08	185 32	185 56	186 20
4	183 40	184 03	184 27	184 51	185 15	185 39	186 03	186 27	186 50	187 14
5	184 25	184 58	185 22	185 46	186 10	186 34	186 58	187 22	187 45	188 08
6	185 30	185 54	186 18	186 42	187 06	187 30	187 53	188 17	188 40	189 03
7	186 25	186 49	187 13	187 37	188 01	188 25	188 48	189 12	189 35	189 57
8	187 21	187 44	188 08	188 32	188 56	189 20	189 43	190 07	190 30	190 52
9	188 16	188 39	189 03	189 27	189 51	190 15	190 38	191 02	191 25	191 46
10	189 11	189 34	189 58	190 22	190 46	191 10	191 33	191 57	192 19	192 41
11	190 06	190 29	190 53	191 17	191 41	192 05	192 28	192 52	193 14	193 36
12	191 02	191 25	191 48	192 12	192 36	192 59	193 23	193 47	194 09	194 31
13	191 57	192 20	192 43	193 08	193 31	193 55	194 18	194 41	195 04	195 26
14	192 53	193 16	193 39	194 03	194 26	194 50	195 13	195 36	195 59	196 21
15	193 48	194 12	194 35	194 58	195 21	195 45	196 08	196 31	196 54	197 16
16	194 44	195 07	195 30	195 53	196 16	196 40	197 03	197 26	197 49	198 11
17	195 40	196 02	196 25	196 48	197 11	197 35	197 58	198 21	198 44	199 06
18	196 35	196 58	197 21	197 44	198 07	198 30	198 53	199 16	199 39	200 01
19	197 31	197 54	198 17	198 40	199 02	199 25	199 48	200 11	200 34	200 56
20	198 27	198 50	199 13	199 36	199 58	200 21	200 43	201 07	201 29	201 51
21	199 23	199 46	200 09	200 32	200 54	201 16	201 39	202 02	202 24	202 46
22	200 20	200 42	201 05	201 28	201 50	202 12	202 34	202 57	203 19	203 41
23	201 16	201 38	202 01	202 24	202 46	203 08	203 30	203 52	204 14	204 36
24	202 12	202 35	202 57	203 20	203 42	204 04	204 26	204 48	205 10	205 31
25	203 09	203 31	203 53	204 16	204 38	205 00	205 21	205 43	206 05	206 26
26	204 06	204 29	204 50	205 12	205 34	205 56	206 17	206 39	207 00	207 22
27	205 02	205 25	205 47	206 09	206 31	206 53	207 15	207 37	207 58	208 19
28	205 59	206 22	206 43	207 05	207 27	207 48	208 09	208 30	208 51	209 12
29	206 57	207 19	207 40	208 01	208 22	208 44	209 05	209 26	209 47	210 08
30	207 54	208 16	208 37	208 58	209 19	209 40	210 01	210 22	210 43	211 04

## Tables of Right Ascension.

South Latitude.

	0	1	2	3	4	5	6	7	8	9
$\alpha$	D. M.	D. M.	D. M.	D. M.	D. M.	D. M.	D. M.	D. M.	D. M.	D. M.
0	180 00	179 37	179 13	178 49	178 25	178 01	177 37	177 13	176 48	176 24
1	180 55	180 32	180 08	179 44	179 20	178 56	178 32	178 08	177 43	177 19
2	181 50	181 27	181 03	180 39	180 15	179 51	179 27	179 03	178 38	178 14
3	182 45	182 22	181 58	181 34	181 10	180 46	180 22	179 58	179 34	179 09
4	183 40	183 17	182 53	182 29	182 05	181 41	181 17	180 53	180 29	180 05
5	184 35	184 12	183 48	183 24	183 00	182 36	182 12	181 48	181 24	181 00
6	185 30	185 07	184 43	184 19	183 55	183 31	183 07	182 43	182 19	181 55
7	186 25	186 02	185 38	185 14	184 50	184 26	184 02	183 38	183 14	182 50
8	187 21	186 57	186 33	186 09	185 45	185 21	184 57	184 33	184 09	183 45
9	188 16	187 52	187 28	187 04	186 40	186 16	185 52	185 28	185 04	184 41
10	189 11	188 47	188 23	187 59	187 35	187 11	186 47	186 23	185 59	185 36
11	190 06	189 42	189 18	188 55	188 31	188 07	187 43	187 18	186 55	186 32
12	191 02	190 38	190 14	189 51	189 27	189 03	188 39	188 14	187 51	187 27
13	191 57	191 33	191 09	190 46	190 22	189 58	189 34	189 10	188 46	188 23
14	192 53	192 29	192 05	191 42	191 18	190 54	190 30	190 06	189 42	189 18
15	193 48	193 25	193 01	192 38	192 14	191 50	191 26	191 02	190 38	190 14
16	194 44	194 20	193 57	193 34	193 10	192 46	192 22	191 58	191 34	191 10
17	195 40	195 16	194 53	194 30	194 06	193 42	193 18	192 54	192 30	192 06
18	196 35	196 12	195 49	195 26	195 02	194 38	194 15	193 51	193 27	193 02
19	197 31	197 07	196 45	196 22	195 58	195 35	195 11	194 47	194 23	193 59
20	198 27	198 04	197 41	197 18	196 54	196 31	196 07	195 44	195 20	194 55
21	199 23	199 00	198 37	198 14	197 51	197 28	197 04	196 41	196 17	195 52
22	200 20	199 56	199 33	199 10	198 48	198 25	198 01	197 38	197 14	196 49
23	201 16	200 53	200 30	200 08	199 45	199 22	198 58	198 35	198 11	197 46
24	202 12	201 50	201 27	201 05	200 42	200 19	199 55	199 32	199 08	198 44
25	203 09	202 47	202 24	202 02	201 39	201 16	200 52	200 29	200 05	199 41
26	204 06	203 44	203 21	202 59	202 36	202 13	201 50	201 27	201 03	200 39
27	205 02	204 41	204 19	203 57	203 34	203 11	202 48	202 25	202 01	201 37
28	205 59	205 38	205 16	204 54	204 31	204 08	203 46	203 23	202 59	202 35
29	206 57	206 35	206 13	205 51	205 29	205 07	204 44	204 21	203 57	203 34
30	207 54	207 33	207 11	206 49	206 27	206 05	205 42	205 19	204 56	204 33



## Tables of Right Ascension.

North Latitude.

	0	1	2	3	4	5	6	7	8	9
m	D. M.	D. M.	D. M.	D. M.	D. M.	D. M.	D. M.	D. M.	D. M.	D. M.
0	207 54	208 16	208 37	208 58	209 19	209 40	210 01	210 22	210 43	211 04
1	208 51	209 13	209 34	209 55	210 16	210 37	210 57	211 18	211 39	211 59
2	209 47	210 18	210 39	211 00	211 21	211 42	212 03	212 24	212 45	213 05
3	210 46	211 17	211 38	211 59	212 10	212 31	212 52	213 13	213 34	213 54
4	211 44	212 05	212 26	212 47	213 07	213 28	213 49	214 10	214 31	214 52
5	212 42	213 03	213 24	213 45	214 04	214 25	214 46	215 07	215 28	215 49
6	213 40	214 01	214 22	214 43	215 04	215 25	215 46	216 07	216 28	216 49
7	214 38	214 59	215 20	215 41	215 62	216 03	216 24	216 45	217 06	217 27
8	215 37	215 58	216 19	216 40	217 01	217 22	217 43	218 04	218 25	218 46
9	216 36	216 57	217 18	217 39	217 60	218 01	218 22	218 43	219 04	219 25
10	217 34	217 55	218 16	218 37	218 58	219 19	219 40	220 01	220 22	220 43
11	218 33	218 54	219 15	219 36	219 57	220 18	220 39	220 60	221 01	221 22
12	219 32	219 53	220 14	220 35	220 56	221 17	221 38	221 59	222 20	222 41
13	220 31	220 52	221 13	221 34	221 55	222 16	222 37	222 58	223 19	223 40
14	221 30	221 51	222 12	222 33	222 54	223 15	223 36	223 57	224 18	224 39
15	222 29	222 50	223 11	223 32	223 53	224 14	224 35	224 56	225 17	225 38
16	223 28	223 49	224 10	224 31	224 52	225 13	225 34	225 55	226 16	226 37
17	224 27	224 48	225 09	225 30	225 51	226 12	226 33	226 54	227 15	227 36
18	225 26	225 47	226 08	226 29	226 50	227 11	227 32	227 53	228 14	228 35
19	226 25	226 46	227 07	227 28	227 49	228 10	228 31	228 52	229 13	229 34
20	227 24	227 45	228 06	228 27	228 48	229 09	229 30	229 51	230 12	230 33
21	228 23	228 44	229 05	229 26	229 47	230 08	230 29	230 50	231 11	231 32
22	229 22	229 43	230 04	230 25	230 46	231 07	231 28	231 49	232 10	232 31
23	230 21	230 42	231 03	231 24	231 45	232 06	232 27	232 48	233 09	233 30
24	231 20	231 41	232 02	232 23	232 44	233 05	233 26	233 47	234 08	234 29
25	232 19	232 40	233 01	233 22	233 43	234 04	234 25	234 46	235 07	235 28
26	233 18	233 39	234 00	234 21	234 42	235 03	235 24	235 45	236 06	236 27
27	234 17	234 38	235 00	235 21	235 42	236 03	236 24	236 45	237 06	237 27
28	235 16	235 37	236 00	236 21	236 42	237 03	237 24	237 45	238 06	238 27
29	236 15	236 36	237 00	237 21	237 42	238 03	238 24	238 45	239 06	239 27
30	237 14	237 35	238 00	238 21	238 42	239 03	239 24	239 45	240 06	240 27

## Tables of Right Ascension.

South Latitude.

	0	1	2	3	4	5	6	7	8	9
m	D. M.	D. M.	D. M.	D. M.	D. M.	D. M.	D. M.	D. M.	D. M.	D. M.
0	207 54	208 16	208 37	208 58	209 19	209 40	210 01	210 22	210 43	211 04
1	208 51	209 13	209 34	209 55	210 16	210 37	210 57	211 18	211 39	211 59
2	209 47	210 18	210 39	211 00	211 21	211 42	212 03	212 24	212 45	213 05
3	210 46	211 17	211 38	211 59	212 10	212 31	212 52	213 13	213 34	213 54
4	211 44	212 05	212 26	212 47	213 07	213 28	213 49	214 10	214 31	214 52
5	212 42	213 03	213 24	213 45	214 04	214 25	214 46	215 07	215 28	215 49
6	213 40	214 01	214 22	214 43	215 04	215 25	215 46	216 07	216 28	216 49
7	214 38	214 59	215 20	215 41	215 62	216 03	216 24	216 45	217 06	217 27
8	215 37	215 58	216 19	216 40	217 01	217 22	217 43	218 04	218 25	218 46
9	216 36	216 57	217 18	217 39	217 60	218 01	218 22	218 43	219 04	219 25
10	217 34	217 55	218 16	218 37	218 58	219 19	219 40	220 01	220 22	220 43
11	218 33	218 54	219 15	219 36	219 57	220 18	220 39	220 60	221 01	221 22
12	219 32	219 53	220 14	220 35	220 56	221 17	221 38	221 59	222 20	222 41
13	220 31	220 52	221 13	221 34	221 55	222 16	222 37	222 58	223 19	223 40
14	221 30	221 51	222 12	222 33	222 54	223 15	223 36	223 57	224 18	224 39
15	222 29	222 50	223 11	223 32	223 53	224 14	224 35	224 56	225 17	225 38
16	223 28	223 49	224 10	224 31	224 52	225 13	225 34	225 55	226 16	226 37
17	224 27	224 48	225 09	225 30	225 51	226 12	226 33	226 54	227 15	227 36
18	225 26	225 47	226 08	226 29	226 50	227 11	227 32	227 53	228 14	228 35
19	226 25	226 46	227 07	227 28	227 49	228 10	228 31	228 52	229 13	229 34
20	227 24	227 45	228 06	228 27	228 48	229 09	229 30	229 51	230 12	230 33
21	228 23	228 44	229 05	229 26	229 47	230 08	230 29	230 50	231 11	231 32
22	229 22	229 43	230 04	230 25	230 46	231 07	231 28	231 49	232 10	232 31
23	230 21	230 42	231 03	231 24	231 45	232 06	232 27	232 48	233 09	233 30
24	231 20	231 41	232 02	232 23	232 44	233 05	233 26	233 47	234 08	234 29
25	232 19	232 40	233 01	233 22	233 43	234 04	234 25	234 46	235 07	235 28
26	233 18	233 39	234 00	234 21	234 42	235 03	235 24	235 45	236 06	236 27
27	234 17	234 38	235 00	235 21	235 42	236 03	236 24	236 45	237 06	237 27
28	235 16	235 37	236 00	236 21	236 42	237 03	237 24	237 45	238 06	238 27
29	236 15	236 36	237 00	237 21	237 42	238 03	238 24	238 45	239 06	239 27
30	237 14	237 35	238 00	238 21	238 42	239 03	239 24	239 45	240 06	240 27



### Tables of Right Ascension.

North Latitude.

	0		1		2		3		4		5		6		7		8		9	
F	D.	M.	D.	M.	D.	M.	D.	M.	D.	M.	D.	M.	D.	M.	D.	M.	D.	M.	D.	M.
0	237	48	238	02	238	15	238	29	238	42	238	55	239	07	239	20	239	32	239	44
1	238	51	239	04	239	17	239	30	239	43	239	55	240	07	240	20	240	32	240	44
2	239	53	240	06	240	19	240	31	240	44	240	56	241	08	241	20	241	32	241	43
3	240	56	241	09	241	21	241	33	241	45	241	57	242	09	242	21	242	32	242	43
4	241	59	242	11	242	23	242	35	242	48	242	58	243	09	243	21	243	32	243	43
5	243	03	243	14	243	25	243	37	243	48	243	59	244	10	244	21	244	32	244	43
6	244	06	244	17	244	28	244	39	244	50	245	01	245	11	245	22	245	32	245	43
7	245	09	245	20	245	31	245	41	245	52	246	02	246	12	246	22	246	32	246	43
8	246	13	246	23	246	34	246	44	246	54	247	04	247	13	247	23	247	33	247	43
9	247	17	247	27	247	37	247	47	247	56	248	06	248	15	248	24	248	33	248	43
10	248	21	248	30	248	40	248	49	248	58	249	07	249	16	249	25	249	33	249	43
11	249	25	249	34	249	43	249	52	250	00	250	09	250	17	250	26	250	34	250	44
12	250	30	250	38	250	46	250	55	251	03	251	11	251	19	251	27	251	35	251	44
13	251	34	251	42	251	49	251	57	252	05	252	13	252	21	252	28	252	36	252	44
14	252	38	252	46	252	53	253	01	253	08	253	15	253	23	253	30	253	37	253	45
15	253	43	253	50	253	57	254	04	254	11	254	18	254	25	254	32	254	38	254	45
16	254	47	254	54	255	01	255	07	255	14	255	20	255	27	255	33	255	39	255	46
17	255	52	255	58	256	05	256	11	256	17	256	22	256	29	256	35	256	42	256	47
18	256	57	257	03	257	09	257	15	257	20	257	25	257	31	257	37	257	42	257	48
19	258	02	258	07	258	13	258	18	258	23	258	28	258	33	258	38	258	43	258	48
20	259	07	259	12	259	17	259	21	259	26	259	31	259	35	259	40	259	44	260	50
21	260	12	260	17	260	21	260	25	260	29	260	34	260	38	260	42	260	46	260	51
22	261	17	261	21	261	25	261	28	261	32	261	36	261	40	261	44	261	47	261	52
23	262	22	262	25	262	28	262	32	262	35	262	39	262	42	262	46	262	49	262	54
24	263	28	263	30	263	33	263	37	263	40	263	43	263	47	263	50	263	53	263	54
25	264	33	264	3	264	37	264	40	264	42	264	45	264	47	264	50	264	51	264	55
26	265	38	265	4	265	41	265	44	265	45	265	48	265	49	265	52	265	53	265	57
27	266	44	266	45	266	46	266	47	266	47	266	51	266	52	266	54	266	55	266	57
28	267	48	267	49	267	49	267	50	267	50	267	54	267	54	267	56	267	57	267	57
29	268	55	268	55	268	55	268	56	268	56	268	57	268	57	268	58	268	58	268	58
30	270	00	270	00	270	00	270	00	270	00	270	00	270	00	270	00	270	00	270	00

### Tables of Right Ascension.

*South Latitude.*

	0		1		2		3		4		5		6		7		8		9	
°	D.	M.	D.	M.	D.	M.	D.	M.	D.	M.	D.	M.	D.	M.	D.	M.	D.	M.	D.	M.
0	237	48	237	35	237	21	237	07	236	53	236	38	236	23	236	08	235	53	235	38
1	238	51	238	38	238	24	238	10	237	57	237	42	237	28	237	13	236	59	236	45
2	239	53	239	41	239	28	239	14	239	01	238	47	238	33	238	19	238	05	237	51
3	240	56	240	44	240	31	240	18	240	05	239	52	239	38	239	25	239	11	238	58
4	241	59	241	47	241	35	241	22	241	10	240	57	240	44	240	31	240	17	240	05
5	243	03	242	51	242	39	242	27	242	15	242	02	241	50	241	37	241	24	241	12
6	244	06	244	55	243	43	243	32	243	20	243	08	242	56	242	44	242	31	242	19
7	245	09	244	59	244	47	244	37	244	25	244	13	244	02	243	50	243	38	243	26
8	246	13	246	03	245	52	245	42	245	30	245	19	245	08	244	56	244	45	244	34
9	247	17	247	07	246	57	246	47	246	36	246	25	246	14	246	03	245	52	245	41
10	248	21	248	11	248	02	247	52	247	42	247	31	247	21	247	10	247	00	246	49
11	249	25	249	16	249	07	248	57	248	48	248	38	248	28	248	18	248	08	247	57
12	250	29	250	21	250	12	250	03	249	54	249	45	249	35	249	26	249	16	249	06
13	251	34	251	26	251	17	251	09	251	00	250	51	250	42	250	33	250	24	250	14
14	252	38	252	31	252	22	252	15	252	06	251	58	251	49	251	40	251	32	251	23
15	253	43	253	36	253	28	253	21	253	13	253	05	252	57	252	49	252	41	252	32
16	254	47	254	41	254	33	254	27	254	19	254	12	254	04	253	57	253	49	253	41
17	255	52	255	46	255	39	255	33	255	26	255	19	255	12	255	05	254	58	254	51
18	256	57	256	51	256	45	256	39	256	33	256	27	256	20	256	14	256	07	256	00
19	258	02	257	56	257	51	257	45	257	40	257	34	257	28	257	22	257	16	257	10
20	259	07	259	02	258	57	258	52	258	47	258	41	258	36	258	30	258	25	258	20
21	260	12	260	08	260	03	259	59	259	54	259	49	259	43	259	39	259	34	259	30
22	261	17	261	13	261	09	261	05	261	01	260	56	260	52	260	48	260	44	260	40
23	262	22	262	18	262	15	262	11	262	08	262	04	262	00	261	57	261	52	261	50
24	263	28	263	24	263	21	263	18	263	15	263	12	263	09	263	06	263	02	263	00
25	264	33	264	30	264	27	264	25	264	22	264	20	264	17	264	15	264	11	264	10
26	265	38	265	36	265	33	265	32	265	29	265	28	265	26	265	24	265	21	265	20
27	266	44	266	42	266	40	266	39	266	37	266	36	266	34	266	33	266	31	266	30
28	267	49	267	48	267	46	267	46	267	44	267	44	267	43	267	42	267	40	267	40
29	268	55	268	54	268	53	268	53	268	52	268	52	268	51	268	51	268	50	268	50
30	270	03	270	03	270	03	270	03	270	03	270	03	270	03	270	03	270	03	270	03



## Tables of Right Ascension.

North Latitude.

	0	1	2	3	4	5	6	7	8	9
$\varphi$	D. M.	D. M.	D. M.	D. M.	D. M.	D. M.	D. M.	D. M.	D. M.	D. M.
0	170 00	170 00	170 00	170 00	170 00	170 00	170 00	170 00	170 00	170 00
1	171 05	171 05	171 05	171 05	171 05	171 05	171 05	171 05	171 05	171 05
2	172 11	172 10	172 10	172 08	172 08	172 06	172 06	172 04	172 04	172 03
3	173 16	173 15	173 14	173 12	173 11	173 09	173 08	173 06	173 05	173 04
4	174 22	174 20	174 19	174 16	174 15	174 12	174 11	174 08	174 07	174 06
5	175 27	175 25	175 23	175 20	175 18	175 15	175 13	175 10	175 09	175 07
6	176 32	176 30	176 27	176 24	176 21	176 18	176 15	176 12	176 10	176 08
7	177 38	177 35	177 31	177 28	177 25	177 21	177 18	177 14	177 12	177 10
8	178 43	178 39	178 35	178 32	178 28	178 24	178 20	178 16	178 13	178 11
9	179 48	179 43	179 39	179 35	179 31	179 26	179 22	179 18	179 14	179 12
10	180 53	180 48	180 43	180 39	180 34	180 29	180 25	180 20	180 16	180 13
11	181 58	181 53	181 47	181 42	181 37	181 32	181 27	181 22	181 17	181 14
12	183 03	182 57	182 51	182 45	182 40	182 34	182 29	182 23	182 19	182 15
13	184 08	184 02	183 55	183 49	183 43	183 37	183 31	183 25	183 20	183 15
14	185 13	185 05	184 59	184 53	184 46	184 40	184 33	184 27	184 21	184 16
15	186 17	186 10	186 03	185 56	185 49	185 42	185 35	185 28	185 22	185 16
16	187 22	187 14	187 07	186 59	186 52	186 45	186 38	186 31	186 23	186 16
17	188 26	188 18	188 11	188 02	187 55	187 47	187 39	187 32	187 24	187 17
18	189 31	189 22	189 14	189 05	188 57	188 49	188 41	188 33	188 25	188 17
19	190 35	190 26	190 17	190 08	189 59	189 51	189 43	189 35	189 26	189 17
20	191 39	191 30	191 20	191 11	191 02	190 53	190 44	190 35	190 27	190 17
21	192 43	192 33	192 23	192 13	192 04	191 55	191 45	191 36	191 27	191 17
22	193 47	193 37	193 26	193 16	193 06	192 56	192 47	192 37	192 28	192 17
23	194 51	194 40	194 29	194 19	194 08	193 58	193 48	193 38	193 28	193 17
24	195 54	195 43	195 32	195 21	195 10	194 59	194 49	194 38	194 28	194 17
25	196 57	196 46	196 35	196 23	196 12	196 01	195 50	195 39	195 28	195 17
26	198 01	197 49	197 37	197 25	197 14	197 02	196 51	196 39	196 28	196 17
27	199 04	198 51	198 39	198 27	198 15	198 03	197 51	197 39	197 27	197 16
28	200 07	199 54	199 41	199 29	199 16	199 04	198 52	198 40	198 28	198 16
29	201 09	200 56	200 43	200 30	200 17	200 05	199 53	199 40	199 28	199 16
30	202 12	201 58	201 45	201 31	201 18	201 05	200 53	200 40	200 28	200 16

## Tables of Right Ascension.

South Latitude.

	0	1	2	3	4	5	6	7	8	9
$\varphi$	D. M.	D. M.	D. M.	D. M.	D. M.	D. M.	D. M.	D. M.	D. M.	D. M.
0	270 00	270 00	270 00	270 00	270 00	270 00	270 00	270 00	270 00	270 00
1	271 05	271 06	271 07	271 07	271 08	271 08	271 09	271 09	271 10	271 10
2	272 11	272 12	272 14	272 15	272 16	272 16	272 18	272 18	272 20	272 20
3	273 16	273 18	273 20	273 23	273 23	273 24	273 26	273 27	273 29	273 30
4	274 22	274 24	274 26	274 31	274 31	274 32	274 34	274 36	274 39	274 40
5	275 27	275 30	275 33	275 38	275 38	275 40	275 43	275 45	275 48	275 50
6	276 32	276 36	276 39	276 45	276 45	276 48	276 51	276 54	276 58	277 00
7	277 38	277 41	277 45	277 52	277 52	277 56	277 59	278 03	278 07	278 10
8	278 43	278 47	278 51	278 59	278 59	279 04	279 08	279 12	279 17	279 20
9	279 48	279 52	279 57	280 06	280 06	280 11	280 16	280 21	280 26	280 30
10	280 53	280 58	281 03	281 13	281 13	281 15	281 18	281 21	281 25	281 29
11	281 58	282 04	282 09	282 20	282 20	282 26	282 32	282 38	282 44	282 50
12	283 03	283 09	283 15	283 27	283 27	283 33	283 40	283 46	283 53	284 00
13	284 08	284 14	284 21	284 34	284 34	284 41	284 48	284 55	285 03	285 09
14	285 13	285 19	285 27	285 41	285 41	285 48	285 56	286 03	286 11	286 19
15	286 17	286 24	286 32	286 47	286 47	286 55	287 03	287 11	287 19	287 28
16	287 22	287 29	287 38	287 54	287 54	288 02	288 11	288 19	288 28	288 37
17	288 26	288 34	288 43	289 00	289 00	289 09	289 18	289 27	289 36	289 45
18	289 31	289 39	289 48	290 06	290 06	290 15	290 25	290 34	290 44	290 54
19	290 35	290 44	290 53	291 12	291 12	291 21	291 32	291 42	291 52	292 02
20	291 39	291 49	291 58	292 18	292 18	292 29	292 39	292 50	293 00	293 11
21	292 43	292 53	293 03	293 24	293 24	293 35	293 46	293 57	294 08	294 19
22	293 47	293 57	294 08	294 30	294 30	294 41	294 52	295 03	295 15	295 27
23	294 51	295 01	295 13	295 35	295 35	295 47	295 58	296 10	296 22	296 34
24	295 54	296 05	296 17	296 40	296 40	296 53	297 04	297 16	297 28	297 42
25	296 57	297 09	297 21	297 45	297 45	297 58	298 10	298 23	298 36	298 50
26	298 01	298 13	298 25	298 50	298 50	299 03	299 16	299 29	299 43	299 57
27	299 04	299 16	299 29	299 55	299 55	300 08	300 22	300 35	300 49	301 04
28	300 07	300 19	300 33	301 00	301 00	301 13	301 27	301 41	301 55	302 10
29	301 09	301 22	301 36	302 03	302 03	302 18	302 32	302 47	303 01	303 16
30	302 12	302 25	302 39	303 07	303 07	303 23	303 37	303 52	304 07	304 22



## Tables of Right Ascension.

North Latitude.

	0	1	2	3	4	5	6	7	8	9
<i>m</i>	<i>D. M.</i>	<i>D. M.</i>	<i>D. M.</i>	<i>D. M.</i>	<i>D. M.</i>	<i>D. M.</i>	<i>D. M.</i>	<i>D. M.</i>	<i>D. M.</i>	<i>D. M.</i>
0	302 12	01 58	301 45	301 31	301 18	301 05	300 53	300 40	300 28	300 16
1	303 14	303 02	302 47	302 33	302 19	302 06	301 53	301 40	301 28	301 15
2	304 16	304 02	303 48	303 34	303 20	303 06	302 53	302 40	302 27	302 14
3	305 18	305 03	304 50	304 35	304 21	304 07	303 53	303 39	303 26	303 13
4	306 20	306 05	305 51	305 36	305 22	305 07	304 53	304 39	304 25	304 12
5	307 22	307 07	306 52	306 36	306 22	306 07	305 52	305 38	305 24	305 10
6	308 24	308 08	307 53	307 37	307 22	307 07	306 52	306 37	306 23	306 09
7	309 25	309 09	308 54	308 37	308 22	308 07	307 51	307 36	307 22	307 07
8	310 26	310 10	309 54	309 37	309 22	309 06	308 50	308 35	308 20	308 05
9	311 27	311 10	310 54	310 37	310 21	310 05	309 49	309 33	309 18	309 03
10	312 28	312 11	311 54	311 37	311 21	311 04	310 48	310 31	310 17	310 01
11	313 28	313 11	312 54	312 37	312 20	312 03	311 47	311 31	311 15	310 59
12	314 29	314 11	313 54	313 37	313 19	313 02	312 46	312 29	312 13	311 57
13	315 29	315 11	314 54	314 36	314 18	314 01	313 45	313 27	313 11	312 54
14	316 29	316 11	315 53	315 35	315 17	315 00	314 43	314 25	314 09	313 52
15	317 29	317 10	316 52	316 34	316 16	315 58	315 41	315 23	315 06	314 50
16	318 29	318 10	317 51	317 33	317 15	316 57	316 39	316 21	316 04	315 47
17	319 28	319 09	318 50	318 32	318 14	317 55	317 37	317 19	317 02	316 44
18	320 27	320 08	319 49	319 30	319 12	318 53	318 35	318 17	317 59	317 41
19	321 27	321 07	320 48	320 29	320 10	319 51	319 33	319 15	318 56	318 38
20	322 26	322 06	321 47	321 27	321 08	320 49	320 31	320 12	319 53	319 35
21	323 25	323 04	322 45	322 25	322 06	321 47	321 28	321 09	320 50	320 31
22	324 23	324 03	323 43	323 23	323 04	322 45	322 25	322 06	321 47	321 28
23	325 22	325 01	324 41	324 21	324 01	323 42	323 22	323 03	322 44	322 24
24	326 20	325 59	325 39	325 19	324 59	324 39	324 19	323 59	323 40	323 21
25	327 18	326 57	326 37	326 17	325 56	325 36	325 16	324 56	324 37	324 17
26	328 16	327 55	327 35	327 14	326 54	326 33	326 13	325 53	325 33	325 13
27	329 14	328 53	328 32	328 11	327 50	327 30	327 10	326 49	326 29	326 09
28	330 11	329 50	329 29	329 08	328 47	328 27	328 06	327 46	327 25	327 05
29	331 09	330 47	330 26	330 05	329 44	329 23	329 02	328 42	328 21	328 01
30	332 06	331 44	331 23	331 02	330 41	330 20	329 59	329 38	329 17	328 56

## Tables of Right Ascension.

South Latitude.

	0	1	2	3	4	5	6	7	8	9
<i>m</i>	<i>D. M.</i>	<i>D. M.</i>	<i>D. M.</i>	<i>D. M.</i>	<i>D. M.</i>	<i>D. M.</i>	<i>D. M.</i>	<i>D. M.</i>	<i>D. M.</i>	<i>D. M.</i>
0	302 12	302 25	302 37	302 53	303 07	303 22	303 37	303 52	304 07	304 22
1	303 14	303 28	303 42	303 57	304 11	304 26	304 42	304 57	305 12	305 28
2	304 16	304 31	304 45	305 00	305 15	305 30	305 46	306 02	306 17	306 33
3	305 18	305 33	305 48	306 03	306 18	306 34	306 50	307 07	307 22	307 38
4	306 20	306 36	306 51	307 07	307 22	307 38	307 54	308 11	308 27	308 43
5	307 22	307 38	307 54	308 09	308 25	308 42	308 58	309 15	309 32	309 48
6	308 24	308 40	308 56	309 12	309 28	309 45	310 02	310 19	310 36	310 53
7	309 25	309 42	309 58	310 14	310 31	310 48	311 05	311 23	311 40	311 57
8	310 26	310 43	311 00	311 16	311 33	311 51	312 08	312 26	312 44	313 01
9	311 27	311 44	312 01	312 18	312 35	312 53	313 11	313 29	313 47	314 05
10	312 28	312 45	313 02	313 20	313 37	313 55	314 14	314 32	314 50	315 08
11	313 28	313 46	314 03	314 21	314 39	314 57	315 16	315 35	315 53	316 11
12	314 29	314 46	315 04	315 22	315 40	315 59	316 18	316 37	316 56	317 14
13	315 29	315 47	316 05	316 23	316 41	317 00	317 19	317 38	317 57	318 15
14	316 29	316 47	317 06	317 24	317 42	318 01	318 21	318 41	319 00	319 19
15	317 29	317 47	318 06	318 24	318 43	319 02	319 22	319 42	320 02	320 22
16	318 29	318 47	319 06	319 25	319 44	320 03	320 23	320 43	321 03	321 24
17	319 28	319 47	320 06	320 25	320 45	321 04	321 25	321 45	322 06	322 26
18	320 27	320 46	321 06	321 25	321 45	322 05	322 26	322 46	323 07	323 27
19	321 27	321 46	322 06	322 25	322 45	323 06	323 27	323 47	324 08	324 28
20	322 26	322 45	323 04	323 23	323 43	324 04	324 25	324 46	325 07	325 28
21	323 25	323 44	324 05	324 24	324 45	325 06	325 27	325 48	326 09	326 30
22	324 23	324 43	325 03	325 23	325 44	326 06	326 27	326 48	327 10	327 31
23	325 22	325 42	326 02	326 23	326 44	327 05	327 27	327 48	328 10	328 31
24	326 20	326 40	327 00	327 21	327 43	328 04	328 26	328 48	329 10	329 31
25	327 18	327 38	328 01	328 21	328 42	329 03	329 25	329 47	330 10	330 31
26	328 16	328 37	328 58	329 19	329 41	330 02	330 24	330 46	331 09	331 31
27	329 14	329 35	329 56	330 17	330 39	331 01	331 23	331 45	332 08	332 30
28	330 11	330 33	330 54	331 15	331 37	331 59	332 22	332 44	333 07	333 29
29	331 09	331 30	331 52	332 13	332 35	332 57	333 20	333 43	334 06	334 28
30	332 06	332 27	332 49	333 11	333 33	333 55	334 18	334 41	335 04	335 27



## Tables of Right Ascension.

North Latitude.

	0	1	2	3	4	5	6	7	8	9
°	D. M.	D. M.	D. M.	D. M.	D. M.	D. M.	D. M.	D. M.	D. M.	D. M.
0	332 06	331 44	331 23	331 02	330 41	330 20	329 59	329 38	329 17	328 56
1	333 04	332 41	332 20	331 59	331 38	331 16	330 55	330 34	330 13	329 52
2	334 01	333 38	333 17	332 55	332 34	332 12	331 51	331 30	331 09	330 47
3	334 58	334 35	334 13	333 51	333 30	333 08	332 47	332 25	332 04	331 42
4	335 55	335 32	335 10	334 48	334 26	334 04	333 43	333 21	333 00	332 37
5	336 51	336 28	336 07	335 44	335 22	335 00	334 39	334 17	333 55	333 32
6	337 48	337 25	337 03	336 40	336 18	335 56	335 34	335 12	334 50	334 27
7	338 44	338 22	337 59	337 36	337 14	336 52	336 30	336 08	335 46	335 22
8	339 40	339 18	338 55	338 32	338 10	337 48	337 26	337 03	336 41	336 17
9	340 37	340 14	339 51	339 28	339 06	338 43	338 21	337 58	337 36	337 12
10	341 33	341 10	340 47	340 24	340 02	339 39	339 17	338 54	338 31	338 07
11	342 29	342 06	341 43	341 20	340 58	340 35	340 12	339 49	339 26	339 02
12	343 25	343 02	342 39	342 16	341 53	341 30	341 07	340 44	340 21	339 57
13	344 20	343 58	343 35	343 12	342 49	342 25	342 02	341 39	341 16	340 52
14	345 16	344 53	344 30	344 07	343 44	343 20	342 57	342 34	342 11	341 48
15	346 12	345 49	345 25	345 02	344 39	344 15	343 52	343 29	343 06	342 43
16	347 07	346 44	346 21	345 57	345 34	345 10	344 47	344 24	344 01	343 38
17	348 03	347 40	347 17	346 52	346 29	346 05	345 42	345 18	344 55	344 33
18	348 58	348 35	348 12	347 47	347 24	347 00	346 37	346 13	345 51	345 28
19	349 54	349 31	349 07	348 43	348 19	347 55	347 32	347 08	346 46	346 23
20	350 49	350 26	350 02	349 38	349 14	348 50	348 27	348 03	347 41	347 19
21	351 44	351 21	350 57	350 33	350 09	349 45	349 22	348 58	348 36	348 14
22	352 39	352 16	351 52	351 28	351 04	350 40	350 17	349 53	349 30	349 09
23	353 35	353 11	352 47	352 23	351 59	351 35	351 12	350 48	350 25	350 04
24	354 30	354 06	353 42	353 18	352 54	352 30	352 07	351 43	351 20	350 59
25	355 25	355 01	354 37	354 13	353 49	353 25	353 02	352 38	352 15	351 53
26	356 20	355 56	355 32	355 08	354 44	354 20	353 57	353 33	353 10	352 49
27	357 15	356 51	356 27	356 03	355 39	355 15	354 52	354 28	354 04	353 42
28	358 10	357 46	357 22	356 58	356 34	356 10	355 47	355 23	355 00	354 36
29	359 05	358 41	358 17	357 53	357 29	357 05	356 42	356 18	355 55	355 30
30	360 00	359 36	359 12	358 48	358 24	358 00	357 37	357 13	356 50	356 24

## Tables of Right Ascension.

South Latitude.

	0	1	2	3	4	5	6	7	8	9
°	D. M.	D. M.	D. M.	D. M.	D. M.	D. M.	D. M.	D. M.	D. M.	D. M.
0	332 06	332 28	332 49	333 11	333 33	333 55	334 18	334 41	335 04	335 27
1	333 04	333 25	333 47	334 09	334 31	334 53	335 16	335 39	336 03	336 26
2	334 01	334 22	334 44	335 06	335 29	335 51	336 14	336 37	337 01	337 25
3	334 58	335 19	335 41	336 03	336 26	336 49	337 12	337 35	337 59	338 23
4	335 55	336 16	336 38	337 01	337 24	337 47	338 10	338 32	338 57	339 21
5	336 51	337 13	337 36	337 58	338 21	338 44	339 08	339 31	339 55	340 18
6	337 48	338 10	338 33	338 55	339 18	339 41	340 05	340 28	340 52	341 16
7	338 44	339 07	339 30	339 52	340 15	340 38	341 02	341 25	341 48	342 13
8	339 40	340 04	340 27	340 49	341 12	341 35	341 59	342 22	342 46	343 10
9	340 37	341 00	341 23	341 46	342 09	342 32	342 56	343 19	343 43	344 07
10	341 33	341 56	342 19	342 42	343 06	343 29	343 53	344 16	344 40	345 04
11	342 29	342 52	343 15	343 38	344 02	344 25	344 49	345 13	345 37	346 01
12	343 25	343 48	344 11	344 34	344 58	345 21	345 45	346 09	346 33	346 58
13	344 20	344 44	345 07	345 30	345 54	346 18	346 42	347 06	347 30	347 54
14	345 16	345 40	346 03	346 26	346 50	347 14	347 38	348 02	348 26	348 50
15	346 12	346 35	346 59	347 22	347 46	348 10	348 34	348 58	349 22	349 46
16	347 07	347 31	347 55	348 18	348 42	349 06	349 30	349 54	350 18	350 42
17	348 03	348 27	348 51	349 14	349 38	350 02	350 26	350 50	351 14	351 38
18	348 58	349 22	349 46	350 09	350 33	350 57	351 21	351 45	352 09	352 33
19	349 54	350 18	350 42	351 05	351 29	351 53	352 17	352 41	353 05	353 29
20	350 49	351 13	351 37	352 01	352 25	352 49	353 13	353 37	354 01	354 24
21	351 44	352 08	352 32	352 56	353 20	353 44	354 08	354 32	354 56	355 20
22	352 39	353 03	353 27	353 51	354 15	354 39	355 03	355 27	355 51	356 15
23	353 35	353 58	354 22	354 46	355 10	355 34	355 58	356 22	356 46	357 10
24	354 30	354 53	355 17	355 41	356 05	356 29	356 53	357 17	357 41	358 06
25	355 25	355 48	356 12	356 36	356 60	357 24	357 48	358 12	358 36	359 01
26	356 20	356 43	357 07	357 31	357 55	358 19	358 43	359 07	359 31	359 56
27	357 15	357 38	358 02	358 26	358 50	359 14	359 38	0 02	0 26	0 52
28	358 10	358 33	358 57	359 21	359 45	0 09	0 33	0 57	1 22	1 47
29	359 05	359 28	359 52	0 16	0 40	1 04	1 28	1 52	2 17	2 42
30	360 00	0 23	0 47	0 11	1 35	1 59	2 23	2 47	3 12	3 37



Tables of the Amplitudes, Ortive and Occasive.

[illegible]

### Tables of the Amplitudes, Ortive and Occasive.

[illegible]



Tables of the Amplitudes, Ortive and Occasive:

Degrees of the Declination.	Elevation of the Pole.																							
	20		21		22		23		24		25		26		27		28		29					
	D.	M.	D.	M.	D.	M.	D.	M.	D.	M.	D.	M.	D.	M.	D.	M.	D.	M.	D.	M.				
1	04	1	04	1	05	1	05	1	06	1	06	1	07	1	07	1	08	1	08	1	08			
2	07	2	07	2	08	2	09	2	10	2	11	2	12	2	12	2	13	2	13	2	14			
3	10	3	10	3	11	3	13	3	14	3	15	3	17	3	19	3	21	3	23	3	24			
4	17	4	17	4	19	4	21	4	23	4	25	4	27	4	29	4	31	4	34	4	36			
5	19	5	21	5	23	5	26	5	28	5	31	5	33	5	36	5	39	5	43	5	45			
6	24	6	24	6	26	6	29	6	32	6	35	6	38	6	41	6	45	6	48	6	52			
7	27	7	27	7	29	7	32	7	36	7	40	7	44	7	48	7	52	7	56	7	60			
8	31	8	31	8	34	8	38	8	42	8	46	8	50	8	55	9	59	9	65	9	70			
9	35	9	35	9	39	9	43	9	47	9	51	9	56	10	01	10	06	10	12	10	18			
10	38	10	38	10	43	10	48	10	53	10	58	11	03	11	09	11	15	11	21	11	27			
11	39	11	39	11	45	11	51	11	57	12	02	12	08	12	14	12	21	12	28	12	35			
12	42	12	42	12	50	12	57	13	03	13	09	13	16	13	23	13	30	13	37	13	44			
13	45	13	45	13	54	13	04	14	09	14	15	14	22	14	29	14	36	14	44	14	53			
14	48	14	48	14	58	15	05	15	15	15	22	15	29	15	37	15	46	15	55	15	66			
15	50	15	50	15	06	16	16	16	26	16	36	16	46	16	57	17	07	17	18	17	29			
16	57	16	57	16	17	17	27	17	37	17	47	17	57	18	08	18	18	18	29	18	40			
17	58	17	58	17	18	18	29	18	39	18	49	18	59	19	10	19	21	19	32	19	43			
18	19	18	20	19	31	19	42	19	53	20	04	20	15	20	26	20	37	20	48	20	59			
19	20	19	21	20	32	20	43	20	54	21	05	21	16	21	27	21	38	21	49	21	60			
20	21	20	22	21	33	21	44	21	55	22	06	22	17	22	28	22	39	22	50	22	61			
21	22	21	23	22	34	22	45	22	56	23	07	23	18	23	29	23	40	23	51	23	62			
22	23	22	24	23	35	23	46	23	57	24	08	24	19	24	30	24	41	24	52	24	63			
23	24	23	25	24	36	24	47	24	58	25	09	25	20	25	31	25	42	25	53	25	64			
24	25	24	26	25	37	25	48	25	59	26	10	26	21	26	32	26	43	26	54	26	65			
25	26	25	27	26	38	26	49	26	60															
26	27	26	28	27	39	27	50	27	61															
27	28	27	29	28	40	28	51	28	62															
28	29	28	30	29	41	29	52	29	63															
29	30	29	31	30	42	30	53	30	64															
30	31	30	32	31	43	31	54	31	65															
31	33	31	34	33	45	33	56	33	67															
32	34	32	35	34	46	34	57	34	68															
33	35	33	36	35	47	35	58	35	69															
34	37	34	38	36	49	36	60	36	71															
35	38	35	39	37	50	37	61	37	72															
36	39	36	40	38	51	38	62	38	73															
37	40	37	41	39	52	39	63	39	74															
38	41	38	42	40	53	40	64	40	75															
39	42	39	43	41	54	41	65	41	76															
40	43	40	44	42	55	42	66	42	77															

### Tables of the Amplitudes, Ortive and Occasive.

Degrees of Declination.	Elevation of the Pole.																			
	30		31		32		33		34		35		36		37		38		39	
	D.	M.	D.	M.	D.	M.	D.	M.	D.	M.	D.	M.	D.	M.	D.	M.	D.	M.	D.	M.
1	09	1	10	1	11	1	12	1	12	1	13	1	14	1	15	1	16	1	17	
2	17	2	17	2	21	2	23	2	25	2	26	2	28	2	29	2	32	2	34	
3	26	3	26	3	29	3	31	3	34	3	37	3	40	3	42	3	45	3	48	3
4	34	4	34	4	41	4	44	4	48	4	52	4	55	4	57	5	5	5	5	5
5	46	5	46	5	54	5	58	5	62	5	66	6	6	6	6	6	6	6	6	6
6	57	6	57	7	10	7	16	7	11	7	15	7	20	7	25	7	31	7	37	7
7	08	7	08	8	18	8	20	8	25	8	32	8	40	8	48	8	47	8	54	8
8	15	8	15	9	21	9	27	9	33	9	40	9	54	10	02	10	18	10	19	10
9	20	9	20	10	31	10	38	10	45	10	53	11	01	11	11	18	11	17	11	17
10	34	11	34	11	42	11	50	11	58	12	05	12	17	12	24	12	33	12	43	12
11	42	12	44	12	51	12	59	13	08	13	17	13	27	13	38	13	49	14	01	14
12	53	14	53	14	02	14	12	22	14	32	14	42	14	53	15	05	15	15	15	15
13	02	15	02	15	11	15	21	15	31	15	41	15	56	16	06	16	22	16	35	16
14	16	16	16	16	24	16	33	16	46	16	58	17	11	17	24	17	37	17	53	18
15	23	17	23	17	31	17	40	17	58	18	11	18	25	18	48	18	55	19	19	19
16	38	18	38	18	45	18	58	19	11	19	25	19	44	19	55	20	11	22	28	28
17	44	19	44	19	57	20	10	22	24	20	35	20	55	21	11	21	28	21	42	22
18	54	20	54	21	00	21	12	25	37	21	53	22	12	22	32	22	42	22	05	23
19	05	22	05	22	19	22	34	22	50	23	07	23	25	24	04	24	03	24	14	24
20	16	23	16	23	31	23	47	24	04	24	22	24	41	25	06	25	21	25	43	26
21	24	25	24	25	41	25	01	25	19	25	37	25	57	26	18	26	39	27	05	27
22	35	26	35	26	55	26	13	26	32	26	52	27	13	27	35	27	55	28	23	28
23	48	27	48	27	07	27	26	27	46	28	07	28	29	28	53	29	17	29	43	30
24	29	28	49	28	28	28	39	29	01	29	23	29	46	30	11	30	31	31	01	31
25	13	29	13	29	32	29	54	30	16	30	39	31	04	31	30	51	32	27	32	32
26	30	30	25	30	46	31	08	31	21	31	55	32	12	32	48	33	17			
27	31	31	37	31	58	32	23	32	47	33	13	33	31	33	08	34	17	34	57	35
28	32	32	33	33	13	33	37	34	04	34	36	34	55	35	28	36	06	36	33	37
29	34	05	34	27	34	52	35	19	35	47	36	16	36	49	37	3	37	38	38	38
30	35	16	35	41	36	05	36	37	05	37	38	18	38	48	39	26	39	26	40	40
31	36	36	36	36	57	37	24	37	53	38	24	38	57	39	34	40	6	40	55	41
32	37	43	37	41	38	46	39	12	39	44	40	19	40	55	41	12	18	41	33	42
33	38	58	39	29	39	59	40	30	41	05	41	42	29	42	29	43	5	43	5	43
34	40	13	40	17	41	16	41	49	42	26	43	05	43	45	44	34	5	44	1	44
35	41	29	42	05	42	34	43	09	43	28	44	25	45	16	46	47	0	47	0	47
36	42	44	43	23	43	52	44	39	45	09	45	51	46	36	47	33	48	34	49	2
37	43	55	44	41	45	15	45	16	46	34	47	18	48	09	49	35	50	48	51	3
38	45	15	45	59	46	29	47	14	47	59	48	49	36	50	33	51	42	52	30	4
39	46	30	47	17	47	58	48	37	49	24	50	15	51	6	52	43	54	54	41	5
40	47	53	48	35	49	17	50	12	50	51	41	52	37	53	36	54	55	55	55	5



Tables of the Amplitudes, Ortive and Occasive.

Degrees of the Declination.	Elevation of the Pole.															
	40		41		42		43		44		45		46		47	
	D.	M.	D.	M.	D.	M.	D.	M.	D.	M.	D.	M.	D.	M.	D.	M.
1	1	18	1	19	1	20	1	21	1	23	1	25	1	26	1	27
2	2	37	2	39	2	42	2	44	2	47	2	50	2	53	2	56
3	3	55	3	58	4	02	4	06	4	10	4	15	4	19	4	25
4	5	13	5	17	5	22	5	28	5	34	5	40	5	46	5	52
5	6	32	6	38	6	44	6	51	6	58	7	05	7	12	7	20
6	7	51	7	58	8	06	8	13	8	21	8	30	8	39	8	49
7	9	09	9	17	9	26	9	35	9	45	9	55	10	06	10	18
8	10	28	10	37	10	47	10	58	10	09	10	21	11	33	11	46
9	11	47	11	57	12	09	12	21	12	33	12	47	13	01	13	16
10	12	06	12	18	13	31	12	44	12	58	12	13	14	28	14	44
11	14	26	14	39	15	52	15	07	15	22	15	39	15	57	16	16
12	15	45	15	60	16	15	16	31	16	48	17	06	17	25	18	06
13	17	05	17	22	17	37	17	55	18	14	18	33	17	22	19	35
14	18	25	18	43	19	00	19	19	19	39	19	00	20	23	20	46
15	19	45	19	03	19	23	19	44	19	05	19	23	20	46	21	12
16	21	05	21	25	21	46	22	08	22	32	22	56	23	53	23	24
17	22	20	22	42	23	10	23	34	23	58	24	25	24	53	25	25
18	23	48	24	16	24	34	25	00	25	26	25	54	26	25	26	50
19	25	09	25	33	25	59	26	26	26	54	27	24	27	57	28	30
20	26	31	26	57	27	24	27	53	28	23	28	50	30	08	30	44
21	27	53	28	26	28	49	29	20	29	54	30	27	31	41	32	23
22	29	17	29	45	30	16	30	49	31	24	31	59	32	38	33	19
23	30	40	31	16	31	43	32	17	32	54	33	52	34	13	34	57
24	32	04	32	42	33	16	33	53	34	30	35	07	35	56	36	45
25	33	29	34	06	34	43	35	23	35	06	36	42	37	34	38	27
26	34	54	35	36	35	16	36	57	37	38	38	19	39	13	40	07
27	36	20	37	03	37	46	38	39	39	13	39	57	40	52	41	57
28	37	48	38	35	39	26	40	06	40	58	41	36	42	36	43	44
29	39	16	40	04	40	52	41	40	42	28	43	14	44	25	45	33
30	40	45	41	36	42	27	43	18	44	09	45	06	46	12	48	36
31	42	14	43	08	44	02	44	56	45	51	46	48	47	44	50	41
32	43	47	44	40	45	34	46	28	47	30	48	33	49	57	51	21
33	45	17	46	10	46	32	48	10	49	15	50	24	51	46	53	12
34	46	53	47	46	48	38	49	52	51	01	52	16	53	36	55	04
35	48	29	49	21	50	32	51	46	52	55	54	15	55	42	57	18
36	50	07	51	09	52	16	53	29	54	48	56	14	57	48	59	32
37	51	47	52	54	54	06	55	24	56	55	58	08	59	54		
38	53	29	54	40	55	56	57	26	58	52	60	33				
39	55	15	56	31	57	54	59	05	61	09						
40	57	03	58	23	59	52	61	31								

Tables of the Amplitudes, Ortive and Occasive.

Degrees of the Declination.	Elevation of the Pole.															
	50		51		52		53		54		55		56		57	
	D.	M.	D.	M.	D.	M.	D.	M.	D.	M.	D.	M.	D.	M.	D.	M.
1	1	33	1	35	1	37	1	39	1	42	1	45	1	47	1	50
2	3	07	3	11	3	15	3	19	3	24	3	29	3	35	3	41
3	4	40	4	46	4	52	4	59	5	06	5	14	5	22	5	31
4	6	14	6	22	6	30	6	39	6	49	6	59	7	10	7	22
5	7	48	7	58	8	09	8	20	8	31	8	44	8	57	9	12
6	9	21	9	33	9	46	10	00	10	14	10	30	10	46	11	03
7	10	56	11	10	11	25	11	41	11	58	12	16	12	35	12	56
8	12	31	12	47	13	04	13	22	13	41	14	03	14	24	14	48
9	14	05	14	24	14	44	15	04	15	26	15	50	16	15	16	42
10	15	40	16	01	16	23	16	46	17	11	17	37	18	06	18	36
11	17	19	17	39	18	03	18	29	18	56	19	29	19	56	20	29
12	18	52	19	17	19	41	20	11	20	42	21	15	21	50	22	27
13	17	20	17	37	17	55	18	14	18	33	18	54	19	16	19	38
14	22	06	22	30	23	06	23	42	24	18	24	57	25	38	26	22
15	23	45	24	17	24	52	25	28	26	07	26	45	27	35	28	22
16	25	24	25	58	26	35	27	15	27	58	28	43	29	33	30	24
17	27	03	27	40	28	21	29	04	29	50	30	39	31	32	32	28
18	28	42	29	24	30	08	30	54	31	43	32	38	33	33	34	34
19	30	20	31	05	31	55	32	44	33	38	34	35	35	36	36	42
20	32	55	33	45	34	38	35	35	36	37	36	39	37	43	38	54
21	33	53	34	42	35	36	36	32	37	34	38	40	39	51	41	11
22	35	39	36	12	37	26	38	30	39	20	40	47	42	05	43	27
23	37	26	38	33	39	23	40	29	41	40	42	56	43	45	45	50
24	39	15	40	20	41	37	42	49	44	00	45	16	47	01	48	52
25	41	06	42	22	43	38	44	55	46	10	47	28	49	30	51	32
26	42	52	44	13	45	34	46	56	48	18	49	41	51	59	54	18
27	44	57	46	26	47	54	49	23	50	51	52	20	54	55	60	05
28	46	55	48	37	50	07	51	43	53	19	54	56	57	55	64	53
29	48	58	50	42	52	27	54	12	55	57	57	42	61	20	64	53
30	51	04	52	59	54	54	56	49	58	44	60	39				
31	53	15	55	22	57	30	59	38	61	46	63	54				
32	55	33	57	56	60	19	62	43	65	07	67	31				
33	58	00														
34	60	27														



Tables of Difference of Ascension.

Degrees of the Declination.	Elevation of the Pole.																			
	1		2		3		4		5		6		7		8		9		10	
	D.	M.	D.	M.	D.	M.	D.	M.	D.	M.	D.	M.	D.	M.	D.	M.	D.	M.	D.	M.
1	0	1	0	2	0	3	0	4	0	5	0	6	0	7	0	8	0	9	0	11
2	0	2	0	4	0	6	0	8	0	10	0	13	0	15	0	17	0	19	0	21
3	0	3	0	6	0	9	0	13	0	16	0	19	0	22	0	25	0	29	0	32
4	0	4	0	8	0	13	0	17	0	21	0	25	0	30	0	34	0	38	0	42
5	0	5	0	10	0	16	0	21	0	26	0	32	0	37	0	42	0	48	0	53
6	0	6	0	13	0	19	0	25	0	32	0	38	0	44	0	51	0	57	1	04
7	0	7	0	15	0	22	0	30	0	37	0	44	0	52	0	59	1	07	1	14
8	0	8	0	17	0	25	0	34	0	42	0	51	0	59	1	08	1	16	1	25
9	0	9	0	19	0	29	0	38	0	48	0	57	1	07	1	16	1	26	1	36
10	0	11	0	21	0	32	0	42	0	53	1	04	1	14	1	25	1	36	1	47
11	0	12	0	23	0	35	0	47	0	58	1	10	1	22	1	34	1	46	1	58
12	0	13	0	25	0	38	0	51	1	04	1	17	1	30	1	43	1	56	2	09
13	0	14	0	28	0	42	0	56	1	05	1	23	1	37	1	52	2	06	2	20
14	0	15	0	30	0	45	1	00	1	15	1	30	1	45	2	01	2	16	2	31
15	0	16	0	32	0	48	1	04	1	21	1	37	1	53	2	10	2	26	2	42
16	0	17	0	34	0	52	1	09	1	26	1	44	2	01	2	19	2	36	2	54
17	0	18	0	37	0	55	1	14	1	32	1	50	2	09	2	28	2	47	3	05
18	0	19	0	39	0	59	1	18	1	38	1	57	2	15	2	37	2	57	3	17
19	0	21	0	41	0	02	1	23	1	44	2	04	2	25	2	46	3	08	3	29
20	0	22	0	44	0	06	1	27	1	49	2	12	2	34	2	56	3	18	3	41
21	0	23	0	45	1	09	1	32	1	55	2	19	2	41	3	06	3	29	3	53
22	0	24	0	46	1	13	1	37	2	02	2	26	2	50	3	15	3	40	4	05
23	0	25	0	51	1	17	1	42	2	08	2	33	2	59	3	25	3	51	4	18
24	0	27	0	53	1	20	1	47	2	14	2	31	3	00	3	35	4	03	4	30
25	0	28	0	56	1	24	1	52	2	20	2	49	3	17	3	45	4	14	4	43
26	0	29	0	59	1	28	1	57	2	27	2	56	3	26	3	56	4	26	4	56
27	0	31	0	01	1	32	2	03	2	33	3	04	3	35	4	06	4	38	5	09
28	0	32	0	04	1	36	2	08	2	40	3	12	3	45	4	17	4	50	5	23
29	0	33	0	07	1	40	2	13	2	47	3	20	3	54	4	28	5	02	5	37
30	0	35	0	09	1	44	2	19	2	54	3	29	4	04	4	39	5	15	5	51
31	0	35	1	12	1	48	2	24	3	01	3	37	4	14	4	51	5	28	6	05

Tables of Difference of Ascension.

Degrees of the Declination.	Elevation of the Pole.																			
	1		2		3		4		5		6		7		8		9		10	
	D.	M.	D.	M.	D.	M.	D.	M.	D.	M.	D.	M.	D.	M.	D.	M.	D.	M.	D.	M.
32	0	37	1	15	1	53	2	30	3	08	3	46	4	24	5	02	5	41	6	20
33	0	39	1	18	1	57	2	36	3	15	3	55	4	34	5	14	5	54	6	35
34	0	40	1	21	2	02	2	42	3	23	4	04	4	45	5	26	6	08	6	50
35	0	42	1	24	2	06	2	48	3	31	4	13	4	56	5	39	6	22	7	06
36	0	44	1	27	2	11	2	55	3	39	4	23	5	07	5	52	6	36	7	22
37	0	45	1	30	2	16	3	02	3	47	4	33	5	11	6	05	6	51	7	38
38	0	47	1	34	2	21	3	08	3	55	4	43	5	30	6	18	7	06	7	55
39	0	49	1	37	2	26	3	15	4	04	4	53	5	42	6	32	7	22	8	13
40	0	50	1	41	2	31	3	22	4	13	5	04	5	55	6	46	7	38	8	31
41	0	52	1	44	2	37	3	29	4	22	5	15	6	08	7	01	7	55	8	49
42	0	54	1	48	2	42	3	37	4	31	5	26	6	21	7	16	8	12	9	08
43	0	56	1	52	2	48	3	44	4	41	5	38	6	34	7	32	8	32	9	28
44	0	58	1	56	2	54	3	52	4	51	5	50	6	49	7	48	8	48	9	48
45	1	00	2	00	3	00	4	01	5	01	6	02	7	03	8	05	9	07	10	09
46	1	02	2	04	3	07	4	09	5	12	6	15	7	18	8	22	9	29	10	31
47	1	04	2	09	3	13	4	18	5	23	6	28	7	34	8	40	9	47	10	54
48	1	07	2	13	3	20	4	27	5	35	6	42	7	50	8	58	10	08	11	18
49	1	09	2	18	3	27	4	37	5	47	6	57	8	07	9	19	10	30	11	42
50	1	12	2	23	3	35	4	47	5	59	7	11	8	25	9	39	10	53	12	08
51	1	14	2	28	3	43	4	57	6	12	7	27	8	43	10	00	11	17	12	35
52	1	17	2	34	3	51	5	08	6	26	7	44	9	03	10	22	11	42	13	03
53	1	20	2	39	3	55	5	19	6	40	8	01	9	23	10	45	12	08	13	32
54	1	23	2	45	4	08	5	31	6	55	8	19	9	44	11	09	12	35	14	03
55	1	26	2	52	4	18	5	44	7	11	8	38	10	06	11	35	13	04	15	35
56	1	29	2	58	4	27	5	57	7	27	8	58	10	29	12	02	13	35	15	09
57	1	32	3	05	4	38	6	11	7	44	9	19	10	54	12	30	14	07	15	45
58	1	36	3	12	4	43	6	26	8	02	9	41	11	23	13	00	14	41	16	23
59	1	40	3	20	5	00	6	41	8	22	10	04	11	48	13	32	15	17	17	04
60	1	44	3	28	5	12	6	55	8	43	10	2	12	17	14	05	15	55	17	47
61	1	48	3	37	5	25	7	15	9	05	10	56	12	48	14	45	16	36	18	33
62	1	53	3	46	5	39	7	33	9	28	11	24	13	21	15	20	17	20	10	22



## Tables of Difference of Ascension.

Degrees of the Declination.	Elevation of the Pole.																			
	1		2		3		4		5		6		7		8		9		10	
	D.	M.	D.	M.	D.	M.	D.	M.	D.	M.	D.	M.	D.	M.	D.	M.	D.	M.	D.	M.
63	1	58	3	56	5	54	7	53	9	53	11	54	13	57	16	01	18	07	20	15
64	2	03	4	06	6	10	8	18	10	20	12	27	14	55	16	45	18	57	21	12
65	2	09	4	18	6	27	8	37	0	49	13	02	15	16	17	32	19	51	22	13
66	2	15	4	30	6	46	9	02	11	20	13	39	16	01	18	24	20	50	23	20
67	2	21	4	33	7	06	9	29	11	55	14	20	16	49	19	20	21	55	24	33
68	2	29	4	57	7	27	9	58	12	30	15	05	17	42	20	21	23	05	25	53
69	2	36	5	13	7	51	10	30	13	10	15	53	18	39	21	29	24	23	27	21
70	2	45	5	30	8	17	11	05	13	55	16	4	19	43	22	43	25	48	28	59
71	2	54	5	49	8	45	11	43	14	43	17	46	20	53	24	05	27	13	30	48
72	3	05	6	10	9	17	12	26	15	3	18	52	22	12	25	38	29	10	32	52
73	3	16	6	34	9	52	13	13	16	3	20	06	23	41	27	22	31	12	35	13
74	3	29	7	00	10	32	14	07	17	46	26	30	25	21	29	21	33	32	37	56
75	3	44	7	29	11	17	15	08	19	03	23	06	27	10	31	38	36	14	41	09
76	4	01	8	03	12	08	16	17	20	39	24	56	29	38	34	19	39	26	45	01
77	4	20	8	42	13	07	17	58	22	16	27	05	32	08	37	30	43	19	49	48
78	4	43	9	2	14	16	19	12	24	18	29	38	35	17	41	23	48	10	56	03
79	5	05	10	21	15	38	21	04	26	45	32	44	39	10	46	18	54	34	65	07
80	5	41	11	25	17	17	23	22	29	45	36	35	44	09	52	51	63	55	90	00
81	6	19	12	44	19	19	26	12	33	32	41	35	50	50	62	33	90	00		
82	7	08	14	23	21	54	29	50	38	30	48	24	60	33	90	00				
83	8	10	16	31	25	16	34	43	15	27	53	52	90	00						
84	9	34	19	24	29	55	41	42	56	21	90	00								
85	11	31	23	31	36	49	53	00	00											
86	14	27	30	58	48	23	90	00												
87	19	27	41	47	90	00														
88	36	51	90	00																
89	00	0	00																	

## Tables of Difference of Ascension.

Degrees of the Declination.	Elevation of the Pole.																			
	11		12		13		14		15		16		17		18		19		20	
	D.	M.	D.	M.	D.	M.	D.	M.	D.	M.	D.	M.	D.	M.	D.	M.	D.	M.	D.	M.
1	0	12	0	13	0	14	0	15	0	16	0	17	0	18	0	19	0	21	0	22
2	0	23	0	25	0	28	0	30	0	33	0	34	0	37	0	39	0	42	0	44
3	0	35	0	38	0	42	0	45	0	48	0	52	0	54	0	59	1	02	1	06
4	0	47	0	51	0	56	1	00	1	04	1	09	1	14	1	18	1	23	1	27
5	0	58	1	04	1	09	1	15	1	21	1	26	1	32	1	38	1	44	1	49
6	1	10	1	17	1	23	1	30	1	37	1	44	1	50	1	57	2	04	2	12
7	1	22	1	30	1	37	1	45	1	53	2	01	2	09	2	17	2	25	2	34
8	1	35	1	43	1	52	2	00	2	09	2	19	2	28	2	37	2	46	2	56
9	1	46	1	56	2	06	2	16	2	26	2	36	2	47	2	57	3	08	3	18
10	1	58	2	09	2	20	2	31	2	42	2	54	3	05	3	17	3	20	3	41
11	2	10	2	22	2	34	2	47	2	59	3	12	3	24	3	37	3	50	4	03
12	2	22	2	35	2	49	3	02	3	16	3	30	3	44	3	58	4	12	4	26
13	2	34	2	49	3	03	3	18	3	33	3	48	4	03	4	18	4	34	4	49
14	2	47	3	02	3	18	3	34	3	50	4	06	4	22	4	39	4	56	5	12
15	2	59	3	16	3	33	3	50	4	07	4	24	4	42	5	00	5	18	5	36
16	3	12	3	30	3	48	4	06	4	24	4	43	5	02	5	21	5	40	5	59
17	3	24	3	44	4	03	4	22	4	42	5	02	5	22	5	42	6	02	6	23
18	3	37	3	58	4	18	4	39	5	00	5	21	5	42	6	04	6	25	6	47
19	3	50	4	12	4	34	4	55	5	18	5	40	6	03	6	26	6	49	7	12
20	4	03	4	26	4	49	5	12	5	36	5	59	6	24	6	48	7	12	7	37
21	4	17	4	41	5	05	5	30	5	54	6	15	6	45	7	10	7	36	8	02
22	4	30	4	56	5	21	5	47	6	13	6	39	7	06	7	33	8	00	8	27
23	4	44	5	11	5	37	6	05	6	32	6	59	7	27	7	56	8	24	8	53
24	4	58	5	26	5	54	6	23	6	51	7	20	7	49	8	19	8	49	9	19
25	5	12	5	41	6	11	6	41	7	11	7	41	8	12	8	43	9	14	9	46
26	5	26	5	57	6	28	6	59	7	31	8	02	8	35	9	07	9	40	10	14
27	5	41	6	13	6	45	7	18	7	51	8	24	8	58	9	32	10	06	10	41
28	5	56	6	29	7	03	7	37	8	11	8	46	9	21	9	57	10	33	11	09
29	6	11	6	46	7	21	7	57	8	32	9	09	9	45	10	23	11	00	11	38
30	6	27	7	03	7	40	8	17	8	54	9	32	10	10	10	49	11	28	12	08
31	6	42	7	20	7	58	8	37	9	16	9	55	10	35	11	16	11	56	12	38



Tables of Difference of Ascension.

Degrees of the Declination.	Elevation of the Pole.																			
	11		12		13		14		15		16		17		18		19		20	
	D. M.	D. M.	D. M.	D. M.	D. M.	D. M.	D. M.	D. M.	D. M.	D. M.	D. M.	D. M.	D. M.	D. M.	D. M.	D. M.	D. M.	D. M.	D. M.	D. M.
32	6	59	7	38	8	18	8	58	9	35	10	19	11	01	11	43	12	23	13	09
33	7	15	7	56	8	37	9	19	10	01	10	44	11	27	12	11	12	53	13	40
34	7	32	8	15	8	57	9	41	10	25	11	09	11	54	12	40	13	26	14	13
35	7	49	8	34	9	18	10	03	10	43	11	35	12	22	13	09	13	57	14	46
36	8	07	8	53	9	39	10	26	11	13	12	01	12	50	13	39	14	29	15	20
37	8	25	9	13	10	01	10	50	11	38	12	29	13	10	14	10	15	02	15	55
38	8	44	9	34	10	23	11	14	12	05	12	57	13	49	14	42	15	36	16	31
39	9	03	9	55	10	46	11	39	12	32	13	26	14	20	15	15	16	11	17	08
40	9	23	10	16	11	10	12	05	13	00	13	55	14	51	15	49	16	48	17	47
41	9	44	10	39	11	35	12	31	13	28	14	26	15	25	16	24	17	25	18	27
42	10	05	11	02	12	00	12	53	13	58	14	58	15	59	17	01	18	04	19	08
43	10	27	11	26	13	26	13	27	14	28	15	31	16	34	17	38	18	44	19	50
44	10	49	11	51	12	53	13	56	15	00	16	05	17	10	18	17	19	25	20	35
45	11	13	12	16	13	21	14	28	15	33	16	40	17	48	18	58	20	08	21	21
46	11	37	12	45	13	50	14	58	16	07	17	10	18	27	19	40	20	53	22	09
47	12	02	13	11	14	20	15	30	16	42	17	54	19	08	20	23	21	40	22	58
48	12	28	13	39	14	51	16	08	17	19	34	19	51	21	06	22	29	33	51	
49	12	55	14	00	15	24	16	40	17	57	19	16	20	36	21	57	23	20	24	45
50	13	24	14	40	15	58	17	17	18	37	19	59	21	22	22	47	24	15	25	42
51	13	53	15	13	16	34	17	56	19	19	20	44	22	11	23	39	25	10	26	43
52	14	24	15	47	17	11	18	37	20	03	21	32	23	02	24	34	26	09	27	46
53	14	57	16	23	17	50	19	19	20	50	22	22	23	56	25	37	27	11	28	53
54	15	31	17	11	18	32	20	04	21	37	23	15	24	53	26	34	28	17	30	04
55	15	07	17	40	19	18	20	52	22	30	24	10	25	53	27	30	29	27	31	19
56	16	45	18	22	20	01	21	42	23	24	25	05	26	57	28	40	30	42	32	38
57	17	25	19	06	20	45	22	35	24	22	26	12	28	05	30	01	32	01	34	05
58	18	07	19	52	21	41	23	37	25	23	27	15	29	18	31	20	33	26	35	37
59	18	52	20	43	22	36	24	31	26	29	28	30	30	35	32	44	34	58	37	17
60	19	40	21	36	23	37	25	37	27	39	29	47	31	58	34	15	36	37	39	05
61	20	32	22	23	24	37	26	44	28	54	31	06	33	28	35	53	38	24	41	03
62	21	27	23	24	25	44	27	58	30	16	32	38	35	06	37	40	40	22	43	12

Tables of Difference of Ascension.

Degrees of the Declination.	Elevation of the Pole.																			
	11		12		13		14		15		16		17		18		19		20	
	D. M.	D. M.	D. M.	D. M.	D. M.	D. M.	D. M.	D. M.	D. M.	D. M.	D. M.	D. M.	D. M.	D. M.	D. M.	D. M.	D. M.	D. M.	D. M.	D. M.
63	22	26	24	39	26	57	29	18	31	44	34	15	36	52	39	37	42	34	45	35
64	23	29	25	50	28	15	30	41	33	15	36	01	38	49	41	46	44	54	48	16
65	24	38	27	07	29	41	32	10	35	04	37	56	40	58	44	10	47	36	51	19
66	25	53	28	31	31	14	34	03	37	00	40	06	43	22	46	52	50	39	54	50
67	27	15	30	03	32	57	35	58	39	08	42	30	46	04	49	56	54	13	59	02
68	28	45	31	45	34	51	38	06	41	33	45	13	49	10	53	52	58	07	64	16
69	30	25	33	37	36	58	40	30	44	16	48	20	52	48	57	50	63	47	71	28
70	32	13	35	44	39	22	43	14	47	24	51	59	57	08	63	13	71	05	90	00
71	34	22	38	07	42	06	46	23	51	06	56	23	62	37	70	40	90	00		
72	36	45	40	51	45	17	50	07	55	33	61	57	70	12	90	00				
73	39	29	44	03	49	02	54	38	61	13	69	42	90	00						
74	42	41	47	50	53	37	60	17	69	08	90	00								
75	46	30	52	30	59	30	68	31	90	00										
76	51	14	58	29	67	49	90	00												
77	57	21	67	02	90	00														
78	66	08	90	00																
79	90	00																		



## Tables of Difference of Ascension.

Degrees of the Declination.	Elevation of the Pole.									
	21	22	23	24	25	26	27	28	29	30
	D. M.	D. M.	D. M.	D. M.	D. M.	D. M.	D. M.	D. M.	D. M.	D. M.
1	0 23	0 24	0 25	0 27	0 28	0 29	0 31	0 32	0 33	0 35
2	0 46	0 49	0 51	0 53	0 56	0 59	1 01	1 04	1 07	1 09
3	1 09	1 13	1 17	1 20	1 24	1 28	1 32	1 36	1 40	1 44
4	1 32	1 37	1 42	1 47	1 52	1 57	2 03	2 08	2 13	2 19
5	1 55	2 02	2 08	2 14	2 20	2 27	2 33	2 40	2 47	2 54
6	2 19	2 26	2 33	2 41	2 49	2 56	3 04	3 12	3 20	3 29
7	2 42	2 51	2 59	3 08	3 17	3 26	3 35	3 45	3 54	4 04
8	3 06	3 15	3 25	3 35	3 45	3 56	4 06	4 17	4 28	4 39
9	3 29	3 40	3 51	4 03	4 14	4 26	4 38	4 50	5 02	5 15
10	3 53	4 05	4 18	4 30	4 43	4 56	5 09	5 23	5 38	5 51
11	4 17	4 30	4 44	4 58	5 12	5 26	5 41	5 56	6 11	6 27
12	4 41	4 56	5 11	5 26	5 41	5 57	6 13	6 29	6 46	7 03
13	5 05	5 21	5 36	5 54	6 11	6 28	6 45	7 03	7 21	7 40
14	5 30	5 47	6 05	6 22	6 41	6 59	7 18	7 37	7 56	8 17
15	5 54	6 13	6 32	6 51	7 11	7 31	7 51	8 11	8 32	8 54
16	6 19	6 39	6 59	7 20	7 41	8 03	8 24	8 46	9 08	9 32
17	6 44	7 05	7 27	7 49	8 12	8 35	8 58	9 21	9 45	10 10
18	7 10	7 33	7 56	8 19	8 43	9 07	9 32	9 56	10 23	10 49
19	7 36	8 00	8 24	8 49	9 14	9 40	10 06	10 33	11 00	11 28
20	8 02	8 27	8 53	9 19	9 46	10 14	10 41	11 09	11 38	12 08
21	8 28	8 55	9 23	9 50	10 19	10 47	11 17	11 46	12 17	12 48
22	8 55	9 24	9 53	10 22	10 52	11 22	11 53	12 24	12 56	13 29
23	9 22	9 53	10 25	10 57	11 29	12 01	12 35	13 08	13 41	14 11
24	9 50	10 23	10 54	11 26	11 59	12 33	13 07	13 42	14 17	14 54
25	10 19	10 52	11 25	11 59	12 34	13 09	13 45	14 21	14 59	15 37
26	10 47	11 22	11 57	12 33	13 09	13 46	14 24	15 02	15 41	16 21
27	11 17	11 53	12 29	13 07	13 45	14 23	15 03	15 43	16 24	17 06
28	11 47	12 24	13 03	13 42	14 21	15 01	15 43	16 25	17 08	17 53
29	12 17	12 57	13 37	14 18	14 59	15 41	16 24	17 08	17 54	18 40

## Tables of Difference of Ascension.

Degrees of the Declination.	Elevation of the Pole.									
	21	22	23	24	25	26	27	28	29	30
	D. M.	D. M.	D. M.	D. M.	D. M.	D. M.	D. M.	D. M.	D. M.	D. M.
30	12 48	13 29	14 11	14 54	15 37	16 21	17 06	17 53	18 40	19 28
31	13 20	14 03	14 47	15 31	16 16	17 02	17 50	18 38	19 27	20 18
32	13 53	14 37	15 23	16 09	16 56	17 45	18 34	19 24	20 16	21 09
33	14 26	15 13	16 00	16 48	17 37	18 27	19 20	20 12	21 06	22 01
34	15 00	15 49	16 38	17 29	18 20	19 12	20 06	21 01	21 57	22 55
35	15 36	16 26	17 17	18 09	19 03	19 58	20 54	21 51	22 50	23 51
36	16 12	17 04	17 58	18 53	19 49	20 45	21 44	22 44	23 45	24 48
37	16 49	17 44	18 39	19 36	20 34	21 34	22 35	23 37	24 41	25 47
38	17 27	18 24	19 22	20 21	21 21	22 23	23 24	24 28	25 35	26 44
39	18 06	19 06	20 06	21 08	22 12	23 16	24 22	25 30	26 40	27 52
40	18 47	19 49	20 52	21 56	23 02	24 09	25 19	26 30	27 43	28 59
41	19 30	20 34	21 39	22 46	23 55	25 05	26 17	27 32	28 48	30 07
42	20 13	21 20	22 28	23 38	24 50	26 06	27 18	28 36	29 56	31 19
43	20 59	22 08	23 19	24 32	25 46	26 63	27 83	28 53	30 17	31 44
44	21 45	22 58	24 12	25 28	26 46	28 06	29 28	30 54	32 22	33 55
45	22 34	23 50	25 08	26 27	27 48	29 11	30 38	32 07	33 40	35 16
46	23 26	24 44	26 05	27 27	28 52	30 20	31 53	33 34	35 20	36 44
47	24 18	25 41	27 07	28 33	30 03	31 38	33 23	35 07	36 58	38 33
48	24 14	26 40	28 08	29 38	31 11	32 47	34 36	36 36	38 33	40 15
49	26 12	27 42	29 14	30 49	32 26	34 08	35 53	37 53	39 41	41 37
50	27 13	28 47	30 23	32 03	33 33	35 06	37 02	39 19	41 11	43 29
51	28 17	29 53	31 33	33 21	35 00	36 37	38 53	41 04	43 11	45 29
52	29 26	31 08	32 54	34 41	36 38	38 40	41 22	43 42	45 53	48 09
53	30 37	32 25	34 16	36 13	38 40	40 42	43 44	46 11	48 53	51 07
54	31 51	33 42	35 45	37 48	39 49	42 15	45 17	48 02	50 52	53 31
55	33 14	35 14	37 19	39 39	41 45	44 06	46 41	49 52	52 58	56 05
56	34 41	36 48	39 11	41 43	44 46	47 19	49 52	52 58	56 05	59 52
57	36 14	38 40	41 43	44 43	47 43	50 51	54 14	57 58	61 62	65 45
58	37 54	40 40	44 45	47 45	50 51	54 14	57 58	61 62	65 45	69 31



## Tables of Difference of Ascension.

Degrees of the Declination.	Elevation of the Pole.											
	21		22		23		24		25		26	
	D.	M.	D.	M.	D.	M.	D.	M.	D.	M.	D.	M.
59	39	40	42	16	44	57	47	49	50	54	54	16
60	41	50	44	25	47	19	50	27	53	52	57	39
61	43	50	46	48	49	59	53	26	57	36	61	38
62	46	12	49	27	52	58	56	52	61	17	66	32
63	48	53	52	28	56	25	60	54	66	14	73	11
64	51	55	55	53	60	29	65	54	72	57	90	00
65	55	23	60	03	65	21	72	42	90	00		
66	59	34	65	09	72	26	90	00				
67	64	44	72	03	90	00						
68	71	49	90	00								
69	90	00										

## Tables of Difference of Ascension.

Degrees of the Declination.	Elevation of the Pole.																			
	31		32		33		34		35		36		37		38		39		40	
	D.	M.	D.	M.	D.	M.	D.	M.	D.	M.	D.	M.	D.	M.	D.	M.	D.	M.	D.	M.
1	0	36	0	37	0	39	0	40	0	42	0	44	0	45	0	47	0	49	0	50
2	1	12	1	15	1	18	1	21	1	24	1	27	1	31	2	34	1	37	1	41
3	1	48	1	53	1	57	2	02	2	06	2	11	2	16	2	21	2	26	2	31
4	2	24	2	30	2	36	2	42	2	48	2	55	3	01	3	08	3	15	3	22
5	3	01	3	08	3	15	3	23	3	31	3	39	3	47	3	55	4	04	4	13
6	3	37	3	46	3	55	4	03	4	13	4	23	4	33	4	43	4	53	5	04
7	4	14	4	24	4	34	4	45	4	56	5	07	5	19	5	30	5	42	5	55
8	4	51	5	02	5	14	5	26	5	37	5	52	6	05	6	18	6	32	6	46
9	5	28	5	41	5	54	6	08	6	22	6	37	6	51	7	06	7	22	7	38
10	6	05	6	20	6	35	6	50	7	09	7	22	7	38	7	55	8	13	8	30
11	6	42	6	59	7	15	7	32	7	49	8	07	8	25	8	44	9	03	9	23
12	7	20	7	38	7	56	8	15	8	34	8	53	9	13	9	34	9	55	10	16
13	7	58	8	18	8	37	8	58	9	18	9	39	10	01	10	24	10	48	11	10
14	8	37	8	58	9	19	9	41	10	03	10	26	10	50	11	14	11	39	12	04
15	9	16	9	38	10	01	10	25	10	49	11	14	11	39	12	05	12	32	13	02
16	9	55	10	15	10	44	11	09	11	35	12	02	12	29	12	57	13	26	13	55
17	10	35	11	01	11	27	11	54	12	22	12	50	13	19	13	49	14	20	14	52
18	11	16	11	43	12	11	12	40	13	09	13	37	14	10	14	42	15	15	15	49
19	11	56	12	26	12	55	13	26	13	57	14	29	15	02	15	36	16	11	6	48
20	12	38	13	09	13	40	14	13	14	46	15	20	15	55	16	31	17	08	17	47
21	13	20	13	53	14	26	15	00	15	36	16	12	16	49	17	27	18	07	18	47
22	14	03	14	37	15	13	15	49	16	27	17	05	17	44	18	24	19	06	19	49
23	14	47	15	23	16	00	16	38	17	17	17	58	18	39	19	22	20	06	20	52
24	15	31	16	09	16	48	17	29	18	10	18	52	19	36	20	21	21	08	21	56
25	16	16	16	56	17	38	18	20	19	03	19	48	20	34	21	21	22	11	23	01
26	17	02	17	45	18	28	19	12	19	58	20	45	21	34	22	24	23	16	24	10
27	17	50	18	34	19	19	20	06	20	54	21	44	22	35	23	28	24	22	25	15
28	18	38	19	24	20	12	21	01	21	51	22	41	23	37	24	33	25	30	26	30
29	19	27	20	16	21	06	21	57	22	50	23	41	24	41	25	40	26	40	27	43
30	20	18	21	09	22	01	22	55	23	51	24	46	25	46	26	47	27	52	28	59
31	21	10	22	03	22	58	23	55	24	53	25	55	26	55	28	00	29	07	30	17
32	22	03	22	59	23	56	24	56	25	57	27	00	28	05	29	13	30	24	31	37



Tables of Difference of Ascension.

Degrees of the Declination.	Elevation of the Pole.									
	31		32		33		34		35	
	D.	M.	D.	M.	D.	M.	D.	M.	D.	M.
33	22	58	23	56	24	57	25	55	27	03
34	23	55	24	56	25	59	27	04	28	11
35	24	53	25	57	27	05	28	11	29	22
36	25	53	27	00	28	09	29	21	30	35
37	26	55	28	05	29	18	30	32	31	50
38	28	03	29	13	30	29	31	48	33	10
39	29	01	30	23	31	44	33	06	34	33
40	30	17	31	37	33	01	34	25	35	59
41	31	25	32	54	34	22	35	53	37	31
42	32	45	34	15	35	47	37	23	39	05
43	34	05	35	35	37	16	38	59	40	46
44	35	28	37	07	38	50	40	39	42	33
45	36	56	38	40	40	32	42	25	44	30
46	38	27	40	19	42	16	44	18	45	29
47	40	07	42	04	44	08	46	20	48	40
48	41	52	43	57	46	09	48	31	51	03
49	43	44	45	57	48	20	50	53	53	40
50	45	43	48	05	50	43	53	36	56	34
51	47	54	50	30	53	19	56	24	59	51
52	50	16	53	07	56	13	59	42	63	25
53	52	53	56	01	59	31	63	19	74	37
54	55	48	59	18	63	21	65	11	74	30
55	59	06	63	11	68	02	74	26	90	32
56	62	59	66	53	74	19	80	00		
57	67	42	74	11	90	00				
58	74	04	90	00						
59	90	00								

Tables of Difference of Ascension.

Degrees of the Declination.	Elevation of the Pole.									
	41		42		43		44		45	
	D.	M.	D.	M.	D.	M.	D.	M.	D.	M.
1	0	52	0	54	0	56	0	58	1	0
2	1	44	1	48	1	52	1	56	2	0
3	2	37	2	42	2	48	2	54	3	0
4	3	2	3	37	3	44	3	52	4	1
5	4	22	4	31	4	41	4	51	5	1
6	5	15	5	26	5	37	5	5	6	2
7	6	08	6	21	6	34	6	49	7	5
8	7	01	7	16	7	32	7	48	8	8
9	7	55	8	12	8	31	8	48	9	9
10	8	49	9	08	9	28	9	48	10	10
11	9	44	10	05	10	27	10	4	11	12
12	10	39	11	02	11	26	11	51	12	16
13	11	35	12	00	12	26	12	53	13	21
14	12	31	12	58	13	27	13	56	14	26
15	13	28	13	58	14	28	15	00	15	32
16	14	26	14	58	15	31	16	05	16	41
17	15	25	15	59	16	34	17	10	17	48
18	16	24	17	01	17	38	18	17	18	59
19	17	25	18	04	18	41	19	25	20	09
20	18	27	19	08	19	51	20	32	21	22
21	19	30	20	13	20	59	21	46	22	34
22	20	34	21	20	22	08	22	58	23	44
23	21	39	22	28	23	19	24	12	25	07
24	22	46	23	38	24	32	25	28	26	27
25	23	55	24	50	25	47	26	40	27	40
26	25	05	26	03	27	03	28	06	29	11
27	26	17	27	18	28	22	29	38	31	20
28	27	31	28	36	29	44	30	54	32	07
29	28	48	29	50	31	05	32	22	33	40
30	30	07	31	09	32	35	33	16	36	43
31	31	29	32	45	34	05	35	28	36	56



Tables of Difference of Ascension.

Degrees of the Declination.	Elevation of the Pole.															
	41		42		43		44		45		46		47		48	
	D.	M.	D.	M.	D.	M.	D.	M.	D.	M.	D.	M.	D.	M.	D.	M.
32	32	54	34	14	35	38	37	38	40	40	19	42	04	43	57	48
33	34	22	35	47	37	16	38	50	40	30	42	16	44	08	46	20
34	35	53	37	23	38	59	40	39	44	25	44	18	46	20	48	31
35	37	30	39	05	40	46	42	33	44	26	46	29	48	40	51	03
36	39	10	40	52	42	39	44	33	45	30	48	48	51	11	53	48
37	40	55	42	44	44	39	46	42	48	54	51	17	53	58	56	49
38	42	47	44	42	46	46	48	59	51	22	54	00	56	48	60	11
39	44	45	46	49	49	02	51	27	54	03	56	57	60	16	64	04
40	46	50	49	04	51	25	54	08	57	04	60	20	64	08	68	44
41	49	05	51	31	54	09	57	05	60	23	64	10	68	47	74	54
42	51	3	54	10	57	06	60	24	64	13	68	49	74	55	90	00
43	54	09	57	06	60	24	64	14	68	49	74	56	90	00		
44	57	0	50	24	64	14	68	50	74	57	90	00				
45	60	23	64	13	68	49	74	5	90	00						
46	64	10	68	39	74	56	90	00								
47	68	47	74	55	90	00										
48	74	54	90	00												
49	90	00														

Tables of Difference of Ascension.

Degrees of the Declination.	Elevation of the Pole.															
	51		52		53		54		55		56		57		58	
	D.	M.	D.	M.	D.	M.	D.	M.	D.	M.	D.	M.	D.	M.	D.	M.
1	1	14	1	17	1	20	1	23	1	26	1	29	1	32	1	36
2	2	28	2	34	2	39	2	43	2	58	2	58	3	03	3	12
3	3	43	3	51	3	59	4	08	4	18	4	27	4	38	4	40
4	4	57	5	08	5	19	5	31	5	44	5	57	6	11	6	25
5	6	12	6	26	6	40	6	55	7	11	7	27	7	44	8	03
6	7	27	7	44	8	01	8	19	8	38	8	58	9	19	9	41
7	8	43	9	02	9	23	9	44	10	06	10	24	10	54	11	20
8	10	00	10	22	10	45	11	09	11	35	12	01	12	30	13	00
9	11	17	11	42	12	08	12	35	13	04	13	35	14	07	14	41
10	12	35	13	03	13	32	14	03	14	35	15	09	15	48	16	23
11	13	53	14	24	14	57	15	31	16	0	16	48	17	28	18	08
12	15	15	15	4	16	23	17	00	17	40	18	22	19	03	19	53
13	16	31	17	11	17	50	18	32	18	15	19	00	20	56	21	41
14	17	46	18	37	19	16	20	04	20	52	21	42	22	35	23	31
15	19	10	20	04	20	50	21	38	22	50	23	24	24	25	25	26
16	20	44	21	32	22	23	22	15	24	10	25	09	26	12	27	19
17	22	11	23	02	23	56	24	53	25	53	26	5	28	03	29	18
18	23	30	24	34	25	38	26	34	27	39	28	48	30	01	31	20
19	25	12	26	09	27	18	28	17	29	27	30	41	32	01	33	26
20	26	47	27	46	28	5	30	04	31	10	32	38	34	05	35	37
21	28	1	29	20	30	57	31	54	33	15	34	41	36	14	37	54
22	29	56	31	08	32	33	47	35	14	36	48	38	28	0	39	42
23	31	43	32	54	34	17	45	44	37	19	39	0	40	9	41	57
24	33	32	34	44	36	18	37	4	39	29	41	18	43	17	43	26
25	35	21	36	39	38	12	39	59	41	45	43	48	45	54	45	16
26	37	10	38	38	40	20	42	10	44	0	46	18	48	41	51	10
27	39	0	40	42	42	33	44	32	46	41	49	04	51	41	54	3
28	41	02	42	53	44	53	47	02	49	24	52	01	54	58	59	10
29	43	15	45	12	47	21	50	41	52	20	55	10	58	36	63	31



Tables of Difference of Ascension.

Degree of the Declination.	Elevation of the Pole.									
	51		52		53		54		55	
	D.	M.	D.	M.	D.	M.	D.	M.	D.	M.
30	45	29	47	35	50	01	52	37	55	32
31	47	54	50	16	52	53	55	48	59	06
32	50	30	53	07	56	01	59	16	63	10
33	52	19	56	13	59	31	63	21	68	02
34	56	24	59	42	63	31	68	11	74	26
35	59	51	63	40	68	19	74	22	80	00
36	63	48	68	28	74	37	80	00		
37	68	31	70	42	80	00				
38	74	45	80	00						
39	80	00								

A Traverse-Table for every Point, Half-Point, and Quarter-Point of the Compass, to the 100 part of a League or Mile, which gives the Difference of Latitude and Departure from the Meridian.

Diff. in Long. or Miles full.	52 deg. 49 min.				55 deg. 37 min.				58 deg. 26 min.				61 deg. 15 min.				Diff. in Long. or Miles full.
	o Point $\frac{1}{4}$				co Point $\frac{1}{4}$				o Point $\frac{1}{4}$				1 Point.				
	N	S	E	W	N	S	E	W	N	S	E	W	N	S	E	W	
1	01	00	00	05	01	00	00	10	00	00	00	14	00	00	00	20	1
2	02	00	00	10	01	00	00	20	01	00	00	29	01	00	00	39	2
3	03	00	00	15	02	00	00	29	02	00	00	44	02	00	00	58	3
4	04	00	00	20	03	00	00	39	03	00	00	55	03	00	00	78	4
5	04	00	00	25	04	00	00	49	04	00	00	73	04	00	00	98	5
6	05	00	00	29	05	00	00	59	05	00	00	88	05	00	00	117	6
7	06	00	00	34	06	00	00	60	06	00	00	02	06	00	00	137	7
8	07	00	00	39	07	00	00	78	07	00	00	17	07	00	00	156	8
9	08	00	00	44	08	00	00	85	08	00	00	32	08	00	00	176	9
10	09	00	00	49	09	00	00	98	09	00	00	46	09	00	00	195	10
11	10	00	00	54	10	00	00	08	10	00	00	61	10	00	00	215	11
12	11	00	00	59	11	00	00	18	11	00	00	76	11	00	00	234	12
13	12	00	00	65	12	00	00	27	12	00	00	91	12	00	00	254	13
14	13	00	00	68	13	00	00	37	13	00	00	05	13	00	00	273	14
15	14	00	00	73	14	00	00	47	14	00	00	20	14	00	00	292	15
16	15	00	00	78	15	00	00	57	15	00	00	34	15	00	00	312	16
17	16	00	00	83	16	00	00	07	16	00	00	49	16	00	00	332	17
18	17	00	00	88	17	00	00	17	17	00	00	64	17	00	00	351	18
19	18	00	00	93	18	00	00	26	18	00	00	79	18	00	00	371	19
20	19	00	00	98	19	00	00	36	19	00	00	93	19	00	00	390	20
21	20	00	00	03	20	00	00	46	20	00	00	08	20	00	00	410	21
22	21	00	00	08	21	00	00	56	21	00	00	22	21	00	00	429	22
23	22	00	00	13	22	00	00	65	22	00	00	37	22	00	00	449	23
24	23	00	00	17	23	00	00	75	23	00	00	52	23	00	00	468	24
25	24	00	00	22	24	00	00	85	24	00	00	66	24	00	00	488	25
26	25	00	00	27	25	00	00	95	25	00	00	81	25	00	00	507	26
27	26	00	00	32	26	00	00	05	26	00	00	96	26	00	00	527	27
28	27	00	00	37	27	00	00	15	27	00	00	11	27	00	00	546	28
29	28	00	00	42	28	00	00	25	28	00	00	25	28	00	00	566	29
30	29	00	00	47	29	00	00	34	29	00	00	34	29	00	00	585	30
31	30	00	00	53	30	00	00	44	30	00	00	44	30	00	00	605	31
32	31	00	00	57	31	00	00	54	31	00	00	54	31	00	00	624	32
E				W	E			W	E			W	E			W	
7 Points $\frac{1}{2}$					7 Points $\frac{1}{2}$				7 Points $\frac{1}{2}$				7 Points.				
52 deg. 11 min.					84 deg. 22 min.				81 deg. 24 min.				78 deg. 45 min.				



A *Traverse-Table* for every *Point*, *Half-Point*, and *Quarter-Point* of the *Compass*, to the 100 part of a *League* or *Mile*, which gives the *Difference of Latitude* and *Departure* from the *Meridian*.

Diff. in Long. or Miles full 100	12 deg. 49 min.				15 deg. 37 min.				18 deg. 20 min.				11 deg. 15 min.				Diff. in Long. or Miles full 100
	1 Point $\frac{1}{4}$				1 Point $\frac{1}{2}$				1 Point $\frac{3}{4}$				1 Point				
	N	S	E	W	N	S	E	W	N	S	E	W	N	S	E	W	
33	32	96	01	61	32	84	03	23	32	64	04	84	32	57	06	44	33
34	33	95	01	66	33	84	03	33	33	63	04	98	33	55	06	03	34
35	34	95	01	71	34	83	03	43	34	62	05	13	34	53	06	08	35
36	35	95	01	75	35	83	03	53	35	61	05	23	35	51	07	02	36
37	36	95	01	81	36	82	03	63	36	60	05	33	36	29	07	22	37
38	37	95	01	86	37	82	03	73	37	59	05	53	37	27	07	41	38
39	38	95	01	91	38	81	03	82	38	58	05	53	38	25	07	61	39
40	39	95	01	96	39	81	03	92	39	57	05	63	39	23	07	81	40
41	40	95	02	01	40	80	04	02	40	55	06	02	40	21	08	00	41
42	41	95	02	06	41	80	04	12	41	54	06	12	41	19	08	10	42
43	42	95	02	11	42	79	04	21	42	53	06	31	42	17	08	39	43
44	43	94	02	15	43	79	04	31	43	52	06	41	43	15	08	58	44
45	44	94	02	20	44	78	04	41	44	51	06	51	44	14	08	79	45
46	45	94	02	25	45	78	04	51	45	50	06	61	45	12	08	77	46
47	46	94	02	30	46	77	04	61	46	49	06	80	47	10	09	36	47
48	47	94	02	35	47	77	04	70	47	48	07	00	47	08	09	56	48
49	48	94	02	40	48	76	04	80	48	47	07	10	48	06	09	56	49
50	49	94	02	45	49	76	04	90	49	46	07	20	49	04	09	75	50
51	50	93	02	50	50	75	05	00	50	45	07	45	50	02	09	95	51
52	51	93	02	55	51	75	05	10	51	45	07	55	51	00	10	14	52
53	52	93	02	60	52	74	05	20	52	44	07	70	52	08	10	34	53
54	53	93	02	65	53	74	05	29	53	44	07	80	53	06	10	53	54
55	54	93	02	70	54	73	05	39	54	43	08	00	53	04	10	73	55
56	55	93	02	75	55	73	05	49	55	42	08	10	54	02	10	92	56
57	56	93	02	80	56	72	05	59	56	40	08	20	55	00	11	12	57
58	57	93	02	84	57	72	05	68	57	39	08	51	56	00	11	31	58
59	58	92	02	89	58	71	05	78	58	38	08	65	57	00	11	51	59
60	59	92	02	94	59	71	05	88	59	35	08	80	58	00	11	70	60
70	69	91	03	45	69	66	06	86	69	24	10	27	68	05	13	65	70
80	79	90	03	92	79	61	07	80	79	13	11	73	78	06	15	60	80
90	89	89	04	40	89	56	08	80	89	02	13	20	88	07	17	55	90
100	99	88	04	00	99	51	09	80	99	01	14	67	98	08	19	50	100
200	199	76	09	80	199	02	19	92	199	02	29	34	196	10	39	00	200
	E	W	N	S	E	W	N	S	E	W	N	S	E	W	N	S	
	7 Points $\frac{1}{4}$				7 Points $\frac{1}{2}$				7 Points $\frac{3}{4}$				7 Points				
	87 deg. 11 min.				84 deg. 22 min.				81 deg. 34 min.				78 deg. 45 min.				

A *Traverse-Table* for every *Point*, *Half-Point*, and *Quarter-Point* of the *Compass*, to the 100 part of a *League* or *Mile*, which gives the *Difference of Latitude* and *Departure* from the *Meridian*.

Diff. in Long. or Miles full 100	14 deg. 04 min.				16 deg. 52 min.				19 deg. 41 min.				22 deg. 30 min.				Diff. in Long. or Miles full 100
	1 Point $\frac{1}{4}$				1 Point $\frac{1}{2}$				1 Point $\frac{3}{4}$				2 Points.				
	N	S	E	W	N	S	E	W	N	S	E	W	N	S	E	W	
1	00	99	00	24	00	99	00	26	00	94	00	35	00	92	00	38	1
2	01	94	00	40	01	94	00	55	01	88	00	07	01	85	00	76	2
3	02	91	00	72	02	87	00	07	02	83	01	01	02	77	01	75	3
4	03	88	00	97	03	83	01	10	03	77	01	34	03	70	01	53	4
5	04	85	01	21	04	79	01	45	04	71	01	68	04	62	01	91	5
6	05	82	01	45	05	74	01	74	05	65	02	02	05	54	02	30	6
7	06	79	01	70	06	70	02	03	06	59	02	35	06	47	02	68	7
8	07	76	01	94	07	66	02	32	07	53	02	72	07	39	03	16	8
9	08	73	02	18	08	61	02	61	08	47	03	62	08	31	03	44	9
10	09	70	02	43	09	57	02	92	09	41	03	37	09	24	03	83	10
11	10	67	02	67	10	53	03	19	10	36	03	74	10	16	04	21	11
12	11	64	02	91	11	48	03	48	11	31	04	04	11	09	04	59	12
13	12	61	03	15	12	44	03	77	12	24	04	30	12	01	04	97	13
14	13	58	03	40	13	41	04	06	13	18	04	72	12	03	05	36	14
15	14	55	03	64	14	35	04	35	14	12	05	05	13	05	05	74	15
16	15	52	03	88	15	31	04	64	15	06	05	39	14	05	06	12	16
17	16	49	04	13	16	27	04	93	16	00	05	70	15	00	06	51	17
18	17	46	04	37	17	22	05	21	17	00	06	00	16	00	06	30	18
19	18	43	04	61	18	18	05	51	18	00	06	40	17	00	07	27	19
20	19	40	04	86	19	14	05	81	19	00	06	74	18	00	07	05	20
21	20	37	05	10	20	10	06	10	20	00	07	08	19	01	08	03	21
22	21	34	05	34	21	05	06	39	21	00	07	41	20	01	08	44	22
23	22	31	05	58	22	00	06	68	22	00	07	75	21	01	09	25	23
24	23	28	05	53	23	00	06	97	23	00	07	09	22	01	09	56	24
25	24	25	06	07	24	00	07	26	23	00	08	40	23	01	09	55	25
26	25	22	06	31	24	00	07	55	24	00	08	71	24	02	09	95	26
27	26	19	06	56	25	00	07	84	25	00	08	02	25	02	10	33	27
28	27	16	06	80	26	00	08	13	26	00	08	45	25	03	10	71	28
29	28	13	07	04	27	01	08	42	27	01	08	36	26	03	11	10	29
30	29	10	07	28	28	01	08	71	28	01	09	11	27	04	11	48	30
31	30	07	07	53	29	00	09	00	29	00	09	41	28	04	11	86	31
32	31	04	07	77	30	00	09	29	30	00	09	70	29	05	12	25	32
	E	W	N	S	E	W	N	S	E	W	N	S	E	W	N	S	
	6 Points $\frac{1}{4}$				6 Points $\frac{1}{2}$				6 Points $\frac{3}{4}$				6 Points.				
	75 deg. 56 min.				73 deg. 07 min.				70 deg. 19 min.				67 deg. 30 min.				



A Traverse-Table for every Point, Half-Point, and Quarter-Point of the Compass, to the 100 part of a League or Mile, which gives the Difference of Latitude and Departure from the Meridian.

Diff. in Long. or Miles full	14 deg. 04 min.	16 deg. 52 min.	19 deg. 41 min.	22 deg. 30 min.	Diff. in Long. or Miles full
	1 Point $\frac{1}{4}$	1 Point $\frac{1}{2}$	1 Point $\frac{3}{4}$	2 Points.	
	N S E W	N S E W	N S E W	N S E W	
33	32 01 08 01	31 58 09 58	31 07 11 12	30 49 12 63	33
34	32 08 38 26	32 54 02 87	32 01 11 45	31 44 13 01	34
35	33 05 38 50	33 49 10 16	32 05 11 79	32 34 13 39	35
36	33 02 38 74	34 45 10 45	33 09 12 13	33 26 13 78	36
37	33 58 08 99	35 41 10 74	34 04 12 47	34 18 14 16	37
38	34 26 09 23	36 36 11 03	35 08 12 84	35 11 14 54	38
39	35 03 09 47	37 32 11 32	36 02 13 14	36 03 14 92	39
40	35 38 09 71	38 28 11 61	37 06 13 48	36 59 15 31	40
41	36 03 09 96	39 23 11 90	38 00 13 81	37 48 16 09	41
42	40 74 10 21	40 19 12 19	39 34 14 15	38 40 16 07	42
43	41 71 10 44	41 15 12 48	40 49 14 49	39 73 16 45	43
44	42 68 10 69	42 12 12 77	41 43 14 72	40 05 16 84	44
45	43 65 10 63	43 06 13 06	42 37 15 16	41 57 17 22	45
46	44 62 11 17	44 02 13 35	43 41 15 50	42 50 17 60	46
47	45 59 11 42	44 08 13 64	44 25 15 83	43 42 17 99	47
48	46 56 11 66	45 03 13 93	45 19 16 17	44 35 18 37	48
49	47 53 11 92	46 09 14 22	46 13 16 37	45 27 18 75	49
50	48 50 12 14	47 05 14 51	47 08 16 85	46 19 19 13	50
51	49 47 12 39	48 00 14 80	48 01 17 18	47 12 19 52	51
52	50 44 12 63	49 00 15 09	49 06 17 31	48 04 19 89	52
53	51 41 12 87	50 02 15 38	49 00 17 05	49 07 20 28	53
54	52 38 13 12	51 03 15 67	50 04 18 19	49 09 20 66	54
55	53 35 13 36	52 04 15 96	51 06 18 53	50 01 21 04	55
56	54 32 13 60	53 05 16 26	52 07 19 18	51 03 21 15	56
57	55 29 13 85	54 06 16 55	53 07 19 24	52 06 21 43	57
58	56 26 14 09	55 07 17 08	54 01 19 51	53 08 22 81	58
59	57 23 14 33	56 08 17 23	55 05 19 80	54 21 22 20	59
60	58 20 14 57	57 09 17 47	56 09 20 21	55 43 22 58	60
61	59 17 15 21	58 10 18 01	57 13 20 58	56 47 26 78	61
62	60 14 15 45	59 11 18 25	58 17 21 31	57 51 30 61	62
63	61 11 16 09	60 12 18 49	59 21 22 04	58 55 34 44	63
64	62 08 16 33	61 13 19 13	60 25 22 37	59 59 38 27	64
65	63 05 16 57	62 14 19 37	61 29 23 10	60 63 42 10	65
66	64 02 17 21	63 15 19 61	62 33 23 43	61 67 45 53	66
67	65 00 17 45	64 16 20 05	63 37 24 16	62 71 49 36	67
68	66 00 18 09	65 17 20 29	64 41 24 49	63 75 53 19	68
69	67 00 18 33	66 18 20 53	65 45 25 22	64 79 57 02	69
70	68 00 18 57	67 19 21 17	66 49 25 55	65 83 60 45	70
71	69 00 19 21	68 20 21 41	67 53 26 28	66 87 64 28	71
72	70 00 19 45	69 21 22 05	68 57 27 01	67 91 68 11	72
73	71 00 20 09	70 22 22 29	69 61 27 34	68 95 71 54	73
74	72 00 20 33	71 23 22 53	70 65 28 07	69 99 75 37	74
75	73 00 20 57	72 24 23 17	71 69 28 40	70 103 79 20	75
76	74 00 21 21	73 25 23 41	72 73 29 03	71 107 83 03	76
77	75 00 21 45	74 26 24 05	73 77 29 26	72 111 86 46	77
78	76 00 22 09	75 27 24 29	74 81 29 49	73 115 90 29	78
79	77 00 22 33	76 28 24 53	75 85 30 12	74 119 94 12	79
80	78 00 22 57	77 29 25 17	76 89 30 35	75 123 97 55	80
81	79 00 23 21	78 30 25 41	77 93 30 58	76 127 101 38	81
82	80 00 23 45	79 31 26 05	78 97 31 21	77 131 105 21	82
83	81 00 24 09	80 32 26 29	79 101 31 44	78 135 109 04	83
84	82 00 24 33	81 33 26 53	80 105 32 07	79 139 112 47	84
85	83 00 24 57	82 34 27 17	81 109 32 30	80 143 116 30	85
86	84 00 25 21	83 35 27 41	82 113 32 53	81 147 120 13	86
87	85 00 25 45	84 36 28 05	83 117 33 16	82 151 123 56	87
88	86 00 26 09	85 37 28 29	84 121 33 39	83 155 127 39	88
89	87 00 26 33	86 38 28 53	85 125 34 02	84 159 131 22	89
90	88 00 26 57	87 39 29 17	86 129 34 25	85 163 135 05	90
91	89 00 27 21	88 40 29 41	87 133 34 48	86 167 138 48	91
92	90 00 27 45	89 41 30 05	88 137 35 11	87 171 142 31	92
93	91 00 28 09	90 42 30 29	89 141 35 34	88 175 146 14	93
94	92 00 28 33	91 43 30 53	90 145 35 57	89 179 150 00	94
95	93 00 28 57	92 44 31 17	91 149 36 20	90 183 153 43	95
96	94 00 29 21	93 45 31 41	92 153 36 43	91 187 157 26	96
97	95 00 29 45	94 46 32 05	93 157 37 06	92 191 161 09	97
98	96 00 30 09	95 47 32 29	94 161 37 29	93 195 164 52	98
99	97 00 30 33	96 48 32 53	95 165 37 52	94 199 168 35	99
100	98 00 30 57	97 49 33 17	96 169 38 15	95 203 172 18	100
101	99 00 31 21	98 50 33 41	97 173 38 38	96 207 176 01	101
102	100 00 31 45	99 51 34 05	98 177 39 01	97 211 179 44	102
103	101 00 32 09	100 52 34 29	99 181 39 24	98 215 183 27	103
104	102 00 32 33	101 53 34 53	100 185 39 47	99 219 187 10	104
105	103 00 32 57	102 54 35 17	101 189 40 10	100 223 190 53	105
106	104 00 33 21	103 55 35 41	102 193 40 33	101 227 194 36	106
107	105 00 33 45	104 56 36 05	103 197 40 56	102 231 198 19	107
108	106 00 34 09	105 57 36 29	104 201 41 19	103 235 202 02	108
109	107 00 34 33	106 58 36 53	105 205 41 42	104 239 205 45	109
110	108 00 34 57	107 59 37 17	106 209 42 05	105 243 209 28	110
111	109 00 35 21	108 60 37 41	107 213 42 28	106 247 213 11	111
112	110 00 35 45	109 61 38 05	108 217 42 51	107 251 216 54	112
113	111 00 36 09	110 62 38 29	109 221 43 14	108 255 220 37	113
114	112 00 36 33	111 63 38 53	110 225 43 37	109 259 224 20	114
115	113 00 36 57	112 64 39 17	111 229 44 00	110 263 228 03	115
116	114 00 37 21	113 65 39 41	112 233 44 23	111 267 231 46	116
117	115 00 37 45	114 66 40 05	113 237 44 46	112 271 235 29	117
118	116 00 38 09	115 67 40 29	114 241 45 09	113 275 239 12	118
119	117 00 38 33	116 68 40 53	115 245 45 32	114 279 242 55	119
120	118 00 38 57	117 69 41 17	116 249 45 55	115 283 246 38	120
121	119 00 39 21	118 70 41 41	117 253 46 18	116 287 250 21	121
122	120 00 39 45	119 71 42 05	118 257 46 41	117 291 254 04	122
123	121 00 40 09	120 72 42 29	119 261 47 04	118 295 257 47	123
124	122 00 40 33	121 73 42 53	120 265 47 27	119 299 261 30	124
125	123 00 40 57	122 74 43 17	121 269 47 50	120 303 265 13	125
126	124 00 41 21	123 75 43 41	122 273 48 13	121 307 268 56	126
127	125 00 41 45	124 76 44 05	123 277 48 36	122 311 272 39	127
128	126 00 42 09	125 77 44 29	124 281 48 59	123 315 276 22	128
129	127 00 42 33	126 78 44 53	125 285 49 22	124 319 280 05	129
130	128 00 42 57	127 79 45 17	126 289 49 45	125 323 283 48	130
131	129 00 43 21	128 80 45 41	127 293 50 08	126 327 287 31	131
132	130 00 43 45	129 81 46 05	128 297 50 31	127 331 291 14	132
133	131 00 44 09	130 82 46 29	129 301 50 54	128 335 294 57	133
134	132 00 44 33	131 83 46 53	130 305 51 17	129 339 298 40	134
135	133 00 44 57	132 84 47 17	131 309 51 40	130 343 302 23	135
136	134 00 45 21	133 85 47 41	132 313 52 03	131 347 306 06	136
137	135 00 45 45	134 86 48 05	133 317 52 26	132 351 309 49	137
138	136 00 46 09	135 87 48 29	134 321 52 49	133 355 313 32	138
139	137 00 46 33	136 88 48 53	135 325 53 12	134 359 317 15	139
140	138 00 46 57	137 89 49 17	136 329 53 35	135 363 320 58	140
141	139 00 47 21	138 90 49 41	137 333 53 58	136 367 324 41	141
142	140 00 47 45	139 91 50 05	138 337 54 21	137 371 328 24	142
143	141 00 48 09	140 92 50 29	139 341 54 44	138 375 332 07	143
144	142 00 48 33	141 93 50 53	140 345 55 07	139 379 335 50	144
145	143 00 48 57	142 94 51 17	141 349 55 30	140 383 339 33	145
146	144 00 49 21	143 95 51 41	142 353 55 53	141 387 343 16	146
147	145 00 49 45	144 96 52 05	143 357 56 16	142 391 346 59	147
148	146 00 50 09	145 97 52 29	144 361 56 39	143 395 350 42	148
149	147 00 50 33	146 98 52 53	145 365 56 62	144 399 354 25	149
150	148 00 50 57	147 99 53 17	146 369 56 85	145 403 358 08	150
151	149 00 51 21	148 100 53 41	147 373 57 08	146 407 361 51	151
152	150 00 51 45	149 101 54 05	148 377 57 31	147 411 365 34	152
153	151 00 52 09	150 102 54 29	149 381 57 54	148 415 369 17	153
154	152 00 52 33	151 103 54 53	150 385 58 17	149 419 373 00	154
155	153 00 52 57	152 104 55 17	151 389 58 40	150 423 376 43	155
156	154 00 53 21	153 105 55 41	152 393 59 03	151 427 380 26	156
157	155 00 53 45	154 106 56 05	153 397 59 26	152 431 384 09	157
158	156 00 54 09	155 107 56 29	154 401 59 49	153 435 387 52	158
159	157 00 54 33	156 108 56 53	155 405 60 12	154 439 391 35	159
160	158 00 54 57	157 109 57 17	156 409 60 35	155 443 395 18	160
161	159 00 55 21	158 110 57 41	157 413 60 58	156 447 399 01	161
162	160 00 55 45	159 111 58 05	158 417 61 21	157 451 402 44	162
163	161 00 56 09	160 112 58 29	159 421 61 44	158 455 406 27	163
164	162 00 56 33	161 113 58 53	160 425 62 07	159 459 410 10	164
165	163 00 56 57	162 114 59 17	161 429 62 30	160 463 413 53	165
166	164 00 57 21	163 115 59 41	162 433 62 53	161 467 417 36	166
167	165 00 57 45	164 116 59 65	163 437 63 16	162 471 421 19	167
168	166 00 58 09	165 117 60 09	164 441 63 39	163 475 425 02	168
169	167 00 58 33	1			



A *Traverse-Table* for every *Point*, *Half-Point*, and *Quarter-Point* of the *Compass*, to the 100 part of a *League* or *Mile*, which gives the *Difference of Latitude* and *Departure* from the *Meridian*.

25 deg. 19 min.	28 deg. 0 min.	30 deg. 56 min.	33 deg. 45 min.	36 deg. 33 min.
2 Points $\frac{1}{4}$	2 Points $\frac{1}{4}$	2 Points $\frac{1}{4}$	3 Points.	3 Points.
N S E W	N S E W	N S E W	N S E W	N S E W
33 29 83 14 11	29 10 15 56	28 31 10 97	27 44 18 33	26 57 25 33
34 30 74 14 50	29 08 16 03	29 16 17 48	28 27 18 89	27 48 26 37
35 31 64 14 51	29 57 16 50	30 02 17 99	29 10 19 44	28 39 27 35
36 32 51 15 32	31 75 16 97	30 88 18 51	29 93 20 00	29 30 28 36
37 33 45 15 82	32 63 17 44	31 74 19 02	30 76 20 56	30 21 29 37
38 34 35 16 28	33 57 17 91	32 59 19 54	31 60 21 11	31 04 30 38
39 35 26 16 65	34 40 18 38	33 45 20 05	32 43 21 67	31 47 31 39
40 36 16 17 10	35 28 18 83	34 31 20 56	33 26 22 22	32 30 32 40
41 37 06 17 53	36 16 19 31	35 17 21 08	34 09 23 08	33 12 33 41
42 37 67 17 98	37 04 19 81	36 02 21 59	34 92 23 32	33 55 34 42
43 38 87 18 38	37 92 20 27	36 88 22 11	35 75 23 89	34 38 35 43
44 39 78 18 81	38 80 20 74	37 74 22 62	36 58 24 44	35 21 36 44
45 40 68 19 24	39 69 21 21	38 60 23 14	37 42 25 00	36 04 37 45
46 41 51 19 07	40 57 21 68	39 46 23 65	38 25 25 56	36 47 38 46
47 42 40 20 00	41 44 22 16	40 31 24 16	39 08 26 11	37 30 39 47
48 43 30 20 52	42 33 22 63	41 17 24 68	39 91 26 67	38 13 40 48
49 44 20 21 45	43 21 23 10	42 03 25 16	40 74 27 22	38 56 41 49
50 45 10 22 38	44 10 23 57	42 89 25 71	41 57 27 78	39 39 42 50
51 46 12 23 01	44 58 24 04	43 74 26 22	42 40 28 33	40 22 43 51
52 47 01 23 03	45 46 24 51	44 60 26 73	43 24 28 89	41 05 44 52
53 47 47 23 08	46 34 25 48	45 46 27 25	44 07 29 44	41 48 45 53
54 48 32 23 68	47 21 26 44	46 32 27 76	44 90 30 00	42 31 46 54
55 49 17 23 52	48 08 27 92	47 17 28 28	45 73 30 59	43 14 47 55
56 50 02 24 01	48 56 28 40	48 03 28 79	46 56 31 11	43 57 48 56
57 50 47 24 27	49 44 29 37	48 89 29 30	47 39 31 67	44 40 49 57
58 51 33 24 59	50 32 30 34	49 75 29 82	48 22 32 22	45 23 50 58
59 52 19 25 33	51 19 31 31	50 61 30 33	49 05 32 78	46 06 51 59
60 53 05 25 68	52 07 32 28	51 46 30 35	49 89 33 33	46 49 52 60
61 53 51 26 02	52 55 33 25	52 31 31 36	50 72 34 38	47 32 53 61
62 54 37 26 37	53 43 34 22	53 16 32 37	51 55 35 43	48 15 54 62
63 55 23 27 10	54 31 35 19	54 01 33 38	52 38 36 48	48 58 55 63
64 56 09 27 45	55 19 36 16	54 46 34 39	53 21 37 53	49 41 56 64
65 56 55 28 20	56 07 37 13	55 31 35 40	54 04 38 58	50 24 57 65
66 57 41 28 55	56 55 38 10	56 16 36 41	54 47 39 63	51 07 58 66
67 58 27 29 30	57 43 39 07	57 01 37 42	55 30 40 68	51 50 59 67
68 59 13 30 05	58 31 40 04	57 46 38 43	56 13 41 73	52 33 60 68
69 60 00 30 40	59 19 41 01	58 31 39 44	56 56 42 78	53 16 61 69
70 60 46 31 15	60 07 41 58	59 16 40 45	57 39 43 83	53 59 62 70
71 61 32 31 50	60 55 42 55	60 01 41 46	58 22 44 88	54 42 63 71
72 62 18 32 25	61 43 43 52	60 46 42 47	59 05 45 93	55 25 64 72
73 63 04 33 00	62 31 44 49	61 31 43 48	59 48 46 98	56 08 65 73
74 63 50 33 45	63 19 45 46	62 16 44 49	60 31 47 03	56 51 66 74
75 64 36 34 20	64 07 46 43	63 01 45 50	61 14 48 08	57 34 67 75
76 65 22 35 05	64 55 47 40	63 46 46 51	61 57 49 13	58 17 68 76
77 66 08 35 40	65 43 48 37	64 31 47 52	62 40 50 18	59 00 69 77
78 66 54 36 15	66 31 49 34	65 16 48 53	63 23 51 23	59 43 70 78
79 67 40 36 50	67 19 50 31	66 01 49 54	64 06 52 28	60 26 71 79
80 68 26 37 25	68 07 51 28	66 46 50 55	64 49 53 33	61 09 72 80
81 69 12 38 00	68 55 52 25	67 31 51 56	65 32 54 38	61 52 73 81
82 69 58 38 45	69 43 53 22	68 16 52 57	66 15 55 43	62 35 74 82
83 70 44 39 20	70 31 54 19	69 01 53 58	66 58 56 48	63 18 75 83
84 71 30 40 05	71 19 55 16	69 46 54 59	67 41 57 53	64 01 76 84
85 72 16 40 50	72 07 56 13	70 31 55 60	68 24 58 58	64 44 77 85
86 73 02 41 25	72 55 57 10	71 16 56 61	69 07 59 63	65 27 78 86
87 73 48 42 00	73 43 58 07	72 01 57 62	69 50 60 68	66 10 79 87
88 74 34 42 45	74 31 59 04	72 46 58 63	70 33 61 73	66 53 80 88
89 75 20 43 20	75 19 60 01	73 31 59 64	71 16 62 78	67 36 81 89
90 76 06 44 05	76 07 60 58	74 16 60 65	71 99 63 83	68 19 82 90
91 76 52 44 50	76 55 61 55	75 01 61 66	72 82 64 88	69 02 83 91
92 77 38 45 25	77 43 62 52	75 46 62 67	73 65 65 93	69 45 84 92
93 78 24 46 00	78 31 63 49	76 31 63 68	74 48 66 98	70 28 85 93
94 79 10 46 45	79 19 64 46	77 16 64 69	75 31 67 03	71 11 86 94
95 79 56 47 20	80 07 65 43	78 01 65 70	76 14 68 08	71 54 87 95
96 80 42 48 05	80 55 66 40	78 46 66 71	76 57 69 13	72 37 88 96
97 81 28 48 50	81 43 67 37	79 31 67 72	77 40 70 18	73 20 89 97
98 82 14 49 25	82 31 68 34	80 16 68 73	78 23 71 23	74 03 90 98
99 83 00 50 10	83 19 69 31	81 01 69 74	79 06 72 28	74 46 91 99
100 83 46 50 55	84 07 70 28	81 46 70 75	79 49 73 33	75 29 92 100
101 84 32 51 40	84 55 71 25	82 31 71 76	80 32 74 38	76 12 93 101
102 85 18 52 25	85 43 72 22	83 16 72 77	81 15 75 43	76 55 94 102
103 86 04 53 00	86 31 73 19	84 01 73 78	81 98 76 48	77 38 95 103
104 86 50 53 45	87 19 74 16	84 46 74 79	82 81 77 53	78 21 96 104
105 87 36 54 30	88 07 75 13	85 31 75 80	83 64 78 58	79 04 97 105
106 88 22 55 15	88 55 76 10	86 16 76 81	84 47 79 63	79 47 98 106
107 89 08 55 50	89 43 77 07	87 01 77 82	85 30 80 68	80 30 99 107
108 89 54 56 35	90 31 78 04	87 46 78 83	86 13 81 73	81 13 100 108
109 90 40 57 20	91 19 79 01	88 31 79 84	86 56 82 78	81 56 101 109
110 91 26 58 05	92 07 80 00	89 16 80 85	87 39 83 83	82 39 102 110
111 92 12 58 50	92 55 80 57	90 01 81 86	88 22 84 88	83 22 103 111
112 92 58 59 35	93 43 81 54	90 46 82 87	89 05 85 93	84 05 104 112
113 93 44 60 20	94 31 82 51	91 31 83 88	89 48 86 98	84 48 105 113
114 94 30 61 05	95 19 83 48	92 16 84 89	90 31 87 03	85 31 106 114
115 95 16 61 50	96 07 84 45	93 01 85 90	91 14 88 08	86 14 107 115
116 96 02 62 35	96 55 85 42	93 46 86 91	91 57 89 13	86 57 108 116
117 96 48 63 20	97 43 86 39	94 31 87 92	92 40 90 18	87 40 109 117
118 97 34 64 05	98 31 87 36	95 16 88 93	93 23 91 23	88 23 110 118
119 98 20 64 50	99 19 88 33	96 01 89 94	94 06 92 28	89 06 111 119
120 99 06 65 35	100 07 89 30	96 46 90 95	94 49 93 33	89 49 112 120
121 99 52 66 20	100 55 90 27	97 31 91 96	95 32 94 38	90 32 113 121
122 100 38 67 05	101 43 91 24	98 16 92 97	96 15 95 43	91 15 114 122
123 101 24 67 50	102 31 92 21	99 01 93 98	96 58 96 48	91 58 115 123
124 102 10 68 35	103 19 93 18	99 46 94 99	97 41 97 53	92 41 116 124
125 102 56 69 20	104 07 94 15	100 31 95 00	98 24 98 58	93 24 117 125
126 103 42 70 05	104 55 95 12	101 16 96 01	99 07 99 63	94 07 118 126
127 104 28 70 50	105 43 96 09	102 01 97 02	99 50 100 68	94 50 119 127
128 105 14 71 35	106 31 97 06	102 46 98 03	100 33 101 73	95 33 120 128
129 106 00 72 20	107 19 98 03	103 31 99 04	101 16 102 78	96 16 121 129
130 106 46 73 05	108 07 99 00	104 16 100 05	101 99 103 83	96 59 122 130
131 107 32 73 50	108 55 100 00	105 01 101 06	102 82 104 88	97 42 123 131
132 108 18 74 35	109 43 101 00	105 46 102 07	103 65 105 93	98 25 124 132
133 109 04 75 20	110 31 102 00	106 31 103 08	104 48 106 98	99 08 125 133
134 109 50 76 05	111 19 103 00	107 16 104 09	105 31 107 03	99 51 126 134
135 110 36 76 50	112 07 104 00	108 01 105 10	106 14 108 08	100 34 127 135
136 111 22 77 35	112 55 105 00	108 46 106 11	106 57 109 13	101 17 128 136
137 112 08 78 20	113 43 106 00	109 31 107 12	107 40 110 18	102 00 129 137
138 112 54 79 05	114 31 107 00	110 16 108 13	108 23 111 23	102 43 130 138
139 113 40 79 50	115 19 108 00	111 01 109 14	109 06 112 28	103 26 131 139
140 114 26 80 35	116 07 109 00	111 46 110 15	109 49 113 33	104 09 132 140
141 115 12 81 20	116 55 110 00	112 31 111 16	110 32 114 38	104 52 133 141
142 115 58 82 05	117 43 111 00	113 16 112 17	111 15 115 43	105 35 134 142
143 116 44 82 50	118 31 112 00	114 01 113 18	111 98 116 48	106 18 135 143
144 117 30 83 35	119 19 113 00	114 46 114 19	112 81 117 53	107 01 136 144
145 118 16 84 20	120 07 114 00	115 31 115 20	113 64 118 58	107 44 137 145
146 119 02 85 05	120 55 115 00	116 16 116 21	114 47 119 63	108 27 138 146
147 119 48 85 50	121 43 116 00	117 01 117 22	115 30 120 68	109 10 139 147
148 120 34 86 35	122 31 117 00	117 46 118 23	116 13 121 73	109 53 140 148
149 121 20 87 20	123 19 118 00	118 31 119 24	116 56 122 78	110 36 141 149
150 122 06 88 05	124 07 119 00	119 16 120 25	117 39 123 83	111 19 142 150
151 122 52 88 50	124 55 120 00	120 01 121 26	118 22 124 88	112 02 143 151
152 123 38 89 35	125 43 121 00	120 46 122 27	119 05 125 93	112 45 144 152
153 124 24 90 20	126 31 122 00	121 31 123 28	119 48 126 98	113 28 145 153
154 125 10 91 05	127 19 123 00	122 16 124 29	120 31 127 03	114 11 146 154
155 125 56 91 50	128 07 124 00	123 01 125 30	121 14 128 08	114 54 147 155
156 126 42 92 35	128 55 125 00	123 46 126 31	121 57 129 13	115 37 148 156
157 127 28 93 20	129 43 126 00	124 31 127 32	122 40 130 18	116 20 149 157
158 128 14 94 05	130 31 127 00	125 16 128 33	123 23 131 23	117 03 150 158
159 129 00 94 50	131 19 128 00	126 01 129 34	124 06 132 28	117 46 151 159
160 129 46 95 35	132 07 129 00	126 46 130 35	124 49 133 33	118 29 152 160
161 130 32 96 20	132 55 130 00	127 31 131 36	125 32 134 38	119 12 153 161
162 131 18 97 05	133 43 131 00	128 16 132 37	126 15 135 43	119 55 154 162
163 132 04 97 50	134 31 132 00	129 01 133 38	126 58 136 48	120 38 155 163
164 132 50 98 35	135 19 133 00	129 46 134 39	127 41 137 53	121 21 156 164
165 133 36 99 20	136 07 134 00	130 31 135 40	128 24 138 58	122 04 157 165
166 134 22 100 05	136 55 135 00	131 16 136 41	129 07 139 63	122 47 158 166
167 135 08 100 50	137 4			

A *Traverse-Table* for every *Point*, *Half-Point*, and *Quarter-Point* of the *Compass*, to the 100 part of a *League* or *Mile*, which gives the *Difference of Latitude* and *Departure* from the *Meridian*.

Diff. in Long. on Merid. (m'd)	36 deg. 34 min.				39 deg. 22 min.				42 deg. 11 min.				45 deg. 00 min.				Diff. in Long. on Merid. (m'd)
	3 Points $\frac{1}{4}$				3 Points $\frac{1}{2}$				3 Points $\frac{1}{4}$				4 Points.				
	N	S	E	W	N	S	E	W	N	S	E	W	N	S	E	W	
1	00	80	00	60	00	77	00	63	00	74	00	67	00	71	00	66	
2	01	61	01	41	01	55	01	27	01	48	01	34	01	41	01	41	
3	02	41	01	41	02	32	01	90	02	32	02	01	02	12	02	12	
4	03	21	02	38	03	09	02	54	03	22	02	69	03	83	03	83	
5	04	02	02	98	03	86	03	17	03	70	03	36	03	54	03	54	
6	04	82	03	57	04	64	03	81	04	44	04	03	04	24	04	24	
7	05	62	04	17	05	41	04	44	05	18	04	78	05	04	95	7	
8	06	43	04	7	06	18	05	07	06	03	05	37	06	63	05	66	
9	07	23	05	36	06	06	05	71	06	67	06	04	06	36	06	36	
10	08	03	05	96	07	73	06	34	07	41	06	72	07	07	07	10	
11	08	83	06	55	08	52	06	98	08	15	07	39	07	78	07	78	
12	09	63	07	15	09	28	07	61	08	89	08	06	08	49	08	49	
13	10	44	07	74	10	05	08	25	09	63	08	73	09	19	09	19	
14	11	24	08	34	10	82	08	88	10	37	09	40	09	90	09	90	
15	12	05	08	91	11	60	09	52	11	11	10	07	10	61	10	61	
16	12	85	09	53	12	37	10	15	11	85	10	74	11	01	11	01	
17	13	66	10	13	13	14	10	78	12	70	11	42	12	02	12	02	
18	14	46	10	72	13	91	11	42	13	34	12	09	12	73	12	73	
19	15	26	11	32	14	69	12	04	14	08	12	76	13	44	13	44	
20	16	06	11	91	15	46	12	69	14	82	13	43	14	14	14	14	
21	16	87	12	51	16	23	13	32	15	56	14	10	14	85	14	85	
22	17	67	13	11	17	01	13	96	16	33	14	77	15	56	15	56	
23	18	47	13	71	17	78	14	59	17	04	15	45	16	26	16	26	
24	19	28	14	31	18	55	15	22	17	78	16	12	16	97	16	97	
25	20	08	14	89	19	32	15	86	18	52	16	79	17	67	17	68	
26	20	88	15	49	20	10	16	49	19	26	17	46	18	38	18	38	
27	21	69	16	08	20	87	17	13	20	06	18	13	19	69	18	69	
28	22	49	16	68	21	64	17	76	20	75	18	79	19	80	19	80	
29	23	29	17	27	22	42	18	40	21	49	19	41	20	51	20	51	
30	24	10	17	87	23	19	19	03	22	33	20	12	21	21	21	21	
31	24	00	18	47	23	06	19	67	23	07	20	82	21	62	21	62	
32	25	70	19	06	24	74	20	30	23	71	21	49	22	63	22	63	
	E	W	N	S	E	W	N	S	E	W	N	S	E	W	N	S	
	4 Points $\frac{1}{4}$				4 Points $\frac{1}{2}$				4 Points $\frac{1}{4}$				4 Points.				
	53 deg. 26 min.				50 deg. 37 min.				47 deg. 40 min.				45 deg. 00 min.				



A Traverse-Table for every Point, Half-Point, and Quarter-Point of the Compass, to the 100 part of a League or Mile, which gives the Difference of Latitude and Departure from the Meridian.

Diff. in Long. or Miles sailed	36 deg. 34 min.				39 deg. 22 min.				42 deg. 11 min.				45 deg. 00 min.				Diff. in Long. or Miles sailed					
	3 Points $\frac{1}{4}$				3 Points $\frac{1}{2}$				3 Points $\frac{3}{4}$				4 Points.									
	N	SE	W		N	SE	W		N	SE	W		N	SE	W							
	100				100				100				100									
33	26	51	19	66	25	51	20	93	24	45	22	16	23	33	23	33	33					
34	27	31	20	85	26	28	21	57	25	19	22	83	24	04	24	04	34					
35	28	11	20	85	27	06	22	20	25	93	23	50	24	75	24	75	35					
36	28	9	21	46	27	83	22	84	26	07	24	17	25	40	25	40	36					
37	29	72	22	04	28	60	23	47	27	41	24	85	26	16	26	16	37					
38	30	52	22	64	29	37	24	11	28	16	25	52	26	87	26	87	38					
39	31	33	23	23	30	15	24	74	28	90	26	19	27	56	27	56	39					
40	32	13	23	83	30	92	25	38	29	64	26	86	28	28	28	28	40					
41	32	23	24	42	31	69	26	01	30	38	27	53	28	99	28	99	41					
42	33	73	25	02	32	47	26	64	31	12	28	21	29	10	29	10	42					
43	33	54	25	61	33	24	27	28	31	86	28	88	30	41	30	41	43					
44	35	34	26	21	34	01	27	91	32	60	29	55	31	11	31	11	44					
45	36	14	26	81	34	78	28	55	33	34	30	22	31	82	31	82	45					
46	36	94	27	40	35	56	29	18	34	08	30	89	32	53	32	53	46					
47	37	75	28	00	36	33	29	82	34	82	31	56	33	23	33	23	47					
48	38	55	28	59	37	10	30	45	35	57	32	23	33	94	33	94	48					
49	39	36	29	19	37	58	31	08	36	31	32	91	34	05	34	05	49					
50	40	17	29	78	38	65	31	72	37	05	33	58	35	35	35	35	50					
51	40	98	30	38	39	42	32	35	37	79	34	25	36	06	36	06	51					
52	41	77	30	98	40	20	32	99	38	53	34	92	36	77	36	77	52					
53	42	57	31	57	40	97	33	62	39	27	35	59	37	48	37	48	53					
54	43	37	32	17	41	74	34	26	40	01	36	26	38	14	38	14	54					
55	44	18	32	76	42	52	34	86	40	75	36	94	38	89	38	89	55					
56	44	98	33	36	43	29	35	53	41	49	37	61	39	60	39	60	56					
57	45	78	33	96	44	06	36	16	42	23	38	28	40	30	40	30	57					
58	46	59	34	55	44	83	36	79	43	07	38	95	41	01	41	01	58					
59	47	39	35	15	45	61	37	43	43	72	39	62	41	72	41	72	59					
60	48	19	35	74	46	38	38	00	44	45	40	29	42	43	42	43	60					
70	56	22	41	69	44	11	44	41	51	85	47	00	49	49	49	49	70					
80	64	25	47	65	61	84	50	75	59	26	53	72	56	56	56	56	80					
90	72	28	53	61	69	57	57	09	66	67	60	44	63	63	63	63	90					
100	80	32	59	56	77	35	63	43	74	08	67	15	70	71	70	71	100					
200	160	64	119	12	154	60	120	86	148	16	134	30	141	41	141	41	200					
53 deg. 26 min.	E	W	N	S	50 deg. 37 min.	E	W	N	S	47 deg. 49 min.	E	W	N	S	45 deg. 00 min.	E	W	N	S			
	4 Points $\frac{1}{4}$					4 Points $\frac{1}{2}$					4 Points $\frac{3}{4}$					4 Points.						
	100					100					100					100						

# A TABLE OF Meridional Parts.



L.	0	1	2	3	4	5	6
M.	Min.	Min.	Min.	Min.	Min.	Min.	Min.
0	0	600	1200	1801	2402	3004	3607
1	10	610	1210	1811	2412	3014	3617
2	20	620	1220	1821	2422	3024	3627
3	30	630	1230	1831	2432	3034	3637
4	40	640	1240	1841	2442	3044	3647
5	50	650	1250	1851	2452	3054	3657
6	60	660	1260	1861	2462	3064	3667
7	70	670	1270	1871	2472	3074	3677
8	80	680	1280	1881	2482	3084	3687
9	90	690	1290	1891	2492	3094	3697
10	100	700	1300	1901	2502	3104	3707
11	110	710	1310	1911	2512	3114	3717
12	120	720	1320	1921	2522	3124	3727
13	130	730	1330	1931	2532	3134	3737
14	140	740	1340	1941	2542	3144	3747
15	150	750	1350	1951	2552	3154	3758
16	160	760	1360	1961	2562	3165	3768
17	170	770	1370	1971	2572	3175	3778
18	180	780	1380	1981	2582	3185	3788
19	190	790	1390	1991	2593	3195	3798
20	200	800	1400	2001	2603	3205	3808
21	210	810	1410	2011	2613	3215	3818
22	220	820	1420	2021	2623	3225	3828
23	230	830	1430	2031	2633	3235	3838
24	240	840	1440	2041	2643	3245	3848
25	250	850	1450	2051	2653	3255	3858
26	260	860	1460	2061	2663	3265	3868
27	270	870	1470	2071	2673	3275	3878
28	280	880	1481	2081	2683	3285	3888
29	290	890	1491	2091	2693	3295	3898

L.	0	1	2	3	4	5	6
M.	Min.	Min.	Min.	Min.	Min.	Min.	Min.
30	300	900	1501	2101	2702	3305	3908
31	310	910	1511	2111	2713	3315	3919
32	320	920	1521	2121	2723	3325	3929
33	330	930	1531	2131	2733	3335	3939
34	340	940	1541	2141	2743	3345	3949
35	350	950	1551	2151	2753	3355	3959
36	360	960	1561	2161	2763	3365	3969
37	370	970	1571	2171	2773	3375	3979
38	380	980	1581	2182	2783	3386	3989
39	390	990	1591	2192	2793	3396	3999
40	400	1000	1601	2202	2803	3406	4009
41	410	1010	1611	2212	2813	3416	4019
42	420	1020	1621	2222	2823	3426	4029
43	430	1030	1631	2232	2833	3436	4039
44	440	1040	1641	2242	2843	3446	4049
45	450	1050	1651	2252	2853	3456	4059
46	460	1060	1661	2262	2863	3466	4070
47	470	1070	1671	2272	2873	3476	4080
48	480	1080	1681	2282	2883	3486	4090
49	490	1090	1691	2292	2893	3496	4100
50	500	1100	1701	2302	2903	3506	4110
51	510	1110	1711	2312	2914	3516	4120
52	520	1120	1721	2322	2924	3526	4130
53	530	1130	1731	2332	2934	3536	4140
54	540	1140	1741	2342	2944	3546	4150
55	550	1150	1751	2352	2954	3556	4160
56	560	1160	1761	2362	2964	3566	4170
57	570	1170	1771	2372	2974	3576	4180
58	580	1180	1781	2382	2984	3587	4190
59	590	1190	1791	2392	2994	3597	4200



L.	7	8	9	10	11	12	13
<i>M.</i>	<i>Min.</i>	<i>Min.</i>	<i>Min.</i>	<i>Min.</i>	<i>Min.</i>	<i>Min.</i>	<i>Min.</i>
0	4211	4816	5422	6031	6641	7253	7868
1	4221	4826	5433	6041	6651	7264	7879
2	4231	4836	5443	6051	6661	7274	7889
3	4241	4846	5453	6061	6671	7284	7899
4	4251	4856	5463	6071	6681	7294	7909
5	4261	4866	5473	6082	6692	7305	7920
6	4271	4876	5483	6092	6702	7315	7930
7	4281	4886	5493	6102	6712	7325	7940
8	4291	4896	5503	6112	6722	7335	7950
9	4301	4907	5514	6122	6732	7346	7961
10	4311	4917	5524	6132	6743	7356	7971
11	4321	4927	5534	6142	6753	7366	7981
12	4331	4937	5544	6153	6763	7376	7991
13	4342	4947	5554	6163	6773	7387	8002
14	4352	4957	5564	6173	6783	7397	8012
15	4362	4967	5574	6183	6794	7407	8022
16	4372	4977	5584	6193	6804	7417	8032
17	4382	4987	5594	6203	6814	7428	8043
18	4392	4998	5605	6213	6824	7438	8053
19	4402	5008	5615	6224	6834	7448	8063
20	4412	5018	5625	6234	6845	7458	8073
21	4422	5028	5635	6244	6855	7469	8084
22	4432	5038	5645	6254	6865	7479	8094
23	4442	5048	5655	6264	6875	7489	8104
24	4452	5058	5666	6274	6885	7499	8114
25	4463	5068	5676	6285	6896	7510	8125
26	4473	5078	5686	6295	6906	7520	8135
27	4483	5089	5696	6305	6916	7530	8145
28	4493	5099	5706	6315	6926	7540	8155
29	4503	5100	5716	6325	6936	7551	8166

L.	7	8	9	10	11	12	13
<i>M.</i>	<i>Min.</i>	<i>Min.</i>	<i>Min.</i>	<i>Min.</i>	<i>Min.</i>	<i>Min.</i>	<i>Min.</i>
30	4513	5119	5726	6335	6947	7561	8176
31	4523	5129	5737	6346	6957	7571	8186
32	4533	5139	5747	6356	6967	7581	8196
33	4543	5149	5757	6366	6977	7592	8207
34	4553	5159	5767	6376	6987	7602	8217
35	4563	5169	5777	6386	6998	7612	8227
36	4573	5180	5787	6396	7008	7622	8237
37	4584	5190	5797	6406	7018	7633	8248
38	4594	5200	5808	6417	7028	7643	8258
39	4604	5210	5818	6427	7038	7653	8268
40	4614	5220	5828	6437	7049	7663	8279
41	4624	5230	5838	6447	7059	7674	8289
42	4634	5240	5848	6457	7069	7684	8299
43	4644	5250	5858	6467	7079	7694	8310
44	4654	5260	5868	6477	7089	7704	8320
45	4664	5271	5879	6488	7100	7715	8330
46	4674	5281	5889	6498	7110	7725	8341
47	4684	5291	5899	6508	7120	7735	8351
48	4695	5301	5909	6518	7130	7745	8361
49	4705	5311	5919	6528	7141	7756	8372
50	4715	5321	5929	6539	7151	7766	8382
51	4725	5331	5939	6549	7161	7776	8392
52	4735	5341	5950	6559	7171	7786	8403
53	4745	5351	5960	6569	7182	7797	8413
54	4755	5362	5970	6579	7192	7807	8423
55	4765	5372	5980	6590	7202	7817	8434
56	4775	5382	5990	6600	7212	7827	8444
57	4785	5392	6000	6610	7223	7838	8454
58	4796	5402	6010	6620	7233	7848	8465
59	4806	5412	6021	6630	7243	7858	8475



L.	14	15	16	17	18	19	20
M.	Min.	Min.	Min.	Min.	Min.	Min.	Min.
0	8485	9105	9728	10353	10982	11615	12251
1	8495	9115	9738	10363	10993	11625	12262
2	8506	9126	9748	10374	11003	11636	12273
3	8516	9136	9759	10384	11014	11647	12283
4	8526	9146	9769	10395	11024	11657	12294
5	8537	9157	9780	10405	11035	11668	12304
6	8547	9167	9790	10416	11045	11678	12315
7	8557	9177	9800	10426	11056	11689	12326
8	8568	9188	9811	10437	11066	11700	12336
9	8578	9198	9821	10447	11077	11710	12347
10	8589	9208	9832	10458	11087	11721	12358
11	8599	9219	9842	10468	11098	11731	12368
12	8610	9229	9852	10479	11108	11742	12379
13	8620	9239	9863	10489	11119	11752	12390
14	8630	9250	9873	10499	11129	11763	12400
15	8641	9260	9884	10510	11140	11774	12411
16	8651	9270	9894	10520	11150	11784	12422
17	8661	9281	9904	10531	11161	11795	12432
18	8672	9291	9915	10541	11171	11805	12443
19	8682	9301	9925	10552	11182	11816	12454
20	8692	9312	9936	10562	11192	11827	12464
21	8703	9322	9946	10573	11203	11837	12475
22	8713	9332	9956	10583	11213	11848	12486
23	8723	9343	9967	10593	11224	11858	12496
24	8734	9353	9977	10604	11234	11869	12507
25	8744	9363	9988	10614	11245	11880	12518
26	8754	9374	9998	10625	11255	11890	12528
27	8765	9384	10008	10635	11266	11901	12539
28	8775	9394	10019	10646	11276	11911	12550
29	8785	9405	10029	10656	11287	11922	12560

L.	14	15	16	17	18	19	20
M.	Min.	Min.	Min.	Min.	Min.	Min.	Min.
30	8796	9415	10040	10667	11297	11932	12571
31	8806	9425	10050	10677	11308	11943	12582
32	8816	9436	10061	10688	11318	11954	12592
33	8827	9446	10071	10698	11329	11964	12603
34	8837	9456	10081	10709	11340	11975	12614
35	8847	9467	10092	10720	11351	11985	12624
36	8858	9477	10103	10730	11361	11996	12635
37	8868	9487	10113	10741	11372	12007	12646
38	8878	9498	10123	10751	11382	12017	12656
39	8889	9508	10134	10762	11393	12028	12667
40	8899	9519	10144	10772	11403	12039	12678
41	8909	9529	10154	10783	11414	12049	12688
42	8920	9539	10165	10793	11424	12060	12699
43	8930	9550	10175	10804	11435	12071	12710
44	8940	9560	10186	10814	11446	12081	12721
45	8951	9571	10196	10825	11456	12092	12731
46	8961	9581	10206	10835	11467	12102	12742
47	8971	9592	10217	10846	11477	12113	12753
48	8982	9602	10227	10856	11488	12124	12763
49	8992	9613	10238	10867	11498	12134	12774
50	9002	9623	10248	10877	11509	12145	12785
51	9012	9634	10259	10888	11520	12155	12795
52	9023	9644	10269	10898	11530	12166	12806
53	9033	9655	10280	10909	11541	12177	12817
54	9043	9665	10290	10919	11551	12187	12827
55	9054	9676	10301	10930	11561	12198	12838
56	9064	9686	10311	10940	11571	12209	12849
57	9074	9696	10322	10951	11583	12219	12860
58	9084	9707	10332	10961	11594	12230	12870
59	9095	9717	10343	10972	11604	12241	12881



L.	21	22	23	24	25	26	27
M.	Min.	Min.	Min.	Min.	Min.	Min.	Min.
0	12892	13537	14187	14841	15500	16165	16836
1	12902	13548	14197	14852	15511	16176	16847
2	12913	13558	14208	14863	15522	16187	16858
3	12924	13569	14219	14873	15533	16198	16869
4	12935	13580	14230	14884	15544	16209	16880
5	12945	14590	14241	14895	15555	16220	16891
6	12956	13601	14251	14906	15566	16232	16903
7	12967	13612	14262	14917	15577	16243	16914
8	12978	13623	14273	14928	15588	16254	16925
9	12988	13633	14284	14939	15599	16265	16936
10	12999	13644	14295	14950	15610	16276	16948
11	13010	13655	14306	14961	15621	16287	16959
12	13020	13666	14317	14972	15632	16298	16970
13	13031	13676	14328	14983	15643	16310	16981
14	13042	13687	14339	14994	15654	16320	16993
15	13053	13698	14349	15005	15665	16332	17004
16	13063	13709	14360	15016	15676	16343	17015
17	13074	13720	14371	15027	15687	16354	17026
18	13085	13731	14382	15038	15698	16365	17038
19	13096	13742	14393	15049	15710	16377	17049
20	13106	13753	14404	15060	15721	16388	17060
21	13117	13764	14415	15071	15732	16399	17071
22	13128	13774	14426	15082	15743	16410	17083
23	13138	13785	14437	15093	15754	16421	17094
24	13149	13796	14448	15104	15765	16432	17105
25	13160	13807	14458	15115	15776	16443	17116
26	13171	13818	14469	15126	15787	16455	17128
27	13181	13828	14480	15137	15798	16466	17139
28	13192	13839	14491	15148	15809	16477	17150
29	13203	13850	14502	15159	15820	16488	17161

L.	21	22	23	24	25	26	27
M.	Min.	Min.	Min.	Min.	Min.	Min.	Min.
30	13214	13861	14513	15170	15832	16499	17173
31	13224	13872	14524	15181	15843	16510	17184
32	13235	13883	14535	15192	15854	16522	17195
33	13246	13894	14546	15203	15865	16533	17207
34	13257	13904	14557	15214	15876	16544	17218
35	13267	13915	14568	15225	15887	16555	17229
36	13278	13926	14579	15235	15898	16566	17240
37	13289	13937	14589	15247	15909	16578	17252
38	13300	13948	14600	15258	15920	16589	17263
39	13310	13958	14611	15269	15932	16600	17274
40	13321	13969	14622	15280	15943	16611	17286
41	13332	13980	14633	15291	15954	16622	17297
42	13342	13991	14644	15302	15965	16634	17308
43	13353	14002	14655	15313	15976	16645	17319
44	13364	14013	14666	15324	15987	16656	17331
45	13375	14024	14677	15335	15998	16667	17342
46	13386	14034	14688	15346	16009	16678	17353
47	13397	14045	14698	15357	16020	16689	17365
48	13407	14056	14709	15368	16031	16701	17376
49	13418	14067	14720	15379	16043	16712	17387
50	13429	14078	14731	15390	16054	16723	17399
51	13440	14088	14742	15401	16065	16734	17410
52	13450	14099	14753	15412	16076	16746	17421
53	13461	14110	14764	15423	16087	16757	17432
54	13472	14121	14775	15434	16098	16769	17444
55	13483	14132	14786	15445	16109	16780	17455
56	13494	14143	14797	15456	16120	16791	17466
57	13504	14154	14808	15467	16131	16802	17478
58	13515	14165	14819	15478	16143	16813	17489
59	13526	14176	14830	15489	16154	16824	17500



L.	28	29	30	31	32	33	34
M.	Min.	Min.	Min.	Min.	Min.	Min.	Min.
0	17512	18195	18884	19581	20284	20996	21715
1	17523	18206	18895	19592	20296	21007	21727
2	17534	18217	18907	19604	20307	21019	21739
3	17546	18229	18919	19615	20319	21031	21751
4	17557	18240	18930	19627	20331	21043	21763
5	17568	18252	18942	19639	20343	21055	21775
6	17580	18263	18953	19650	20355	21067	21787
7	17591	18275	18965	19662	20367	21079	21800
8	17602	18286	18976	19674	20378	21091	21812
9	17614	18297	18988	19685	20390	21103	21824
10	17625	18309	18999	19697	20402	21115	21836
11	17636	18320	19011	19709	20414	21127	21848
12	17648	18332	19023	19720	20426	21139	21860
13	17659	18343	19034	19732	20438	21151	21872
14	17670	18355	19046	19744	20449	21163	21884
15	17682	18366	19057	19756	20461	21175	21896
16	17693	18378	19069	19768	20473	21187	21908
17	17705	18389	19081	19779	20485	21198	21920
18	17716	18401	19092	19791	20497	21210	21933
19	17727	18412	19104	19803	20508	21222	21945
20	17739	18424	19115	19814	20520	21234	21957
21	17750	18435	19127	19826	20532	21246	21969
22	17761	18446	19138	19837	20544	21258	21981
23	17772	18458	19150	19849	20556	21270	21993
24	17784	18469	19162	19861	20568	21282	22005
25	17795	18481	19173	19873	20580	21294	22017
26	17806	18492	19185	19884	20591	21306	22030
27	17818	18504	19196	19896	20603	21318	22042
28	17830	18515	19208	19908	20615	21330	22054
29	17841	18527	19219	19920	20627	21342	22066

L.	28	29	30	31	32	33	34
M.	Min.	Min.	Min.	Min.	Min.	Min.	Min.
30	17852	18538	19231	19931	20639	21354	22078
31	17864	18550	19243	19943	20651	21366	22090
32	17875	18561	19254	19955	20662	21378	22102
33	17886	18573	19266	19966	20674	21390	22114
34	17898	18584	19278	19978	20686	21402	22127
35	17909	18596	19289	19990	20698	21414	22139
36	17921	18607	19301	20002	20710	21426	22151
37	17932	18619	19313	20013	20722	21438	22163
38	17943	18630	19324	20025	20734	21450	22175
39	17955	18642	19336	20037	20746	21462	22187
40	17966	18653	19347	20049	20757	21474	22199
41	17978	18665	19359	20060	20769	21486	22212
42	17989	18676	19371	20072	20781	21498	22224
43	18000	18688	19382	20084	20793	21510	22236
44	18012	18699	19394	20096	20805	21522	22248
45	18023	18711	19405	20107	20817	21534	22260
46	18035	18722	19417	20119	20829	21546	22272
47	18046	18734	19429	20131	20841	21558	22285
48	18057	18745	19440	20143	20853	21570	22297
49	18069	18757	19452	20154	20865	21582	22309
50	18080	18768	19464	20166	20877	21594	22321
51	18092	18780	19475	20178	20889	21607	22333
52	18103	18792	19487	20190	20901	21619	22346
53	18114	18703	19499	20202	20913	21631	22358
54	18126	18815	19510	20213	20925	21643	22370
55	18137	18826	19522	20225	20937	21655	22382
56	18149	18838	19534	20237	20949	21667	22394
57	18160	18849	19545	20249	20961	21679	22407
58	18172	18861	19557	20260	20973	21691	22419
59	18183	18872	19568	20272	20985	21703	22431



L.	35	36	37	38	39	40	41
M.	Min.	Min.	Min.	Min.	Min.	Min.	Min.
0	22443	23180	23927	24683	25450	26227	27016
1	22455	23193	23939	24696	25462	26240	27029
2	22468	23205	23952	24708	25475	26253	27043
3	22480	23217	23964	24721	25488	26266	27056
4	22492	23230	23977	24734	25501	26279	27069
5	22504	23242	23989	24746	25514	26292	27083
6	22516	23254	24002	24759	25527	26305	27096
7	22529	23267	24014	24771	25540	26319	27109
8	22541	23279	24027	24785	25553	26332	27122
9	22553	23292	24039	24797	25566	26345	27136
10	22565	23304	24052	24810	25578	26358	27149
11	22578	23316	24064	24823	25591	26371	27162
12	22590	23329	24077	24835	25604	26384	27175
13	22602	23341	24090	24848	25617	26397	27189
14	22614	23353	24102	24861	25630	26410	27202
15	22627	23366	24115	24874	25643	26423	27215
16	22639	23378	24127	24886	25656	26436	27229
17	22651	23390	24140	24899	25669	26449	27242
18	22663	23403	24152	24912	25682	26463	27255
19	22676	23415	24165	24925	25695	26476	27269
20	22688	23428	24178	24937	25707	26489	27282
21	22700	23440	24190	24950	25720	26502	27295
22	22712	23453	24203	24963	25733	26515	27308
23	22725	23465	24215	24976	25746	26528	27322
24	22737	23478	24228	24988	25759	26541	27335
25	22749	23490	24240	25001	25772	26554	27348
26	22761	23502	24253	25014	25785	26568	27362
27	22774	23515	24265	25027	25798	26581	27375
28	22786	23527	24278	25034	25811	26594	27388
29	22798	23540	24291	25052	25824	26607	27402

L.	35	36	37	38	39	40	41
M.	Min.	Min.	Min.	Min.	Min.	Min.	Min.
30	22810	23552	24303	25065	25837	26620	27415
31	22823	23565	24316	25078	25850	26633	27429
32	22835	23577	24329	25090	25863	26646	27442
33	22847	23589	24341	25103	25876	26660	27455
34	22860	23602	24354	25116	25889	26673	27469
35	22872	23614	24367	25129	25902	26686	27482
36	22884	23627	24379	25142	25915	26699	27495
37	22897	23639	24392	25154	25928	26712	27509
38	22909	23652	24404	25167	25941	26725	27522
39	22921	23664	24417	25180	25954	26739	27535
40	22933	23677	24430	25193	25967	26751	27549
41	22946	23689	24442	25206	25980	26765	27562
42	22958	23702	24455	25218	25993	26778	27576
43	22970	23714	24468	25231	26006	26791	27589
44	22983	23727	24480	25244	26019	26805	27602
45	22995	23739	24493	25257	26032	26818	27615
46	23007	23752	24506	25270	26045	26831	27629
47	23020	23764	24518	25283	26058	26844	27643
48	23032	23777	24531	25295	26071	26857	27656
49	23044	23789	24543	25308	26084	26871	27669
50	23057	23801	24556	25321	26097	26884	27683
51	23069	23813	24569	25334	26110	26898	27696
52	23081	23826	24581	25347	26123	26910	27710
53	23094	23839	24594	25360	26136	26923	27723
54	23106	23851	24607	25372	26149	26937	27737
55	23118	23864	24616	25385	26162	26950	27750
56	23131	23876	24632	25398	26175	26963	27764
57	23143	23889	24645	25411	26188	26976	27777
58	23155	23902	24658	25424	26201	26990	27790
59	23167	23914	24670	25437	26214	27003	27804



L.	42	43	44	45	46	47	48
M.	Min.	Min.	Min.	Min.	Min.	Min.	Min.
0	27817	28631	29459	30300	31156	32028	32916
1	27831	28645	29472	30314	31170	32042	32931
2	27844	28658	29486	30328	31185	32057	32946
3	27858	28672	29500	30342	31199	32072	32961
4	27871	28685	29514	30356	31214	32086	32975
5	27885	28700	29528	30370	31228	32101	32990
6	27898	28713	29542	30384	31242	32116	33005
7	27912	28727	29556	30398	31257	32130	33020
8	27925	28741	29570	30413	31271	32145	33035
9	27939	28754	29584	30427	31286	32160	33050
10	27951	28768	29598	30441	31300	32174	33065
11	27966	28782	29611	30455	31315	32189	33080
12	27979	28795	29625	30470	31329	32204	33095
13	27993	28809	29639	30484	31343	32219	33110
14	28006	28823	29653	30498	31358	32233	33125
15	28020	28837	29667	30512	31372	32248	33140
16	28033	28850	29681	30526	31387	32263	33155
17	28047	28864	29695	30541	31401	32277	33170
18	28060	28878	29709	30555	31416	32292	33185
19	28074	28892	29723	30569	31430	32307	33200
20	28087	28905	29737	30583	31445	32322	33215
21	28101	28919	29751	30597	31459	32336	33231
22	28114	28933	29765	30612	31474	32351	33246
23	28128	28947	29779	30626	31488	32366	33261
24	28141	28960	29793	30640	31503	32381	33276
25	28155	28974	29807	30654	31517	32395	33291
26	28168	28988	29821	30669	31532	32410	33306
27	28182	29002	29835	30683	31546	32425	33321
28	28195	29015	29849	30697	31561	32440	33336
29	28209	29029	29863	30711	31575	32455	33351

L.	42	43	44	45	46	47	48
M.	Min.	Min.	Min.	Min.	Min.	Min.	Min.
30	28223	29043	29877	30726	31590	32469	33366
31	28236	29057	29891	30740	31604	32484	33381
32	28250	29071	29905	30754	31619	32499	33396
33	28263	29084	29919	30769	31633	32514	33411
34	28277	29097	29933	30783	31648	32529	33427
35	28290	29112	29947	30797	31662	32544	33442
36	28304	29126	29961	30811	31677	32558	33457
37	28318	29140	29975	30826	31691	32573	33472
38	28331	29153	29989	30840	31706	32588	33487
39	28345	29167	30003	30854	31721	32603	33501
40	28358	29181	30018	30869	31735	32618	33517
41	28372	29195	30032	30883	31750	32633	33532
42	28386	29209	30046	30897	31764	32647	33548
43	28399	29223	30060	30912	31779	32662	33563
44	28413	29236	30074	30926	31793	32677	33578
45	28426	29250	30088	30940	31808	32692	33593
46	28440	29264	30102	30955	31823	32707	33608
47	28454	29278	30116	30969	31837	32722	33623
48	28467	29292	30130	30983	31852	32737	33639
49	28481	29306	30144	30998	31866	32752	33654
50	28495	29320	30158	31012	31881	32766	33669
51	28508	29333	30172	31026	31896	32781	33684
52	28522	29347	30187	31041	31910	32796	33699
53	28536	29361	30201	31056	31925	32811	33715
54	28550	29375	30215	31070	31940	32826	33730
55	28563	29389	30229	31084	31954	32841	33745
56	28577	29403	30243	31098	31969	32856	33760
57	28591	29417	30257	31112	31983	32871	33776
58	28605	29431	30271	31127	31998	32886	33791
59	28618	29444	30285	31141	32013	32901	33806



L.	49	50	51	52	53	54	55
M.	Min.	Min.	Min.	Min.	Min.	Min.	Min.
0	33821	34745	35688	36652	37638	38647	39680
1	33836	34761	35704	36669	37655	38664	39697
2	33852	34776	35720	36685	37671	38681	39715
3	33867	34792	35736	36701	37688	38698	39732
4	33882	34807	35752	36717	37704	38715	39750
5	33897	34823	35768	36734	37721	38732	39767
6	33913	34839	35784	36750	37738	38749	39785
7	33928	34854	35800	36766	37754	38766	39802
8	33943	34870	35816	36782	37771	38783	39820
9	33959	34885	35832	36799	37788	38800	39837
10	33974	34901	35848	36815	37804	38817	39855
11	33989	34917	35864	36831	37821	38834	39872
12	34004	34932	35880	36848	37838	38851	39890
13	34020	34948	35895	36864	37855	38868	39907
14	34035	34963	35911	36880	37871	38886	39925
15	34050	34979	35927	36897	37888	38903	39942
16	34066	34995	35943	36913	37905	38920	39960
17	34081	35010	35959	36929	37921	38937	39977
18	34196	35026	35975	36946	37938	38954	39995
19	34112	35042	35991	36962	37955	38971	40013
20	34127	35057	36007	36978	37972	38988	40030
21	34142	35073	36023	36995	37988	39005	40048
22	34158	35089	36039	37011	38005	39023	40065
23	34173	35104	36055	37027	38022	39040	40083
24	34188	35120	36071	37044	38039	39057	40100
25	34204	35136	36087	37060	38055	39074	40118
26	34219	35151	36103	37077	38072	39091	40136
27	34235	35167	36119	37093	38089	39109	40153
28	34250	35183	36136	37109	38106	39126	40171
29	34265	35198	36152	37126	38123	39143	40189

L.	49	50	51	52	53	54	55
M.	Min.	Min.	Min.	Min.	Min.	Min.	Min.
30	34281	35214	36168	37142	38139	39160	40206
31	34296	35230	36184	37159	38156	39177	40224
32	34312	35246	36200	37175	38173	39195	40242
33	34327	35261	36216	37192	38190	39212	40259
34	34342	35277	36232	37208	38207	39229	40277
35	34358	35293	36248	37224	38223	39246	40295
36	34373	35309	36264	37241	38240	39264	40312
37	34389	35324	36280	37257	38257	39281	40330
38	34404	35340	36296	37274	38274	39298	40348
39	34420	35356	36313	37290	38291	39315	40366
40	34435	35372	36329	37307	38308	39333	40383
41	34450	35388	36345	37323	38325	39350	40401
42	34466	35403	36361	37340	38343	39367	40419
43	34481	35419	36377	37356	38358	39385	40436
44	34497	35425	36393	37373	38375	39402	40454
45	34512	35451	36409	37389	38392	39419	40472
46	34528	35467	36425	37406	38409	39437	40490
47	34543	35482	36442	37422	38426	39454	40508
48	34559	35498	36458	37439	38443	39471	40525
49	34574	35514	36474	37456	38460	39489	40543
50	34590	35530	36490	37472	38477	39505	40561
51	34605	35546	36506	37489	38494	39523	40579
52	34621	35561	36523	37505	38511	39541	40597
53	34636	35577	36539	37522	38528	39558	40614
54	34652	35593	36555	37538	38545	39576	40632
55	34667	35609	36571	37555	38562	39593	40650
56	34683	35625	36587	37572	38579	39610	40668
57	34698	35641	36604	37588	38596	39628	40686
58	34714	35657	36620	37605	38613	39645	40704
59	34730	35673	36636	37621	38630	39663	40722



L.	56	57	58	59	60	61	62
M.	Min.	Min.	Min.	Min.	Min.	Min.	Min.
0	40739	41827	42943	44092	45274	46493	47750
1	40757	41845	42962	44111	45294	46513	47771
2	40775	41863	42981	44131	45314	46534	47793
3	40793	41882	43000	44150	45334	46555	47814
4	40811	41900	43019	44170	45354	46575	47835
5	40829	41918	43038	44189	45374	46596	47857
6	40847	41937	43057	44208	45394	46617	47878
7	40865	41955	43076	44228	45414	46637	47900
8	40883	41974	43095	44247	45434	46658	47921
9	40901	41992	43114	44267	45454	46679	47942
10	40919	42011	43132	44286	45475	46699	47964
11	40937	42029	43151	44306	45495	46720	47985
12	40955	42047	43170	44325	45515	46741	48007
13	40973	42066	43189	44345	45535	46762	48028
14	40991	42084	43208	44364	45555	46782	48049
15	41009	42103	43227	44384	45575	46803	48071
16	41027	42121	43246	44404	45595	46824	48092
17	41045	42140	43265	44423	45615	46845	48114
18	41063	42158	43284	44443	45636	46866	48135
19	41081	42177	43303	44462	45656	46886	48157
20	41099	42195	43322	44482	45676	46907	48178
21	41117	42214	43342	44502	45696	46928	48200
22	41135	42232	43361	44521	45716	46948	48222
23	41153	42251	43380	44541	45737	46970	48243
24	41171	42270	43399	44560	45757	46991	48265
25	41189	42288	43418	44580	45777	47012	48286
26	41207	42307	43437	44600	45797	47032	48308
27	41225	42325	43456	44619	45818	47053	48329
28	41243	42344	43475	44639	45838	47074	48351
29	41261	42362	43494	44660	45858	47095	48373

L.	56	57	58	59	60	61	62
M.	Min.	Min.	Min.	Min.	Min.	Min.	Min.
30	41279	42381	43513	44678	45878	47116	48394
31	41297	42400	43533	44698	45899	47137	48416
32	41316	42418	43552	44718	45919	47158	48438
33	41334	42437	43571	44738	45939	47179	48459
34	41352	42456	43590	44757	45960	47200	48481
35	41370	42474	43609	44777	45980	47221	48503
36	41388	42493	43628	44797	46001	47242	48525
37	41406	42512	43648	44817	46021	47263	48546
38	41425	42530	43667	44836	46041	47284	48568
39	41443	42549	43686	44856	46062	47305	48590
40	41461	42568	43705	44876	46082	47326	48612
41	41479	42586	43725	44896	46103	47347	48633
42	41497	42605	43744	44916	46123	47369	48655
43	41516	42624	43763	44935	46143	47390	48677
44	41534	42643	43782	44955	46164	47411	48699
45	41552	42661	43802	44975	46184	47432	48721
46	41570	42680	43821	44995	46205	47453	48743
47	41588	42699	43840	45015	46225	47474	48764
48	41607	42718	43859	45035	46246	47495	48786
49	41625	42736	43879	45055	46266	47517	48808
50	41643	42755	43898	45075	46287	47538	48830
51	41662	42774	43917	45094	46307	47559	48852
52	41680	42793	43937	45114	46328	47580	48874
53	41698	42811	43956	45134	46348	47601	48896
54	41717	42830	43975	45154	46369	47623	48918
55	41735	42849	43995	45174	46390	47644	48940
56	41753	42868	44014	45194	46410	47665	48962
57	41772	42887	44034	45214	46431	47686	48984
58	41790	42906	44053	45234	46451	47708	49006
59	41808	42925	44072	45254	46472	47729	49028



L.	63	64	65	66	67	68	69
M.	Min.	Min.	Min.	Min.	Min.	Min.	Min.
0	49050	50395	51788	53236	54740	56309	57946
1	49072	50417	51812	53260	54766	56333	57974
2	49094	50440	51836	53285	54792	56362	58002
3	49116	50463	51860	53309	54817	56389	58030
4	49138	50486	51883	53334	54843	56415	58058
5	49160	50509	51907	53359	54869	56442	58086
6	49182	50532	51931	53383	54894	56469	58114
7	49204	50555	51954	53408	54920	56490	58142
8	49226	50577	51978	53433	54946	56523	58170
9	49248	50600	52002	53457	54971	56550	58198
10	49271	50623	52026	53482	54997	56576	58226
11	49293	50646	52050	53507	55023	56603	58254
12	49315	50669	52073	53532	55049	56630	58282
13	49337	50692	52097	53556	55075	56657	58310
14	49359	50715	52121	53581	55100	56684	58339
15	49381	50738	52145	53606	55126	56711	58367
16	49404	50761	52169	53631	55152	56738	58395
17	49426	50784	52193	53656	55178	56765	58423
18	49448	50807	52217	53681	55204	56792	58452
19	49470	50830	52241	53705	55230	56819	58480
20	49493	50853	52265	53730	55256	56846	58508
21	49515	50877	52289	53755	55282	56873	58537
22	49537	50900	52313	53780	55308	56900	58565
23	49560	50923	52337	53805	55334	56928	58593
24	49582	50946	52361	53830	55360	56955	58622
25	49604	50969	52385	53855	55386	56982	58650
26	49627	50992	52409	53880	55412	57009	58679
27	49649	51015	52433	53905	55438	57036	58707
28	49671	51039	52457	53930	55464	57063	58735
29	49694	51062	52481	53955	55490	57091	58764

L.	63	64	65	66	67	68	69
M.	Min.	Min.	Min.	Min.	Min.	Min.	Min.
30	49716	51085	52505	53980	55516	57118	58793
31	49739	51108	52529	54005	55542	57145	58821
32	49761	51131	52553	54030	55568	57173	58850
33	49783	51155	52577	54056	55595	57200	58878
34	49806	51178	52601	54081	55621	57227	58907
35	49828	51201	52626	54106	55647	57255	58936
36	49851	51225	52650	54131	55673	57282	58964
37	49873	51248	52674	54156	55699	57310	58993
38	49896	51271	52698	54181	55726	57337	59022
39	49918	51295	52723	54207	55752	57364	59051
40	49941	51318	52747	54232	55778	57392	59079
41	49963	51341	52771	54257	55805	57419	59108
42	49986	51365	52795	54282	55831	57447	59137
43	50009	51388	52820	54308	55857	57475	59166
44	50031	51412	52844	54333	55884	57502	59195
45	50054	51435	52868	54358	55910	57530	59224
46	50076	51459	52893	54384	55937	57557	59253
47	50099	51482	52917	54409	55963	57585	59281
48	50122	51506	52942	54435	55990	57613	59310
49	50144	51529	52966	54460	56016	57640	59339
50	50167	51553	52990	54485	56043	57668	59368
51	50190	51576	53015	54511	56069	57696	59397
52	50212	51600	53039	54536	56096	57725	59426
53	50235	51623	53064	54562	56122	57751	59455
54	50258	51647	53088	54587	56149	57779	59485
55	50281	51670	53113	54613	56175	57807	59514
56	50303	51694	53137	54638	56202	57835	59543
57	50326	51718	53162	54664	56229	57862	59572
58	50349	51741	53186	54689	56255	57890	59601
59	50372	51765	53211	54715	56282	57918	59630



L.	70	71	72	73	74	75	76
M.	Min.	Min.	Min.	Min.	Min.	Min.	Min.
0	59660	61457	63349	65345	67457	69703	72101
1	59689	61488	63381	65379	67494	6 742	72142
2	59718	61519	63414	65413	67530	69781	72183
3	59747	61550	63446	65447	67566	69819	72225
4	59777	61580	63478	65482	67603	69858	72266
5	59806	61611	63511	65516	67639	69897	72308
6	59835	61642	63543	65550	67676	69936	72349
7	59865	61673	63576	65585	67712	69975	72391
8	59894	61704	63609	65619	67749	70014	72433
9	59924	61735	63641	65654	67785	70053	72475
10	59953	61766	63674	65688	67822	70092	72516
11	59983	61797	63706	65723	67858	70131	72558
12	60012	61828	63739	65757	67895	70170	72600
13	60042	61859	63772	65792	67932	70209	72642
14	60071	61890	63805	65826	67969	70248	72684
15	60101	61921	63837	65861	68005	70287	72726
16	60130	61952	63870	65895	68042	70327	72768
17	60160	61983	63903	65930	68079	70366	72810
18	60190	62014	63936	65965	68116	70405	72852
19	60219	62046	63969	66000	68153	70445	72894
20	60249	62077	64002	66034	68190	70484	72937
21	60279	62108	64035	66069	68227	70524	72979
22	60308	62139	64068	66104	68264	70563	73021
23	60338	62171	64101	66139	68301	70600	73064
24	60368	62202	64134	66174	68338	70642	73006
25	60398	62233	64167	66209	68376	70682	73149
26	60427	62265	64200	66244	68413	70722	73191
27	60457	62296	64233	66279	68450	70762	73234
28	60487	62327	64266	66314	68487	70801	73277
29	60517	62358	64299	66350	68525	70841	73320

L.	70	71	72	73	74	75	76
M.	Min.	Min.	Min.	Min.	Min.	Min.	Min.
30	60547	62390	64332	66385	68562	70881	73362
31	60577	62422	64366	66420	68600	70921	73405
32	60607	62453	64399	66455	68637	70961	73448
33	60637	62485	64432	66491	68675	71001	73491
34	60667	62517	64466	66526	68712	71041	73534
35	60697	62548	64499	66561	68750	71082	73577
36	60727	62580	64533	66597	68787	71122	73620
37	60757	62612	64566	66632	68825	71162	73664
38	60788	62644	64600	66668	68863	71202	73707
39	60818	62675	64633	66703	68901	71243	73750
40	60848	62707	64667	66739	68938	71283	73794
41	60878	62739	64700	66774	68976	71323	73837
42	60908	62771	64734	66810	69014	71364	73880
43	60939	62803	64768	66846	69052	71404	73924
44	60969	62835	64801	66881	69090	71445	73968
45	60999	62866	64835	66917	69128	71486	74011
46	61030	62898	64869	66953	69166	71526	74055
47	61060	62930	64903	66989	69204	71567	74099
48	61091	62962	64936	67024	69242	71608	74142
49	61121	62994	64970	67060	69281	71649	74186
50	61151	63027	65004	67096	69319	71690	74230
51	61182	63059	65038	67132	69357	71730	74274
52	61212	63091	65072	67168	69395	71771	74318
53	61243	63123	65106	67204	69434	71812	74362
54	61274	63155	65140	67240	69472	71853	74406
55	61304	63187	65174	67276	69511	71895	74450
56	61335	63220	65208	67312	69549	71936	74495
57	61365	63252	65242	67349	69588	71977	74539
58	61396	63284	65276	67385	69626	72018	74583
59	61427	63317	65310	67421	69665	72059	74628



L.	77	78	79	80	81	82	83.
M.	Min.	Min.	Min.	Min.	Min.	Min.	Min.
0	74672	77446	80457	83753	87391	91456	96059
1	74717	77494	80510	83810	87455	91527	96141
2	74761	77542	80562	83868	87519	91599	96224
3	74806	77590	80615	83926	87583	91672	96306
4	74850	77639	80668	83983	87648	91744	96389
5	74895	77687	80720	84041	87712	91816	96472
6	74940	77735	80773	84099	87777	91889	96555
7	74985	77784	80826	84158	87841	91962	96638
8	75029	77832	80879	84216	87906	92035	96722
9	75074	77881	80932	84274	87971	92108	96806
10	75119	77930	80985	84333	88036	92181	96890
11	75164	77978	81038	84391	88101	92254	96974
12	75209	78027	81092	84450	88166	92328	97058
13	75254	78076	81145	84509	88232	92402	97142
14	75300	78125	81198	84568	88297	92476	97227
15	75345	78174	81252	84626	88363	92550	97312
16	75390	78223	81306	84686	88428	92624	97397
17	75436	78272	81359	84745	88494	92699	97483
18	75481	78322	81413	84804	88560	92773	97568
19	75527	78371	81467	84863	88626	92848	97654
20	75572	78420	81521	84923	88693	92923	97740
21	75618	78470	81575	84982	88759	92998	97827
22	75663	78519	81629	85042	88826	93073	97913
23	75709	78569	81683	85102	88892	93148	98000
24	75755	78619	81737	85162	88959	93224	98086
25	75801	78668	81792	85222	89026	93300	98173
26	75847	78718	81846	85282	89093	93375	98261
27	75893	78768	81901	85342	89160	93452	98348
28	75939	78818	81955	85402	89227	93528	98436
29	75985	78868	82010	85462	89295	93604	98524

L.	77	78	79	80	81	82	83
M.	Min.	Min.	Min.	Min.	Min.	Min.	Min.
30	76031	78918	82065	85523	89362	93681	98613
31	76077	78968	82120	85584	89430	93758	98701
32	76123	79019	82175	85644	89498	93835	98790
33	76170	79069	82230	85705	89566	93912	98878
34	76216	79119	82285	85766	89634	93989	98967
35	76263	79170	82341	85827	89702	94066	99057
36	76309	79221	82396	85889	89771	94144	99146
37	76356	79271	82451	85950	89839	94221	99236
38	76402	79322	82507	86011	89908	94299	99327
39	76449	79373	82563	86073	89977	94378	99417
40	76496	79424	82618	86135	90046	94456	99508
41	76543	79475	82674	86196	90115	94534	99598
42	76590	79526	82730	86258	90184	94613	99689
43	76637	79577	82786	86320	90254	94691	99780
44	76684	79628	82842	86382	90323	94770	99872
45	76731	79680	82899	86445	90393	94849	99963
46	76778	79731	82955	86507	90463	94929	100055
47	76826	79782	83011	86569	90533	95008	100148
48	76873	79834	83068	86632	90603	95088	100240
49	76920	79885	83124	86695	90673	95168	100333
50	76968	79937	83181	86757	90744	95248	100426
51	77015	79989	83238	86820	90814	95329	100519
52	77063	80040	83294	86883	90885	95409	100613
53	77110	80092	83351	86946	90956	95489	100706
54	77158	80144	83408	87010	91027	95570	100800
55	77206	80196	83466	87073	91098	95651	100894
56	77254	80248	83523	87136	91169	95732	100989
57	77302	80300	83580	87200	91240	95814	101084
58	77350	80353	83637	87264	91312	95895	101179
59	77398	80405	83695	87327	91384	95977	101274



L.	84	85	86	87	88	89
<i>M.</i>	<i>Min.</i>	<i>Min.</i>	<i>Min.</i>	<i>Min.</i>	<i>Min.</i>	<i>Min.</i>
0	101370	107647	115326	125223	139166	162998
1	101466	107762	115470	125414	139454	163575
2	101562	107877	115614	125607	139744	164163
3	101658	107993	115759	125800	140037	164761
4	101754	108109	115905	125995	140332	165370
5	101851	108225	116050	126191	140630	165949
6	101948	108342	116198	126389	140930	166620
7	102046	108459	116345	126586	141233	167262
8	102144	108577	116493	126786	141539	167917
9	102242	108696	116641	126986	141847	168585
10	102340	108814	116791	127188	142158	169265
11	102438	108933	116940	127391	142472	169906
12	102537	109052	117091	127595	142789	170669
13	102636	109172	117242	127800	143109	171303
14	102735	109291	117394	128007	143432	172132
15	102835	109412	117547	128215	143758	172887
16	102935	109533	117700	128425	144087	173660
17	103035	109655	117854	128635	144419	174450
18	103136	109777	118009	128847	144754	175259
19	103237	109899	118164	129060	145093	176087
20	103338	110022	118320	129274	145435	176936
21	103440	110145	118476	129489	145781	177807
22	103541	110269	118634	129706	146130	178699
23	103643	110393	118792	129925	146483	179616
24	103745	110517	118951	130144	146839	180558
25	103848	110642	119110	130366	147199	181526
26	103951	110768	119271	130588	147563	182523
27	104054	110893	119431	130812	147930	183549
28	104158	111020	119594	131038	148302	184607
29	104262	111146	119756	131265	148678	185698

L.	84	85	86	87	88	89
<i>M.</i>	<i>Min.</i>	<i>Min.</i>	<i>Min.</i>	<i>Min.</i>	<i>Min.</i>	<i>Min.</i>
30	104366	111274	119920	131493	149058	186825
31	104471	111401	120084	131723	149442	187991
32	104575	111529	120249	131955	149830	189197
33	104680	111658	120415	132188	150223	190447
34	104785	111787	120582	132423	150621	191744
35	104891	111917	120749	132659	151023	193092
36	104997	112047	120917	132897	151430	194495
37	105104	112177	121086	133137	151842	195958
38	105211	112309	121256	133378	152258	197486
39	105318	112440	121427	133621	152680	199085
40	105426	112572	121599	133866	153107	200752
41	105533	112705	121771	134112	153540	202525
42	105641	112838	121944	134361	153978	204383
43	105749	112971	122118	134611	154421	206348
44	105858	113106	122293	134863	154870	208431
45	105967	113240	122469	135116	155326	200649
46	106077	113376	122646	135372	155787	213020
47	106187	113511	122824	135630	156255	215566
48	106297	113648	123002	135889	156730	218317
49	106408	113784	123182	136151	157210	221306
50	106519	113922	123363	136414	157698	224580
51	106630	114060	123544	136680	158193	228199
52	106741	114198	123727	136947	158695	232243
53	106853	114337	123910	137217	159204	236829
54	106965	114477	124095	137489	159721	242118
55	107077	114617	124280	137763	160246	248359
56	107191	114758	124467	138039	160779	256008
57	107304	114899	124655	138317	161320	265829
58	107418	115041	124842	138598	161870	279580
59	107533	115183	125031	138881	162429	303643



# A TABLE

OF THE

MILES of East and West, answering to  
the Degrees of Longitude in the Fourth  
Rumb.

Miles			Miles			Miles		
Latitude.	East & West.	Longitude.	Latitude.	East & West.	Longitude.	Latitude.	East & West.	Longitude.
D. M.		D. M.	D. M.		D. M.	D. M.		D. M.
0 0	0	0 0	3 0	180	3 0	6 0	360	6 0
0 10	10	0 10	3 10	190	3 10	6 10	370	6 10
0 20	20	0 20	3 20	200	3 20	6 20	380	6 20
0 30	30	0 30	3 30	210	3 30	6 30	390	6 30
0 40	40	0 40	3 40	220	3 40	6 40	400	6 40
0 50	50	0 50	3 50	230	3 50	6 50	410	6 50
1 0	60	1 0	4 0	240	4 0	7 0	420	7 0
1 10	70	1 10	4 10	250	4 10	7 10	430	7 10
1 20	80	1 20	4 20	260	4 20	7 20	440	7 20
1 30	90	1 30	4 30	270	4 30	7 30	450	7 30
1 40	100	1 40	4 40	280	4 40	7 40	460	7 40
1 50	110	1 50	4 50	290	4 50	7 50	470	7 50
2 0	120	2 0	5 0	300	5 0	8 0	480	8 0
2 10	130	2 10	5 10	310	5 10	8 10	490	8 10
2 20	140	2 20	5 20	320	5 20	8 20	500	8 20
2 30	150	2 30	5 30	330	5 30	8 30	510	8 30
2 40	160	2 40	5 40	340	5 40	8 40	520	8 40
2 50	170	2 50	5 50	350	5 50	8 50	530	8 50

Miles			Miles			Miles		
Latitude.	East & West.	Longitude.	Latitude.	East & West.	Longitude.	Latitude.	East & West.	Longitude.
D. M.		D. M.	D. M.		D. M.	D. M.		D. M.
9 0	540	9 00	15 0	500	15 10	21 0	1230	21 23
9 10	550	9 10	15 10	910	15 21	21 10	1270	21 39
9 20	560	9 20	15 20	920	15 31	21 20	1280	21 50
9 30	570	9 30	15 30	930	15 41	21 30	1290	22 01
9 40	580	9 40	15 40	940	15 51	21 40	1300	22 12
9 50	590	9 50	15 50	950	16 00	21 50	1310	22 22
10 0	600	10 00	16 0	960	16 12	22 0	1320	22 33
10 10	610	10 10	16 10	970	16 23	22 10	1330	22 44
10 20	620	10 20	16 20	980	16 33	22 20	1340	22 55
10 30	630	10 30	16 30	990	16 44	22 30	1350	23 06
10 40	640	10 40	16 40	1000	16 55	22 40	1360	23 17
10 50	650	10 50	16 50	1010	17 05	22 50	1370	23 23
11 0	660	11 00	17 0	1020	17 15	23 0	1380	23 39
11 10	670	11 10	17 10	1030	17 25	23 10	1390	23 49
11 20	680	11 20	17 20	1040	17 36	23 20	1400	23 00
11 30	690	11 30	17 30	1050	17 47	23 30	1410	24 11
11 40	700	11 40	17 40	1060	17 57	23 40	1420	24 22
11 50	710	11 50	17 50	1070	18 08	23 50	1430	24 33
12 0	720	12 00	18 0	1080	18 18	24 0	1440	24 44
12 10	730	12 10	18 10	1090	18 29	24 10	1450	24 55
12 20	740	12 20	18 20	1100	18 39	24 20	1460	25 06
12 30	750	12 30	18 30	1110	18 49	24 30	1470	25 17
12 40	760	12 40	18 40	1120	19 00	24 40	1480	25 28
12 50	770	12 50	18 50	1130	19 10	24 50	1490	25 38
13 0	780	13 00	19 0	1140	19 21	25 0	1500	25 50
13 10	790	13 10	19 10	1150	19 31	25 10	1510	26 01
13 20	800	13 20	19 20	1160	19 42	25 20	1520	26 12
13 30	810	13 30	19 30	1170	19 53	25 30	1530	26 23
13 40	820	13 40	19 40	1180	20 04	25 40	1540	26 34
13 50	830	13 50	19 50	1190	20 14	25 50	1550	26 45
14 0	840	14 00	20 0	1200	20 25	26 0	1560	26 56
14 10	850	14 10	20 10	1210	20 35	26 10	1570	27 07
14 20	860	14 20	20 20	1220	20 46	26 20	1580	27 08
14 30	870	14 30	20 30	1230	20 57	26 30	1590	27 29
14 40	880	14 40	20 40	1240	21 07	26 40	1600	27 40
14 50	890	14 50	20 50	1250	21 18	26 50	1610	27 51



Latitude		Miles East & West	Longitude		Latitude		Miles East & West	Longitude		Latitude		Miles East & West	Longitude	
D.	M.		D.	M.	D.	M.		D.	M.	D.	M.		D.	M.
27	0	162	28	03	33	0	1980	35	02	33	0	2340	42	26
27	1	163	28	14	33	1	1990	35	12	33	1	2350	42	39
27	2	164	28	25	33	2	2000	35	23	33	2	2360	42	52
27	3	165	28	37	33	3	2010	35	33	33	3	2370	43	04
27	4	166	28	48	33	4	2020	35	47	33	4	2380	43	17
27	5	167	28	59	33	5	2030	35	59	33	5	2390	43	30
28	0	168	29	11	34	0	2040	36	11	40	0	2400	43	43
28	1	169	29	22	34	1	2050	36	23	40	1	2410	43	56
28	2	170	29	34	34	2	2060	36	03	40	2	2420	44	09
28	3	171	29	46	34	3	2070	36	47	40	3	2430	44	21
28	4	172	29	57	34	4	2080	36	59	40	4	2440	44	34
28	5	173	30	08	34	5	2090	37	12	40	5	2450	44	48
29	0	174	30	19	35	0	2100	37	24	41	0	2460	45	02
29	1	175	30	31	35	1	2110	37	36	41	1	2470	45	16
29	2	176	30	43	35	2	2120	37	48	41	2	2480	45	29
29	3	177	30	54	35	3	2130	38	00	41	3	2490	45	42
29	4	178	31	05	35	4	2140	38	13	41	4	2500	45	55
29	5	179	31	17	35	5	2150	38	25	41	5	2510	46	08
30	0	180	31	28	36	0	2160	38	38	42	0	2520	46	22
30	1	181	31	40	36	1	2170	38	50	42	1	2530	46	36
30	2	182	31	51	36	2	2180	39	03	42	2	2540	46	49
30	3	183	32	03	36	3	2190	39	15	42	3	2550	47	02
30	4	184	32	15	36	4	2200	39	27	42	4	2560	47	16
30	5	185	32	26	36	5	2210	39	40	42	5	2570	47	30
31	0	186	32	37	37	0	2220	39	53	43	0	2580	47	43
31	1	187	32	49	37	1	2230	40	05	43	1	2590	47	56
31	2	188	33	00	37	2	2240	40	18	43	2	2600	48	10
31	3	189	33	12	37	3	2250	40	31	43	3	2610	48	23
31	4	190	33	25	37	4	2260	40	43	43	4	2620	48	35
31	5	191	33	37	37	5	2270	40	56	43	5	2630	48	53
32	0	192	33	48	38	0	2280	41	08	44	0	2640	49	06
32	1	193	34	00	38	1	2290	41	21	44	1	2650	49	20
32	2	194	34	12	38	2	2300	41	33	44	2	2660	49	34
32	3	195	34	24	38	3	2310	41	46	44	3	2670	49	48
32	4	196	34	36	38	4	2320	42	00	44	4	2680	50	02
32	5	197	34	48	38	5	2330	42	13	44	5	2690	50	16

Latitude		Miles East & West	Longitude		Latitude		Miles East & West	Longitude		Latitude		Miles East & West	Longitude	
D.	M.		D.	M.	D.	M.		D.	M.	D.	M.		D.	M.
45	0	2700	50	30	51	0	3060	59	30	57	0	3440	70	42
45	1	2710	50	43	51	1	3070	59	46	57	1	3450	70	56
45	2	2720	50	57	51	2	3080	60	01	57	2	3460	71	10
45	3	2730	51	12	51	3	3090	60	17	57	3	3470	71	24
45	4	2740	51	26	51	4	3100	60	33	57	4	3480	71	38
45	5	2750	51	40	51	5	3110	60	49	57	5	3490	71	52
46	0	2760	51	54	52	0	3120	61	05	58	0	3500	72	06
46	1	2770	52	10	52	1	3130	61	21	58	1	3510	72	20
46	2	2780	52	25	52	2	3140	61	37	58	2	3520	72	34
46	3	2790	52	39	52	3	3150	61	54	58	3	3530	73	00
46	4	2800	52	54	52	4	3160	62	10	58	4	3540	73	14
46	5	2810	53	08	52	5	3170	62	26	58	5	3550	73	28
47	0	2820	53	23	53	0	3180	62	43	59	0	3560	73	42
47	1	2830	53	37	53	1	3190	63	00	59	1	3570	74	00
47	2	2840	53	52	53	2	3200	63	17	59	2	3580	74	14
47	3	2850	54	06	53	3	3210	63	34	59	3	3590	75	00
47	4	2860	54	21	53	4	3220	63	51	59	4	3600	75	14
47	5	2870	54	36	53	5	3230	64	08	59	5	3610	75	28
48	0	2880	54	52	54	0	3240	64	24	60	0	3620	76	00
48	1	2890	55	05	54	1	3250	64	41	60	1	3630	76	14
48	2	2900	55	22	54	2	3260	64	58	60	2	3640	76	28
48	3	2910	55	37	54	3	3270	65	15	60	3	3650	77	00
48	4	2920	55	51	54	4	3280	65	32	60	4	3660	77	14
48	5	2930	56	07	54	5	3290	65	50	60	5	3670	77	28
49	0	2940	56	22	55	0	3300	66	08	61	0	3680	78	00
49	1	2950	56	38	55	1	3310	66	26	61	1	3690	78	14
49	2	2960	56	52	55	2	3320	66	42	61	2	3700	78	28
49	3	2970	57	08	55	3	3330	67	01	61	3	3710	79	00
49	4	2980	57	23	55	4	3340	67	19	61	4	3720	79	14
49	5	2990	57	39	55	5	3350	67	36	61	5	3730	79	28
50	0	3000	57	54	56	0	3360	67	54	62	0	3740	80	00
50	1	3010	58	10	56	1	3370	68	11	62	1	3750	80	14
50	2	3020	58	26	56	2	3380	68	29	62	2	3760	81	00
50	3	3030	58	42	56	3	3390	68	47	62	3	3770	81	14
50	4	3040	58	58	56	4	3400	69	05	62	4	3780	81	28
50	5	3050	59	14	56	5	3410	69	24	62	5	3790	81	42



Miles				Miles				Miles			
Latitude. East		Longitude. West.		Latitude. East		Longitude. West.		Latitude. East		Longitude. West.	
D.	M.	D.	M.	D.	M.	D.	M.	D.	M.	D.	M.
63	03780	81	44	66	03960	88	44	69	04140	96	33
63	103790	82	06	66	103970	89	08	69	104150	97	02
63	203800	82	28	66	203980	89	32	69	204160	97	30
63	303810	82	51	66	303990	89	57	69	304170	98	00
63	403820	83	14	66	404000	90	23	69	404180	98	29
63	503830	83	36	66	504010	90	48	69	504190	98	58
64	03840	83	59	67	04020	91	13	70	04200	99	26
64	103850	84	22	67	104030	91	38				
64	203860	84	45	67	204040	92	04				
64	303870	85	09	67	304050	92	30				
64	403880	85	35	67	404060	92	56				
64	503890	85	55	67	504070	93	23				
65	03900	86	15	68	04080	93	50				
65	103910	86	42	68	104090	94	17				
65	203920	87	06	68	204100	94	44				
65	303930	87	29	68	304110	95	11				
65	403940	87	55	68	404120	95	38				
65	503950	88	20	68	504130	96	05				

# A TABLE

FOR

*Changing the Degrees and Minutes of East  
and West into MILES.*



Parallel.	1 Mi- nute.	2 Mi- nutes.	3 Mi- nutes.	4 Mi- nutes.	5 Mi- nutes.	6 Mi- nutes.	7 Mi- nutes.	8 Mi- nutes.	9 Mi- nutes.
	M. c.p.	M. c.p.	M. c.p.	M. c.p.	M. c.p.	M. c.p.	M. c.p.	M. c.p.	M. c.p.
0	1	0	2	0	3	0	4	0	5
1	1	0	2	0	3	0	4	0	5
2	1	0	2	0	3	0	4	0	5
3	1	0	2	0	3	0	4	0	5
4	1	0	2	0	3	0	4	0	5
5	1	0	2	0	3	0	4	0	5
6	1	0	2	0	3	0	4	0	5
7	1	0	2	0	3	0	4	0	5
8	1	0	2	0	3	0	4	0	5
9	1	0	2	0	3	0	4	0	5
10	1	0	2	0	3	0	4	0	5
11	1	0	2	0	3	0	4	0	5
12	1	0	2	0	3	0	4	0	5
13	1	0	2	0	3	0	4	0	5
14	1	0	2	0	3	0	4	0	5
15	1	0	2	0	3	0	4	0	5
16	1	0	2	0	3	0	4	0	5
17	1	0	2	0	3	0	4	0	5
18	1	0	2	0	3	0	4	0	5
19	1	0	2	0	3	0	4	0	5
20	0	9	1	0	2	0	3	0	4
21	0	9	1	0	2	0	3	0	4
22	0	9	1	0	2	0	3	0	4
23	0	9	1	0	2	0	3	0	4
24	0	9	1	0	2	0	3	0	4
25	0	9	1	0	2	0	3	0	4
26	0	9	1	0	2	0	3	0	4
27	0	9	1	0	2	0	3	0	4
28	0	9	1	0	2	0	3	0	4
29	0	9	1	0	2	0	3	0	4
30	0	9	1	0	2	0	3	0	4
31	0	9	1	0	2	0	3	0	4
32	0	9	1	0	2	0	3	0	4
33	0	9	1	0	2	0	3	0	4
34	0	9	1	0	2	0	3	0	4

Parallel.	1 Mi- nute.	2 Mi- nutes.	3 Mi- nutes.	4 Mi- nutes.	5 Mi- nutes.	6 Mi- nutes.	7 Mi- nutes.	8 Mi- nutes.	9 Mi- nutes.
	M. c.p.	M. c.p.	M. c.p.	M. c.p.	M. c.p.	M. c.p.	M. c.p.	M. c.p.	M. c.p.
35	0	8	1	0	2	0	3	0	4
36	0	8	1	0	2	0	3	0	4
37	0	8	1	0	2	0	3	0	4
38	0	8	1	0	2	0	3	0	4
39	0	8	1	0	2	0	3	0	4
40	0	8	1	0	2	0	3	0	4
41	0	8	1	0	2	0	3	0	4
42	0	7	1	0	2	0	3	0	4
43	0	7	1	0	2	0	3	0	4
44	0	7	1	0	2	0	3	0	4
45	0	7	1	0	2	0	3	0	4
46	0	7	1	0	2	0	3	0	4
47	0	7	1	0	2	0	3	0	4
48	0	7	1	0	2	0	3	0	4
49	0	7	1	0	2	0	3	0	4
50	0	6	1	0	2	0	3	0	4
51	0	6	1	0	2	0	3	0	4
52	0	6	1	0	2	0	3	0	4
53	0	6	1	0	2	0	3	0	4
54	0	6	1	0	2	0	3	0	4
55	0	6	1	0	2	0	3	0	4
56	0	5	1	0	2	0	3	0	4
57	0	5	1	0	2	0	3	0	4
58	0	5	1	0	2	0	3	0	4
59	0	5	1	0	2	0	3	0	4
60	0	5	1	0	2	0	3	0	4
61	0	5	1	0	2	0	3	0	4
62	0	5	1	0	2	0	3	0	4
63	0	5	1	0	2	0	3	0	4
64	0	4	0	9	1	0	2	0	3
65	0	4	0	8	1	0	2	0	3
66	0	4	0	8	1	0	2	0	3
67	0	4	0	8	1	0	2	0	3
68	0	4	0	7	1	0	2	0	3
69	0	4	0	7	1	0	2	0	3



Parallel.	10 Mi- nutes.	20 Mi- nutes.	30 Mi- nutes.	40 Mi- nutes.	50 Mi- nutes.	1 De- gree.	2 De- grees.	3 De- grees.	4 De- grees.
	M. c.p.	M. c.p.	M. c.p.	M. c.p.	M. c.p.	M. c.p.	M. c.p.	M. c.p.	M. c.p.
0	10	20	30	40	50	0	120	180	240
1	10	20	30	40	50	0	120	180	240
2	10	20	30	40	50	0	119	179	239
3	10	20	30	39	49	9	119	179	239
4	10	20	29	39	49	9	119	179	239
5	10	19	29	39	49	8	119	179	239
6	9	19	29	39	49	7	119	179	238
7	9	19	29	39	49	6	119	178	238
8	9	19	29	39	49	5	118	178	237
9	9	19	29	39	49	4	118	177	237
10	9	19	29	39	49	3	118	177	236
11	9	19	29	39	49	2	117	176	236
12	9	19	29	39	49	1	117	176	235
13	9	19	29	39	49	0	116	175	235
14	9	19	29	39	49	0	116	175	234
15	9	19	29	39	49	0	115	174	234
16	9	19	29	39	49	0	115	174	233
17	9	19	29	39	49	0	114	173	233
18	9	19	29	39	49	0	114	173	232
19	9	19	29	39	49	0	113	172	232
20	9	19	29	39	49	0	112	171	231
21	9	19	29	39	49	0	112	171	230
22	9	19	29	39	49	0	111	170	230
23	9	19	29	39	49	0	111	170	229
24	9	19	29	39	49	0	110	169	229
25	9	19	29	39	49	0	109	168	228
26	9	19	29	39	49	0	108	167	228
27	9	19	29	39	49	0	107	166	227
28	9	19	29	39	49	0	106	165	227
29	9	19	29	39	49	0	105	164	226
30	9	19	29	39	49	0	104	163	226
31	9	19	29	39	49	0	103	162	225
32	9	19	29	39	49	0	102	161	225
33	9	19	29	39	49	0	101	160	224
34	9	19	29	39	49	0	100	159	224

Parallel.	10 Mi- nutes.	20 Mi- nutes.	30 Mi- nutes.	40 Mi- nutes.	50 Mi- nutes.	1 De- gree.	2 De- grees.	3 De- grees.	4 De- grees.
	M. c.p.	M. c.p.	M. c.p.	M. c.p.	M. c.p.	M. c.p.	M. c.p.	M. c.p.	M. c.p.
35	8	216	424	532	641	750	858	967	1076
36	8	116	224	332	440	548	657	765	874
37	8	016	024	031	039	047	095	143	191
38	7	515	823	631	539	447	545	643	741
39	7	815	523	331	138	546	693	839	986
40	7	715	323	030	638	546	693	839	986
41	7	515	122	630	137	745	390	643	896
42	7	414	922	329	737	244	619	243	817
43	7	314	621	929	236	643	917	713	617
44	7	214	421	628	835	643	26	3129	5172
45	7	114	121	228	335	442	484	8127	2169
46	6	913	920	827	834	741	683	4125	0166
47	6	813	620	427	234	140	981	8122	8163
48	6	713	320	026	633	340	079	9119	9159
49	6	613	119	726	332	839	478	7118	1151
50	6	412	619	325	732	138	677	1115	7154
51	6	312	918	925	231	537	875	5113	3151
52	6	212	313	524	630	836	973	9110	8147
53	6	012	018	124	130	136	172	2108	3144
54	5	911	817	623	529	435	370	5105	8141
55	5	711	517	222	928	734	468	8103	2137
56	5	611	216	822	428	033	667	1100	7134
57	5	411	916	321	827	232	765	598	3131
58	5	310	615	921	226	531	663	691	4127
59	5	210	315	520	625	830	961	892	7123
60	5	010	015	020	025	030	060	090	120
61	4	819	714	519	424	229	158	287	3116
62	4	719	414	118	823	428	256	384	5112
63	4	619	113	618	222	727	254	581	7109
64	4	519	813	217	522	926	322	678	5105
65	4	419	512	716	521	125	450	776	1101
66	4	319	412	216	320	324	448	873	297
67	3	917	811	715	619	523	446	970	393
68	3	717	511	215	018	722	545	667	899
69	3	617	210	814	317	921	543	164	886
70	3	517	110	013	416	720	440	160	180



Parallel.	5 De- grees.	6 De- grees.	7 De- grees.	8 De- grees.	9 De- grees.	10 De- grees.	20 De- grees.
	M. c.p.	M. c.p.	M. c.p.	M. c.p.	M. c.p.	M. c.p.	M. c.p.
0	300	0360	0420	0480	0540	0600	01200
1	300	0359	0419	0479	0539	0599	01199
2	299	0359	0419	0479	0539	0599	01199
3	299	0359	0419	0479	0539	0599	01199
4	299	0359	0419	0478	0538	0598	01197
5	298	0358	0418	0478	0537	0597	01195
6	298	0358	0417	0477	0537	0596	01193
7	297	0357	0416	0476	0536	0595	01191
8	297	0356	0415	0475	0534	0594	01188
9	296	0355	0414	0474	0533	0592	01185
10	295	0354	0413	0472	0531	0590	01181
11	294	0353	0412	0471	0529	0588	01177
12	293	0352	0410	0469	0528	0586	01173
13	292	0350	0409	0467	0526	0584	01169
14	291	0349	0407	0465	0524	0582	01164
15	289	0347	0405	0463	0521	0579	01159
16	288	0346	0403	0461	0519	0576	01153
17	286	0344	0401	0459	0516	0573	01147
18	285	0342	0399	0456	0513	0570	01141
19	283	0340	0397	0453	0510	0567	01134
20	281	0338	0394	0451	0507	0563	01127
21	280	0336	0392	0448	0504	0560	01120
22	278	0333	0389	0445	0500	0556	01112
23	276	0331	0386	0441	0497	0552	01104
24	274	0328	0384	0438	0493	0548	01096
25	272	0326	0380	0435	0489	0543	01087
26	269	0323	0377	0431	0485	0539	01078
27	267	0320	0374	0427	0481	0534	01069
28	264	0317	0370	0423	0476	0529	01059
29	262	0314	0367	0419	0472	0524	01049
30	259	0311	0363	0415	0467	0519	01039
31	257	0308	0360	0411	0462	0514	01028
32	254	0305	0356	0407	0457	0508	01017
33	251	0301	0352	0402	0452	0503	01006
34	248	0297	0348	0397	0447	0497	00994

Parallel.	5 De- grees.	6 De- grees.	7 De- grees.	8 De- grees.	9 De- grees.	10 De- grees.	20 De- grees.
	M. c.p.	M. c.p.	M. c.p.	M. c.p.	M. c.p.	M. c.p.	M. c.p.
35	245	0294	0344	0393	0442	0491	0583
36	242	0291	0339	0388	0436	0485	0570
37	239	0281	0335	0383	0431	0479	0558
38	236	0283	0331	0378	0425	0472	0545
39	233	0279	0326	0373	0419	0466	0532
40	229	0275	0321	0367	0413	0459	0519
41	226	0271	0317	0362	0407	0452	0505
42	222	0267	0312	0356	0401	0445	0491
43	219	0263	0307	0351	0394	0438	0477
44	215	0259	0302	0345	0388	0431	0463
45	212	0254	0296	0339	0381	0424	0448
46	208	0250	0291	0333	0375	0416	0433
47	204	0245	0286	0327	0368	0409	0418
48	199	0239	0279	0319	0359	0399	0399
49	196	0236	0275	0314	0354	0393	0387
50	192	0231	0270	0308	0347	0385	0371
51	188	0226	0264	0302	0340	0377	0355
52	184	0221	0258	0295	0332	0369	0338
53	180	0216	0252	0288	0325	0361	0322
54	176	0211	0246	0282	0317	0352	0305
55	172	0206	0240	0275	0309	0344	0288
56	167	0201	0234	0268	0302	0335	0271
57	163	0196	0229	0262	0295	0326	0253
58	159	0190	0222	0254	0286	0318	0236
59	154	0185	0216	0247	0278	0309	0218
60	150	0180	0210	0240	0270	0300	0200
61	145	0174	0203	0232	0261	0290	0181
62	140	0169	0197	0225	0253	0281	0163
63	136	0163	0190	0217	0245	0272	0144
64	131	0157	0184	0210	0236	0263	0126
65	126	0152	0177	0202	0228	0253	0107
66	122	0146	0170	0195	0219	0244	0088
67	117	0140	0164	0187	0211	0234	0068
68	112	0134	0157	0179	0202	0224	0049
69	107	0129	0150	0172	0193	0215	0030
70	100	0120	0140	0160	0180	0200	0010



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A  
TABLE

FOR

*Reducing MILES of East and West  
into Degrees of Longitude.*

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Parallel.	1 Mile.			2 Miles.			3 Miles.			4 Miles.			5 Miles.		
	D.	M.	S.	D.	M.	S.	D.	M.	S.	D.	M.	S.	D.	M.	S.
0	0	1	0	0	2	0	0	3	0	0	4	0	0	5	0
1	0	1	0	0	2	0	0	3	0	0	4	0	0	5	0
2	0	1	0	0	2	0	0	3	0	0	4	0	0	5	0
3	0	1	0	0	2	0	0	3	0	0	4	0	0	5	0
4	0	1	0	0	2	0	0	3	0	0	4	1	0	5	1
5	0	1	0	0	2	0	0	3	1	0	4	1	0	5	1
6	0	1	0	0	2	1	0	3	1	0	4	1	0	5	2
7	0	1	0	0	2	1	0	3	1	0	4	2	0	5	2
8	0	1	1	0	2	1	0	3	2	0	4	2	0	5	3
9	0	1	1	0	2	1	0	3	2	0	4	3	0	5	3
10	0	1	1	0	2	2	0	3	3	0	4	4	0	5	4
11	0	1	1	0	2	2	0	3	3	0	4	4	0	5	5
12	0	1	2	0	2	3	0	3	4	0	4	5	0	5	6
13	0	1	2	0	2	3	0	3	5	0	4	6	0	5	7
14	0	1	2	0	2	4	0	3	5	0	4	7	0	5	8
15	0	1	2	0	2	4	0	3	6	0	4	8	0	5	9
16	0	1	2	0	2	5	0	3	7	0	4	10	0	5	11
17	0	1	3	0	2	6	0	3	8	0	4	11	0	5	12
18	0	1	3	0	2	6	0	3	9	0	4	12	0	5	13
19	0	1	3	0	2	7	0	3	10	0	4	14	0	5	15
20	0	1	4	0	2	8	0	3	12	0	4	15	0	5	17
21	0	1	4	0	2	9	0	3	13	0	4	17	0	5	19
22	0	1	5	0	2	9	0	3	14	0	4	19	0	5	21
23	0	1	5	0	2	10	0	3	16	0	4	21	0	5	23
24	0	1	6	0	2	11	0	3	17	0	4	23	0	5	26
25	0	1	6	0	2	12	0	3	19	0	4	25	0	5	31
26	0	1	7	0	2	13	0	3	20	0	4	27	0	5	34
27	0	1	7	0	2	15	0	3	22	0	4	29	0	5	37
28	0	1	8	0	2	16	0	3	24	0	4	31	0	5	39
29	0	1	9	0	2	17	0	3	26	0	4	34	0	5	43
30	0	1	9	0	2	19	0	3	28	0	4	37	0	5	46
31	0	1	10	0	2	20	0	3	30	0	4	40	0	5	50
32	0	1	11	0	2	21	0	3	32	0	4	43	0	5	54
33	0	1	12	0	2	23	0	3	35	0	4	46	0	5	58
34	0	1	12	0	2	25	0	3	37	0	4	50	0	6	02

Parallel.	6 Miles.			7 Miles.			8 Miles.			9 Miles.		
	D.	M.	S.	D.	M.	S.	D.	M.	S.	D.	M.	S.
0	0	6	0	0	7	0	0	8	0	0	9	0
1	0	6	0	0	7	0	0	8	0	0	9	0
2	0	6	0	0	7	0	0	8	0	0	9	1
3	0	6	0	0	7	1	0	8	1	0	9	1
4	0	6	1	0	7	1	0	8	1	0	9	1
5	0	6	1	0	7	2	0	8	2	0	9	2
6	0	6	2	0	7	2	0	8	3	0	9	3
7	0	6	3	0	7	3	0	8	4	0	9	4
8	0	6	3	0	7	4	0	8	4	0	9	5
9	0	6	4	0	7	5	0	8	6	0	9	6
10	0	6	6	0	7	7	0	8	7	0	9	8
11	0	6	7	0	7	8	0	8	9	0	9	10
12	0	6	8	0	7	9	0	8	11	0	9	12
13	0	6	9	0	7	11	0	8	12	0	9	14
14	0	6	11	0	7	13	0	8	15	0	9	16
15	0	6	13	0	7	15	0	8	17	0	9	19
16	0	6	14	0	7	17	0	8	19	0	9	22
17	0	6	16	0	7	19	0	8	22	0	9	25
18	0	6	18	0	7	21	0	8	25	0	9	28
19	0	6	20	0	7	24	0	8	28	0	9	31
20	0	6	22	0	7	25	0	8	29	0	9	34
21	0	6	26	0	7	30	0	8	34	0	9	38
22	0	6	28	0	7	33	0	8	38	0	9	42
23	0	6	31	0	7	37	0	8	41	0	9	47
24	0	6	33	0	7	39	0	8	44	0	9	50
25	0	6	37	0	7	43	0	8	50	0	9	56
26	0	6	40	0	7	47	0	8	54	0	10	01
27	0	6	42	0	7	51	0	9	59	0	10	06
28	0	6	47	0	7	55	0	9	03	0	10	11
29	0	6	52	0	8	00	0	9	09	0	10	17
30	0	6	56	0	8	05	0	9	14	0	10	24
31	0	7	00	0	8	10	0	9	20	0	10	30
32	0	7	04	0	8	15	0	9	26	0	10	37
33	0	7	09	0	8	21	0	9	32	0	10	44
34	0	7	14	0	8	27	0	9	39	0	10	51



## A Table for reducing Miles of East

Parallel.	1 Mile.			2 Miles.			3 Miles.			4 Miles.			5 Miles.		
	D.	M.	S.	D.	M.	S.	D.	M.	S.	D.	M.	S.	D.	M.	S.
35	0	1	13	0	2	26	0	3	40	0	4	53	0	6	6
36	0	1	14	0	2	28	0	3	42	0	4	57	0	6	11
37	0	1	15	0	2	30	0	3	45	0	5	01	0	6	16
38	0	1	16	0	2	32	0	3	48	0	5	05	0	6	21
39	0	1	17	0	2	34	0	3	52	0	5	09	0	6	26
40	0	1	18	0	2	37	0	3	55	0	5	13	0	6	32
41	0	1	19	0	2	39	0	3	58	0	5	18	0	6	37
42	0	1	21	0	2	41	0	4	02	0	5	23	0	6	44
43	0	1	22	0	2	44	0	4	06	0	5	28	0	6	50
44	0	1	23	0	2	47	0	4	10	0	5	34	0	6	57
45	0	1	25	0	2	50	0	4	15	0	5	39	0	7	4
46	0	1	26	0	2	53	0	4	19	0	5	45	0	7	12
47	0	1	28	0	2	56	0	4	24	0	5	52	0	7	20
48	0	1	30	0	2	59	0	4	29	0	5	59	0	7	28
49	0	1	31	0	3	03	0	4	34	0	6	06	0	7	37
50	0	1	33	0	3	07	0	4	40	0	6	13	0	7	47
51	0	1	35	0	3	11	0	4	46	0	6	21	0	7	57
52	0	1	37	0	3	14	0	4	52	0	6	30	0	8	07
53	0	1	40	0	3	19	0	4	59	0	6	38	0	8	18
54	0	1	42	0	3	24	0	5	06	0	6	48	0	8	30
55	0	1	45	0	3	29	0	5	14	0	6	57	0	8	43
56	0	1	47	0	3	35	0	5	22	0	7	05	0	8	56
57	0	1	50	0	3	40	0	5	30	0	7	21	0	9	11
58	0	1	53	0	3	46	0	5	40	0	7	33	0	9	26
59	0	1	56	0	3	53	0	5	49	0	7	46	0	9	42
60	0	2	00	0	4	00	0	6	00	0	8	00	0	10	00
61	0	2	04	0	4	07	0	6	11	0	8	15	0	10	19
62	0	2	08	0	4	16	0	6	23	0	8	31	0	10	39
63	0	2	12	0	4	24	0	6	36	0	8	49	0	11	01
64	0	2	17	0	4	34	0	6	51	0	9	07	0	11	24
65	0	2	22	0	4	44	0	7	06	0	9	28	0	11	50
66	0	2	28	0	4	55	0	7	23	0	9	50	0	12	18
67	0	2	33	0	5	06	0	7	39	0	10	12	0	12	45
68	0	2	40	0	5	27	0	8	14	0	11	01	0	13	48
69	0	2	47	0	5	34	0	8	21	0	11	08	0	13	55
70	0	2	55	0	5	50	0	8	45	0	11	40	0	14	35

## and West into Degrees of Longitude.

Parallel.	6 Miles.			7 Miles.			8 Miles.			9 Miles.		
	D.	M.	S.	D.	M.	S.	D.	M.	S.	D.	M.	S.
35	0	7	19	0	8	33	0	9	46	0	10	59
36	0	7	25	0	8	39	0	9	53	0	11	08
37	0	7	31	0	8	46	0	10	01	0	11	16
38	0	7	37	0	8	53	0	10	09	0	11	25
39	0	7	43	0	9	00	0	10	18	0	11	35
40	0	7	50	0	9	08	0	10	27	0	11	45
41	0	7	57	0	9	16	0	10	36	0	11	55
42	0	8	04	0	9	25	0	10	46	0	12	07
43	0	8	12	0	9	34	0	10	56	0	12	20
44	0	8	21	0	9	44	0	11	07	0	12	31
45	0	8	29	0	9	55	0	11	19	0	12	44
46	0	8	38	0	10	05	0	11	31	0	12	57
47	0	8	48	0	10	16	0	11	44	0	13	12
48	0	8	58	0	10	28	0	11	57	0	13	27
49	0	9	08	0	10	40	0	11	12	0	13	43
50	0	9	20	0	10	53	0	12	27	0	14	00
51	0	9	22	0	10	57	0	12	33	0	14	08
52	0	9	44	0	11	22	0	13	00	0	14	37
53	0	9	58	0	11	38	0	13	18	0	14	57
54	0	10	12	0	11	55	0	13	36	0	15	19
55	0	10	28	0	12	12	0	13	57	0	15	41
56	0	10	44	0	12	31	0	14	18	0	16	06
57	0	11	01	0	12	51	0	14	41	0	16	31
58	0	11	19	0	13	13	0	15	06	0	16	59
59	0	11	39	0	13	35	0	15	32	0	17	28
60	0	12	00	0	14	00	0	16	00	0	18	00
61	0	12	22	0	14	26	0	16	30	0	18	33
62	0	12	47	0	14	55	0	17	02	0	19	10
63	0	13	13	0	15	25	0	17	37	0	19	49
64	0	13	41	0	15	58	0	18	15	0	20	32
65	0	14	12	0	16	34	0	18	55	0	21	18
66	0	14	45	0	17	12	0	19	40	0	22	08
67	0	15	18	0	17	51	0	20	24	0	22	57
68	0	16	25	0	19	22	0	22	09	0	23	56
69	0	16	42	0	19	29	0	22	16	0	25	03
70	0	17	30	0	20	25	0	23	20	0	26	13



Parallel.	10 Miles.			20 Miles.			30 Miles.			40 Miles.			50 Miles.		
	D.	M.	S.	D.	M.	S.	D.	M.	S.	D.	M.	S.	D.	M.	S.
0	0	10	0	0	20	0	0	30	0	0	40	0	0	50	0
1	0	10	0	0	20	0	0	30	0	0	40	0	0	50	0
2	0	10	1	0	20	1	0	30	1	0	40	1	0	50	1
3	0	10	1	0	20	2	0	30	2	0	40	3	0	50	4
4	0	10	1	0	20	3	0	30	4	0	40	6	0	50	7
5	0	10	2	0	20	5	0	30	7	0	40	9	0	50	11
6	0	10	3	0	20	6	0	30	9	0	40	13	0	50	16
7	0	10	4	0	20	9	0	30	13	0	40	18	0	50	22
8	0	10	6	0	20	1	0	30	17	0	40	23	0	50	28
9	0	10	7	0	20	5	0	30	22	0	40	30	0	50	37
10	0	10	9	0	20	18	0	30	28	0	40	37	0	50	46
11	0	10	11	0	20	22	0	30	34	0	40	45	0	50	56
12	0	10	13	0	20	27	0	30	40	0	40	53	0	51	06
13	0	10	16	0	20	32	0	30	47	0	41	03	0	51	19
14	0	10	18	0	20	37	0	30	55	0	41	13	0	51	31
15	0	10	21	0	20	42	0	31	03	0	41	24	0	51	46
16	0	10	24	0	20	49	0	31	13	0	41	37	0	52	01
17	0	10	27	0	20	55	0	31	21	0	41	49	0	52	16
18	0	10	31	0	21	02	0	31	33	0	42	04	0	52	34
19	0	10	34	0	21	09	0	31	44	0	42	18	0	52	53
20	0	10	38	0	21	17	0	31	55	0	42	34	0	53	12
21	0	10	43	0	21	25	0	32	08	0	42	51	0	53	33
22	0	10	47	0	21	34	0	32	21	0	43	09	0	53	56
23	0	10	52	0	21	44	0	32	35	0	43	27	0	54	19
24	0	10	57	0	21	54	0	32	50	0	43	47	0	54	44
25	0	11	02	0	22	04	0	33	06	0	44	08	0	55	10
26	0	11	07	0	22	15	0	33	22	0	44	30	0	55	37
27	0	11	13	0	22	27	0	33	40	0	44	53	0	56	07
28	0	11	19	0	22	37	0	33	56	0	45	16	0	56	35
29	0	11	26	0	22	52	0	34	18	0	45	44	0	57	10
30	0	11	33	0	23	06	0	34	38	0	46	11	0	57	44
31	0	11	40	0	23	19	0	34	58	0	46	38	0	58	18
32	0	11	47	0	23	35	0	35	22	0	47	10	0	58	57
33	0	11	55	0	23	50	0	35	46	0	47	41	0	59	37
34	0	12	04	0	24	08	0	36	11	0	48	15	1	00	19

Parallel.	60 Miles.			70 Miles.			80 Miles.			90 Miles.			100 Miles.		
	D.	M.	S.	D.	M.	S.	D.	M.	S.	D.	M.	S.	D.	M.	S.
0	1	0	0	1	10	00	1	20	00	1	30	00	1	40	00
1	1	0	1	1	10	01	1	20	01	1	30	00	1	40	01
2	1	0	2	1	10	03	1	20	03	1	30	03	1	40	04
3	1	0	5	1	10	06	1	20	07	1	30	07	1	40	08
4	1	0	9	1	10	10	1	20	12	1	30	13	1	40	14
5	1	0	14	1	10	16	1	20	18	1	30	21	1	40	23
6	1	0	19	1	10	21	1	20	24	1	30	27	1	40	31
7	1	0	27	1	10	31	1	20	35	1	30	39	1	40	45
8	1	0	34	1	10	40	1	20	46	1	30	52	1	40	59
9	1	0	45	1	10	52	1	20	59	1	31	07	1	41	15
10	1	0	55	1	11	05	1	21	14	1	31	23	1	41	34
11	1	1	07	1	11	19	1	21	30	1	31	41	1	41	52
12	1	1	20	1	11	33	1	21	46	1	31	60	1	42	13
13	1	1	35	1	11	50	1	22	06	1	32	22	1	42	38
14	1	1	50	1	12	09	1	22	27	1	32	45	1	43	04
15	1	2	07	1	12	28	1	22	49	1	33	10	1	43	32
16	1	2	26	1	12	50	1	23	14	1	33	39	1	44	03
17	1	2	43	1	13	11	1	23	38	1	34	06	1	44	34
18	1	3	05	1	13	36	1	24	07	1	34	38	1	45	08
19	1	3	27	1	14	01	1	24	37	1	35	11	1	45	46
20	1	3	51	1	14	29	1	25	08	1	35	46	1	46	20
21	1	4	16	1	14	59	1	25	41	1	36	24	1	47	06
22	1	4	43	1	15	30	1	26	17	1	37	04	1	47	52
23	1	5	11	1	16	03	1	26	55	1	37	46	1	48	38
24	1	5	41	1	16	37	1	27	34	1	38	31	1	49	27
25	1	6	12	1	17	14	1	28	18	1	39	20	1	50	22
26	1	6	44	1	17	51	1	28	58	1	40	05	1	51	13
27	1	7	20	1	18	33	1	29	47	1	41	00	1	52	13
28	1	7	55	1	19	14	1	30	34	1	41	53	1	53	15
29	1	8	36	1	20	02	1	31	28	1	42	54	1	54	20
30	1	9	17	1	20	49	1	32	23	1	44	55	1	55	28
31	1	9	58	1	21	37	1	33	18	1	44	57	1	56	38
32	1	10	45	1	22	32	1	34	20	1	46	07	1	57	55
33	1	11	42	1	23	37	1	35	33	1	47	28	1	59	13
34	1	12	23	1	24	26	1	36	31	1	48	34	2	00	38



Parallel.	10 Miles.	20 Miles.	30 Miles.	40 Miles.	50 Miles.
	D. M. S.	D. M. S.	D. M. S.	D. M. S.	D. M. S.
35	0 12 12	0 24 25	0 36 37	0 48 50	1 1 02
36	0 12 22	0 24 43	0 37 05	0 49 27	1 1 48
37	0 12 31	0 25 03	0 37 34	0 50 05	1 2 37
38	0 12 41	0 25 23	0 38 04	0 50 45	1 3 27
39	0 12 52	0 25 44	0 38 36	0 51 28	1 4 20
40	0 13 03	0 26 06	0 39 09	0 52 13	1 5 16
41	0 13 15	0 26 30	0 39 45	0 53 00	1 6 15
42	0 13 27	0 26 55	0 40 22	0 53 49	1 7 17
43	0 13 42	0 27 25	0 41 17	0 54 49	1 8 32
44	0 13 54	0 27 48	0 41 42	0 55 37	1 9 30
45	0 14 08	0 28 16	0 42 24	0 56 33	1 10 41
46	0 14 24	0 28 47	0 43 11	0 57 39	1 11 58
47	0 14 40	0 29 20	0 43 59	0 58 34	1 13 19
48	0 14 57	0 29 53	0 44 50	0 59 47	1 14 43
49	0 15 14	0 30 29	0 45 33	1 0 57	1 16 11
50	0 15 33	0 31 07	0 46 40	1 2 14	1 17 47
51	0 15 53	0 31 47	0 47 40	1 3 33	1 19 27
52	0 16 14	0 32 29	0 48 43	1 4 58	1 21 12
53	0 16 37	0 33 14	0 49 51	1 6 28	1 23 05
54	0 17 01	0 34 02	0 51 02	1 8 03	1 25 04
55	0 17 26	0 34 52	0 52 18	1 9 48	1 27 10
56	0 17 53	0 35 46	0 53 39	1 11 32	1 29 25
57	0 18 21	0 36 43	0 55 05	1 13 27	1 31 48
58	0 18 52	0 37 44	0 56 36	1 15 29	1 34 21
59	0 19 24	0 38 50	0 58 14	1 17 39	1 37 04
60	0 20 00	0 40 00	1 0 00	1 20 00	1 40 00
61	0 20 37	0 41 15	1 1 52	1 22 30	1 43 07
62	0 21 18	0 42 36	1 3 54	1 25 12	1 46 30
63	0 22 12	0 44 03	1 6 05	1 28 07	1 50 08
64	0 22 48	0 45 37	1 8 16	1 31 15	1 54 03
65	0 23 40	0 47 09	1 10 49	1 34 29	1 58 08
66	0 24 35	0 49 10	1 13 45	1 38 21	2 02 56
67	0 25 35	0 51 10	1 16 45	1 42 20	2 07 55
68	0 26 42	0 53 24	1 20 06	1 46 48	2 13 30
69	0 27 54	0 55 45	1 23 42	1 51 36	2 19 30
70	0 29 14	0 59 28	1 27 42	1 56 56	2 26 10

Parallel.	60 Miles.	70 Miles.	80 Miles.	90 Miles.	100 Miles.
	D. M. S.	D. M. S.	D. M. S.	D. M. S.	D. M. S.
35	1 13 14	1 25 26	1 37 38	1 49 50	2 2 05
36	1 14 10	1 26 32	1 38 53	1 51 15	2 3 36
37	1 13 08	1 27 39	1 40 11	1 52 41	2 5 13
38	1 16 08	1 28 49	1 41 31	1 54 12	2 6 53
39	1 17 12	1 30 04	1 42 56	1 55 48	2 8 40
40	1 18 19	1 31 22	1 44 25	1 57 28	2 10 32
41	1 19 30	1 32 45	1 46 00	1 59 15	2 12 30
42	1 20 44	1 34 11	1 47 38	2 01 06	2 14 33
43	1 22 14	1 35 56	1 49 39	2 03 21	2 17 03
44	1 23 25	1 37 19	1 51 13	2 05 07	2 19 02
45	1 24 50	1 38 58	1 53 07	2 07 19	2 21 25
46	1 26 22	1 40 45	1 55 09	2 10 32	2 23 55
47	1 27 59	1 42 38	1 57 18	2 11 58	2 26 38
48	1 29 40	1 44 36	1 59 33	2 14 30	2 29 27
49	1 31 26	1 46 40	2 01 54	2 17 08	2 32 25
50	1 33 21	1 48 54	2 04 28	2 20 01	2 35 35
51	1 35 20	1 51 13	2 07 07	2 23 00	2 38 53
52	1 37 27	1 53 41	2 09 55	2 26 09	2 42 20
53	1 39 42	1 56 19	2 12 56	2 29 33	2 46 15
54	1 42 05	1 59 06	2 16 07	2 33 07	2 50 08
55	1 44 36	2 02 02	2 19 28	2 36 54	2 54 20
56	1 47 18	2 05 11	2 23 04	2 41 57	2 58 50
57	1 50 10	2 08 32	2 26 53	2 45 15	3 03 36
58	1 53 13	2 12 05	2 30 57	2 49 49	3 08 43
59	1 56 29	2 15 54	2 35 19	2 54 43	3 14 08
60	2 00 00	2 20 00	2 40 00	3 00 00	3 20 00
61	2 03 45	2 24 22	2 45 40	3 05 37	3 26 15
62	2 07 48	2 29 06	2 50 24	3 11 42	3 33 00
63	2 12 10	2 34 12	2 56 13	3 18 15	3 40 16
64	2 16 52	2 39 41	3 02 29	3 25 18	3 48 06
65	2 21 47	2 45 27	3 09 06	3 32 46	3 56 37
66	2 27 21	2 51 56	3 16 31	3 41 07	4 05 41
67	2 33 30	2 59 05	3 24 40	3 50 15	4 15 50
68	2 40 12	2 06 54	3 33 36	4 00 18	4 27 00
69	2 47 14	2 15 18	3 43 12	4 11 16	4 39 30
70	2 55 24	2 24 38	3 53 52	4 23 06	4 52 20



Parallel.	200 Miles.	300 Miles.	400 Miles.	500 Miles.	600 Miles.
	D. M. S.	D. M. S.	D. M. S.	D. M. S.	D. M. S.
0	3 20 00	5 0 00	6 40 00	8 20 00	10 0 00
1	3 20 02	5 0 03	6 40 04	8 20 04	10 0 05
2	3 20 07	5 0 11	6 40 14	8 20 13	10 0 22
3	3 20 17	5 0 25	6 40 33	8 20 45	10 0 53
4	3 20 29	5 0 44	6 40 59	8 20 13	10 1 27
5	3 20 46	5 1 09	6 41 32	8 21 55	10 2 18
6	3 21 03	5 1 35	6 42 07	8 22 39	10 3 11
7	3 21 30	5 2 15	6 43 00	8 23 45	10 4 30
8	3 21 58	5 2 57	6 43 56	8 24 55	10 5 54
9	3 22 29	5 3 44	6 44 59	8 26 14	10 7 29
10	3 23 06	5 4 39	6 46 12	8 27 45	10 9 18
11	3 23 44	5 5 36	6 47 28	8 29 20	10 11 12
12	3 24 26	5 6 49	6 49 02	8 31 15	10 13 28
13	3 25 16	5 7 54	6 50 32	8 33 10	10 15 48
14	3 26 08	5 9 12	6 52 16	8 35 20	10 18 24
15	3 27 04	5 10 36	6 54 08	8 37 40	10 21 12
16	3 28 06	5 12 09	6 56 12	8 40 15	10 24 18
17	3 29 08	5 13 42	6 58 26	8 43 00	10 27 34
18	3 30 18	5 15 27	7 00 36	8 45 45	10 30 56
19	3 31 32	5 17 18	7 03 04	8 48 50	10 34 36
20	3 32 40	5 19 00	7 05 20	8 51 40	10 38 00
21	3 34 12	5 21 18	7 08 24	8 55 30	10 42 36
22	3 35 44	5 23 36	7 11 28	8 59 20	10 47 12
23	3 37 16	5 27 54	7 16 32	9 05 10	10 53 48
24	3 38 54	5 28 21	7 19 48	9 07 15	10 56 42
25	3 40 44	5 31 06	7 21 28	9 11 50	11 02 12
26	3 42 26	5 33 39	7 24 52	9 16 05	11 07 18
27	3 44 26	5 36 39	7 28 52	9 21 05	11 13 18
28	3 46 30	5 39 45	7 33 00	9 26 15	11 19 30
29	3 48 40	5 43 00	7 37 20	9 31 40	11 26 00
30	3 50 56	5 46 24	7 41 52	9 37 20	11 32 48
31	3 53 16	5 49 54	7 45 32	9 42 10	11 38 48
32	3 55 50	5 53 45	7 51 40	9 49 35	11 47 20
33	3 58 26	5 57 39	7 56 52	9 56 05	11 55 18
34	4 01 16	6 01 54	8 02 32	10 03 10	12 03 48

Parallel.	700 Miles.	800 Miles.	900 Miles.	1000 Miles.
	D. M. S.	D. M. S.	D. M. S.	D. M. S.
0	11 40 00	13 20 00	15 0 00	16 40 00
1	11 40 06	13 20 07	15 0 09	16 40 10
2	11 40 26	13 20 30	15 0 34	16 40 38
3	11 41 00	13 21 08	15 1 17	16 41 25
4	11 41 41	13 21 55	15 2 19	16 42 23
5	11 42 41	13 23 04	15 3 27	16 43 48
6	11 43 43	13 24 15	15 4 47	16 45 18
7	11 45 15	13 26 00	15 6 45	16 47 30
8	11 46 53	13 27 52	15 8 51	16 49 50
9	11 48 44	13 29 59	15 11 14	16 52 27
10	11 50 51	13 32 24	15 13 57	16 55 37
11	11 53 04	13 34 56	15 16 48	16 58 42
12	11 55 41	13 37 54	15 20 07	17 02 10
13	11 57 26	13 40 04	15 22 42	17 04 18
14	12 01 28	13 44 32	15 27 36	17 10 36
15	12 04 44	13 48 16	15 31 48	17 15 17
16	12 08 21	13 52 24	15 36 27	17 20 31
17	12 12 08	13 56 42	15 41 16	17 25 41
18	12 16 05	14 01 14	15 46 23	17 31 27
19	12 20 22	14 06 08	15 51 05	17 37 37
20	12 24 20	14 10 40	15 57 00	17 43 20
21	12 29 42	14 16 48	16 03 54	17 50 00
22	12 35 04	14 22 56	16 10 48	17 58 31
23	12 42 26	14 31 04	16 19 42	18 08 20
24	12 46 09	14 35 36	16 25 30	18 14 30
25	12 52 34	14 42 56	16 33 18	18 23 40
26	12 58 38	14 49 44	16 40 57	18 32 10
27	13 05 31	14 57 44	16 49 57	18 42 13
28	13 12 45	15 06 00	16 59 15	18 53 30
29	13 20 20	15 14 40	17 09 00	19 03 20
30	13 28 16	15 23 44	17 19 12	19 14 43
31	13 35 26	15 32 04	17 29 42	19 26 23
32	13 45 15	15 43 10	17 41 05	19 39 10
33	13 54 31	15 53 44	17 52 57	19 50 13
34	14 04 26	16 05 04	18 05 42	20 06 23



## A Table for reducing Miles of East

Parallel.	200 Miles.			300 Miles.			400 Miles.			500 Miles.			600 Miles.		
	D.	M.	S.	D.	M.	S.	D.	M.	S.	D.	M.	S.	D.	M.	S.
35	4	04	10	6	06	15	8	08	20	10	10	25	12	12	30
36	4	07	14	6	10	51	8	14	28	10	13	05	12	21	42
37	4	10	26	6	13	39	8	20	52	10	26	05	12	31	18
38	4	13	40	6	20	39	8	27	32	10	34	25	12	41	18
39	4	17	20	6	26	00	8	34	40	10	43	20	12	52	00
40	4	21	4	6	31	36	8	42	05	10	52	40	13	03	12
41	4	25	0	6	37	30	8	50	00	11	02	30	13	15	00
42	4	29	8	6	43	42	8	53	16	11	12	50	13	27	24
43	4	34	6	6	51	09	9	03	12	11	25	15	13	42	18
44	4	38	4	6	57	06	9	16	03	11	35	10	13	54	12
45	4	42	50	7	04	15	9	25	40	11	47	05	14	08	30
46	4	47	52	7	11	43	9	35	44	11	59	40	14	23	36
47	4	53	16	7	19	54	9	46	32	12	13	10	14	39	48
48	4	58	54	7	28	21	9	57	48	12	27	15	14	56	42
49	5	04	50	7	37	15	10	09	40	12	42	05	14	14	30
50	5	11	10	7	46	45	10	22	20	12	57	55	15	33	20
51	5	17	46	7	56	39	10	31	22	13	14	15	15	53	08
52	5	24	50	8	07	15	10	49	40	13	32	05	16	14	30
53	5	32	20	8	18	30	11	04	40	13	50	50	16	37	00
54	5	40	16	8	30	24	11	20	22	14	10	40	17	00	43
55	5	48	40	8	43	30	11	37	20	14	31	55	17	26	00
56	5	57	40	8	56	30	11	55	20	14	54	15	17	53	00
57	6	07	14	9	10	91	12	14	28	15	18	05	18	21	42
58	6	17	26	9	26	09	12	34	52	15	43	35	18	52	18
59	6	28	16	9	42	25	12	56	33	16	10	40	19	24	50
60	6	40	00	10	00	00	13	20	00	16	40	00	20	00	00
61	6	52	30	10	18	45	13	45	00	17	11	15	20	37	30
62	7	06	00	10	39	00	14	12	00	17	45	00	21	18	00
63	7	20	32	11	00	48	14	41	04	18	21	20	22	01	36
64	7	36	12	11	24	18	15	12	24	19	00	30	22	48	36
65	7	53	13	11	49	41	15	46	24	19	43	00	23	39	36
66	8	11	22	12	17	03	16	22	44	20	28	25	24	34	06
67	8	31	40	12	47	30	17	03	20	21	19	10	25	35	00
68	8	54	00	13	21	00	17	48	00	22	15	00	26	42	00
69	9	18	00	13	57	00	18	36	00	23	15	00	27	54	00
70	9	44	40	14	37	00	19	29	20	24	21	00	29	14	00

and West into Degrees of Longitude.

Parallel.	700 Miles.			800 Miles.			900 Miles.			1000 Miles.		
	D.	M.	S.	D.	M.	S.	D.	M.	S.	D.	M.	S.
35	14	14	35	16	16	40	18	18	45	20	20	50
36	14	25	19	16	28	56	18	32	33	20	36	10
37	14	36	31	16	41	44	18	46	57	20	53	51
38	14	48	11	16	55	04	19	01	57	21	01	30
39	15	00	40	17	09	20	19	08	00	21	26	40
40	15	13	44	17	24	16	19	34	48	21	45	26
41	15	27	30	17	40	00	19	52	30	22	05	00
42	15	41	58	17	56	22	20	10	56	22	25	30
43	15	59	21	18	16	24	20	33	27	22	50	13
44	16	13	14	18	32	16	20	51	11	23	10	20
45	16	29	55	18	51	20	21	12	45	23	34	10
46	16	47	32	19	11	23	21	35	24	23	59	10
47	17	06	26	19	33	04	21	59	42	24	26	10
48	17	26	09	19	55	36	22	25	03	24	54	26
49	17	46	55	20	19	20	22	51	45	25	24	10
50	18	08	55	20	44	30	23	20	05	25	55	50
51	18	32	01	21	10	54	23	47	47	26	28	53
52	18	57	15	21	39	30	24	21	55	27	04	20
53	19	23	10	22	09	20	24	55	30	27	41	40
54	19	50	56	22	41	04	25	31	12	28	21	20
55	20	20	20	23	14	40	26	09	00	29	03	20
56	20	51	50	23	50	40	26	49	30	29	48	20
57	21	25	19	24	28	56	27	32	23	30	36	00
58	22	01	01	25	09	44	28	18	27	31	27	10
59	22	38	58	25	53	06	29	07	15	32	21	23
60	23	20	00	26	40	00	30	00	00	33	20	00
61	24	03	45	27	30	00	30	56	15	34	22	30
62	24	51	00	28	24	00	31	57	00	35	30	00
63	25	41	52	29	29	08	33	02	24	36	42	40
64	26	36	42	30	24	48	34	12	54	38	06	00
65	27	36	12	31	32	58	35	29	24	39	26	00
66	28	39	47	32	45	23	36	51	09	40	56	50
67	29	50	50	34	06	40	38	22	30	42	38	20
68	31	09	00	35	36	00	40	03	00	44	30	00
69	32	33	00	37	12	00	41	51	00	46	30	00
70	34	06	24	38	57	40	43	51	00	48	43	20



# LOXODROMIQUES, or MILES, with the Difference of

Latitude	1 Rumb, 11° 15'		2 Rumb, 22° 30'		3 Rumb, 33° 45'		4 Rumb, 45° 00'	
	Longitude	Dift. in Miles.	Longitude	Dift. in Miles.	Longitude	Dift. in Miles.	Longitude	Dift. in Miles.
D. M.	D. M.		D. M.		D. M.		D. M.	
0 0	0 0	0	0 0	0	0 0	0	0 0	0
0 10	0 2	10	0 4	11	0 7	12	0 10	14
0 20	0 4	20	0 8	22	0 13	25	0 20	28
0 30	0 6	31	0 12	32	0 20	36	0 30	42
0 40	0 8	41	0 16	43	0 27	48	0 40	57
0 50	0 10	51	0 20	54	0 33	60	0 50	71
1 0	0 12	61	0 24	65	0 40	72	1 0	85
1 10	0 14	71	0 29	76	0 47	84	1 10	99
1 20	0 16	82	0 33	87	0 53	96	1 20	113
1 30	0 18	92	0 37	99	1 00	100	1 30	127
1 40	0 20	102	0 41	108	1 07	110	1 40	141
1 50	0 22	112	0 45	119	1 13	122	1 50	156
2 0	0 24	122	0 49	130	1 20	144	2 0	170
2 10	0 26	133	0 53	141	1 27	156	2 10	184
2 20	0 28	143	0 57	152	1 33	168	2 20	198
2 30	0 30	153	1 02	162	1 40	180	2 30	212
2 40	0 32	163	1 06	173	1 47	192	2 40	226
2 50	0 34	173	1 10	184	1 53	204	2 50	240
3 0	0 36	184	1 15	194	2 00	216	3 0	255
3 10	0 38	194	1 19	206	2 07	229	3 10	269
3 20	0 40	204	1 23	216	2 13	241	3 20	283
3 30	0 42	214	1 27	227	2 20	253	3 30	297
3 40	0 44	224	1 32	238	2 27	265	3 40	311
3 50	0 46	234	1 36	249	2 33	277	3 50	325
4 0	0 48	245	1 39	260	2 40	289	4 0	339
4 10	0 50	255	1 44	271	2 47	301	4 10	354
4 20	0 52	265	1 48	281	2 54	313	4 20	368
4 30	0 54	275	1 52	292	3 01	325	4 30	382
4 40	0 56	285	1 56	303	3 07	337	4 40	396
4 50	0 58	295	2 00	314	3 14	349	4 50	410
5 0	1 0	306	2 04	325	3 20	361	5 0	424
5 10	1 2	316	2 08	336	3 27	373	5 10	438
5 20	1 4	326	2 12	346	3 34	385	5 20	453
5 30	1 6	336	2 16	357	3 40	397	5 30	467
5 40	1 8	347	2 20	368	3 47	409	5 40	481
5 50	1 10	357	2 24	378	3 54	421	5 50	495

# TRAVERSE-TABLES of Longitudes and Latitudes.

Latitude	5 Rumb, 56° 15'		6 Rumb, 67° 30'		7 Rumb, 78° 45'	
	Longitude	Dift. in Miles.	Longitude	Dift. in Miles.	Longitude	Dift. in Miles.
D. M.	D. M.		D. M.		D. M.	
0 0	0 0	0	0 0	0	0 0	0
0 10	0 15	18	0 24	26	0 51	51
0 20	0 30	36	0 48	52	1 33	103
0 30	0 45	54	1 12	78	2 29	154
0 40	1 00	72	1 36	105	3 20	205
0 50	1 15	90	2 00	131	4 11	256
1 0	1 30	108	2 24	157	5 02	308
1 10	1 45	126	2 49	183	5 53	359
1 20	2 00	144	3 12	209	6 44	410
1 30	2 15	162	3 38	235	7 35	461
1 40	2 30	180	4 02	261	8 22	513
1 50	2 45	198	4 26	287	9 13	564
2 0	3 00	216	4 50	314	10 04	615
2 10	3 15	234	5 14	340	10 55	666
2 20	3 30	252	5 38	366	11 42	718
2 30	3 45	270	6 02	392	12 33	769
2 40	4 00	288	6 25	418	13 24	820
2 50	4 15	309	6 50	444	14 16	871
3 0	4 30	324	7 14	470	15 07	923
3 10	4 45	342	7 38	496	15 54	974
3 20	5 00	360	8 02	523	16 49	1025
3 30	5 15	378	8 26	549	17 36	1076
3 40	5 30	396	8 52	575	18 27	1128
3 50	5 45	414	9 15	601	19 18	1179
4 0	6 00	432	9 39	627	20 09	1230
4 10	6 15	450	10 04	653	21 00	1281
4 20	6 30	468	10 29	679	21 48	1333
4 30	6 45	486	10 53	706	22 39	1384
4 40	7 00	504	11 17	732	23 30	1435
4 50	7 15	522	11 40	758	24 21	1487
5 0	7 30	540	12 05	784	25 08	1538
5 10	7 45	558	12 29	810	26 03	1589
5 20	8 00	576	12 53	836	26 51	1640
5 30	8 15	594	13 17	862	27 42	1692
5 40	8 30	612	13 42	888	28 33	1743
5 50	8 45	630	14 06	915	29 24	1794



Latitude		1 Rumb, 11° 15'.		2 Rumb, 22° 30'.		3 Rumb, 33° 45'.		4 Rumb, 45° 00'.	
Longitude		Diff. in Miles.		Longitude		Diff. in Miles.		Longitude	
D. M.	D. M.	D. M.	D. M.	D. M.	D. M.	D. M.	D. M.	D. M.	D. M.
6 0	1 12	367	2 28	390	4 01	433	6 0	509	
6 10	1 14	377	2 33	401	4 07	441	6 10	523	
6 20	1 16	387	2 37	411	4 14	451	6 20	537	
6 30	1 18	398	2 41	422	4 21	469	6 30	552	
6 40	1 20	408	2 45	433	4 27	481	6 40	566	
6 50	1 22	418	2 50	443	4 34	493	6 50	580	
7 0	1 24	428	2 54	453	4 41	505	7 0	594	
7 10	1 26	438	2 58	463	4 47	517	7 10	608	
7 20	1 28	449	3 02	476	4 54	529	7 20	622	
7 30	1 30	459	3 06	487	5 01	541	7 30	636	
7 40	1 32	469	3 11	498	5 08	553	7 40	651	
7 50	1 34	479	3 15	509	5 14	565	7 50	665	
8 0	1 36	490	3 19	520	5 21	577	8 0	679	
8 10	1 38	500	3 24	530	5 28	589	8 10	693	
8 20	1 40	510	3 28	541	5 35	601	8 20	707	
8 30	1 42	520	3 32	552	5 41	613	8 30	721	
8 40	1 44	530	3 36	563	5 48	625	8 40	735	
8 50	1 46	540	3 40	574	5 55	637	8 50	749	
9 0	1 48	553	3 44	584	6 02	649	9 0	764	
9 10	1 50	561	3 49	595	6 08	661	9 10	778	
9 20	1 52	571	3 53	606	6 15	673	9 20	792	
9 30	1 54	581	3 57	617	6 22	686	9 30	805	
9 40	1 56	591	4 01	628	6 29	698	9 40	820	
9 50	1 58	602	4 05	638	6 35	709	9 50	834	
10 0	2 0	612	4 10	649	6 42	722	10 0	849	
10 10	2 2	622	4 14	660	6 49	734	10 10	863	
10 20	2 4	632	4 18	671	6 56	746	10 20	877	
10 30	2 6	642	4 22	682	7 01	758	10 30	891	
10 40	2 8	653	4 26	693	7 09	770	10 40	905	
10 50	2 10	663	4 30	704	7 16	782	10 50	919	
11 0	2 12	673	4 34	714	7 23	794	11 0	933	
11 10	2 14	683	4 38	725	7 30	806	11 10	948	
11 20	2 16	693	4 42	732	7 36	818	11 20	966	
11 30	2 18	704	4 48	747	7 44	830	11 30	980	
11 40	2 20	714	4 54	758	7 51	842	11 40	994	
11 50	2 22	724	4 50	768	7 58	854			

Latitude		5 Rumb, 56° 15'.		6 Rumb, 67° 30'.		7 Rumb, 78° 45'.	
Longitude		Diff. in Miles.		Longitude		Diff. in Miles.	
D. M.	D. M.	D. M.	D. M.	D. M.	D. M.	D. M.	D. M.
6 0	9 0	648	14 30	941	30 14	1845	
6 10	9 15	666	14 55	969	31 03	1897	
6 20	9 30	684	15 19	993	31 54	1948	
6 30	9 45	702	15 44	1019	32 46	1999	
6 40	10 00	720	16 08	1045	33 37	2050	
6 50	10 15	738	16 33	1071	34 25	2102	
7 0	10 30	756	16 57	1098	35 18	2153	
7 10	10 45	774	17 21	1124	36 07	2204	
7 20	11 00	792	17 45	1150	37 00	2255	
7 30	11 16	810	18 10	1176	38 00	2307	
7 40	11 32	828	18 34	1202	38 42	2368	
7 50	11 46	846	18 58	1228	39 29	2409	
8 0	12 01	864	19 22	1254	40 21	2460	
8 10	12 16	882	19 47	1280	40 12	2512	
8 20	12 31	900	20 11	1307	42 04	2563	
8 30	12 47	918	20 35	1333	42 51	2614	
8 40	13 02	936	21 00	1359	43 43	2665	
8 50	13 17	954	21 24	1385	44 34	2717	
9 0	13 32	972	21 50	1411	45 26	2768	
9 10	13 47	990	22 14	1437	46 18	2819	
9 20	14 02	1008	22 39	1463	47 09	2870	
9 30	14 16	1026	23 03	1489	47 57	2922	
9 40	14 32	1044	23 27	1516	48 40	2973	
9 50	14 48	1062	23 52	1542	49 41	3024	
10 0	15 03	1080	24 16	1568	50 32	3075	
10 10	15 17	1098	24 41	1594	51 24	3127	
10 20	15 33	1116	25 05	1620	52 16	3178	
10 30	15 47	1134	25 30	1646	52 04	3229	
10 40	16 03	1152	25 54	1662	53 56	3271	
10 50	16 18	1170	26 18	1689	54 48	3322	
11 0	16 34	1188	26 43	1725	55 36	3373	
11 10	16 49	1207	27 08	1751	56 23	3424	
11 20	17 05	1224	27 32	1777	57 20	3476	
11 30	17 19	1242	27 58	1803	58 12	3527	
11 40	17 35	1260	28 22	1829	59 41	3578	
11 50	17 50	1278	28 47	1855	60 56	3636	



1 Rumb, 11° 15'			2 Rumb, 22° 30'			3 Rumb, 33° 45'			4 Rumb, 45° 00'		
Longitude.		Dift. in Miles.	Longitude.		Dift. in Miles.	Longitude.		Dift. in Miles.	Longitude.		Dift. in Miles.
D. M.	D. M.		D. M.	D. M.		D. M.	D. M.		D. M.	D. M.	
12 0	2 24	734	5 2	779	8 4	866	12 5	1018	12 0	13 05	1296
12 10	2 26	744	5 5	791	8 11	873	12 15	1032	12 10	13 20	1314
12 20	2 28	755	5 9	801	8 18	890	12 26	1047	12 20	13 36	1332
12 30	2 30	765	5 13	812	8 25	902	12 35	1061	12 30	13 51	1350
12 40	2 32	775	5 17	823	8 32	914	12 46	1075	12 40	19 07	1368
12 50	2 34	785	5 21	833	8 39	926	12 56	1089	12 50	19 22	1386
13 0	2 36	795	5 26	844	8 46	938	13 6	1103	13 0	19 38	1404
13 10	2 38	805	5 30	855	8 53	950	13 17	1117	13 10	19 52	1422
13 20	2 40	816	5 34	866	8 59	962	13 28	1131	13 20	20 08	1440
13 30	2 43	826	5 38	877	9 06	974	13 38	1146	13 30	20 34	1458
13 40	2 45	836	5 43	887	9 14	986	13 48	1160	13 40	20 30	1476
13 50	2 47	846	5 47	898	9 21	998	13 58	1174	13 50	20 54	1494
14 0	2 49	856	5 51	909	9 28	1010	14 8	1188	14 0	21 10	1512
14 10	2 51	867	5 55	920	9 34	1022	14 18	1202	14 10	21 25	1530
14 20	2 53	877	6 00	931	9 41	1034	14 28	1216	14 20	21 40	1548
14 30	2 55	887	6 04	942	9 47	1046	14 38	1230	14 30	21 55	1566
14 40	2 57	897	6 08	952	9 54	1058	14 48	1244	14 40	22 11	1584
14 50	2 59	907	6 13	963	10 01	1070	14 58	1259	14 50	22 26	1592
15 0	3 1	918	6 17	974	10 08	1082	15 10	1272	15 0	22 43	1621
15 10	3 3	928	6 21	985	10 15	1094	15 21	1281	15 10	22 57	1638
15 20	3 6	938	6 26	996	10 22	1106	15 31	1301	15 20	23 14	1656
15 30	3 8	948	6 30	1007	10 30	1118	15 41	1315	15 30	23 28	1674
15 40	3 10	958	6 34	1017	10 37	1131	15 51	1329	15 40	23 44	1692
15 50	3 12	968	6 39	1028	10 44	1143	16 1	1343	15 50	24 04	1710
16 0	3 14	979	6 43	1039	10 50	1155	16 12	1358	16 0	24 16	1728
16 10	3 16	989	6 47	1050	10 56	1167	16 23	1372	16 10	24 31	1746
16 20	3 18	999	6 51	1061	11 03	1179	16 33	1386	16 20	24 47	1764
16 30	3 20	1009	6 55	1072	11 10	1191	16 44	1400	16 30	25 02	1782
16 40	3 22	1020	6 59	1082	11 17	1203	16 55	1414	16 40	25 18	1800
16 50	3 24	1030	7 04	1093	11 24	1215	17 5	1428	16 50	25 34	1818
17 0	3 26	1040	7 09	1104	11 31	1227	17 15	1442	17 0	25 49	1836
17 10	3 28	1050	7 13	1115	11 39	1239	17 25	1457	17 10	26 05	1854
17 20	3 30	1060	7 17	1126	11 46	1251	17 36	1471	17 20	26 21	1872
17 30	3 32	1070	7 21	1136	11 53	1263	17 47	1485	17 30	26 36	1890
17 40	3 34	1081	7 26	1147	12 00	1275	17 57	1499	17 40	26 52	1908
17 50	3 36	1091	7 30	1158	12 07	1287	18 8	1513	17 50	27 08	1926

5 Rumb, 56° 15'			6 Rumb, 67° 30'			7 Rumb, 78° 45'		
Longitude.		Dift. in Miles.	Longitude.		Dift. in Miles.	Longitude.		Dift. in Miles.
D. M.	D. M.		D. M.	D. M.		D. M.	D. M.	
12 0	13 05	1296	29 12	1881	60 48	3691		
12 10	13 20	1314	29 36	1908	61 36	3742		
12 20	13 36	1332	30 00	1934	62 28	3793		
12 30	13 51	1350	30 25	1960	63 20	3844		
12 40	19 07	1368	30 50	1986	64 12	3896		
12 50	19 22	1386	31 15	2012	65 05	3947		
13 0	19 38	1404	31 39	2038	65 55	3998		
13 10	19 52	1422	32 04	2064	66 46	4049		
13 20	20 08	1440	32 29	2090	67 38	4101		
13 30	20 34	1458	32 53	2117	68 30	4152		
13 40	20 30	1476	33 18	2143	69 23	4203		
13 50	20 54	1494	33 43	2169	70 15	4252		
14 0	21 10	1512	34 10	2195	71 08	4306		
14 10	21 25	1530	34 34	2221	71 57	4357		
14 20	21 40	1548	34 59	2247	72 49	4408		
14 30	21 55	1566	35 24	2273	73 42	4459		
14 40	22 11	1584	35 49	2300	74 34	4511		
14 50	22 26	1592	36 13	2326	75 28	4562		
15 0	22 43	1621	36 38	2352	76 16	4613		
15 10	22 57	1638	37 03	2378	77 09	4664		
15 20	23 14	1656	37 28	2404	78 02	4716		
15 30	23 28	1674	37 52	2430	78 55	4767		
15 40	23 44	1692	38 18	2456	79 47	4818		
15 50	24 04	1710	38 42	2482	80 38	4870		
16 0	24 16	1728	39 08	2509	81 29	4921		
16 10	24 31	1746	39 35	2535	82 28	4972		
16 20	24 47	1764	39 58	2561	83 16	5023		
16 30	25 02	1782	40 25	2587	84 09	5075		
16 40	25 18	1800	40 50	2613	84 58	5126		
16 50	25 34	1818	41 15	2639	85 55	5177		
17 0	25 49	1836	41 40	2665	86 44	5228		
17 10	26 05	1854	42 05	2691	87 33	5280		
17 20	26 21	1872	42 30	2718	88 31	5331		
17 30	26 36	1890	42 56	2744	89 25	5382		
17 40	26 52	1908	43 21	2770	90 18	5433		
17 50	27 08	1926	43 46	2796	91 07	5484		



1 Rumb, 11° 15'			2 Rumb, 22° 30'			3 Rumb, 33° 45'			4 Rumb, 45° 00'		
Longitude.		Dist. in Miles.	Longitude.		Dist. in Miles.	Longitude.		Dist. in Miles.	Longitude.		Dist. in Miles.
D. M.	D. M.		D. M.	D. M.		D. M.	D. M.		D. M.	D. M.	
18 0	3 38	1101	7 34	1169	12 14	1290	13 19	1527	18 0	27 24	1944
18 10	3 40	1111	7 40	1180	12 21	1318	18 29	1541	18 10	27 39	1962
18 20	3 42	1122	7 44	1191	12 28	1323	18 39	1556	18 20	27 55	1980
18 30	3 44	1132	7 48	1201	12 35	1335	18 49	1570	18 30	28 11	1998
18 40	3 46	1142	7 52	1212	12 42	1347	19 00	1584	18 40	28 27	2016
18 50	3 49	1152	7 57	1223	12 49	1359	19 10	1598	18 50	28 42	2034
19 0	3 51	1162	8 01	1234	12 56	1371	19 21	1612	19 0	28 58	2052
19 10	3 53	1173	8 05	1245	13 03	1383	19 31	1626	19 10	29 14	2070
19 20	3 55	1183	8 10	1256	13 11	1395	19 42	1640	19 20	29 30	2088
19 30	3 57	1193	8 14	1266	13 18	1407	19 53	1655	19 30	29 46	2106
19 40	3 59	1203	8 19	1277	13 25	1419	20 04	1669	19 40	30 02	2124
19 50	4 01	1213	8 23	1288	13 32	1431	20 14	1683	19 50	30 18	2142
20 0	4 04	1224	8 28	1299	13 39	1443	20 25	1697	20 0	30 34	2160
20 10	4 07	1234	8 32	1310	13 46	1455	20 35	1711	20 10	30 50	2178
20 20	4 09	1244	8 36	1321	13 53	1467	20 46	1725	20 20	31 06	2196
20 30	4 11	1254	8 41	1331	14 02	1479	20 57	1739	20 30	31 21	2214
20 40	4 13	1264	8 45	1342	14 08	1491	21 07	1744	20 40	31 37	2232
20 50	4 15	1274	8 49	1353	14 15	1503	21 18	1758	20 50	31 53	2250
21 0	4 17	1285	8 54	1364	14 22	1515	21 28	1782	21 0	32 09	2265
21 10	4 19	1295	8 59	1375	14 29	1527	21 39	1796	21 10	32 25	2286
21 20	4 21	1305	9 03	1385	14 36	1539	21 50	1811	21 20	32 42	2304
21 30	4 23	1315	9 07	1396	14 44	1551	22 01	1825	21 30	32 57	2322
21 40	4 25	1325	9 12	1407	14 51	1563	22 12	1839	21 40	33 14	2340
21 50	4 27	1336	9 16	1418	14 58	1575	22 22	1854	21 50	33 30	2358
22 0	4 29	1346	9 20	1429	15 05	1588	22 33	1867	22 0	33 46	2376
22 10	4 31	1356	9 25	1440	15 12	1600	22 44	1871	22 10	34 02	2394
22 20	4 33	1366	9 30	1450	15 19	1612	22 55	1885	22 20	34 18	2412
22 30	4 35	1376	9 34	1461	15 26	1624	23 06	1899	22 30	34 35	2430
22 40	4 37	1387	9 38	1472	15 33	1636	23 17	1903	22 40	34 51	2448
22 50	4 40	1397	9 43	1483	15 41	1648	23 28	1917	22 50	35 07	2466
23 0	4 42	1407	9 48	1494	15 48	1660	23 39	1952	23 0	35 23	2484
23 10	4 44	1417	9 52	1505	15 55	1672	23 49	1966	23 10	35 40	2502
23 20	4 46	1427	9 57	1515	16 03	1684	24 00	1980	23 20	35 56	2520
23 30	4 48	1438	10 02	1526	16 10	1696	24 11	1993	23 30	36 12	2538
23 40	4 50	1448	10 07	1537	16 17	1708	24 22	2008	23 40	36 28	2556
23 50	4 52	1458	10 11	1548	16 24	1720	24 33	2022	23 50	36 45	2574

5 Rumb, 56° 15'			6 Rumb, 67° 30'			7 Rumb, 78° 45'		
Longitude.		Dist. in Miles.	Longitude.		Dist. in Miles.	Longitude.		Dist. in Miles.
D. M.	D. M.		D. M.	D. M.		D. M.	D. M.	
18 0	27 24	1944	44 11	2822	92 01	5536		
18 10	27 39	1962	44 37	2848	92 55	5587		
18 20	27 55	1980	44 02	2874	93 44	5638		
18 30	28 11	1998	45 27	2901	94 40	5690		
18 40	28 27	2016	45 55	2927	95 32	5741		
18 50	28 42	2034	46 18	2953	95 56	5792		
19 0	28 58	2052	46 45	2979	97 29	5843		
19 10	29 14	2070	47 11	3005	98 14	5895		
19 20	29 30	2088	47 36	3031	99 04	5946		
19 30	29 46	2106	48 02	3057	99 58	5997		
19 40	30 02	2124	48 27	3083	100 52	6048		
19 50	30 18	2142	48 53	3110	101 46	6100		
20 0	30 34	2160	49 18	3136	102 40	6151		
20 10	30 50	2178	49 44	3162	103 30	6202		
20 20	31 06	2196	50 09	3188	104 25	6254		
20 30	31 21	2214	50 35	3216	105 19	6305		
20 40	31 37	2232	51 01	3230	106 14	6356		
20 50	31 53	2250	51 26	3266	107 08	6407		
21 0	32 09	2265	51 52	3292	108 03	6458		
21 10	32 25	2286	52 20	3319	108 53	6510		
21 20	32 42	2304	52 43	3345	109 48	6561		
21 30	32 57	2322	53 11	3371	110 43	6612		
21 40	33 14	2340	53 37	3397	111 38	6664		
21 50	33 30	2358	54 03	3423	112 32	6715		
22 0	33 46	2376	54 29	3449	113 25	6746		
22 10	34 02	2394	54 55	3475	114 20	6777		
22 20	34 18	2412	55 21	3502	115 13	6849		
22 30	34 35	2430	55 47	3528	116 09	6900		
22 40	34 51	2448	56 13	3554	117 04	6951		
22 50	35 07	2466	56 39	3580	117 59	7002		
23 0	35 23	2484	57 05	3606	118 50	7075		
23 10	35 40	2502	57 31	3632	119 45	7126		
23 20	35 56	2520	57 57	3658	120 41	7177		
23 30	36 12	2538	58 23	3684	121 37	7228		
23 40	36 28	2556	58 52	3711	122 32	7280		
23 50	36 45	2574	59 18	3736	123 24	7331		



Latitude	1 Rumb, 11° 15'			2 Rumb, 22° 30'			3 Rumb, 33° 45'			4 Rumb, 45° 00'		
	Longitude	Dift. in Miles.		Longitude	Dift. in Miles.		Longitude	Dift. in Miles.		Longitude	Dift. in Miles.	
D. M.	D. M.			D. M.			D. M.			D. M.		
24 0	4 55	1468	10 15	1559	16 31	1732	24 44	2036				
24 10	4 57	1478	10 19	1570	16 39	1744	24 55	2041				
24 20	4 59	1489	10 24	1580	16 46	1756	25 06	2055				
24 30	5 02	1499	10 29	1591	16 53	1768	25 17	2069				
24 40	5 04	1509	10 33	1602	17 01	1780	25 28	2083				
24 50	5 06	1519	10 37	1613	17 08	1792	25 32	2097				
25 0	5 08	1530	10 42	1624	17 16	1804	25 50	2121				
25 10	5 10	1540	10 46	1634	17 23	1816	26 01	2135				
25 20	5 12	1550	10 51	1645	17 30	1828	26 12	2150				
25 30	5 14	1560	10 56	1656	17 38	1840	26 23	2164				
25 40	5 16	1570	11 01	1667	17 45	1852	26 34	2178				
25 50	5 18	1580	11 05	1678	17 52	1864	26 45	2192				
26 0	5 21	1591	11 09	1688	18 00	1876	26 56	2206				
26 10	5 23	1601	11 14	1699	18 07	1888	27 07	2220				
26 20	5 26	1611	11 19	1710	18 15	1900	27 08	2234				
26 30	5 28	1621	11 23	1721	18 22	1912	27 29	2249				
26 40	5 30	1631	11 28	1732	18 30	1924	27 40	2263				
26 50	5 32	1642	11 32	1743	18 37	1936	27 51	2277				
27 0	5 34	1652	11 37	1753	18 45	1948	28 03	2291				
27 10	5 36	1662	11 42	1764	18 52	1960	28 14	2305				
27 20	5 39	1672	11 47	1775	19 00	1972	28 25	2319				
27 30	5 41	1682	11 51	1786	19 07	1984	28 37	2333				
27 40	5 43	1693	11 56	1797	19 15	1996	28 49	2348				
27 50	5 46	1703	12 01	1808	19 22	2008	28 59	2362				
28 0	5 48	1713	12 06	1818	19 30	2020	29 11	2376				
28 10	5 50	1723	12 10	1829	19 37	2033	29 22	2390				
28 20	5 52	1733	12 15	1840	19 45	2045	29 34	2404				
28 30	5 55	1744	12 20	1851	19 56	2057	29 46	2418				
28 40	5 57	1754	12 25	1862	20 00	2069	29 57	2432				
28 50	6 00	1764	12 30	1872	20 08	2081	30 08	2447				
29 0	6 02	1774	12 34	1883	20 16	2093	30 19	2461				
29 10	6 04	1784	12 39	1894	20 23	2105	30 31	2475				
29 20	6 07	1795	12 43	1905	20 30	2117	30 43	2489				
29 30	6 09	1805	12 48	1916	20 38	2129	30 54	2503				
29 40	6 11	1815	12 52	1927	20 46	2141	31 05	2517				
29 50	6 13	1825	12 57	1937	20 54	2153	31 17	2531				

Latitude	5 Rumb, 56° 15'			6 Rumb, 67° 30'			7 Rumb, 78° 45'		
	Longitude	Dift. in Miles.		Longitude	Dift. in Miles.		Longitude	Dift. in Miles.	
D. M.	D. M.			D. M.			D. M.		
24 0	37 01	2592	59 44	3763	124 24	7381			
24 10	37 17	2610	60 11	3789	125 15	7432			
24 20	37 34	2628	60 37	3815	126 11	7484			
24 30	37 50	2646	61 03	3841	127 07	7535			
24 40	38 07	2664	61 30	3867	128 00	7586			
24 50	38 22	2682	61 56	3894	128 57	7537			
25 0	38 40	2200	62 22	3920	129 52	7689			
25 10	38 56	2718	62 49	3946	130 48	7740			
25 20	39 13	2736	63 15	3972	131 44	7791			
25 30	39 29	2754	63 42	3998	132 56	7842			
25 40	39 46	2772	64 09	4024	133 33	7894			
25 50	40 02	2790	64 34	4050	134 29	7945			
26 0	40 19	2808	65 02	4076	135 26	7996			
26 10	40 36	2826	65 31	4103	136 23	8048			
26 20	40 53	2844	65 56	4129	137 20	8098			
26 30	41 09	2862	66 25	4155	138 17	8150			
26 40	41 26	2880	66 50	4181	139 09	8201			
26 50	41 42	2898	67 19	4207	140 07	8253			
27 0	42 00	2916	67 45	4233	141 04	8304			
27 10	42 17	2934	68 12	4259	142 01	8355			
27 20	42 33	2952	68 39	4285	142 56	8406			
27 30	42 50	2970	69 06	4312	143 51	8458			
27 40	43 07	2988	69 33	4338	144 49	8500			
27 50	43 24	2906	70 00	4344	145 46	8560			
28 0	43 41	3024	70 27	4390	146 44	8611			
28 10	43 58	3042	70 55	4416	147 33	8663			
28 20	44 15	3060	71 22	4442	148 35	8714			
28 30	44 32	3078	71 49	4468	149 33	8765			
28 40	44 49	3096	72 19	4495	150 31	8816			
28 50	45 06	3114	72 44	4521	151 29	8868			
29 0	45 23	3132	73 14	4547	152 28	8919			
29 10	45 40	3150	73 41	4573	153 24	8970			
29 20	45 57	3168	74 09	4599	154 23	9021			
29 30	46 15	3186	74 37	4625	155 19	9073			
29 40	46 22	3204	75 04	4651	156 17	9124			
29 50	46 49	3222	75 32	4677	157 16	9175			



Latitude	1 Rumb, 11° 15'			2 Rumb, 22° 30'			3 Rumb, 33° 45'			4 Rumb, 45° 00'		
	Longitude	Dift. in Miles.		Longitude	Dift. in Miles.		Longitude	Dift. in Miles.		Longitude	Dift. in Miles.	
D. M.	D. M.			D. M.			D. M.			D. M.		
30 0	6 16	1835		13 02	1843		21 01	2165		31 27	2546	
30 10	6 18	1845		13 07	1859		21 08	2177		31 40	2560	
30 20	6 20	1850		13 11	1907		21 17	2189		31 51	2574	
30 30	6 23	1860		13 16	1911		21 24	2201		32 03	2588	
30 40	6 25	1876		13 21	1921		21 32	2213		32 15	2602	
30 50	6 27	1886		13 26	2002		21 41	2225		32 29	2616	
31 0	6 29	1896		13 30	2013		21 47	2237		32 38	2630	
31 10	6 31	1907		13 35	2024		21 55	2249		32 49	2645	
31 20	6 34	1917		13 40	2035		22 03	2261		33 00	2659	
31 30	6 36	1927		13 45	2046		22 11	2273		33 12	2673	
31 40	6 39	1937		13 50	2056		22 19	2285		33 25	2687	
31 50	6 41	1947		13 56	2067		22 27	2297		33 37	2701	
32 0	6 43	1958		14 01	2078		22 34	2309		33 48	2715	
32 10	6 46	1968		14 06	2089		22 42	2321		34 00	2730	
32 20	6 48	1978		14 10	2100		22 50	2333		34 12	2744	
32 30	6 50	1988		14 15	2111		22 58	2345		34 24	2758	
32 40	6 52	1998		14 20	2121		23 06	2357		34 36	2772	
32 50	6 55	2009		14 25	2132		23 14	2369		34 48	2786	
33 0	6 57	2019		14 30	2143		23 21	2381		35 00	2800	
33 10	7 00	2029		14 35	2154		23 30	2393		35 12	2814	
33 20	7 03	2039		14 40	2165		23 38	2405		35 25	2828	
33 30	7 05	2049		14 45	2176		23 46	2417		35 35	2843	
33 40	7 08	2060		14 49	2186		23 54	2429		35 47	2857	
33 50	7 10	2070		14 54	2197		24 02	2441		35 59	2871	
34 0	7 13	2080		14 59	2208		24 10	2454		36 11	2885	
34 10	7 15	2090		15 04	2219		24 18	2466		36 23	2899	
34 20	7 18	2100		15 09	2230		24 26	2478		36 35	2903	
34 30	7 20	2111		15 14	2240		24 34	2490		36 47	2917	
34 40	7 22	2121		15 20	2251		24 42	2502		36 56	2932	
34 50	7 24	2131		15 25	2262		24 50	2514		37 12	2946	
35 0	7 26	2141		15 29	2273		24 59	2526		37 24	2970	
35 10	7 29	2151		15 34	2284		25 07	2538		37 36	2984	
35 20	7 31	2162		15 39	2295		25 15	2550		37 48	3008	
35 30	7 34	2172		15 44	2305		25 23	2562		38 00	3022	
35 40	7 36	2182		15 50	2316		25 31	2574		38 13	3036	
35 50	7 38	2192		15 55	2327		25 40	2586		38 25	3050	

Latitude	5 Rumb, 56° 15'			6 Rumb, 67° 30'			7 Rumb, 78° 45'		
	Longitude	Dift. in Miles.		Longitude	Dift. in Miles.		Longitude	Dift. in Miles.	
D. M.	D. M.			D. M.			D. M.		
30 0	47 06	3240		76 00	4704		158 15	9226	
30 10	47 24	3258		76 27	4730		159 14	9279	
30 20	47 41	3276		76 55	4756		160 08	9329	
30 30	47 58	3294		77 23	4782		161 08	9380	
30 40	48 16	3312		77 51	4808		162 07	9431	
30 50	48 33	3330		78 19	4834		163 06	9483	
31 0	48 50	3348		78 47	4860		164 03	9534	
31 10	49 08	3366		79 17	4886		165 03	9585	
31 20	49 25	3384		79 43	4913		166 01	9636	
31 30	49 43	3402		80 13	4939		167 00	9688	
31 40	50 01	3420		80 41	4965		168 00	9739	
31 50	50 18	3438		81 10	4991		169 00	9790	
32 0	50 36	3456		81 38	5017		170 00	9842	
32 10	50 53	3474		82 06	5043		170 55	9893	
32 20	51 11	3492		82 35	5069		171 55	9944	
32 30	51 29	3510		83 31	5095		172 56	9995	
32 40	51 47	3528		83 32	5122		173 56	10047	
32 50	52 04	3546		84 01	5148		174 53	10098	
33 0	52 22	3564		84 29	5174		175 54	10149	
33 10	52 40	3582		84 58	5200		176 55	10200	
33 20	52 58	3600		85 26	5226		177 56	10252	
33 30	53 16	3618		85 55	5252		178 57	10303	
33 40	53 34	3636		86 26	5278		179 58	10354	
33 50	53 50	3654		86 52	5305		180 57	10405	
34 0	54 10	3672		87 24	5331		181 56	10457	
34 10	54 28	3690		87 52	5357		182 57	10508	
34 20	54 46	3708		88 02	5383		183 59	10559	
34 30	55 04	3726		88 50	5409		184 59	10610	
34 40	55 22	3744		89 20	5435		185 58	10662	
34 50	55 41	3762		89 49	5461		187 00	10713	
35 0	55 59	3780		90 19	5488		188 02	10764	
35 10	56 17	3798		90 48	5514		189 03	10815	
35 20	56 35	3816		91 18	5540		190 04	10867	
35 30	56 54	3834		91 48	5566		191 06	10918	
35 40	57 12	3852		92 17	5592		192 07	10969	
35 50	57 30	3870		92 46	5618		193 11	11020	



Latitude	1 Rumb, 11° 15'			2 Rumb, 22° 30'			3 Rumb, 33° 45'			4 Rumb, 45° 00'		
	Longitude	Dift. in Miles.		Longitude	Dift. in Miles.		Longitude	Dift. in Miles.		Longitude	Dift. in Miles.	
D. M.	D. M.			D. M.			D. M.			D. M.		
36 0	7 41	2202		16 00	2338		25 49	2598		38 38	3035	
36 10	7 43	2212		16 05	2349		25 57	2610		38 50	3069	
36 20	7 46	2223		16 11	2362		26 05	2622		39 03	3083	
36 30	7 48	2233		16 16	2370		26 13	2634		39 15	3097	
36 40	7 50	2243		16 21	2381		26 22	2646		39 27	3111	
36 50	7 53	2253		16 26	2392		26 30	2658		39 40	3125	
37 0	7 56	2263		16 32	2403		26 38	2670		39 53	3140	
37 10	7 59	2274		16 37	2414		26 47	2681		40 05	3154	
37 20	8 02	2284		16 42	2425		26 55	2693		40 18	3168	
37 30	8 04	2294		16 47	2435		27 03	2705		40 31	3182	
37 40	8 06	2304		16 52	2446		27 12	2717		40 43	3196	
37 50	8 09	2314		16 57	2457		27 20	2729		40 56	3210	
38 0	8 11	2325		17 02	2468		27 28	2742		41 08	3224	
38 10	8 13	2335		17 08	2479		27 37	2754		41 21	3239	
38 20	8 16	2345		17 13	2490		27 45	2766		41 33	3259	
38 30	8 19	2355		17 18	2500		27 54	2778		41 46	3262	
38 40	8 21	2366		17 23	2511		28 03	2790		42 00	3281	
38 50	8 24	2376		17 28	2522		28 11	2802		42 13	3296	
39 0	8 26	2386		17 32	2533		28 20	2814		42 26	3309	
39 10	8 28	2396		17 37	2544		28 29	2826		42 39	3323	
39 20	8 31	2406		17 44	2554		28 37	2838		42 52	3338	
39 30	8 34	2417		17 49	2565		28 46	2850		43 04	3352	
39 40	8 37	2427		17 55	2576		28 55	2862		43 17	3366	
39 50	8 39	2437		18 00	2587		29 04	2874		43 30	3380	
40 0	8 42	2447		18 06	2598		29 12	2886		43 43	3394	
40 10	8 44	2457		18 12	2609		29 21	2898		43 56	3408	
40 20	8 47	2467		18 20	2619		29 30	2911		44 09	3422	
40 30	8 49	2478		18 22	2630		29 38	2923		44 21	3437	
40 40	8 52	2488		18 28	2641		29 47	2935		44 34	3451	
40 50	8 55	2498		18 34	2652		29 56	2947		44 48	3465	
41 0	8 57	2508		18 40	2663		30 05	2959		45 02	3479	
41 10	9 00	2519		18 45	2674		30 14	2971		45 16	3493	
41 20	9 03	2529		18 50	2684		30 23	2983		45 29	3507	
41 30	9 06	2539		18 56	2695		30 32	2995		45 42	3521	
41 40	9 08	2549		19 01	2706		30 40	3006		45 55	3535	
41 50	9 12	2560		19 06	2717		30 50	3019		46 08	3550	

Latitude.	5 Rumb, 56° 15'			6 Rumb, 67° 30'			7 Rumb, 78° 45'		
	Longitude.	Dift. in Miles.		Longitude.	Dift. in Miles.		Longitude.	Dift. in Miles.	
D. M.	D. M.			D. M.			D. M.		
36 0	57 49	3883		93 16	5644		194 14	11072	
36 10	58 08	3906		93 48	5670		195 17	11123	
36 20	58 26	3924		94 16	5697		196 18	11174	
36 30	58 45	3942		94 48	5723		197 20	11226	
36 40	59 03	3960		95 18	5741		198 22	11277	
36 50	59 22	3978		95 48	5775		199 26	11328	
37 0	59 41	3996		96 18	5801		200 29	11379	
37 10	60 00	4014		96 48	5827		201 31	11421	
37 20	60 18	4032		97 18	5853		202 33	11472	
37 30	60 37	4050		97 48	5879		203 37	11423	
37 40	60 56	4068		98 19	5906		204 41	11574	
37 50	61 15	4086		98 49	5932		205 46	11626	
38 0	61 34	4104		99 19	5958		206 50	11687	
38 10	61 52	4122		99 49	5984		207 54	11738	
38 20	62 12	4140		100 20	6010		208 55	11789	
38 30	62 31	4158		100 51	6036		210 06	11841	
38 40	62 50	4176		101 24	6062		211 05	11892	
38 50	63 09	4194		101 52	6089		212 10	11943	
39 0	63 29	4212		102 26	6115		213 15	11994	
39 10	63 48	4230		102 56	6141		214 20	12046	
39 20	64 07	4248		103 28	6167		215 24	12097	
39 30	64 27	4266		103 58	6193		216 29	12148	
39 40	64 46	4284		104 30	6219		217 35	12199	
39 50	65 06	4302		105 02	6245		218 41	12251	
40 0	65 25	4320		105 32	6271		219 42	12302	
40 10	65 45	4338		106 04	6288		220 49	12353	
40 20	66 04	4356		106 35	6324		221 56	12404	
40 30	66 24	4374		107 06	6350		223 03	12456	
40 40	66 44	4392		107 39	6378		224 10	12507	
40 50	67 04	4410		108 10	6402		225 18	12558	
41 0	67 23	4428		108 42	6428		226 23	12609	
41 10	67 43	4446		109 16	6454		227 27	12661	
41 20	68 03	4464		109 45	6480		228 35	12712	
41 30	68 23	4482		110 20	6507		229 43	12763	
41 40	68 43	4499		110 52	6533		230 46	12815	
41 50	69 03	4518		111 25	6559		231 53	12866	



Latitude.	1 Rumb, 11 15'			2 Rumb, 22° 30'			3 Rumb, 33° 45'			4 Rumb, 45° 00'		
	Longitude.	Dift. in Miles.		Longitude.	Dift. in Miles.		Longitude.	Dift. in Miles.		Longitude.	Dift. in Miles.	
D. M.	D. M.			D. M.			D. M.			D. M.		
42 0	9 13	2569		19 12	2728		31 00	3031		46 22	3364	
42 15	9 16	2570		19 11	2739		31 08	3043		46 36	3378	
42 30	9 18	2591		19 23	2749		31 17	3055		46 49	3392	
42 30	9 21	2600		19 29	2760		31 26	3067		47 02	3406	
42 45	9 24	2611		19 33	2771		31 35	3079		47 16	3420	
42 50	9 27	2620		19 40	2782		31 44	3091		47 30	3434	
43 0	9 30	2631		19 45	2793		31 53	3103		47 43	3447	
43 15	9 32	2641		19 51	2803		32 02	3115		47 56	3461	
43 30	9 35	2651		19 57	2814		32 11	3127		48 10	3475	
43 30	9 37	2661		20 03	2825		32 20	3139		48 23	3489	
43 40	9 40	2671		20 06	2836		32 29	3151		48 37	3503	
43 50	9 43	2682		20 13	2847		32 38	3163		48 50	3517	
44 0	9 46	2692		20 19	2858		32 47	3175		49 06	3531	
44 10	9 48	2701		20 26	2868		32 57	3187		49 20	3545	
44 20	9 51	2712		20 32	2879		33 07	3199		49 34	3559	
44 30	9 54	2722		20 38	2890		33 16	3211		49 48	3573	
44 40	9 57	2733		20 44	2901		33 25	3223		50 02	3587	
44 50	10 00	2743		20 50	2912		33 34	3235		50 16	3601	
45 0	10 03	2753		20 56	2923		33 43	3247		50 30	3615	
45 10	10 06	2763		21 01	2933		33 53	3259		50 43	3629	
45 20	10 08	2773		21 07	2944		34 02	3271		50 57	3643	
45 30	10 11	2784		21 16	2955		34 12	3283		51 12	3657	
45 40	10 14	2794		21 19	2966		34 23	3295		51 26	3671	
45 50	10 17	2804		21 25	2977		34 33	3307		51 40	3685	
46 0	10 19	2814		21 31	2988		34 42	3319		51 54	3699	
46 10	10 22	2825		21 33	2998		34 52	3331		52 10	3713	
46 20	10 25	2835		21 42	3009		35 01	3343		52 23	3727	
46 30	10 28	2845		21 48	3020		35 11	3355		52 39	3741	
46 40	10 31	2855		21 54	3031		35 21	3368		52 54	3755	
46 50	10 34	2865		22 00	3041		35 30	3380		53 08	3769	
47 0	10 37	2875		22 06	3052		35 40	3392		53 23	3783	
47 10	10 40	2886		22 13	3063		35 50	3404		53 37	3797	
47 20	10 43	2896		22 18	3074		36 00	3416		53 52	3811	
47 30	10 45	2906		22 24	3085		36 10	3428		54 06	3825	
47 40	10 48	2916		22 30	3096		36 20	3440		54 21	3839	
47 50	10 51	2926		22 36	3106		36 30	3452		54 36	3853	

Latitude.	5 Rumb, 56° 15'			6 Rumb, 67° 30'			7 Rumb, 78° 45'		
	Longitude.	Dift. in Miles.		Longitude.	Dift. in Miles.		Longitude.	Dift. in Miles.	
D. M.	D. M.			D. M.			D. M.		
42 0	69 23	4536		111 56	6583		233 03	12917	
42 10	69 43	4554		112 29	6611		234 12	12968	
42 20	70 04	4572		113 01	6637		235 21	13020	
42 30	70 24	4590		113 34	6663		236 30	13061	
42 40	70 44	4608		114 06	6680		237 34	13112	
42 50	71 04	4626		114 39	6716		238 43	13163	
43 0	71 25	4644		115 12	6742		239 53	13215	
43 10	71 45	4662		115 45	6768		241 02	13266	
43 20	72 06	4680		116 19	6794		242 12	13317	
43 30	72 27	4698		116 51	6820		243 20	13368	
43 40	72 47	4716		117 27	6846		244 34	13420	
43 50	73 08	4734		117 58	6872		245 37	13471	
44 0	73 29	4752		118 34	6899		246 50	13532	
44 10	73 50	4770		119 06	6925		248 01	13583	
44 20	74 11	4788		119 40	6951		249 12	13635	
44 30	74 31	4806		120 13	6977		250 23	13686	
44 40	74 52	4824		120 48	7003		251 29	13737	
44 50	75 12	4842		121 21	7029		252 41	13788	
45 0	75 33	4860		121 56	7055		253 34	13840	
45 10	75 56	4878		122 30	7082		255 04	13891	
45 20	76 17	4896		123 04	7108		256 11	13942	
45 30	76 38	4914		123 38	7134		257 24	13993	
45 40	77 00	4932		124 13	7160		258 38	14045	
45 50	77 21	4950		124 47	7186		259 50	14096	
46 0	77 43	4968		125 22	7212		261 04	14147	
46 10	78 04	4986		125 56	7238		262 12	14198	
46 20	78 26	5004		126 31	7264		263 28	14250	
46 30	78 47	5022		127 08	7291		264 39	14301	
46 40	79 09	5040		127 43	7317		265 53	14352	
46 50	79 30	5058		128 18	7343		267 08	14403	
47 0	79 53	5076		128 53	7369		268 23	14455	
47 10	80 15	5094		129 28	7395		269 23	14506	
47 20	80 37	5112		130 04	7421		270 47	14557	
47 30	80 59	5130		130 40	7447		272 02	14609	
47 40	81 22	5148		131 13	7473		273 18	14660	
47 50	81 43	5166		131 52	7499		274 34	14711	



Latitude	1 Rumb, 11° 15'			2 Rumb, 22° 30'			3 Rumb, 33° 45'			4 Rumb, 45° 00'			
	Longitude		Diff. in Miles.	Longitude		Diff. in Miles.	Longitude		Diff. in Miles.	Longitude		Diff. in Miles.	
D. M.	D. M.			D. M.			D. M.			D. M.			
48	0	10	54	2936	22	41	3117	36	40	3464	54	52	4073
48	10	10	57	2947	22	49	3128	36	50	3476	55	05	4087
48	20	11	00	2957	22	56	3139	37	00	3488	55	22	4101
48	30	11	04	2967	23	03	3150	37	10	3500	55	37	4115
48	40	11	07	2977	23	10	3161	37	20	3512	55	51	4129
48	50	11	10	2987	23	16	3171	37	30	3524	56	07	4144
49	0	11	13	2998	23	22	3182	37	40	3536	56	22	4158
49	10	11	16	3008	23	27	3193	37	50	3548	56	38	4172
49	20	11	19	3018	23	33	3204	38	00	3560	56	52	4186
49	30	11	22	3028	23	40	3215	38	10	3572	57	08	4200
49	40	11	25	3038	23	46	3225	38	20	3584	57	23	4214
49	50	11	28	3049	23	52	3236	38	30	3596	57	39	4228
50	0	11	31	3059	23	59	3247	38	42	3608	57	54	4243
50	10	11	34	3069	24	05	3258	38	52	3620	58	10	4255
50	20	11	37	3079	24	12	3269	39	03	3632	58	26	4271
50	30	11	40	3089	24	19	3280	39	13	3644	58	42	4285
50	40	11	44	3100	24	26	3290	39	24	3656	58	58	4299
50	50	11	47	3110	24	32	3301	39	34	3668	59	14	4313
51	0	11	50	3120	24	38	3312	39	45	3680	59	30	4327
51	10	11	53	3130	24	45	3323	39	55	3692	59	46	4342
51	20	11	56	3140	24	52	3334	40	06	3704	60	01	4356
51	30	12	00	3150	24	58	3345	40	16	3716	60	17	4370
51	40	12	03	3161	25	05	3355	40	27	3728	60	33	4384
51	50	12	06	3171	25	12	3366	40	38	3741	60	49	4398
52	0	12	09	3181	25	18	3377	40	49	3753	61	05	4412
52	10	12	12	3191	25	25	3388	41	00	3765	61	21	4426
52	20	12	15	3202	25	32	3399	41	10	3777	61	37	4441
52	30	12	19	3212	25	39	3410	41	22	3789	61	54	4455
52	40	12	22	3222	25	45	3420	41	32	3801	62	10	4469
52	50	12	26	3232	25	52	3431	41	43	3813	62	26	4483
53	0	12	29	3242	25	56	3442	41	55	3825	62	43	4497
53	10	12	32	3253	26	09	3453	42	06	3837	63	00	4511
53	20	12	36	3263	26	13	3464	42	17	3849	63	17	4525
53	30	12	39	3273	26	20	3474	42	28	3861	63	34	4540
53	40	12	42	3283	26	27	3485	42	39	3873	63	51	4554
53	50	12	45	3293	26	34	3496	42	51	3885	64	08	4568

Latitude.		5 Rumb, 56° 15'.			6 Rumb, 67° 30'.			7 Rumb, 78° 45'.		
		Longitude.		Diff. in Miles.	Longitude.		Diff. in Miles.	Longitude.		Diff. in Miles.
D. M.	D. M.	D. M.	D. M.		D. M.	D. M.				
48	0	82	06	5184	132	28	7426	275	50	14762
48	10	82	23	5202	133	03	7452	277	00	14814
48	20	82	51	5220	133	38	7478	278	17	14865
48	30	83	14	5238	134	16	7504	279	34	14916
48	40	83	36	5256	134	54	7530	280	51	14967
48	50	83	58	5274	135	28	7556	282	08	15019
49	0	84	22	5292	136	07	7683	283	23	15070
49	10	84	44	5310	136	42	7709	284	38	15121
49	20	85	07	5328	137	20	7735	285	56	15172
49	30	85	30	5346	137	57	7761	287	24	15224
49	40	85	54	5364	138	34	7787	288	33	15275
49	50	86	16	5382	139	12	7813	289	46	15326
50	0	86	44	5400	139	49	7839	291	05	15377
50	10	87	03	5418	140	26	7865	292	24	15429
50	20	87	27	5436	141	04	7892	295	44	15480
50	30	87	50	5454	141	41	7918	296	04	15531
50	40	88	14	5472	142	20	7944	296	24	15582
50	50	88	39	5480	142	58	7970	297	45	15634
51	0	89	01	5508	143	36	7996	299	00	15685
51	10	89	25	5526	144	17	8022	300	21	15736
51	20	89	49	5544	144	52	8048	301	43	15787
51	30	90	13	5562	145	34	8074	303	04	15839
51	40	90	37	5580	146	12	8101	304	20	15890
51	50	91	00	5598	146	51	8127	305	42	15941
52	0	91	25	5616	147	30	8153	307	05	15992
52	10	91	50	5634	148	09	8179	308	23	16044
52	20	92	14	5652	148	48	8205	309	52	16095
52	30	92	39	5670	149	28	8231	311	12	16146
52	40	93	03	5688	150	07	8257	312	36	16198
52	50	93	28	5706	150	47	8284	313	57	16249
53	0	93	53	5724	151	27	8310	315	22	16300
53	10	94	18	5742	152	07	8336	316	46	16351
53	20	94	43	5760	152	47	8362	318	12	16403
53	30	95	03	5778	153	27	8388	319	35	16454
53	40	95	33	5796	154	11	8414	320	56	16505
53	50	95	58	5814	154	48	8440	322	23	16556



Latitude	1 Rumb, 11° 15'			2 Rumb, 22° 30'			3 Rumb, 33° 45'			4 Rumb, 45° 00'		
	Longitude	D. M.	Dist. in Miles.	Longitude	D. M.	Dist. in Miles.	Longitude	D. M.	Dist. in Miles.	Longitude	D. M.	Dist. in Miles.
54° 0'	12 49	3303	26 41	3507	43 03	3897	54 24	4582				
54° 10'	12 52	3314	26 48	3518	43 14	3909	54 41	4596				
54° 20'	12 56	3324	26 58	3528	43 25	3921	54 58	4610				
54° 30'	12 59	3334	27 02	3539	43 37	3933	55 15	4624				
54° 40'	13 02	3344	27 09	3550	43 48	3945	55 32	4639				
54° 50'	13 05	3355	27 16	3561	44 00	3957	55 50	4653				
55° 0'	13 09	3365	27 28	3572	44 12	3969	56 08	4667				
55° 10'	13 12	3375	27 31	3583	44 23	3981	56 26	4681				
55° 20'	13 16	3385	27 38	3594	44 35	3993	56 42	4695				
55° 30'	13 20	3395	27 44	3604	44 46	4005	57 01	4709				
55° 40'	13 23	3405	27 53	3615	44 58	4017	57 19	4723				
55° 50'	13 26	3416	28 00	3626	45 10	4029	57 36	4738				
56° 0'	13 30	3426	28 07	3637	45 22	4041	57 54	4752				
56° 10'	13 33	3436	28 15	3648	45 33	4053	58 11	4766				
56° 20'	13 37	3446	28 22	3658	45 45	4065	58 29	4780				
56° 30'	13 41	3456	28 30	3669	45 58	4077	58 47	4794				
56° 40'	13 44	3467	28 37	3680	46 10	4089	59 05	4808				
56° 50'	13 48	3477	28 45	3691	46 22	4101	59 24	4822				
57° 0'	13 52	3487	28 52	3702	46 35	4113	59 42	4837				
57° 10'	13 56	3497	29 00	3713	46 47	4125	70 00	4851				
57° 20'	14 00	3507	29 08	3723	46 59	4137	70 20	4865				
57° 30'	14 03	3518	29 15	3734	47 11	4150	70 38	4879				
57° 40'	14 07	3528	29 23	3745	47 24	4162	70 58	4893				
57° 50'	14 11	3538	29 31	3756	47 37	4174	71 14	4907				
58° 0'	14 15	3548	29 39	3757	47 50	4186	71 34	4921				
58° 10'	14 18	3558	29 46	3778	48 02	4198	71 53	4936				
58° 20'	14 22	3569	29 54	3788	48 15	4210	72 12	4950				
58° 30'	14 26	3578	30 02	3799	48 27	4222	72 31	4963				
58° 40'	14 30	3586	30 10	3810	48 40	4234	72 50	4978				
58° 50'	14 34	3595	30 19	3821	48 53	4246	73 09	4992				
59° 0'	14 37	3609	30 27	3832	49 06	4258	73 28	5006				
59° 10'	14 41	3620	30 35	3843	49 19	4270	73 48	5020				
59° 20'	14 44	3630	30 43	3853	49 32	4282	74 08	5035				
59° 30'	14 48	3640	30 51	3864	49 45	4294	74 26	5049				
59° 40'	14 52	3650	30 59	3875	49 59	4306	74 46	5063				
59° 50'	14 56	3660	31 08	3886	50 01	4318	75 07	5077				

Latitude	5 Rumb, 56° 15'			6 Rumb, 67° 30'			7 Rumb, 78° 45'		
	Longitude	D. M.	Dist. in Miles.	Longitude	D. M.	Dist. in Miles.	Longitude	D. M.	Dist. in Miles.
54° 0'	95 24	5832	155 32	7467	323 47	16608			
54° 10'	96 50	5850	156 13	8493	325 16	16659			
54° 20'	97 15	5868	156 54	8519	326 40	16710			
54° 30'	97 40	5885	157 36	8545	328 04	16761			
54° 40'	98 07	5904	158 17	8571	329 33	16813			
54° 50'	98 32	5922	158 58	8597	331 01	16864			
55° 0'	98 59	5940	159 40	8623	332 30	16915			
55° 10'	99 24	5958	160 22	8649	334 00	16966			
55° 20'	99 51	5976	161 05	8675	335 21	17018			
55° 30'	100 17	5994	161 47	8702	336 51	17069			
55° 40'	100 46	6012	162 29	8728	338 21	17120			
55° 50'	101 10	6030	163 12	8754	339 52	17171			
56° 0'	101 37	6048	163 55	8780	341 23	17223			
56° 10'	102 04	6066	164 40	8806	342 47	17274			
56° 20'	102 31	6084	165 21	8832	344 19	17325			
56° 30'	102 58	6102	166 08	8858	345 51	17376			
56° 40'	103 25	6120	166 52	8885	347 24	17428			
56° 50'	103 52	6138	167 36	8911	348 57	17479			
57° 0'	104 20	6156	168 20	8937	350 27	17530			
57° 10'	104 46	6174	169 04	8963	352 00	17581			
57° 20'	105 15	6192	169 48	8989	353 31	17633			
57° 30'	105 43	6210	170 33	9015	355 06	17684			
57° 40'	105 11	6228	171 18	9041	356 41	17735			
57° 50'	106 39	6246	172 02	9067	358 16	17787			
58° 0'	107 07	6264	172 47	9094	359 45	17838			
58° 10'	107 35	6282	173 32	9120	361 21	17889			
58° 20'	108 04	6300	174 18	9146	362 59	17940			
58° 30'	108 32	6318	175 04	9172	364 36	17992			
58° 40'	109 01	6336	175 54	9198	366 14	18043			
58° 50'	109 30	6354	176 37	9224	367 52	18094			
59° 0'	109 59	6372	177 27	9250	369 29	18145			
59° 10'	110 28	6390	178 13	9277	371 23	18197			
59° 20'	110 57	6408	179 00	9303	372 43	18248			
59° 30'	111 27	6426	179 47	9329	374 23	18299			
59° 40'	111 56	6444	180 35	9355	375 58	18350			
59° 50'	112 26	6462	181 22	9381	377 37	18402			



1 Rumb, 11° 15'			2 Rumb, 22° 30'			3 Rumb, 33° 45'			4 Rumb, 45° 00'		
Latitude	Longitude	Dift. in Miles.	Longitude	Dift. in Miles.	Longitude	Dift. in Miles.	Longitude	Dift. in Miles.	Longitude	Dift. in Miles.	Dift. in Miles.
D. M.	D. M.		D. M.		D. M.		D. M.		D. M.		
60	0 15	00	3671	31 16	3399	50 25	4330	75 25	5091		
60	10 15	04	3691	31 24	3907	50 35	4342	75 47	5105		
60	20 15	08	3701	31 32	3911	50 53	4354	76 08	5119		
60	30 15	12	3711	31 41	3929	51 06	4366	76 28	5134		
60	40 15	16	3721	31 48	3941	51 20	4378	76 48	5148		
60	50 15	20	3722	31 57	3951	51 33	4390	77 08	5162		
61	0 15	25	3732	32 06	3962	51 46	4402	77 29	5176		
61	10 15	29	3742	32 15	3972	52 00	4414	77 49	5190		
61	20 15	33	3752	32 23	3983	52 14	4426	78 10	5204		
61	30 15	37	3762	32 31	3994	52 28	4438	78 31	5218		
61	40 15	41	3773	32 40	4005	52 42	4450	78 51	5233		
61	50 15	45	3783	32 49	4016	52 56	4462	79 12	5247		
62	0 15	49	3793	32 58	4027	53 10	4474	79 34	5260		
62	10 15	54	3803	33 07	4037	53 24	4486	79 55	5275		
62	20 15	58	3813	33 16	4048	53 38	4498	80 17	5289		
62	30 16	03	3824	33 25	4059	53 53	4510	80 38	5303		
62	40 16	07	3834	33 34	4070	54 07	4532	81 00	5317		
62	50 16	12	3844	33 43	4080	54 21	4554	81 22	5332		
63	0 16	16	3854	33 52	4091	54 38	4546	81 44	5346		
63	10 16	20	3864	34 01	4102	54 52	4558	82 06	5360		
63	20 16	24	3875	34 10	4113	55 06	4570	82 28	5374		
63	30 16	29	3895	34 19	4124	55 22	4582	82 51	5388		
63	40 16	34	3905	34 28	4135	55 37	4594	83 14	5402		
63	50 16	38	3910	34 38	4145	55 52	4616	83 36	5416		
64	0 16	43	3915	34 48	4156	56 07	4618	83 59	5431		
64	10 16	47	3925	34 58	4167	56 22	4630	84 22	5445		
64	20 16	52	3936	35 00	4178	56 38	4642	84 45	5459		
64	30 16	56	3946	35 16	4189	56 53	4654	85 09	5473		
64	40 17	01	3956	35 26	4200	57 08	4666	85 31	5487		
64	50 17	05	3966	35 36	4210	57 24	4679	85 55	5501		
65	0 17	10	3976	35 46	4221	57 40	4690	86 19	5515		
65	10 17	15	3987	35 55	4232	57 56	4701	86 42	5530		
65	20 17	20	3997	36 05	4243	58 12	4715	87 06	5544		
65	30 17	25	4007	36 15	4254	58 28	4727	87 29	5558		
65	40 17	20	4017	36 25	4267	58 44	4739	87 55	5572		
65	50 17	34	4027	36 36	4275	59 01	4750	88 20	5586		

5 Rumb, 56° 15'			6 Rumb, 67° 30'			7 Rumb, 78° 45'		
Latitude.	Longitude.	Dift. in Miles.	Longitude.	Dift. in Miles.	Longitude.	Dift. in Miles.	Longitude.	Dift. in Miles.
D. M.	D. M.		D. M.		D. M.		D. M.	
60	0 12	56	6480	183 11	9407	379 19	18453	
60	10 13	25	6498	182 59	9433	381 01	18504	
60	20 113	56	6506	183 48	9459	382 44	18555	
60	30 114	26	6524	184 36	9486	384 27	18607	
60	40 114	57	6542	185 26	9512	386 10	18658	
60	50 115	27	6560	186 13	9538	387 50	18709	
61	0 115	58	6588	187 04	9564	389 32	18760	
61	10 116	29	6606	187 57	9590	391 18	18812	
61	20 116	59	6624	188 43	9616	393 04	18863	
61	30 117	31	6642	188 38	9642	394 50	18914	
61	40 118	03	6660	190 28	9668	396 29	18965	
61	50 118	34	6678	191 19	9695	398 17	19017	
62	0 119	06	6696	192 10	9721	400 05	19068	
62	10 119	37	6714	193 01	9747	401 54	19119	
62	20 120	10	6732	193 52	9773	403 43	19170	
62	30 120	43	6750	194 44	9799	405 28	19222	
62	40 121	15	6768	195 37	9825	407 16	19273	
62	50 121	44	6786	196 30	9851	409 08	19324	
63	0 122	21	6804	197 23	9878	411 00	19376	
63	10 122	53	6822	198 16	9904	412 52	19427	
63	20 123	27	6840	199 09	9930	414 36	19478	
63	30 124	00	6858	200 03	9956	416 31	19529	
63	40 124	34	6876	201 00	9982	418 25	19581	
63	50 125	08	6894	201 51	10008	420 20	19632	
64	0 125	42	6912	202 49	10034	422 16	19683	
64	10 126	16	6930	203 43	10060	424 08	19734	
64	20 126	51	6948	204 38	10087	426 01	19787	
64	30 127	26	6966	205 34	10113	428 00	19837	
64	40 128	00	6984	206 31	10139	430 00	19888	
64	50 128	35	7002	207 27	10165	431 58	19939	
65	0 129	11	7020	208 24	10191	433 58	19991	
65	10 129	46	7038	209 20	10217	435 50	20041	
65	20 130	22	7056	210 18	10243	437 52	20093	
65	30 130	58	7074	211 16	10269	439 54	20144	
65	40 131	34	7092	212 15	10296	441 57	20195	
65	50 132	10	7110	213 12	10322	444 02	20247	



Latitude.		1 Rumb, 11° 15'.		2 Rumb, 22° 30'.		3 Rumb, 33° 45'.		4 Rumb, 45° 00'.	
Longitude.		Dift. in Miles.		Longitude.		Dift. in Miles.		Longitude.	
D. M.	D. M.	D. M.	D. M.	D. M.	D. M.	D. M.	D. M.	D. M.	D. M.
66	0	17	39	4038	36	46	4285	39	17
66	10	17	43	4048	36	56	4297	39	33
66	20	17	48	4058	37	03	4303	39	50
66	30	17	53	4068	37	16	4315	40	06
66	40	17	58	4073	37	26	4330	40	23
66	50	18	03	4080	37	38	4340	40	40
67	0	18	08	4089	37	48	4355	41	13
67	10	18	13	4100	37	58	4362	41	38
67	20	18	18	4110	38	07	4373	41	59
67	30	18	24	4120	38	20	4384	42	04
67	40	18	30	4140	38	30	4394	42	07
67	50	18	33	4150	38	40	4405	42	24
68	0	18	40	4160	38	52	4416	42	41
68	10	18	45	4170	39	04	4427	42	59
68	20	18	51	4180	39	15	4438	43	17
68	30	18	56	4190	39	26	4448	43	35
68	40	19	02	4201	39	38	4459	43	54
68	50	19	07	4211	39	50	4470	44	12
69	0	19	12	4221	40	00	4481	44	31
69	10	19	17	4231	40	12	4492	44	50
69	20	19	24	4241	40	24	4503	45	08
69	30	19	29	4252	40	35	4514	45	27
69	40	19	35	4262	40	45	4524	45	45
69	50	19	40	4272	40	58	4535	46	05
70	0	19	45	4282	41	10	4546	46	25
70	10	19	50	4292	42	26	4557	46	47
70	20	19	55	4302	43	45	4568	47	03
70	30	20	00	4312	45	07	4578	47	27
70	40	20	05	4322	46	31	4589	47	50
70	50	20	10	4332	46	00	4600	48	11

Latitude.		5 Rumb, 56° 15'.		6 Rumb, 67° 30'.		7 Rumb, 78° 45'.	
Longitude.		Dift. in Miles.		Longitude.		Dift. in Miles.	
D. M.	D. M.	D. M.	D. M.	D. M.	D. M.	D. M.	D. M.
65	0	132	47	7128	214	11	10348
66	10	133	24	7146	215	10	10374
66	20	134	01	7164	216	13	10400
66	30	134	38	7182	217	15	10426
66	40	135	16	7200	218	17	10452
66	50	135	54	7218	219	18	10479
67	0	136	32	7236	220	19	10506
67	10	137	09	7254	221	20	10531
67	20	137	49	7272	222	21	10557
67	30	138	28	7290	223	23	10583
67	40	139	08	7308	224	26	10609
67	50	139	47	7326	225	29	10635
68	0	140	27	7344	226	33	10661
68	10	141	07	7362	227	36	10688
68	20	141	47	7380	228	41	10714
68	30	142	29	7398	229	45	10740
68	40	143	09	7416	230	49	10766
68	50	143	49	7434	232	41	10792
69	0	144	32	7452	233	13	10818
69	10	145	14	7470	234	21	10844
69	20	145	56	7488	235	29	10870
69	30	146	39	7506	236	37	10897
69	40	147	22	7524	237	46	10923
69	50	148	06	7542	238	54	10949
70	0	148	48	7560	240	04	10975
70	10	149	33	7578	241	13	11001
70	20	150	17	7596	242	23	11027
70	30	151	01	7614	242	34	11053
70	40	151	47	7632	244	48	11080
70	50	152	31	7650	244	00	11106



# A TABLE of LOGARITHMS

For Numbers increasing orderly from 1 to 10000,  
with their Differences:

*Whereby the Logarithm of any Number under 1000000  
may be readily taken.*

Nu.	Log.	Nu.	Log.	Nu.	Log.	Nu.	Log.
1	0.000000	26	1.4149733	51	1.7075702	76	1.8808136
2	0.3010300	27	1.4313637	52	1.7160033	77	1.8864907
3	0.4771212	28	1.4471580	53	1.7242759	78	1.8920946
4	0.6020600	29	1.4623980	54	1.7323937	79	1.8976271
5	0.6989700	30	1.4771212	55	1.7403627	80	1.9030900
6	0.7781512	31	1.4913617	56	1.7481880	81	1.9084850
7	0.8450980	32	1.5051500	57	1.7558748	82	1.9138138
8	0.9030900	33	1.5185139	58	1.7634280	83	1.9190781
9	0.9542425	34	1.5314789	59	1.7708520	84	1.9242793
10	1.0000002	35	1.5440580	60	1.7781512	85	1.9294189
11	1.0413927	36	1.5563025	61	1.7853298	86	1.9344984
12	1.0791812	37	1.5682017	62	1.7923917	87	1.9395192
13	1.1139433	38	1.5797836	63	1.7993405	88	1.9444827
14	1.1461280	39	1.5910646	64	1.8061800	89	1.9493900
15	1.1760912	40	1.6020600	65	1.8129133	90	1.9542425
16	1.2041200	41	1.6127838	66	1.8195439	91	1.9590414
17	1.2304489	42	1.6232493	67	1.8260748	92	1.9637878
18	1.2552725	43	1.6334684	68	1.8325089	93	1.9684829
19	1.2787536	44	1.6434527	69	1.8388491	94	1.9731273
20	1.3010300	45	1.6532125	70	1.8450080	95	1.9777236
21	1.3222193	46	1.6627578	71	1.85112583	96	1.9822712
22	1.3424227	47	1.6720978	72	1.8573325	97	1.9867717
23	1.3617278	48	1.6812412	73	1.8633229	98	1.9912261
24	1.3802112	49	1.6901961	74	1.8692317	99	1.9956352
25	1.3979400	50	1.6989700	75	1.8750613	100	2.0000000



Num.	0	1	2	3	4
100	0000000	0004341	0008677	0013009	0017337
101	0043214	0047511	0051803	0056094	0060379
102	0086002	0090257	0094509	0098756	0102999
103	0128372	0132537	0136794	0141003	0145205
104	0170333	0174507	0178677	0182843	0187005
105	0211833	0216027	0220157	0224284	0228406
106	0253057	0257154	0261245	0265333	0269416
107	0295858	0299895	0303943	0307997	0312043
108	0334237	0338257	0342273	0346284	0350293
109	0374205	0378247	0382225	0386202	0390173
110	0413927	0417933	0421816	0425755	0429691
111	0453230	0457140	0461048	0464952	0468852
112	0492180	0496056	0499928	0503797	0507663
113	0530784	0534626	0538464	0542299	0546130
114	0569048	0572856	0576661	0580462	0584260
115	0606978	0610753	0614525	0618293	0622058
116	0644580	0648322	0652061	0655797	0659530
117	0681839	0685559	0689276	0692980	0696681
118	0718825	0722499	0726173	0729847	0733517
119	0755470	0759118	0762762	0766404	0770043
120	0791812	0795430	0799045	0802656	0806265
121	0827854	0831441	0835026	0838608	0842187
122	0863593	0867157	0870712	0874264	0877814
123	0899051	0902580	0906107	0909631	0913151
124	0934217	0937713	0941216	0944711	0948204
125	0969100	0972573	0976043	0979511	0982975
126	1003705	1007151	1010593	1014033	1017471
127	1038037	1041451	1044871	1048284	1051699
128	1072100	1075491	1078880	1082266	1085650
129	1105897	1109262	1112625	1115985	1119343
130	1139433	1142773	1146110	1149444	1152776
131	1172713	1176027	1179338	1182647	1185954
132	1205739	1209028	1212314	1215593	1218880
133	1238516	1241780	1245042	1248301	1251558
134	1271048	1274288	1277525	1280760	1283993
135	1303338	1306553	1309767	1312978	1316177
136	1335389	1338581	1341771	1344958	1348144
137	1367206	1370374	1373541	1376705	1379867
138	1398791	1401937	1405080	1408222	1411361
139	1430148	1433271	1436392	1439511	1442628
140	1461280	1464381	1467480	1470577	1473671
141	1492191	1495270	1498347	1501422	1504494

5	6	7	8	9	Diff.
0021001	0025930	0030295	0034605	0038912	4324
0064660	0068937	0073209	0077478	0081742	4481
0107239	0111473	0115704	0119931	0124154	4240
0144403	0148597	0152778	0156953	0161155	4198
0191163	0195317	0199467	0203613	0207755	4153
0232524	0236639	0240750	0244857	0248960	4118
0273406	0277522	0281644	0285712	0289777	4080
0314285	0318313	0322357	0326388	0330424	4042
0355427	0359429	0363429	0367426	0371429	4004
0396141	0399105	0403066	0407023	0410977	3968
0433623	0437551	0441476	0445398	0449315	3932
0472749	0476642	0480532	0484418	0488301	3897
0511525	0515384	0519239	0523091	0526939	3862
0549358	0553178	0556993	0560804	0564611	3828
0588055	0591846	0595634	0599419	0603200	3795
0625820	0629578	0633333	0637085	0640834	3762
0663219	0666945	0670670	0674393	0678115	3729
0700379	0704093	0707803	0711513	0715218	3698
0737183	0740847	0744507	0748164	0751818	3666
0773679	0777312	0780941	0784568	0788192	3636
0809770	0813347	0816923	0820496	0824066	3605
0845763	0849336	0852906	0856473	0860037	3576
0881361	0884905	0888446	0891984	0895519	3547
0916662	0920185	0923706	0927220	0930712	3518
0951693	0955180	0958664	0962146	0965624	3489
0986437	0989896	0993353	0996806	1000257	3462
1020905	1024337	1027766	1031192	1034616	3434
1055102	1058506	1061909	1065308	1068703	3408
1089031	1092410	1095785	1099156	1102525	3381
1122698	1126050	1129400	1132746	1136091	3355
1156105	1159432	1162756	1166077	1169396	3329
1189257	1192559	1195858	1199154	1202448	3303
1222159	1225435	1228709	1231981	1235250	3279
1254813	1258064	1261314	1264561	1267806	3255
1287223	1290450	1293676	1296900	1300119	3230
1319333	1322559	1325785	1328998	1332209	3204
1351326	1354527	1357725	1360916	1364104	3182
1383027	1386184	1389339	1392492	1395643	3160
1414438	1417582	1420725	1423865	1426999	3137
1445742	1448874	1451994	1455112	1458227	3114
1476763	1479883	1482994	1486104	1489211	3092
1507664	1510762	1513858	1516952	1519984	3070



Num.	0	1	2	3	4
142	1522883	1525941	1528996	1532043	1535100
143	1553360	1556396	1559430	1562462	1565491
144	1583625	1586640	1589653	1592663	1595672
145	1613680	1616674	1619666	1622656	1625644
146	1643528	1646502	1649474	1652443	1655411
147	1673173	1676127	1679078	1682027	1684975
148	1702617	1705550	1708482	1711411	1714339
149	1731863	1734776	1737683	1740598	1743506
150	1760913	1763807	1766699	1769590	1772478
151	1789769	1792645	1795518	1798389	1801259
152	1818436	1821292	1824146	1826999	1829850
153	1846914	1849752	1852588	1855421	1858253
154	1875207	1878026	1880844	1883659	1886473
155	1903317	1906118	1908917	1911714	1914510
156	1931246	1934029	1936810	1939590	1942367
157	1958966	1961762	1964525	1967287	1970047
158	1986571	1989319	1992065	1994809	1997552
159	2013771	2016702	2019431	2022158	2024883
160	2041200	2043913	2046625	2049335	2052044
161	2068259	2070955	2073650	2076344	2079035
162	2095150	2097830	2100508	2103185	2105860
163	2121876	2124540	2127201	2129862	2132521
164	2148438	2151086	2153732	2156376	2159018
165	2174839	2177471	2180100	2182728	2185355
166	2201081	2203696	2206310	2208922	2211533
167	2227165	2229767	2232363	2234959	2237554
168	2253093	2255677	2258260	2260841	2263421
169	2278867	2281436	2284003	2286570	2289134
170	2304489	2307043	2309596	2312146	2314696
171	2329961	2332500	2335038	2337574	2340108
172	2355284	2357809	2360331	2362853	2365373
173	2380461	2382971	2385479	2387986	2390491
174	2405492	2407988	2410481	2412974	2415465
175	2430380	2432861	2435341	2437819	2440296
176	2455127	2457593	2460059	2462523	2464986
177	2479733	2482186	2484637	2487087	2489536
178	2504200	2506639	2509077	2511513	2513948
179	2528530	2530956	2533380	2535803	2538224
180	2552725	2555137	2557548	2559958	2562365
181	2576786	2579184	2581582	2583978	2586373
182	2600714	2603099	2605484	2607867	2610248
183	2624511	2626883	2629255	2631625	2633993

5	6	7	8	9	Diff.
1538149	1541195	1544240	1547282	1550322	3049
1568519	1571544	1574568	1577589	1580603	3028
1598673	1601683	1604683	1607686	1610684	3006
1628630	1631614	1634595	1637575	1640553	2986
1658376	1661340	1664301	1667260	1670218	2965
1687920	1690863	1693805	1696744	1709682	2945
1717264	1720188	1723110	1726029	1728947	2925
1746412	1749316	1752218	1755118	1758016	2906
1775365	1778250	1781132	1784013	1786892	2887
1804126	1806992	1809856	1812718	1815578	2867
1832698	1835545	1838390	1841233	1844075	2831
1861084	1863912	1866739	1869563	1872386	2829
1889285	1892095	1894903	1897709	1900514	2812
1917304	1920096	1922886	1925674	1928461	2794
1945143	1947917	1950690	1953460	1956229	2776
1972806	1975562	1978317	1981070	1983821	2759
2000293	2003032	2005769	2008505	2011239	2741
2027607	2030329	2033049	2035768	2038485	2724
2054750	2057455	2060159	2062869	2065560	2706
2081725	2084413	2087100	2089785	2092468	2690
2108534	2111203	2113876	2116544	2119211	2674
2135178	2137833	2140487	2143139	2145789	2657
2161659	2164298	2166936	2169572	2172206	2641
2187980	2190603	2193225	2195845	2198464	2625
2214142	2216750	2219356	2221960	2224563	2609
2240148	2242740	2245331	2247920	2250507	2604
2265999	2268576	2271151	2273724	2276296	2578
2291697	2294258	2296818	2299377	2301934	2563
2317244	2319790	2322335	2324879	2327421	2548
2342641	2345173	2347703	2350242	2352780	2533
2367821	2370403	2372923	2375437	2377950	2518
2392925	2395497	2397998	2400498	2402996	2504
2417954	2420442	2422929	2425414	2427898	2489
2442771	2445245	2447718	2450189	2452658	2475
2467447	2469907	2472365	2474823	2477278	2461
2491934	2494430	2496874	2499317	2501759	2448
2516382	2518814	2521246	2523675	2526103	2434
2540645	2543063	2545481	2547897	2550312	2421
2564772	2567177	2569581	2571984	2574386	2407
2588766	2591158	2593549	2595939	2598327	2393
2612629	2615008	2617385	2619762	2622137	2381
2636361	2638727	2641092	2643455	2645817	2368



Num.	0	1	2	3	4
184	264 <sup>8</sup> 178	265 <sup>5</sup> 533	265 <sup>2</sup> 96	265 <sup>5</sup> 253	265 <sup>7</sup> 69
185	264 <sup>1</sup> 717	265 <sup>4</sup> 64	265 <sup>6</sup> 410	265 <sup>8</sup> 754	266 <sup>1</sup> 097
186	269 <sup>5</sup> 129	269 <sup>4</sup> 464	269 <sup>7</sup> 97	270 <sup>2</sup> 128	270 <sup>4</sup> 459
187	271 <sup>8</sup> 416	272 <sup>0</sup> 738	272 <sup>3</sup> 058	272 <sup>5</sup> 378	272 <sup>7</sup> 696
188	274 <sup>1</sup> 575	274 <sup>3</sup> 838	274 <sup>6</sup> 196	274 <sup>8</sup> 509	275 <sup>0</sup> 809
189	276 <sup>4</sup> 018	276 <sup>6</sup> 211	277 <sup>1</sup> 506	277 <sup>3</sup> 800	277 <sup>5</sup> 000
190	278 <sup>7</sup> 586	278 <sup>9</sup> 821	279 <sup>2</sup> 05	279 <sup>4</sup> 388	279 <sup>6</sup> 669
191	280 <sup>0</sup> 334	281 <sup>2</sup> 60	281 <sup>4</sup> 879	281 <sup>7</sup> 150	281 <sup>9</sup> 419
192	283 <sup>3</sup> 012	283 <sup>5</sup> 274	283 <sup>7</sup> 534	283 <sup>9</sup> 793	284 <sup>2</sup> 051
193	285 <sup>5</sup> 573	285 <sup>7</sup> 823	286 <sup>0</sup> 071	286 <sup>2</sup> 318	286 <sup>4</sup> 565
194	288 <sup>8</sup> 017	288 <sup>0</sup> 255	288 <sup>2</sup> 492	288 <sup>4</sup> 728	288 <sup>6</sup> 963
195	290 <sup>1</sup> 0345	290 <sup>3</sup> 273	290 <sup>5</sup> 498	290 <sup>7</sup> 722	290 <sup>9</sup> 246
196	292 <sup>2</sup> 561	292 <sup>4</sup> 76	292 <sup>6</sup> 90	292 <sup>8</sup> 223	293 <sup>0</sup> 445
197	294 <sup>3</sup> 032	294 <sup>5</sup> 266	294 <sup>7</sup> 506	294 <sup>9</sup> 741	295 <sup>1</sup> 971
198	296 <sup>4</sup> 052	296 <sup>6</sup> 285	296 <sup>8</sup> 516	297 <sup>0</sup> 747	297 <sup>2</sup> 972
199	298 <sup>5</sup> 531	298 <sup>7</sup> 763	298 <sup>9</sup> 993	299 <sup>1</sup> 223	299 <sup>3</sup> 450
200	300 <sup>6</sup> 000	300 <sup>8</sup> 231	300 <sup>1</sup> 461	300 <sup>3</sup> 690	300 <sup>5</sup> 917
201	302 <sup>7</sup> 01	302 <sup>9</sup> 241	303 <sup>1</sup> 471	303 <sup>3</sup> 700	303 <sup>5</sup> 927
202	305 <sup>8</sup> 514	305 <sup>1</sup> 745	305 <sup>3</sup> 975	306 <sup>5</sup> 205	306 <sup>7</sup> 435
203	307 <sup>9</sup> 460	307 <sup>1</sup> 690	307 <sup>3</sup> 920	308 <sup>5</sup> 150	308 <sup>7</sup> 380
204	309 <sup>0</sup> 602	309 <sup>2</sup> 832	309 <sup>4</sup> 062	309 <sup>6</sup> 292	310 <sup>8</sup> 522
205	311 <sup>1</sup> 753	311 <sup>3</sup> 983	312 <sup>5</sup> 213	312 <sup>7</sup> 443	312 <sup>9</sup> 673
206	313 <sup>2</sup> 672	313 <sup>4</sup> 902	314 <sup>6</sup> 132	314 <sup>8</sup> 362	314 <sup>1</sup> 592
207	315 <sup>3</sup> 723	315 <sup>5</sup> 953	316 <sup>7</sup> 183	316 <sup>9</sup> 413	317 <sup>1</sup> 643
208	318 <sup>4</sup> 633	318 <sup>6</sup> 863	319 <sup>8</sup> 093	319 <sup>1</sup> 323	319 <sup>3</sup> 553
209	320 <sup>5</sup> 463	320 <sup>7</sup> 693	320 <sup>9</sup> 923	321 <sup>1</sup> 153	321 <sup>3</sup> 383
210	322 <sup>6</sup> 293	322 <sup>8</sup> 523	322 <sup>1</sup> 753	322 <sup>3</sup> 983	323 <sup>5</sup> 213
211	324 <sup>7</sup> 223	324 <sup>9</sup> 453	324 <sup>1</sup> 683	324 <sup>3</sup> 913	325 <sup>5</sup> 143
212	326 <sup>8</sup> 333	326 <sup>1</sup> 563	326 <sup>3</sup> 793	326 <sup>5</sup> 023	326 <sup>7</sup> 253
213	328 <sup>9</sup> 396	328 <sup>1</sup> 626	328 <sup>3</sup> 856	328 <sup>5</sup> 086	328 <sup>7</sup> 316
214	330 <sup>0</sup> 413	330 <sup>2</sup> 643	330 <sup>4</sup> 873	331 <sup>6</sup> 103	331 <sup>8</sup> 333
215	332 <sup>1</sup> 423	332 <sup>3</sup> 653	332 <sup>5</sup> 883	333 <sup>7</sup> 113	333 <sup>9</sup> 343
216	334 <sup>2</sup> 433	334 <sup>4</sup> 663	334 <sup>6</sup> 893	335 <sup>8</sup> 123	335 <sup>1</sup> 353
217	336 <sup>3</sup> 443	336 <sup>5</sup> 673	336 <sup>7</sup> 903	337 <sup>9</sup> 133	337 <sup>1</sup> 363
218	338 <sup>4</sup> 453	338 <sup>6</sup> 683	338 <sup>8</sup> 913	339 <sup>1</sup> 143	339 <sup>3</sup> 373
219	340 <sup>5</sup> 463	340 <sup>7</sup> 693	340 <sup>9</sup> 923	341 <sup>1</sup> 153	341 <sup>3</sup> 383
220	342 <sup>6</sup> 473	342 <sup>8</sup> 703	342 <sup>1</sup> 933	343 <sup>3</sup> 163	343 <sup>5</sup> 393
221	344 <sup>7</sup> 483	344 <sup>9</sup> 713	344 <sup>1</sup> 943	345 <sup>3</sup> 173	345 <sup>5</sup> 403
222	346 <sup>8</sup> 493	346 <sup>1</sup> 723	346 <sup>3</sup> 953	347 <sup>5</sup> 183	347 <sup>7</sup> 413
223	348 <sup>9</sup> 503	348 <sup>1</sup> 733	348 <sup>3</sup> 963	349 <sup>5</sup> 193	349 <sup>7</sup> 423
224	350 <sup>0</sup> 513	350 <sup>2</sup> 743	350 <sup>4</sup> 973	351 <sup>6</sup> 203	351 <sup>8</sup> 433
225	352 <sup>1</sup> 523	352 <sup>3</sup> 753	352 <sup>5</sup> 983	353 <sup>7</sup> 213	353 <sup>9</sup> 443

5	6	7	8	9	Diff.
2659964	2662317	2664669	2667020	2669369	2355
2683439	2685780	2688119	2690457	2692794	2342
2706783	2709116	2711443	2713769	2716093	2329
2730013	2732323	2734643	2736956	2739268	2317
2753113	2755417	2757719	2760020	2762320	2304
2776222	2778523	2780823	2783122	2785420	2292
2799350	2801649	2803947	2806244	2808540	2281
2822488	2824785	2827081	2829376	2831671	2269
2845607	2847903	2850198	2852492	2854786	2256
2868710	2871005	2873299	2875592	2877885	2245
2891816	2894109	2896401	2898693	2900985	2233
2914968	2917260	2919551	2921842	2924133	2222
2938125	2940416	2942706	2944996	2947285	2211
2961282	2963572	2965861	2968150	2970439	2200
2984439	2986728	2989016	2991304	2993592	2188
3007596	3009884	3012171	3014458	3016745	2178
3039903	3042190	3044476	3046762	3049048	2167
3062250	3064536	3066821	3069106	3071391	2156
3084597	3086882	3089166	3091450	3093734	2145
3106933	3109217	3111500	3113783	3116066	2135
3129269	3131552	3133834	3136116	3138398	2124
3151605	3153887	3156168	3158449	3160729	2114
3173961	3176242	3178522	3180802	3183081	2103
3196317	3198597	3200876	3203155	3205433	2094
3218692	3220971	3223249	3225527	3227805	2084
3241067	3243345	3245622	3247899	3250176	2073
3263442	3265719	3267995	3270271	3272547	2064
3285817	3288093	3290368	3292643	3294918	2054
3308192	3310467	3312742	3315017	3317291	2044
3330567	3332842	3335116	3337390	3339664	2035
3352942	3355216	3357490	3359764	3362038	2025
3375317	3377591	3379864	3382138	3384411	2016
3397692	3400000	3402308	3404616	3406924	2006
3419967	3422275	3424583	3426891	3429199	1997
3442342	3444650	3446958	3449266	3451574	1988
3464717	3467025	3469333	3471641	3473949	1979
3487092	3489399	3491707	3494015	3496323	1970
3509467	3511775	3514083	3516391	3518699	1961
3531842	3534150	3536458	3538766	3541074	1952
3554217	3556525	3558833	3561141	3563449	1943
3576592	3578900	3581208	3583516	3585824	1934
3598967	3601275	3603583	3605891	3608199	1924
3621342	3623650	3625958	3628266	3630574	1916
3643717	3646025	3648333	3650641	3652949	1907
3666092	3668400	3670708	3673016	3675324	1898
3688467	3690775	3693083	3695391	3697699	1889
3710842	3713150	3715458	3717766	3720074	1880
3733217	3735525	3737833	3740141	3742449	1871
3755592	3757900	3760208	3762516	3764824	1862
3777967	3780275	3782583	3784891	3787199	1853
3800342	3802650	3804958	3807266	3809574	1844
3822717	3825025	3827333	3829641	3831949	1835
3845092	3847400	3849708	3852016	3854324	1826



Num.	0	1	2	3	4
226	3541084	3543006	3544926	3546845	3548764
227	3560259	3562171	3564083	3565994	3567905
228	3579348	3581253	3583156	3585059	3586961
229	3598355	3600251	3602146	3604040	3605934
230	3617278	3619166	3621053	3622939	3624825
231	3636120	3638000	3639878	3641756	3643633
232	3654830	3656751	3658622	3660492	3662361
233	3673559	3675423	3677285	3679147	3681008
234	3692159	3694014	3695869	3697723	3699576
235	3710679	3712526	3714373	3716219	3718065
236	3729120	3730960	3732799	3734637	3736475
237	3747483	3749316	3751147	3752977	3754807
238	3765769	3767594	3769418	3771240	3773062
239	3783979	3785796	3787612	3789427	3791241
240	3802112	3803922	3805730	3807538	3809343
241	3820170	3821972	3823773	3825573	3827373
242	3838154	3839948	3841741	3843534	3845326
243	3856063	3857850	3859636	3861421	3863206
244	3873898	3875678	3877457	3879235	3881012
245	3891661	3893433	3895205	3896975	3898746
246	3909351	3911116	3912880	3914644	3916407
247	3926969	3928727	3930485	3932241	3933997
248	3944517	3946268	3948013	3949767	3951516
249	3961993	3963737	3965480	3967223	3968964
250	3979400	3981137	3982873	3984608	3986343
251	3996737	3998467	4000196	4001925	4003653
252	4014005	4015728	4017451	4019172	4020893
253	4031205	4032921	4034637	4036352	4038066
254	4048337	4050047	4051755	4053464	4055171
255	4065402	4067105	4068807	4070508	4072209
256	4082400	4084096	4085791	4087486	4089180
257	4099331	4101021	4102710	4104398	4106085
258	4116197	4117880	4119562	4121244	4122925
259	4132998	4134674	4136350	4138025	4139700
260	4149733	4151404	4153073	4154742	4156410
261	4166405	4168069	4169732	4171394	4173056
262	4183013	4184670	4186327	4187983	4189638
263	4199557	4201203	4202850	4204495	4206138
264	4216039	4217684	4219328	4220972	4222614
265	4232459	4234097	4235735	4237372	4239009
266	4248816	4250449	4252081	4253712	4255342
267	4265113	4266739	4268365	4269990	4271614

5	6	7	8	9	Diff.
3550682	3552599	3554513	3556430	3558345	1918
3560813	3571723	3573630	3575537	3577443	1908
3588862	3590762	3592652	3594560	3596458	1901
3609827	3609719	3611610	3613508	3615390	1893
3626709	3628593	3630476	3632358	3634239	1884
3645510	3647386	3649260	3651134	3653007	1877
3664230	3666097	3667964	3669830	3671695	1869
3682869	3684725	3686587	3688445	3690302	1861
3701423	3703280	3705131	3706981	3708830	1852
3719509	3721353	3723206	3725048	3726879	1844
3738111	3740147	3741983	3743817	3745651	1836
3756636	3758464	3760292	3762118	3763944	1829
3774884	3776704	3778524	3780343	3782161	1822
3793055	3794868	3796680	3798492	3800302	1814
3811151	3812956	3814761	3816565	3818368	1806
3829171	3830969	3832766	3834563	3836359	1798
3847117	3848908	3850698	3852487	3854275	1791
3864990	3866773	3868555	3870337	3872118	1784
3882789	3884565	3886340	3888114	3889888	1774
3900515	3902284	3904052	3905819	3907585	1769
3918169	3919931	3921691	3923452	3925211	1762
3935752	3937506	3939250	3941013	3942765	1755
3953264	3955011	3956758	3958504	3960249	1748
3970705	3972446	3974185	3975924	3977662	1741
3988077	3989811	3991543	3993275	3995007	1734
4005380	4007106	4008832	4010557	4012282	1727
4022614	4024333	4026052	4027771	4029488	1721
4039780	4041492	4043205	4044916	4046627	1714
4056878	4058584	4060289	4061994	4063698	1707
4073929	4075608	4077307	4079005	4080703	1700
4090874	4092567	4094259	4095950	4097641	1694
4107772	4109459	4111144	4112829	4114513	1687
4124605	4126285	4127964	4129643	4131320	1680
4141374	4143047	4144719	4146391	4148063	1674
4158077	4159744	4161410	4163076	4164741	1667
4174717	4176377	4178037	4179696	4181355	1661
4191293	4192947	4194601	4196254	4197906	1655
4207806	4209454	4211101	4212748	4214394	1648
4224257	4225898	4227539	4229180	4230820	1643
4240645	4242281	4243915	4245558	4247183	1636
4256972	4258601	4260230	4261858	4263486	1630
4273238	4274861	4276484	4278106	4279727	1624



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268	4281348	4282968	4284588	4286207	4287825
269	4297523	4299137	4300751	4302364	4303976
270	4313638	4315246	4316853	4318460	4320067
271	4329693	4331295	4332897	4334498	4336098
272	4345689	4347285	4348881	4350476	4352071
273	4361626	4363217	4364807	4366396	4367985
274	4377506	4379090	4380674	4382258	4383841
275	4393327	4394906	4396484	4398062	4399639
276	4409091	4410664	4412237	4413809	4415380
277	4424798	4426365	4427932	4429499	4431065
278	4440448	4442010	4443571	4445132	4446692
279	4456042	4457598	4459154	4460709	4462264
280	4471580	4473131	4474681	4476231	4477780
281	4487063	4488608	4490153	4491697	4493241
282	4502491	4504031	4505570	4507109	4508647
283	4517864	4519399	4520932	4522466	4523998
284	4533183	4534712	4536241	4537769	4539296
285	4548442	4549972	4551495	4553018	4554540
286	4563660	4565179	4566696	4568213	4569731
287	4578819	4580332	4581844	4583356	4584868
288	4593923	4595433	4596940	4598446	4599953
289	4609078	4610481	4611983	4613484	4614985
290	4624180	4625677	4627174	4628670	4629966
291	4639230	4640722	4642214	4643705	4645195
292	4654283	4655766	4657248	4658728	4660207
293	4669336	4670813	4672289	4673764	4675238
294	4684383	4685850	4687317	4688783	4690248
295	4699422	4700889	4702354	4703819	4705283
296	4714461	4715924	4717387	4718849	4720311
297	4729500	4730959	4732418	4733876	4735333
298	4744539	4745994	4747449	4748903	4750357
299	4759578	4761030	4762482	4763934	4765386
300	4774617	4776066	4777515	4778963	4780411
301	4789656	4791102	4792548	4793993	4795438
302	4804695	4806139	4807583	4809027	4810471
303	4819734	4821177	4822620	4824063	4825506
304	4834773	4836214	4837655	4839096	4840537
305	4849812	4851251	4852691	4854131	4855571
306	4864851	4866289	4867728	4869167	4870606
307	4879890	4881327	4882765	4884203	4885641
308	4894929	4896366	4897803	4899240	4900678
309	4909967	4911403	4912839	4914275	4915711

5	6	7	8	9	Diff.
4289443	4291060	4292677	4294293	4295908	1618
4305588	4307199	4308809	4310419	4312029	1612
4321673	4323278	4324883	4326487	4328090	1606
4337768	4339298	4340896	4342494	4344092	1600
4353865	4355258	4356851	4358444	4360035	1594
4369953	4371161	4372748	4374334	4375920	1588
4386042	4387055	4388587	4390167	4391747	1582
4402126	4402792	4404363	4405943	4407517	1577
4418210	4418852	4420492	4422161	4423829	1571
4434293	4434951	4435759	4437322	4438885	1565
4450376	4450981	4451737	4452298	4453448	1560
4466459	4467062	4467825	4468477	4469029	1554
4482542	4483144	4483877	4484539	4485151	1549
4498625	4499226	4499868	4500510	4501151	1543
4514708	4515309	4515951	4516593	4517234	1537
4530791	4531382	4532023	4532664	4533305	1533
4546874	4547465	4548106	4548747	4549388	1527
4562957	4563548	4564189	4564830	4565471	1521
4579040	4579631	4580272	4580913	4581554	1515
4595123	4595714	4596355	4596996	4597637	1510
4611206	4611797	4612438	4613079	4613720	1505
4627289	4627880	4628521	4629162	4629803	1501
4643372	4643963	4644604	4645245	4645886	1495
4659455	4659996	4660637	4661278	4661919	1491
4675538	4676179	4676820	4677461	4678102	1485
4691621	4692262	4692903	4693544	4694185	1480
4707704	4708345	4708986	4709627	4710268	1475
4723787	4724428	4725069	4725710	4726351	1470
4739870	4740511	4741152	4741793	4742434	1465
4755953	4756594	4757235	4757876	4758517	1460
4772036	4772677	4773318	4773959	4774600	1455
4788119	4788760	4789401	4790042	4790683	1450
4804202	4804843	4805484	4806125	4806766	1446
4820285	4820926	4821567	4822208	4822849	1441
4836368	4836999	4837640	4838281	4838922	1436
4852451	4853092	4853733	4854374	4855015	1431
4868534	4869175	4869816	4870457	4871098	1427
4884617	4885258	4885899	4886540	4887181	1422
4900700	4901341	4901982	4902623	4903264	1417
4916783	4917424	4918065	4918706	4919347	1412
4932866	4933507	4934148	4934789	4935430	1408
4948949	4949590	4950231	4950872	4951513	1404



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310	4913617	4915018	4916418	4917818	4919217
311	4927604	4929000	4930396	4931791	4933186
312	4941545	4942938	4944329	4945720	4947110
313	4955443	4956831	4958218	4959604	4960990
314	4969256	4970679	4972062	4973444	4974825
315	4983106	4984484	4985862	4987240	4988617
316	4996871	4998245	4999619	5000992	5002365
317	5010593	5011962	5013332	5014701	5016069
318	5024271	5025637	5027002	5028366	5029731
319	5037907	5039268	5040629	5041989	5043349
310	5051500	5052857	5054213	5055569	5056925
32	5065050	5066403	5067755	5069107	5070459
32	5078559	5079907	5081255	5082603	5083950
323	5092025	5093370	5094713	5096057	5097400
324	5105450	5106790	5108130	5109469	5110808
325	5118834	5120170	5121505	5122841	5124175
326	5132176	5133508	5134840	5136171	5137501
327	5145478	5146805	5148133	5149460	5150787
328	5158738	5160062	5161386	5162709	5164031
329	5171959	5173279	5174598	5175917	5177236
330	5185139	5186455	5187771	5189086	5190400
331	5198280	5199592	5200903	5202214	5203525
332	5211381	5212689	5213996	5215303	5216610
333	5224442	5225746	5227050	5228353	5229656
334	5237465	5238765	5240064	5241364	5242663
335	5250448	5251744	5253040	5254335	5255631
336	5263393	5264685	5265977	5267269	5268560
337	5276299	5277588	5278876	5280163	5281451
338	5289167	5290452	5291736	5293020	5294303
339	5301997	5303278	5304558	5305839	5307118
340	5314789	5316066	5317343	5318619	5319895
341	5327544	5328817	5330090	5331363	5332635
342	5340261	5341531	5342800	5344069	5345338
343	5352941	5354207	5355473	5356738	5358003
344	5365584	5366847	5368109	5369370	5370631
345	5378191	5379450	5380708	5381966	5383223
346	5390761	5392016	5393271	5394525	5395779
347	5403295	5404546	5405797	5407048	5408298
348	5415792	5417040	5418288	5419535	5420781
349	5428254	5429498	5430742	5431986	5433229
350	5440680	5441921	5443161	5444401	5445641
351	5453071	5454308	5455545	5456781	5458017

5	6	7	8	9	Diff.
4920616	4922014	4923413	4924810	4926207	1339
4934380	4935974	4937363	4938761	4940154	1394
4948500	4949890	4951279	4952667	4954056	1390
4962375	4963761	4965145	4966529	4967913	1385
4976206	4977587	4978967	4980347	4981727	1381
4989994	4991370	4992746	4994121	4995495	1377
5003737	5005109	5006481	5007852	5009222	1372
5017437	5018805	5020172	5021539	5022905	1363
5031094	5032458	5033821	5035183	5036545	1363
5044709	5046068	5047426	5048785	5050142	1360
5058230	5059635	5060990	5062344	5063697	1355
5071310	5072660	5074011	5075360	5076710	1351
5085237	5086644	5087990	5089335	5090680	1347
5098743	5100085	5101427	5102768	5104109	1343
5112147	5113485	5114823	5116160	5117497	1339
5125510	5126844	5128178	5129515	5130844	1335
5138832	5140162	5141491	5142820	5144149	1331
5152113	5153439	5154764	5156089	5157414	1326
5165354	5166676	5167997	5169318	5170639	1323
5178554	5179872	5181189	5182506	5183823	1318
5191715	5193028	5194342	5195655	5196968	1315
5204835	5206145	5207455	5208764	5210073	1310
5217916	5219222	5220528	5221833	5223138	1306
5230958	5232260	5233562	5234863	5236164	1302
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5256925	5258219	5259513	5260807	5262100	1294
5269851	5271141	5272431	5273721	5275010	1291
5282758	5284042	5285311	5286596	5287882	1287
5295587	5296869	5298152	5299434	5300716	1284
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5321197	5322446	5323721	5324996	5326270	1276
5333907	5335179	5336450	5337721	5338991	1272
5346606	5347874	5349141	5350408	5351675	1268
5359267	5360532	5361795	5363059	5364322	1264
5371892	5373153	5374413	5375672	5376932	1261
5384481	5385737	5386994	5388250	5389506	1258
5397032	5398286	5399538	5400791	5402043	1253
5409548	5410793	5412047	5413296	5414544	1250
5422028	5423274	5424519	5425765	5427010	1247
5434472	5435714	5436956	5438198	5439439	1243
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355	5502283	5503507	5504730	5505952	5507174
356	5514500	5515720	5516939	5518158	5519377
357	5526682	5527898	5529114	5530330	5531545
358	5538830	5540043	5541256	5542468	5543680
359	5550944	5552154	5553362	5554572	5555781
360	5563025	5564231	5565437	5566643	5567848
361	5575073	5576275	5577477	5578680	5579881
362	5587086	5588285	5589484	5590683	5591882
363	5599066	5600262	5601458	5602654	5603849
364	5611014	5612207	5613399	5614592	5615784
365	5622029	5623218	5624407	5625595	5626783
366	5634811	5635997	5637183	5638369	5639555
367	5646661	5647844	5649027	5650209	5651392
368	5658478	5659658	5660838	5662017	5663196
369	5670264	5671440	5672617	5673793	5674969
370	5682017	5683191	5684364	5685537	5686710
371	5693739	5694910	5696080	5697249	5698419
372	5705420	5706597	5707764	5708930	5710097
373	5717088	5718252	5719416	5720580	5721743
374	5728716	5729878	5731038	5732198	5733358
375	5740313	5741471	5742628	5743786	5744943
376	5751878	5753033	5754188	5755342	5756496
377	5763413	5764565	5765717	5766868	5768019
378	5774917	5776067	5777215	5778363	5779511
379	5786392	5787538	5788683	5789828	5790973
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381	5809250	5810395	5811529	5812668	5813807
382	5820634	5821770	5822907	5824043	5825179
383	5831988	5833122	5834255	5835388	5836521
384	5843312	5844443	5845574	5846704	5847834
385	5854607	5855735	5856863	5857990	5859117
386	5865873	5866998	5868123	5869247	5870371
387	5877110	5878232	5879353	5880475	5881596
388	5888317	5889436	5890555	5891674	5892792
389	5899496	5900612	5901728	5902844	5903959
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391	5921768	5922878	5923988	5925098	5926208
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393	5943925	5945030	5946135	5947239	5948344

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397	5987905	5989099	5990092	5991186	5992279
398	5998831	5999922	6001013	6002103	6003193
399	6009729	6010817	6011903	6012993	6014081
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401	6031444	6032527	6033609	6034692	6035774
402	6042261	6043341	6044421	6045500	6046580
403	6053050	6054128	6055205	6056282	6057359
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407	6095944	6097011	6098078	6099144	6100210
408	6106602	6107666	6108730	6109794	6110857
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410	6127839	6128898	6129957	6131015	6132073
411	6138418	6139475	6140531	6141587	6142643
412	6148972	6150026	6151080	6152137	6153187
413	6159501	6160552	6161603	6162654	6163705
414	6170003	6171052	6172101	6173149	6174197
415	6180481	6181527	6182573	6183619	6184665
416	6190933	6191977	6193021	6194064	6195107
417	6201360	6202402	6203448	6204484	6205524
418	6211763	6212802	6213840	6214879	6215917
419	6222140	6223177	6224213	6225249	6226284
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422	6253124	6254153	6255182	6256211	6257239
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425	6283889	6284911	6285933	6286954	6287975
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427	6304279	6305295	6306312	6307329	6308345
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432	6354837	6355843	6356848	6357852	6358857
433	6364879	6365882	6366884	6367887	6368889
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6237660	6238693	6239725	6240757	6241789	1033
6247976	6249006	6250036	6251066	6252095	1031
6258267	6259295	6260322	6261350	6262377	1028
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443	6464037	6465017	6465997	6466977	6467957
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445	6483600	6484576	6485552	6486527	6487502
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455	6580114	6581068	6582023	6582976	6583930
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457	6599162	6600112	6601062	6602012	6602962
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465	6674530	6675463	6676397	6677331	6678264
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473	6748611	6749529	6750447	6751365	6752283
474	6757783	6758690	6759615	6760531	6761447
475	6766936	6767850	6768764	6769678	6770592
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6897527	6898414	6899301	6900188	6901074	887
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6915235	6916119	6917002	6917885	6918768	883
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7037212	7038071	7038929	7039788	7040647	857
7045794	7046652	7047509	7048366	7049223	855
7054360	7055216	7056072	7056927	7057782	854
7062910	7063764	7064611	7065461	7066314	853
7071442	7072295	7073146	7073998	7074850	850
7079957	7080808	7081659	7082509	7083359	849
7088456	7089305	7090154	7091003	7091851	848
7096939	7097786	7098633	7099480	7100327	845
7105404	7106250	7107096	7107941	7108786	844
7113854	7114698	7115543	7116385	7117229	843
7122287	7123129	7123971	7124813	7125655	841
7130703	7131544	7132385	7133225	7134065	840
7139104	7139943	7140782	7141620	7142459	838
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522	7176705	7177537	7178369	7179200	7180032
523	7185017	7185847	7186677	7187507	7188337
524	7193313	7194142	7194970	7195799	7196627
525	7201563	7202420	7203247	7204074	7204901
526	7209857	7210683	7211508	7212334	7213159
527	7218106	7218930	7219754	7220578	7221401
528	7226333	7227163	7227984	7228806	7229628
529	7234557	7235378	7236198	7237019	7237839
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531	7250945	7251763	7252581	7253398	7254215
532	7259116	7259933	7260749	7261565	7262380
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534	7275413	7276226	7277039	7277852	7278664
535	7283558	7284349	7285161	7285972	7286784
536	7291648	7292458	7293268	7294078	7294888
537	7299743	7300551	7301360	7302168	7302977
538	7307823	7308630	7309437	7310244	7311051
539	7315888	7316693	7317499	7318304	7319109
540	7323938	7324742	7325546	7326350	7327153
541	7331973	7332775	7333578	7334380	7335182
542	7339993	7340794	7341595	7342396	7343197
543	7347998	7348798	7349598	7350397	7351196
544	7355989	7356787	7357585	7358383	7359181
545	7363965	7364762	7365558	7366355	7367151
546	7371926	7372722	7373517	7374312	7375107
547	7379873	7380667	7381461	7382254	7383048
548	7387806	7388598	7389390	7390182	7390974
549	7395723	7396514	7397305	7398096	7398886
550	7403627	7404416	7405206	7405995	7406784
551	7411516	7412304	7413092	7413880	7414668
552	7419391	7420177	7420964	7421750	7422537
553	7427251	7428037	7428822	7429607	7430392
554	7435098	7435881	7436665	7437449	7438232
555	7442930	7443712	7444495	7445277	7446059
556	7450748	7451529	7452310	7453091	7453871
557	7458552	7459332	7460111	7460890	7461670
558	7466342	7467120	7467898	7468676	7469454
559	7474118	7474895	7475672	7476448	7477225
560	7481880	7482656	7483431	7484206	7484981
561	7489629	7490403	7491177	7491950	7492724

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7180863	7181694	7182525	7183356	7184186	831
7189167	7189996	7190826	7191655	7192484	830
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7213984	7214809	7215633	7216458	7217282	825
7222225	7223048	7223871	7224694	7225517	824
7230450	7231272	7232093	7232914	7233736	822
7238660	7239480	7240300	7241120	7241939	821
7246854	7247672	7248491	7249309	7250127	819
7255033	7255850	7256667	7257483	7258300	818
7263196	7264012	7264827	7265642	7266457	816
7271344	7272158	7272972	7273786	7274599	814
7279477	7280290	7281101	7281914	7282726	813
7287595	7288406	7289216	7290027	7290838	811
7295697	7296507	7297316	7298125	7298934	809
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7319914	7320719	7321524	7322329	7323133	805
7327957	7328760	7329564	7330367	7331170	804
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7343997	7344798	7345598	7346398	7347198	800
7351695	7352494	7353293	7354092	7354891	799
7359979	7360776	7361574	7362371	7363168	798
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7375902	7376696	7377491	7378285	7379079	795
7383841	7384634	7385427	7386220	7387013	793
7391766	7392558	7393350	7394141	7394932	792
7399677	7400467	7401257	7402047	7402837	791
7407573	7408362	7409151	7409939	7410728	789
7415455	7416243	7417030	7417817	7418604	787
7423323	7424109	7424895	7425680	7426465	786
743116	7431946	7432735	7433523	7434311	784
7439015	7439799	7440582	7441365	7442147	783
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7454652	7455432	7456212	7456992	7457772	781
7462449	7463228	7464006	7464785	7465564	779
7470232	7471009	7471787	7472564	7473341	778
7478001	7478777	7479553	7480329	7481105	776
7485756	7486531	7487306	7488080	7488854	775
7493498	7494271	7495044	7495817	7496590	774



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565	7522044	7522815	7523585	7524355	7525125
566	7528164	7528934	7529704	7530474	7531244
567	7535831	7536601	7537371	7538141	7538911
568	7543483	7544253	7545023	7545793	7546563
569	7551123	7551893	7552663	7553433	7554203
570	7558749	7559519	7560289	7561059	7561829
571	7566361	7567131	7567901	7568671	7569441
572	7573966	7574736	7575506	7576276	7577046
573	7581546	7582316	7583086	7583856	7584626
574	7589119	7589889	7590659	7591429	7592199
575	7596688	7597458	7598228	7598998	7599768
576	7604225	7604995	7605765	7606535	7607305
577	7611758	7612528	7613298	7614068	7614838
578	7619278	7620048	7620818	7621588	7622358
579	7626783	7627553	7628323	7629093	7629863
580	7634280	7635050	7635820	7636590	7637360
581	7641761	7642531	7643301	7644071	7644841
582	7649230	7649999	7650769	7651539	7652309
583	7656806	7657576	7658346	7659116	7659886
584	7664128	7664898	7665668	7666438	7667208
585	7671539	7672309	7673079	7673849	7674619
586	7678966	7679736	7680506	7681276	7682046
587	7686381	7687151	7687921	7688691	7689461
588	7693773	7694543	7695313	7696083	7696853
589	7701153	7701923	7702693	7703463	7704233
590	7708520	7709290	7710060	7710830	7711600
591	7715875	7716645	7717415	7718185	7718955
592	7723217	7723987	7724757	7725527	7726297
593	7730547	7731317	7732087	7732857	7733627
594	7737864	7738634	7739404	7740174	7740944
595	7745170	7745940	7746710	7747480	7748250
596	7752463	7753233	7754003	7754773	7755543
597	7759743	7760513	7761283	7762053	7762823
598	7767012	7767782	7768552	7769322	7770092
599	7774268	7775038	7775808	7776578	7777348
600	7781513	7782283	7783053	7783823	7784593
601	7788745	7789515	7790285	7791055	7791825
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7524326	7525094	7525862	7526629	7527397	768
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7539599	7540364	7541129	7541894	7542659	766
7547305	7548069	7548832	7549596	7550359	764
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7562536	7563298	7564059	7564820	7565580	761
7570162	7570922	7571682	7572441	7573201	760
7577755	7578513	7579272	7580030	7580788	759
7585334	7586091	7586848	7587605	7588362	757
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7638022	7638770	7639518	7640266	7641014	748
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7652959	7653705	7654450	7655195	7655941	745
7660409	7661153	7661897	7662641	7663385	744
7667845	7668588	7669331	7670074	7670816	743
7675269	7676011	7676752	7677494	7678235	742
7682635	7683371	7684101	7684840	7685579	741
7690009	7690748	7691487	7692226	7692965	740
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7734207	7734939	7735670	7736402	7737133	732
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7748818	7749547	7750276	7751005	7751734	730
7756104	7756832	7757560	7758288	7759016	728
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7770642	7771367	7772093	7772818	7773543	726
7777892	7778616	7779340	7780065	7780789	725
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607	7812387	7813102	7813817	7814533	7815248
608	7813003	7813717	7814431	7815147	7815862
609	7813617	7814331	7815045	7815761	7816475
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611	7814845	7815559	7816273	7816987	7817701
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615	7817301	7818015	7818729	7819443	7820157
616	7817915	7818629	7819343	7820057	7820771
617	7818529	7819243	7819957	7820671	7821385
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619	7819757	7820471	7821185	7821899	7822613
620	7820371	7821085	7821799	7822513	7823227
621	7820985	7821699	7822413	7823127	7823841
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624	7822827	7823541	7824259	7824973	7825683
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626	7824055	7824769	7825483	7826201	7826915
627	7824669	7825383	7826015	7826815	7827529
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631	7827125	7827839	7828453	7829167	7829881
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633	7828353	7829067	7830181	7830895	7831609
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635	7829581	7830295	7831413	7832123	7832837
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648	8122447	8123116	8123785	8124454	8125123
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650	8135810	8136477	8137144	8137811	8138478
651	8142476	8143142	8143808	8144474	8145140
652	8149132	8149797	8150462	8151127	8151791
653	8155777	8156441	8157105	8157769	8158433
654	8162413	8163076	8163739	8164402	8165064
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659	8195439	8196097	8196755	8197413	8198071
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661	8208580	8209236	8209892	8210548	8211203
662	8215135	8215790	8216445	8217100	8217755
663	8221681	8222335	8222989	8223643	8224296
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665	8234742	8235394	8236046	8236698	8237350
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667	8247765	8248415	8249065	8249715	8250364
668	8254261	8254910	8255559	8256208	8256857
669	8260748	8261396	8262044	8262692	8263340
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671	8273693	8274339	8274985	8275631	8276277
672	8280151	8280796	8281441	8282086	8282731
673	8286599	8287243	8287887	8288532	8289176
674	8293038	8293681	8294324	8294967	8295611
675	8299467	8300109	8300752	8301394	8302036
676	8305885	8306528	8307170	8307811	8308452
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678	8318698	8319337	8319977	8320616	8321255
679	8325089	8325728	8326366	8327005	8327643
680	8331471	8332109	8332746	8333384	8334021
681	8337844	8338480	8339117	8339754	8340390
682	8344207	8344843	8345479	8346114	8346750
683	8350561	8351196	8351831	8352465	8353100
684	8356906	8357540	8358174	8358807	8359441
685	8363241	8363874	8364507	8365140	8365773
686	8369567	8370199	8370832	8371463	8372095

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8125792	8126460	8127129	8127797	8128465	669
8132473	8133141	8133808	8134475	8135143	668
8139144	8139811	8140477	8141144	8141810	667
8145805	8146471	8147136	8147801	8148467	666
8152456	8153120	8153785	8154449	8155113	665
8159096	8159760	8160423	8161087	8161750	664
8165727	8166389	8167052	8167714	8168376	663
8172347	8173009	8173670	8174331	8174993	662
8178958	8179618	8180278	8180939	8181599	661
8185558	8186217	8186877	8187536	8188195	660
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8198723	8199386	8200043	8200700	8201358	658
8205298	8205955	8206611	8207268	8207924	657
8211859	8212514	8213170	8213825	8214480	656
8218409	8219064	8219718	8220372	8221027	655
8224950	8225603	8226257	8226910	8227563	654
8231481	8232133	8232786	8233438	8234090	653
8238002	8238653	8239305	8239956	8240607	652
8244513	8245163	8245814	8246464	8247114	651
8251014	8251664	8252313	8252963	8253612	650
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8263983	8264635	8265283	8265931	8266578	648
8270460	8271107	8271753	8272400	8273046	647
8276923	8277569	8278214	8278860	8279505	646
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8296254	8296896	8297539	8298182	8298824	643
8302678	8303320	8303962	8304603	8305245	642
8309093	8309734	8310375	8311016	8311656	641
8315499	8316139	8316778	8317418	8318058	640
8321895	8322534	8323173	8323812	8324450	639
8328281	8328919	8329558	8330195	8330833	638
8334659	8335296	8335933	8336570	8337207	637
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8347385	8348021	8348656	8349291	8349926	635
8353735	8354369	8355003	8355638	8356272	634
8360075	8360708	8361341	8361975	8362608	633
8366405	8367038	8367670	8368303	8368935	632
8372727	8373359	8373990	8374622	8375253	631



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685	838491	8389120	839050	8390379	8391008
686	8394710	8395419	839637	8396666	8397294
687	8401061	8401683	8402316	8402943	8403571
688	8407332	8407951	8408586	8409212	8409838
689	8413595	8414220	8414846	8415472	8416097
690	8419848	8420473	8421098	8421722	8422347
691	8426092	8426716	8427340	8427964	8428588
692	8432323	8432943	8433574	8434197	8434819
693	8438554	8439176	8439799	8440420	8441042
694	8444772	8445393	8446014	8446635	8447256
695	8450990	8451601	8452221	8452841	8453461
696	8457180	8457800	8458419	8459038	8459658
697	8463371	8463990	8464608	8465227	8465845
698	8469553	8470171	8470789	8471406	8472024
699	8475744	8476363	8476981	8477598	8478214
700	8481929	8482547	8483163	8483779	8484395
701	8488047	8488662	8489277	8489892	8490507
702	8494294	8494908	8495523	8496137	8496751
703	8500433	8501046	8501659	8502272	8502886
704	8506562	8507175	8507787	8508399	8509012
705	8512683	8513295	8513907	8514518	8515130
706	8518806	8519417	8520028	8520639	8521250
707	8524920	8525531	8526142	8526753	8527364
708	8531033	8531644	8532255	8532866	8533477
709	8537142	8537753	8538364	8538975	8539586
710	8543250	8543861	8544472	8545083	8545694
711	8549359	8549970	8550581	8551192	8551803
712	8555468	8556079	8556690	8557301	8557912
713	8561577	8562188	8562799	8563410	8564021
714	8567686	8568297	8568908	8569519	8570130
715	8573795	8574406	8575017	8575628	8576239
716	8579904	8580515	8581126	8581737	8582348
717	8586013	8586624	8587235	8587846	8588457
718	8592122	8592733	8593344	8593955	8594566
719	8598231	8598842	8599453	8599964	8600575
720	8604340	8604951	8605562	8606173	8606784
721	8610449	8611060	8611671	8612282	8612893
722	8616558	8617169	8617780	8618391	8618902
723	8622667	8623278	8623889	8624490	8625101
724	8628776	8629387	8629998	8630609	8631220
725	8634885	8635496	8636107	8636718	8637329
726	8640994	8641605	8642216	8642827	8643438
727	8647103	8647714	8648325	8648936	8649547
728	8653212	8653823	8654434	8655045	8655656
729	8659321	8659932	8660543	8661154	8661765

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8416722	8417348	8417973	8418598	8419223	625
8422971	8423596	8424220	8424844	8425468	624
8429211	8429835	8430459	8431081	8431705	623
8435442	8436065	8436687	8437310	8437932	623
8441664	8442286	8442907	8443529	8444150	622
8447877	8448498	8449119	8449739	8450360	621
8454081	8454701	8455321	8455941	8456561	620
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8466463	8467081	8467699	8468318	8468935	618
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8484970	8485586	8486201	8486817	8487432	615
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733	86341040	8634700	8635296	8635891	8636486
734	86341961	8634792	8635391	8635986	8636581
735	86342873	8634884	8635486	8636081	8636676
736	86343788	8634975	8635581	8636176	8636771
737	86344695	8635062	8635676	8636271	8636866
738	86345604	8635153	8635771	8636366	8636961
739	86346511	8635244	8635866	8636461	8637056
740	86347417	8635335	8635961	8636556	8637151
741	86348322	8635426	8636056	8636651	8637246
742	86349229	8635517	8636151	8636746	8637341
743	86350133	8635608	8636246	8636841	8637436
744	86351039	8635699	8636341	8636936	8637531
745	86351944	8635790	8636436	8637031	8637626
746	86352849	8635881	8636531	8637126	8637721
747	86353754	8635972	8636626	8637221	8637816
748	86354659	8636063	8636721	8637316	8637911
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752	86358279	8636427	8637101	8637696	8638291
753	86359184	8636518	8637196	8637791	8638386
754	86360089	8636609	8637291	8637886	8638481
755	86360994	8636700	8637386	8637981	8638576
756	86361899	8636791	8637481	8638076	8638671
757	86362804	8636882	8637576	8638171	8638766
758	86363709	8636973	8637671	8638266	8638861
759	86364614	8637064	8637766	8638361	8638956
760	86365519	8637155	8637861	8638456	8639051
761	86366424	8637246	8637956	8638551	8639146
762	86367329	8637337	8638051	8638646	8639241
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764	86369139	8637519	8638241	8638836	8639431
765	86370044	8637610	8638336	8638931	8639526
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767	86371854	8637792	8638526	8639121	8639716
768	86372759	8637883	8638621	8639216	8639811
769	86373664	8637974	8638716	8639311	8639906
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771	86375474	8638156	8638906	8639501	8640096

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8695351	8695937	8696523	8697108	8697693	587
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8709565	8705149	87-08134	8708719	8709304	585
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8-18647	8719250	8719834	8720419	8720980	583
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8799556	8800128	8800701	8801273	8801846	573
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775	8893017	8893577	8894138	8894698	8895258
776	8898617	8899177	8899736	8900296	8900855
777	8904210	8904769	8905328	8905887	8906445
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779	8915375	8915932	8916489	8917047	8917604
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781	8926510	8927066	8927622	8928178	8928734
782	8932068	8932623	8933178	8933733	8934288
783	8937613	8938168	8938722	8939277	8939832
784	8943161	8943715	8944268	8944822	8945376
785	8948697	8949250	8949803	8950356	8950909
786	8954225	8954778	8955330	8955883	8956435
787	8959747	8960299	8960851	8961403	8961954
788	8965262	8965813	8966364	8966915	8967466
789	8970770	8971320	8971871	8972421	8972971
790	8976271	8976821	8977370	8977920	8978469
791	8981765	8982314	8982863	8983412	8983960
792	8987252	8987800	8988348	8988897	8989445
793	8992732	8993279	8993827	8994375	8994922
794	8998205	8998752	8999299	8999846	9000392
795	9003671	9004218	9004764	9005310	9005856
796	9009131	9009676	9010222	9010767	9011313
797	9014583	9015128	9015673	9016218	9016762
798	9020029	9020573	9021117	9021661	9022205
799	9025468	9026011	9026555	9027098	9027641
800	9030900	9031443	9031985	9032528	9033071
801	9036325	9036867	9037409	9037951	9038493
802	9041744	9042285	9042827	9043368	9043909
803	9047155	9047696	9048237	9048778	9049318
804	9052560	9053101	9053641	9054181	9054721
805	9057960	9058498	9059038	9059577	9060116
806	9063351	9063889	9064428	9064967	9065505
807	9068735	9069272	9069812	9070350	9070888
808	9074114	9074651	9075188	9075726	9076263
809	9079485	9080022	9080559	9081095	9081632
810	9084850	9085386	9085922	9086458	9086994
811	9090209	9090744	9091279	9091815	9092350
812	9095560	9096095	9096630	9097165	9097700
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8956937	8957489	8958042	8958594	8959145	552
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818	9127533	9128064	9128595	9129126	9129656
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820	9138139	9138668	9139198	9139727	9140257
821	9143432	9143961	9144489	9145018	9145547
822	9148718	9149245	9149775	9150303	9150831
823	9153998	9154526	9155054	9155581	9156109
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827	9175055	9175580	9176105	9176630	9177155
828	9180303	9180828	9181352	9181877	9182401
829	9185545	9186069	9186593	9187117	9187640
830	9190781	9191304	9191827	9192350	9192873
831	9196010	9196533	9197055	9197578	9198100
832	9201233	9201755	9202277	9202799	9203321
833	9206450	9206971	9207493	9208014	9208535
834	9211661	9212181	9212702	9213222	9213743
835	9216865	9217385	9217905	9218425	9218945
836	9222063	9222582	9223102	9223621	9224140
837	9227255	9227773	9228292	9228811	9229330
838	9232440	9232958	9233477	9233995	9234513
839	9237620	9238137	9238655	9239172	9239690
840	9242793	9243310	9243827	9244344	9244860
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843	9258276	9258791	9259306	9259821	9260336
844	9263424	9263939	9264453	9264968	9265482
845	9268567	9269081	9269595	9270109	9270622
846	9273704	9274217	9274730	9275243	9275757
847	9279834	9279347	9279859	9280372	9280885
848	9284959	9284471	9284983	9285495	9286007
849	9289077	9289588	9290100	9290611	9291123
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852	9304396	9304906	9305415	9305925	9306434
853	9309490	9309999	9310508	9311017	9311526
854	9314579	9315087	9315596	9316104	9316612
855	9319661	9320169	9320677	9321185	9321692

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9114240	9114772	9115305	9115837	9116369	533
9119562	9120094	9120626	9121157	9121689	532
9124883	9125415	9125947	9126478	9127009	532
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9135490	9136019	9136549	9137079	9137609	530
9140786	9141315	9141844	9142373	9142903	529
9146076	9146604	9147133	9147661	9148190	529
9151359	9151887	9152415	9152943	9153471	528
9156636	9157163	9157691	9158218	9158745	527
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9167171	9167697	9168223	9168749	9169275	526
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9177680	9178205	9178730	9179254	9179779	525
9182925	9183449	9183973	9184497	9185021	524
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9193396	9193919	9194442	9194965	9195488	523
9198623	9199145	9199667	9200189	9200711	523
9205842	9206364	9206886	9207407	9207929	521
9211098	9211619	9212140	9212661	9213182	521
9218426	9218947	9219468	9220000	9220521	520
9224659	9225179	9225698	9226217	9226736	519
9229848	9230367	9230885	9231404	9231922	518
9235031	9235549	9236066	9236584	9237102	518
9240208	9240724	9241242	9241759	9242276	518
9245377	9245894	9246410	9246927	9247444	517
9250541	9251057	9251573	9252089	9252605	516
9255699	9256215	9256730	9257245	9257761	515
9260851	9261366	9261880	9262395	9262910	515
9265997	9266511	9267025	9267539	9268053	515
9271136	9271650	9272163	9272677	9273190	514
9276270	9276783	9277296	9277808	9278321	513
9281397	9281909	9282422	9282934	9283446	512
9286518	9287030	9287542	9288054	9288565	511
9291634	9292145	9292656	9293167	9293678	511
9296743	9297254	9297764	9298275	9298785	511
9301847	9302357	9302866	9303376	9303886	510
9306944	9307453	9307963	9308472	9308981	510
9312035	9312544	9313053	9313561	9314070	509
9317121	9317629	9318137	9318645	9319153	509
9322200	9322708	9323215	9323723	9324230	508



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857	9324848	9325355	9325862	9326369	9326877
858	9324958	9325465	9325972	9326479	9326987
859	9325068	9325575	9326082	9326589	9327097
860	9325178	9325685	9326192	9326699	9327207
861	9325288	9325795	9326302	9326809	9327317
862	9325398	9325905	9326412	9326919	9327427
863	9325508	9326015	9326522	9327029	9327537
864	9325618	9326125	9326632	9327139	9327647
865	9325728	9326235	9326742	9327249	9327757
866	9325838	9326345	9326852	9327359	9327867
867	9325948	9326455	9326962	9327469	9327977
868	9326058	9326565	9327072	9327579	9328087
869	9326168	9326675	9327182	9327689	9328197
870	9326278	9326785	9327292	9327799	9328307
871	9326388	9326895	9327402	9327909	9328417
872	9326498	9327005	9327512	9328019	9328527
873	9326608	9327115	9327622	9328129	9328637
874	9326718	9327225	9327732	9328239	9328747
875	9326828	9327335	9327842	9328349	9328857
876	9326938	9327445	9327952	9328459	9328967
877	9327048	9327555	9328062	9328569	9329077
878	9327158	9327665	9328172	9328679	9329187
879	9327268	9327775	9328282	9328789	9329297
880	9327378	9327885	9328392	9328899	9329407
881	9327488	9327995	9328502	9329009	9329517
882	9327598	9328105	9328612	9329119	9329627
883	9327708	9328215	9328722	9329229	9329737
884	9327818	9328325	9328832	9329339	9329847
885	9327928	9328435	9328942	9329449	9329957
886	9328038	9328545	9329052	9329559	9330067
887	9328148	9328655	9329162	9329669	9330177
888	9328258	9328765	9329272	9329779	9330287
889	9328368	9328875	9329382	9329889	9330397
890	9328478	9328985	9329492	9330000	9330507
891	9328588	9329095	9329602	9330110	9330617
892	9328698	9329205	9329712	9330220	9330727
893	9328808	9329315	9329822	9330330	9330837
894	9328918	9329425	9329932	9330440	9330947
895	9329028	9329535	9330042	9330550	9331057
896	9329138	9329645	9330152	9330660	9331167
897	9329248	9329755	9330262	9330770	9331277

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9327274	9327781	9328288	9328795	9329301	507
9332341	9332848	9333354	9333860	9334367	506
9337403	9337909	9338415	9338920	9339426	505
9342459	9342964	9343469	9343974	9344479	506
9347509	9348013	9348518	9349022	9349527	505
9352553	9353057	9353561	9354065	9354569	504
9357551	9358055	9358558	9359061	9359565	504
9362623	9363126	9363629	9364132	9364635	503
9367650	9368152	9368655	9369157	9369659	502
9372671	9373172	9373674	9374176	9374677	502
9377635	9378137	9378638	9379139	9379640	502
9382693	9383195	9383696	9384196	9384697	501
9387698	9388198	9388698	9389198	9389698	500
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9397638	9398137	9398635	9399134	9399633	499
9402664	9403162	9403660	9404159	9404657	498
9407654	9408152	9408650	9409147	9409645	497
9412621	9413116	9413623	9414119	9414617	497
9417598	9418095	9418591	9419088	9419584	497
9422551	9423053	9423554	9424049	9424545	496
9427510	9428015	9428510	9429005	9429501	495
9432471	9432966	9433461	9433956	9434450	495
9437413	9437912	9438406	9438900	9439395	494
9442353	9442852	9443346	9443840	9444333	494
9447294	9447787	9448280	9448773	9449266	494
9452223	9452716	9453203	9453691	9454183	493
9457147	9457639	9458131	9458623	9459115	492
9462066	9462557	9463048	9463540	9464031	492
9466978	9467469	9467960	9468451	9468942	491
9471886	9472376	9472866	9473357	9473847	491
9476787	9477277	9477767	9478257	9478747	490
9481684	9482173	9482662	9483151	9483641	490
9486574	9487063	9487552	9488040	9488529	489
9491460	9491948	9492436	9492924	9493412	489
9496330	9496817	9497304	9497792	9498279	488
9501213	9501691	9502173	9502655	9503138	487
9506082	9506569	9507051	9507532	9508012	486
9510946	9511432	9511913	9512394	9512873	486
9515803	9516289	9516774	9517250	9517735	485
9520656	9521141	9521624	9522101	9522595	485
9525503	9525987	9526472	9526956	9527440	485
9530345	9530828	9531312	9531796	9532280	484



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899	9537597	9538080	9538563	9539046	9539529
900	9542425	9542908	9543390	9543872	9544355
901	9547248	9547730	9548212	9548694	9549176
902	9552065	9552547	9553028	9553510	9553991
903	9556877	9557358	9557839	9558320	9558801
904	9561684	9562165	9562645	9563125	9563605
905	9566486	9566966	9567445	9567925	9568405
906	9571282	9571761	9572241	9572720	9573199
907	9576073	9576552	9577030	9577509	9577988
908	9580858	9581337	9581815	9582293	9582771
909	9585639	9586117	9586594	9587072	9587549
910	9590414	9590891	9591368	9591845	9592322
911	9595184	9595660	9596137	9596614	9597090
912	9599948	9600425	9600901	9601377	9601853
913	9604708	9605183	9605659	9606135	9606610
914	9609462	9609937	9610412	9610887	9611362
915	9614211	9614686	9615160	9615635	9616109
916	9618955	9619429	9619903	9620377	9620851
917	9623693	9624167	9624640	9625114	9625587
918	9628427	9628900	9629373	9629846	9630319
919	9633155	9633628	9634100	9634573	9635045
920	9637878	9638350	9638822	9639294	9639766
921	9642596	9643068	9643539	9644011	9644482
922	9647309	9647780	9648251	9648722	9649193
923	9652017	9652488	9652958	9653428	9653899
924	9656720	9657190	9657660	9658130	9658599
925	9661417	9661887	9662356	9662826	9663295
926	9666110	9666579	9667048	9667517	9667985
927	9670797	9671266	9671734	9672203	9672671
928	9675480	9675948	9676416	9676883	9677351
929	9680157	9680625	9681092	9681559	9682027
930	9684829	9685296	9685763	9686230	9686697
931	9689497	9689963	9690430	9690896	9691362
932	9694159	9694625	9695091	9695557	9696023
933	9698816	9699282	9699747	9700213	9700678
934	9703469	9703934	9704399	9704863	9705328
935	9708116	9708581	9709045	9709509	9709974
936	9712758	9713222	9713686	9714150	9714614
937	9717396	9717859	9718323	9718786	9719249
938	9722028	9722491	9722954	9723417	9723880
939	9726656	9727118	9727581	9728043	9728506

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9540012	9540494	9540977	9541460	9541943	483
9544837	9545319	9545802	9546284	9546766	482
9549657	9550139	9550621	9551102	9551584	481
9554472	9554953	9555434	9555915	9556397	480
9559282	9559762	9560243	9560723	9561204	479
9564086	9564566	9565046	9565526	9566006	478
9568885	9569364	9569844	9570323	9570803	477
9573678	9574157	9574636	9575115	9575594	476
9578466	9578945	9579423	9579902	9580380	475
9583249	9583727	9584205	9584683	9585161	474
9588027	9588505	9588982	9589459	9589937	473
9592799	9593276	9593753	9594230	9594707	472
9597567	9598043	9598520	9598996	9599472	471
9602305	9602780	9603256	9603731	9604206	470
9607086	9607561	9608036	9608511	9608987	469
9611837	9612312	9612787	9613261	9613736	468
9616583	9617058	9617532	9618006	9618481	467
9621325	9621799	9622272	9622746	9623220	466
9626061	9626534	9627007	9627481	9627954	465
9630792	9631264	9631737	9632210	9632683	464
9635517	9635990	9636462	9636934	9637406	463
9640238	9640710	9641181	9641653	9642125	462
9644953	9645425	9645896	9646367	9646838	461
9649664	9650134	9650605	9651076	9651546	460
9654369	9654839	9655309	9655780	9656250	459
9659069	9659539	9660009	9660478	9660948	458
9663764	9664233	9664703	9665172	9665641	457
9668454	9668923	9669392	9669860	9670329	456
9673167	9673637	9674106	9674574	9675042	455
9677819	9678287	9678754	9679222	9679690	454
9682494	9682961	9683428	9683895	9684362	453
9687164	9687630	9688097	9688564	9689030	452
9691829	9692295	9692761	9693227	9693693	451
9696488	9696954	9697420	9697885	9698351	450
9701143	9701608	9702074	9702539	9703004	449
9705793	9706258	9706722	9707187	9707652	448
9710438	9710902	9711366	9711830	9712294	447
9715078	9715542	9716005	9716469	9716932	446
9719713	9720176	9720639	9721102	9721565	445
9724343	9724805	9725268	9725731	9726193	444
9728968	9729430	9729892	9730354	9730816	443



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941	9733896	9736358	9736819	9737281	9737742
942	9740509	9740970	9741431	9741892	9742353
943	9745117	9745577	9746038	9746498	9746959
944	9749720	9750180	9750640	9751100	9751560
945	9754318	9754778	9755237	9755697	9756156
946	9758911	9759370	9759829	9760288	9760747
947	9763500	9763958	9764417	9764875	9765334
948	9768083	9768541	9768999	9769457	9769915
949	9772662	9773120	9773577	9774035	9774492
950	9777236	9777693	9778150	9778607	9779064
951	9781805	9782262	9782718	9783175	9783631
952	9786369	9786826	9787282	9787738	9788194
953	9790929	9791385	9791840	9792296	9792751
954	9795484	9795939	9796394	9796849	9797304
955	9800034	9800488	9800943	9801398	9801852
956	9804579	9805033	9805487	9805942	9806396
957	9809119	9809573	9810027	9810481	9810934
958	9813655	9814108	9814562	9815015	9815468
959	9818186	9818639	9819092	9819544	9819997
960	9822712	9823165	9823617	9824069	9824522
961	9827234	9827686	9828138	9828589	9829041
962	9831751	9832202	9832654	9833105	9833556
963	9836263	9836714	9837165	9837616	9838066
964	9840770	9841221	9841671	9842122	9842572
965	9845273	9845723	9846173	9846623	9847073
966	9849771	9850221	9850670	9851120	9851569
967	9854265	9854714	9855163	9855612	9856061
968	9858754	9859202	9859651	9860099	9860548
969	9863238	9863686	9864134	9864582	9865030
970	9867717	9868165	9868613	9869060	9869508
971	9872192	9872640	9873087	9873534	9873981
972	9876663	9877109	9877556	9878003	9878449
973	9881128	9881575	9882021	9882467	9882913
974	9885590	9886035	9886481	9886927	9887373
975	9890046	9890492	9890937	9891382	9891828
976	9894498	9894943	9895388	9895833	9896278
977	9898946	9899390	9899835	9900279	9900723
978	9903389	9903833	9904277	9904721	9905164
979	9907827	9908270	9908714	9909158	9909601
980	9912261	9912704	9913147	9913590	9914033
981	9916690	9917133	9917575	9918018	9918461

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9738203	9738664	9739126	9739587	9740048	461
9742814	9743274	9743735	9744196	9744656	461
9747419	9747879	9748340	9748800	9749260	460
9752020	9752479	9752939	9753399	9753858	460
9756615	9757075	9757534	9757993	9758452	459
9761206	9761665	9762124	9762582	9763041	459
9765792	9766251	9766709	9767167	9767625	458
9770373	9770831	9771289	9771747	9772204	458
9774950	9775407	9775864	9776322	9776779	458
9779521	9779978	9780435	9780892	9781348	457
9784088	9784544	9785001	9785457	9785913	457
9788650	9789106	9789562	9790017	9790473	456
9793207	9793662	9794118	9794573	9795028	456
9797759	9798214	9798669	9799124	9799579	455
9802307	9802761	9803216	9803670	9804125	455
9806850	9807304	9807758	9808212	9808666	454
9811388	9811841	9812295	9812748	9813202	454
9815921	9816374	9816827	9817280	9817733	453
9820450	9820902	9821355	9821807	9822260	453
9824974	9825426	9825878	9826330	9826782	452
9829493	9829945	9830396	9830848	9831299	452
9834007	9834459	9834910	9835361	9835812	451
9838517	9838968	9839419	9839869	9840320	451
9843022	9843473	9843923	9844373	9844823	450
9847523	9847973	9848422	9848872	9849322	450
9852019	9852468	9852917	9853366	9853816	450
9856510	9856959	9857407	9857856	9858305	449
9860996	9861445	9861893	9862341	9862790	448
9865478	9865926	9866374	9866822	9867270	448
9869955	9870403	9870850	9871298	9871745	447
9874428	9874875	9875322	9875769	9876216	447
9878896	9879343	9879789	9880236	9880682	447
9883360	9883806	9884252	9884698	9885144	446
9887818	9888264	9888710	9889155	9889601	446
9892273	9892718	9893163	9893608	9894050	445
9896722	9897167	9897612	9898056	9898501	445
9901168	9901612	9902056	9902500	9902944	444
9905608	9906052	9906496	9906940	9907383	444
9910044	9910488	9910931	9911374	9911818	443
9914476	9914919	9915362	9915805	9916247	443
9918903	9919345	9919788	9920230	9920673	442



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983	9925535	9925977	9926419	9926860	9927302
984	9929951	9930392	9930834	9931275	9931716
985	9934362	9934803	9935244	9935685	9936126
986	9938769	9939210	9939650	9940090	9940531
987	9943172	9943612	9944051	9944491	9944931
988	9947569	9948009	9948448	9948888	9949327
989	9951963	9952402	9952841	9953280	9953719
990	9956352	9956791	9957229	9957668	9958106
991	9960737	9961175	9961613	9962051	9962489
992	9965117	9965554	9965992	9966430	9966868
993	9969492	9969930	9970367	9970804	9971242
994	9973861	9974301	9974738	9975174	9975611
995	9978231	9978667	9979104	9979540	9979976
996	9982593	9983029	9983465	9983901	9984337
997	9986952	9987387	9987823	9988258	9988694
998	9991305	9991740	9992176	9992611	9993046
999	9995655	9996090	9996524	9996959	9997393

The END of

5	6	7	8	9	Dif.
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9927744	9928185	9928627	9929068	9929510	442
9932157	9932598	9933039	9933480	9933921	441
9936566	9937007	9937448	9937888	9938329	441
9940971	9941411	9941851	9942291	9942731	440
9945371	9945811	9946251	9946690	9947130	440
9949767	9950206	9950645	9951085	9951524	440
9954158	9954597	9955036	9955474	9955913	439
9958545	9958983	9959422	9959860	9960298	439
9962927	9963365	9963803	9964241	9964679	438
9967305	9967743	9968180	9968618	9969055	438
9971679	9972116	9972553	9972990	9973427	437
9976048	9976485	9976921	9977358	9977794	437
9980413	9980849	9981285	9981721	9982157	437
9984773	9985209	9985645	9986080	9986516	436
9989129	9989564	9990000	9990435	9990870	435
9993481	9993916	9994350	9994785	9995220	435
9997828	9998262	9998697	9999131	9999566	435

the LOGARITHMS.



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A  
TABLE  
OF  
Proportional Parts.

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Diff.	1	2	3	4	5	6	7	8	9
44	4	9	13	18	22	26	31	35	40
46	5	9	14	18	23	28	32	37	41
48	5	10	14	19	24	29	34	38	43
50	5	10	15	20	25	30	35	40	45
52	5	10	16	21	26	31	36	42	47
54	5	11	16	22	27	32	38	43	49
56	6	11	17	22	28	34	39	45	50
58	6	12	17	23	29	35	41	46	52
60	6	12	18	24	30	36	42	48	54
62	6	12	19	25	31	37	43	50	56
64	6	13	19	26	32	38	45	51	58
66	7	13	20	26	33	40	46	53	59
68	7	14	20	27	34	41	48	54	61
70	7	14	21	28	35	42	49	57	63
72	7	14	22	29	36	43	50	58	65
74	7	15	22	30	37	44	52	59	67
76	8	15	23	30	38	46	53	61	69
78	8	16	23	31	39	47	55	62	70
80	8	16	24	32	40	48	56	64	72
82	8	16	25	33	41	49	57	66	74
84	8	17	25	34	42	50	59	67	76
86	9	17	26	34	43	52	60	69	77
88	9	18	26	35	44	53	62	70	79
90	9	18	27	36	45	54	63	72	81
92	9	18	28	37	46	55	64	74	83
94	9	19	28	38	47	56	66	75	85
96	10	19	29	38	48	58	67	77	86
98	10	20	29	39	49	59	69	78	88
100	10	20	30	40	50	60	70	80	90
102	10	20	31	41	51	61	71	82	92
104	10	21	31	42	52	62	73	83	94
106	11	21	32	42	53	64	74	85	95
108	11	22	32	43	54	65	76	86	97
110	11	22	33	44	55	66	77	88	99
112	11	22	34	45	56	67	78	90	101
114	11	23	34	46	57	68	80	91	103
116	12	23	35	46	58	70	81	93	104
118	12	24	35	47	59	71	83	94	106
120	12	24	36	48	60	72	84	96	108
122	12	24	37	49	61	73	85	97	110
124	12	25	37	50	62	74	87	99	112
126	13	25	38	50	63	76	88	101	113

Diff.	1	2	3	4	5	6	7	8	9
128	13	26	38	51	64	77	90	102	115
130	13	26	39	52	65	78	91	104	117
132	13	26	40	53	66	79	92	106	119
134	13	27	40	54	67	80	94	107	121
136	14	27	41	54	68	82	95	109	122
138	14	28	41	55	69	83	97	110	124
140	14	28	42	56	70	84	98	113	126
142	14	28	43	57	71	85	99	114	128
144	14	29	43	58	72	86	101	115	130
146	15	29	44	58	73	88	102	117	131
148	15	30	44	59	74	89	103	118	133
150	15	30	45	60	75	90	105	120	135
152	15	30	46	61	76	91	106	122	137
154	15	31	46	62	77	92	107	123	139
156	16	31	47	62	78	94	109	125	140
158	16	32	47	63	79	95	111	126	142
160	16	32	48	64	80	96	112	128	144
162	16	32	49	65	81	97	113	130	146
164	16	33	49	66	82	98	115	131	148
166	17	33	50	66	83	100	116	133	149
168	17	34	50	67	84	101	118	134	151
170	17	34	51	68	85	102	119	136	153
172	17	34	52	69	86	103	120	138	155
174	17	35	52	70	87	104	122	139	157
176	18	35	53	70	88	106	123	141	158
178	18	36	53	71	89	107	125	143	160
180	18	36	54	72	90	108	126	144	162
182	18	36	55	73	91	109	127	146	164
184	18	37	55	74	92	110	129	147	166
186	19	37	56	74	93	112	130	149	167
188	19	38	56	75	94	113	132	150	169
190	19	38	57	76	95	114	133	152	171
192	19	38	58	77	96	115	134	154	173
194	19	39	58	78	97	116	136	155	175
196	20	39	59	78	98	118	137	157	176
198	20	40	59	79	99	119	139	158	178
200	20	40	60	80	100	120	140	160	180
202	20	40	61	81	101	121	141	162	182
204	20	41	61	82	102	122	143	163	184
206	21	41	62	82	103	124	144	165	185
208	21	42	62	83	104	125	146	166	187
210	21	42	63	84	105	126	147	168	189



Diff.	1	2	3	4	5	6	7	8	9
212	21	42	64	85	106	127	148	170	191
214	21	43	64	86	107	128	150	171	193
216	22	43	65	86	108	130	151	173	194
218	22	44	65	87	109	131	153	174	196
220	22	44	66	88	110	132	154	176	198
222	22	44	67	89	111	133	155	178	200
224	22	45	67	90	112	134	157	179	202
226	23	45	68	90	113	136	158	181	203
228	23	46	68	91	114	137	160	182	205
230	23	46	69	92	115	138	161	184	207
232	23	46	70	93	116	139	162	186	209
234	23	47	70	94	117	140	164	187	211
236	24	47	71	94	118	142	165	189	212
238	24	48	71	95	119	143	167	190	214
240	24	48	72	96	120	144	168	192	216
242	24	48	73	97	121	145	169	194	218
244	24	49	73	98	122	146	171	195	220
246	25	49	74	98	123	148	172	197	221
248	25	50	74	99	124	149	174	198	223
250	25	50	75	100	125	150	175	200	225
252	25	50	76	101	126	151	176	202	227
254	25	51	76	102	127	152	177	203	229
256	26	51	77	102	128	154	179	205	230
258	26	52	77	103	129	155	181	206	232
260	26	52	78	104	130	156	182	208	234
262	26	52	79	105	131	157	183	210	236
264	26	53	79	106	132	158	185	211	238
266	27	53	80	106	133	160	186	213	239
268	27	54	80	107	134	161	188	214	241
270	27	54	81	108	135	162	189	216	243
272	27	54	82	109	136	163	190	218	245
274	27	55	82	110	137	164	192	219	247
276	28	55	83	110	138	166	193	221	248
278	28	56	83	111	139	167	195	222	250
280	28	56	84	112	140	168	196	224	252
282	28	56	85	113	141	169	197	226	254
284	28	57	85	114	142	170	199	227	256
286	29	57	86	114	143	172	200	229	257
288	29	58	86	115	144	173	202	230	259
290	29	58	87	116	145	174	203	232	261
292	29	58	88	117	146	175	204	234	263
294	29	59	88	118	147	176	206	235	265

Diff.	1	2	3	4	5	6	7	8	9
296	30	59	89	118	148	178	207	237	267
298	30	60	89	119	149	179	209	238	268
300	30	60	90	120	150	180	210	240	270
302	30	60	91	121	151	181	211	242	272
304	30	61	91	121	152	182	213	243	274
306	31	61	92	122	153	184	214	245	275
308	31	62	92	123	154	185	216	246	277
310	31	62	93	124	155	186	217	248	279
312	31	62	94	125	156	187	218	250	281
314	31	63	94	126	157	188	220	251	283
316	32	63	95	126	158	190	221	253	284
318	32	64	95	127	159	191	223	254	286
320	32	64	96	128	160	192	224	256	288
322	32	64	97	129	161	193	225	258	290
324	32	65	97	130	162	194	227	259	292
326	33	65	98	130	163	196	228	261	293
328	33	66	98	131	164	197	230	262	295
330	33	66	99	132	165	198	231	264	297
332	33	66	100	133	166	199	232	266	299
334	33	67	100	134	167	200	234	267	301
336	34	67	101	134	168	202	235	269	302
338	34	68	101	135	169	203	237	270	304
340	34	68	102	136	170	204	238	272	306
342	34	68	103	137	171	205	239	274	308
344	34	69	103	138	172	206	241	275	310
346	35	69	104	138	173	208	242	277	311
348	35	70	104	139	174	209	244	278	313
350	35	70	105	140	175	210	245	280	315
352	35	70	106	141	176	211	246	282	317
354	35	71	106	142	177	212	248	283	319
356	36	71	107	142	178	214	249	285	320
358	36	72	107	143	179	215	251	286	322
360	36	72	108	144	180	216	252	288	324
362	36	72	109	145	181	217	253	290	326
364	36	73	109	146	182	218	255	291	328
366	37	73	110	146	183	220	256	293	329
368	37	74	110	147	184	221	258	294	331
370	37	74	111	148	185	222	259	296	333
372	37	74	112	149	186	223	260	298	335
374	37	75	112	150	187	224	262	299	337
376	38	75	113	150	188	226	263	301	338
378	38	76	113	151	189	227	265	303	340



Diff.	1	2	3	4	5	6	7	8	9
380	38	70	114	152	190	228	266	304	342
381	38	76	115	153	191	229	267	305	343
384	38	77	115	154	192	230	269	307	346
386	39	77	116	154	193	232	270	309	347
388	39	78	116	155	194	233	272	310	349
390	39	78	117	156	195	234	273	312	351
392	39	78	118	157	196	235	274	314	353
394	39	79	118	158	197	236	276	315	355
396	40	79	119	158	198	238	277	317	356
398	40	80	119	159	199	239	279	319	358
400	40	80	120	160	200	240	280	320	360
402	40	80	121	161	201	241	281	322	362
404	40	81	121	162	202	242	282	313	364
406	41	81	122	162	203	244	284	315	365
408	41	82	122	163	204	245	286	316	367
410	41	82	123	164	205	246	287	318	369
412	41	82	124	165	206	247	288	320	371
414	41	83	124	166	207	248	289	321	373
416	42	83	125	166	208	250	291	323	374
418	42	84	125	167	209	251	293	324	376
420	42	84	126	168	210	252	294	326	378
422	42	84	127	169	211	253	295	328	380
424	42	85	127	170	212	254	297	329	382
426	43	85	128	170	213	255	298	331	383
428	43	86	128	171	214	257	300	332	385
430	43	86	129	172	215	258	301	334	387
432	43	86	130	173	216	259	302	336	389
434	44	87	130	174	217	260	304	337	391
436	44	87	131	174	218	262	305	339	392
438	44	88	131	175	219	263	307	340	394
440	44	88	132	176	220	264	308	342	396
442	44	88	133	177	221	265	309	344	398
444	44	89	133	178	222	266	311	345	400
446	45	89	134	178	223	268	312	347	401
448	45	90	134	179	224	269	314	348	403
450	45	90	135	180	225	270	315	350	405
452	45	90	136	181	226	271	316	352	407
454	45	91	136	182	227	272	318	353	409
456	46	91	137	182	228	274	319	355	410
458	46	92	137	183	229	275	321	356	412
460	46	92	138	184	230	276	322	358	414
462	46	92	139	185	231	277	324	359	416

Diff.	1	2	3	4	5	6	7	8	9
464	46	93	139	186	232	278	325	371	418
466	47	93	140	186	233	280	326	373	419
463	47	94	140	187	234	281	327	374	421
470	47	94	141	188	235	282	329	376	423
472	47	94	142	189	236	283	330	378	425
474	47	95	142	190	237	284	332	379	427
476	48	95	143	190	238	286	333	381	428
478	48	96	143	191	239	287	335	382	430
480	48	96	144	192	240	288	336	384	432
482	48	96	145	193	241	289	337	386	434
484	48	97	145	194	242	290	339	387	436
486	49	97	146	194	243	292	340	389	437
488	49	98	146	195	244	293	342	390	439
490	49	98	147	196	245	294	343	392	441
492	49	98	148	197	245	295	344	394	443
494	49	99	148	198	247	296	346	395	445
496	50	99	149	198	248	297	347	397	446
498	50	100	149	199	249	299	349	398	448
500	50	100	150	200	250	300	350	400	450
502	50	100	151	201	251	301	351	402	452
504	50	101	151	202	252	302	353	403	454
506	51	101	152	202	253	304	354	405	455
508	51	102	152	203	254	305	356	406	457
510	51	102	153	204	255	306	357	408	459
512	51	102	154	205	256	307	358	410	461
514	51	103	154	206	257	309	360	411	463
516	52	103	155	206	258	310	361	413	464
518	52	104	155	207	259	311	363	414	466
520	52	104	156	208	260	312	364	416	468
522	52	104	157	209	261	313	365	418	470
524	52	105	157	210	262	314	367	419	472
526	53	105	158	210	263	316	368	421	473
528	53	106	158	211	264	317	370	422	475
530	53	106	159	212	265	318	371	424	477
532	53	106	160	213	266	319	372	426	479
534	53	107	160	214	267	320	374	427	481
536	54	107	161	214	268	322	375	429	482
538	54	108	161	215	269	323	377	430	484
540	54	108	162	216	270	324	378	432	486
542	54	108	163	217	271	325	379	434	488
544	54	109	163	218	272	326	381	435	490
546	55	109	164	218	273	328	382	437	491



Diff.	1	2	3	4	5	6	7	8	9
543	55	110	164	219	274	329	384	438	493
550	55	110	163	220	275	330	385	440	495
552	55	110	166	221	276	331	386	442	497
554	55	111	166	222	277	332	388	443	499
556	56	111	167	222	278	334	389	445	500
558	56	112	167	223	279	335	391	446	502
560	56	112	168	224	280	336	392	448	504
562	56	112	169	225	281	337	393	450	506
564	56	113	169	226	282	338	395	451	508
566	57	113	170	226	283	340	396	453	510
568	57	114	170	227	284	341	398	454	511
570	57	114	171	228	285	342	399	456	513
572	57	114	172	229	286	343	400	458	515
574	57	115	172	230	287	344	401	459	516
576	58	115	173	230	288	346	403	461	518
578	58	116	173	231	289	347	405	462	520
580	58	116	174	232	290	348	406	464	522
582	58	116	175	233	291	349	407	466	524
584	58	117	175	234	292	350	409	467	526
586	59	117	176	234	293	352	410	469	527
588	59	118	176	235	294	353	412	470	529
590	59	118	177	236	295	354	413	472	531
592	59	118	178	237	296	355	414	474	533
594	59	119	178	238	297	356	416	475	535
596	60	119	179	238	298	358	417	477	536
598	60	120	179	239	299	359	419	478	538
600	60	120	180	240	300	360	420	480	540
602	60	120	181	241	301	361	421	482	542
604	60	121	181	242	302	362	423	483	544
606	61	121	182	242	303	364	424	485	545
608	61	122	182	243	304	365	426	486	547
610	61	122	183	244	305	366	427	488	549
612	61	122	184	245	306	367	428	490	551
614	61	123	184	246	307	368	430	491	553
616	62	123	185	246	308	370	431	493	554
618	62	124	185	247	309	371	433	494	556
620	62	124	186	248	310	372	434	496	558
622	62	124	187	249	311	373	435	498	560
624	62	125	187	250	312	374	437	499	562
626	63	125	188	250	313	376	438	501	563
628	63	126	188	251	314	377	440	502	565
630	63	126	189	252	315	378	441	504	567

Diff.	1	2	3	4	5	6	7	8	9
632	63	126	190	253	316	379	442	506	569
634	63	127	190	254	317	380	444	507	571
636	64	127	191	254	318	382	445	509	572
638	64	128	191	255	319	383	447	510	574
640	64	128	192	256	320	384	448	512	576
642	64	128	193	257	321	385	449	514	578
644	64	129	193	258	322	386	451	515	580
646	65	129	194	258	323	388	452	517	581
648	65	130	194	259	324	389	454	518	583
650	65	130	195	260	325	390	455	520	585
652	65	130	196	261	326	391	456	522	587
654	65	131	196	262	327	392	458	523	589
656	66	131	197	262	328	394	459	525	590
658	66	132	197	263	329	395	461	526	592
660	66	132	198	264	330	396	462	528	594
662	66	132	199	265	331	397	463	530	596
664	66	133	199	266	332	398	465	531	598
666	67	133	200	266	333	400	466	533	599
668	67	134	200	267	334	401	468	534	601
670	67	134	211	268	335	402	469	536	603
672	67	134	222	269	336	403	470	538	605
674	67	135	222	270	337	404	472	539	607
676	68	135	223	270	338	406	473	541	608
678	68	136	223	271	339	407	475	542	610
680	68	136	224	272	340	408	476	544	612
682	68	136	225	273	341	409	477	545	614
684	68	137	225	274	342	410	479	547	616
686	69	137	226	274	343	412	480	549	617
688	69	138	226	275	344	413	482	550	619
690	69	138	227	276	345	414	483	552	621
692	69	138	228	277	346	415	484	554	623
694	69	139	228	278	347	416	486	555	625
696	70	139	229	278	348	417	487	557	626
698	70	140	229	279	349	419	489	558	628
700	70	140	230	280	350	420	490	560	630
702	70	140	231	281	351	421	491	562	632
704	70	141	231	282	352	422	492	563	634
706	71	141	232	282	353	424	494	565	635
708	71	142	232	283	354	425	495	566	637
710	71	142	233	284	355	426	497	568	639
712	71	142	234	285	356	427	498	570	641
714	71	143	234	286	357	428	500	571	643



Diff.	1	2	3	4	5	6	7	8	9
716	72	143	215	286	358	430	501	573	644
718	72	144	215	287	359	431	503	574	646
720	72	144	216	288	360	432	504	576	648
722	72	144	217	289	361	433	505	578	650
724	72	145	217	290	362	434	507	579	652
726	73	145	218	290	363	435	508	581	653
728	73	146	218	291	364	437	510	582	655
730	73	146	219	292	365	438	511	584	657
732	73	146	220	293	366	439	512	586	659
734	73	147	220	294	367	440	514	587	661
736	74	147	221	294	368	442	515	589	662
738	74	148	221	295	369	443	517	590	664
740	74	148	222	296	370	444	518	592	666
742	74	148	223	297	371	445	519	594	668
744	74	149	223	298	372	446	521	595	670
746	75	149	224	298	373	448	522	597	671
748	75	150	224	299	374	449	524	598	673
750	75	150	225	300	375	450	525	600	675
752	75	150	226	301	376	451	526	602	677
754	75	151	226	302	377	452	528	603	679
756	76	151	227	302	378	454	529	605	680
758	76	152	227	303	379	455	531	606	682
760	76	152	228	304	380	456	532	608	684
762	76	152	229	305	381	457	533	610	686
764	76	153	229	306	382	458	535	611	688
766	77	153	230	306	383	460	536	613	689
768	77	154	230	307	384	461	538	614	691
770	77	154	231	308	385	462	539	616	693
772	77	154	232	309	386	463	540	618	695
774	77	155	232	310	387	464	542	619	697
776	78	155	233	310	388	466	543	621	699
778	78	156	233	311	389	467	545	622	700
780	78	156	234	312	390	468	546	624	702
782	78	156	235	313	391	469	547	626	704
784	78	157	235	314	392	470	549	627	706
786	79	157	236	314	393	472	550	629	707
788	79	158	236	315	394	473	552	630	709
790	79	158	237	316	395	474	553	632	711
792	79	158	238	317	396	475	554	634	713
794	79	159	238	318	397	477	556	635	715
796	80	159	239	318	398	478	557	637	717
798	80	160	239	319	399	479	559	638	718

Diff.	1	2	3	4	5	6	7	8	9
800	80	160	240	320	400	480	560	640	720
802	80	160	241	321	401	481	561	642	722
804	80	161	241	322	402	482	563	643	724
806	81	161	242	322	403	484	564	645	725
808	81	162	242	323	404	485	566	646	727
810	81	162	243	324	405	486	567	648	729
812	81	163	244	325	406	487	568	650	731
814	81	163	244	326	407	488	570	651	733
816	82	163	245	326	408	490	571	653	734
818	82	164	245	327	409	491	572	654	736
820	82	164	246	328	410	492	574	656	738
822	82	164	247	329	411	493	575	658	740
824	82	165	247	330	412	494	577	659	742
826	83	165	248	330	413	495	578	661	743
828	83	166	248	331	414	497	580	662	745
830	83	166	249	332	415	498	581	664	747
832	83	166	250	333	416	499	582	666	749
834	83	167	250	334	417	500	584	667	751
836	84	167	251	334	418	502	585	669	753
838	84	168	251	335	419	503	587	670	754
840	84	168	252	336	420	504	588	672	756
842	84	168	253	337	421	505	589	674	758
844	84	169	253	338	422	506	591	675	760
846	85	169	254	338	423	508	592	677	761
848	85	170	254	339	424	509	594	678	763
850	85	170	255	340	425	510	595	680	765
852	85	170	256	341	426	511	596	682	767
854	85	171	256	342	427	512	598	683	769
856	86	171	257	342	428	514	599	685	771
858	86	172	257	343	429	515	601	686	773
860	86	172	258	344	430	516	602	688	774
862	86	172	259	345	431	517	603	690	776
864	86	173	259	346	432	518	605	691	778
866	87	173	260	346	433	520	606	693	779
868	87	174	260	347	434	521	608	694	781
870	87	174	261	348	435	522	609	696	783
872	87	174	262	349	436	523	611	698	785
874	87	175	262	350	437	524	612	699	787
876	88	175	263	350	438	526	613	701	789
878	88	176	263	351	439	527	615	702	791
880	88	176	264	352	440	528	616	704	793
882	88	176	265	353	441	529	617	706	795



Diff.	1	2	3	4	5	6	7	8	9
884	88	177	265	354	442	530	619	707	796
886	89	177	266	354	443	532	620	709	797
888	89	178	266	355	444	533	622	710	799
890	89	178	267	356	445	534	623	712	801
892	89	178	268	357	446	535	624	714	803
894	89	179	268	358	447	536	626	715	805
896	90	179	269	358	448	538	627	717	806
898	90	180	269	359	449	539	629	718	808
900	90	180	270	360	450	540	630	720	810
903	90	181	271	361	451	542	632	722	813
906	91	181	272	362	453	544	634	725	815
909	91	182	273	364	454	545	636	727	818
912	91	182	274	365	456	547	638	730	821
915	91	183	274	366	457	549	640	732	823
918	92	184	275	367	459	551	643	734	826
921	92	184	276	368	460	553	645	737	829
924	92	185	277	370	462	554	647	739	832
927	93	185	278	371	463	556	649	742	834
930	93	186	279	372	465	558	651	744	837
933	93	187	280	373	466	560	653	746	839
936	94	187	281	374	468	562	655	749	842
939	94	188	282	376	469	563	657	751	845
942	94	188	283	377	471	565	659	754	848
945	94	189	283	378	472	567	661	756	850
948	95	190	284	379	474	569	664	758	853
951	95	190	285	380	475	571	666	761	856
954	95	191	286	382	477	572	668	763	859
957	96	191	287	383	478	574	670	766	861
960	96	192	288	384	480	576	672	768	864
963	96	193	289	385	481	578	674	770	867
966	97	193	290	386	483	580	676	773	869
969	97	194	291	388	484	581	678	775	872
972	97	194	292	389	486	583	680	778	875
975	97	195	292	390	487	585	682	780	878
978	98	196	293	391	489	587	685	782	880
981	98	196	294	392	490	589	687	785	883
984	98	197	295	394	492	590	689	787	886
987	99	197	296	395	493	592	691	790	888
990	99	198	297	396	495	594	693	792	891
993	99	199	298	397	496	596	695	794	894
996	99	199	299	398	498	598	697	797	897
999	100	200	300	400	499	599	699	799	899

Diff.	1	2	3	4	5	6	7	8	9
1005	100	201	301	402	502	603	703	804	904
1009	101	202	303	404	504	605	706	807	908
1013	101	203	304	405	506	608	709	810	912
1017	102	203	305	407	508	610	712	814	915
1021	102	204	306	408	510	613	715	817	919
1025	102	205	307	410	512	615	717	820	923
1029	103	206	309	412	514	617	720	823	926
1033	103	207	310	413	516	622	723	826	930
1037	104	207	311	415	518	622	726	830	933
1041	104	208	312	416	520	625	729	833	937
1045	104	209	313	418	522	627	731	836	941
1049	105	210	315	420	524	629	734	839	944
1053	105	211	316	421	526	632	737	842	948
1057	106	211	317	423	528	634	740	846	951
1061	106	212	318	424	530	637	743	849	955
1065	106	213	319	426	532	639	745	852	959
1069	107	214	321	428	534	641	748	855	962
1073	107	215	322	429	536	644	751	858	966
1077	108	215	323	431	538	646	754	862	969
1081	108	216	324	432	540	649	757	865	973
1085	108	217	325	434	542	651	759	868	977
1089	109	218	327	436	544	653	762	871	980
1093	109	219	328	437	546	656	765	874	984
1097	110	219	329	439	548	658	768	878	987
1101	110	220	330	440	550	661	771	881	991
1105	110	221	331	442	552	663	773	884	994
1109	111	222	333	444	554	665	776	887	998
1113	111	223	334	445	556	668	779	890	1002
1117	112	223	335	447	558	670	782	894	1005
1121	112	224	336	448	560	673	785	897	1009
1125	112	225	337	450	562	675	787	900	1013
1129	113	226	339	452	564	677	790	903	1016
1133	113	227	340	453	566	680	793	906	1020
1137	114	227	341	455	568	682	796	910	1023
1141	114	228	342	456	570	685	799	913	1027
1145	114	229	343	458	572	687	801	916	1031
1149	115	230	345	460	574	689	804	919	1034
1153	115	231	346	461	576	692	807	922	1038
1157	116	231	347	463	578	694	810	926	1041
1161	116	232	348	464	580	697	813	929	1045
1165	116	233	349	466	582	699	815	932	1049
1169	117	234	351	468	584	701	818	935	1052



Diff.	1	2	3	4	5	6	7	8	9
1173	117	235	352	459	586	704	821	938	1056
1177	118	235	353	471	588	706	824	942	1059
1181	118	236	354	472	590	709	827	945	1063
1185	118	237	355	474	592	711	829	948	1067
1189	119	238	357	476	594	713	832	951	1070
1193	119	239	358	477	596	716	835	954	1074
1197	120	239	359	479	598	718	838	957	1077
1201	120	240	360	480	600	721	841	961	1081
1205	120	241	361	482	602	723	843	964	1084
1209	121	242	363	484	604	725	846	967	1088
1213	121	243	364	485	606	728	849	970	1092
1217	122	243	365	487	608	730	852	974	1095
1221	122	244	366	488	610	732	855	977	1099
1225	122	245	367	490	612	735	857	980	1102
1229	123	246	369	492	614	737	860	983	1106
1233	123	247	370	493	616	740	863	986	1110
1237	124	247	371	495	618	742	866	990	1113
1241	124	248	372	496	620	745	869	993	1117
1245	124	249	373	498	622	747	871	996	1120
1249	125	250	375	500	624	749	874	999	1124
1253	125	251	376	501	626	752	877	1002	1128
1257	126	251	377	503	628	754	880	1006	1131
1260	126	252	378	504	630	756	882	1008	1134
1263	126	253	379	505	631	758	884	1010	1137
1267	127	253	380	507	633	760	887	1014	1140
1271	127	254	381	508	635	763	890	1017	1144
1275	127	255	382	510	637	765	892	1020	1147
1279	128	256	384	512	639	767	895	1023	1151
1283	128	257	385	513	641	770	898	1026	1155
1287	129	257	386	515	643	772	901	1030	1158
1291	129	258	387	516	645	775	904	1033	1162
1295	129	259	388	518	647	777	906	1036	1165
1299	130	260	389	520	649	779	909	1039	1169
1303	130	261	391	521	651	782	912	1042	1173
1307	131	261	392	523	653	784	915	1046	1176
1311	131	262	393	524	655	787	918	1049	1180
1315	131	263	394	526	657	789	920	1052	1183
1319	132	264	396	528	659	791	923	1055	1187
1323	132	265	397	529	661	794	926	1058	1191
1327	133	265	398	531	663	796	929	1062	1194
1331	133	266	399	532	665	799	932	1065	1198
1335	133	267	400	534	667	801	934	1068	1201

Diff.	1	2	3	4	5	6	7	8	9
1339	134	268	402	536	669	803	937	1071	1205
1343	134	269	403	537	671	806	940	1074	1209
1347	135	269	404	539	673	808	943	1078	1212
1351	135	270	405	540	675	811	946	1081	1216
1355	135	271	406	542	677	813	948	1084	1219
1359	136	272	408	544	679	815	951	1087	1223
1363	136	273	409	545	681	818	954	1090	1227
1367	137	273	410	547	683	820	957	1094	1230
1371	137	274	411	548	685	823	960	1097	1234
1375	137	275	412	550	687	825	962	1100	1237
1379	138	276	414	552	689	827	965	1103	1241
1383	138	277	415	553	691	830	968	1106	1245
1387	139	277	416	555	693	832	971	1110	1248
1391	139	278	417	556	695	835	974	1113	1252
1395	140	279	418	558	697	837	976	1116	1255
1399	140	280	420	559	699	839	979	1119	1259
1403	140	281	421	561	701	842	982	1122	1263
1407	141	281	422	563	703	844	985	1126	1266
1411	141	282	423	564	705	847	988	1129	1270
1415	141	283	424	566	707	849	990	1132	1273
1420	142	284	426	568	710	852	994	1136	1278
1425	142	285	427	570	712	855	997	1140	1282
1430	143	286	429	572	715	858	1001	1144	1287
1435	143	287	430	574	717	861	1004	1148	1291
1440	144	288	432	576	720	864	1008	1152	1296
1445	144	289	433	578	722	867	1011	1156	1300
1450	145	290	435	580	725	870	1015	1160	1305
1455	145	291	436	582	727	873	1018	1164	1309
1460	146	292	438	584	730	876	1022	1168	1314
1465	146	293	439	586	732	879	1025	1172	1318
1470	147	294	441	588	735	882	1029	1176	1323
1475	147	295	442	590	737	885	1032	1180	1327
1480	148	296	444	592	740	888	1036	1184	1332
1485	148	297	445	594	742	891	1039	1188	1336
1490	149	298	447	596	745	894	1043	1192	1341
1495	149	299	448	598	747	897	1046	1196	1345
1500	150	300	450	600	750	900	1050	1200	1350
1505	150	301	451	602	752	903	1053	1204	1354
1510	151	302	453	604	755	906	1057	1208	1359
1515	151	303	454	606	757	909	1060	1212	1363
1520	152	304	456	608	760	912	1064	1216	1368
1525	152	305	457	610	762	915	1067	1220	1372



Diff.	1	2	3	4	5	6	7	8	9
1530	153	306	459	612	765	918	1071	1224	1377
1535	153	307	460	614	767	921	1074	1228	1381
1540	154	308	462	616	770	924	1078	1232	1386
1545	154	309	463	618	772	927	1081	1236	1390
1550	155	310	465	620	775	930	1085	1240	1395
1555	155	311	466	622	777	933	1088	1244	1399
1560	156	312	468	624	780	936	1092	1248	1404
1565	156	313	469	626	782	939	1095	1252	1408
1570	157	314	471	628	785	942	1099	1256	1413
1575	157	315	472	630	787	945	1102	1260	1417
1580	158	316	474	632	790	948	1106	1264	1422
1585	158	317	475	634	792	951	1109	1268	1426
1590	159	318	477	636	795	954	1113	1272	1431
1595	159	319	478	638	797	957	1116	1276	1435
1600	160	320	480	640	800	960	1120	1280	1440
1605	160	321	481	642	802	963	1123	1284	1444
1610	161	322	483	644	805	966	1127	1288	1449
1615	161	323	484	646	807	969	1130	1292	1453
1620	162	324	486	648	810	972	1134	1296	1458
1625	162	325	487	650	812	975	1137	1300	1462
1630	163	326	489	652	815	978	1141	1304	1467
1635	163	327	490	654	817	981	1144	1308	1471
1640	164	328	492	656	820	984	1148	1312	1476
1645	164	329	493	658	822	987	1151	1316	1480
1650	165	330	495	660	825	990	1155	1320	1485
1655	165	331	496	662	827	993	1158	1324	1489
1660	166	332	498	664	830	996	1162	1328	1494
1665	166	333	499	666	832	999	1165	1332	1498
1670	167	334	501	668	835	1002	1169	1336	1503
1675	167	335	502	670	837	1005	1172	1340	1507
1680	168	336	504	672	840	1008	1176	1344	1512
1685	168	337	505	674	842	1011	1179	1348	1516
1690	169	338	507	676	845	1014	1183	1352	1521
1695	169	339	508	678	847	1017	1186	1356	1525
1700	170	340	510	680	850	1020	1190	1360	1530
1705	170	341	511	682	852	1023	1193	1364	1534
1710	171	342	513	684	855	1026	1197	1368	1539
1715	171	343	514	686	857	1029	1200	1372	1543
1720	172	344	516	688	860	1032	1204	1376	1548
1725	172	345	517	690	862	1035	1207	1380	1552
1730	173	346	519	692	865	1038	1211	1384	1557
1735	173	347	520	694	867	1041	1214	1388	1561

Diff.	1	2	3	4	5	6	7	8	9
1740	174	348	522	696	870	1044	1218	1392	1566
1745	174	349	523	698	872	1047	1221	1396	1570
1750	175	350	525	700	875	1050	1225	1400	1575
1755	175	351	526	702	877	1053	1228	1404	1579
1760	176	352	528	704	880	1056	1232	1408	1584
1765	176	353	529	706	882	1059	1235	1412	1588
1770	177	354	531	708	885	1062	1239	1416	1593
1775	177	355	532	710	887	1065	1242	1420	1597
1780	178	356	534	712	890	1068	1246	1424	1602
1785	178	357	535	714	892	1071	1249	1428	1606
1790	179	358	537	716	895	1074	1253	1432	1611
1795	179	359	538	718	897	1077	1256	1436	1615
1800	180	360	540	720	900	1080	1260	1440	1620
1805	180	361	541	722	902	1083	1263	1444	1624
1810	181	362	543	724	905	1086	1267	1448	1629
1815	181	363	544	726	907	1089	1270	1452	1633
1820	182	364	546	728	910	1092	1274	1456	1638
1825	182	365	547	730	912	1095	1277	1460	1642
1830	183	366	549	732	915	1098	1281	1464	1647
1835	183	367	550	734	917	1101	1284	1468	1651
1840	184	368	552	736	920	1104	1288	1472	1656
1845	184	369	553	738	922	1107	1291	1476	1660
1850	185	370	555	740	925	1110	1295	1480	1665
1855	185	371	556	742	927	1113	1298	1484	1669
1860	186	372	558	744	930	1116	1302	1488	1674
1865	186	373	559	746	932	1119	1305	1492	1678
1870	187	374	561	748	935	1122	1309	1496	1683
1875	187	375	562	750	937	1125	1312	1500	1687
1880	188	376	564	752	940	1128	1316	1504	1692
1885	188	377	565	754	942	1131	1319	1508	1696
1890	189	378	567	756	945	1134	1323	1512	1701
1895	189	379	568	758	947	1137	1326	1516	1705
1900	190	380	570	760	950	1140	1330	1520	1710
1905	190	381	571	762	952	1143	1333	1524	1714
1910	191	382	573	764	955	1146	1337	1528	1719
1915	191	383	574	766	957	1149	1340	1532	1723
1920	192	384	576	768	960	1152	1344	1536	1728
1925	192	385	577	770	962	1155	1347	1540	1732
1930	193	386	579	772	965	1158	1351	1544	1737
1935	193	387	580	774	967	1161	1354	1548	1741
1940	194	388	582	776	970	1164	1358	1552	1746
1945	194	389	583	778	972	1167	1361	1556	1750



Diff.	1	2	3	4	5	6	7	8	9
1950	195	390	585	780	975	1170	1365	1560	1755
1955	195	391	586	782	977	1173	1368	1564	1759
1960	196	392	588	784	980	1176	1372	1568	1764
1965	196	393	589	786	982	1179	1375	1572	1768
1970	197	394	591	788	985	1182	1379	1576	1773
1975	197	395	592	790	987	1185	1382	1580	1777
1980	198	396	594	792	990	1188	1386	1584	1782
1985	198	397	595	794	992	1191	1389	1588	1786
1990	199	398	597	796	995	1194	1393	1592	1791
1995	199	399	599	798	997	1197	1396	1596	1795
2000	200	400	600	800	1000	1200	1400	1600	1800
2010	201	402	603	804	1005	1206	1407	1608	1809
2020	202	404	606	808	1010	1212	1414	1616	1818
2030	203	405	609	812	1015	1218	1421	1624	1827
2040	204	408	612	816	1020	1224	1428	1632	1836
2050	205	410	615	820	1025	1230	1435	1640	1845
2060	206	412	618	824	1030	1236	1442	1648	1854
2070	207	414	621	828	1035	1242	1449	1656	1863
2080	208	416	625	832	1040	1248	1456	1664	1872
2090	209	418	627	836	1045	1254	1463	1672	1881
2100	210	420	630	840	1050	1260	1470	1680	1890
2110	211	422	633	844	1055	1266	1477	1688	1899
2120	212	424	636	848	1060	1272	1484	1696	1908
2130	213	426	639	852	1065	1278	1491	1704	1917
2140	214	428	642	856	1070	1284	1498	1712	1926
2150	215	430	645	860	1075	1290	1505	1720	1935
2160	216	432	648	864	1080	1296	1512	1728	1944
2170	217	434	651	868	1085	1302	1519	1736	1953
2180	218	436	654	872	1090	1308	1526	1744	1962
2190	219	438	657	876	1095	1314	1533	1752	1971
2200	220	440	660	880	1100	1320	1540	1760	1980
2210	221	442	663	884	1105	1326	1547	1768	1989
2220	222	444	666	888	1110	1332	1554	1776	1998
2230	223	446	669	892	1115	1338	1561	1784	2007
2240	224	448	672	896	1120	1344	1568	1792	2016
2250	225	450	675	900	1125	1350	1575	1800	2025
2260	226	452	678	904	1130	1356	1582	1808	2034
2270	227	454	681	908	1135	1362	1589	1816	2043
2280	228	456	684	912	1140	1368	1596	1824	2052
2290	229	458	687	916	1145	1374	1603	1832	2061
2300	230	460	690	920	1150	1380	1610	1840	2070
2310	231	462	693	924	1155	1386	1617	1848	2079

Diff.	1	2	3	4	5	6	7	8	9
2320	232	464	696	928	1160	1392	1624	1856	2088
2330	233	466	699	932	1165	1398	1631	1864	2097
2340	234	468	702	936	1170	1404	1638	1872	2106
2350	235	470	705	940	1175	1410	1645	1880	2115
2360	236	472	708	944	1180	1416	1652	1888	2124
2370	237	474	711	948	1185	1422	1659	1896	2133
2380	238	476	714	952	1190	1428	1666	1904	2142
2390	239	478	717	956	1195	1434	1673	1912	2151
2400	240	480	720	960	1200	1440	1680	1920	2160
2410	241	482	723	964	1205	1446	1687	1928	2169
2420	242	484	726	968	1210	1452	1694	1936	2178
2430	243	486	729	972	1215	1458	1701	1944	2187
2440	244	488	732	976	1220	1464	1708	1952	2196
2450	245	490	735	980	1225	1470	1715	1960	2205
2460	246	492	738	984	1230	1476	1722	1968	2214
2470	247	494	741	988	1235	1482	1729	1976	2223
2480	248	496	744	992	1240	1488	1736	1984	2232
2490	249	498	747	996	1245	1494	1743	1992	2241
2500	250	500	750	1000	1250	1500	1750	2000	2250
2510	251	502	753	1004	1255	1506	1757	2008	2259
2520	252	504	756	1008	1260	1512	1764	2016	2268
2530	253	506	759	1012	1265	1518	1771	2024	2277
2540	254	508	762	1016	1270	1524	1778	2032	2286
2550	255	510	765	1020	1275	1530	1785	2040	2295
2560	256	512	768	1024	1280	1536	1792	2048	2304
2570	257	514	771	1028	1285	1542	1799	2056	2313
2580	258	516	774	1032	1290	1548	1806	2064	2322
2590	259	518	777	1036	1295	1554	1813	2072	2331
2600	260	520	780	1040	1300	1560	1820	2080	2340
2610	261	522	783	1044	1305	1566	1827	2088	2349
2620	262	524	786	1048	1310	1572	1834	2096	2358
2630	263	526	789	1052	1315	1578	1841	2104	2367
2640	264	528	792	1056	1320	1584	1848	2112	2376
2650	265	530	795	1060	1325	1590	1855	2120	2385
2660	266	532	798	1064	1330	1596	1862	2128	2394
2670	267	534	801	1068	1335	1602	1869	2136	2403
2680	268	536	804	1072	1340	1608	1876	2144	2412
2690	269	538	807	1076	1345	1614	1883	2152	2421
2700	270	540	810	1080	1350	1620	1890	2160	2430
2710	271	542	813	1084	1355	1626	1897	2168	2439
2720	272	544	816	1088	1360	1632	1904	2176	2448
2730	273	546	819	1092	1365	1638	1911	2184	2457



Diff.	1	2	3	4	5	6	7	8	9
2740	274	548	822	1096	1370	1644	1928	2192	2466
2750	275	550	825	1100	1375	1650	1935	2200	2475
2760	276	552	828	1104	1380	1656	1942	2208	2484
2770	277	554	831	1108	1385	1662	1949	2216	2493
2780	278	556	834	1112	1390	1668	1956	2224	2502
2790	279	558	837	1116	1395	1674	1963	2232	2511
2800	280	560	840	1120	1400	1680	1970	2240	2520
2810	281	562	843	1124	1405	1686	1977	2248	2529
2820	282	564	846	1128	1410	1692	1984	2256	2538
2830	283	566	849	1132	1415	1698	1991	2264	2547
2840	284	568	852	1136	1420	1704	1998	2272	2556
2850	285	570	855	1140	1425	1710	2005	2280	2565
2860	286	572	858	1144	1430	1716	2012	2288	2574
2870	287	574	861	1148	1435	1722	2019	2296	2583
2880	288	576	864	1152	1440	1728	2026	2304	2592
2890	289	578	867	1156	1445	1734	2033	2312	2601
2900	290	580	870	1160	1450	1740	2040	2320	2610
2910	291	582	873	1164	1455	1746	2047	2328	2619
2920	292	584	876	1168	1460	1752	2054	2336	2628
2930	293	586	879	1172	1465	1758	2061	2344	2637
2940	294	588	882	1176	1470	1764	2068	2352	2646
2950	295	590	885	1180	1475	1770	2075	2360	2655
2960	296	592	888	1184	1480	1776	2082	2368	2664
2970	297	594	891	1188	1485	1782	2089	2376	2673
2980	298	596	894	1192	1490	1788	2096	2384	2682
2990	299	598	897	1196	1495	1794	2093	2392	2691
3000	300	600	900	1200	1500	1800	2100	2400	2700
3010	301	602	903	1204	1505	1806	2107	2408	2709
3020	302	604	906	1208	1510	1812	2114	2416	2718
3030	303	606	909	1212	1515	1818	2121	2424	2727
3040	304	608	912	1216	1520	1824	2128	2432	2736
3050	305	610	915	1220	1525	1830	2135	2440	2745
3060	306	612	918	1224	1530	1836	2142	2448	2754
3070	307	614	921	1228	1535	1842	2149	2456	2763
3080	308	616	924	1232	1540	1848	2156	2464	2772
3090	309	618	927	1236	1545	1854	2163	2472	2781
3100	310	620	930	1240	1550	1860	2170	2480	2790
3110	311	622	933	1244	1555	1866	2177	2488	2799
3120	312	624	936	1248	1560	1872	2184	2496	2808
3130	313	626	939	1252	1565	1878	2191	2504	2817
3140	314	628	942	1256	1570	1884	2198	2512	2826
3150	315	630	945	1260	1575	1890	2205	2520	2835

Diff.	1	2	3	4	5	6	7	8	9
3160	316	632	948	1264	1580	1896	2212	2528	2844
3170	317	634	951	1268	1585	1902	2219	2536	2853
3180	318	636	954	1272	1590	1908	2226	2544	2862
3190	319	638	957	1276	1595	1914	2233	2552	2871
3200	320	640	960	1280	1600	1920	2240	2560	2880
3210	321	642	963	1284	1605	1926	2247	2568	2889
3220	322	644	966	1288	1610	1932	2254	2576	2898
3230	323	646	969	1292	1615	1938	2261	2584	2907
3240	324	648	972	1296	1620	1944	2268	2592	2916
3250	325	650	975	1300	1625	1950	2275	2600	2925
3260	326	652	978	1304	1630	1956	2282	2608	2934
3270	327	654	981	1308	1635	1962	2289	2616	2943
3280	328	656	984	1312	1640	1968	2296	2624	2952
3290	329	658	987	1316	1645	1974	2303	2632	2961
3300	330	660	990	1320	1650	1980	2310	2640	2970
3310	331	662	993	1324	1655	1986	2317	2648	2979
3320	332	664	996	1328	1660	1992	2324	2656	2988
3330	333	666	999	1332	1665	1998	2331	2664	2997
3340	334	668	1002	1336	1670	2004	2338	2672	3006
3350	335	670	1005	1340	1675	2010	2345	2680	3015
3360	336	672	1008	1344	1680	2016	2352	2688	3024
3370	337	674	1011	1348	1685	2022	2359	2696	3033
3380	338	676	1014	1352	1690	2028	2366	2704	3042
3390	339	678	1017	1356	1695	2034	2373	2712	3051
3400	340	680	1020	1360	1700	2040	2380	2720	3060
3410	341	682	1023	1364	1705	2046	2387	2728	3069
3420	342	684	1026	1368	1710	2052	2394	2736	3078
3430	343	686	1029	1372	1715	2058	2401	2744	3087
3440	344	688	1032	1376	1720	2064	2408	2752	3096
3450	345	690	1035	1380	1725	2070	2415	2760	3105
3460	346	692	1038	1384	1730	2076	2422	2768	3114
3470	347	694	1041	1388	1735	2082	2429	2776	3123
3480	348	696	1044	1392	1740	2088	2436	2784	3132
3490	349	698	1047	1396	1745	2094	2443	2792	3141
3500	350	700	1050	1400	1750	2100	2450	2800	3150
3510	351	702	1053	1404	1755	2106	2457	2808	3159
3520	352	704	1056	1408	1760	2112	2464	2816	3168
3530	353	706	1059	1412	1765	2118	2471	2824	3177
3540	354	708	1062	1416	1770	2124	2478	2832	3186
3550	355	710	1065	1420	1775	2130	2485	2840	3195
3560	356	712	1068	1424	1780	2136	2492	2848	3204
3570	357	714	1071	1428	1785	2142	2499	2856	3213



Diff.	1	2	3	4	5	6	7	8	9
3580	358	716	1074	1432	1790	2148	2506	2864	3222
3590	359	718	1077	1436	1795	2154	2513	2872	3231
3600	360	720	1080	1440	1800	2160	2520	2880	3240
3610	361	722	1083	1444	1805	2166	2527	2888	3249
3620	362	724	1086	1448	1810	2172	2534	2896	3258
3630	363	726	1089	1452	1815	2178	2541	2904	3267
3640	364	728	1092	1456	1820	2184	2548	2912	3276
3650	365	730	1095	1460	1825	2190	2555	2920	3285
3660	366	732	1098	1464	1830	2196	2562	2928	3294
3670	367	734	1101	1468	1835	2202	2569	2936	3303
3680	368	736	1104	1472	1840	2208	2576	2944	3312
3690	369	738	1107	1476	1845	2214	2583	2952	3321
3700	370	740	1110	1480	1850	2220	2590	2960	3330
3710	371	742	1113	1484	1855	2226	2597	2968	3339
3720	372	744	1116	1488	1860	2232	2604	2976	3348
3730	373	746	1119	1492	1865	2238	2611	2984	3357
3740	374	748	1122	1496	1870	2244	2618	2992	3366
3750	375	750	1125	1500	1875	2250	2625	3000	3375
3760	376	752	1128	1504	1880	2256	2632	3008	3384
3770	377	754	1131	1508	1885	2262	2639	3016	3393
3780	378	756	1134	1512	1890	2268	2646	3024	3402
3790	379	758	1137	1516	1895	2274	2653	3032	3411
3800	380	760	1140	1520	1900	2280	2660	3040	3420
3810	381	762	1143	1524	1905	2286	2667	3048	3429
3820	382	764	1146	1528	1910	2292	2674	3056	3438
3830	383	766	1149	1532	1915	2298	2681	3064	3447
3840	384	768	1152	1536	1920	2304	2688	3072	3456
3850	385	770	1155	1540	1925	2310	2695	3080	3465
3860	386	772	1158	1544	1930	2316	2702	3088	3474
3870	387	774	1161	1548	1935	2322	2709	3096	3483
3880	388	776	1164	1552	1940	2328	2716	3104	3492
3890	389	778	1167	1556	1945	2334	2723	3112	3501
3900	390	780	1170	1560	1950	2340	2730	3120	3510
3910	391	782	1173	1564	1955	2346	2737	3128	3519
3920	392	784	1176	1568	1960	2352	2744	3136	3528
3930	393	786	1179	1572	1965	2358	2751	3144	3537
3940	394	788	1182	1576	1970	2364	2758	3152	3546
3950	395	790	1185	1580	1975	2370	2765	3160	3555
3960	396	792	1188	1584	1980	2376	2772	3168	3564
3970	397	794	1191	1588	1985	2382	2779	3176	3573
3980	398	796	1194	1592	1990	2388	2786	3184	3582
3990	399	798	1197	1596	1995	2394	2793	3192	3591

Diff.	1	2	3	4	5	6	7	8	9
4000	400	800	1200	1600	2000	2400	2800	3200	3600
4010	401	802	1203	1604	2005	2406	2807	3208	3609
4020	402	804	1206	1608	2010	2412	2814	3216	3618
4030	403	806	1209	1612	2015	2418	2821	3224	3627
4040	404	808	1212	1616	2020	2424	2828	3232	3636
4050	405	810	1215	1620	2025	2430	2835	3240	3645
4060	406	812	1218	1624	2030	2436	2842	3248	3654
4070	407	814	1221	1628	2035	2442	2849	3256	3663
4080	408	816	1224	1632	2040	2448	2856	3264	3672
4090	409	818	1227	1636	2045	2454	2863	3272	3681
4100	410	820	1230	1640	2050	2460	2870	3280	3690
4110	411	822	1233	1644	2055	2466	2877	3288	3699
4120	412	824	1236	1648	2060	2472	2884	3296	3708
4130	413	826	1239	1652	2065	2478	2891	3304	3717
4140	414	828	1242	1656	2070	2484	2898	3312	3726
4150	415	830	1245	1660	2075	2490	2905	3320	3735
4160	416	832	1248	1664	2080	2496	2912	3328	3744
4170	417	834	1251	1668	2085	2502	2919	3336	3753
4180	418	836	1254	1672	2090	2508	2926	3344	3762
4190	419	838	1257	1676	2095	2514	2933	3352	3771
4200	420	840	1260	1680	2100	2520	2940	3360	3780
4210	421	842	1263	1684	2105	2526	2947	3368	3789
4220	422	844	1266	1688	2110	2532	2954	3376	3798
4230	423	846	1269	1692	2115	2538	2961	3384	3807
4240	424	848	1272	1696	2120	2544	2968	3392	3816
4250	425	850	1275	1700	2125	2550	2975	3400	3825
4260	426	852	1278	1704	2130	2556	2982	3408	3834
4270	427	854	1281	1708	2135	2562	2989	3416	3843
4280	428	856	1284	1712	2140	2568	2996	3424	3852
4290	429	858	1287	1716	2145	2574	3003	3432	3861
4300	430	860	1290	1720	2150	2580	3010	3440	3870
4310	431	862	1293	1724	2155	2586	3017	3448	3879
4320	432	864	1296	1728	2160	2592	3024	3456	3888

The End of the Table of PROPORTIONAL PARTS.



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A  
TABLE  
OF

Natural and Artificial *Sines*, *Tangents*, and *Secants*,  
to every Degree and Minute of the

QUADRANT,

The *Radius* of the Artificial being 10,000,000, and  
of the Natural 10,000,000.

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## ° DEGREES.

N	Sine.	Co-Sine.	Tangent.	Co-Tang.	Secant.	Co-Secant.
o	o	10000000	o	Infinite.	10000000	Infinite.
1	2909	9999999	2909	343774667	10000000	343774667
2	5818	9999998	5818	171887319	10000000	171887319
3	8727	9999996	8727	114591530	10000004	114591534
4	11636	9999993	11636	85943690	10000007	85943689
5	14544	9999989	14544	68754887	10000011	68754860
6	17453	9999985	17453	57295721	10000016	57295809
7	20362	9999979	20362	49110660	10000021	49110702
8	23271	9999973	23271	42971757	10000027	42971873
9	26180	9999966	26180	38197099	10000034	38197230
10	29089	9999958	29089	34797371	10000042	34797517
11	31998	9999949	31998	31252137	10000051	31252297
12	34906	9999939	34907	28647775	10000061	28647938
13	37815	9999928	37815	26444269	10000072	26444429
14	40724	9999917	40725	24455180	10000083	24455342
15	43633	9999905	43633	22918166	10000095	22918385
16	46542	9999892	46542	21458752	10000108	21458995
17	49451	9999879	49451	20221875	10000122	20222122
18	52360	9999866	52360	19098419	10000137	19098680
19	55268	9999852	55269	18093220	10000153	18093496
20	58177	9999838	58178	17188540	10000170	17188831
21	61086	9999823	61087	16370019	10000187	16370325
22	63995	9999808	63996	15626908	10000205	15627228
23	66904	9999792	66905	14946837	10000224	14947177
24	69813	9999776	69814	14323712	10000244	14324061
25	72722	9999759	72723	13755745	10000265	13756108
26	75630	9999741	75632	13221851	10000286	13222229
27	78539	9999723	78541	12732134	10000308	12732526
28	81448	9999705	81450	12277366	10000331	12277803
29	84357	9999686	84360	11854018	10000355	11854440
30	87265	9999667	87269	11452865	10000380	11453301
Co-Sine.	Sine.		Co-Tang.	Tangent.	Co-Secant.	Secant.

89 DEGREES.

## Latitude 00 Deg. 00 Min. North Declination.

		o	d.	2	d.	4	d.	6	d.	8	d.	10	d.	12	d.	14	d.	16	d.	20	d.	22	d.	24	d.	28	d.	32
N	S			b. m.	b. m.	b. m.	b. m.	b. m.	b. m.	b. m.	b. m.	b. m.	b. m.	b. m.	b. m.	b. m.	b. m.	b. m.	b. m.	b. m.	b. m.	b. m.	b. m.	b. m.	b. m.	b. m.	b. m.	b. m.
1	2			12.0	12.0	12.0		12.0	12.0	12.0		12.0	12.0	12.0		12.0	12.0	12.0	12.0	12.0		12.0	12.0	12.0	12.0	12.0	12.0	12.0
3	4			20.1	10.2	20.0		20.0	20.0	20.0		20.0	20.1	20.1		20.1	20.1	20.1	20.1	20.1		20.1	20.1	20.1	20.1	20.1	20.1	20.1
5	6			20.3	30.0	30.0		30.0	30.0	30.0		30.0	30.2	30.2		30.2	30.2	30.2	30.2	30.2		30.2	30.2	30.2	30.2	30.2	30.2	30.2
7	8			30.5	50.0	50.1		50.1	50.2	50.2		50.2	60.3	60.3		60.3	60.3	60.3	60.3	60.3		60.3	60.3	60.3	60.3	60.3	60.3	60.3
9	10			60.8	80.1	80.2		80.2	80.2	80.2		80.2	90.5	90.5		90.5	90.5	90.5	90.5	90.5		90.5	90.5	90.5	90.5	90.5	90.5	90.5
11	12			10.1	130.2	130.3		130.3	130.3	130.3		130.3	140.6	140.6		140.6	140.6	140.6	140.6	140.6		140.6	140.6	140.6	140.6	140.6	140.6	140.6
13	14			20.2	20.4	20.1		20.1	20.1	20.1		20.1	21.4	21.4		21.4	21.4	21.4	21.4	21.4		21.4	21.4	21.4	21.4	21.4	21.4	21.4
15	16			30.5	50.1	50.3		50.3	50.3	50.3		50.3	60.5	60.5		60.5	60.5	60.5	60.5	60.5		60.5	60.5	60.5	60.5	60.5	60.5	60.5



## ° DEGREES.

M	N. Sine.	N. Co-Sine.	N. Tangent.	N. Co-Tang.	N. Secant.	N. Co-Secant.	
30	87265	9999619	87265	11458855	10000380	11459301	30
31	92174	9999593	92174	1159205	10000406	11089656	29
32	97083	9999566	97087	10742648	10000433	10743114	28
33	99992	9999539	99990	10117594	10000461	104117574	27
34	99900	9999511	99905	10117590	10000489	10111185	26
35	101809	9999484	101814	99217943	10000518	98223033	25
36	104718	9999457	104724	95494711	99999548	95494711	24
37	107627	9999430	107633	92506487	10000579	92513869	23
38	110535	9999403	110542	89463336	10000611	90468863	22
39	113444	9999376	113451	86433572	10000644	88149244	21
40	116353	9999349	116361	83403807	10000677	85945609	20
41	119261	9999322	119270	80374042	10000711	83449470	19
42	122170	9999295	122179	77344277	10000746	81553150	18
43	125079	9999268	125085	74314512	10000782	79945684	17
44	127987	9999241	127995	71284747	10000819	77132742	16
45	130896	9999214	130904	68254982	10000857	76306554	15
46	133805	9999187	133817	65225217	10000896	74735856	14
47	136714	9999160	136720	62195452	10000935	73145827	13
48	139622	9999133	139633	59165687	10000975	71622052	12
49	142530	9999106	142543	56135922	10010016	70160474	11
50	145439	9999079	145454	53106157	10010058	68757369	10
51	148348	9999052	148364	50076392	10010101	67409272	9
52	151256	9998885	151273	66105473	10010145	66111036	8
53	154165	9998811	154183	64855003	10010189	64863716	7
54	157073	9998766	157093	63696741	10010234	63664595	6
55	159982	9998720	159992	62499154	10010280	62507153	5
56	162890	9998675	162912	61302935	10010327	61319105	4
57	165799	9998629	165821	60305820	10010375	60314110	3
58	168707	9998584	168731	59268572	10010424	59274308	2
59	171616	9998537	171641	58261174	10010473	58259755	1
60	174524	9998497	174551	57283962	10010523	57293689	0
N. Co-Sine.		N. Sine.	N. Co-Tang.		N. Tangent.	N. Co-Secant.	N. Secant.
							M

89 DEGREES.

## ° DEGREES.

M	L. Sine.	L. Co-Sine.	L. Tangent.	L. Co-Tang.	L. Secant.	L. Co-Secant.	
30	7.9408419	9.9999635	7.9408584	12.0591416	10.0000165	12.0591581	30
31	7.9550819	9.9999823	7.9550996	12.0449004	10.0000177	12.0449181	29
32	7.9688868	9.9999810	7.9688936	12.0311114	10.0000183	12.0311302	28
33	7.9822334	9.9999800	7.9822334	12.0177456	10.0000189	12.0177656	27
34	7.9951980	9.9999788	7.9951980	12.0047806	10.0000192	12.0048020	26
35	8.0077867	9.9999775	8.0077867	11.9921908	10.0000195	11.9922133	25
36	8.0200207	9.9999762	8.0200207	11.9795955	10.0000198	11.9796181	24
37	8.0319195	9.9999745	8.0319195	11.9668054	10.0000202	11.9668281	23
38	8.0435009	9.9999735	8.0435009	11.9538476	10.0000205	11.9538691	22
39	8.0547814	9.9999721	8.0547814	11.9407806	10.0000209	11.9408166	21
40	8.0657763	9.9999706	8.0657763	11.9276493	10.0000214	11.9276837	20
41	8.0764967	9.9999691	8.0764967	11.9144949	10.0000219	11.9145237	19
42	8.0869526	9.9999676	8.0869526	11.9013630	10.0000224	11.9013954	18
43	8.0971832	9.9999663	8.0971832	11.8882738	10.0000229	11.8883068	17
44	8.1071669	9.9999654	8.1071669	11.8752273	10.0000234	11.8752381	16
45	8.1169262	9.9999648	8.1169262	11.8622336	10.0000239	11.8622437	15
46	8.1264710	9.9999641	8.1264710	11.8492909	10.0000244	11.8493006	14
47	8.1358104	9.9999635	8.1358104	11.8364140	10.0000249	11.8364236	13
48	8.1449532	9.9999631	8.1449532	11.8235904	10.0000254	11.8236081	12
49	8.1539975	9.9999629	8.1539975	11.8108184	10.0000259	11.8108369	11
50	8.1628508	9.9999621	8.1628508	11.7980973	10.0000264	11.7981158	10
51	8.1715284	9.9999616	8.1715284	11.7854272	10.0000269	11.7854457	9
52	8.1799729	9.9999610	8.1799729	11.7728071	10.0000274	11.7728250	8
53	8.1882945	9.9999604	8.1882945	11.7602370	10.0000279	11.7602549	7
54	8.1964902	9.9999600	8.1964902	11.7477169	10.0000284	11.7477348	6
55	8.2045703	9.9999594	8.2045703	11.7352468	10.0000289	11.7352647	5
56	8.2125349	9.9999590	8.2125349	11.7228267	10.0000294	11.7228446	4
57	8.2203811	9.9999585	8.2203811	11.7104566	10.0000299	11.7104745	3
58	8.2281135	9.9999581	8.2281135	11.6981365	10.0000304	11.6981544	2
59	8.2357358	9.9999577	8.2357358	11.6858664	10.0000309	11.6858843	1
60	8.2432553	9.9999573	8.2432553	11.6736463	10.0000314	11.6736642	0
	L. Co-Sine.	L. Sine.	L. Co-Tang.	L. Tangent.	L. Co-Secant.	L. Secant.	M

89 DEGREES.

89 DEGREES.

## Latitude 1 Deg. 00 Min. North Declination.

	0	d.	2	4	d.	6	d.	8	d.	10	d.	12	d.	14	d.	16	d.	18	d.	20	d.	22	d.	23
N.S.	b.m.	b.m.	b.m.	b.m.	b.m.	b.m.	b.m.	b.m.	b.m.	b.m.	b.m.	b.m.	b.m.	b.m.	b.m.	b.m.	b.m.	b.m.	b.m.	b.m.	b.m.	b.m.	b.m.	b.m.
1	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0
2	12.1	12.1	12.1	12.1	12.1	12.1	12.1	12.1	12.1	12.1	12.1	12.1	12.1	12.1	12.1	12.1	12.1	12.1	12.1	12.1	12.1	12.1	12.1	12.1
3	12.2	12.2	12.2	12.2	12.2	12.2	12.2	12.2	12.2	12.2	12.2	12.2	12.2	12.2	12.2	12.2	12.2	12.2	12.2	12.2	12.2	12.2	12.2	12.2
4	12.3	12.3	12.3	12.3	12.3	12.3	12.3	12.3	12.3	12.3	12.3	12.3	12.3	12.3	12.3	12.3	12.3	12.3	12.3	12.3	12.3	12.3	12.3	12.3
5	12.4	12.4	12.4	12.4	12.4	12.4	12.4	12.4	12.4	12.4	12.4	12.4	12.4	12.4	12.4	12.4	12.4	12.4	12.4	12.4	12.4	12.4	12.4	12.4
6	12.5	12.5	12.5	12.5	12.5	12.5	12.5	12.5	12.5	12.5	12.5	12.5	12.5	12.5	12.5	12.5	12.5	12.5	12.5	12.5	12.5	12.5	12.5	12.5
7	12.6	12.6	12.6	12.6	12.6	12.6	12.6	12.6	12.6	12.6	12.6	12.6	12.6	12.6	12.6	12.6	12.6	12.6	12.6	12.6	12.6	12.6	12.6	12.6

## Latitude 1 Deg. 00 Min. South Declination.

Table 1. Right Ascension (h, m, s) and Declination (°)																									
	0	d.	2	d.	4	d.	6	d.	8	d.	10	d.	12	d.	14	d.	16	d.	18	d.	20	d.	22	d.	23
	b. m.	m.	b. m.	m.	b. m.	m.	b. m.	m.	b. m.	m.	b. m.	m.	b. m.	m.	b. m.	m.	b. m.	m.	b. m.	m.	b. m.	m.	b. m.	m.	b. m.
5N 12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0
1 00.1	1 00.1	1 00.2	1 00.3	1 00.5	2 00.7	2 00.9	1 01.0	1 01.1	2 01.3	2 01.5	2 01.7	2 01.9	2 02.1	4 02.5	4 02.9	4 03.3	4 03.7	2 04.1	2 04.5	2 04.9	2 05.3	2 05.7	2 06.1	2 06.5	2 06.9
2 00.2	3 00.5	3 00.8	3 01.1	3 01.4	4 01.8	4 02.1	4 02.5	4 02.9	4 03.3	4 03.7	2 04.1	2 04.5	2 04.9	2 05.3	2 05.7	2 06.1	2 06.5	2 06.9	2 07.3	2 07.7	2 08.1	2 08.5	2 08.9	2 09.3	2 09.7
3 00.3	5 00.8	5 01.3	5 01.8	5 02.4	6 03.0	6 03.6	6 04.2	6 04.8	6 05.4	6 06.0	6 06.6	6 07.2	6 07.8	6 08.4	6 09.0	6 09.6	6 10.2	6 10.8	6 11.4	6 12.0	6 12.6	6 13.2	6 13.8	6 14.4	6 15.0
4 00.4	8 01.2	8 02.0	8 02.8	8 03.6	9 04.5	9 05.3	9 06.2	9 07.1	9 08.0	9 08.9	9 09.8	9 10.7	9 11.6	9 12.5	9 13.4	9 14.3	9 15.2	9 16.1	9 17.0	9 17.9	9 18.8	9 19.7	9 20.6	9 21.5	9 22.4
5 00.6	12 01.8	12 03.3	12 04.8	12 06.3	13 07.8	13 09.3	13 10.8	13 12.3	13 13.8	13 15.3	13 16.8	13 18.3	13 19.8	13 21.3	13 22.8	13 24.3	13 25.8	13 27.3	13 28.8	13 30.3	13 31.8	13 33.3	13 34.8	13 36.3	13 37.8
6 01.0	20 03.6	20 05.2	20 06.8	20 08.4	21 09.9	21 11.5	21 13.1	21 14.7	21 16.3	21 17.9	21 19.5	21 21.1	21 22.7	21 24.3	21 25.9	21 27.5	21 29.1	21 30.7	21 32.3	21 33.9	21 35.5	21 37.1	21 38.7	21 40.3	21 41.9
7 02.0	49 10.9	49 20.5	50 30.1	50 40.7	51 50.3	52 00.9	52 11.5	52 22.1	52 32.7	52 43.3	52 53.9	53 04.5	53 15.1	53 25.7	53 36.3	53 46.9	53 57.5	54 08.1	54 18.7	54 29.3	54 39.9	54 50.5	55 01.1	55 11.7	55 22.3



I. D E G R E E.									
M	N. Sine.	N. Co-Sine.	V. Tangent.	V. Co-Tang.	N. Secant.	N. Co-Secant.			
0	174524	9998477	174551	57289962	10001523	57288688	60		
1	177432	9998426	177460	56350590	10001574	56359462	59		
2	180341	9998374	180370	55441517	10001626	55450534	58		
3	183249	9998321	183280	54561300	10001679	54570453	57		
4	186158	9998267	186190	53703837	10001733	53717896	56		
5	189066	9998212	189100	52852109	10001788	52891564	55		
6	191974	9998157	192010	52030673	10001843	52090272	54		
7	194883	9998101	194920	51303157	10001899	51312902	53		
8	197791	9998044	197830	50548526	10001956	50583966	52		
9	200699	9997986	200740	49815825	10002014	49825762	51		
10	203608	9997927	203650	49103881	10002073	49114062	50		
11	206516	9997867	206560	48412134	10002133	48422411	49		
12	209424	9997805	209470	47739591	10002194	47749974	48		
13	212332	9997745	212380	47085343	10002255	47095961	47		
14	215241	9997683	215291	46443862	10002317	46459625	46		
15	218149	9997620	218201	45829351	10002380	45840266	45		
16	221057	9997556	221111	45226141	10002444	45237195	44		
17	223965	9997491	224021	44635556	10002509	44645795	43		
18	226873	9997425	226932	44056113	10002575	44077458	42		
19	229781	9997359	229842	43485122	10002641	43519612	41		
20	232689	9997292	232753	42934677	10002708	42957713	40		
21	235596	9997224	235663	42403464	10002776	42445245	39		
22	238506	9997155	238574	418915790	10002845	41927717	38		
23	241414	9997085	241484	41405381	10002915	41422660	37		
24	244322	9997014	244395	40917412	10002986	40925639	36		
25	247230	9996943	247305	40435837	10003058	40445201	35		
26	250138	9996871	250216	39965460	10003130	39977969	34		
27	253046	9996798	253127	39505345	10003203	39513549	33		
28	255954	9996724	256038	39066771	10003277	39069571	32		
29	258862	9996649	258948	386417735	10003352	38636631	31		
30	261769	9996573	261859	38188459	10003428	38201550	30		
	N. Co-Sine.	N. Sine.	N. Co-Tang.	N. Tangent.	N. Co-Secant.	N. Secant.	M		

I. DEGREE.						
M	<i>L. Sine.</i>	<i>L. Co-Sine.</i>	<i>L. Tangent.</i>	<i>L. Co-Tang.</i>	<i>L. Secant.</i>	<i>L. Co-Secant.</i>
0	8.2418553	9.99993738	8.2419215	11.7580785	10.0000661	11.7581447
1	8.2490332	9.9999316	8.2491015	11.7580858	10.0000684	11.7590663
2	8.2563943	9.9999294	8.2561649	11.7438351	10.0000706	11.7439076
3	8.2630424	9.9999271	8.2631153	11.7368842	10.0000729	11.7369576
4	8.2696810	9.9999247	8.2699563	11.7300437	10.0000753	11.7301890
5	8.2763163	9.9999224	8.2766912	11.7233088	10.0000776	11.7233864
6	8.2829434	9.9999200	8.2833234	11.7166766	10.0000800	11.7167566
7	8.2895773	9.9999175	8.2898585	11.7101441	10.0000825	11.7102266
8	8.2962067	9.9999150	8.2962917	11.7037933	10.0000850	11.7037933
9	8.3028460	9.9999125	8.3028353	11.6973665	10.0000875	11.6974540
10	8.3094791	9.9999100	8.3093842	11.6911158	10.0000900	11.6912059
11	8.3161056	9.9999074	8.3155462	11.6854937	10.0000926	11.6855164
12	8.3210269	9.9999047	8.3211221	11.6798773	10.0000953	11.6798773
13	8.3270163	9.9998021	8.3271143	11.6728357	10.0000979	11.6729837
14	8.3329243	9.9998994	8.3330249	11.6667751	10.0001006	11.6667075
15	8.3387529	9.9998966	8.3385863	11.6611437	10.0001034	11.6612471
16	8.3445043	9.9998939	8.3445105	11.6553895	10.0001061	11.6554957
17	8.3501805	9.9998911	8.3502895	11.6497105	10.0001089	11.6498195
18	8.3557835	9.9998882	8.3558953	11.6441047	10.0001118	11.6442165
19	8.3613150	9.9998853	8.3614297	11.6383703	10.0001147	11.6386850
20	8.3667769	9.9998824	8.3668824	11.6331055	10.0001176	11.6332231
21	8.3721710	9.9998794	8.3722915	11.6277085	10.0001206	11.6278290
22	8.3774988	9.9998764	8.3776423	11.6223777	10.0001236	11.6225012
23	8.3827620	9.9998734	8.3828586	11.6171114	10.0001266	11.6172380
24	8.3879622	9.9998703	8.3880918	11.6119052	10.0001297	11.6121278
25	8.3931008	9.9998672	8.3932336	11.6067664	10.0001328	11.6068992
26	8.3981793	9.9998641	8.3983152	11.6016848	10.0001359	11.6018207
27	8.4031990	9.9998609	8.4033351	11.5966619	10.0001391	11.5968013
28	8.4081614	9.9998577	8.4083037	11.5916963	10.0001423	11.5918356
29	8.4130676	9.9998544	8.4132132	11.5867858	10.0001456	11.5869324
30	8.4179190	9.9998512	8.4180679	11.5819321	10.0001488	11.5820510
	<i>L. Co-Sine.</i>	<i>L. Sine.</i>	<i>L. Co-Tang.</i>	<i>L. Tangent.</i>	<i>L. Co-Secant.</i>	<i>L. Secant.</i>

[illegible]

	<i>0</i>	<i>d.</i>	<i>2</i>	<i>d.</i>	<i>4</i>	<i>d.</i>	<i>6</i>	<i>d.</i>	<i>8</i>	<i>d.</i>	<i>10</i>	<i>d.</i>	<i>12</i>	<i>d.</i>	<i>14</i>	<i>d.</i>	<i>16</i>	<i>d.</i>	<i>18</i>	<i>d.</i>	<i>20</i>	<i>d.</i>	<i>22</i>	<i>d.</i>	<i>24</i>
<i>S N</i>	<i>b. m.</i>	<i>m.</i>	<i>b. m.</i>	<i>m.</i>	<i>b. m.</i>	<i>m.</i>	<i>b. m.</i>	<i>m.</i>	<i>b. m.</i>	<i>m.</i>	<i>b. m.</i>	<i>m.</i>	<i>b. m.</i>	<i>m.</i>	<i>b. m.</i>	<i>m.</i>	<i>b. m.</i>	<i>m.</i>	<i>b. m.</i>	<i>m.</i>	<i>b. m.</i>	<i>m.</i>	<i>b. m.</i>	<i>m.</i>	<i>b. m.</i>
1	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0
2	00.2	1 00.3	1 00.3	1 00.4	2 00.6	2 00.6	2 00.8	2 0.10	1 0.11	1 0.12	2 0.14	2 0.16	2 0.18	2 0.18	2 0.20	2 0.20	2 0.22	2 0.22	2 0.24	2 0.24	2 0.26	2 0.26	2 0.28	2 0.28	2 0.30
3	00.3	3 00.6	3 00.6	3 00.9	3 00.9	3 01.2	4 0.16	4 0.20	3 0.23	3 0.26	4 0.30	4 0.34	4 0.38	4 0.42	4 0.42	4 0.44	4 0.46	4 0.48	4 0.50	4 0.50	4 0.52	4 0.54	4 0.56	4 0.58	4 0.60
4	00.5	5 0.10	5 0.15	5 0.20	6 0.26	6 0.32	6 0.38	6 0.42	5 0.37	6 0.43	6 0.49	6 0.55	6 1.01	7 1.08	7 1.14	7 1.18	7 1.22	7 1.26	7 1.30	7 1.34	7 1.38	7 1.42	7 1.46	7 1.50	7 1.54
5	00.8	8 0.16	8 0.24	8 0.32	8 0.42	9 0.49	9 0.57	9 1.06	9 1.15	9 1.27	10 1.31	10 1.35	10 1.39	10 1.43	10 1.47	10 1.51	10 1.55	11 1.59	11 2.03	11 2.07	11 2.11	11 2.15	11 2.19	11 2.23	11 2.27
6	01.6	20 0.36	21 0.57	21 1.18	21 1.39	21 2.00	25 2.28	29 2.57	29 3.26	29 3.55	29 4.24	30 4.52	30 5.21	30 5.50	30 6.19	30 6.48	30 7.17	30 7.46	30 8.15	30 8.44	30 9.13	30 9.42	30 10.11	30 10.40	30 11.09
7	04.0	48 1.28	48 2.16	49 3.05	49 3.54	49 4.43	49 5.32	49 6.21	49 7.10	49 8.00	49 8.89	49 9.78	49 10.67	49 11.56	49 12.45	49 13.34	49 14.23	49 15.12	49 16.01	49 16.90	49 17.79	49 18.68	49 19.57	49 20.46	49 21.35



A TABLE of Natural and

1 D E G R E E.

M.	N. Sine.	N. Co-Sine.	N. Tangent.	V. Co-Tang.	N. Secant.	N. Co-Secant.		
30	261769	9995573	261869	38183459	10003428	38201550	30	
31	264677	9996496	264770	37765613	10003505	37781849	29	
32	217585	9996419	267531	37575932	10003582	37571273	28	
33	273493	9996341	273592	36956311	10003660	36969528	27	
34	273481	9996262	273583	36562669	10003739	36566332	26	
35	276390	9996182	276414	35177596	10003819	36191414	25	
36	279216	9996101	279235	33820553	10003900	35814517	24	
37	282124	9996019	282216	32431252	10003982	35445391	23	
38	285032	9995936	285149	31062545	10004065	35083500	22	
39	287940	9995853	288068	34711811	10004148	34729515	21	
40	290847	9995769	290970	34367771	10004232	34382316	20	
41	293755	9995684	293832	34027338	10004317	34041924	19	
42	296662	9995598	296792	33691509	10004402	33707345	18	
43	299570	9995511	299735	33356164	10004489	33381176	17	
44	302478	9995424	302616	33021813	10004575	33056300	16	
45	305386	9995336	305548	32679264	10004662	32724556	15	
46	308293	9995247	308439	32342129	10004750	32406713	14	
47	311200	9995157	311351	32012515	10004837	32103665	13	
48	314108	9995065	314263	31682516	10004926	31806225	12	
49	317015	9994974	317171	31352522	10005015	31514446	11	
50	319922	9994881	320036	31021577	10005102	31225777	10	
51	322830	9994788	322958	30693923	10005189	30947607	9	
52	325737	9994694	325910	30363367	10005276	30669558	8	
53	328644	9994600	328822	30041180	10005363	303925017	7	
54	331552	9994503	331734	29714619	10005450	301161201	6	
55	334459	9994406	334645	29382299	10005538	298390265	5	
56	337366	9994308	337558	29054499	10005626	295643373	4	
57	340273	9994209	340471	28721116	10005713	292918821	3	
58	343181	9994109	343383	28392205	10005799	290193169	2	
59	346088	9994009	346295	28067709	10005884	287494394	1	
60	348995	9993908	349208	28662253	10005969	284837005	0	
N. Co-Sine.		N. Sine.	N. Co-Tang.		N. Tangent.	N. Co-Secant.	N. Secant.	M

88

DEGREES.

58 DEGREES.

*Latitude 3 Deg. 00 Min. North Declination.*

[illegible]

1 DEGREE.

M	<i>L. Sine.</i>	<i>L. Co-Sine.</i>	<i>L. Tangent.</i>	<i>L. Co-Tang.</i>	<i>L. Secant.</i>	<i>L. Co-Secant.</i>	
30	8.4179199	9.9998512	8.4186679	11.5812321	10.0001438	11.5822810	30
31	8.4227168	9.9998478	8.4228660	11.5771340	10.0001522	11.5778352	29
32	8.4274621	9.9998445	8.4276176	11.5731824	10.0001555	11.5735173	28
33	8.4321561	9.9998411	8.4323150	11.5693866	10.0001589	11.5697439	27
34	8.4367999	9.9998376	8.4369622	11.5656375	10.0001624	11.5653201	26
35	8.4413949	9.9998342	8.4415603	11.5619397	10.0001658	11.5615656	25
36	8.4459409	9.9998306	8.4461103	11.5582857	10.0001694	11.5582091	24
37	8.4504802	9.9998271	8.4506131	11.5546769	10.0001729	11.5549559	23
38	8.4549834	9.9998235	8.4551639	11.5511203	10.0001765	11.5516166	22
39	8.4593013	9.9998199	8.4594814	11.5476186	10.0001801	11.5482698	21
40	8.4635639	9.9998162	8.4631848	11.5441514	10.0001838	11.5453351	20
41	8.4676785	9.9998125	8.4681175	11.5407125	10.0001875	11.5423150	19
42	8.4716266	9.9998088	8.4724535	11.5373462	10.0001912	11.5392734	18
43	8.4754954	9.9998050	8.4766933	11.5340667	10.0001950	11.5362167	17
44	8.4792832	9.9998012	8.4803820	11.5308680	10.0001988	11.5331925	16
45	8.4829879	9.9997974	8.4839535	11.5277495	10.0002026	11.5311512	15
46	8.4866062	9.9997935	8.4871656	11.5247054	10.0002065	11.5291268	14
47	8.4901398	9.9997897	8.4903252	11.5217395	10.0002104	11.5271696	13
48	8.4935978	9.9997856	8.4937328	11.5188472	10.0002144	11.5252212	12
49	8.4969788	9.9997817	8.4961282	11.5159318	10.0002183	11.5232822	11
50	8.5002847	9.9997776	8.4985127	11.5130003	10.0002224	11.5213535	10
51	8.5035197	9.9997736	8.4998081	11.5100599	10.0002264	11.5194351	9
52	8.5128073	9.9997695	8.5118078	11.5070978	10.0002305	11.5175264	8
53	8.5167264	9.9997653	8.5169016	11.5041332	10.0002347	11.5156275	7
54	8.5205514	9.9997612	8.5207272	11.5011669	10.0002388	11.5137485	6
55	8.5242830	9.9997570	8.5243866	11.4981991	10.0002430	11.5118796	5
56	8.5281017	9.9997527	8.5283490	11.4952300	10.0002473	11.5100308	4
57	8.5318281	9.9997484	8.5319797	11.4922596	10.0002516	11.4681719	3
58	8.5355628	9.9997441	8.5357785	11.4892878	10.0002559	11.4663472	2
59	8.5393156	9.9997398	8.5395445	11.4863154	10.0002602	11.4645377	1
60	8.5428192	9.9997354	8.5429638	11.4833424	10.0002646	11.4627430	0
	<i>L. Co-Sine.</i>	<i>L. Sine.</i>	<i>L. Co-Tang.</i>	<i>L. Tangent.</i>	<i>L. Co-Secant.</i>	<i>L. Secant.</i>	M

88 DEGREES.

Latitude 3 Deg. 00 Min. South Declination

[illegible]



## A TABLE of Natural and

2 DEGREES.

M	N. Sine.	N. Co-Sine.	N. Tangent.	N. Co-Tang.	N. Secant.	N. Co-Secant.	
0	348995	9993908	349208	28656253	10006095	28653708	60
1	351902	9993806	352120	28399397	10006197	28416997	59
2	354809	9993703	355033	28166422	10006300	28184168	58
3	357716	9993599	357945	27937233	10006404	27955125	57
4	360623	9993495	360858	27711740	10006509	27729777	56
5	363530	9993390	363771	27493535	10006615	27508035	55
6	366437	9993284	366593	27271486	10006721	27289814	54
7	369344	9993177	369566	27056557	10006828	27075030	53
8	372251	9993069	372499	26844934	10006936	26863303	52
9	375158	9992960	375422	26636690	10007045	26655455	51
10	378065	9992851	378335	26431600	10007155	26450510	50
11	380971	9992740	381248	26229638	10007266	26245694	49
12	383878	9992629	384161	26030736	10007377	26049937	48
13	386785	9992517	387074	25834823	10007489	25854169	47
14	389692	9992404	389985	25641830	10007602	25661324	46
15	392599	9992290	392901	25451700	10007716	25471337	45
16	395505	9992175	395814	25264361	10007831	25284144	44
17	398411	9992060	398723	25079757	10007947	25099685	43
18	401318	9991944	401631	24897926	10008063	24917900	42
19	404224	9991827	404535	24718912	10008180	24738731	41
20	407131	9991709	407442	24542755	10008298	24562123	40
21	410037	9991590	410348	24369599	10008417	24388020	39
22	412944	9991470	413255	24199574	10008537	24216370	38
23	415850	9991349	416161	24032820	10008658	24047121	37
24	418757	9991228	419067	23869477	10008780	23880224	36
25	421663	9991106	421973	23709457	10008902	23715630	35
26	424569	9990983	424879	23552852	10009025	23559290	34
27	427475	9990859	427785	23399177	10009149	23393161	33
28	430382	9990734	430691	23248566	10009274	23235196	32
29	433288	9990608	433599	23099767	10009400	23079351	31
30	436194	9990482	436509	22953705	10009527	22925586	30
	N. Co-Sine.	N. Sine.	N. Co-Tang.	N. Tangent.	N. Co-Secant.	N. Secant.	M

87 DEGREES.

Latitude + Deg. 00 Min. North Declination.

	2	d.	4	6	d.	8	d.	10	d.	12	d.	14	d.	16	d.	18	d.	20	d.	22	d.	23
	b. m.	m.	b. m.	b. m.	b. m.	b. m.	b. m.	b. m.	b. m.	b. m.	b. m.	b. m.	b. m.	b. m.	b. m.	b. m.	b. m.	b. m.	b. m.	b. m.	b. m.	b. m.
SN 12.0	1	00.1	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0
2 00.2	2	00.1	100.2	100.2	100.3	200.5	100.6	100.7	200.9	201.1	201.3	201.5	201.7	201.9	202.1	202.3	202.5	202.7	202.9	203.1	203.3	203.5
3 00.5	3	00.2	400.6	400.6	400.7	801.1	401.2	401.3	801.5	401.7	401.9	402.1	402.3	402.5	402.7	402.9	403.1	403.3	403.5	403.7	403.9	404.1
4 00.7	4	00.2	600.8	600.8	600.9	1201.4	601.5	601.6	1201.6	601.8	601.9	602.1	602.3	602.5	602.7	602.9	603.1	603.3	603.5	603.7	603.9	604.1
5 01.1	5	00.2	1101.3	1101.3	1101.4	2201.7	1101.8	1101.9	2202.0	1102.1	1102.2	1102.3	1102.4	1102.5	1102.6	1102.7	1102.8	1102.9	1103.0	1103.1	1103.2	1103.3
6 01.6	6	00.4	1902.3	1902.3	1902.4	3802.7	1902.8	1902.9	3803.0	1903.1	1903.2	1903.3	1903.4	1903.5	1903.6	1903.7	1903.8	1903.9	1904.0	1904.1	1904.2	1904.3
7 02.3	7	01.0	4605.6	4605.6	4605.7	9205.9	4606.0	4606.1	9206.2	4606.3	4606.4	4606.5	4606.6	4606.7	4606.8	4606.9	4607.0	4607.1	4607.2	4607.3	4607.4	4607.5
NE 3.35																						

## Artificial Sines, Tangents, and Secants.

2 DEGREES.

M	L. Sine.	L. Co-Sine.	L. Tangent.	L. Co-Tang.	L. Secant.	L. Co-Secant.	
0	8.5428192	9.9997354	8.5430383	11.4569162	10.0002646	11.4571808	60
1	8.5464218	9.9997309	8.5466909	11.4533091	10.0002691	11.4535782	59
2	8.5500948	9.9997265	8.5502683	11.4497317	10.0002735	11.4500052	58
3	8.5535386	9.9997220	8.5538166	11.4461834	10.0002780	11.4464614	57
4	8.5570536	9.9997174	8.5573362	11.4426658	10.0002826	11.4429464	56
5	8.5605404	9.9997128	8.5608276	11.4391724	10.0002872	11.4394596	55
6	8.5639994	9.9997082	8.5642912	11.4357058	10.0002918	11.4360006	54
7	8.5674310	9.9997036	8.5677275	11.4322725	10.0002964	11.4325690	53
8	8.5708357	9.9996989	8.5711363	11.4288632	10.0003011	11.4291643	52
9	8.5742139	9.9996942	8.5745197	11.4254853	10.0003058	11.4257861	51
10	8.5775660	9.9996894	8.5778766	11.4221423	10.0003106	11.4224340	50
11	8.5808923	9.9996846	8.5812077	11.4188293	10.0003154	11.4191077	49
12	8.5841933	9.9996798	8.5845136	11.4155484	10.0003202	11.4158267	48
13	8.5874694	9.9996749	8.5877945	11.4122955	10.0003251	11.4125306	47
14	8.5907209	9.9996700	8.5910509	11.4090741	10.0003300	11.4092791	46
15	8.5939483	9.9996650	8.5942832	11.4058768	10.0003350	11.4060517	45
16	8.5971517	9.9996601	8.5974917	11.4027083	10.0003399	11.4028483	44
17	8.6003317	9.9996550	8.6006767	11.3995693	10.0003449	11.3996683	43
18	8.6034886	9.9996500	8.6038386	11.3964564	10.0003500	11.3965514	42
19	8.6066226	9.9996449	8.6069777	11.3933723	10.0003551	11.3934774	41
20	8.6097341	9.9996398	8.6100943	11.3903195	10.0003602	11.3904269	40
21	8.6128255	9.9996346	8.6131859	11.3872911	10.0003654	11.3873965	39
22	8.6158910	9.9996294	8.6162616	11.3842834	10.0003706	11.3843890	38
23	8.6189369	9.9996242	8.6193127	11.3812917	10.0003758	11.3813861	37
24	8.6219615	9.9996189	8.6223277	11.3783139	10.0003811	11.3784084	36
25	8.6249657	9.9996136	8.6253518	11.3753482	10.0003864	11.3754437	35
26	8.6279481	9.9996083	8.6283402	11.3723958	10.0003918	11.3724916	34
27	8.6309111	9.9996028	8.6313083	11.3694567	10.0003972	11.3695539	33
28	8.6338537	9.9995974	8.6342563	11.3665317	10.0004026	11.3666286	32
29	8.6367764	9.9995919	8.6371845	11.3636215	10.0004081	11.3637186	31
30	8.6396796	9.9995865	8.6400921	11.3599059	10.0004135	11.3600204	30
	L. Co-Sine.	L. Sine.	L. Co-Tang.	L. Tangent.	L. Co-Secant.	L. Secant.	M

87 DEGREES.

Latitude 4 Deg. 00 Min. South Declination.

	2	d.	4	6	d.	8	d.	10	d.	12	d.	14	d.	16	d.	18	d.	20	d.	22	d.	23
	b. m.	m.	b. m.	b. m.	b. m.	b. m.	b. m.	b. m.	b. m.	b. m.	b. m.	b. m.	b. m.	b. m.	b. m.	b. m.	b. m.	b. m.	b. m.	b. m.	b. m.	b. m.
SN 12.0	1	00.1	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0
1 00.2	2	00.1	100.2	100.2	100.3	200.5	100.6	100.7	200.9	201.1	201.3	201.5	201.7	201.9	202.1	202.3	202.5	202.7	202.9	203.1	203.3	203.5
2 00.5	3	00.2	400.6	400.6	400.7	801.1	401.2	401.3	801.5	401.7	401.9	402.1	402.3	402.5	402.7	402.9	403.1	403.3	403.5	403.7	403.9	404.1
3 00.7	4	00.2	600.8	600.8	600.9	1201.4	601.5	601.6	1201.6	601.8	601.9	602.1	602.3	602.5	602.7	602.9	603.1	603.3	603.5	603.7	603.9	604.1
4 01.1	5	00.2	1101.3	1101.3	1101.4	2201.7	1101.8	1101.9	2202.0	1102.1	1102.2	1102.3	1102.4	1102.5	1102.6	1102.7	1102.8	1102.9	1103.0	1103.1	1103.2	1103.3
5 01.6	6	00.4	1902.3	1902.3	1902.4	3802.7	1902.8	1902.9	3803.0	1903.1	1903.2	1903.3	1903.4	1903.5	1903.6	1903.7	1903.8	1903.9	1904.0	1904.1	1904.2	1904.3
6 02.3	7	01.0	4605.6	4605.6	4605.7	9205.9	4606.0	4606.1	9206.2	4606.3	4606.4	4606.5	4606.6	4606.7	4606.8	4606.9	4607.0	4607.1	4607.2	4607.3	4607.4	4607.5
NE 3.35																						



## 2 DEGREES.

M	N. Sine.	N. Co-Sine.	N. Tangent.	N. Co-Tang.	N. Secant.	N. Co-Secant.	M
30	436194	9990482	436609	2293765	10005527	2295586	30
31	439100	9990355	439524	22751502	10009655	2277357	29
32	442006	9990227	442438	22562015	10009783	22584126	28
33	444912	9990098	445353	22374096	10009912	22396137	27
34	447818	9989968	448265	22186077	10010042	22208199	26
35	450724	9989837	451172	22162930	10010173	22186252	25
36	453630	9989705	454097	22221710	10010305	22244403	24
37	456536	9989573	457012	21881251	10010438	21904090	23
38	459442	9989440	459927	21745569	10010571	21765553	22
39	462347	9989306	462842	21605630	10010705	21628759	21
40	465253	9989171	465757	21472401	10010840	21493676	20
41	468159	9989035	468673	21336851	10010976	21360272	19
42	471064	9988898	471588	21202949	10011113	21228515	18
43	473970	9988761	474503	21071461	10011251	21098375	17
44	476876	9988623	477419	20942565	10011390	20969824	16
45	479781	9988484	480334	20815828	10011530	20842830	15
46	482687	9988344	483257	20693220	10011670	20717368	14
47	485592	9988203	486165	20569115	10011811	20593409	13
48	488498	9988061	489082	20446186	10011953	20470925	12
49	491403	9987918	491997	20325307	10012096	20349892	11
50	494308	9987775	494913	20205553	10012240	20230284	10
51	497214	9987631	497829	20086919	10012385	20112075	9
52	500119	9987486	500746	19970219	10012530	19995241	8
53	503024	9987340	503662	19854591	10012676	19879718	7
54	505929	9987193	506575	19740291	10012823	19765604	6
55	508835	9987045	509495	19627295	10012971	19652754	5
56	511740	9986897	512411	19515584	10013120	19541187	4
57	514645	9986748	515328	19405133	10013270	19430882	3
58	517550	9986598	518244	19295922	10013420	19321816	2
59	520455	9986447	521161	19187930	10013571	19213970	1
60	523360	9986295	524078	19081137	10013723	19107323	0
N. Co-Sine.	N. Sine.	N. Co-Tang.	N. Tangent.	N. Co-Secant.	N. Secant.	M	

## 87 DEGREES.

## Latitude 5 Deg. 00 Min. North Declination.

	2		d.	4	d.	6	d.	8	d.	10	d.	12	d.	14	d.	16	d.	18	d.	20	d.	22	d.	23
	b. m.		m.	b. m.	n.	b. m.	n.	b. m.	n.	b. m.	n.	b. m.	n.	b. m.	n.	b. m.	n.	b. m.	n.	b. m.	n.	b. m.	n.	b. m.
S N	12.0		N S	12.0		12.0		12.0		12.0		12.0		12.0		12.0		12.0		12.0		12.0		12.0
1	00.2		1			00.1		1 00.2		2 00.4		1 00.5		1 00.6		2 00.8		2 01.0		2 01.2		2 01.4		2 01.6
2	00.4		2			00.2		2 00.5		3 00.8		3 01.1		3 01.4		4 01.6		4 02.2		4 02.6		4 03.0		3 03.3
3	00.6		3			00.3		3 00.8		6 01.4		5 01.9		6 02.5		6 03.1		6 03.7		6 04.3		6 04.5		5 04.4
4	01.2		4			00.4		4 01.2		8 02.2		9 02.9		9 03.8		9 04.7		9 05.6		9 06.5		9 07.1		7 12.2
5	02.2		5			00.6		5 02.2		10 03.1		11 03.4		11 03.8		11 04.1		11 04.5		11 04.9		11 05.3		3 21.0
6	02.8		6			01.0		6 03.0		21 05.1		27 11.8		27 12.7		28 14.5		28 16.0		28 17.1		28 18.0		4 00.0
7	03.4		7			01.5		7 03.5		1 08 53		2 01												
NE	4.12																							

## 2 DEGREES.

M	L. Sine.	L. Co-Sine.	L. Tangent.	L. Co-Tang.	L. Secant.	L. Co-Secant.	M
30	8.6396796	9.9995865	8.6400931	11.3599069	10.0004135	11.3603204	30
31	8.6425634	9.9995809	8.6429823	11.3570175	10.0004191	11.3574366	29
32	8.6454282	9.9995753	8.6458523	11.3541472	10.0004247	11.3545718	28
33	8.6482742	9.9995697	8.6487044	11.3512956	10.0004303	11.3517258	27
34	8.6511016	9.9995641	8.6515375	11.3484625	10.0004359	11.3488984	26
35	8.6539107	9.9995584	8.6543522	11.3456478	10.0004416	11.3460832	25
36	8.6567017	9.9995527	8.6571490	11.3428510	10.0004473	11.3432983	24
37	8.6594748	9.9995469	8.6599279	11.3400721	10.0004530	11.3405252	23
38	8.6622303	9.9995411	8.6626891	11.3373109	10.0004589	11.3377692	22
39	8.6649684	9.9995353	8.6654331	11.3345669	10.0004647	11.3350316	21
40	8.6676893	9.9995295	8.6681598	11.3318402	10.0004705	11.3323107	20
41	8.6703932	9.9995236	8.6708597	11.3291303	10.0004764	11.3296668	19
42	8.6730804	9.9995176	8.6735628	11.3264372	10.0004824	11.3269196	18
43	8.6757510	9.9995116	8.6762393	11.3237607	10.0004884	11.3242490	17
44	8.6784052	9.9995056	8.6788995	11.3211004	10.0004944	11.3215943	16
45	8.6810433	9.9994996	8.6815437	11.3184563	10.0005004	11.3189567	15
46	8.6836654	9.9994935	8.6841719	11.3158281	10.0005065	11.3163346	14
47	8.6862718	9.9994874	8.6867844	11.3132166	10.0005126	11.3137282	13
48	8.6888635	9.9994812	8.6893813	11.3106187	10.0005188	11.3111375	12
49	8.6914379	9.9994750	8.6919629	11.3080371	10.0005250	11.3085621	11
50	8.6939980	9.9994688	8.6945292	11.3054708	10.0005312	11.3060190	10
51	8.6965431	9.9994625	8.6970806	11.3029191	10.0005375	11.3034569	9
52	8.6990734	9.9994562	8.6996173	11.3003828	10.0005438	11.3009266	8
53	8.7015889	9.9994498	8.7021390	11.2978610	10.0005502	11.2984111	7
54	8.7040899	9.9994435	8.7046463	11.2953535	10.0005565	11.2959101	6
55	8.7065766	9.9994372	8.7071395	11.2928603	10.0005630	11.2934234	5
56	8.7090490	9.9994308	8.7096185	11.2903815	10.0005694	11.2909510	4
57	8.7115075	9.9994244	8.7120834	11.2879166	10.0005759	11.2884925	3
58	8.7139520	9.9994179	8.7145345	11.2854655	10.0005824	11.2860480	2
59	8.7163829	9.9994116	8.7169719	11.2830281	10.0005890	11.2836171	1
60	8.7188002	9.9994054	8.7193958	11.2806042	10.0005956	11.2811998	0
L. Co-Sine.	L. Sine.	L. Co-Tang.	L. Tangent.	L. Co-Secant.	L. Secant.	M	

## 87 DEGREES.

## Latitude 5 Deg. 00 Min. South Declination.

	0	d. 2	d. 4	d. 6	d. 8	d. 10	d. 12	d. 14	d. 16	d. 18	d. 20	d. 22	d. 24
	b. m.	b. m.	b. m.	b. m.	b. m.	b. m.	b. m.	b. m.	b. m.	b. m.	b. m.	b. m.	b. m.
5 N 12.0		12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0
1 00.4	1 00.5	1 00.6	2 00.8	2 01.0	2 01.2	3 01.3	3 01.4	4 01.6	4 01.8	5 02.0	5 02.2	6 02.4	6 02.6
2 00.8	3 01.1	3 01.4	3 01.7	3 02.1	4 02.5	4 02.8	5 03.1	5 03.5	6 03.9	6 04.3	7 04.7	7 05.0	8 05.4
3 01.3	5 01.8	5 02.3	6 02.8	6 03.4	6 04.0	7 04.5	7 05.1	8 05.7	8 06.2	9 06.9	9 07.6	10 08.1	10 08.7
4 02.0	8 02.8	8 03.6	9 04.4	9 05.2	9 06.0	9 06.9	9 07.8	10 08.7	10 09.6	11 10.5	11 11.4	12 12.3	12 13.2
5 02.8	12 04.2	13 05.1	13 06.1	14 07.1	14 08.1	15 09.1	15 10.1	16 11.1	16 12.1	17 13.1	18 14.1	19 15.1	20 16.1
6 03.5	19 04.8	19 05.7	20 06.8	20 07.8	21 08.9	21 10.0	22 11.1	22 12.2	23 13.3	24 14.4	25 15.5	26 16.6	27 17.7
7 04.2	21 05.9	21 06.8	22 07.9	22 08.9	23 10.0	23 11.1	24 12.2	24 13.3	25 14.4	26 15.5	27 16.6	28 17.7	29 18.8
NE 6.00													







M	N. Sine.	N. Co-Sine.	N. Tangent.	N. Co-Tang.	N. Secant.	N. Co-Secant.	
30	610485	9981348	611625	16349855	10018687	16380408	30
31	613389	9981170	614546	16272174	10018866	16302873	29
32	616292	9980991	617465	16195225	10019046	16226069	28
33	619196	9980811	620365	16118995	10019226	16149987	27
34	622099	9980630	623306	16043482	10019407	16074617	26
35	625002	9980449	626228	15968667	10019589	15999248	25
36	627905	9980267	629147	15894545	10019772	15925971	24
37	630808	9980084	632067	15821104	10019956	15852676	23
38	633711	9979900	634988	15748337	10020141	15780064	22
39	636614	9979715	637908	15676233	10020326	15708066	21
40	639517	9979529	640829	15604734	10020512	15636793	20
41	642420	9979343	643750	15533981	10020699	15566135	19
42	645323	9979156	646671	15463814	10020887	15496914	18
43	648225	9978968	649592	15394276	10021076	15426721	17
44	651129	9978779	652513	15325358	10021266	15357949	16
45	654031	9978589	655435	15257052	10021457	15289788	15
46	656934	9978398	658356	15189349	10021649	15222231	14
47	659836	9978206	661278	15122242	10021841	15155279	13
48	662739	9978014	664199	15055723	10022034	15088856	12
49	665641	9977821	667121	14989734	10022228	15023103	11
50	668544	9977627	670043	14924417	10022423	14957882	10
51	671446	9977432	672965	14859615	10022619	14893226	9
52	674348	9977236	675887	14795372	10022816	14829128	8
53	677251	9977039	678809	14731695	10023013	14765580	7
54	680153	9976842	681732	14668529	10023211	14702576	6
55	683055	9976644	684654	14605916	10023410	14640109	5
56	685957	9976445	687577	14543833	10023610	14578171	4
57	688859	9976245	690499	14482273	10023811	14516767	3
58	691761	9976044	693422	14421230	10024013	14455899	2
59	694663	9975842	696345	14360695	10024216	14395471	1
60	697565	9975640	699268	14300665	10024419	14335587	0
	N. Co-Sine.	N. Sine.	N. Co-Tang.	N. Tangent.	N. Co-Secant.	N. Secant.	M

[illegible]

M	<i>L. Sine.</i>	<i>L. Co-Sine.</i>	<i>L. Tangent.</i>	<i>L. Co-Tang.</i>	<i>L. Secant.</i>	<i>L. Co-Secant.</i>	
30	8.7856753	9.9991832	8.7854561	11.2135139	10.0008168	11.2143247	20
31	8.7877359	9.9991855	8.7858544	11.2114455	10.0008185	11.2122641	30
32	8.7897867	9.9991737	8.7906130	11.2093870	10.0008263	11.2102133	28
33	8.7918278	9.9991659	8.7926620	11.2073370	10.0008341	11.2081722	27
34	8.7938594	9.9991580	8.7947014	11.2052986	10.0008420	11.2061406	26
35	8.7958814	9.9991501	8.7967513	11.2032587	10.0008499	11.2041186	25
36	8.7978941	9.9991422	8.7987519	11.2012151	10.0008578	11.2021059	24
37	8.7998974	9.9991342	8.8007632	11.1992368	10.0008658	11.2001026	23
38	8.8018915	9.9991262	8.8027653	11.1972347	10.0008738	11.1981085	22
39	8.8038864	9.9991182	8.8047583	11.1952417	10.0008818	11.1961236	21
40	8.8058823	9.9991101	8.8067422	11.1932578	10.0008899	11.1941477	20
41	8.8078792	9.9991020	8.8087171	11.1912828	10.0008980	11.1921808	19
42	8.8098772	9.9990938	8.8106934	11.1893166	10.0009062	11.1902228	18
43	8.8118764	9.9990856	8.8126707	11.1873593	10.0009144	11.1882736	17
44	8.8138768	9.9990774	8.8146584	11.1854166	10.0009226	11.1863332	16
45	8.8158795	9.9990691	8.8166524	11.1834706	10.0009309	11.1844015	15
46	8.8178847	9.9990608	8.8186608	11.1815392	10.0009392	11.1824783	14
47	8.8198923	9.9990525	8.8206838	11.1796162	10.0009475	11.1805637	13
48	8.8219025	9.9990441	8.8227284	11.1777011	10.0009559	11.1786575	12
49	8.8239240	9.9990357	8.8247846	11.1757954	10.0009643	11.1767596	11
50	8.8259529	9.9990273	8.8268626	11.1738974	10.0009727	11.1748701	10
51	8.8279912	9.9990188	8.8279924	11.1720067	10.0009812	11.1729888	9
52	8.8288844	9.9990103	8.8298741	11.1701259	10.0009897	11.1711156	8
53	8.8307495	9.9990017	8.8317478	11.1682525	10.0009983	11.1692505	7
54	8.8326066	9.9989931	8.8336134	11.1663866	10.0010069	11.1673934	6
55	8.8344557	9.9989845	8.8354712	11.1645288	10.0010155	11.1655443	5
56	8.8362969	9.9989758	8.8373211	11.1626789	10.0010242	11.1637031	4
57	8.8381304	9.9989671	8.8391633	11.1608367	10.0010329	11.1618696	3
58	8.8399561	9.9989584	8.8409977	11.1589933	10.0010416	11.1600439	2
59	8.8417741	9.9989496	8.8428244	11.1571755	10.0010504	11.1582239	1
60	8.8435845	9.9989408	8.8446337	11.1553763	10.0010592	11.1564155	0
	<i>L. Co-Sine.</i>	<i>L. Sine.</i>	<i>L. Co-Tang.</i>	<i>L. Tangent.</i>	<i>L. Co-Secant.</i>	<i>L. Secant.</i>	M

[illegible]



M	N. Sine.	N. Co-Sine.	N. Tangent.	N. Co-Tang.	N. Secant.	N. Co-Secant.	
0	697565	9275640	699268	14300666	10024419	14335597	60
1	700466	9975437	702191	14241134	10024632	14276200	59
2	703368	9975233	705115	14182092	10024828	14217304	58
3	706270	9975028	708038	14123536	10025034	14158894	57
4	709171	9974822	710961	14064559	10025241	14100962	56
5	712073	9974615	713885	14005786	10025449	14043504	55
6	714974	9974407	716809	13947019	10025658	13985614	54
7	717875	9974199	719733	13888245	10025868	13929985	53
8	720777	9973990	722657	13829472	10026078	13873913	52
9	723678	9973780	725581	13770698	10026289	13818291	51
10	726580	9973569	728505	13711925	10026501	13763115	50
11	729481	9973357	731430	13653156	10026714	13708379	49
12	732382	9973144	734354	13594389	10026928	13654077	48
13	735283	9972931	737279	13535639	10027143	13602205	47
14	738184	9972717	740203	13476895	10027358	13546758	46
15	741085	9972502	743128	13418158	10027574	13493731	45
16	743986	9972286	746053	13359427	10027791	13441118	44
17	746887	9972069	748978	13300693	10028009	13388914	43
18	749787	9971851	751903	13241957	10028228	13337116	42
19	752688	9971632	754828	13183219	10028448	13285719	41
20	755589	9971413	757753	13124483	10028668	13234716	40
21	758490	9971193	760678	13065747	10028889	13184106	39
22	761390	9970972	763603	13007011	10029111	13133882	38
23	764290	9970750	766528	12948275	10029334	13084240	37
24	767190	9970527	769453	12889539	10029558	13034576	36
25	770091	9970303	772378	12830802	10029783	12984856	35
26	772991	9970079	775303	12772065	10030009	12935675	34
27	775891	9969858	778228	12713328	10030236	12886410	33
28	778791	9969638	781153	12654591	10030464	12840452	32
29	781691	9969417	784078	12595854	10030693	12792779	31
30	784591	9969193	787003	12537117	10030922	12745495	30
	N. Co-Sine.	N. Sine.	N. Co-Tang.	N. Tangent.	N. Co-Secant.	N. Secant.	M

*Latitude 8 Deg. 00 Min. North Declination.*

[illegible]

4 DEGREES.							
M	<i>L. Sine.</i>	<i>L. Co-Sine.</i>	<i>L. Tangent.</i>	<i>L. Co-Tang.</i>	<i>L. Secant.</i>	<i>L. Co-Secant.</i>	
0	8.8435845	9.9989408	8.8446437	11.1553563	10.0010592	11.1564155	60
1	8.8453874	9.9989319	8.8464554	11.1535446	10.0010581	11.1546126	59
2	8.8471827	9.9989230	8.8482597	11.1517403	10.0010570	11.1528173	58
3	8.8489707	9.9989141	8.8500566	11.1499434	10.0010559	11.1510293	57
4	8.8507512	9.9989052	8.8518461	11.1481539	10.0010948	11.1492488	56
5	8.8525245	9.9988962	8.8536283	11.1463717	10.0010937	11.1474755	55
6	8.8542905	9.9988871	8.8554034	11.1445966	10.0011129	11.1457095	54
7	8.8560493	9.9988780	8.8571713	11.1428287	10.0011220	11.1439507	53
8	8.8578010	9.9988689	8.8589321	11.1410679	10.0011311	11.1421920	52
9	8.8595457	9.9988598	8.8606859	11.1393141	10.0011402	11.1404453	51
10	8.8612833	9.9988506	8.8624327	11.1375673	10.0011494	11.1387167	50
11	8.8630139	9.9988414	8.8641725	11.1358275	10.0011586	11.1369861	49
12	8.8647376	9.9988321	8.8659055	11.1340945	10.0011679	11.1352624	48
13	8.8664545	9.9988228	8.8676317	11.1323633	10.0011772	11.1335455	47
14	8.8681646	9.9988135	8.8693511	11.1306449	10.0011865	11.1318354	46
15	8.8698680	9.9988041	8.8710638	11.1289362	10.0011959	11.1301320	45
16	8.8715646	9.9987947	8.8727699	11.1272351	10.0012053	11.1284355	44
17	8.8732546	9.9987853	8.8744694	11.1255306	10.0012147	11.1267454	43
18	8.8749381	9.9987758	8.8761623	11.1238377	10.0012242	11.1250519	42
19	8.8766150	9.9987663	8.8778486	11.1221513	10.0012337	11.1233580	41
20	8.8782854	9.9987567	8.8795286	11.1204714	10.0012433	11.1216746	40
21	8.8799493	9.9987471	8.8812022	11.1187975	10.0012529	11.1200007	39
22	8.8816059	9.9987375	8.8828694	11.1171306	10.0012625	11.1183931	38
23	8.8832581	9.9987278	8.8845303	11.1154697	10.0012722	11.1167749	37
24	8.8849031	9.9987181	8.8861850	11.1138150	10.0012819	11.1151569	36
25	8.8865418	9.9987084	8.8878334	11.1121666	10.0012916	11.1135482	35
26	8.8881743	9.9986986	8.8894757	11.1105243	10.0013014	11.1119425	34
27	8.8898007	9.9986888	8.8911119	11.1088888	10.0013112	11.1103393	33
28	8.8914209	9.9986790	8.8927420	11.1072580	10.0013210	11.1087391	32
29	8.8930351	9.9986691	8.8943660	11.1056340	10.0013309	11.1071396	31
30	8.8946433	9.9986591	8.8959842	11.1040158	10.0013409	11.1055467	30
	<i>L. Co-Sine.</i>	<i>L. Sine.</i>	<i>L. Co-Tang.</i>	<i>L. Tangent.</i>	<i>L. Co-Secant.</i>	<i>L. Secant.</i>	M

Latitude 8 Deg. 00 Min. South Declination.

[illegible]



## A TABLE of Natural and

## 4 DEGREES.

M	N. Sine.	N. Co-Sine.	N. Tangent.	N. Co-Tang.	N. Secant.	N. Co-Secant.	M	
30	784591	9969173	787017	12706225	10039222	12745495	30	
31	787491	9968944	789944	12699125	10031152	12698560	29	
32	790391	9968715	792871	12612390	10031383	12651971	28	
33	793290	9968485	795798	12565997	10031615	12605724	27	
34	796190	9968254	798726	12519942	10031848	12559815	26	
35	799090	9968022	801653	12474221	10032081	12514240	25	
36	801989	9967789	804581	12428831	10032315	12468995	24	
37	804889	9967555	807509	12383768	10032550	12424078	23	
38	807788	9967320	810437	12339028	10032786	12379484	22	
39	810687	9967085	813365	12294608	10033023	12335210	21	
40	813587	9966849	816293	12250506	10033261	12291252	20	
41	816486	9966612	819221	12206716	10033500	12247608	19	
42	819385	9966374	822150	12163236	10033740	12204274	18	
43	822284	9966135	825078	12120062	10033980	12161246	17	
44	825183	9965895	828007	12077192	10034221	12118822	16	
45	828082	9965655	830936	12034622	10034463	12076098	15	
46	830981	9965414	833865	11992349	10034706	12033970	14	
47	833880	9965172	836794	11950370	10034951	11992317	13	
48	836778	9964929	839723	11908682	10035195	11950595	12	
49	839677	9964685	842653	11867282	10035441	11909340	11	
50	842576	9964440	845583	11826167	10035687	11868370	10	
51	845474	9964194	848512	11785333	10035934	11827683	9	
52	848373	9963948	851442	11744779	10036182	11787274	8	
53	851271	9963701	854372	11704500	10036431	11747141	7	
54	854169	9963453	857302	11664495	10036681	11707282	6	
55	857067	9963204	860233	11624761	10036932	11667693	5	
56	859966	9962954	863163	11585294	10037184	11628372	4	
57	862864	9962703	866094	11546093	10037436	11589316	3	
58	865762	9962452	869025	11507154	10037689	11550523	2	
59	868660	9962200	871956	11468474	10037943	11511990	1	
60	871557	9961947	874887	11429052	10038198	11473713	0	
N. Co-Sine.		N. Sine.	N. Co-Tang.		N. Tangent.	N. Co-Secant.	N. Secant.	M
								85 DEGREES.

## 85 DEGREES.

## Latitude 9 Deg. 00 Min. North Declination.

	2 d.	4 d.	6 d.	8 d.		d.	10 d.	12 d.	14 d.	16 d.	18 d.	20 d.	22 d.	23 d.
	b. m.	b. m.	b. m.	b. m.		b. m.	b. m.	b. m.	b. m.	b. m.	b. m.	b. m.	b. m.	b. m.
S N 12.0	12.0	12.0	12.0	12.0	N 5	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0
1 00.5	1 00.4	1 00.3	2 00.1		1	00.1	1 00.2	1 00.3	2 00.5	2 00.7	2 00.9	2 01.1	1 01.2	
2 01.1	3 00.8	3 00.5	3 00.2		2	00.2	3 00.5	3 00.8	3 01.1	4 01.5	4 01.9	4 02.3	3 02.6	
3 01.8	5 01.3	5 00.8	5 00.3		3	00.3	5 00.8	5 01.3	6 01.9	6 02.5	6 03.1	7 03.8	5 04.3	
4 02.8	8 02.0	8 01.2	8 00.4		4	00.4	8 01.2	8 02.0	9 02.9	9 03.8	9 04.7	10 05.7	8 10.5	
5 04.0	11 02.9	11 01.8	12 00.6		5	00.6	13 02.9	13 03.2	14 04.6	14 10.2	14 11.4	15 12.0	12 14.2	
6 10.3	17 04.6	18 02.8	18 01.0		6	01.0	25 03.5	25 1 00.25	1 25.25	1 50.25	2 15.40	2 55.47	47 34.2	
7 15.8	32 1.26	32 05.4	33 02.1		7	02.1	54 1.15							
NE 5.08	12 4.06	13 3.03	13 2.00											

## Artificial Sines, Tangents, and Secants.

## 4 DEGREES.

M	L. Sine.	L. Co-Sine.	L. Tangent.	L. Co-Tang.	L. Secant.	L. Co-Secant.	
30	8.8946433	9.9986591	8.8959842	11.1040158	10.0013409	11.1053567	30
31	8.8962455	9.9986492	8.8975963	11.1024037	10.0013508	11.1037545	29
32	8.8978418	9.9986392	8.8992026	11.1007974	10.0013608	11.1021582	28
33	8.8994322	9.9986292	8.9008030	11.0991970	10.0013708	11.1005676	27
34	8.9010168	9.9986191	8.9023977	11.0976023	10.0013809	11.0989832	26
35	8.9025955	9.9986090	8.9039866	11.0960134	10.0013910	11.0974045	25
36	8.9041635	9.9985988	8.9055697	11.0944303	10.0014012	11.0958315	24
37	8.9057338	9.9985886	8.9071472	11.0928528	10.0014114	11.0942542	23
38	8.9072975	9.9985784	8.9087190	11.0912810	10.0014216	11.0926792	22
39	8.9088535	9.9985682	8.9102853	11.0897147	10.0014318	11.0911065	21
40	8.9104039	9.9985579	8.9118460	11.0881540	10.0014421	11.0895361	20
41	8.9119457	9.9985475	8.9134012	11.0865988	10.0014525	11.0880513	19
42	8.9134881	9.9985372	8.9149509	11.0850491	10.0014628	11.0865119	18
43	8.9150219	9.9985268	8.9164952	11.0835038	10.0014732	11.0849781	17
44	8.9165504	9.9985163	8.9180340	11.0819660	10.0014837	11.0834406	16
45	8.9180734	9.9985058	8.9195675	11.0804325	10.0014942	11.0819265	15
46	8.9195911	9.9984953	8.9210957	11.0789033	10.0015047	11.0804089	14
47	8.9211034	9.9984848	8.9226185	11.0773784	10.0015152	11.0788966	13
48	8.9226105	9.9984742	8.9241363	11.0758637	10.0015253	11.0773895	12
49	8.9241123	9.9984636	8.9256457	11.0743513	10.0015356	11.0758877	11
50	8.9256089	9.9984529	8.9271560	11.0728440	10.0015471	11.0743911	10
51	8.9271003	9.9984422	8.9286581	11.0713419	10.0015578	11.0728997	9
52	8.9285866	9.9984315	8.9301552	11.0698445	10.0015685	11.0714134	8
53	8.9300678	9.9984207	8.9316471	11.0683529	10.0015793	11.0699522	7
54	8.9315439	9.9984099	8.9331340	11.0668660	10.0015901	11.0684651	6
55	8.9330150	9.9983990	8.9346160	11.0653840	10.0016010	11.0669850	5
56	8.9344811	9.9983881	8.9360929	11.0639071	10.0016119	11.0655189	4
57	8.9359422	9.9983772	8.9375650	11.0624350	10.0016228	11.0640578	3
58	8.9373983	9.9983663	8.9390321	11.0609679	10.0016337	11.0626017	2
59	8.9388496	9.9983553	8.9404944	11.0595056	10.0016447	11.0611504	1
60	8.9402960	9.9983442	8.9419518	11.0580482	10.0016558	11.0597040	0
L. Co-Sine.		L. Sine.	L. Co-Tang.		L. Tangent.	L. Co-Secant.	L. Secant.
							M

## 85 DEGREES.

## Latitude 9 Deg. 00 Min. South Declination.

	0 d.	2 d.	4 d.	6 d.	8 d.	10 d.	12 d.	14 d.	16 d.	18 d.	20 d.	22 d.	23 d.
	b. m.	b. m.	b. m.	b. m.	b. m.	b. m.	b. m.	b. m.	b. m.	b. m.	b. m.	b. m.	b. m.
S N 12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0
1 00.5	1 00.8	1 00.9	1 00.9	2 01.1	2 01.3	2 01.5	1 01.6	2 01.8	2 02.0	2 02.2	2 02.4	2 02.6	1 02.7
2 01.7	3 01.8	3 02.1	3 02.1	3 02.4	3 02.7	4 03.1	3 03.4	3 03.7	4 04.1	4 04.5	4 04.9	5 05.4	2 04.6
3 02.4	5 02.9	5 03.4	5 03.9	5 04.4	6 05.0	6 05.5	6 10.1	6 10.7	6 11.3	6 11.9	7 12.6	5 13.1	
4 03.6	7 04.3	8 05.1	8 05.9	8 10.7	8 11.5	8 12.3	9 13.2	9 14.1	9 15.0	9 15.9	10 16.9	7 17.6	
5 05.1	11 04.2	12 16.2	12 18.2	12 18.2	12 18.2	12 18.2	13 20.5	13 21.8	13 23.1	14 24.5	14 25.9	15 31.5	13 28.8
6 12.3	18 14.1	18 15.9	18 17.9	18 19.9	19 21.9	19 23.9	20 25.9	20 27.9	21 29.9	22 31.9	23 33.9	24 35.9	
7 23.3	34 30.7	35 34.2	35 41.7	35 48.2	35 54.7	36 01.2	37 03.2	37 05.2	38 07.2	39 09.2	40 11.2	41 13.2	
NE 6.00													



## S DEGREES.

M	N. Sine.	N. Co-Sine.	N. Tangent.	N. Co-Tang.	N. Secant.	N. Co-Secant.	
1	871557	9261947	874887	1143002	10038198	11473713	60
2	871455	9261633	877818	11391885	10038454	11435692	59
3	871353	9261438	880749	11353970	10038711	11397922	58
4	871251	9261182	883681	11316304	10038959	11360402	57
5	871148	9260926	886612	11278886	10039228	11323129	56
6	871046	9260669	889544	11241712	10039487	11286101	55
7	870943	9260411	892475	11204790	10039747	11249316	54
8	870840	9260152	895408	11168069	10040008	11212770	53
9	870738	9259892	898341	11131638	10040270	11176462	52
10	870635	9259631	901273	11095416	10040533	11140389	51
11	870532	9259369	904206	11059411	10040797	11104549	50
12	870429	9259107	907138	11023676	10041061	11068940	49
13	870326	9258844	910071	10988150	10041326	11033560	48
14	870223	9258580	913004	10952850	10041592	10998406	47
15	870119	9258315	915938	10917775	10041859	10963476	46
16	870016	9258049	918871	10882921	10042127	10928768	45
17	869913	9257782	921804	10848288	10042396	10894281	44
18	869810	9257515	924738	10813872	10042666	10860011	43
19	869706	9257247	927672	10779675	10042937	10825957	42
20	869603	9256978	930606	10745687	10043208	10792117	41
21	869500	9256708	933540	10711913	10043480	10758435	40
22	869397	9256437	936474	10678348	10043753	10725000	39
23	869294	9256165	939409	10644992	10044027	10691800	38
24	869191	9255892	942344	10611841	10044302	10658854	37
25	869088	9255619	945278	10578895	10044578	10626054	36
26	868985	9255345	948213	10546161	10044855	10593455	35
27	868882	9255070	951148	10513677	10045133	10561057	34
28	868779	9254794	954084	10481261	10045411	10528857	33
29	868676	9254517	957019	10448912	10045690	10496854	32
30	868573	9254240	959955	10416715	10045970	10465046	31
31	868470	9253962	962890	10384697	10046251	10433430	30
N. Co-Sine.	N. Sine.	N. Co-Tang.	N. Tangent.	N. Co-Secant.	N. Secant.	M	

84 DEGREES.

Latitude 10 Deg. 00 Min. North Declination.

10 to 12 Deg. C. Rain.											13 to 16 Deg. C. Rain.												
1	2	d.	4	d.	6	d.	8		10		12	d.	14	d.	16	d.	18	d.	20	d.	22	d.	24
S N		b. m.	b. m.	b. m.	b. m.	b. m.	b. m.		N		b. m.	b. m.	b. m.	b. m.	b. m.	b. m.	b. m.	b. m.	b. m.	b. m.	b. m.	b. m.	b. m.
1	00.6	12.0	12.0	12.0	12.0	12.0	12.0		1	00.6	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0
2	01.2	12.0	12.0	12.0	12.0	12.0	12.0		2	00.4	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0
3	02.1	12.0	12.0	12.0	12.0	12.0	12.0		3	00.5	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0
4	03.2	12.0	12.0	12.0	12.0	12.0	12.0		4	00.5	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0
5	04.6	12.0	12.0	12.0	12.0	12.0	12.0		5	01.2	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0
6	1.12	12.0	12.0	12.0	12.0	12.0	12.0		6	02.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0
7	2.11	12.0	12.0	12.0	12.0	12.0	12.0		7	03.6	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0
8	3.13	12.0	12.0	12.0	12.0	12.0	12.0																



		Latitude 11 Deg. 00 Min.										South Declination.														
		0	d.	2	d	4	d.	6	d.	8	d.	10	d.	12	d.	14	d.	16	d.	18	d.	20	d.	22	d.	24
		b. m.	m. b. m.	m. b. m.	m. b. m.	m. b. m.	m. b. m.	m. b. m.	m. b. m.	m. b. m.	m. b. m.	m. b. m.	m. b. m.	m. b. m.	m. b. m.	m. b. m.	m. b. m.	m. b. m.	m. b. m.	m. b. m.	m. b. m.	m. b. m.	m. b. m.	m. b. m.	m. b. m.	m. b. m.
S	N	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0
1		00.9	10.10	10.11	2.0.13	2.0.13	2.0.15	2.0.17	10.18	10.19	20.21	20.23	20.25	20.27	10.28	10.29	10.30	10.31	10.32	10.33	10.34	10.35	10.36	10.37	10.38	
2		0.18	30.21	30.24	30.27	30.30	40.34	30.37	30.40	40.44	40.48	40.52	40.56	30.59	30.62	30.65	30.68	30.71	30.74	30.77	30.80	30.83	30.86	30.89	30.92	
3		0.29	50.34	50.39	50.44	50.49	60.55	51.00	61.06	61.12	61.18	61.24	61.30	51.36	51.42	51.48	51.54	51.60	51.66	51.72	51.78	51.84	51.90	51.96	52.02	
4		0.43	70.50	80.58	81.06	81.14	81.22	81.30	81.38	91.47	91.56	92.05	102.15	72.24	72.33	72.42	72.51	72.60	72.69	72.78	72.87	72.96	73.05	73.14	73.23	
5		1.04	111.15	111.26	111.37	121.49	122.01	132.11	132.27	132.43	132.53	143.07	163.23	123.39	123.55	124.11	124.27	124.43	124.59	125.15	125.31	125.47	125.63	125.79	125.95	
6		1.39	181.57	182.15	182.33	182.51	193.10	233.32	233.56	234.19	234.42	235.05	235.68	236.31	236.94	237.57	238.20	238.83	239.46	240.09	240.72	241.35	241.98	242.61	243.24	
NE	6.00	31.26	31.36	31.47	31.57	32.08	32.19	32.30	32.41	32.52	33.03	33.14	33.25	33.36	33.47	33.58	34.09	34.20	34.31	34.42	34.53	34.64	34.75	34.86	34.97	



M	N. Sine.	N. Co-Sine.	N. Tangent.	N. Co-Tang.	N. Secant.	N. Co-Secant.	M
0	1045285	9245215	1051042	95143645	10055682	95667722	60
1	1048175	9244914	1053935	94578149	10055930	95403686	59
2	1051070	9244619	1056924	94014116	10055699	95141110	58
3	1053963	9244333	1059965	93451531	10056009	94879984	57
4	1056856	9244052	1062858	92893934	10056320	94620296	56
5	1059743	9243765	1065750	92330663	10056631	94362033	55
6	1062641	9243479	1068692	91772355	10056943	94105184	54
7	1065533	9243199	1071634	91215459	10057256	93849738	53
8	1068425	9242919	1074576	90659936	10057570	93595652	52
9	1071313	9242643	1077519	90105002	10057885	93343006	51
10	1074210	9242365	1080462	89553035	10058201	93091699	50
11	1077102	9242083	1083405	89001627	10058518	92841749	49
12	1079994	9241805	1086348	88450159	10058835	92592145	48
13	1082885	9241524	1089291	87900835	10059153	92345777	47
14	1085777	9241243	1092234	87353436	10059472	92099934	46
15	1088669	9240963	1095178	86808113	10059792	91855305	45
16	1091560	9240683	1098122	86264564	10060113	91611980	44
17	1094452	9240403	1101065	85721074	10060435	91359949	43
18	1097343	9240123	1104008	85178667	10060758	91112920	42
19	1100234	9239843	1106951	84636333	10061081	90869725	41
20	1103126	9239563	1109894	84094964	10061405	90626112	40
21	1106017	9239283	1112837	83553568	10061730	90414533	39
22	1108908	9239003	1115780	83012198	10062056	90213837	38
23	1111799	9238723	1118723	82470826	10062383	89944354	37
24	1114689	9238443	1121666	81929458	10062711	89711095	36
25	1117580	9238163	1124609	81388094	10063040	89479051	35
26	1120471	9237883	1127552	80846726	10063370	89248211	34
27	1123361	9237603	1130495	80305358	10063701	89018567	33
28	1126252	9237323	1133438	79763994	10064032	88790109	32
29	1129142	9237043	1136381	79222626	10064364	88562628	31
30	1132033	9236763	1139324	78681258	10064697	88336715	30
	N. Co-Sine.	N. Sine.	N. Co-Tang.	N. Tangent.	N. Co-Secant.	N. Secant.	M

	2	d.	4	6	d.	8	d.	10		d.	12	d.	14	d.	16	d.	18	d.	20	d.	22	d.	23
S N	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	N S	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0
1	0.07	1.00	1.00	1.00	1.00	1.00	1.00	1.00	1	0.00	1.00	1.00	1.00	1.00	1.00	1.00	1.00	1.00	1.00	1.00	1.00	1.00	1.00
2	0.16	3.01	3.01	3.01	3.01	3.01	3.01	3.01	2	0.00	3.00	3.00	3.00	3.00	3.00	3.00	3.00	3.00	3.00	3.00	3.00	3.00	3.00
3	0.26	5.01	5.01	5.01	5.01	5.01	5.01	5.01	3	0.00	5.00	5.00	5.00	5.00	5.00	5.00	5.00	5.00	5.00	5.00	5.00	5.00	5.00
4	0.38	7.01	7.01	7.01	7.01	7.01	7.01	7.01	4	0.00	7.00	7.00	7.00	7.00	7.00	7.00	7.00	7.00	7.00	7.00	7.00	7.00	7.00
5	0.52	9.01	9.01	9.01	9.01	9.01	9.01	9.01	5	0.01	12.01	12.01	12.01	12.01	12.01	12.01	12.01	12.01	12.01	12.01	12.01	12.01	12.01
6	1.29	15.11	15.11	15.11	15.11	15.11	15.11	15.11	6	0.02	18.02	18.02	18.02	18.02	18.02	18.02	18.02	18.02	18.02	18.02	18.02	18.02	18.02
7	2.38	30.20	30.20	30.20	30.20	30.20	30.20	30.20	7	0.03	21.03	21.03	21.03	21.03	21.03	21.03	21.03	21.03	21.03	21.03	21.03	21.03	21.03
NE	5.22	46.43	46.43	46.43	46.43	46.43	46.43	46.43															

M	L. Sine.	L. Co-Sine.	L. Tangent.	L. Co-Tang.	L. Secant.	L. Co-Secant.	M
0	9.0192346	9.9976143	9.0216202	10.9783798	10.0023857	10.9807654	60
1	9.0204348	9.9976011	9.0228338	10.9771662	10.0023959	10.9795652	59
2	9.0216318	9.9975877	9.0240441	10.9759559	10.0024123	10.9783682	58
3	9.0228254	9.9975743	9.0252510	10.9747490	10.0024257	10.9771746	57
4	9.0240157	9.9975609	9.0264548	10.9735452	10.0024391	10.9759843	56
5	9.0252027	9.9975475	9.0276552	10.9723448	10.0024525	10.9747973	55
6	9.0263865	9.9975340	9.0288524	10.9711476	10.0024660	10.9736135	54
7	9.0275669	9.9975205	9.0300464	10.9699536	10.0024795	10.9724331	53
8	9.0287442	9.9975069	9.0312373	10.9687627	10.0024931	10.9712558	52
9	9.0299182	9.9974933	9.0324249	10.9675751	10.0025067	10.9700818	51
10	9.0310890	9.9974797	9.0336093	10.9663907	10.0025203	10.9689110	50
11	9.0322567	9.9974660	9.0347906	10.9652094	10.0025340	10.9677433	49
12	9.0334212	9.9974523	9.0359688	10.9640312	10.0025477	10.9665778	48
13	9.0345825	9.9974386	9.0371439	10.9628561	10.0025614	10.9654175	47
14	9.0357407	9.9974248	9.0383159	10.9616841	10.0025752	10.9642592	46
15	9.0368958	9.9974110	9.0394843	10.9605152	10.0025890	10.9631043	45
16	9.0380477	9.9973971	9.0406506	10.9593494	10.0026029	10.9619523	44
17	9.0391966	9.9973833	9.0418134	10.9581866	10.0026167	10.9608034	43
18	9.0403424	9.9973693	9.0429731	10.9570269	10.0026307	10.9596576	42
19	9.0414852	9.9973554	9.0441299	10.9558701	10.0026446	10.9585148	41
20	9.0426249	9.9973414	9.0452836	10.9547164	10.0026586	10.9573751	40
21	9.0437617	9.9973273	9.0464343	10.9535657	10.0026727	10.9562383	39
22	9.0448954	9.9973132	9.0475821	10.9524179	10.0026868	10.9551046	38
23	9.0460261	9.9972991	9.0487273	10.9512730	10.0027009	10.9539739	37
24	9.0471538	9.9972850	9.0498699	10.9501311	10.0027150	10.9528462	36
25	9.0482796	9.9972708	9.0510098	10.9489922	10.0027292	10.9517214	35
26	9.0494005	9.9972566	9.0521439	10.9478561	10.0027434	10.9505995	34
27	9.0505194	9.9972423	9.0532771	10.9467229	10.0027577	10.9494806	33
28	9.0516354	9.9972280	9.0544104	10.9455926	10.0027720	10.9483646	32
29	9.0527485	9.9972137	9.0555439	10.9444651	10.0027863	10.9472515	31
30	9.0538588	9.9971993	9.0566595	10.9433405	10.0028007	10.9461412	30
	L. Co-Sine.	L. Sine.	L. Co-Tang.	L. Tangent.	L. Co-Secant.	L. Secant.	M

	2	d.	4	6	d.	8	d.	10	d.	12	d.	14	d.	16	d.	18	d.	20	d.	22	d.	23
S N	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	S N	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0
1	0.07	1.01	1.01	1.01	1.01	1.01	1.01	1.01	1	0.00	1.01	1.01	1.01	1.01	1.01	1.01	1.01	1.01	1.01	1.01	1.01	1.01
2	0.26	3.02	3.02	3.02	3.02	3.02	3.02	3.02	2	0.00	3.02	3.02	3.02	3.02	3.02	3.02	3.02	3.02	3.02	3.02	3.02	3.02
3	0.38	5.02	5.02	5.02	5.02	5.02	5.02	5.02	3	0.00	5.02	5.02	5.02	5.02	5.02	5.02	5.02	5.02	5.02	5.02	5.02	5.02
4	0.52	7.02	7.02	7.02	7.02	7.02	7.02	7.02	4	0.01	12.02	12.02	12.02	12.02	12.02	12.02	12.02	12.02	12.02	12.02	12.02	12.02
5	1.29	15.12	15.12	15.12	15.12	15.12	15.12	15.12	5	0.02	18.02	18.02	18.02	18.02	18.02	18.02	18.02	18.02	18.02	18.02	18.02	18.02
6	2.38	30.21	30.21	30.21	30.21	30.21	30.21	30.21	6	0.03	21.03	21.03	21.03	21.03	21.03	21.03	21.03	21.03	21.03	21.03	21.03	21.03
NE	5.22	46.44	46.44	46.44	46.44	46.44	46.44	46.44														



## A TABLE of Natural and

## 6 DEGREES.

M	N. Sine.	N. Co-Sine.	N. Tangent.	N. Co-Tang.	N. Secant.	N. Co-Secant.	M
30	1132032	9935718	1139356	87768874	10064697	88336715	30
31	1134922	9935388	1142303	87542461	10065031	88111761	29
32	1137812	9935058	1145250	87317198	10065366	87887957	28
33	1140702	9934727	1148197	87093077	10065702	87665295	27
34	1143592	9934395	1151144	86870088	10066039	87443766	26
35	1146482	9934062	1154091	86648223	10066377	87223361	25
36	1149371	9933728	1157039	86427475	10066715	87004071	24
37	1152261	9933393	1159987	86207833	10067054	86785889	23
38	1155151	9933057	1162935	85989290	10067394	86568805	22
39	1158040	9932720	1165883	85771838	10067735	86352812	21
40	1160929	9932383	1168831	85555468	10068077	86137901	20
41	1163818	9932045	1171780	85340172	10068420	85924065	19
42	1166707	9931706	1174729	85125943	10068764	85711295	18
43	1169596	9931366	1177678	84912772	10069108	85499584	17
44	1172485	9931025	1180628	84700651	10069453	85288923	16
45	1175374	9930684	1183578	84489573	10069799	85079304	15
46	1178263	9930342	1186528	84279531	10070146	84870721	14
47	1181151	9929999	1189478	84070515	10070494	84663165	13
48	1184040	9929655	1192428	83862519	10070843	84456629	12
49	1186928	9929310	1195378	83655536	10071193	84251105	11
50	1189816	9928964	1198328	83449557	10071544	84046586	10
51	1192704	9928617	1201279	83244577	10071896	83843065	9
52	1195593	9928270	1204230	83040586	10072248	83640534	8
53	1198481	9927922	1207181	82837579	10072601	83438986	7
54	1201368	9927575	1210132	82635547	10072955	83238415	6
55	1204256	9927223	1213084	82434485	10073310	83038812	5
56	1207144	9926872	1216036	82234384	10073666	82840171	4
57	1210031	9926521	1218988	82035239	10074023	82642435	3
58	1212919	9926169	1221940	81837041	10074381	82445748	2
59	1215806	9925816	1224893	81639786	10074740	82249952	1
60	1218693	9925462	1227846	81443464	10075099	82055090	0
N. Co-Sine.	N. Sine.	N. Co-Tang.	N. Tangent.	N. Co-Secant.	N. Secant.	M	

## 83 DEGREES.

## Latitude 13 Deg. 00 Min. North Declination.

	2	d.	4	d.	6	d.	8	d.	10	d.	12		d.	14	d.	16	d.	18	d.	20	d.	22	d.	23	
	b. m.	b. m.	b. m.	b. m.	b. m.	b. m.	b. m.	b. m.	b. m.	b. m.	b. m.		b. m.	b. m.	b. m.	b. m.	b. m.	b. m.	b. m.	b. m.	b. m.	b. m.	b. m.	b. m.	
N 12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0		12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	
1 00.8	1 00.7	1 00.6	1 00.5	1 00.4	1 00.3	1 00.2	1 00.1	1 00.0	1 00.0	1 00.0	1 00.0	1	00.1	1 00.2	1 00.3	1 00.4	1 00.5	1 00.6	1 00.7	1 00.8	1 00.9	1 01.0	1 01.1	1 01.2	
2 01.7	2 01.6	2 01.5	2 01.4	2 01.3	2 01.2	2 01.1	2 01.0	2 00.9	2 00.8	2 00.7	2 00.6	2	00.2	2 00.4	2 00.6	2 00.8	2 01.0	2 01.2	2 01.4	2 01.6	2 01.8	2 02.0	2 02.2	2 02.4	
3 02.9	3 02.8	3 02.7	3 02.6	3 02.5	3 02.4	3 02.3	3 02.2	3 02.1	3 02.0	3 01.9	3 01.8	3	00.5	3 00.9	3 01.3	3 01.7	3 02.1	3 02.5	3 02.9	3 03.3	3 03.7	3 04.1	3 04.5	3 04.9	
4 04.2	4 04.1	4 04.0	4 03.9	4 03.8	4 03.7	4 03.6	4 03.5	4 03.4	4 03.3	4 03.2	4 03.1	4	00.9	4 01.3	4 01.7	4 02.1	4 02.5	4 02.9	4 03.3	4 03.7	4 04.1	4 04.5	4 04.9	4 05.3	
5 05.3	5 05.2	5 05.1	5 05.0	5 04.9	5 04.8	5 04.7	5 04.6	5 04.5	5 04.4	5 04.3	5 04.2	5	01.3	5 01.7	5 02.1	5 02.5	5 02.9	5 03.3	5 03.7	5 04.1	5 04.5	5 04.9	5 05.3	5 05.7	
6 06.4	6 06.3	6 06.2	6 06.1	6 06.0	6 05.9	6 05.8	6 05.7	6 05.6	6 05.5	6 05.4	6 05.3	6	01.7	6 02.1	6 02.5	6 02.9	6 03.3	6 03.7	6 04.1	6 04.5	6 04.9	6 05.3	6 05.7	6 06.1	
7 07.5	7 07.4	7 07.3	7 07.2	7 07.1	7 07.0	7 06.9	7 06.8	7 06.7	7 06.6	7 06.5	7 06.4	7	02.1	7 02.5	7 02.9	7 03.3	7 03.7	7 04.1	7 04.5	7 04.9	7 05.3	7 05.7	7 06.1	7 06.5	
NE 5.21	5.21	5.21	5.21	5.21	5.21	5.21	5.21	5.21	5.21	5.21	5.21		0.35	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	

## Artificial Sines, Tangents, and Secants.

## 6 DEGREES.

M	L. Sine.	L. Co-Sine.	L. Tangent.	L. Co-Tang.	L. Secant.	L. Co-Secant.	M
30	9.0538888	9.9971993	9.0566595	10.9433405	10.0028007	10.9461412	30
31	9.0549651	9.9971849	9.0577813	10.9422187	10.0028151	10.9450339	29
32	9.0560706	9.9971704	9.0589002	10.9410998	10.0028296	10.9439294	28
33	9.0571723	9.9971559	9.0600164	10.9399836	10.0028441	10.9428377	27
34	9.0582711	9.9971414	9.0611297	10.9388703	10.0028586	10.9417289	26
35	9.0593672	9.9971268	9.0622403	10.9377597	10.0028732	10.9406328	25
36	9.0604604	9.9971122	9.0633482	10.9366518	10.0028878	10.9395496	24
37	9.0615509	9.9970976	9.0644533	10.9355467	10.0029024	10.9384491	23
38	9.0626386	9.9970829	9.0655566	10.9344444	10.0029171	10.9373614	22
39	9.0637235	9.9970682	9.0666593	10.9333447	10.0029318	10.9362765	21
40	9.0648057	9.9970535	9.0677522	10.9322478	10.0029465	10.9351943	20
41	9.0658852	9.9970387	9.0688455	10.9311535	10.0029613	10.9341148	19
42	9.0669619	9.9970239	9.0699381	10.9300619	10.0029761	10.9330381	18
43	9.0680360	9.9970090	9.0710270	10.9289730	10.0029910	10.9319640	17
44	9.0691074	9.9969941	9.0721133	10.9278867	10.0030059	10.9308926	16
45	9.0701761	9.9969792	9.0731969	10.9268031	10.0030209	10.9298239	15
46	9.0712421	9.9969642	9.0742779	10.9257221	10.0030358	10.9287579	14
47	9.0723055	9.9969492	9.0753563	10.9246437	10.0030508	10.9276945	13
48	9.0733663	9.9969343	9.0764321	10.9235679	10.0030658	10.9266337	12
49	9.0744244	9.9969191	9.0775053	10.9224947	10.0030809	10.9255756	11
50	9.0754799	9.9969040	9.0785760	10.9214240	10.0030960	10.9245201	10
51	9.0765329	9.9968888	9.0796441	10.9203559	10.0031112	10.9234671	9
52	9.0775832	9.9968736	9.0807096	10.9192904	10.0031264	10.9224168	8
53	9.0786310	9.9968584	9.0817726	10.9182274	10.0031416	10.9213690	7
54	9.0796762	9.9968431	9.0828331	10.9171669	10.0031569	10.9203238	6
55	9.0807189	9.9968278	9.0838911	10.9161089	10.0031722	10.9192811	5
56	9.0817590	9.9968125	9.0849466	10.9150534	10.0031875	10.9182410	4
57	9.0827966	9.9967971	9.0859996	10.9140004	10.0032029	10.9172034	3
58	9.0838317	9.9967817	9.0870501	10.9129499	10.0032183	10.9161683	2
59	9.0848643	9.9967662	9.0880981	10.9119019	10.0032338	10.9151357	1
60	9.0858945	9.9967507	9.0891438	10.9108562	10.0032493	10.9141055	0
L. Co-Sine.	L. Sine.	L. Tangent.	L. Co-Tang.	L. Tangent.	L. Secant.	L. Co-Secant.	M

## 83 DEGREES.

## Latitude 13 Deg. 00 Min. South Declination.

2-column, 18-column																										
	0	d. 2	d. 4	d. 6	d. 8	d. 10	d. 12	d. 14	d. 16	d. 18	d. 20	d. 22	d. 23													
	b. m.	b. m.	b. m.	b. m.	b. m.	b. m.	b. m.	b. m.	b. m.	b. m.	b. m.	b. m.	b. m.	b. m.	b. m.	b. m.	b. m.	b. m.	b. m.	b. m.	b. m.	b. m.	b. m.	b. m.	b. m.	b. m.
S 12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0
1 01.0	1 01.1	1 01.2	1 01.3	1 01.4	1 01.5	1 01.6	1 01.7	1 01.8	1 01.9	1 02.0	1 02.1	1 02.2	1 02.3	1 02.4	1 02.5	1 02.6	1 02.7	1 02.8	1 02.9	1 03.0	1 03.1	1 03.2	1 03.3	1 03.4	1 03.5	1 03.6
2 02.1	2 02.2	2 02.3	2 02.4	2 02.5	2 02.6	2 02.7	2 02.8	2 02.9	2 03.0	2 03.1	2 03.2	2 03.3	2 03.4	2 03.5	2 03.6	2 03.7	2 03.8	2 03.9	2 04.0	2 04.1	2 04.2	2 04.3	2 04.4	2 04.5	2 04.6	2 04.7
3 03.2	3 03.3	3 03.4	3 03.5	3 03.6	3 03.7	3 03.8	3 03.9	3 04.0	3 04.1	3 04.2	3 04.3	3 04.4	3 04.5	3 04.6	3 04.7	3 04.8	3 04.9	3 05.0	3 05.1	3 05.2	3 05.3	3 05.4	3 05.5	3 05.6	3 05.7	3 05.8
4 04.3	4 04.4	4 04.5	4 04.6	4 04.7	4 04.8	4 04.9	4 05.0	4 05.1	4 05.2	4 05.3	4 05.4	4 05.5	4 05.6	4 05.7	4 05.8	4 05.9	4 06.0	4 06.1	4 06.2	4 06.3	4 06.4	4 06.5	4 06.6	4 06.7	4 06.8	4 06.9
5 05.4	5 05.5	5 05.6	5 05.7	5 05.8	5 05.9	5 06.0	5 06.1	5 06.2	5 06.3	5 06.4	5 06.5	5 06.6	5 06.7	5 06.8	5 06.9	5 07.0	5 07.1	5 07.2	5 07.3	5 07.4	5 07.5	5 07.6	5 07.7	5 07.8	5 07.9	5 08.0
6 06.5	6 06.6	6 06.7	6 06.8	6 06.9	6 07.0	6 07.1	6 07.2	6 07.3	6 07.4	6 07.5	6 07.6	6 07.7	6 07.8	6 07.9	6 08.0	6 08.1	6 08.2	6 08.3	6 08.4	6 08.5	6 08.6	6 08.7	6 08.8	6 08.9	6 09.0	6 09.1
7 07.6	7 07.7	7 07.8	7 07.9	7 08.0	7 08.1	7 08.2	7 08.3	7 08.4	7 08.5	7 08.6	7 08.7	7 08.8	7 08.9	7 09.0	7 09.1	7 09.2	7 09.3	7 09.4	7 09.5	7 09.6	7 09.7	7 09.8	7 09.9	7 10.0	7 10.1	7 10.2
NE 6.00	6.00	6.00	6.00	6.00	6.00	6.00	6.00	6.00	6.00	6.00	6.00	6.00	6.00	6.00	6.00	6.00	6.00	6.00	6.00	6.00	6.00	6.00	6.00	6.00	6.00	6.00



## A TABLE of Natural and

7 DEGREES.

M	N. Sine.	N. Co-Sine.	N. Tangent.	N. Co-Tang.	N. Secant.	N. Co-Secant.
0	12218693	9925462	1227846	81443464	10075092	82055090
1	1221581	9925107	1230799	81248071	10075459	81861157
2	1224468	9924751	1233752	81053599	10075820	81668145
3	1227355	9924394	1236705	80860042	10076182	81475608
4	1230241	9924036	1239658	80667394	10076545	81284560
5	1233128	9923678	1242612	80475647	10076903	81094573
6	1236015	9923319	1245565	80284796	10077274	80905152
7	1238901	9922959	1248520	80094535	10077639	80716681
8	1241788	9922598	1251474	79903765	10078005	80529062
9	1244674	9922236	1254429	79712555	10078372	80342321
10	1247560	9921874	1257384	79521322	10078740	80156450
11	1250446	9921511	1260339	79330222	10079109	79971445
12	1253332	9921147	1263294	79139151	10079479	79782298
13	1256218	9920782	1266249	78948395	10079850	79604003
14	1259104	9920416	1269205	78757948	10080222	79421556
15	1261990	9920051	1272161	78568043	10080595	79239950
16	1264876	9919686	1275117	78378191	10080969	79059179
17	1267761	9919321	1278073	78188340	10081343	78879238
18	1270646	9918956	1281029	78002212	10081718	78700120
19	1273531	9918591	1283986	77822453	10082094	78521821
20	1276416	9918226	1286943	77642700	10082471	78344335
21	1279301	9917861	1289900	77462947	10082849	78167656
22	1282186	9917496	1292857	77283194	10083228	77991778
23	1285071	9917131	1295814	77103441	10083607	77816697
24	1287956	9916766	1298771	76923688	10083988	77642406
25	1290841	9916401	1301731	76743935	10084370	77468901
26	1293726	9916036	1304689	76564182	10084752	77296166
27	1296611	9915671	1307648	76384429	10085135	77124227
28	1299496	9915306	1310607	76204676	10085519	76953047
29	1302381	9914941	1313566	76024923	10085904	76782531
30	1305266	9914576	1316525	75845170	10086290	76612976
	N. Co-Sine.	N. Sine.	N. Co-Tang.	N. Tangent.	N. Co-Secant.	N. Secant.

82 DEGREES.

Latitude 14 Deg. 00 Min. North Declination.												
	2 d.	4 d.	6 d.	8 d.	10 d.	12 d.		14 d.	16 d.	18 d.	20 d.	22 d.
SIN	b. m.	b. m.	b. m.	b. m.	b. m.	b. m.	N S	b. m.	b. m.	b. m.	b. m.	b. m.
1	12.0	12.0	12.0	12.0	12.0	12.0	1	12.0	12.0	12.0	12.0	12.0
2	0.59	1.00	1.00	1.00	1.00	1.00	2	0.59	1.00	1.00	1.00	1.00
3	0.19	0.10	0.13	0.13	0.13	0.13	3	0.19	0.10	0.13	0.13	0.13
4	0.31	0.26	0.21	0.21	0.21	0.21	4	0.31	0.26	0.21	0.21	0.21
5	0.46	0.39	0.32	0.32	0.32	0.32	5	0.46	0.39	0.32	0.32	0.32
6	1.08	1.11	1.05	1.05	1.05	1.05	6	1.08	1.11	1.05	1.05	1.05
7	1.44	1.16	1.12	1.12	1.12	1.12	7	1.44	1.16	1.12	1.12	1.12
8	2.56	2.26	2.30	2.30	2.30	2.30	8	2.56	2.26	2.30	2.30	2.30
9	5.25	3.64	4.49	4.49	4.49	4.49	9	5.25	3.64	4.49	4.49	4.49

## Artificial Sines, Tangents, and Secants.

7 DEGREES.

M	L. Sine.	L. Co-Sine.	L. Tangent.	L. Co-Tang.	L. Secant.	L. Co-Secant.
0	9.0858945	9.9967507	9.0891438	10.9108562	10.0032493	10.9141055
1	9.0869221	9.9967352	9.0901869	10.9098131	10.0032648	10.9137779
2	9.0879473	9.9967196	9.0912277	10.9087723	10.0032804	10.9134527
3	9.0889700	9.9967040	9.0922660	10.9077340	10.0032960	10.9131300
4	9.0899903	9.9966884	9.0933020	10.9066980	10.0033116	10.9128077
5	9.0910082	9.9966727	9.0943355	10.9056645	10.0033273	10.9124855
6	9.0920237	9.9966570	9.0953669	10.9046333	10.0033430	10.9121633
7	9.0930367	9.9966412	9.0963955	10.9036045	10.0033588	10.9118411
8	9.0940474	9.9966254	9.0974219	10.9025781	10.0033746	10.9115189
9	9.0950566	9.9966096	9.0984460	10.9015540	10.0033904	10.9111967
10	9.0960645	9.9965937	9.0994678	10.9005322	10.0034063	10.9108745
11	9.0970715	9.9965778	9.1004872	10.8995128	10.0034222	10.9105523
12	9.0980766	9.9965619	9.1015044	10.8984956	10.0034381	10.9102301
13	9.0990805	9.9965459	9.1025192	10.8974808	10.0034541	10.9099079
14	9.1000838	9.9965299	9.1035317	10.8964683	10.0034701	10.9095857
15	9.1010858	9.9965139	9.1045420	10.8954580	10.0034862	10.9092635
16	9.1020877	9.9964979	9.1055500	10.8944500	10.0035023	10.9089413
17	9.1030893	9.9964816	9.1065557	10.8934443	10.0035184	10.9086191
18	9.1040906	9.9964655	9.1075591	10.8924409	10.0035345	10.9082969
19	9.1050916	9.9964493	9.1085604	10.8914395	10.0035507	10.9079747
20	9.1060924	9.9964330	9.1095594	10.8904400	10.0035670	10.9076525
21	9.1070929	9.9964167	9.1105562	10.8894435	10.0035833	10.9073303
22	9.1080932	9.9964004	9.1115508	10.8884492	10.0035996	10.9070081
23	9.1090932	9.9963841	9.1125431	10.8874569	10.0036159	10.9066859
24	9.1100929	9.9963677	9.1135333	10.8864667	10.0036323	10.9063637
25	9.1110926	9.9963513	9.1145213	10.8854787	10.0036487	10.9060415
26	9.1120920	9.9963348	9.1155072	10.8844928	10.0036652	10.9057193
27	9.1130911	9.9963183	9.1164909	10.8835091	10.0036817	10.9053971
28	9.1140900	9.9963018	9.1174724	10.8825276	10.0036982	10.9050749
29	9.1150887	9.9962853	9.1184518	10.8815482	10.0037148	10.9047527
30	9.1160872	9.9962688	9.1194291	10.8805709	10.0037314	10.9044305
	L. Co-Sine.	L. Sine.	L. Co-Tang.	L. Tangent.	L. Co-Secant.	L. Secant.

82 DEGREES.

Latitude 14 Deg. 00 Min. South Declination.												
	2 d.	4 d.	6 d.	8 d.	10 d.	12 d.		14 d.	16 d.	18 d.	20 d.	22 d.
SIN	b. m.	b. m.	b. m.	b. m.	b. m.	b. m.	N S	b. m.	b. m.	b. m.	b. m.	b. m.
1	0.11	0.12	0.13	0.13	0.13	0.13	1	0.11	0.12	0.13	0.13	0.13
2	0.23	0.26	0.28	0.28	0.28	0.28	2	0.23	0.26	0.28	0.28	0.28
3	0.37	0.42	0.47	0.47	0.47	0.47	3	0.37	0.42	0.47	0.47	0.47
4	0.54	0.61	0.69	0.69	0.69	0.69	4	0.54	0.61	0.69	0.69	0.69
5	1.12	1.11	1.11	1.12	1.12	1.12	5	1.12	1.11	1.11	1.12	1.12
6	2.01	1.61	1.13	1.13	1.13	1.13	6	2.01	1.61	1.13	1.13	1.13
7	3.22	2.63	2.08	2.08	2.08	2.08	7	3.22	2.63	2.08	2.08	2.08



M	N. Sine.	N. Co-Sine.	V. Tangent.	V. Co-Tang.	N. Secant.	N.Co-Secant.	
30	1305262	9214449	1316525	75957541	10086290	76612976	30
31	1308146	9214069	1319484	75787179	10086677	76444075	29
32	1311030	9913688	1322444	75617567	10087065	76275923	28
33	1313913	9913306	1325404	75448699	10087453	76108516	27
34	1316797	9912923	1328364	75280571	10087842	75941849	26
35	1319681	9912539	1331324	75113178	10088232	75775916	25
36	1322564	9912155	1334285	74940514	10088623	75610713	24
37	1325447	9911770	1337246	74765057	10089015	75446236	23
38	1328330	9911384	1340207	74615357	10089408	75282478	22
39	1331213	9911097	1343168	74465855	10089802	75119437	21
40	1334096	9910699	1346129	74316704	10090197	74957106	20
41	1336979	9910221	1349091	74167397	10090592	74797842	19
42	1339862	9909832	1352053	739961595	10090988	74634560	18
43	1342744	9909442	1355015	73799909	10091385	744747335	17
44	1345627	9909051	1357977	73638916	10091783	74314803	16
45	1348509	9908659	1360940	73478610	10092182	74155959	15
46	1351392	9908266	1363903	73318989	10092582	73997798	14
47	1354274	9907872	1366866	73160047	10092983	73834018	13
48	1357156	9907478	1369829	73001780	10093385	73683512	12
49	1360038	9907083	1372793	72844184	10093788	73527377	11
50	1362919	9906687	1375757	72686725	10094192	73371909	10
51	1365801	9906290	1378721	72530987	10094596	73217102	9
52	1368683	9905892	1381685	72375378	10095001	73062954	8
53	1371564	9905493	1384650	72220422	10095407	72909460	7
54	1374446	9905094	1387615	72066116	10095814	72756616	6
55	1377327	9904694	1390580	71912456	10096222	72604417	5
56	1380208	9904293	1393545	71759437	10096631	72452839	4
57	1383089	9903893	1396510	71607056	10097041	72301940	3
58	1385970	9903493	1399476	71455308	10097452	72151653	2
59	1388850	9903094	1402442	71304190	10097864	72001996	1
60	1391731	9902690	1405408	71152697	10098276	71852965	0
N. Co-Sine.		N. Sine.	N. Co-Tang.		N. Tangent.	N. Co-Secant.	N. Secant.

82 DEGREES.

[illegible]

7 DEGREES

M	<i>L. Sinc.</i>	<i>L. Co-Sinc.</i>	<i>L. Tangent.</i>	<i>L. Co-Tang.</i>	<i>L. Secant.</i>	<i>L. Co-Secant.</i>	
30	9.1156977	9.9962686	9.1194291	10.8805709	10.0037314	10.8843023	29
31	9.1166562	9.9962686	9.1204404	10.8799597	10.0037481	10.8833438	30
32	9.1176125	9.9962352	9.1213773	10.8786627	10.0037648	10.8823873	28
33	9.1185667	9.9962185	9.1223482	10.8776518	10.0037815	10.8814335	27
34	9.1195188	9.9962017	9.1233171	10.8766829	10.0037983	10.8804812	26
35	9.1204688	9.9961849	9.1242879	10.8757161	10.0038151	10.8795312	25
36	9.1214167	9.9961681	9.1252486	10.8747454	10.0038319	10.8785833	24
37	9.1223624	9.9961512	9.1262121	10.8737888	10.0038488	10.8776376	23
38	9.1233061	9.9961343	9.1271718	10.8728282	10.0038657	10.8766939	22
39	9.1242477	9.9961174	9.1281303	10.8718697	10.0038826	10.8757523	21
40	9.1251872	9.9961004	9.1290868	10.8709132	10.0038996	10.8748128	20
41	9.1261246	9.9960834	9.1300413	10.8699587	10.0039166	10.8738754	19
42	9.1270600	9.9960663	9.1309937	10.8690063	10.0039337	10.8729490	18
43	9.1279934	9.9960492	9.1319442	10.8680558	10.0039508	10.8720266	17
44	9.1289247	9.9960321	9.1328926	10.8671074	10.0039679	10.8710753	16
45	9.1298539	9.9960149	9.1338391	10.8661609	10.0039851	10.8701461	15
46	9.1307812	9.9959977	9.1347835	10.8652165	10.0040023	10.8692188	14
47	9.1317064	9.9959804	9.1357260	10.8642746	10.0040196	10.8682936	13
48	9.1326297	9.9959631	9.1366665	10.8633335	10.0040369	10.8673793	12
49	9.1335509	9.9959458	9.1376051	10.8623949	10.0040542	10.8664644	11
50	9.1344702	9.9959284	9.1385417	10.8614583	10.0040716	10.8655529	10
51	9.1353875	9.9959111	9.1394704	10.8605235	10.0040889	10.8646412	9
52	9.1363028	9.9958936	9.1404092	10.8595908	10.0041064	10.8637292	8
53	9.1372161	9.9958761	9.1413430	10.8586600	10.0041239	10.8628139	7
54	9.1381275	9.9958586	9.1422689	10.8577311	10.0041414	10.8618975	6
55	9.1390370	9.9958413	9.1431959	10.8568041	10.0041589	10.8609830	5
56	9.1399445	9.9958235	9.1441210	10.8558790	10.0041765	10.8600655	4
57	9.1408501	9.9958059	9.1450442	10.8549558	10.0041941	10.8591499	3
58	9.1417537	9.9957882	9.1459655	10.8540345	10.0042118	10.8582363	2
59	9.1426555	9.9957705	9.1468850	10.8531150	10.0042295	10.8573145	1
60	9.1435553	9.9957528	9.1478025	10.8521975	10.0042472	10.8563947	0
	<i>L. Co-Sinc.</i>	<i>L. Sinc.</i>	<i>L. Co-Tang.</i>	<i>L. Tangent.</i>	<i>L. Co-Secant.</i>	<i>L. Secant.</i>	M

82 D E G R E E S.

[illegible]



## A TABLE of Natural and

8 DEGREES.

M	N. Sine.	N. Co-Sine.	N. Tangent.	N. Co-Tang.	N. Secant.	N. Co-Secant.
0	1391731	9902680	1405408	71153697	10098276	71852965
1	1394612	9902275	1408374	71003826	10098689	71704556
2	1397492	9901869	1411341	70854573	10099103	71556764
3	1400372	9901462	1414308	70705934	10099518	71409593
4	1403252	9901054	1417275	70557905	10099934	71263019
5	1406132	9900646	1420243	70410482	10100351	71117058
6	1409012	9900238	1423211	70263662	10100769	70971700
7	1411892	9899830	1426179	70117441	10101188	70826941
8	1414772	9899415	1429147	69971806	10101607	70682777
9	1417651	9899003	1432115	69826981	10102027	70539205
10	1420531	9898590	1435084	69682375	10102448	70395620
11	1423410	9898176	1438053	69538333	10102870	70253820
12	1426289	9897762	1441022	69395192	10103293	70112601
13	1429168	9897347	1443991	69252489	10103717	69970760
14	1432047	9896931	1446961	69110559	10104142	69830092
15	1434926	9896514	1449931	68968799	10104568	69689994
16	1437805	9896096	1452901	68827807	10104995	69550464
17	1440684	9895677	1455871	68687378	10105423	69411466
18	1443562	9895257	1458842	68547508	10105851	69273089
19	1446440	9894837	1461813	68408196	10106280	69135239
20	1449319	9894416	1464784	68269437	10106710	68997942
21	1452197	9893994	1467755	68131227	10107141	68861195
22	1455075	9893571	1470727	67993565	10107573	68724995
23	1457953	9893147	1473699	67856446	10108006	68589338
24	1460830	9892723	1476671	67719867	10108440	68454222
25	1463708	9892298	1479644	67583526	10108875	68319642
26	1466585	9891872	1482617	67448319	10109311	68185597
27	1469463	9891445	1485590	67313341	10109747	68052082
28	1472340	9891017	1488563	67178581	10110184	67919095
29	1475217	9890588	1491536	67044966	10110622	67786631
30	1478094	9890158	1494510	66911562	10111061	67654691
	V. Co-Sine.	N. Sine.	N. Co-Tang.	N. Tangent.	N. Co-Secant.	N. Secant.

8 DEGREES.

Latitude 16 Deg. 00 Min. North Declination.

	2	d.	4	d.	6	d.	8	d.	10	d.	12	d.	14	d.	16		d.	18	d.	20	d.	22	d.	23
S N	12	0	1	2	3	4	5	6	7	8	9	10	11	12	13		14	15	16	17	18	19	20	21
1	0.11	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0		12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0
2	0.22	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0		12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0
3	0.36	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0		12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0
4	0.53	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0		12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0
5	1.15	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0		12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0
6	1.57	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0		12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0
7	3.11	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0		12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0
NE	5.29	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0		12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0

## Artificial Sines, Tangents, and Secants.

8 DEGREES.

M	L. Sine.	L. Co-Sine.	L. Tangent.	L. Co-Tang.	L. Secant.	L. Co-Secant.
0	9.1435553	9.9957528	9.1437025	10.8521975	10.0042472	10.8564447
1	9.1444532	9.9957350	9.1487182	10.8512818	10.0042650	10.8555468
2	9.1453493	9.9957172	9.1496321	10.8503679	10.0042828	10.8546507
3	9.1462435	9.9956993	9.1505441	10.8494559	10.0043007	10.8537565
4	9.1471358	9.9956815	9.1514543	10.8485457	10.0043185	10.8528642
5	9.1480262	9.9956635	9.1523627	10.8476373	10.0043365	10.8519738
6	9.1489148	9.9956456	9.1532692	10.8467308	10.0043544	10.8510852
7	9.1498015	9.9956276	9.1541739	10.8458261	10.0043724	10.8501985
8	9.1506864	9.9956095	9.1550780	10.8449231	10.0043905	10.8493136
9	9.1515694	9.9955915	9.1559780	10.8440220	10.0044085	10.8484306
10	9.1524507	9.9955734	9.1568773	10.8431227	10.0044266	10.8475493
11	9.1533301	9.9955552	9.1577748	10.8422252	10.0044448	10.8466699
12	9.1542076	9.9955370	9.1586706	10.8413294	10.0044630	10.8457924
13	9.1550834	9.9955188	9.1595646	10.8404354	10.0044812	10.8449166
14	9.1559574	9.9955005	9.1604569	10.8395431	10.0044995	10.8440426
15	9.1568296	9.9954822	9.1613473	10.8386527	10.0045178	10.8431704
16	9.1577000	9.9954639	9.1622361	10.8377639	10.0045361	10.8423000
17	9.1585686	9.9954455	9.1631231	10.8368769	10.0045545	10.8414314
18	9.1594334	9.9954272	9.1640083	10.8359917	10.0045729	10.8405646
19	9.1603005	9.9954087	9.1648919	10.8351081	10.0045913	10.8396995
20	9.1611639	9.9953902	9.1657737	10.8342263	10.0046098	10.8388361
21	9.1620254	9.9953717	9.1666538	10.8333462	10.0046283	10.8379745
22	9.1628853	9.9953531	9.1675322	10.8324678	10.0046469	10.8371147
23	9.1637434	9.9953345	9.1684089	10.8315911	10.0046655	10.8362566
24	9.1645998	9.9953159	9.1692839	10.8307161	10.0046841	10.8354002
25	9.1654544	9.9952972	9.1701572	10.8298428	10.0047028	10.8345466
26	9.1663074	9.9952785	9.1710289	10.8289711	10.0047215	10.8336926
27	9.1671586	9.9952597	9.1718989	10.8281011	10.0047403	10.8328414
28	9.1680081	9.9952409	9.1727672	10.8272328	10.0047591	10.8319919
29	9.1688559	9.9952221	9.1736338	10.8263662	10.0047779	10.8311441
30	9.1697021	9.9952033	9.1744988	10.8255012	10.0047967	10.8302979
	L. Co-Sine.	L. Sine.	L. Co-Tang.	L. Tangent.	L. Co-Secant.	L. Secant.

8 DEGREES.

Latitude 16 Deg. 00 Min. South Declination.

	2	d.	4	d.	6	d.	8	d.	10	d.	12	d.	14	d.	16		d.	18	d.	20	d.	22	d.	23
S N	12	0	1	2	3	4	5	6	7	8	9	10	11	12	13		14	15	16	17	18	19	20	21
1	0.13	10.14	10.15	10.16	10.17	10.18	10.19	10.20	10.21	10.22	10.23	10.24	10.25	10.26	10.27		10.28	10.29	10.30	10.31	10.32	10.33	10.34	10.35
2	0.26	10.14	10.15	10.16	10.17	10.18	10.19	10.20	10.21	10.22	10.23	10.24	10.25	10.26	10.27		10.28	10.29	10.30	10.31	10.32	10.33	10.34	10.35
3	0.42	10.14	10.15	10.16	10.17	10.18	10.19	10.20	10.21	10.22	10.23	10.24	10.25	10.26	10.27		10.28	10.29	10.30	10.31	10.32	10.33	10.34	10.35
4	1.02	10.14	10.15	10.16	10.17	10.18	10.19	10.20	10.21	10.22	10.23	10.24	10.25	10.26	10.27		10.28	10.29	10.30	10.31	10.32	10.33	10.34	10.35
5	1.30	10.14	10.15	10.16	10.17	10.18	10.19	10.20	10.21	10.22	10.23	10.24	10.25	10.26	10.27		10.28	10.29	10.30	10.31	10.32	10.33	10.34	10.35
6	2.15	12.30	12.31	12.32	12.33	12.34	12.35	12.36	12.37	12.38	12.39	12.40	12.41	12.42	12.43		12.44	12.45	12.46	12.47	12.48	12.49	12.50	12.51
7	3.37	12.30	12.31	12.32	12.33	12.34	12.35	12.36	12.37	12.38	12.39	12.40	12.41	12.42	12.43		12.44	12.45	12.46	12.47	12.48	12.49	12.50	12.51
WE	6.00	12.30	12.31	12.32	12.33	12.34	12.35	12.36	12.37	12.38	12.39	12.40	12.41	12.42	12.43		12.44	12.45	12.46	12.47	12.48	12.49	12.50	12.51



## 8 DEGREES.

M	N. Sine.	N. Co-Sine.	N. Tangent.	N. Co-Tang.	N. Secant.	N. Co-Secant.	M
30	1473694	9590158	1494810	66911562	10111061	67654691	30
31	1480971	9582728	1497184	66773677	10111501	67523268	29
32	1488343	9575297	1500455	66645377	10111942	67392360	28
33	1495724	9567865	1503733	66514449	10112384	67261965	27
34	1503105	9560432	1507010	66383100	10112827	67132079	26
35	1510487	9552995	1510287	66252255	10113271	67002699	25
36	1517868	9545563	1513564	66121919	10113715	66873822	24
37	1525250	9538132	1516841	65992086	10114160	66745446	23
38	1532632	9530702	1520118	65862739	10114606	66617568	22
39	1540014	9523271	1523395	65733992	10115053	66490184	21
40	1547396	9515841	1526672	65605355	10115501	66363293	20
41	1554778	9508410	1529949	65476762	10115950	66236990	19
42	1562160	9500979	1533226	65348293	10116400	66110973	18
43	1569542	9493548	1536503	65223396	10116851	65985540	17
44	1576924	9486117	1539780	65099981	10117303	65860587	16
45	1584306	9478686	1543057	64977043	10117756	65736112	15
46	1591688	9471255	1546334	64854581	10118209	65612113	14
47	1599070	9463824	1549611	64732951	10118663	65488585	13
48	1606452	9456393	1552888	64612322	10119118	65365528	12
49	1613834	9448962	1556165	64492017	10119574	65242938	11
50	1621216	9441531	1559442	64372428	10120031	65120812	10
51	1628598	9434100	1562719	64253001	10120489	64999148	9
52	1635980	9426669	1565996	64133573	10120948	64877944	8
53	1643362	9419238	1569273	64014146	10121408	64757195	7
54	1650744	9411807	1572550	63894719	10121869	64636921	6
55	1658126	9404376	1575827	63775292	10122331	64517559	5
56	1665508	9396945	1579104	63655865	10122793	64397666	4
57	1672890	9389514	1582381	63536438	10123256	64278119	3
58	1680272	9382083	1585658	63417011	10123720	64160216	2
59	1687654	9374652	1588935	63297584	10124185	64042154	1
60	1695036	9367221	1592212	63178157	10124651	63924532	0
N. Co-Sine.		N. Sine.	N. Co-Tang.	N. Tangent.	N. Co-Secant.	N. Secant.	M

81 DEGREES.

## 8 DEGREES.

M	L. Sine.	L. Co-Sine.	L. Tangent.	L. Co-Tang.	L. Secant.	L. Co-Secant.	M
30	9-1697221	9-9952033	9-1744988	10-8255012	10-0247567	10-8322979	30
31	9-1705465	9-9951844	9-1753222	10-8216378	10-0245156	10-8324534	29
32	9-1713893	9-9951654	9-1762239	10-8217761	10-0243346	10-8326167	28
33	9-1722353	9-9951464	9-1771840	10-8229160	10-0241536	10-8327795	27
34	9-1730893	9-9951274	9-1781993	10-8240575	10-0239726	10-8329421	26
35	9-1739577	9-9951084	9-1792893	10-8252007	10-0237916	10-8331047	25
36	9-1748439	9-9950893	9-1804646	10-8263454	10-0236107	10-8332673	24
37	9-1757384	9-9950702	9-1816552	10-8274918	10-0234299	10-8334300	23
38	9-1766412	9-9950510	9-1828622	10-8286398	10-0232491	10-8335927	22
39	9-1775425	9-9950318	9-1840866	10-8297894	10-0230683	10-8337554	21
40	9-1784521	9-9950125	9-1853285	10-8309405	10-0228875	10-8339181	20
41	9-1793693	9-9949933	9-1865878	10-8320932	10-0227067	10-8340808	19
42	9-1797265	9-9949740	9-1878645	10-8332475	10-0225259	10-8342435	18
43	9-1805512	9-9949548	9-1891595	10-8344034	10-0223451	10-8344062	17
44	9-1813744	9-9949355	9-1904732	10-8355608	10-0221643	10-8345689	16
45	9-1821960	9-9949163	9-1918052	10-8367198	10-0219835	10-8347316	15
46	9-1830165	9-9948970	9-1931564	10-8378804	10-0218027	10-8348943	14
47	9-1838354	9-9948778	9-1945267	10-8390425	10-0216219	10-8350570	13
48	9-1846512	9-9948585	9-1959172	10-8402061	10-0214411	10-8352197	12
49	9-1854655	9-9948393	9-1973287	10-8413713	10-0212603	10-8353824	11
50	9-1862802	9-9948200	9-1987613	10-8425381	10-0210795	10-8355451	10
51	9-1870923	9-9948008	9-1992139	10-8437061	10-0208987	10-8357078	9
52	9-1879029	9-9947815	9-1996865	10-8448764	10-0207179	10-8358705	8
53	9-1887120	9-9947623	9-1997591	10-8460491	10-0205371	10-8360332	7
54	9-1895195	9-9947430	9-1998317	10-8472231	10-0203563	10-8361959	6
55	9-1903254	9-9947238	9-1999043	10-8483984	10-0201755	10-8363586	5
56	9-1911299	9-9947045	9-1999769	10-8495751	10-0200000	10-8365213	4
57	9-1919328	9-9946853	9-1999495	10-8507531	10-0198245	10-8366840	3
58	9-1927344	9-9946660	9-1999221	10-8519324	10-0196490	10-8368467	2
59	9-1935341	9-9946468	9-1998947	10-8531131	10-0194735	10-8370094	1
60	9-1943324	9-9946275	9-1998673	10-8542942	10-0192980	10-8371721	0
L. Co-Sine.		L. Sine.	L. Co-Tang.	L. Tangent.	L. Co-Secant.	L. Secant.	M

81 DEGREES.

## Latitude 1° Deg. 00 Min. North Declination.

	2	d.	4	d.	6	d.	8	d.	10	d.	12	d.	14	d.	16		d.	18	d.	20	d.	22	d.	23
	b.	m.	b.	m.	b.	m.	b.	m.	b.	m.	b.	m.	b.	m.	b.		b.	m.	b.	m.	b.	m.	b.	m.
S N	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	N S	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0
1	0.11	10.10	1.00	9.09	1.00	8.08	2.00	6.05	1.00	5.04	1.00	4.03	2.00	2.00	2.00	1	0.00	2.00	2.00	2.00	2.00	2.00	2.00	2.00
2	0.24	20.21	3.01	19.18	3.01	15.05	3.01	12.01	3.00	9.00	3.00	6.00	4.00	4.00	4.00	2	0.01	4.00	4.00	4.00	4.00	4.00	4.00	4.00
3	0.39	30.36	5.02	29.29	5.02	24.09	4.01	15.00	5.01	10.00	5.01	8.00	6.00	6.00	6.00	3	0.01	7.00	7.00	7.00	7.00	7.00	7.00	7.00
4	0.55	40.51	7.04	39.43	8.03	26.08	7.02	17.01	7.01	12.00	8.00	6.00	6.00	6.00	6.00	4	0.04	9.00	9.00	9.00	9.00	9.00	9.00	9.00
5	1.12	51.11	1.14	11.13	11.13	11.02	11.04	11.03	10.01	10.01	10.01	10.01	10.01	10.01	10.01	5	0.05	14.00	14.00	14.00	14.00	14.00	14.00	14.00
6	2.05	15.10	15.15	1.35	16.19	16.15	1.03	15.04	16.00	16.00	16.00	16.00	16.00	16.00	16.00	6	0.08	25.00	25.00	25.00	25.00	25.00	25.00	25.00
7	3.20	22.58	23.25	2.35	23.12	23.14	2.25	1.49	25.14	25.14	25.14	25.14	25.14	25.14	25.14	7	0.15	21.00	21.00	21.00	21.00	21.00	21.00	21.00
NE	5.31	28.50	28.45	4.35	28.47	28.38	3.29	36.20	36.20	36.20	36.20	36.20	36.20	36.20	36.20									
								5.58	25	5.33	26	5.07												

## Latitude 1° Deg. 00 Min. South Declination.

	0	d.	2	d.	4	d.	6	d.	8	d.	10	d.	12	d.	14	d.	16	d.	18	d.	20	d.	22	d.	23
	b. m.	a	b. m.	a	b. m.	a	b. m.	a	b. m.	a	b. m.	a	b. m.	a	b. m.	a	b. m.	a	b. m.	a	b. m.	a	b. m.	a	b. m.
S N	12.0		12.0		12.0		12.0		12.0		12.0		12.0		12.0		12.0		12.0		12.0		12.0		12.0
1	0.13		10.14		1.0.15		2.0.17		2.0.19		2.0.21		1.0.22		1.0.23		2.0.25		2.0.27		2.0.29		2.0.31		2.0.33
2	0.28		30.31		3.0.34		3.0.37		3.0.40		3.0.43		3.0.46		3.0.49		4.0.53		4.0.57		4.1.01		3.1.04		3.1.07
3	0.44		50.49		5.0.54		6.0.59		5.1.04		5.1.09		5.1.14		5.1.19		6.1.25		6.1.31		6.1.37		6.1.43		4.1.48
4	1.05		7.1.12		7.1.19		7.1.26		8.1.24		8.1.42		9.1.50		9.1.58		8.2.05		8.2.13		9.2.23		9.2.32		7.2.39
5	1.35		10.1.45		10.1.55		11.2.06		11.2.17		11.2.28		12.2.40		12.2.52		12.3.04		12.3.16		13.3.29		13.3.42		12.3.55
6	2.21		15.2.36		15.2.51		16.3.07		16.3.23		16.3.39		19.3.53		19.4.17		19.4.35		19.4.55		19.5.14		25.5.35		
7	3.45		22.4.05		23.4.25		23.4.51		23.5.14		23.5.37														
NE	5.30		28.4.00																						



M	N. Sine.	N. Co-Sine.	N. Tangent.	N. Co-Tang.	N. Secant.	N. Co-Secant.	
0	1564345	9876883	1583844	63137515	10124651	63924532	60
1	1567218	9876428	1586826	631018866	10125118	63807347	59
2	1570091	9875972	1589808	629000551	10125586	63690595	58
3	1572964	9875515	1592791	627828368	10126055	63574276	57
4	1575836	9875057	1595774	626655514	10126525	63458386	56
5	1578708	9874599	1598757	625483885	10126996	63342923	55
6	1581581	9874138	1601740	624312056	10127467	63227584	54
7	1584453	9873677	1604724	623160097	10127939	63113269	53
8	1587325	9873216	1607708	622003347	10128412	62999073	52
9	1590197	9872754	1610692	620851006	10128886	62885295	51
10	1593069	9872291	1613677	619702799	10129361	62771933	50
11	1595940	9871827	1616662	618558667	10129837	62658984	49
12	1598812	9871362	1619647	617418665	10130314	62546446	48
13	1601683	9870897	1622632	61628272	10130792	62434316	47
14	1603555	9870431	1625617	61515085	10131271	62322594	46
15	1607426	9869964	1628603	61402305	10131751	62211275	45
16	1610297	9869496	1631589	61289923	10132231	62100359	44
17	1613167	9869027	1634576	61177943	10132712	61989843	43
18	1616038	9868557	1637563	61066560	10133194	61879725	42
19	1618909	9868086	1640550	60955174	10133677	61770003	41
20	1621779	9867615	1643537	60844381	10134161	61660674	40
21	1624650	9867143	1646525	60733979	10134646	61551736	39
22	1627520	9866670	1649513	60623967	10135132	61443189	38
23	1630390	9866199	1652501	60514343	10135619	61335028	37
24	1633260	9865721	1655489	60405103	10136107	61227255	36
25	1636129	9865246	1658478	60296247	10136595	61119861	35
26	1638999	9864770	1661467	60187772	10137084	61012850	34
27	1641868	9864293	1664456	60079676	10137574	60906219	33
28	1644738	9863815	1667445	59971957	10138065	60799964	32
29	1647607	9863336	1670433	59864614	10138557	60694085	31
30	1650476	9862856	1673422	59757654	10139050	60588580	30
	N. Co-Sine.	N. Sine.	N. Co-Tang.	N. Tangent.	N. Co-Secant.	N. Secant.	

## 80 DEGREES.

Latitude 18 Deg. 00 Min. North Declination.																										
	2	d.	4	d.	6	d.	8	d.	10	d.	12	d.	14	d.	16	d.	18			d.	20	d.	22	d.	23	
	b. m.	m.	b. m.	m.	b. m.	m.	b. m.	m.	b. m.	m.	b. m.	m.	b. m.	m.	b. m.	m.	b. m.			b. m.	m.	b. m.	m.	b. m.	m.	
<i>S. N.</i>	12.0		12.0		12.0		12.0		12.0		12.0		12.0		12.0		12.0	<i>N</i>		12.0		12.0		12.0		
<i>1</i>	0.12		1.0.11		1.0.10		2.0.53		2.0.66		1.0.55		1.0.34		2.00.2		2.00.0	<i>1</i>		0.0.2		1.00.3		2.00.5		
<i>2</i>	0.25		3.0.22		3.0.19		3.0.16		3.0.13		3.0.10		3.0.07		3.00.4		3.00.1	<i>2</i>		0.0.4		3.00.7		3.0.10		
<i>3</i>	0.41		5.0.36		5.0.31		5.0.26		5.0.21		5.0.16		5.0.11		5.00.6		5.00.1	<i>3</i>		0.0.6		6.0.12		4.0.16		
<i>4</i>	1.01		7.0.54		7.0.47		7.0.40		8.0.32		7.0.25		7.0.18		8.0.10		8.00.2	<i>4</i>		0.0.9		8.0.17		7.0.24		
<i>5</i>	1.23		10.1.18		1.0.8		10.0.58		11.0.47		10.36		11.0.25		11.0.14		12.0.2	<i>5</i>		1.0.13		14.0.27		11.0.38		
<i>6</i>	2.10		14.1.56		1.41		15.1.26		15.1.11		15.05		17.0.38		17.0.21		17.00.4	<i>6</i>		0.21		24.0.45		21.1.06		
<i>WE</i>	3.06		21.3.05		2.44		22.2.22		22.2.00		23.1		32.28		1.04.28		0.36.28	<i>7</i>		0.53						
<i>1</i>	5.32		25.5.07		4.41		26.4.15		26.3.49		44		3.05		44.2.21		44.1.37		0.52							
													43		5.53		43		5.10		43		4.27			

9 DEGREES.							
M	<i>L. Sine.</i>	<i>L. Co-Sine.</i>	<i>L. Tangent.</i>	<i>L. Co-Tang.</i>	<i>L. Secant.</i>	<i>L. Co-Secant.</i>	
0	9.1943324	9.9946199	9.1997125	10.8002875	10.0053801	10.8056676	60
1	9.1951293	9.9945999	9.2005294	10.7994706	10.0054001	10.8048707	59
2	9.1959247	9.9945798	9.2013489	10.7986551	10.0054202	10.8040753	58
3	9.1967186	9.9945597	9.2021548	10.7978411	10.0054403	10.8032814	57
4	9.1975110	9.9945396	9.2029714	10.7970286	10.0054604	10.8024889	56
5	9.1983019	9.9945194	9.2037825	10.7962175	10.0054805	10.8016981	55
6	9.1990913	9.9944992	9.2045922	10.7954078	10.0055008	10.8009087	54
7	9.1998793	9.9944789	9.2054004	10.7945996	10.0055211	10.8001207	53
8	9.2006658	9.9944587	9.2062072	10.7937928	10.0055413	10.7993342	52
9	9.2014509	9.9944385	9.2070126	10.7929874	10.0055617	10.7985491	51
10	9.2022345	9.9944180	9.2078165	10.7921835	10.0055820	10.7977655	50
11	9.2030167	9.9943975	9.2086191	10.7913809	10.0056025	10.7969833	49
12	9.2037974	9.9943771	9.2094203	10.7905797	10.0056229	10.7962026	48
13	9.2045766	9.9943566	9.2102200	10.7897800	10.0056434	10.7954234	47
14	9.2053545	9.9943361	9.2110184	10.7889816	10.0056639	10.7946455	46
15	9.2061309	9.9943156	9.2118153	10.7881847	10.0056844	10.7938691	45
16	9.2069059	9.9942950	9.2126109	10.7873891	10.0057050	10.7930941	44
17	9.2076795	9.9942743	9.2134051	10.7865936	10.0057257	10.7923205	43
18	9.2084516	9.9942537	9.2141980	10.7858020	10.0057463	10.7915484	42
19	9.2092224	9.9942330	9.2149894	10.7850106	10.0057670	10.7907776	41
20	9.2099917	9.9942122	9.2157795	10.7842185	10.0057878	10.7900083	40
21	9.2107597	9.9941914	9.2165683	10.7834317	10.0058086	10.7892403	39
22	9.2115263	9.9941706	9.2173556	10.7826444	10.0058294	10.7884737	38
23	9.2122914	9.9941498	9.2181417	10.7818573	10.0058502	10.7877086	37
24	9.2130552	9.9941289	9.2189264	10.7810736	10.0058711	10.7869448	36
25	9.2138176	9.9941079	9.2197097	10.7802903	10.0058921	10.7861824	35
26	9.2145787	9.9940870	9.2204917	10.7795083	10.0059130	10.7854213	34
27	9.2153384	9.9940659	9.2212724	10.7787276	10.0059341	10.7846616	33
28	9.2160967	9.9940449	9.2220518	10.7779452	10.0059551	10.7839032	32
29	9.2168536	9.9940238	9.2228298	10.7771702	10.0059762	10.7831464	31
30	9.2176092	9.9940027	9.2236065	10.7763925	10.0059973	10.7823908	30
	<i>L. Co-Sine</i>	<i>L. Sine</i>	<i>L. Co-Tangent</i>	<i>L. Tangent</i>	<i>L. Co-Secant</i>	<i>L. Secant</i>	

## 80 DEGREES.

[illegible]



## A TABLE of Natural and

## 9 DEGREES.

M	N. Sine.	N. Co-Sine.	N. Tangent.	N. Co-Tang.	N. Secant.	N. Co-Secant.
30	1660476	9868316	1671429	59757644	10139050	60588580
31	1663345	9862375	1674416	59851045	10139544	60483445
32	1666214	9856434	1677407	59944815	10140039	60378310
33	1669082	9850493	1680398	59938591	10140535	60273175
34	1671951	9844552	1683389	59932365	10141032	60168040
35	1674819	9838611	1686381	59926140	10141530	60062905
36	1677687	9832670	1689372	59919915	10142029	59957770
37	1680556	9826729	1692363	59913690	10142529	59852635
38	1683424	9820788	1695354	59907465	10143029	59747500
39	1686293	9814847	1698345	59901240	10143530	59642365
40	1689161	9808906	1701336	59895015	10144032	59537230
41	1692030	9802965	1704327	59888790	10144535	59432095
42	1694898	9797024	1707318	59882565	10145039	59326960
43	1697767	9791083	1710309	59876340	10145544	59221825
44	1700635	9785142	1713299	59870115	10146050	59116690
45	1703504	9779201	1716290	59863890	10146557	59011555
46	1706372	9773260	1719281	59857665	10147064	58906420
47	1709241	9767319	1722272	59851440	10147572	58801285
48	1712109	9761378	1725263	59845215	10148081	58696150
49	1714978	9755437	1728254	59838990	10148591	58591015
50	1717846	9749496	1731245	59832765	10149102	58485880
51	1720715	9743555	1734236	59826540	10149614	58380745
52	1723583	9737614	1737227	59820315	10150127	58275610
53	1726452	9731673	1740218	59814090	10150641	58170475
54	1729320	9725732	1743209	59807865	10151156	58065340
55	1732189	9719791	1746199	59801640	10151672	57960205
56	1735057	9713850	1749190	59795415	10152189	57855070
57	1737926	9707909	1752181	59789190	10152707	57749935
58	1740794	9701968	1755172	59782965	10153225	57644800
59	1743663	9696027	1758163	59776740	10153745	57539665
60	1746531	9690086	1761154	59770515	10154267	57434530

## 80 DEGREES.

## Latitude 19 Deg. 00 Min. North Declination.

	2 d.	4 d.	6 d.	8 d.	10 d.	12 d.	14 d.	16 d.	18 d.		20 d.	22 d.	23 d.
S N	b. m.	b. m.	b. m.	b. m.	b. m.	b. m.	b. m.	b. m.	b. m.	N	b. m.	b. m.	b. m.
1	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	1	12.0	12.0	12.0
2	0.13	0.12	0.11	0.10	0.09	0.08	0.07	0.06	0.05	2	0.04	0.03	0.02
3	0.27	0.24	0.21	0.18	0.15	0.12	0.09	0.06	0.03	3	0.01	0.00	0.00
4	1.04	0.99	0.94	0.89	0.84	0.79	0.74	0.69	0.64	4	0.00	0.00	0.00
5	1.36	1.11	1.05	1.00	0.95	0.90	0.85	0.80	0.75	5	0.00	0.00	0.00
6	2.17	1.82	1.75	1.69	1.64	1.59	1.54	1.49	1.44	6	0.00	0.00	0.00
7	3.31	2.83	2.75	2.69	2.64	2.59	2.54	2.49	2.44	7	0.00	0.00	0.00
NE	5.32	4.59	4.49	4.41	4.34	4.27	4.20	4.13	4.06				

## Artificial Sines, Tangents, and Secants.

## 9 DEGREES.

M	L. Sine.	L. Co-Sine.	L. Tangent.	L. Co-Tang.	L. Secant.	L. Co-Secant.
30	9.2176092	9.9940027	9.2236855	10.7763935	10.0036973	10.7823909
31	9.2183635	9.9939815	9.2243519	10.7763181	10.0036185	10.7816365
32	9.2191164	9.9939603	9.2250183	10.7762427	10.0035397	10.7808836
33	9.2198680	9.9939391	9.2256847	10.7761673	10.0034609	10.7801302
34	9.2206196	9.9939179	9.2263511	10.7760919	10.0033821	10.7793768
35	9.2213711	9.9938966	9.2270175	10.7760165	10.0033033	10.7786234
36	9.2221227	9.9938754	9.2276839	10.7759411	10.0032245	10.7778700
37	9.2228742	9.9938542	9.2283503	10.7758657	10.0031457	10.7771166
38	9.2236258	9.9938330	9.2290167	10.7757903	10.0030669	10.7763632
39	9.2243773	9.9938118	9.2296831	10.7757149	10.0029881	10.7756098
40	9.2251289	9.9937906	9.2303495	10.7756395	10.0029093	10.7748564
41	9.2258804	9.9937694	9.2310159	10.7755641	10.0028305	10.7741030
42	9.2266319	9.9937482	9.2316823	10.7754887	10.0027517	10.7733496
43	9.2273835	9.9937270	9.2323487	10.7754133	10.0026729	10.7725962
44	9.2281350	9.9937058	9.2330151	10.7753379	10.0025941	10.7718428
45	9.2288866	9.9936846	9.2336815	10.7752625	10.0025153	10.7710894
46	9.2296381	9.9936634	9.2343479	10.7751871	10.0024365	10.7703360
47	9.2303897	9.9936422	9.2350143	10.7751117	10.0023577	10.7695826
48	9.2311412	9.9936210	9.2356807	10.7750363	10.0022789	10.7688292
49	9.2318928	9.9936000	9.2363471	10.7749609	10.0021997	10.7680758
50	9.2326443	9.9935788	9.2370135	10.7748855	10.0021209	10.7673224
51	9.2333959	9.9935576	9.2376799	10.7748101	10.0020417	10.7665690
52	9.2341474	9.9935364	9.2383463	10.7747347	10.0019629	10.7658156
53	9.2348990	9.9935152	9.2390127	10.7746593	10.0018837	10.7650622
54	9.2356505	9.9934940	9.2396791	10.7745839	10.0018049	10.7643088
55	9.2364021	9.9934728	9.2403455	10.7745085	10.0017257	10.7635554
56	9.2371536	9.9934516	9.2410119	10.7744331	10.0016469	10.7628020
57	9.2379052	9.9934304	9.2416783	10.7743577	10.0015677	10.7620486
58	9.2386567	9.9934092	9.2423447	10.7742823	10.0014889	10.7612952
59	9.2394083	9.9933880	9.2430111	10.7742069	10.0014097	10.7605418
60	9.2401598	9.9933668	9.2436775	10.7741315	10.0013309	10.7597884

## 80 DEGREES.

## Latitude 19 Deg. 00 Min. South Declination.

	0 d.	2 d.	4 d.	6 d.	8 d.	10 d.	12 d.	14 d.	16 d.	18 d.	20 d.	22 d.	23 d.
S N	b. m.	b. m.	b. m.	b. m.	b. m.	b. m.	b. m.	b. m.	b. m.	b. m.	b. m.	b. m.	b. m.
1	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0
2	0.15	0.14	0.13	0.12	0.11	0.10	0.09	0.08	0.07	0.06	0.05	0.04	0.03
3	0.29	0.27	0.25	0.24	0.22	0.21	0.20	0.19	0.18	0.17	0.16	0.15	0.14
4	1.04	0.99	0.94	0.89	0.84	0.79	0.74	0.69	0.64	0.59	0.54	0.49	0.44
5	1.36	1.11	1.05	1.00	0.95	0.90	0.85	0.80	0.75	0.70	0.65	0.60	0.55
6	2.17	1.82	1.75	1.69	1.64	1.59	1.54	1.49	1.44	1.39	1.34	1.29	1.24
7	3.31	2.83	2.75	2.69	2.64	2.59	2.54	2.49	2.44	2.39	2.34	2.29	2.24
NE	5.32	4.59	4.49	4.41	4.34	4.27	4.20	4.13	4.06				



## A TABLE of Natural and

to DEGREES.

M	N. Sine.	N. Co-Sine.	V. Tangent.	V. Co-Tang.	N. Secant.	N. Co-Secant.
0	1736482	9548077	1763270	56712815	10154267	57587705
1	1739346	9547571	1766269	56616509	10154788	57492861
2	1742211	9547065	1769269	56520513	10155310	57398333
3	1745075	9546558	1772269	56424518	10155833	57304211
4	1747939	9546050	1775269	56328474	10156357	57210223
5	1750803	9545541	1778270	56232421	10156882	57116636
6	1753667	9545031	1781271	56136350	10157408	57023360
7	1756531	9544521	1784272	56040285	10157935	56930393
8	1759395	9544010	1787274	55944211	10158463	56837734
9	1762258	9543498	1790276	55848138	10158992	56745380
10	1765121	9542985	1793278	55752065	10159521	56653331
11	1767984	9542471	1796281	55655992	10160051	56561584
12	1770847	9541956	1799284	55559919	10160582	56470140
13	1773710	9541440	1802285	55463846	10161114	56378695
14	1776573	9540924	1805287	55367773	10161647	56287251
15	1779436	9540407	1808289	55271700	10162181	56195807
16	1782298	9539889	1811292	55175627	10162716	56104364
17	1785160	9539370	1814295	55079554	10163252	56012921
18	1788022	9538850	1817298	54983481	10163789	55921478
19	1790884	9538329	1820301	54887408	10164327	55829934
20	1793746	9537808	1823304	54791335	10164866	55738391
21	1796607	9537286	1826307	54695262	10165406	55646848
22	1799469	9536763	1829310	54600189	10165946	55555305
23	1802330	9536241	1832313	54505116	10166487	55463762
24	1805191	9535714	1835316	54410043	10167029	55372219
25	1808052	9535189	1838319	54314970	10167572	55280676
26	1810913	9534663	1841322	54219897	10168116	55189133
27	1813774	9534136	1844325	54124824	10168661	55097590
28	1816635	9533608	1847328	54029751	10169207	55006047
29	1819496	9533079	1850331	53934678	10169754	54914504
30	1822357	9532549	1853334	53839605	10170302	54822961
V. Co-Sine.		N. Sine.	N. Co-Tang.	N. Tangent.	N. Co-Secant.	N. Secant.

79 DEGREES.

Latitude 20 Deg. 00 Min. North Declination.

	2	d.	4	d.	6	d.	8	d.	10	d.	12	d.	14	d.	16	d.	18	d.	20	d.	22	d.	23	d.
S.N.	b.m.	m.	b.m.	m.	b.m.	m.	b.m.	m.	b.m.	m.	b.m.	m.	b.m.	m.	b.m.	m.	b.m.	m.	b.m.	m.	b.m.	m.	b.m.	m.
1	0.14	1.0.13	1.0.12	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0
2	0.28	2.0.26	3.0.23	3.0.20	3.0.17	3.0.15	3.0.13	3.0.11	3.0.09	3.0.07	3.0.05	3.0.03	3.0.01	3.0.00	3.0.00	3.0.00	3.0.00	3.0.00	3.0.00	3.0.00	3.0.00	3.0.00	3.0.00	3.0.00
3	0.45	5.0.40	5.0.35	6.0.29	6.0.23	6.0.18	6.0.13	6.0.07	6.0.01	6.0.00	6.0.00	6.0.00	6.0.00	6.0.00	6.0.00	6.0.00	6.0.00	6.0.00	6.0.00	6.0.00	6.0.00	6.0.00	6.0.00	6.0.00
4	1.07	6.1.01	7.0.54	7.0.47	7.0.40	7.0.34	7.0.27	7.0.20	7.0.13	7.0.07	7.0.01	7.0.00	7.0.00	7.0.00	7.0.00	7.0.00	7.0.00	7.0.00	7.0.00	7.0.00	7.0.00	7.0.00	7.0.00	7.0.00
5	1.36	9.1.27	9.1.18	10.1.08	10.1.00	10.0.52	10.0.44	10.0.36	10.0.28	10.0.21	10.0.13	10.0.07	10.0.01	10.0.00	10.0.00	10.0.00	10.0.00	10.0.00	10.0.00	10.0.00	10.0.00	10.0.00	10.0.00	10.0.00
6	2.21	13.2.08	14.1.54	14.1.40	14.1.26	14.1.13	14.1.05	14.0.59	14.0.45	14.0.31	14.0.23	14.0.17	14.0.11	14.0.05	14.0.00	14.0.00	14.0.00	14.0.00	14.0.00	14.0.00	14.0.00	14.0.00	14.0.00	14.0.00
7	3.37	19.3.18	19.2.59	19.2.45	19.2.31	19.2.17	19.2.03	19.1.49	19.1.35	19.1.21	19.1.07	19.0.53	19.0.39	19.0.25	19.0.11	19.0.00	19.0.00	19.0.00	19.0.00	19.0.00	19.0.00	19.0.00	19.0.00	19.0.00
8	5.32	23.5.09	23.4.46	23.4.23	23.4.00	23.3.37	23.3.14	23.2.51	23.2.28	23.2.14	23.1.51	23.1.28	23.1.05	23.0.42	23.0.19	23.0.00	23.0.00	23.0.00	23.0.00	23.0.00	23.0.00	23.0.00	23.0.00	23.0.00
9	8.00																							

## Artificial Sines, Tangents, and Secants.

to DEGREES.

M	L. Sine.	L. Co-Sine.	L. Tangent.	L. Co-Tang.	L. Secant.	L. Co-Secant.
0	9.2396702	9.9933515	9.2463188	10.7536812	10.0066485	10.7603298
1	9.2403861	9.9933292	9.2470569	10.7529431	10.0066708	10.7596139
2	9.2411007	9.9933068	9.2477939	10.7522061	10.0066932	10.7588993
3	9.2418141	9.9932845	9.2485297	10.7514703	10.0067155	10.7581859
4	9.2425264	9.9932621	9.2492643	10.7507357	10.0067379	10.7574736
5	9.2432374	9.9932396	9.2499998	10.7500022	10.0067604	10.7567626
6	9.2439472	9.9932171	9.2507301	10.7492699	10.0067829	10.7560525
7	9.2446558	9.9931946	9.2514612	10.7485388	10.0068054	10.7553442
8	9.2453632	9.9931720	9.2521912	10.7478088	10.0068280	10.7546368
9	9.2460696	9.9931494	9.2529200	10.7470800	10.0068505	10.7539305
10	9.2467746	9.9931268	9.2536477	10.7463523	10.0068732	10.7532254
11	9.2474784	9.9931041	9.2543743	10.7456257	10.0068959	10.7525216
12	9.2481811	9.9930814	9.2550997	10.7449003	10.0069186	10.7518189
13	9.2488827	9.9930587	9.2558240	10.7441760	10.0069413	10.7511173
14	9.2495830	9.9930359	9.2565472	10.7434528	10.0069641	10.7504170
15	9.2502822	9.9930131	9.2572709	10.7427308	10.0069869	10.7497178
16	9.2509803	9.9929902	9.2579901	10.7420099	10.0070098	10.7490197
17	9.2516772	9.9929673	9.2587099	10.7412901	10.0070327	10.7483228
18	9.2523729	9.9929444	9.2594285	10.7405715	10.0070556	10.7476271
19	9.2530675	9.9929214	9.2601461	10.7398539	10.0070786	10.7469325
20	9.2537609	9.9928984	9.2608625	10.7391375	10.0071016	10.7462391
21	9.2544532	9.9928753	9.2615779	10.7384221	10.0071247	10.7455468
22	9.2551444	9.9928522	9.2622922	10.7377079	10.0071478	10.7448555
23	9.2558344	9.9928291	9.2630053	10.7369947	10.0071709	10.7441656
24	9.2565233	9.9928059	9.2637173	10.7362827	10.0071941	10.7434767
25	9.2572110	9.9927827	9.2644283	10.7355717	10.0072173	10.7427890
26	9.2578977	9.9927595	9.2651382	10.7348618	10.0072405	10.7421023
27	9.2585832	9.9927362	9.2658470	10.7341530	10.0072638	10.7414168
28	9.2592676	9.9927129	9.2665547	10.7334453	10.0072871	10.7407324
29	9.2599509	9.9926895	9.2672613	10.7327387	10.0073105	10.7400491
30	9.2606330	9.9926661	9.2679669	10.7320331	10.0073333	10.7393670
L. Co-Sine.		L. Sine.	L. Co-Tang.	L. Tangent.	L. Co-Secant.	L. Secant.

79 DEGREES.

Latitude 20 Deg. 00 Min. South Declination.

		Continuation.																								
	0	d.	2	d.	4	d	6	d	8	d	10	d	12	d.	14	d	16	d.	18	d.	20	d.	22	d	23	
	b.m.	m.	b.m.	m.	b.m.	m.	b.m.	m.	b.m.	m.	b.m.	m.	b.m.	m.	b.m.	m.	b.m.	m.	b.m.	m.	b.m.	m.	b.m.	m.	b.m.	m.
S.N	12.0		12.0		12.0		12.0		12.0		12.0		12.0		12.0		12.0		12.0		12.0		12.0		12.0	
1	0.16		1.0.17		1.0.18		1.0.19		2.0.21		2.0.23		1.0.24		1.0.25		2.0.27		2.0.29		2.0.31		2.0.33		1.0.34	
2	0.32		3.0.35		3.0.38		3.0.41		3.0.44		4.0.48		3.0.51		3.0.54		3.0.57		4.1.01		4.1.05		3.1.08		3.1.11	
3	0.51		4.0.55		4.0.59		4.1.03		4.1.07		5.1.12		6.1.18		6.1.24		6.1.30		6.1.36		7.1.43		6.1.49		4.1.53	
4	1.16		7.1.23		7.1.30		7.1.37		7.1.44		7.1.51		8.1.59		8.2.07		8.2.15		8.2.23		8.2.31		9.2.40		7.2.47	
5	1.48		10.1.58		10.2.08		10.2.18		10.2.28		11.2.39		11.2.40		11.2.51		12.3.03		12.3.15		12.3.27		13.3.50		10.4.00	
6	2.38		14.2.52		14.3.06		14.3.20		15.3.35		15.3.53		17.4.07		17.4.24		17.4.41		17.4.58		18.5.16		22.5.38			
7	3.59		19.4.18		20.4.38		20.4.58		20.5.18		23.5.38															
WE	6.00																									



## A TABLE of Natural and

10 DEGREES.

M	N. Sine.	N. Co-Sine.	N. Tangent.	N. Co-Tang.	N. Secant.	N. Co-Secant.	M
30	1822555	9532549	1853390	53955172	10172302	54874043	30
31	1825215	9532018	1856392	53867718	10170851	54788055	29
32	1827985	9531487	1859403	53780538	10171401	54702342	28
33	1830935	9530955	1862418	53693630	10171952	54616901	27
34	1833795	9530422	1865423	53606993	10172504	54531731	26
35	1836654	9529889	1868433	53520626	10173056	54446831	25
36	1839513	9529353	1871449	53434527	10173609	54362199	24
37	1842373	9528817	1874460	53348666	10174163	54277855	23
38	1845232	9528281	1877471	53263131	10174718	54193737	22
39	1848091	9527744	1880483	53177550	10175274	54109903	21
40	1850949	9527206	1883495	53092793	10175831	54026333	20
41	1853808	9526667	1886507	53008501	10176389	53943026	19
42	1856666	9526127	1889520	52923505	10176948	53859979	18
43	1859524	9525587	1892533	52839251	10177508	53777192	17
44	1862382	9525048	1895546	52755455	10178069	53694664	16
45	1865240	9524508	1898559	52671517	10178631	53612393	15
46	1868098	9523961	1901573	52588035	10179194	53530379	14
47	1870956	9523417	1904587	52504809	10179758	53448620	13
48	1873813	9522872	1907602	52421836	10180322	53367114	12
49	1876670	9522327	1910616	52339116	10180887	53285861	11
50	1879527	9521781	1913632	52256647	10181453	53204880	10
51	1882384	9521234	1916648	52174423	10182020	53124109	9
52	1885241	9520686	1919664	52092452	10182588	53043608	8
53	1888098	9520137	1922680	52010738	10183157	52963354	7
54	1890954	9519587	1925696	51929264	10183727	52883347	6
55	1893811	9519036	1928713	51848035	10184298	52803557	5
56	1896667	9518485	1931730	51767951	10184870	52724070	4
57	1899523	9517933	1934748	51688311	10185443	52644798	3
58	1902379	9517380	1937766	51608813	10186017	52566768	2
59	1905234	9516826	1940784	51529557	10186592	52489679	1
60	1908090	9516271	1943803	51450540	10187168	52413431	0
	N. Co-Sine.	N. Sine.	N. Co-Tang.	N. Tangent.	N. Co-Secant.	N. Secant.	M

79 DEGREES.

Latitude 21 Deg. 00 Min. North Declination.																								
	2	d.	4	d.	6	d.	8	d.	10	d.	12	d.	14	d.	16	d.	18	d.	20		d.	22	d.	24
	b.	m.	m.	b.	m.	m.	b.	m.	m.	b.	m.	m.	b.	m.	m.	b.	m.	m.	b.	m.	m.	b.	m.	m.
5	12	12	12	12	12	12	12	12	12	12	12	12	12	12	12	12	12	12	12	N	12	12	12	
1	0.14	1.0.13	1.0.12	1.0.11	1.0.11	1.0.10	1.0.09	1.0.08	1.0.07	1.0.07	1.0.06	1.0.05	1.0.04	1.0.03	1.0.03	1.0.02	1.0.02	1.0.01	1.0.01	1	00.1	00.2	00.2	
2	0.28	2.0.27	2.0.24	2.0.21	2.0.18	2.0.15	2.0.12	2.0.09	2.0.06	2.0.03	2.0.00	2.0.00	2.0.00	2.0.00	2.0.00	2.0.00	2.0.00	2.0.00	2.0.00	2	00.2	00.4	00.4	
3	0.44	3.0.44	3.0.39	3.0.34	3.0.29	3.0.24	3.0.19	3.0.14	3.0.09	3.0.04	3.0.00	3.0.00	3.0.00	3.0.00	3.0.00	3.0.00	3.0.00	3.0.00	3.0.00	3	00.3	00.7	00.7	
4	1.00	4.0.14	4.0.07	4.0.00	3.59.53	3.59.46	3.59.39	3.59.32	3.59.25	3.59.18	3.59.11	3.59.04	3.59.00	3.59.00	3.59.00	3.59.00	3.59.00	3.59.00	3.59.00	4	00.4	01.1	01.1	
5	1.16	5.0.13	5.0.05	5.0.00	5.0.00	4.59.53	4.59.46	4.59.39	4.59.32	4.59.25	4.59.18	4.59.11	4.59.04	4.59.00	4.59.00	4.59.00	4.59.00	4.59.00	4.59.00	5	00.6	01.7	01.7	
6	1.32	6.0.12	6.0.03	6.0.00	6.0.00	6.0.00	5.59.53	5.59.46	5.59.39	5.59.32	5.59.25	5.59.18	5.59.11	5.59.04	5.59.00	5.59.00	5.59.00	5.59.00	5.59.00	6	0.11	0.40	0.40	
7	1.48	7.0.11	7.0.01	7.0.00	7.0.00	7.0.00	7.0.00	6.59.53	6.59.46	6.59.39	6.59.32	6.59.25	6.59.18	6.59.11	6.59.04	6.59.00	6.59.00	6.59.00	6.59.00	7	0.24			
8	2.04	8.0.10	8.0.00	8.0.00	8.0.00	8.0.00	8.0.00	8.0.00	7.59.53	7.59.46	7.59.39	7.59.32	7.59.25	7.59.18	7.59.11	7.59.04	7.59.00	7.59.00	7.59.00					
9	2.20	9.0.09	9.0.00	9.0.00	9.0.00	9.0.00	9.0.00	9.0.00	9.0.00	8.59.53	8.59.46	8.59.39	8.59.32	8.59.25	8.59.18	8.59.11	8.59.04	8.59.00	8.59.00					
10	2.36	10.0.08	10.0.00	10.0.00	10.0.00	10.0.00	10.0.00	10.0.00	10.0.00	10.0.00	9.59.53	9.59.46	9.59.39	9.59.32	9.59.25	9.59.18	9.59.11	9.59.04	9.59.00					
11	2.52	11.0.07	11.0.00	11.0.00	11.0.00	11.0.00	11.0.00	11.0.00	11.0.00	11.0.00	11.0.00	11.0.00	11.0.00	11.0.00	11.0.00	11.0.00	11.0.00	11.0.00	11.0.00					
12	3.08	12.0.06	12.0.00	12.0.00	12.0.00	12.0.00	12.0.00	12.0.00	12.0.00	12.0.00	12.0.00	12.0.00	12.0.00	12.0.00	12.0.00	12.0.00	12.0.00	12.0.00	12.0.00					
13	3.24	13.0.05	13.0.00	13.0.00	13.0.00	13.0.00	13.0.00	13.0.00	13.0.00	13.0.00	13.0.00	13.0.00	13.0.00	13.0.00	13.0.00	13.0.00	13.0.00	13.0.00	13.0.00					
14	3.40	14.0.04	14.0.00	14.0.00	14.0.00	14.0.00	14.0.00	14.0.00	14.0.00	14.0.00	14.0.00	14.0.00	14.0.00	14.0.00	14.0.00	14.0.00	14.0.00	14.0.00	14.0.00					
15	3.56	15.0.03	15.0.00	15.0.00	15.0.00	15.0.00	15.0.00	15.0.00	15.0.00	15.0.00	15.0.00	15.0.00	15.0.00	15.0.00	15.0.00	15.0.00	15.0.00	15.0.00	15.0.00					
16	4.12	16.0.02	16.0.00	16.0.00	16.0.00	16.0.00	16.0.00	16.0.00	16.0.00	16.0.00	16.0.00	16.0.00	16.0.00	16.0.00	16.0.00	16.0.00	16.0.00	16.0.00	16.0.00					
17	4.28	17.0.01	17.0.00	17.0.00	17.0.00	17.0.00	17.0.00	17.0.00	17.0.00	17.0.00	17.0.00	17.0.00	17.0.00	17.0.00	17.0.00	17.0.00	17.0.00	17.0.00	17.0.00					
18	4.44	18.0.00	18.0.00	18.0.00	18.0.00	18.0.00	18.0.00	18.0.00	18.0.00	18.0.00	18.0.00	18.0.00	18.0.00	18.0.00	18.0.00	18.0.00	18.0.00	18.0.00	18.0.00					
19	5.00	19.0.00	19.0.00	19.0.00	19.0.00	19.0.00	19.0.00	19.0.00	19.0.00	19.0.00	19.0.00	19.0.00	19.0.00	19.0.00	19.0.00	19.0.00	19.0.00	19.0.00	19.0.00					
20	5.16	20.0.00	20.0.00	20.0.00	20.0.00	20.0.00	20.0.00	20.0.00	20.0.00	20.0.00	20.0.00	20.0.00	20.0.00	20.0.00	20.0.00	20.0.00	20.0.00	20.0.00	20.0.00					
21	5.32	21.0.00	21.0.00	21.0.00	21.0.00	21.0.00	21.0.00	21.0.00	21.0.00	21.0.00	21.0.00	21.0.00	21.0.00	21.0.00	21.0.00	21.0.00	21.0.00	21.0.00	21.0.00					
22	5.48	22.0.00	22.0.00	22.0.00	22.0.00	22.0.00	22.0.00	22.0.00	22.0.00	22.0.00	22.0.00	22.0.00	22.0.00	22.0.00	22.0.00	22.0.00	22.0.00	22.0.00	22.0.00					
23	5.64	23.0.00	23.0.00	23.0.00	23.0.00	23.0.00	23.0.00	23.0.00	23.0.00	23.0.00	23.0.00	23.0.00	23.0.00	23.0.00	23.0.00	23.0.00	23.0.00	23.0.00	23.0.00					
24	5.80	24.0.00	24.0.00	24.0.00	24.0.00	24.0.00	24.0.00	24.0.00	24.0.00	24.0.00	24.0.00	24.0.00	24.0.00	24.0.00	24.0.00	24.0.00	24.0.00	24.0.00	24.0.00					
25	5.96	25.0.00	25.0.00	25.0.00	25.0.00	25.0.00	25.0.00	25.0.00	25.0.00	25.0.00	25.0.00	25.0.00	25.0.00	25.0.00	25.0.00	25.0.00	25.0.00	25.0.00	25.0.00					
26	6.12	26.0.00	26.0.00	26.0.00	26.0.00	26.0.00	26.0.00	26.0.00	26.0.00	26.0.00	26.0.00	26.0.00	26.0.00	26.0.00	26.0.00	26.0.00	26.0.00	26.0.00	26.0.00					
27	6.28	27.0.00	27.0.00	27.0.00	27.0.00	27.0.00	27.0.00	27.0.00	27.0.00	27.0.00	27.0.00	27.0.00	27.0.00	27.0.00	27.0.00	27.0.00	27.0.00	27.0.00	27.0.00					
28	6.44	28.0.00	28.0.00	28.0.00	28.0.00	28.0.00	28.0.00	28.0.00	28.0.00	28.0.00	28.0.00	28.0.00	28.0.00	28.0.00	28.0.00	28.0.00	28.0.00	28.0.00	28.0.00					
29	6.60	29.0.00	29.0.00	29.0.00	29.0.00	29.0.00	29.0.00	29.0.00	29.0.00	29.0.00	29.0.00	29.0.00	29.0.00	29.0.00	29.0.00	29.0.00	29.0.00	29.0.00	29.0.00					
30	6.76	30.0.00	30.0.00	30.0.00	30.0.00	30.0.00	30.0.00	30.0.00	30.0.00	30.0.00	30.0.00	30.0.00	30.0.00	30.0.00	30.0.00	30.0.00	30.0.00	30.0.00	30.0.00					

## Artificial Sines, Tangents, and Secants.

10 DEGREES.

M	L. Sine.	L. Co-Sine.	L. Tangent.	L. Co-Tang.	L. Secant.	L. Co-Secant.	
30	9.2666330	9.9926661	9.2670669	10.7323331	10.0073339	10.7393670	30
31	9.2681341	9.9926427	9.2686714	10.7313246	10.0073573	10.7386859	29
32	9.2696354	9.9926192	9.2696749	10.7306231	10.0073808	10.7380059	28
33	9.2686729	9.9925957	9.2700772	10.7299228	10.0074043	10.7373271	27
34	9.2633507	9.9925722	9.2737885	10.7282214	10.0074277	10.7366443	26
35	9.2640274	9.9925487	9.2714747	10.7265212	10.0074514	10.7359729	25
36	9.2647030	9.9925250	9.2721780	10.7278220	10.0074750	10.7352970	24
37	9.2643775	9.9925013	9.2728762	10.7291238	10.0074987	10.7346225	23
38	9.2660905	9.9924776	9.2735753	10.7264261	10.0075224	10.7339461	22
39	9.2667945	9.9924539	9.2742694	10.7257306	10.0075461	10.7332763	21
40	9.2673942	9.9924301	9.2749644	10.7250356	10.0075699	10.7326055	20
41	9.2680047	9.9924063	9.2756584	10.7243416	10.0075937	10.7319353	19
42	9.2686338	9.9923824	9.2763514	10.7236486	10.0076176	10.7312662	18
43	9.2594019	9.9923585	9.2770434	10.7229566	10.0076415	10.7305981	17
44	9.2700589	9.9923346	9.2777343	10.7222657	10.0076654	10.7299311	16
45	9.2707343	9.9923106	9.2784242	10.7215755	10.0076894	10.7292652	15
46	9.2713997	9.9922866	9.2791131	10.7208859	10.0077134	10.7286015	14
47	9.2720635	9.9922626	9.2798039	10.7201991	10.0077374	10.7279361	13
48	9.2727263	9.9922385	9.2804878	10.7195122	10.0077615	10.7272717	12
49	9.2733880	9.9922144	9.2811736	10.7188264	10.0077856	10.7266122	11
50	9.2740487	9.9921902	9.2818585	10.7181411	10.0078098	10.7259513	10
51	9.2747083	9.9921660	9.2825432	10.7174577	10.0078340	10.7252917	9
52	9.2753659	9.9921418	9.2832251	10.7167749	10.0078582	10.7246331	8
53	9.2760225	9.9921175	9.2839070	10.7160930	10.0078825	10.7239755	7
54	9.2766811	9.9920932	9.2845878	10.7154122	10.0079068	10.7233189	6
55	9.2773365	9.9920689	9.2852677	10.7147322	10.0079311	10.7226634	5
56	9.2779911	9.9920445	9.2859466	10.7140534	10.0079555	10.7220099	4
57	9.2786445	9.9920201	9.2866245	10.7133755	10.0079799	10.7213555	3
58	9.2792970	9.9919956	9.2873014	10.7126986	10.0080044	10.7207030	2
59	9.2799484	9.9919711	9.2879773	10.7120227	10.0080289	10.7200516	1
60	9.2705988	9.9919466	9.2886522	10.7113477	10.0080534	10.7194012	0
	L. Co-Sine.	L. Sine.	L. Co-Tang.	L. Tangent.	L. Co-Secant.	L. Secant.	M



A TABLE of Natural and

## II DEGREES.

N. Sine.		N. Co-Sine.		N. Tangent.		N. Co-Tang.		N. Secant.		N. Co-Secant.	
0	1908090	9816271		1943803	51445540			10187168	524083431	60	
1	1910945	9815716		1945822	51365763			10187744	52330121	59	
2	1913800	9815161		1945841	51286224			10188321	52252050	58	
3	1916655	9814603		1952861	51206921			10188890	52174216	57	
4	1919510	9814045		1955881	51127855			10189478	52095618	56	
5	1922365	9813486		1958901	51049024			10190058	52019254	55	
6	1925220	9812926		1961922	50970426			10190639	51942125	54	
7	1928074	9812366		1964943	50892061			10191221	51865228	53	
8	1930928	9811805		1967964	50813928			10191804	51788563	52	
9	1933782	9811243		1970986	50736025			10192388	51712128	51	
10	1936636	9810680		1974008	50658352			10192973	51635924	50	
11	1939490	9810116		1977030	50580907			10193559	51559948	49	
12	1942344	9809551		1980053	50503690			10194146	51484199	48	
13	1945197	9808986		1983076	50426700			10194734	51408677	47	
14	1948050	9808420		1986100	50349935			10195323	51333381	46	
15	1950903	9807853		1989124	50273395			10195912	51258309	45	
16	1953756	9807285		1992148	50197078			10196502	51183461	44	
17	1956609	9806716		1995172	50120984			10197093	51108835	43	
18	1959461	9806146		1998197	50045111			10197685	51034431	42	
19	1962314	9805576		2001222	49969459			10198278	50962248	41	
20	1965166	9805005		2004248	498934027			10198872	50886284	40	
21	1968018	9804433		2007274	49818813			10199467	50812539	39	
22	1970870	9803860		2010300	49743817			10200063	50739012	38	
23	1973722	9803286		2013327	49669037			10200650	50665701	37	
24	1976573	9802711		2016354	49594474			10201238	50592606	36	
25	1979425	9802136		2019381	49520125			10201857	50519726	35	
26	1982276	9801560		2022409	49445990			10202457	50447060	34	
27	1985127	9800983		2025437	49372068			10203058	50374607	33	
28	1987978	9800405		2028465	49298358			10203660	50302367	32	
29	1990829	9799826		2031494	49224859			10204263	50230337	31	
30	1993679	9799247		2034523	49151570			10204867	50158517	30	
N. Co-Sine.		N. Sine.		N. Co-Tang.		N. Tangent.		N. Co-Secant.		N. Secant.	M

## 78 DEGREES.

Latitude 22 Deg. 00 Min. North Declination.

Latitude 22 Deg. 00 Min.															North Declination.										
	2	d.	4	d.	6	d.	8	d.	10	d.	12	d.	14	d.	16	d.	18	d.	20		d.	22	d.	23	
	b.	m.	b.	m.	b.	m.	b.	m.	b.	m.	b.	m.	b.	m.	b.	m.	b.	m.	b.	m.		b.	m.	b.	m.
1	12.0		12.0		12.0		12.0		12.0		12.0		12.0		12.0		12.0		12.0		N				
2	0.15		0.14		0.13		0.11		0.09		0.08		0.07		0.06		0.04		0.02		I	12.0			
3	0.31		0.29		0.26		0.23		0.20		0.17		0.14		0.11		0.08		0.04		2			00.1	
4	0.50		0.46		0.42		0.37		0.32		0.27		0.22		0.17		0.12		0.06		3			00.3	
5	1.14		1.08		1.01		0.94		0.87		0.80		0.72		0.64		0.56		0.08		4			00.4	
6	1.45		1.36		1.27		1.18		1.08		1.01		0.95		0.88		0.81		0.73		5			00.7	
7	2.30		2.18		2.05		1.93		1.80		1.64		1.51		1.38		1.24		1.09		6			01.0	
8	3.46		3.30		3.13		2.96		2.79		2.62		2.45		2.28		2.12		1.95					01.7	
9	5.35		5.16		4.57		4.37		4.17		3.97		3.76		3.55		3.34		3.13						
10													5.34		5.10		4.40		4.21						

## II DEGREES

D E G R E E S.							
M	<i>L. Sine.</i>	<i>L. Co-Sine.</i>	<i>L. Tangent.</i>	<i>L. Co-Tang.</i>	<i>L. Secant.</i>	<i>L. Co-Secant.</i>	
0	0.2805958	0.9919466	0.2886523	10.7113477	10.0080534	10.7194012	60
1	0.2812483	0.9919220	0.2893263	10.7106537	10.0080780	10.7187517	59
2	0.2818967	0.9918974	0.2899993	10.7100007	10.0081026	10.7181033	58
3	0.2825441	0.9918727	0.2906713	10.7093287	10.0081273	10.7174559	57
4	0.2831905	0.9918480	0.2913424	10.7086566	10.0081520	10.7168095	56
5	0.2838359	0.9918233	0.2920125	10.7079874	10.0081767	10.7161641	55
6	0.2844803	0.9917986	0.2926817	10.7073153	10.0082014	10.7155197	54
7	0.2851237	0.9917737	0.2933500	10.7066500	10.0082263	10.7148763	53
8	0.2857661	0.9917489	0.2940172	10.7059828	10.0082511	10.7142339	52
9	0.2864076	0.9917240	0.2946836	10.7053164	10.0082760	10.7135924	51
10	0.2870480	0.9916991	0.2953489	10.7046511	10.0083009	10.7129520	50
11	0.2876875	0.9916741	0.2960134	10.7039866	10.0083259	10.7123125	49
12	0.2883260	0.9916492	0.2966769	10.7033231	10.0083508	10.7116840	48
13	0.2889636	0.9916241	0.2973395	10.7026505	10.0083759	10.7110364	47
14	0.2896001	0.9915990	0.2980011	10.7019898	10.0084010	10.7103999	46
15	0.2902357	0.9915739	0.2986618	10.7013284	10.0084261	10.7097643	45
16	0.2908704	0.9915488	0.2993216	10.7006678	10.0084512	10.7091296	44
17	0.2915040	0.9915236	0.2999804	10.7000096	10.0084764	10.7084960	43
18	0.2921367	0.9914984	0.3006383	10.6993517	10.0085016	10.7078633	42
19	0.2927685	0.9914731	0.3012934	10.6987045	10.0085269	10.7072315	41
20	0.2933993	0.9914478	0.3019514	10.6980564	10.0085522	10.7066007	40
21	0.2940291	0.9914225	0.3026066	10.6974034	10.0085775	10.7059709	39
22	0.2946580	0.9913971	0.3032609	10.6967591	10.0086029	10.7053420	38
23	0.2952859	0.9913717	0.3039143	10.6961085	10.0086283	10.7047141	37
24	0.2959129	0.9913462	0.3045667	10.6954533	10.0086538	10.7040871	36
25	0.2965390	0.9913207	0.3052183	10.6947817	10.0086793	10.7034610	35
26	0.2971641	0.9912952	0.3058689	10.6941117	10.0087048	10.7028359	34
27	0.2977883	0.9912696	0.3065187	10.6934413	10.0087304	10.7022117	33
28	0.2984116	0.9912440	0.3071674	10.6927725	10.0087560	10.7015884	32
29	0.2990339	0.9912184	0.3078155	10.6921045	10.0087816	10.7009661	31
30	0.2996553	0.9911927	0.3084626	10.6914374	10.0088073	10.7003447	30
	<i>L. Co-Sine.</i>	<i>L. Sine.</i>	<i>L. Co-Tang.</i>	<i>L. Tangent.</i>	<i>L. Co-Secant.</i>	<i>L. Secant.</i>	M

## 78 DEGREES.

Latitude 22 Deg. 00 Min. South. Declination.

[illegible]



A TABLE of Natural and

## II DEGREES.

M.	N. Sine.	N. Co-Sine.	N. Tangent.	N. Co-Tang.	N. Secant.	N. Co-Secant.	
30	1993572	9759247	2034521	42151579	10204867	50158517	30
31	1995530	9758557	2037552	4975491	10205471	50086907	29
32	1999580	9758355	2040582	4970562	10206076	50015505	28
33	2002230	9757804	2043512	4892256	10206682	49944311	27
34	2005080	9756921	2046543	4814339	10207289	49873323	26
35	2007930	9756337	2049574	4838245	10207897	49802541	25
36	2010779	9755752	2052725	4761620	10208506	49731964	24
37	2013622	9755167	2055737	46844359	10209116	49661591	23
38	2016475	9754581	2058759	46072719	10209727	49591421	22
39	2019327	9753994	2061901	45301252	10210339	49521453	21
40	2022176	9753406	2065043	44530045	10210952	49451687	20
41	2025024	9752817	2068587	43759010	10211566	49382120	19
42	2027873	9752228	2072130	42988174	10212181	49312754	18
43	2030721	9751638	2075734	42217536	10212797	49243586	17
44	2033569	9751047	2079395	41447596	10213414	49174616	16
45	2036417	9750455	2083023	40678544	10214032	49105844	15
46	2039265	9750062	2086695	40006507	10214650	49037257	14
47	2042113	9750268	2090367	47996957	10215269	48968886	13
48	2044961	9750674	2094069	47807957	10215889	48900700	12
49	2047805	9750079	2097845	47797537	10216510	48832707	11
50	2050650	9750483	2095151	47748567	10217132	48764907	10
51	2053502	9750886	2098218	47659490	10217755	48697299	9
52	2056349	9750288	2101245	47590523	10218379	48629883	8
53	2059195	9750689	2104293	47521907	10219004	48562657	7
54	2062042	9750090	2107331	47453491	10219630	48495621	6
55	2064888	9750490	2110369	47385081	10220257	48428774	5
56	2067734	9750889	2113427	47316594	10220883	48362114	4
57	2070580	9751287	2116446	47249012	10221514	48295643	3
58	2073426	9751684	2119455	47181246	10222144	48229357	2
59	2076271	9752080	2122452	47113686	10222775	48163235	1
60	2079117	9751476	2125455	47046301	10223407	48097343	0
	N. Co-Sine.	N. Sine.	N. Co-Tang.	N. Tangent.	N. Co-Secant.	N. Secant.	M

75 DEGREES.

## 75 DEGREES

Latitude 23 Deg. 00 Min. North Declination.

[illegible]

## 11 DEGREES.

M	L. Sine.	L. Co-Sine.	L. Tangent.	L. Co-Tang.	L. Secant.	L. Co-Secant.	
30	9.2996553	9.9911927	9.3084626	10.6915371	10.6085371	10.7003412	30
31	9.3002758	9.9911679	9.3091058	10.6908942	10.6088333	10.6997242	29
32	9.3008953	9.9911412	9.3097541	10.6902452	10.6091355	10.6991047	28
33	9.3015140	9.9911154	9.3103965	10.6895915	10.6094366	10.6984860	27
34	9.3021317	9.9910896	9.3110421	10.6889379	10.6097384	10.6978683	26
35	9.3027455	9.9910637	9.3116848	10.6882815	10.6100396	10.6972515	25
36	9.3033544	9.9910375	9.3123266	10.6876273	10.6103402	10.6966356	24
37	9.3039794	9.9910119	9.3129675	10.6869725	10.6106405	10.6960205	23
38	9.3045934	9.9909859	9.3136076	10.6863192	10.6109401	10.6954065	22
39	9.3052066	9.9909593	9.3142458	10.6856632	10.6112394	10.6947934	21
40	9.3058189	9.9909333	9.3148851	10.6850149	10.6115382	10.6941817	20
41	9.3064303	9.9909077	9.3155226	10.6843674	10.6118365	10.6935697	19
42	9.3070407	9.9908815	9.3161592	10.6837198	10.6121345	10.6929593	18
43	9.3076503	9.9908553	9.3167950	10.6830725	10.6124321	10.6923497	17
44	9.3082590	9.9908291	9.3174293	10.6824270	10.6127294	10.6917410	16
45	9.3088668	9.9908029	9.3180640	10.6817831	10.6130261	10.6911332	15
46	9.3094737	9.9907766	9.3186972	10.6811408	10.6133224	10.6905263	14
47	9.3100798	9.9907502	9.3193295	10.6804975	10.6136181	10.6899202	13
48	9.3106849	9.9907239	9.3199611	10.6798539	10.6139136	10.6893151	12
49	9.3112892	9.9906974	9.3205918	10.6792092	10.6142085	10.6887108	11
50	9.3118926	9.9906710	9.3212215	10.6785674	10.6145029	10.6881074	10
51	9.3124951	9.9906445	9.3218506	10.6779194	10.6147965	10.6875049	9
52	9.3130968	9.9906180	9.3224788	10.6772742	10.6150892	10.6869032	8
53	9.3136976	9.9905914	9.3231051	10.6766319	10.6153816	10.6863024	7
54	9.3142975	9.9905648	9.3237327	10.6759873	10.6156732	10.6857025	6
55	9.3148965	9.9905382	9.3243584	10.6753416	10.6159641	10.6851035	5
56	9.3154947	9.9905115	9.3249832	10.6746948	10.6162545	10.6845053	4
57	9.3160921	9.9904848	9.3256073	10.6740497	10.6165442	10.6839079	3
58	9.3166885	9.9904580	9.3262305	10.6734052	10.6168332	10.6833115	2
59	9.3172841	9.9904312	9.3268529	10.6727611	10.6171215	10.6827159	1
60	9.3178789	9.9904044	9.3274745	10.6721255	10.6174096	10.6821211	0
	L. Co-Sine.	L. Sine.	L. Co-Tang.	L. Tangent.	L. Co-Secant.	L. Secant.	M

## 78 D E G R E E S.

*Latitude 23 Deg. 00 Min. South Declination.*

[illegible]



## 12 D E G R E E S.

12 DEGREES.						
M	<i>L. Sine.</i>	<i>L. Co-Sine.</i>	<i>L. Tangent.</i>	<i>L. Co-Tang.</i>	<i>L. Secant.</i>	<i>L. Co-Secant.</i>
0	9.3178789	9.9924244	9.3273745	10.6725235	10.0093956	10.6821211
1	9.3184728	9.9903775	9.3280953	10.6719047	10.0095622	10.6815272
2	9.3190659	9.9883306	9.3287153	10.6712847	10.0097298	10.6809343
3	9.3196581	9.9862837	9.3293345	10.6706655	10.0098976	10.6803419
4	9.3202495	9.9842367	9.3299528	10.6700472	10.0100653	10.6797505
5	9.3208400	9.9821897	9.3305704	10.6694296	10.0102330	10.6791600
6	9.3214297	9.9801426	9.3311872	10.6688128	10.0104007	10.6785703
7	9.3220186	9.9780955	9.3318031	10.6681965	10.0105684	10.6779814
8	9.3226066	9.9760483	9.3324183	10.6675817	10.0107361	10.6773932
9	9.3231938	9.9740012	9.3330327	10.6669673	10.0109038	10.6768062
10	9.3237802	9.991339	9.3336463	10.6663537	10.0110715	10.6762188
11	9.3243657	9.9901067	9.3342591	10.6657409	10.0112392	10.6756343
12	9.3249505	9.9890794	9.3348711	10.6651289	10.0114069	10.6750495
13	9.3255344	9.9900521	9.3354823	10.6645177	10.0115747	10.6744656
14	9.3261174	9.9900247	9.3360927	10.6639073	10.0117424	10.6738826
15	9.3266997	9.9899973	9.3367024	10.6632976	10.0119102	10.6733003
16	9.3272811	9.9899698	9.3373113	10.6626887	10.0120780	10.6727189
17	9.3278617	9.9899423	9.3379194	10.6620806	10.0122457	10.6721383
18	9.3284416	9.9899148	9.3385267	10.6614733	10.0124135	10.6715584
19	9.3290206	9.9898873	9.3391333	10.6608667	10.0125812	10.6709794
20	9.3295988	9.9898597	9.3397391	10.6602629	10.0127490	10.6704012
21	9.3301761	9.9898320	9.3403441	10.6596599	10.0129168	10.6698239
22	9.3307527	9.9898043	9.3409484	10.6590561	10.0130846	10.6692473
23	9.3313285	9.9897766	9.3415519	10.6584541	10.0132523	10.6686715
24	9.3319025	9.9897489	9.3421546	10.6578544	10.0134201	10.6680965
25	9.3324777	9.9897211	9.3427566	10.6572544	10.0135879	10.6675223
26	9.3330511	9.9896932	9.3433578	10.6566544	10.0137557	10.6669489
27	9.3336237	9.9896654	9.3439583	10.6560547	10.0139235	10.6663763
28	9.3341955	9.9896374	9.3445580	10.6554540	10.0140913	10.6658045
29	9.3347666	9.9896095	9.3451570	10.6548540	10.0142591	10.6652335
30	9.3353368	9.9895815	9.3457552	10.6542543	10.0144269	10.6646632
	<i>L. Co-Sine.</i>	<i>L. Sine.</i>	<i>L. Co-Tang.</i>	<i>L. Tangent.</i>	<i>L. Co-Secant.</i>	<i>L. Secant.</i>

*Latitude 24 Deg. 00 Min. South Declination.*

[illegible]



A TABLE of Natural and

12 DEGREES.

M	N. Sine.	N. Co-Sine.	N. Tangent.	N. Co-Tang.	N. Secant.	N. Co-Secant.	
30	2163396	9762960	2216947	45107585	10242795	46222263	30
31	2167236	9752303	2219999	45045072	10243456	46147272	31
32	2170057	9761699	2223051	44973221	10244118	46081343	32
33	2172915	9751067	2226104	44921532	10244781	46021126	33
34	2175754	9760435	2229157	44869000	10245445	45961070	34
35	2178593	9759802	2232211	44798636	10246110	45910174	35
36	2181432	9759165	2235265	44737425	10246776	45841439	36
37	2184271	9758533	2238319	44676379	10247441	45781562	37
38	2187110	9757901	2241374	44615487	10248113	45722444	38
39	2189948	9757260	2244428	44554756	10248780	45663183	39
40	2192786	9756622	2247485	44494281	10249449	45604080	40
41	2195624	9755985	2250541	44433762	10250119	45545134	41
42	2198462	9755346	2253597	44373499	10250790	45486344	42
43	2201300	9754706	2256654	44313392	10251462	45427709	43
44	2204137	9754066	2259711	44253439	10252135	45369229	44
45	2206973	9753423	2262769	44193641	10252809	45310903	45
46	2209811	9752781	2265827	44133996	10253484	45252730	46
47	2212648	9752139	2268885	44074504	10254160	45194711	47
48	2215485	9751494	2271944	44015164	10254837	45136544	48
49	2218321	9750849	2275002	43955976	10255515	45079129	49
50	2221158	9750203	2278063	43896942	10256194	45021565	50
51	2223993	9749556	2281123	43838064	10256874	44964151	51
52	2226829	9748909	2284183	43779317	10257555	44906889	52
53	2229666	9748261	2287244	43720731	10258237	44849775	53
54	2232501	9747612	2290305	43662293	10258920	44792810	54
55	2235337	9746962	2293367	43603903	10259604	44735904	55
56	2238172	9746311	2296429	43545861	10260289	44679324	56
57	2241007	9745660	2299492	43487565	10260975	44622803	57
58	2243841	9745008	2302555	43429018	10261662	44566425	58
59	2246676	9744356	2305618	43372316	10262350	44510198	59
60	2249511	9743704	2308682	43314759	10263039	44454115	60
	N. Co-Sine.	N. Sine.	N. Co-Tang.	N. Tangent.	N. Co-Secant.	N. Secant.	M

77 D E G R E E S.

Latitude 25 Deg. 00 Min. North Declination.

[illegible]

*Artificial Sines, Tangents, and Secants.*

123

12 D E G R E E S.

M	L. Sine.	L. Co-Sine.	L. Tangent.	L. Co-Tang.	L. Secant.	L. Co-Secant.
30	9.3353368	9.9895815	9.2357552	10.6542448	10.0101135	10.6616652
31	9.3359062	9.9895855	9.2376372	10.6513628	10.0101466	10.6610928
32	9.3364749	9.9895894	9.2395194	10.6484806	10.0101745	10.6605212
33	9.3370428	9.9895934	9.2414014	10.6455984	10.0102024	10.6599496
34	9.3376099	9.9895972	9.2432834	10.6427162	10.0102303	10.6593780
35	9.3381762	9.9896010	9.2451654	10.6398340	10.0102582	10.6588064
36	9.3387418	9.9896048	9.2470474	10.6369518	10.0102861	10.6582348
37	9.3393066	9.9896086	9.2489294	10.6340696	10.0103140	10.6576632
38	9.3398706	9.9896124	9.2508114	10.6311874	10.0103419	10.6570916
39	9.3404343	9.9896162	9.2526934	10.6283052	10.0103698	10.6565200
40	9.3409983	9.9896200	9.2545754	10.6254230	10.0103977	10.6559484
41	9.3415620	9.9896238	9.2564574	10.6225408	10.0104256	10.6553768
42	9.3421258	9.9896276	9.2583394	10.6196586	10.0104535	10.6548052
43	9.3426895	9.9896314	9.2602214	10.6167764	10.0104814	10.6542336
44	9.3432532	9.9896352	9.2621034	10.6138942	10.0105093	10.6536620
45	9.3438169	9.9896390	9.2639854	10.6110120	10.0105372	10.6530904
46	9.3443806	9.9896428	9.2658674	10.6081298	10.0105651	10.6525188
47	9.3449443	9.9896466	9.2677494	10.6052476	10.0105930	10.6519472
48	9.3455080	9.9896504	9.2696314	10.6023654	10.0106209	10.6513756
49	9.3460717	9.9896542	9.2715134	10.5994832	10.0106488	10.6508040
50	9.3466354	9.9896580	9.2733954	10.5966010	10.0106767	10.6502324
51	9.3471991	9.9896618	9.2752774	10.5937188	10.0107046	10.6496608
52	9.3477628	9.9896656	9.2771594	10.5908366	10.0107325	10.6490892
53	9.3483265	9.9896694	9.2790414	10.5879544	10.0107604	10.6485176
54	9.3488902	9.9896732	9.2809234	10.5850722	10.0107883	10.6479460
55	9.3494539	9.9896770	9.2828054	10.5821900	10.0108162	10.6473744
56	9.3499976	9.9896808	9.2846874	10.5793078	10.0108441	10.6468028
57	9.3505413	9.9896846	9.2865694	10.5764256	10.0108720	10.6462312
58	9.3509922	9.9896884	9.2884514	10.5735434	10.0109000	10.6456596
59	9.3514431	9.9896922	9.2903334	10.5706612	10.0109279	10.6450880
60	9.3518940	9.9896960	9.2922154	10.5677790	10.0109558	10.6445164
	L. Co-Sine.	L. Sine.	L. Co-Tang.	L. Tangent.	L. Co-Secant.	L. Secant.

77 DEGREES

*Latitude* 25 Deg. 00 Min. *South Declination.*

[illegible]







A TABLE of Natural and

13 DEGREES.									
M	N. Sine.	N. Co-Sine.	N. Tangent.	N. Co-Tangent.	N. Secant.	N. Co-Secant.			
30	2334454	9723652	2127787	4165299	10284152	42836576	2		
31	2337282	9728115	2131854	41599585	10284718	4284738	3		
32	2340110	9722183	2135911	41546001	10285591	42733029	23		
33	2342938	9721658	2140019	41491446	10286312	42581449	24		
34	2345766	9720975	2144307	41440519	10287034	42629956	25		
35	2348594	9720223	2148676	41387719	10287757	42678671	26		
36	2351421	9719492	2153235	41335246	10288481	42527474	24		
37	2354248	9718752	2157893	41283279	10289206	42476402	23		
38	2357075	9718040	2162644	41230979	10289932	42425457	22		
39	2359902	9717354	2167494	41177754	10290668	42374637	21		
40	2362729	9716667	2172345	41124614	10291385	42323943	20		
41	2365555	9715979	2177195	41071569	10292113	42273373	19		
42	2368381	9715291	2182045	41018649	10292842	42222928	18		
43	2371207	9714602	2186895	40965932	10293572	42172605	17		
44	2374033	9713912	2191745	40913187	10294303	42122408	16		
45	2376859	9713221	2196594	40860652	10295035	42072333	15		
46	2379684	9712529	2201443	40808119	10295768	42022380	14		
47	2382510	9711836	2206292	40755582	10296502	41972549	13		
48	2385335	9711143	2211141	40703045	10297237	41922840	12		
49	2388161	9710449	2215990	40650514	10297973	41873252	11		
50	2390984	9709754	2220838	40597970	10298710	41823785	10		
51	2393808	9709058	2225687	40545427	10299448	41774438	9		
52	2396633	9708361	2230535	40492884	10300187	41725102	8		
53	2399457	9707663	2235384	40440341	10300927	41676102	7		
54	2402280	9706965	2240232	40387798	10301668	41627114	6		
55	2405104	9706266	2245081	40335255	10302410	41578243	5		
56	2407927	9705566	2249929	40282712	10303151	41529491	4		
57	2410751	9704865	2254778	40230169	10303897	41480856	3		
58	2413574	9704163	2259626	40177626	10304642	41432339	2		
59	2416398	9703460	2264475	40125083	10305388	41383939	1		
60	2419221	9702757	2269323	40072540	10306135	41335655	0		
	N. Co-Sine.	N. Sine.	N. Tangent.	N. Co-Tangent.	N. Co-Secant.	N. Secant.			M

[illegible]

13 DEGREES.									
M	<i>L. Sine.</i>	<i>L. Co-Sine.</i>	<i>L. Tangent.</i>	<i>L. Co-Tang.</i>	<i>L. Secant.</i>	<i>L. Co-Secant.</i>			
30	9.3681853	9.9878315	9.3823537	10.6156463	1.00121685	1.6319147	30		
31	9.3687111	9.9878012	9.3830910	10.6149090	1.00121958	1.6312189	29		
32	9.3692363	9.9877708	9.3838265	10.6141695	1.00122292	1.6305763	28		
33	9.3697608	9.9877404	9.3845620	10.6134295	1.00122566	1.6302392	27		
34	9.3702847	9.9877099	9.3852975	10.6126892	1.00122841	1.6297153	26		
35	9.3708079	9.9876794	9.3860330	10.6119485	1.00123116	1.6291921	25		
36	9.3713304	9.9876488	9.3867685	10.6112080	1.00123392	1.6286695	24		
37	9.3718523	9.9876183	9.3875040	10.6104675	1.00123667	1.6281477	23		
38	9.3723735	9.9875877	9.3882395	10.6097270	1.00123943	1.6276265	22		
39	9.3728940	9.9875570	9.3889750	10.6089865	1.00124219	1.6271060	21		
40	9.3734139	9.9875263	9.3897105	10.6082460	1.00124495	1.6265861	20		
41	9.3739331	9.9874955	9.3904460	10.6075055	1.00124771	1.6260669	19		
42	9.3744517	9.9874648	9.3911815	10.6067650	1.00125047	1.6255483	18		
43	9.3749696	9.9874339	9.3919170	10.6060245	1.00125323	1.6250294	17		
44	9.3754868	9.9874031	9.3926525	10.6052840	1.00125599	1.6245132	16		
45	9.3760034	9.9873722	9.3933880	10.6045435	1.00125875	1.6240006	15		
46	9.3765194	9.9873413	9.3941235	10.6038030	1.00126151	1.6234906	14		
47	9.3770347	9.9873103	9.3948590	10.6030625	1.00126427	1.6229857	13		
48	9.3775493	9.9872793	9.3955945	10.6023220	1.00126703	1.6224807	12		
49	9.3780633	9.9872482	9.3963300	10.6015815	1.00126979	1.6219757	11		
50	9.3785757	9.9872171	9.3970655	10.6008410	1.00127255	1.6214732	10		
51	9.3790894	9.9871860	9.3978010	10.6001005	1.00127531	1.6209716	9		
52	9.3796019	9.9871549	9.3985365	10.5993600	1.00127807	1.6204735	8		
53	9.3801129	9.9871236	9.3992720	10.5986195	1.00128083	1.6199785	7		
54	9.3806237	9.9870921	9.3999975	10.5978790	1.00128359	1.6194865	6		
55	9.3811339	9.9870611	9.3997130	10.5971385	1.00128635	1.6189961	5		
56	9.3816434	9.9870298	9.3994285	10.5963980	1.00128911	1.6185066	4		
57	9.3821523	9.9869989	9.3991440	10.5956575	1.00129187	1.6180166	3		
58	9.3826605	9.9869676	9.3998595	10.5949170	1.00129463	1.6175273	2		
59	9.3831682	9.9869363	9.3995750	10.5941765	1.00129739	1.6170385	1		
60	9.3836752	9.9869041	9.3992771	10.5934360	1.00129979	1.6165518	0		
	<i>L. Co-Sine.</i>	<i>L. Sine.</i>	<i>L. Co-Tang.</i>	<i>L. Tangent.</i>	<i>L. Co-Secant.</i>	<i>L. Secant.</i>			M

[illegible]



## 14 DEGREES.

M	N. Sine.	N. Co-Sine.	V. Tangent.	V. Co-Tangent.	N. Secant.	N. Co-Secant.	M
0	2119219	9702957	2192250	4010789	10306135	41335655	60
1	2122041	9702253	2496370	40053165	10306883	41287487	59
2	2124563	9701548	2799460	40005632	10307632	41239435	58
3	2127085	9700842	3102551	39959223	10308382	41191498	57
4	2129607	9700135	3405642	39909924	10309133	41143675	56
5	2132129	9699428	3708734	39860739	10309885	41095967	55
6	2134650	9698720	4011825	39811569	10310638	41048374	54
7	2137171	9698011	4314919	39762412	10311392	41000893	53
8	2139692	9697301	4618012	39713265	10312147	40953526	52
9	2142213	9696590	4921106	39664117	10312903	40906272	51
10	2144733	9695879	5224200	39614968	10313660	40859130	50
11	2147254	9695167	5527294	39565811	10314418	40812000	49
12	2149774	9694454	5830389	39516655	10315177	40765181	48
13	2152294	9693740	6133484	39467511	10315936	40718374	47
14	2154813	9693025	6436579	39418367	10316697	40671577	46
15	2157333	9692309	6739674	39369223	10317459	40625091	45
16	2159852	9691592	7042769	39320079	10318222	40578615	44
17	2162371	9690875	7345864	39270935	10318985	40532249	43
18	2164890	9690157	7648959	39221791	10319750	40485922	42
19	2167409	9689438	7952054	39172647	10320516	40439844	41
20	2169928	9688718	8255149	39123503	10321282	40393804	40
21	2172447	9687998	8558244	39074359	10322048	40347762	39
22	2174966	9687277	8861339	39025215	10322815	40302048	38
23	2177485	9686555	9164434	38976071	10323582	40256332	37
24	2179999	9685832	9467529	38926927	10324350	40210722	36
25	2182518	9685108	9770624	38877783	10325119	40165219	35
26	2185037	9684383	10073766	38828639	10325890	40119823	34
27	2187556	9683657	10370888	38779495	10326662	40074532	33
28	2190075	9682931	10668010	38730351	10327434	40029347	32
29	2192594	9682204	10965032	38681207	10328207	39984267	31
30	2195113	9681476	11262054	38632063	10329000	39939292	30
N. Co-Sine.		N. Sine.	N. Co-Tangent.		N. Co-Secant.	N. Secant.	M

## 75 DEGREES.

Latitude 28 Deg. 00 Min. North Declination.																									
	0	d.	2	d.	4	d.	6	d.	8	d.	10	d.	12	d.	14	d.	16	d.	18	d.	20	d.	22	d.	23
	b. m.	b. m.	b. m.	b. m.	b. m.	b. m.	b. m.	b. m.	b. m.	b. m.	b. m.	b. m.	b. m.	b. m.	b. m.	b. m.	b. m.	b. m.	b. m.	b. m.	b. m.	b. m.	b. m.	b. m.	b. m.
S N	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0
1	0.21	1.0.20	1.0.19	1.0.19	1.0.18	1.0.18	2.0.16	2.0.14	2.0.14	1.0.15	1.0.12	1.0.12	1.0.11	1.0.11	2.0.09	2.0.07	2.0.05	2.0.05	1.0.02	1.0.02	1.0.02	1.0.02	1.0.02	1.0.02	1.0.02
2	0.44	2.0.42	2.0.39	2.0.39	2.0.36	2.0.36	3.0.33	3.0.33	3.0.30	3.0.27	3.0.24	3.0.23	3.0.21	3.0.21	3.0.18	4.0.14	3.0.11	3.0.11	3.0.08	3.0.08	3.0.08	3.0.08	3.0.08	3.0.08	3.0.08
3	1.10	4.1.06	4.1.02	4.1.02	5.0.59	5.0.59	5.0.52	5.0.47	5.0.42	5.0.37	5.0.32	5.0.32	5.0.27	5.0.27	5.0.22	6.0.16	5.0.16	5.0.16	5.0.16	5.0.16	5.0.16	5.0.16	5.0.16	5.0.16	5.0.16
4	1.41	6.1.35	6.1.29	6.1.29	7.1.22	7.1.15	7.1.08	6.1.02	6.0.56	7.0.49	7.0.49	7.0.42	7.0.35	7.0.35	10.0.25	6.0.19	6.0.19	6.0.19	6.0.19	6.0.19	6.0.19	6.0.19	6.0.19	6.0.19	6.0.19
5	2.20	8.2.12	8.2.03	8.2.03	9.1.56	9.1.45	9.1.36	8.1.27	8.1.15	8.1.08	8.1.08	8.1.05	10.0.48	11.0.37	9.0.16	9.0.16	9.0.16	9.0.16	9.0.16	9.0.16	9.0.16	9.0.16	9.0.16	9.0.16	9.0.16
6	3.14	11.3.03	11.3.03	11.3.03	11.3.41	12.2.25	12.2.17	13.2.03	13.2.03	15.1.51	15.1.37	15.1.25	14.1.11	16.0.55	12.0.43	12.0.43	12.0.43	12.0.43	12.0.43	12.0.43	12.0.43	12.0.43	12.0.43	12.0.43	12.0.43
7	4.28	14.4.14	14.4.14	14.4.00	14.3.46	14.3.32	15.1.17	17.4.00	17.4.00	17.4.00	17.4.00	17.4.00	17.4.00	17.4.00	17.4.00	17.4.00	17.4.00	17.4.00	17.4.00	17.4.00	17.4.00	17.4.00	17.4.00	17.4.00	17.4.00
WE	6.00	15.5.45	15.5.30	15.5.30	15.5.15	16.4.59	16.4.43	19.1.42	19.1.42	19.1.42	19.1.42	19.1.42	19.1.42	19.1.42	19.1.42	19.1.42	19.1.42	19.1.42	19.1.42	19.1.42	19.1.42	19.1.42	19.1.42	19.1.42	19.1.42
1																									
2																									

## 14 DEGREES.

M	L. Sine.	L. Co-Sine.	L. Tangent.	L. Co-Tangent.	L. Secant.	L. Co-Secant.	M
0	9.9836752	9.9869041	9.9867711	10.632259	10.135829	10.616325	60
1	9.9841515	9.9868726	9.9873059	10.6326911	10.1361474	10.616315	59
2	9.9846273	9.9868410	9.9877485	10.633137	10.1364659	10.616307	58
3	9.9851031	9.9868094	9.9881911	10.633583	10.1367843	10.616299	57
4	9.9855789	9.9867778	9.9886337	10.634029	10.1371007	10.616291	56
5	9.9860547	9.9867461	9.9890763	10.634475	10.1374171	10.616283	55
6	9.9865305	9.9867144	9.9895189	10.634921	10.1377335	10.616275	54
7	9.9870063	9.9866827	9.9899615	10.635367	10.1380499	10.616267	53
8	9.9874821	9.9866510	9.9904041	10.635813	10.1383683	10.616259	52
9	9.9879579	9.9866193	9.9908467	10.636259	10.1386867	10.616251	51
10	9.9884337	9.9865876	9.9912893	10.636705	10.1390051	10.616243	50
11	9.9889095	9.9865559	9.9917319	10.637151	10.1393235	10.616235	49
12	9.9893853	9.9865242	9.9921745	10.637597	10.1396419	10.616227	48
13	9.9898611	9.9864925	9.9926171	10.638043	10.1399603	10.616219	47
14	9.9903369	9.9864608	9.9930597	10.638489	10.1402787	10.616211	46
15	9.9908127	9.9864291	9.9935023	10.638935	10.1405971	10.616203	45
16	9.9912885	9.9863974	9.9939449	10.639381	10.1409155	10.616195	44
17	9.9917643	9.9863657	9.9943875	10.639827	10.1412339	10.616187	43
18	9.9922401	9.9863340	9.9948301	10.640273	10.1415523	10.616179	42
19	9.9927159	9.9863023	9.9952727	10.640719	10.1418707	10.616171	41
20	9.9931917	9.9862706	9.9957153	10.641165	10.1421891	10.616163	40
21	9.9936675	9.9862389	9.9961579	10.641611	10.1425075	10.616155	39
22	9.9941433	9.9862072	9.9966005	10.642057	10.1428259	10.616147	38
23	9.9946191	9.9861755	9.9970431	10.642503	10.1431443	10.616139	37
24	9.9950949	9.9861438	9.9974857	10.642949	10.1434627	10.616131	36
25	9.9955707	9.9861121	9.9979283	10.643395	10.1437811	10.616123	35
26	9.9960465	9.9860804	9.9983709	10.643841	10.1440995	10.616115	34
27	9.9965223	9.9860487	9.9988135	10.644287	10.1444179	10.616107	33
28	9.9969981	9.9860170	9.9992561	10.644733	10.1447363	10.616099	32
29	9.9974739	9.9859853	9.9996987	10.645179	10.1450547	10.616091	31
30	9.9979497	9.9859536	10.0001413	10.645625	10.1453731	10.616083	30
L. Co-Sine.		L. Sine.	L. Co-Tangent.		L. Tangent.	L. Co-Secant.	L. Secant.

## 75 DEGREES.

Latitude 28 Deg. 00 Min. South Declination.																								
	0	d. 2	d. 4	d. 6	d. 8	d. 10	d. 12	d. 14	d. 16	d. 18	d. 20	d. 22	d. 23											
	b. m. m	b. m. m	b. m. m	b. m. m	b. m. m	b. m. m	b. m. m	b. m. m	b. m. m	b. m. m	b. m. m	b. m. m	b. m. m											
S N	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0											
1	0.21	1.0.22	1.0.23	1.0.24	2.0.25	2.0.26	2.0.27	2.0.28	2.0.29	2.0.30	2.0.31	2.0.32	2.0.33											
2	0.44	2.0.45	2.0.46	2.0.47	2.0.48	2.0.49	2.0.50	2.0.51	2.0.52	2.0.53	2.0.54	2.0.55	2.0.56											
3	1.10	4.1.11	4.1.12	4.1.13	4.1.14	4.1.15	4.1.16	4.1.17	4.1.18	4.1.19	4.1.20	4.1.21	4.1.22											
4	1.41	6.1.41	6.1.42	6.1.43	6.1.44	6.1.45	6.1.46	6.1.47	6.1.48	6.1.49	6.1.50	6.1.51	6.1.52											
5	2.20	8.2.21	8.2.22	8.2.23	8.2.24	8.2.25	8.2.26	8.2.27	8.2.28	8.2.29	8.2.30	8.2.31	8.2.32											
6	3.14	11.3.21	11.3.22	11.3.23	11.3.24	11.3.25	11.3.26	11.3.27	11.3.28	11.3.29	11.3.30	11.3.31	11.3.32											
WE	4.23	14.4.22	14.4.23	14.4.24	14.4.25	14.4.26	14.4.27	14.4.28	14.4.29	14.4.30	14.4.31	14.4.32	14.4.33											



## A TABLE of Natural and

14 DEGREES.

M	N. Sine.	N. Co-sine.	V. Tangent.	V. Co-Tang.	N. Secant.	N. Co-Secant.
30	2503500	9681476	2556175	35667131	10329003	39939252
31	2506616	9680747	2558280	35620782	10329781	39894421
32	2509432	9680018	2559284	35574537	10330559	39849654
33	2512248	9679288	2559488	35528396	10331339	39804991
34	2515063	9678557	2559593	35482358	10332119	39760431
35	2517879	9677822	2559699	35436424	10332901	39715975
36	2520694	9677092	2559805	35390591	10333683	39671621
37	2523509	9676358	2559911	35344761	10334467	39627369
38	2526323	9675623	2560018	35298933	10335251	39583219
39	2529137	9674888	2560125	35253107	10336037	39539171
40	2531952	9674152	2560232	35207281	10336823	39495224
41	2534766	9673415	2560340	35161455	10337611	39451379
42	2537579	9672677	2560448	35115629	10338399	39407533
43	2540393	9671939	2560556	35069803	10339188	39363688
44	2543206	9671202	2560664	35023977	10339979	39319843
45	2546019	9670465	2560772	34978151	10340770	39276000
46	2548832	9669728	2560880	34932325	10341563	39232155
47	2551645	9668991	2560988	34886499	10342358	39188311
48	2554458	9668254	2561096	34840673	10343151	39144467
49	2557272	9667517	2561204	34794847	10343946	39100623
50	2560085	9666780	2561312	34749021	10344743	39056779
51	2562898	9666043	2561420	34703195	10345540	39012935
52	2565712	9665306	2561528	34657369	10346338	38969091
53	2568525	9664569	2561636	34611543	10347137	38925247
54	2571338	9663832	2561744	34565717	10347937	38881403
55	2574151	9663095	2561852	34519891	10348738	38837559
56	2576964	9662358	2561960	34474065	10349540	38793715
57	2579777	9661621	2562068	34428239	10350343	38749871
58	2582590	9660884	2562176	34382413	10351148	38706027
59	2585403	9660147	2562284	34336587	10351955	38662183
60	2588216	9659410	2562392	34290761	10352762	38618339
	N. Co-Sine.	N. Sine.	N. Co-Tang.	N. Tangent.	N. Co-Secant.	N. Secant.

75 DEGREES.

Latitude 29 Deg. 00 Min. North Declination.

	0	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20	21	22	23	24
N	k.m.m	k.m.m	k.m.m	k.m.m	k.m.m	k.m.m	k.m.m	k.m.m	k.m.m	k.m.m	k.m.m	k.m.m	k.m.m	k.m.m	k.m.m	k.m.m	k.m.m	k.m.m	k.m.m	k.m.m	k.m.m	k.m.m	k.m.m	k.m.m	k.m.m
1	0.22	1.21	1.21	1.22	1.23	1.24	1.25	1.26	1.27	1.28	1.29	1.30	1.31	1.32	1.33	1.34	1.35	1.36	1.37	1.38	1.39	1.40	1.41	1.42	1.43
2	0.45	2.04	2.03	2.04	2.05	2.06	2.07	2.08	2.09	2.10	2.11	2.12	2.13	2.14	2.15	2.16	2.17	2.18	2.19	2.20	2.21	2.22	2.23	2.24	2.25
3	1.12	4.13	4.13	4.14	4.15	4.16	4.17	4.18	4.19	4.20	4.21	4.22	4.23	4.24	4.25	4.26	4.27	4.28	4.29	4.30	4.31	4.32	4.33	4.34	4.35
4	1.43	6.13	6.13	6.14	6.15	6.16	6.17	6.18	6.19	6.20	6.21	6.22	6.23	6.24	6.25	6.26	6.27	6.28	6.29	6.30	6.31	6.32	6.33	6.34	6.35
5	2.13	8.20	8.20	8.21	8.22	8.23	8.24	8.25	8.26	8.27	8.28	8.29	8.30	8.31	8.32	8.33	8.34	8.35	8.36	8.37	8.38	8.39	8.40	8.41	8.42
6	3.34	14.30	14.30	14.31	14.32	14.33	14.34	14.35	14.36	14.37	14.38	14.39	14.40	14.41	14.42	14.43	14.44	14.45	14.46	14.47	14.48	14.49	14.50	14.51	14.52
7	4.14	16.40	16.40	16.41	16.42	16.43	16.44	16.45	16.46	16.47	16.48	16.49	16.50	16.51	16.52	16.53	16.54	16.55	16.56	16.57	16.58	16.59	16.60	16.61	16.62
8	5.22	18.51	18.51	18.52	18.53	18.54	18.55	18.56	18.57	18.58	18.59	19.00	19.01	19.02	19.03	19.04	19.05	19.06	19.07	19.08	19.09	19.10	19.11	19.12	19.13
9	6.12	20.42	20.42	20.43	20.44	20.45	20.46	20.47	20.48	20.49	20.50	20.51	20.52	20.53	20.54	20.55	20.56	20.57	20.58	20.59	21.00	21.01	21.02	21.03	21.04
10	7.02	22.33	22.33	22.34	22.35	22.36	22.37	22.38	22.39	22.40	22.41	22.42	22.43	22.44	22.45	22.46	22.47	22.48	22.49	22.50	22.51	22.52	22.53	22.54	22.55
11	7.52	24.24	24.24	24.25	24.26	24.27	24.28	24.29	24.30	24.31	24.32	24.33	24.34	24.35	24.36	24.37	24.38	24.39	24.40	24.41	24.42	24.43	24.44	24.45	24.46
12	8.42	26.15	26.15	26.16	26.17	26.18	26.19	26.20	26.21	26.22	26.23	26.24	26.25	26.26	26.27	26.28	26.29	26.30	26.31	26.32	26.33	26.34	26.35	26.36	26.37
13	9.32	28.06	28.06	28.07	28.08	28.09	28.10	28.11	28.12	28.13	28.14	28.15	28.16	28.17	28.18	28.19	28.20	28.21	28.22	28.23	28.24	28.25	28.26	28.27	28.28
14	10.22	29.97	29.97	29.98	29.99	30.00	30.01	30.02	30.03	30.04	30.05	30.06	30.07	30.08	30.09	30.10	30.11	30.12	30.13	30.14	30.15	30.16	30.17	30.18	30.19
15	11.12	31.88	31.88	31.89	31.90	31.91	31.92	31.93	31.94	31.95	31.96	31.97	31.98	31.99	32.00	32.01	32.02	32.03	32.04	32.05	32.06	32.07	32.08	32.09	32.10
16	12.02	33.79	33.79	33.80	33.81	33.82	33.83	33.84	33.85	33.86	33.87	33.88	33.89	33.90	33.91	33.92	33.93	33.94	33.95	33.96	33.97	33.98	33.99	34.00	34.01
17	12.92	35.70	35.70	35.71	35.72	35.73	35.74	35.75	35.76	35.77	35.78	35.79	35.80	35.81	35.82	35.83	35.84	35.85	35.86	35.87	35.88	35.89	35.90	35.91	35.92
18	13.82	37.61	37.61	37.62	37.63	37.64	37.65	37.66	37.67	37.68	37.69	37.70	37.71	37.72	37.73	37.74	37.75	37.76	37.77	37.78	37.79	37.80	37.81	37.82	37.83
19	14.72	39.52	39.52	39.53	39.54	39.55	39.56	39.57	39.58	39.59	39.60	39.61	39.62	39.63	39.64	39.65	39.66	39.67	39.68	39.69	39.70	39.71	39.72	39.73	39.74
20	15.62	41.43	41.43	41.44	41.45	41.46	41.47	41.48	41.49	41.50	41.51	41.52	41.53	41.54	41.55	41.56	41.57	41.58	41.59	41.60	41.61	41.62	41.63	41.64	41.65
21	16.52	43.34	43.34	43.35	43.36	43.37	43.38	43.39	43.40	43.41	43.42	43.43	43.44	43.45	43.46	43.47	43.48	43.49	43.50	43.51	43.52	43.53	43.54	43.55	43.56
22	17.42	45.25	45.25	45.26	45.27	45.28	45.29	45.30	45.31	45.32	45.33	45.34	45.35	45.36	45.37	45.38	45.39	45.40	45.41	45.42	45.43	45.44	45.45	45.46	45.47
23	18.32	47.16	47.16	47.17	47.18	47.19	47.20	47.21	47.22	47.23	47.24	47.25	47.26	47.27	47.28	47.29	47.30	47.31	47.32	47.33	47.34	47.35	47.36	47.37	47.38
24	19.22	49.07	49.07	49.08	49.09	49.10	49.11	49.12	49.13	49.14	49.15	49.16	49.17	49.18	49.19	49.20	49.21	49.22	49.23	49.24	49.25	49.26	49.27	49.28	49.29
25	20.12	50.98	50.98	50.99	51.00	51.01	51.02	51.03	51.04	51.05	51.06	51.07	51.08	51.09	51.10	51.11	51.12	51.13	51.14	51.15	51.16	51.17	51.18	51.19	51.20
26	21.02	52.89	52.89	52.90	52.91	52.92	52.93	52.94	52.95	52.96	52.97	52.98	52.99	53.00	53.01	53.02	53.03	53.04	53.05	53.06	53.07	53.08	53.09	53.10	53.11
27	21.92	54.80	54.80	54.81	54.82	54.83	54.84	54.85	54.86	54.87	54.88	54.89	54.90	54.91	54.92	54.93	54.94	54.95	54.96	54.97	54.98	54.99	55.00	55.01	55.02
28	22.82	56.71	56.71	56.72	56.73	56.74	56.75	56.76	56.77	56.78	56.79	56.80	56.81	56.82	56.83	56.84	56.85	56.86	56.87	56.88	56.89	56.90	56.91	56.92	56.93
29	23.72	58.62	58.62	58.63	58.64	58.65	58.66	58.67	58.68	58.69	58.70	58.71	58.72	58.73	58.74	58.75	58.76	58.77	58.78	58.79	58.80	58.81	58.82	58.83	58.84
30	24.62	60.53	60.53	60.54	60.55	60.56	60.57	60.58	60.59	60.60	60.61	60.62	60.63	60.64	60.65	60.66	60.67	60.68	60.69	60.70	60.71	60.72	60.73	60.74	60.75
31	25.52	62.44	62.44	62.45	62.46	62.47	62.48	62.49	62.50	62.51	62.52	62.53	62.54	62.55	62.56	62.57	62.58	62.59	62.60	62.61	62.62	62.63	62.64	62.65	62.66
32	26.42	64.35	64.35	64.36	64.37	64.38	64.39	64.40	64.41	64.42	64.43	64.44	64.45	64.46	64.47	64.48	64.49	64.50	64.51	64.52	64.53	64.54	64.55	64.56	64.57
33	27.32	66.26	66.26	66.27	66.28	66.29	66.30	66.31	66.32	66.33	66.34	66.35	66.36	66.37	66.38	66.39	66.40	66.41	66.42	66.43	66.44	66.45	66.46	66.47	66.48
34	28.22	68.17	68.17	68.18	68.19	68.20	68.21	68.22	68.23	68.24	68.25	68.26	68.27	68.28	68.29	68.30	68.31	68.32	68.33	68.34	68.35	68.36	68.37	68.38	68.39
35	29.12	70.08	70.08	70.09	70.10	70.11	70.12	70.13	70.14	70.15	70.16	70.17	70.18	70.19	70.20	70.21	70.22	70.23	70.24	70.25	70.26	70.27	70.28	70.29	70.30



## A TABLE of Natural and

15 DEGREES.						
M	N. Sine.	N. Co-Sine.	N. Tangent.	N. Co-Tang.	N. Secant.	N. Co-Secant.
0	255190	9659258	2679492	3732508	10352762	38637033
1	2591000	9655505	2682610	37277131	10353569	38595135
2	2593810	9657751	2685728	37233547	10354373	38553332
3	2596619	9659926	2688847	37192955	10355187	38511622
4	2599428	9662101	2691967	37147561	10355998	38470005
5	2602237	9664276	2695087	37104555	10356809	38428482
6	2605046	9666451	2698207	37061648	10357621	38387051
7	2607855	9668626	2701328	37018830	10358435	38345713
8	2610664	9670801	2704449	36976103	10359249	38304467
9	2613473	9672976	2707571	36933469	10360065	38263313
10	2616282	9675151	2710693	36890835	10360881	38222251
11	2619091	9677326	2713815	36848475	10361699	38181280
12	2621900	9679501	2716937	36806115	10362517	38140399
13	2624709	9681676	2720059	36763755	10363337	38099610
14	2627518	9683851	2723181	36721395	10364157	38058911
15	2630327	9686026	2726303	36679035	10364979	38018301
16	2633136	9688201	2729425	36636675	10365801	37977782
17	2635945	9690376	2732547	36594315	10366625	37937352
18	2638754	9692551	2735669	36551955	10367449	37897011
19	2641563	9694726	2738791	36509595	10368275	37856760
20	2644372	9696901	2741913	36467235	10369101	37816509
21	2647181	9699076	2745035	36424875	10369929	37776258
22	2649990	9701251	2748157	36382515	10370757	37735933
23	2652800	9703426	2751279	36340155	10371587	37695603
24	2655609	9705601	2754401	36297795	10372417	37655274
25	2658418	9707776	2757523	36255435	10373249	37614945
26	2661227	9709951	2760645	36213075	10374079	37574616
27	2664036	9712126	2763767	36170715	10374913	37534287
28	2666845	9714301	2766889	36128355	10375749	37493958
29	2669654	9716476	2770011	36085995	10376585	37453629
30	2672463	9718651	2773133	36043635	10377422	37413300
74 DEGREES.						
M	N. Sine.	N. Co-Sine.	N. Tangent.	N. Co-Tang.	N. Secant.	N. Co-Secant.

## Artificial Sines, Tangents, and Secants.

15 DEGREES.						
M	L. Sine.	L. Co-Sine.	L. Tangent.	L. Co-Tang.	L. Secant.	L. Co-Secant.
0	94129962	99849438	94285575	105719475	105719475	105719475
1	94134674	99845059	94290521	105714425	105714425	105714425
2	94139381	99840680	94295466	105709379	105709379	105709379
3	94144082	99836301	94295466	105704339	105704339	105704339
4	94148778	99831922	94300412	105699293	105699293	105699293
5	94153458	99827543	94305357	105694247	105694247	105694247
6	94158152	99823164	94310303	105689201	105689201	105689201
7	94162852	99818785	94315248	105684155	105684155	105684155
8	94167556	99814406	94320194	105679109	105679109	105679109
9	94172174	99810027	94325139	105674063	105674063	105674063
10	94176837	99805648	94330085	105669017	105669017	105669017
11	94181495	99801269	94335030	105663971	105663971	105663971
12	94186148	99796890	94340076	105658925	105658925	105658925
13	94190795	99792511	94345121	105653879	105653879	105653879
14	94195436	99788132	94350167	105648833	105648833	105648833
15	94200073	99783753	94355213	105643787	105643787	105643787
16	94204704	99779374	94360259	105638741	105638741	105638741
17	94209330	99774995	94365305	105633695	105633695	105633695
18	94213950	99770616	94370351	105628649	105628649	105628649
19	94218566	99766237	94375396	105623603	105623603	105623603
20	94223176	99761858	94380442	105618557	105618557	105618557
21	94227780	99757479	94385487	105613511	105613511	105613511
22	94232390	99753100	94390533	105608465	105608465	105608465
23	94236974	99748721	94395578	105603419	105603419	105603419
24	94241553	99744342	94400624	105598373	105598373	105598373
25	94246147	99739963	94405669	105593327	105593327	105593327
26	94250726	99735584	94410715	105588281	105588281	105588281
27	94255299	99731205	94415761	105583235	105583235	105583235
28	94259867	99726826	94420807	105578189	105578189	105578189
29	94264430	99722447	94425853	105573143	105573143	105573143
30	94268998	99718068	94430899	105568097	105568097	105568097
	L. Co-Sine.	L. Sine.	L. Co-Tang.	L. Tangent.	L. Co-Secant.	L. Secant.



A T A B L E of Natural and

15 DEGREES.									
	N. <i>Star.</i>	N. <i>Co-Star.</i>	N. <i>Tangent.</i>	N. <i>Co-Tang.</i>	N. <i>Secant.</i>	N. <i>Co-Secant.</i>			
30	2672384	9636305	2773245	36588335	10377422	37419775	30		
31	2675187	9635527	2776373	36518146	10373265	37350568	29		
32	2677582	9634743	2779512	364477143	10369098	37281416	28		
33	2680792	9633969	2782646	36377224	10364928	37212409	27		
34	2683994	9633188	2785780	36306690	10360779	37143454	26		
35	2686395	9632405	2788915	36236241	10356621	37074489	25		
36	2689193	9631626	2792050	36165975	10352463	37005505	24		
37	2692000	9630843	2795186	36095794	10348307	36936512	23		
38	2694801	9630059	2798322	36025535	10344152	36867520	22		
39	2697602	9629276	2801459	35955261	10340007	36798536	21		
40	2700403	9628490	2804597	35884979	10335862	36729552	20		
41	2703204	9627704	2807735	35814690	10331717	36660568	19		
42	2706004	9626917	2810873	35744383	10327572	36591584	18		
43	2708805	9626130	2814012	35674077	10323427	36522600	17		
44	2711605	9625342	2817152	35603764	10319282	36453616	16		
45	2714406	9624555	2820292	35533452	10315137	36384632	15		
46	2717207	9623767	2823432	35463140	10310992	36315648	14		
47	2720008	9622979	2826573	35392828	10306847	36246664	13		
48	2722809	9622190	2829715	35322515	10302702	36177680	12		
49	2725610	9621403	2832857	35252203	10298557	36108696	11		
50	2728410	9620615	2835999	35181890	10294412	36039712	10		
51	2731211	9619828	2839142	35111578	10290267	35970728	9		
52	2734012	9619040	2842284	35041265	10286122	35901744	8		
53	2736813	9618253	2845427	34970953	10281977	35832760	7		
54	2739614	9617465	2848570	34900640	10277832	35763776	6		
55	2742415	9616678	2851712	34830328	10273687	35694792	5		
56	2745216	9615891	2854855	34760015	10269542	35625808	4		
57	2748017	9615104	2857997	34689703	10265397	35556824	3		
58	2750818	9614317	2861140	34619390	10261252	35487840	2		
59	2753619	9613530	2864283	34549078	10257107	35418856	1		
60	2756420	9612743	2867425	34478765	10252962	35349872	0		
	N. <i>Co-Star.</i>	N. <i>Star.</i>	N. <i>Co-Tang.</i>	N. <i>Tangent.</i>	N. <i>Co-Secant.</i>	N. <i>Secant.</i>			

[illegible]

15 DEGREES.									
M	<i>L. Sine.</i>	<i>L. Co-Sine.</i>	<i>L. Tangent.</i>	<i>L. Co-Tang.</i>	<i>L. Secant.</i>	<i>L. Co-Secant.</i>			
30	4.265988	9.9832105	9.4428883	10.5571117	10.0160395	10.5731012	30		
31	4.4273541	9.9838755	9.4434786	10.5565214	10.0161245	10.5726459	29		
32	4.4728089	9.9838104	9.4439853	10.5560315	10.0161684	10.5721911	28		
33	4.4826631	9.9838092	9.4444579	10.5555415	10.0161948	10.5717369	27		
34	4.487169	9.9837701	9.4449463	10.5550532	10.0162299	10.5712831	26		
35	4.4917101	9.9837348	9.4454352	10.5545643	10.0162552	10.5708295	25		
36	4.4962285	9.9836995	9.4459232	10.5540768	10.0162801	10.5703772	24		
37	4.500750	9.9836643	9.4464107	10.5535893	10.0163357	10.5699250	23		
38	4.505267	9.9836292	9.4468978	10.5531022	10.0163761	10.5694733	22		
39	4.509779	9.9835936	9.4473843	10.5526167	10.0164161	10.5690211	21		
40	4.514286	9.9835582	9.4478704	10.5521296	10.0164511	10.5685684	20		
41	4.518788	9.9835227	9.4483561	10.5516439	10.0164873	10.5681214	19		
42	4.523285	9.9834872	9.4488413	10.5511587	10.0165248	10.5676715	18		
43	4.527777	9.9834517	9.4493260	10.5506734	10.0165633	10.5672237	17		
44	4.532261	9.9834161	9.4498102	10.5501898	10.0166032	10.5667776	16		
45	4.536746	9.9833805	9.4502940	10.5497066	10.0166435	10.5663254	15		
46	4.541223	9.9833449	9.4507774	10.5492265	10.0166851	10.5658777	14		
47	4.545694	9.9833092	9.4512602	10.5487395	10.0167285	10.5654306	13		
48	4.550161	9.9832735	9.4517437	10.5482537	10.0167725	10.5649839	12		
49	4.554623	9.9832377	9.4522245	10.5477754	10.0168176	10.5645377	11		
50	4.559080	9.9832019	9.452701	10.5472939	10.0168631	10.5640920	10		
51	4.563532	9.9831661	9.4531762	10.5468112	10.0169099	10.5636465	9		
52	4.567980	9.9831302	9.4536503	10.5463302	10.0169583	10.5632020	8		
53	4.572422	9.9830943	9.4541242	10.5458511	10.0169975	10.5627578	7		
54	4.576859	9.9830583	9.4545978	10.5453724	10.0170371	10.5623141	6		
55	4.581292	9.9830223	9.4550705	10.5448933	10.0170777	10.5618705	5		
56	4.585719	9.9829862	9.4555437	10.5444143	10.0170738	10.5614281	4		
57	4.590142	9.9829501	9.4560164	10.5439353	10.0170749	10.5609856	3		
58	4.594560	9.9829140	9.4564892	10.5434563	10.0170760	10.5605430	2		
59	4.598973	9.9828779	9.4569619	10.5429775	10.0170771	10.5601007	1		
60	4.603381	9.9828416	9.4574361	10.5424986	10.0170785	10.5596619	0		
	<i>L. Co-Sine.</i>	<i>L. Sine.</i>	<i>L. Co-Tang.</i>	<i>L. Tangent.</i>	<i>L. Co-Secant.</i>	<i>L. Secant.</i>			<i>M</i>

[illegible]



A TABLE of Natural and

16 DEGREES.									
M	N. Sine.	N. Co-Sine.	N. Tangent.	N. Co-Tangent.	N. Secant.	N. Co-Secant.			
0	2756374	9612617	2587454	3477444	10462994	38279553	60		
1	2759170	9611318	2592522	3478356	10463863	38242788	59		
2	2761965	9610112	2597571	3479274	10464732	38206101	58		
3	2764761	9608943	2602593	3480192	10465602	38169490	57		
4	2767556	9607813	2607593	3481116	10466473	38132957	56		
5	2770352	9606683	2612574	3482046	10467346	38096501	55		
6	2773147	9605542	2617532	3482981	10468219	38060121	54		
7	2775942	9604395	2622462	3483922	10469094	38023813	53		
8	2778737	9603247	2627365	3484869	10469969	38087586	52		
9	2781532	9602098	2632243	3485821	10470845	38051332	51		
10	2784327	9600948	2637096	3486779	10471722	38015063	50		
11	2787122	9599797	2641924	3487743	10472601	38078762	49		
12	2789917	9598645	2646728	3488712	10473481	38042437	48		
13	2792712	9597492	2651507	3489687	10474362	38006086	47		
14	2795507	9596338	2656262	3490667	10475243	38069710	46		
15	2798302	9595183	2661003	3491653	10476126	38033308	45		
16	2801097	9594028	2665720	3492644	10477009	38096841	44		
17	2803892	9592873	2670413	3493640	10477894	38060398	43		
18	2806687	9591718	2675182	3494642	10478780	38023942	42		
19	2809482	9590563	2679927	3495649	10479667	38087490	41		
20	2812277	9589408	2684648	3496662	10480554	38051010	40		
21	2815072	9588253	2689345	3497680	10481443	38014508	39		
22	2817867	9587098	2694018	3498703	10482333	38078026	38		
23	2820662	9585943	2698667	3499731	10483224	38041517	37		
24	2823457	9584788	2703292	3500764	10484116	38005030	36		
25	2826252	9583633	2707893	3501803	10485009	38068518	35		
26	2829047	9582478	2712470	3502848	10485904	38032024	34		
27	2831842	9581323	2717023	3503899	10486800	38095508	33		
28	2834637	9580168	2721552	3504956	10487697	38058962	32		
29	2837432	9579013	2726057	3506019	10488594	38022437	31		
30	2840227	9577858	2730538	3507088	10489492	38085930	30		
	N. Sine.	N. Sine.	N. Tangent.	N. Tangent.	N. Secant.	N. Secant.			

75 DEGREES.

[illegible]

16 DEGREES.							
M	<i>L. Sine.</i>	<i>L. Co-Sine.</i>	<i>L. Tangent.</i>	<i>L. Co-Tangent.</i>	<i>L. Secant.</i>	<i>L. Co-Secant.</i>	
0	9.4303381	9.9828416	9.4574964	10.5425036	10.6171634	10.5555619	60
1	9.4407784	9.9828054	9.4579730	10.5420270	10.6171945	10.5555216	59
2	9.4412162	9.9827691	9.4584491	10.5415509	10.6172259	10.5554818	58
3	9.4416576	9.9827327	9.4589248	10.5410752	10.6172572	10.5554421	57
4	9.4420965	9.9826964	9.4594001	10.5405999	10.6172886	10.5554023	56
5	9.4425369	9.9826600	9.4598749	10.5401251	10.6173200	10.5553631	55
6	9.4429728	9.9826236	9.4603492	10.5396508	10.6173515	10.5553242	54
7	9.4434103	9.9825871	9.4608232	10.5391768	10.6173829	10.5552857	53
8	9.4438472	9.9825506	9.4612967	10.5387033	10.6174144	10.5552472	52
9	9.4442837	9.9825140	9.4617697	10.5382303	10.6174458	10.5552087	51
10	9.4447197	9.9824774	9.4622423	10.5377577	10.6174772	10.5551701	50
11	9.4451553	9.9824408	9.4627145	10.5372855	10.6175086	10.5551316	49
12	9.4455904	9.9824043	9.4631863	10.5368137	10.6175399	10.5550931	48
13	9.4460255	9.9823677	9.4636576	10.5363424	10.6175712	10.5550547	47
14	9.4464591	9.9823310	9.4641285	10.5358715	10.6176024	10.5550162	46
15	9.4468927	9.9822943	9.4645990	10.5354010	10.6176336	10.5549778	45
16	9.4473259	9.9822576	9.4650690	10.5349310	10.6176648	10.5549394	44
17	9.4477596	9.9822209	9.4655385	10.5344614	10.6176959	10.5549010	43
18	9.4481902	9.9821841	9.4660078	10.5339922	10.6177271	10.5548625	42
19	9.4486227	9.9821472	9.4664765	10.5335235	10.6177583	10.5548241	41
20	9.4490540	9.9821103	9.4669445	10.5330552	10.6177895	10.5547856	40
21	9.4494849	9.9820734	9.4674127	10.5325872	10.6178207	10.5547472	39
22	9.4499153	9.9820365	9.4678802	10.5321195	10.6178519	10.5547087	38
23	9.4503452	9.9819997	9.4683473	10.5316523	10.6178831	10.5546703	37
24	9.4507747	9.9819628	9.4688139	10.5311851	10.6179143	10.5546318	36
25	9.4512037	9.9819258	9.4692801	10.5307179	10.6179455	10.5545934	35
26	9.4516321	9.9818889	9.4697459	10.5302511	10.6179767	10.5545549	34
27	9.4520607	9.9818520	9.4702112	10.5297838	10.6180079	10.5545165	33
28	9.4524899	9.9818151	9.4706762	10.5293169	10.6180391	10.5544781	32
29	9.4529185	9.9817784	9.4711407	10.5288503	10.6180703	10.5544396	31
30	9.4533418	9.9817417	9.4716048	10.5283832	10.6181015	10.5544012	30
	<i>L. Co-Sine.</i>	<i>L. Sine.</i>	<i>L. Co-Tang.</i>	<i>L. Tangent.</i>	<i>L. Co-Secant.</i>	<i>L. Secant.</i>	<i>M</i>

73 DEGREES.

[illegible]



## A TABLE of Natural and

16 DEGREES.

M	N. Sine.	N. Co-Sine.	N. Tangent.	N. Co-Tang.	N. Secant.	N. Co-Secant.	
30	2540153	9589197	2962125	33759434	10429489	35202365	30
31	2842942	9587370	2965299	33723408	10430388	35174824	29
32	2845721	9586543	2968464	33687453	10431289	35146354	28
33	2848500	9585715	2971630	33651503	10432190	35117894	27
34	2851279	9584886	2974796	33615553	10433092	35089434	26
35	2854058	9584056	2977962	33579603	10433995	35060974	25
36	2856837	9583225	2981129	33543653	10434900	35032514	24
37	2859616	9582394	2984297	33507703	10435805	34996054	23
38	2862395	9581562	2987465	33471753	10436712	34959594	22
39	2865174	9580729	2990633	33435803	10437619	34923134	21
40	2867953	9579897	2993803	33400003	10438525	34886674	20
41	2870732	9579065	2996973	33364203	10439432	34850214	19
42	2873511	9578232	3000144	33328403	10440348	34813754	18
43	2876290	9577400	3003315	33292603	10441259	34777294	17
44	2879069	9576568	3006486	33256803	10442172	34740834	16
45	2881848	9575735	3009657	33221003	10443086	34704374	15
46	2884627	9574903	3012828	33185203	10444001	34667914	14
47	2887406	9574070	3015999	33149403	10444917	34631454	13
48	2890185	9573237	3019170	33113603	10445833	34594994	12
49	2892964	9572405	3022341	33077803	10446751	34558534	11
50	2895743	9571572	3025512	33042003	10447670	34522074	10
51	2898522	9570740	3028683	33006203	10448590	34485614	9
52	2901301	9569907	3031854	32970403	10449511	34449154	8
53	2904080	9569075	3035025	32934603	10450433	34412694	7
54	2906859	9568242	3038196	32898803	10451357	34376234	6
55	2909638	9567410	3041410	32863003	10452281	34339774	5
56	2912417	9566577	3044625	32827203	10453206	34303314	4
57	2915196	9565745	3047840	32791403	10454132	34266854	3
58	2917975	9564912	3051055	32755603	10455056	34230394	2
59	2920754	9564080	3054270	32719803	10455988	34193934	1
60	2923533	9563247	3057485	32684003	10456915	34157474	0
N. Co-Sine. N. Sine. N. Co-Tang. N. Tangent. N. Co-Secant. N. Secant. M							

73 DEGREES.

Latitude 33 Deg. 00 Min. North Declination.																									
	0	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20	21	22	23	24
	b. m.	b. m.	b. m.	b. m.	b. m.	b. m.	b. m.	b. m.	b. m.	b. m.	b. m.	b. m.	b. m.	b. m.	b. m.	b. m.	b. m.	b. m.	b. m.	b. m.	b. m.	b. m.	b. m.	b. m.	b. m.
1	0-25	1-0-24	1-0-23	1-0-22	1-0-21	1-0-20	1-0-19	1-0-18	1-0-17	1-0-16	1-0-15	1-0-14	1-0-13	1-0-12	1-0-11	1-0-10	1-0-09	1-0-08	1-0-07	1-0-06	1-0-05	1-0-04	1-0-03	1-0-02	1-0-01
2	0-51	2-0-49	2-0-48	2-0-47	2-0-46	2-0-45	2-0-44	2-0-43	2-0-42	2-0-41	2-0-40	2-0-39	2-0-38	2-0-37	2-0-36	2-0-35	2-0-34	2-0-33	2-0-32	2-0-31	2-0-30	2-0-29	2-0-28	2-0-27	2-0-26
3	1-26	3-1-26	3-1-25	3-1-24	3-1-23	3-1-22	3-1-21	3-1-20	3-1-19	3-1-18	3-1-17	3-1-16	3-1-15	3-1-14	3-1-13	3-1-12	3-1-11	3-1-10	3-1-09	3-1-08	3-1-07	3-1-06	3-1-05	3-1-04	3-1-03
4	1-54	4-1-54	4-1-53	4-1-52	4-1-51	4-1-50	4-1-49	4-1-48	4-1-47	4-1-46	4-1-45	4-1-44	4-1-43	4-1-42	4-1-41	4-1-40	4-1-39	4-1-38	4-1-37	4-1-36	4-1-35	4-1-34	4-1-33	4-1-32	4-1-31
5	2-37	5-2-37	5-2-36	5-2-35	5-2-34	5-2-33	5-2-32	5-2-31	5-2-30	5-2-29	5-2-28	5-2-27	5-2-26	5-2-25	5-2-24	5-2-23	5-2-22	5-2-21	5-2-20	5-2-19	5-2-18	5-2-17	5-2-16	5-2-15	5-2-14
6	3-31	6-3-31	6-3-30	6-3-29	6-3-28	6-3-27	6-3-26	6-3-25	6-3-24	6-3-23	6-3-22	6-3-21	6-3-20	6-3-19	6-3-18	6-3-17	6-3-16	6-3-15	6-3-14	6-3-13	6-3-12	6-3-11	6-3-10	6-3-09	6-3-08
7	4-43	7-4-43	7-4-42	7-4-41	7-4-40	7-4-39	7-4-38	7-4-37	7-4-36	7-4-35	7-4-34	7-4-33	7-4-32	7-4-31	7-4-30	7-4-29	7-4-28	7-4-27	7-4-26	7-4-25	7-4-24	7-4-23	7-4-22	7-4-21	7-4-20
WE	6-00	8-6-00	8-5-59	8-5-58	8-5-57	8-5-56	8-5-55	8-5-54	8-5-53	8-5-52	8-5-51	8-5-50	8-5-49	8-5-48	8-5-47	8-5-46	8-5-45	8-5-44	8-5-43	8-5-42	8-5-41	8-5-40	8-5-39	8-5-38	8-5-37
1																									
2																									



17 DEGREES.										
M	N. Sine.	N. Co-Sine.	N. Tangent.	N. Co-Tang.	N. Secant.	N. Co-Secant.				
0	2923717	9563048	3057307	32725526	10456918	34203036	60			
1	2926439	9562197	3060488	32674529	10457848	34170526	59			
2	2929280	9561345	3063669	32624596	10458780	34138080	58			
3	2932061	9560492	3066851	32574728	10459712	34105699	57			
4	2934842	9559639	3070034	32524924	10460646	34073382	56			
5	2937623	9558785	3073215	32475184	10461581	34041130	55			
6	2940403	9557930	3076402	32425508	10462516	34008941	54			
7	2943183	9557074	3079586	32375895	10463453	33976816	53			
8	2945963	9556217	3082771	32326346	10464394	33944754	52			
9	2948743	9555362	3085957	32276860	10465330	33912755	51			
10	2951522	9554506	3089143	32227438	10466270	33880820	50			
11	2954301	9553649	3092330	32178079	10467211	33848948	49			
12	2957080	9552793	3095517	32128783	10468153	33817138	48			
13	2959859	9551936	3098705	32079545	10469096	33785391	47			
14	2962638	9551079	3101893	32030368	10470040	33753707	46			
15	2965416	9550222	3105082	31981253	10470986	33722084	45			
16	2968194	9549365	3108272	31932199	10471932	33690524	44			
17	2970971	9548507	3111462	31883205	10472879	33659028	43			
18	2973749	9547650	3114653	31834264	10473825	33627589	42			
19	2976526	9546792	3117843	31785384	10474772	33596214	41			
20	2979303	9545935	3121033	31736568	10475728	33564900	40			
21	2982079	9545078	3124223	31687817	10476687	33533647	39			
22	2984856	9544221	3127412	31639131	10477647	33502455	38			
23	2987632	9543364	3130601	31590509	10478608	33471324	37			
24	2990408	9542507	3133791	31541952	10479569	33440254	36			
25	2993184	9541650	3136981	31493460	10480530	33409244	35			
26	2995959	9540793	3140171	31445032	10481493	33378294	34			
27	2998734	9539936	3143361	31396568	10482457	33347405	33			
28	3001509	9539079	3146551	31348169	10483422	33316575	32			
29	3004284	9538222	3149741	31299835	10484388	33285805	31			
30	3007059	9537365	3152931	31251566	10485354	33255095	30			
N. Co-Sine.		N. Sine.	N. Tangent.	N. Co-Tang.	N. Co-Secant.	N. Secant.	M			

72 DEGREES.

Latitude 34 Deg. 00 Min. North Declination.																										
0	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20	21	22	23	24	25	
d.	d.	d.	d.	d.	d.	d.	d.	d.	d.	d.	d.	d.	d.	d.	d.	d.	d.	d.	d.	d.	d.	d.	d.	d.	d.	d.
12.0	12.1	12.2	12.3	12.4	12.5	12.6	12.7	12.8	12.9	13.0	13.1	13.2	13.3	13.4	13.5	13.6	13.7	13.8	13.9	14.0	14.1	14.2	14.3	14.4	14.5	14.6
12.0	12.1	12.2	12.3	12.4	12.5	12.6	12.7	12.8	12.9	13.0	13.1	13.2	13.3	13.4	13.5	13.6	13.7	13.8	13.9	14.0	14.1	14.2	14.3	14.4	14.5	14.6
12.0	12.1	12.2	12.3	12.4	12.5	12.6	12.7	12.8	12.9	13.0	13.1	13.2	13.3	13.4	13.5	13.6	13.7	13.8	13.9	14.0	14.1	14.2	14.3	14.4	14.5	14.6
12.0	12.1	12.2	12.3	12.4	12.5	12.6	12.7	12.8	12.9	13.0	13.1	13.2	13.3	13.4	13.5	13.6	13.7	13.8	13.9	14.0	14.1	14.2	14.3	14.4	14.5	14.6
12.0	12.1	12.2	12.3	12.4	12.5	12.6	12.7	12.8	12.9	13.0	13.1	13.2	13.3	13.4	13.5	13.6	13.7	13.8	13.9	14.0	14.1	14.2	14.3	14.4	14.5	14.6
12.0	12.1	12.2	12.3	12.4	12.5	12.6	12.7	12.8	12.9	13.0	13.1	13.2	13.3	13.4	13.5	13.6	13.7	13.8	13.9	14.0	14.1	14.2	14.3	14.4	14.5	14.6
12.0	12.1	12.2	12.3	12.4	12.5	12.6	12.7	12.8	12.9	13.0	13.1	13.2	13.3	13.4	13.5	13.6	13.7	13.8	13.9	14.0	14.1	14.2	14.3	14.4	14.5	14.6
12.0	12.1	12.2	12.3	12.4	12.5	12.6	12.7	12.8	12.9	13.0	13.1	13.2	13.3	13.4	13.5	13.6	13.7	13.8	13.9	14.0	14.1	14.2	14.3	14.4	14.5	14.6
12.0	12.1	12.2	12.3	12.4	12.5	12.6	12.7	12.8	12.9	13.0	13.1	13.2	13.3	13.4	13.5	13.6	13.7	13.8	13.9	14.0	14.1	14.2	14.3	14.4	14.5	14.6
12.0	12.1	12.2	12.3	12.4	12.5	12.6	12.7	12.8	12.9	13.0	13.1	13.2	13.3	13.4	13.5	13.6	13.7	13.8	13.9	14.0	14.1	14.2	14.3	14.4	14.5	14.6
12.0	12.1	12.2	12.3	12.4	12.5	12.6	12.7	12.8	12.9	13.0	13.1	13.2	13.3	13.4	13.5	13.6	13.7	13.8	13.9	14.0	14.1	14.2	14.3	14.4	14.5	14.6
12.0	12.1	12.2	12.3	12.4	12.5	12.6	12.7	12.8	12.9	13.0	13.1	13.2	13.3	13.4	13.5	13.6	13.7	13.8	13.9	14.0	14.1	14.2	14.3	14.4	14.5	14.6
12.0	12.1	12.2	12.3	12.4	12.5	12.6	12.7	12.8	12.9	13.0	13.1	13.2	13.3	13.4	13.5	13.6	13.7	13.8	13.9	14.0	14.1	14.2	14.3	14.4	14.5	14.6
12.0	12.1	12.2	12.3	12.4	12.5	12.6	12.7	12.8	12.9	13.0	13.1	13.2	13.3	13.4	13.5	13.6	13.7	13.8	13.9	14.0	14.1	14.2	14.3	14.4	14.5	14.6
12.0	12.1	12.2	12.3	12.4	12.5	12.6	12.7	12.8	12.9	13.0	13.1	13.2	13.3	13.4	13.5	13.6	13.7	13.8	13.9	14.0	14.1	14.2	14.3	14.4	14.5	14.6
12.0	12.1	12.2	12.3	12.4	12.5	12.6	12.7	12.8	12.9	13.0	13.1	13.2	13.3	13.4	13.5	13.6	13.7	13.8	13.9	14.0	14.1	14.2	14.3	14.4	14.5	14.6
12.0	12.1	12.2	12.3	12.4	12.5	12.6	12.7	12.8	12.9	13.0	13.1	13.2	13.3	13.4	13.5	13.6	13.7	13.8	13.9	14.0	14.1	14.2	14.3	14.4	14.5	14.6
12.0	12.1	12.2	12.3	12.4	12.5	12.6	12.7	12.8	12.9	13.0	13.1	13.2	13.3	13.4	13.5	13.6	13.7	13.8	13.9	14.0	14.1	14.2	14.3	14.4	14.5	14.6
12.0	12.1	12.2	12.3	12.4	12.5	12.6	12.7	12.8	12.9	13.0	13.1	13.2	13.3	13.4	13.5	13.6	13.7	13.8	13.9	14.0	14.1	14.2	14.3	14.4	14.5	14.6
12.0	12.1	12.2	12.3	12.4	12.5	12.6	12.7	12.8	12.9	13.0	13.1	13.2	13.3	13.4	13.5	13.6	13.7	13.8	13.9	14.0	14.1	14.2	14.3	14.4	14.5	14.6
12.0	12.1	12.2	12.3	12.4	12.5	12.6	12.7	12.8	12.9	13.0	13.1	13.2	13.3	13.4	13.5	13.6	13.7	13.8	13.9	14.0	14.1	14.2	14.3	14.4	14.5	14.6
12.0	12.1	12.2	12.3	12.4	12.5	12.6	12.7	12.8	12.9	13.0	13.1	13.2	13.3	13.4	13.5	13.6	13.7	13.8	13.9	14.0	14.1	14.2	14.3	14.4	14.5	14.6
12.0	12.1	12.2	12.3	12.4	12.5	12.6	12.7	12.8	12.9	13.0	13.1	13.2	13.3	13.4	13.5	13.6	13.7	13.8	13.9	14.0	14.1	14.2	14.3	14.4	14.5	14.6
12.0	12.1	12.2	12.3	12.4	12.5	12.6	12.7	12.8	12.9	13.0	13.1	13.2	13.3	13.4	13.5	13.6	13.7	13.8	13.9	14.0	14.1	14.2	14.3	14.4	14.5	14.6
12.0	12.1	12.2	12.3	12.4	12.5	12.6	12.7	12.8	12.9	13.0	13.1	13.2	13.3	13.4	13.5	13.6	13.7	13.8	13.9	14.0	14.1	14.2	14.3	14.4	14.5	14.6
12.0	12.1	12.2	12.3	12.4	12.5	12.6	12.7	12.8	12.9	13.0	13.1	13.2	13.3	13.4	13.5	13.6	13.7	13.8	13.9	14.0	14.1	14.2	14.3	14.4	14.5	14.6
12.0	12.1	12.2	12.3	12.4	12.5	12.6	12.7	12.8	12.9	13.0	13.1	13.2	13.3	13.4	13.5	13.6	13.7	13.8	13.9	14.0	14.1	14.2	14.3	14.4	14.5	14.6
12.0	12.1	12.2	12.3	12.4	12.5	12.6	12.7	12.8	12.9	13.0	13.1	13.2	13.3	13.4	13.5	13.6	13.7	13.8	13.9	14.0	14.1	14.2	14.3	14.4	14.5	14.6
12.0	12.1	12.2	12.3	12.4	12.5	12.6	12.7	12.8	12.9	13.0	13.1	13.2	13.3	13.4	13.5	13.6	13.7	13.8	13.9	14.0	14.1	14.2	14.3	14.4	14.5	14.6
12.0	12.1	12.2	12.3	12.4	12.5	12.6	12.7	12.8	12.9	13.0	13.1	13.2	13.3	13.4	13.5	13.6	13.7	13.8	13.9	14.0	14.1	14.2	14.3	14.4	14.5	14.6
12.0	12.1	12.2	12.3	12.4	12.5	12.6	12.7	12.8	12.9	13.0	13.1	13.2	13.3	13.4	13.5	13.6	13.7	13.8	13.9	14.0	14.1	14.2	14.3	14.4	14.5	14.6
12.0	12.1	12.2	12.3	12.4	12.5	12.6	12.7	12.8	12.9	13.0	13.1	13.2	13.3	13.4	13.5	13.6	13.7	13.8	13.9	14.0	14.1	14.2	14.3	14.4	14.5	14.6
12.0	12.1	12.2	12.3	12.4	12.5	12.6	12.7	12.8	12.9	13.0	13.1	13.2	13.3	13.4	13.5	13.6	13.7	13.8	13.9	14.0	14.1	14.2	14.3	14.4	14.5	14.6
12.0	12.1	12.2	12.3	12.4	12.5	12.6	12.7	12.8	12.9	13.0	13.1	13.2	13.3	13.4	13.5	13.6	13.7	13.8	13.9	14.0	14.1	14.2	14.3	14.4	14.5	14.6
12.0	12.1	12.2	12.3	12.4	12.5	12.6	12.7	12.8	12.9	13.0	13.1	13.2	13.3	13.4	13.5	13.6	13.7	13.8	13.9	14.0	14.1	14.2	14.3	14.4	14.5	14.6
12.0	12.1	12.2	12.3	12.4	12.5	12.6	12.7	12.8	12.9	13.0	13.1	13.2	13.3	13.4	13.5	13.6	13.7	13.8	13.9	14.0	14.1	14.2	14.3	14.4	14.5	14.6
12.0	12.1	12.2	12.3	12.4	12.5	12.6	12.7	12.8	12.9	13.0	13.1	13.2	13.3	13.4	13.5	13.6	13.7	13.8	13.9	14.0	14.1	14.2	14.3	14.4	14.5	14.6
12.0	12.1	12.2	12.3	12.4	12.5	12.6	12.7	12.8	12.9	13.0	13.1	13.2	13.3	13.4	13.5	13.6	13.7	13.8	13.9	14.0	14.1	14.2	14.3	14.4	14.5	14.6
12.0	12.1	12.2	12.3	12.4	12.5	12.6	12.7	12.8	12.9	13.0	13.1	13.2	13.3	13.4	13.5	13.6	13.7	13.8	13.9	14.0	14.1	14.2	14.3	14.4	14.5	14.6
12.0	12.1	12.2	12.3	12.4	12.5	12.6	12.7	12.8	12.9	13.0	13.1	13.2	13.3	13.4	13.5	13.6	13.7	13.8	13.9	14.0	14.1	14.2	14.3	14.4	14.5	14.6
12.0	12.1	12.2	12.3	12.4	12.5	12.6	12.7	12.8	12.9	13.0	13.1	13.2	13.3	13.4	13.5	13.6	13.7	13.8	13.9	14.0	14.1	14.2	14.3	14.4	14.5	14.6
12.0	12.1	12.2	12.3	12.4	12.5	12.6	12.7	12.8	12.9	13.0	13.1	13.2	13.3	13.4	13.5	13.6	13.7	13.8	13.9	14.0	14.1	14.2	14.3	14.4	14.5	14.6
12.0	12.1	12.2	12.3	12.4	12.5	12.6	12.7	12.8	12.9	13.0	13.1	13.2	13.3	13.4	13.5	13.6	13.7	13.8	13.9	14.0	14.1	14.2	14.3	14.4	14.5	14.6
12.0	12.1	12.2	12.3	12.4	12.5	12.6	12.7	12.8	12.9	13.0	13.1	13.2	13.3	13.4	13.5	13.6	13.7	13.8	13.9	14.0	14.1	14.2	14.3	14.4	14.5	14.6
12.0	12.1	12.2	12.3	12.4	12.5	12.6	12.7	12.8	12.9	13.0	13.1	13.2	13.3	13.4	13.5	13.6	13.7	13.8	13.9	14.0	14.1	14.2	14.3	14.4	14.5	14.6
12.0	12.1	12.2	12.3	12.4	12.5	12.6	12.7	12.8	12.9	13.0	13.1	13.2	13.3	13.4	13.5	13.6	13.7	13.8	13.9	14.0	14.1	14.2	14.3	14.4	14.5	14.6
12.0	12.1	12.2	12.3	12.4	12.5	12.6	12.7	12.8	12.9	13.0	13.1	13.2	13.3	13.4	13.5	13.6	13.7	13.8	13.9	14.0	14.1	14.2	14.3	14.4	14.5	14.6
12.0	12.1	12.2	12.3	12.4	12.5	12.6	12.7	12.8	12.9	13.0	13.1	13.2	13.3	13.4	13.5	13.6	13.7	13.8	13.9	14.0	14.1	14.2	14.3	14.4	14.5	14.6
12.0	12.1	12.2	12.3	12.4	12.5	12.6	12.7	12.8	12.9	13.0	13.1	13.2	13.3	13.4	13.5	13.6	13.7	13.8	13.9							



A TABLE of Natural and

17 D E G R E E S.									
M	N. Sine.	N. Co-Sine.	N. Tangent.	N. Co-Tang.	N. Secant.	N. Co-Secant.			
30	3007058	9537169	3124258	31715948	10485291	33255095	30		
31	3009832	9536294	3125615	31683808	10482643	33224444	29		
32	3012606	9535418	3126385	31651728	10487217	33193853	28		
33	3015381	9534541	3127255	31619706	10488181	33163320	27		
34	3018163	9533664	3128235	31587744	10489116	33132842	26		
35	3020926	9532786	3129316	31555840	10490113	33102437	25		
36	3023699	9531907	3130237	31523994	10491080	33072076	24		
37	3026471	9531027	3131258	31492277	10492049	33041778	23		
38	3029244	9530146	3132351	31460648	10493019	33011539	22		
39	3032016	9529264	3133474	31428807	10493988	32981357	21		
40	3034788	9528382	3134695	31397194	10494961	32951234	20		
41	3037559	9527501	3135922	31365639	10495934	32921168	19		
42	3040331	9526619	3137207	31334141	10496908	32891166	18		
43	3043102	9525730	3138461	31302701	10497883	32861209	17		
44	3045872	9524844	3139781	31271317	10498859	32831316	16		
45	3048643	9523958	3141025	31239991	10499836	32801479	15		
46	3051413	9523071	3142232	31208722	10500815	32771700	14		
47	3054183	9522183	3143447	31177509	10501794	32741977	13		
48	3056953	9521294	3144649	31146353	10502774	32712311	12		
49	3059723	9520404	3145858	31115254	10503756	32682702	11		
50	3062492	9519514	3147067	31084210	10504738	32653149	10		
51	3065261	9518623	3148277	31053223	10505722	32623652	9		
52	3068029	9517731	3149485	31022291	10506706	32594211	8		
53	3070798	9516838	3150690	30991416	10507692	32564825	7		
54	3073566	9515944	3151891	30960556	10508679	32535496	6		
55	3076334	9515049	3153121	30929831	10509667	32506222	5		
56	3079102	9514154	3154353	30899122	10510656	32477003	4		
57	3081869	9513258	3155595	30868468	10511646	32447840	3		
58	3084636	9512361	3156856	30837869	10512637	32418732	2		
59	3087403	9511463	3158119	30807325	10513629	32389678	1		
60	3090170	9510565	3159297	30776835	10514622	32360680	0		
N. Co-Sine.	N. Sine.	N. Co-Tang.	N. Tangent.	N. Co-Secant.	N. Secant.				

17 DEGREES.							
M	<i>L. Sine.</i>	<i>L. Co-Sine.</i>	<i>L. Tangent.</i>	<i>L. Co-Tang.</i>	<i>L. Secant.</i>	<i>L. Co-Secant.</i>	
30	9-4781418	9-9794195	9-4987723	10-5012777	10-0205835	10-5215582	30
31	9-4785423	9-9793796	9-4991626	10-5008374	10-0206204	10-5214577	29
32	9-4789423	9-9793398	9-4995606	10-5003974	10-0206582	10-5213577	28
33	9-4793420	9-9792998	9-5000422	10-4999573	10-0207002	10-5212580	27
34	9-4797412	9-9792598	9-5005314	10-4995186	10-0207402	10-5212588	26
35	9-4801401	9-9792198	9-5009203	10-4990795	10-0207802	10-5212599	25
36	9-4805385	9-9791798	9-5013158	10-4986412	10-0208202	10-5212605	24
37	9-4809366	9-9791397	9-5017569	10-4982031	10-0208603	10-5212613	23
38	9-4813342	9-9790996	9-5022347	10-4977653	10-0209004	10-5212625	22
39	9-4817315	9-9790594	9-5026721	10-4973279	10-0209406	10-5212638	21
40	9-4821283	9-9790192	9-5031692	10-4968903	10-0209808	10-5212651	20
41	9-4825248	9-9789789	9-5035459	10-4964541	10-0210211	10-5212752	19
42	9-4829209	9-9789386	9-5039522	10-4960173	10-0210614	10-5210792	18
43	9-4833165	9-9788983	9-5044182	10-4955813	10-0211017	10-5216653	17
44	9-4837117	9-9788579	9-5048838	10-4951462	10-0211421	10-5216285	16
45	9-4841066	9-9788175	9-5052891	10-4947109	10-0211825	10-5215893	15
46	9-4845010	9-9787770	9-5057240	10-4942760	10-0212230	10-5215499	14
47	9-4848951	9-9787365	9-5061856	10-4938414	10-0212635	10-5215109	13
48	9-4852888	9-9786960	9-5066528	10-4934072	10-0213040	10-5214712	12
49	9-4856820	9-9786554	9-5070267	10-4929733	10-0213446	10-5214318	11
50	9-4860749	9-9786148	9-5074002	10-4925393	10-0213852	10-5213925	10
51	9-4864674	9-9785741	9-5077933	10-4921067	10-0214259	10-5213532	9
52	9-4868595	9-9785334	9-5082661	10-4916739	10-0214666	10-5213143	8
53	9-4872512	9-9784927	9-5087286	10-4912414	10-0215073	10-5212748	7
54	9-4876426	9-9784519	9-5091907	10-4908093	10-0215481	10-5212354	6
55	9-4880335	9-9784111	9-5096224	10-4903776	10-0215889	10-5211965	5
56	9-4884240	9-9783702	9-5100539	10-4899461	10-0216293	10-5211576	4
57	9-4888142	9-9783293	9-5104849	10-4895151	10-0216707	10-5211185	3
58	9-4892040	9-9782883	9-5109156	10-4890844	10-0217117	10-5210796	2
59	9-4895934	9-9782474	9-5113460	10-4886540	10-0217526	10-5210406	1
60	9-4899824	9-9782063	9-5117760	10-4882240	10-0217937	10-5210016	0
	<i>L. Co-Sine.</i>	<i>L. Sine.</i>	<i>L. Co-Tang.</i>	<i>L. Tangent.</i>	<i>L. Co-Secant.</i>	<i>L. Secant.</i>	M

[illegible]

Latitude 35 Deg. 00 Min.      South Declination.																	
	0	d. 2	d. 4	d. 6	d. 8	d. 10	d. 12	d. 14	d. 16	d. 18	d. 20	d. 22	d. 24	d. 26	d. 28	d. 30	
	b. m.	m. b. m.	m. b. m.	m. b. m.	m. b. m.	m. b. m.	m. b. m.	m. b. m.	m. b. m.	m. b. m.	m. b. m.	m. b. m.	m. b. m.	m. b. m.	m. b. m.	m. b. m.	
5	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	
1	0.26	1.0.27	1.0.28	1.0.29	2.0.31	2.0.33	1.0.34	1.0.35	1.0.36	2.0.35	2.0.40	1.0.41	1.0.42	1.0.43	1.0.44	1.0.45	
2	0.53	2.0.55	3.0.58	3.1.01	3.1.04	3.1.07	2.1.09	3.1.12	3.1.15	3.1.18	3.1.21	2.1.24	3.1.27	3.1.29	3.1.31	3.1.33	
3	1.24	4.1.28	4.1.32	4.1.36	4.1.40	5.1.45	4.1.49	4.1.53	4.1.57	5.2.02	5.2.07	5.2.12	5.2.16	5.2.19	5.2.22	5.2.25	
4	1.59	5.2.04	6.2.10	6.2.16	6.2.22	6.2.28	6.2.34	6.2.40	6.2.46	6.2.52	7.2.59	7.3.06	7.3.11	7.3.15	7.3.18	7.3.21	
5	2.43	7.2.50	7.2.57	7.3.04	8.3.12	8.3.20	8.3.28	8.3.36	8.3.44	9.3.53	9.4.02	9.4.11	9.4.19	9.4.27	9.4.35	9.4.43	
6	3.37	9.3.46	9.3.55	9.4.04	10.4.14	10.4.24	10.4.34	10.4.44	10.4.54	11.4.04	11.4.14	11.4.24	11.4.34	11.4.44	11.4.54	11.5.04	
7	4.43	11.4.54	11.5.05	11.5.16	12.5.27	12.5.38	12.5.49	12.5.59	13.5.10	13.5.21	13.5.31	13.5.42	13.5.52	14.5.03	14.5.13	14.5.23	



## A TABLE of Natural and

18 DEGREES.

M	N. Sine.	N. Co-Sine.	N. Tangent.	N. Co-Tangent.	N. Secant.	N. Co-Secant.
0	3090170	9513565	3242197	3277653	10514622	32360650
1	3090236	9513585	3242415	3277650	10515617	32331736
2	3090302	9513605	3242630	3277647	10516612	32302845
3	3090368	9513625	3242845	3277643	10517608	32273953
4	3101234	9513645	3243060	3277640	10518604	32245061
5	3103999	9513665	3243275	3277637	10519600	32216169
6	3106764	9513685	3243490	3277634	10520596	32187277
7	3109529	9513705	3243705	3277631	10521592	32158385
8	3112294	9513725	3243920	3277628	10522588	32129493
9	3115059	9513745	3244135	3277625	10523584	32100601
10	3117824	9513765	3244350	3277622	10524580	32071709
11	3120589	9513785	3244565	3277619	10525576	32042817
12	3123354	9513805	3244780	3277616	10526572	32013925
13	3126119	9513825	3244995	3277613	10527568	31985033
14	3128884	9513845	3245210	3277610	10528564	31956141
15	3131649	9513865	3245425	3277607	10529560	31927249
16	3134414	9513885	3245640	3277604	10530556	31898357
17	3137179	9513905	3245855	3277601	10531552	31869465
18	3139944	9513925	3246070	3277598	10532548	31840573
19	3142709	9513945	3246285	3277595	10533544	31811681
20	3145474	9513965	3246500	3277592	10534540	31782789
21	3148239	9513985	3246715	3277589	10535536	31753897
22	3150999	9514005	3246930	3277586	10536532	31725005
23	3153764	9514025	3247145	3277583	10537528	31696113
24	3156529	9514045	3247360	3277580	10538524	31667221
25	3159289	9514065	3247575	3277577	10539520	31638329
26	3162049	9514085	3247790	3277574	10540516	31609437
27	3164809	9514105	3248005	3277571	10541512	31580545
28	3167569	9514125	3248220	3277568	10542508	31551653
29	3170329	9514145	3248435	3277565	10543504	31522761
30	3173089	9514165	3248650	3277562	10544500	31493869
N. Co-Sine. N. Sine. N. Co-Tangent. N. Tangent. N. Co-Secant. N. Secant. M						

71 DEGREES.

Latitude 36 Deg. 00 Min. North Declination.

	0	d.	2	d.	4	6	d.	8	d.	10	d.	12	d.	14	d.	16	d.	18	d.	20	d.	22	d.	24
	b. m.	m.	b. m.	m.	b. m.	m.	b. m.	m.	b. m.	m.	b. m.	m.	b. m.	m.	b. m.	m.	b. m.	m.	b. m.	m.	b. m.	m.	b. m.	m.
S N	12.0		12.0		12.0		12.0		12.0		12.0		12.0		12.0		12.0		12.0		12.0		12.0	
1	0.27	1.26	1.25	1.24	1.23	1.22	1.21	1.20	1.19	1.18	1.17	1.16	1.15	1.14	1.13	1.12	1.11	1.10	1.09	1.08	1.07	1.06	1.05	1.04
2	0.55	2.05	2.04	2.03	2.02	2.01	2.00	1.99	1.98	1.97	1.96	1.95	1.94	1.93	1.92	1.91	1.90	1.89	1.88	1.87	1.86	1.85	1.84	1.83
3	1.26	3.12	3.11	3.10	3.09	3.08	3.07	3.06	3.05	3.04	3.03	3.02	3.01	3.00	2.99	2.98	2.97	2.96	2.95	2.94	2.93	2.92	2.91	2.90
4	2.02	4.12	4.11	4.10	4.09	4.08	4.07	4.06	4.05	4.04	4.03	4.02	4.01	4.00	3.99	3.98	3.97	3.96	3.95	3.94	3.93	3.92	3.91	3.90
5	2.45	5.25	5.24	5.23	5.22	5.21	5.20	5.19	5.18	5.17	5.16	5.15	5.14	5.13	5.12	5.11	5.10	5.09	5.08	5.07	5.06	5.05	5.04	5.03
6	3.39	6.39	6.38	6.37	6.36	6.35	6.34	6.33	6.32	6.31	6.30	6.29	6.28	6.27	6.26	6.25	6.24	6.23	6.22	6.21	6.20	6.19	6.18	6.17
7	4.45	7.45	7.44	7.43	7.42	7.41	7.40	7.39	7.38	7.37	7.36	7.35	7.34	7.33	7.32	7.31	7.30	7.29	7.28	7.27	7.26	7.25	7.24	7.23
WE	8.00	11.54	11.53	11.52	11.51	11.50	11.49	11.48	11.47	11.46	11.45	11.44	11.43	11.42	11.41	11.40	11.39	11.38	11.37	11.36	11.35	11.34	11.33	11.32
1																								
2																								

## Artificial Sines, Tangents, and Secants.

18 DEGREES.

M	L. Sine.	L. Co-Sine.	L. Tangent.	L. Co-Tangent.	L. Secant.	L. Co-Secant.
0	9.4899824	9.9782063	9.5117760	10.4882240	10.0217937	10.5100176
1	9.49093710	9.9781653	9.5126357	10.4877943	10.0218347	10.5096290
2	9.4917929	9.9781241	9.5134954	10.4873649	10.0218759	10.5092408
3	9.4926486	9.9780830	9.5143551	10.4869359	10.0219170	10.5088529
4	9.4935043	9.9780418	9.5152148	10.4865073	10.0219582	10.5084655
5	9.4943600	9.9780006	9.5160745	10.4860790	10.0219994	10.5080784
6	9.4952157	9.9779593	9.5169342	10.4856510	10.0220407	10.5076917
7	9.4960714	9.9779180	9.5177939	10.4852234	10.0220820	10.5073054
8	9.4969271	9.9778767	9.5186536	10.4847961	10.0221233	10.5069194
9	9.4977828	9.9778354	9.5195133	10.4843691	10.0221647	10.5065339
10	9.4986385	9.9777941	9.5203730	10.4839425	10.0222062	10.5061487
11	9.4994942	9.9777528	9.5212327	10.4835162	10.0222477	10.5057639
12	9.4993499	9.9777115	9.5220924	10.4830903	10.0222892	10.5053795
13	9.4992056	9.9776702	9.5229521	10.4826647	10.0223307	10.5049954
14	9.4990613	9.9776289	9.5238118	10.4822394	10.0223723	10.5046117
15	9.4989170	9.9775876	9.5246715	10.4818145	10.0224140	10.5042284
16	9.4987727	9.9775463	9.5255312	10.4813899	10.0224556	10.5038455
17	9.4986284	9.9775050	9.5263909	10.4809656	10.0224974	10.5034630
18	9.4984841	9.9774637	9.5272506	10.4805417	10.0225391	10.5030808
19	9.4983398	9.9774224	9.5281103	10.4801181	10.0225807	10.5026990
20	9.4981955	9.9773811	9.5289699	10.4796948	10.0226223	10.5023176
21	9.4980512	9.9773398	9.5298296	10.4792718	10.0226640	10.5019365
22	9.4979069	9.9772985	9.5306893	10.4788490	10.0227056	10.5015558
23	9.4977626	9.9772572	9.5315490	10.4784270	10.0227473	10.5011755
24	9.4976183	9.9772159	9.5324087	10.4780050	10.0227890	10.5007955
25	9.4974740	9.9771746	9.5332684	10.4775834	10.0228306	10.5004160
26	9.4973297	9.9771333	9.5341281	10.4771621	10.0228723	10.5000367
27	9.4971854	9.9770920	9.5349878	10.4767411	10.0229140	10.4996579
28	9.4970411	9.9770507	9.5358475	10.4763205	10.0229557	10.4992794
29	9.4968968	9.9770094	9.5367072	10.4759001	10.0229974	10.4989013
30	9.4967525	9.9769681	9.5375669	10.4754801	10.0230391	10.4985236
L. Co-Sine. L. Sine. L. Co-Tangent. L. Tangent. L. Co-Secant. L. Secant. M						

71 DEGREES.

Latitude 36 Deg. 00 Min. South Declination.

	0	d.	2	d.	4	6	d.	8	d.	10	d.	12	d.	14	d.	16	d.	18	d.	20	d.	22	d.	24
	b. m.	m.	b. m.	m.	b. m.	m.	b. m.	m.	b. m.	m.	b. m.	m.	b. m.	m.	b. m.	m.	b. m.	m.	b. m.	m.	b. m.	m.	b. m.	m.
S N	12.0		12.0		12.0		12.0		12.0		12.0		12.0		12.0		12.0		12.0		12.0		12.0	
1	0.27	1.26	1.25	1.24	1.23	1.22	1.21	1.20	1.19	1.18	1.17	1.16	1.15	1.14	1.13	1.12	1.11	1.10	1.09	1.08	1.07	1.06	1.05	1.04
2	0.55	2.05	2.04	2.03	2.02	2.01	2.00	1.99	1.98	1.97	1.96	1.95	1.94	1.93	1.92	1.91	1.90	1.89	1.88	1.87	1.86	1.85	1.84	1.83
3	1.26	3.12	3.11	3.10	3.09	3.08	3.07	3.06	3.05	3.04	3.03	3.02	3.01	3.00	2.99	2.98	2.97	2.96	2.95	2.94	2.93	2.92	2.91	2.90
4	2.02	4.12	4.11	4.10	4.09	4.08	4.07	4.06	4.05	4.04	4.03	4.02	4.01	4.00	3.99	3.98	3.97	3.96	3.95	3.94	3.93	3.92	3.91	3.90
5	2.45	5.25	5.24	5.23	5.22	5.21	5.20	5.19	5.18	5.17	5.16	5.15	5.14	5.13	5.12	5.11	5.10	5.09	5.08	5.07	5.06	5.05	5.04	5.03
6	3.39	6.39	6.38	6.37	6.36	6.35	6.34	6.33	6.32	6.31	6.30	6.29	6.28	6.27	6.26	6.25	6.24	6.23	6.22	6.21	6.20	6.19	6.18	6.17
7	4.45	7.45	7.44	7.43	7.42	7.41	7.40	7.39	7.38	7.37	7.36	7.35	7.34	7.33	7.32	7.31	7.30	7.29	7.28	7.27	7.26	7.25	7.24	7.23
WE	8.00	11.54	11.53	11.52	11.51	11.50	11.49	11.48	11.47	11.46	11.45	11.44	11.43	11.42	11.41	11.40	11.39	11.38	11.37	11.36	11.35	11.34	11.33	11.32
1																								
2																								







## A TABLE of Natural and

## 19 DEGREES.

M	N. Sine.	N. Co-Sine.	N. Tangent.	N. Co-Tang.	N. Secant.	N. Co-Secant.
0	3255682	9459185	3443276	29024109	10576207	30715535
1	3255432	9454435	3446530	29014688	10577267	30689610
2	3255182	9453290	3447755	28987314	10578328	30663731
3	3254932	9452141	3448980	28959956	10579390	30637857
4	3254682	9451391	3450205	28932600	10580453	30611911
5	3254432	9450440	3451430	28905246	10581517	30586075
6	3254182	9449489	3452655	28877877	10582583	30560255
7	3253932	9448537	3453880	28850513	10583649	30534435
8	3253682	9447584	3455105	28823149	10584717	30508615
9	3253432	9446633	3456330	28795785	10585786	30482795
10	3253182	9445681	3457555	28768421	10586855	30456975
11	3252932	9444729	3458780	28741057	10587926	30431155
12	3252682	9443776	3459980	28713693	10589000	30405335
13	3252432	9442824	3461180	28686329	10590077	30379515
14	3252182	9441871	3462380	28658965	10591157	30353695
15	3251932	9440919	3463580	28631601	10592239	30327875
16	3251682	9440000	3464780	28604237	10593324	30302055
17	3251432	9439081	3465980	28576873	10594412	30276235
18	3251182	9438162	3467180	28549509	10595503	30250415
19	3250932	9437243	3468380	28522145	10596597	30224595
20	3250682	9436324	3469580	28494781	10597694	30198775
21	3250432	9435405	3470780	28467417	10598794	30172955
22	3250182	9434486	3471980	28440053	10599897	30147135
23	3249932	9433567	3473180	28412689	10600997	30121315
24	3249682	9432648	3474380	28385325	10602100	30095495
25	3249432	9431729	3475580	28357961	10603207	30069675
26	3249182	9430810	3476780	28330597	10604317	30043855
27	3248932	9429891	3477980	28303233	10605430	30018035
28	3248682	9428972	3479180	28275869	10606547	29992215
29	3248432	9428053	3480380	28248505	10607667	29966395
30	3248182	9427134	3481580	28221141	10608790	29940575
N. Co-Sine.	N. Sine.	N. Co-Tang.	N. Tangent.	N. Co-Secant.	N. Secant.	M

## 70 DEGREES.

## Artificial Sines, Tangents, and Secants.

## 19 DEGREES.

M	L. Sine.	L. Co-Sine.	L. Tangent.	L. Co-Tang.	L. Secant.	L. Co-Secant.
0	9.5126419	9.9750701	9.5367719	10.4630281	10.0243299	10.4837581
1	9.5130086	9.9750625	9.5373821	10.4626179	10.0243735	10.4836914
2	9.5133753	9.9750550	9.5379923	10.4622280	10.0244170	10.4836250
3	9.5137410	9.9750474	9.5386025	10.4618381	10.0244605	10.4835586
4	9.5141067	9.9750399	9.5392127	10.4614482	10.0245040	10.4834922
5	9.5144724	9.9750324	9.5398229	10.4610583	10.0245475	10.4834258
6	9.5148381	9.9750249	9.5404331	10.4606684	10.0245910	10.4833594
7	9.5152038	9.9750174	9.5410433	10.4602785	10.0246345	10.4832930
8	9.5155695	9.9750099	9.5416535	10.4598886	10.0246780	10.4832266
9	9.5159352	9.9749974	9.5422637	10.4594987	10.0247215	10.4831602
10	9.5163009	9.9749899	9.5428739	10.4591088	10.0247650	10.4830938
11	9.5166666	9.9749824	9.5434841	10.4587189	10.0248085	10.4830274
12	9.5170323	9.9749749	9.5440943	10.4583290	10.0248520	10.4829610
13	9.5173980	9.9749674	9.5447045	10.4579391	10.0248955	10.4828946
14	9.5177637	9.9749599	9.5453147	10.4575492	10.0249390	10.4828282
15	9.5181294	9.9749524	9.5459249	10.4571593	10.0249825	10.4827618
16	9.5184951	9.9749449	9.5465351	10.4567694	10.0250260	10.4826954
17	9.5188608	9.9749374	9.5471453	10.4563795	10.0250695	10.4826290
18	9.5192265	9.9749299	9.5477555	10.4559896	10.0251130	10.4825626
19	9.5195922	9.9749224	9.5483657	10.4555997	10.0251565	10.4824962
20	9.5199579	9.9749149	9.5489759	10.4552098	10.0252000	10.4824298
21	9.5203236	9.9749074	9.5495861	10.4548199	10.0252435	10.4823634
22	9.5206893	9.9748999	9.5501963	10.4544299	10.0252870	10.4822970
23	9.5210550	9.9748924	9.5508065	10.4540399	10.0253305	10.4822306
24	9.5214207	9.9748849	9.5514167	10.4536499	10.0253740	10.4821642
25	9.5217864	9.9748774	9.5520269	10.4532599	10.0254175	10.4820978
26	9.5221521	9.9748699	9.5526371	10.4528699	10.0254610	10.4820314
27	9.5225178	9.9748624	9.5532473	10.4524799	10.0255045	10.4819650
28	9.5228835	9.9748549	9.5538575	10.4520899	10.0255480	10.4818986
29	9.5232492	9.9748474	9.5544677	10.4516999	10.0255915	10.4818322
30	9.5236149	9.9748399	9.5550779	10.4513099	10.0256350	10.4817658
L. Co-Sine.	L. Sine.	L. Co-Tang.	L. Tangent.	L. Co-Secant.	L. Secant.	M

## 70 DEGREES.

## Latitude 38 Deg. 00 Min. North Declination.

	0	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20	21	22	23
	b. m.	a. b. m.	m.	b. m.	m.	b. m.	b. m.	m.	b. m.	m.	b. m.	b. m.	m.	b. m.	m.	b. m.	b. m.	m.	b. m.	m.	b. m.	m.	b. m.	b. m.
SN	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0
1	0.48	1.02	1.52	2.25	2.51	2.65	2.75	2.85	2.95	3.05	3.15	3.25	3.35	3.45	3.55	3.65	3.75	3.85	3.95	4.05	4.15	4.25	4.35	4.45
2	0.57	2.05	2.55	3.05	3.25	3.45	3.65	3.85	4.05	4.25	4.45	4.65	4.85	5.05	5.25	5.45	5.65	5.85	6.05	6.25	6.45	6.65	6.85	7.05
3	1.29	3.12	4.12	4.72	5.12	5.42	5.62	5.82	6.02	6.22	6.42	6.62	6.82	7.02	7.22	7.42	7.62	7.82	8.02	8.22	8.42	8.62	8.82	9.02
4	2.05	5.21	6.12	6.72	7.12	7.42	7.62	7.82	8.02	8.22	8.42	8.62	8.82	9.02	9.22	9.42	9.62	9.82	10.02	10.22	10.42	10.62	10.82	11.02
5	2.51	7.24	8.12	8.72	9.12	9.42	9.62	9.82	10.02	10.22	10.42	10.62	10.82	11.02	11.22	11.42	11.62	11.82	12.02	12.22	12.42	12.62	12.82	13.02
6	3.41	8.33	9.22	9.82	10.22	10.52	10.72	10.92	11.12	11.32	11.52	11.72	11.92	12.12	12.32	12.52	12.72	12.92	13.12	13.32	13.52	13.72	13.92	14.12
7	4.48	9.43	10.32	10.92	11.32	11.62	11.82	12.02	12.22	12.42	12.62	12.82	13.02	13.22	13.42	13.62	13.82	14.02	14.22	14.42	14.62	14.82	15.02	15.22
WE	6.00	10.50	10.50	10.50	10.50	10.50	10.50	10.50	10.50	10.50	10.50	10.50	10.50	10.50	10.50	10.50	10.50	10.50	10.50	10.50	10.50	10.50	10.50	10.50
1																								
2																								



A T A B L E of Natural and

19 DEGREES.									
M	N. Sine.	N. Co-Sine.	N. Tangent.	N. Co-Tang.	N. Secant.	N. Co-Secant.			
30	333 <sup>50</sup> 69	7425415	3341136	28252129	12638487	29957443	30		
31	334 <sup>20</sup> 10	7425445	3344445	28213045	12639286	29957286	31		
32	334 <sup>35</sup> 52	7424471	3347735	28187005	126401075	29958312	28		
33	334 <sup>46</sup> 39	7423497	3351101	28161004	12641170	29958511	27		
34	334 <sup>50</sup> 34	7422524	3354236	28135048	12642367	29959532	26		
35	335 <sup>1</sup> 775	7421550	3357575	28109134	12643265	29959536	25		
36	335 <sup>45</sup> 16	7420575	3360910	28083263	12644564	29910563	24		
37	335 <sup>7</sup> 235	7419599	3364115	28057433	12646164	29756231	23		
38	335 <sup>9</sup> 956	7418622	3367337	28031646	12647265	29761942	22		
39	336 <sup>2</sup> 735	7417644	3370567	28005909	12648367	29773765	21		
40	336 <sup>4</sup> 475	7416665	3373795	27980189	12649471	29781240	20		
41	336 <sup>52</sup> 214	7415685	3377237	27954537	12650578	29788927	19		
42	337 <sup>0</sup> 953	7414705	3380518	27928917	12651681	29795205	18		
43	337 <sup>3</sup> 691	7413724	3383800	27903339	12652788	29801125	17		
44	337 <sup>6</sup> 424	7412742	3387083	27877802	12653896	29807057	16		
45	337 <sup>9</sup> 167	7411760	3390367	27852307	12655005	29813000	15		
46	338 <sup>19</sup> 05	7410777	3393651	27826851	12656216	29819135	14		
47	338 <sup>46</sup> 42	7409793	3396936	27801440	12657227	29825421	13		
48	338 <sup>7</sup> 737	7408808	3400222	27776069	12658339	29831348	12		
49	339 <sup>0</sup> 116	7407822	3403508	27750735	12659445	29837516	11		
50	339 <sup>2</sup> 353	7406835	3406795	27725448	12660565	29843725	10		
51	339 <sup>5</sup> 589	7405848	3410083	27700199	12661683	29849975	9		
52	339 <sup>8</sup> 25	7404860	3413371	27674990	12662801	29856265	8		
53	340 <sup>1</sup> 060	7403871	3416660	27649722	12663919	29862597	7		
54	340 <sup>3</sup> 795	7402881	3419950	27624495	12665035	29868968	6		
55	340 <sup>6</sup> 530	7401890	3423240	27599265	12666158	29875380	5		
56	340 <sup>9</sup> 265	7400899	3426531	27574061	12667280	29881833	4		
57	341 <sup>2</sup> 000	7399907	3429823	27548854	12668403	29888326	3		
58	341 <sup>4</sup> 734	7398914	3433115	27523655	12669527	29894858	2		
59	341 <sup>7</sup> 468	7397920	3436408	27498461	12670652	29901431	1		
60	342 <sup>0</sup> 202	7396925	3439702	27473274	12671778	29908044	0		
	N. Co-Sine.	N. Sine.	N. Co-Tang.	N. Tangent.	N. Co-Secant.	N. Secant.			M.

[illegible]

19 DEGREES.									
M	<i>L. Sine.</i>	<i>L. Co-Sine.</i>	<i>L. Tangent.</i>	<i>L. Co-Tang.</i>	<i>L. Secant.</i>	<i>L. Co-Secant.</i>			
30	9-5234953	9-9743466	9-5491487	10-4505513	10-0256934	10-4765047	30		
31	9-5238518	9-9743018	9-5495500	10-4504500	10-0256982	10-4761482	29		
32	9-5242081	9-9742570	9-5499511	10-4503489	10-0257030	10-4757919	28		
33	9-5245640	9-9742122	9-5503519	10-4499481	10-0257078	10-4754360	27		
34	9-5249196	9-9741673	9-5507525	10-4492477	10-0257127	10-4750804	26		
35	9-5252749	9-9741224	9-5511525	10-4488474	10-0257176	10-4747251	25		
36	9-5256298	9-9740774	9-5515524	10-4484476	10-0257226	10-4743702	24		
37	9-5259844	9-9740324	9-5519521	10-4480479	10-0256676	10-4740156	23		
38	9-5263387	9-9739873	9-5523514	10-4476485	10-0260127	10-4736612	22		
39	9-5266927	9-9739422	9-5527504	10-4472496	10-0260578	10-4733073	21		
40	9-5270463	9-9738971	9-5531492	10-4468508	10-0261029	10-4729537	20		
41	9-5273997	9-9738519	9-5535477	10-4464523	10-0261481	10-4726003	19		
42	9-5277525	9-9738067	9-5539459	10-4460541	10-0261933	10-4722474	18		
43	9-5281053	9-9737615	9-5543438	10-4456562	10-0262385	10-4718947	17		
44	9-5284577	9-9737162	9-5547415	10-4452585	10-0262838	10-4715423	16		
45	9-5288097	9-9736709	9-5551388	10-4448612	10-0263291	10-4711903	15		
46	9-5291614	9-9736255	9-5555365	10-4444641	10-0263745	10-4708386	14		
47	9-5295128	9-9735801	9-5559327	10-4440673	10-0264199	10-4704872	13		
48	9-5298638	9-9735346	9-5563292	10-4436708	10-0264654	10-4701362	12		
49	9-5302146	9-9734891	9-5567255	10-4432745	10-0265109	10-4697854	11		
50	9-5305650	9-9734435	9-5571214	10-4428786	10-0265565	10-4694350	10		
51	9-5309151	9-9733980	9-5575171	10-4424829	10-0266020	10-4690849	9		
52	9-5312649	9-9733523	9-5579125	10-4420875	10-0266477	10-4687351	8		
53	9-5316143	9-9733067	9-5583077	10-4416923	10-0266933	10-4683857	7		
54	9-5319635	9-9732610	9-5587025	10-4412975	10-0267390	10-4680365	6		
55	9-5323123	9-9732152	9-5590971	10-4409029	10-0267848	10-4676877	5		
56	9-5326608	9-9731694	9-5594914	10-4405086	10-0268306	10-4673392	4		
57	9-5330090	9-9731236	9-5598854	10-4401146	10-0268764	10-4669910	3		
58	9-5333569	9-9730777	9-5602792	10-4397208	10-0269223	10-4666421	2		
59	9-5337044	9-9730318	9-5606727	10-4393273	10-0269682	10-4662936	1		
60	9-5340517	9-9729858	9-5610659	10-4389341	10-0270142	10-4659483	0		
<i>L. Co-Sine.</i>		<i>L. Sine.</i>	<i>L. Co-Tang.</i>	<i>L. Tangent.</i>	<i>L. Co-Secant.</i>	<i>L. Secant.</i>	<i>M</i>		

[illegible]



## A TABLE of Natural and

20 DEGREES.

M	N. Sine.	N. Co-Sine.	N. Tangent.	N. Co-Tang.	N. Secant.	N. Co-Secant.
0	3420202	9396925	3639702	27474774	10641778	29238044
1	3422935	9395931	3642997	27449927	10642905	29214697
2	3425668	9394935	3646292	27425120	10644033	29191389
3	3428401	9393938	3649588	27400352	10645163	29168121
4	3431133	9392940	3652885	27375623	10646294	29144892
5	3433865	9391942	3656182	27350934	10647426	29121703
6	3436597	9390943	3659480	27326284	10648559	29098553
7	3439329	9389943	3662779	27301672	10649693	29075443
8	3442060	9388942	3666079	27277104	10650828	29052372
9	3444791	9387940	3669379	27252569	10651964	29029332
10	3447522	9386937	3672680	27228069	10653101	29006345
11	3450252	9385934	3675982	27203620	10654240	28983391
12	3452982	9384932	3679284	27179284	10655380	28960475
13	3455712	9383929	3682587	27154982	10656521	28937598
14	3458442	9382929	3685891	27130687	10657663	28914760
15	3461171	9381913	3689195	27106416	10658807	28891959
16	3463900	9380906	3692500	27082162	10659951	28869198
17	3466629	9379898	3695806	27057929	10661097	28846474
18	3469357	9378889	3699113	27033713	10662243	28823789
19	3472085	9377879	3702420	27009514	10663391	28801142
20	3474813	9376869	3705728	26985254	10664540	28778532
21	3477540	9375858	3709037	26961181	10665690	28755961
22	3480267	9374846	3712346	26937147	10666842	28733428
23	3482994	9373833	3715656	26913149	10667994	28710932
24	3485721	9372819	3718967	26889190	10669148	28688474
25	3488447	9371805	3722278	26865267	10670302	28666035
26	3491173	9370790	3725590	26841383	10671458	28643670
27	3493899	9369774	3728903	26817535	10672615	28621324
28	3496624	9368757	3732217	26793725	10673774	28599015
29	3499349	9367740	3735532	26769951	10674934	28576744
30	3502074	9366722	3738847	26746215	10676094	28554509
	N. Co-Sine.	N. Sine.	N. Co-Tang.	N. Tangent.	N. Co-Secant.	N. Secant.

69 DEGREES.

Latitude 40 Deg. 00 Min. North Declination.

	0	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20	21	22	23
8 N	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0
1	0.29	1.00	1.00	1.00	1.00	1.00	1.00	1.00	1.00	1.00	1.00	1.00	1.00	1.00	1.00	1.00	1.00	1.00	1.00	1.00	1.00	1.00	1.00	1.00
2	1.00	2.00	2.00	2.00	2.00	2.00	2.00	2.00	2.00	2.00	2.00	2.00	2.00	2.00	2.00	2.00	2.00	2.00	2.00	2.00	2.00	2.00	2.00	2.00
3	1.33	3.13	3.13	3.13	3.13	3.13	3.13	3.13	3.13	3.13	3.13	3.13	3.13	3.13	3.13	3.13	3.13	3.13	3.13	3.13	3.13	3.13	3.13	3.13
4	2.11	5.26	5.26	5.26	5.26	5.26	5.26	5.26	5.26	5.26	5.26	5.26	5.26	5.26	5.26	5.26	5.26	5.26	5.26	5.26	5.26	5.26	5.26	5.26
5	2.56	6.25	6.25	6.25	6.25	6.25	6.25	6.25	6.25	6.25	6.25	6.25	6.25	6.25	6.25	6.25	6.25	6.25	6.25	6.25	6.25	6.25	6.25	6.25
6	3.49	8.41	8.41	8.41	8.41	8.41	8.41	8.41	8.41	8.41	8.41	8.41	8.41	8.41	8.41	8.41	8.41	8.41	8.41	8.41	8.41	8.41	8.41	8.41
7	4.51	9.44	9.44	9.44	9.44	9.44	9.44	9.44	9.44	9.44	9.44	9.44	9.44	9.44	9.44	9.44	9.44	9.44	9.44	9.44	9.44	9.44	9.44	9.44
WE	6.00	9.51	10.44	10.44	10.44	10.44	10.44	10.44	10.44	10.44	10.44	10.44	10.44	10.44	10.44	10.44	10.44	10.44	10.44	10.44	10.44	10.44	10.44	10.44
1																								
2																								
3																								

## Artificial Sines, Tangents, and Secants.

20 DEGREES.

M	L. Sine.	L. Co-Sine.	L. Tangent.	L. Co-Tang.	L. Secant.	L. Co-Secant.
0	9.5340517	9.9729858	9.5610658	10.4389341	10.0279142	10.4659143
1	9.5343886	9.9729398	9.5614588	10.4385412	10.027662	10.4656014
2	9.5347452	9.9728938	9.5618515	10.4381485	10.0274102	10.4652845
3	9.5350915	9.9728477	9.5622439	10.4377561	10.0271583	10.4649655
4	9.5354375	9.9728016	9.5626360	10.4373640	10.0269064	10.4646465
5	9.5357832	9.9727554	9.5630278	10.4369722	10.0266545	10.4643275
6	9.5361286	9.9727092	9.5634194	10.4365806	10.0264026	10.4640085
7	9.5364737	9.9726630	9.5638107	10.4361893	10.0261507	10.4636895
8	9.5368184	9.9726166	9.5642018	10.4357982	10.0258988	10.4633705
9	9.5371628	9.9725703	9.5645925	10.4354075	10.0256469	10.4630515
10	9.5375069	9.9725239	9.5649831	10.4350169	10.0253950	10.4627325
11	9.5378508	9.9724775	9.5653733	10.4346267	10.0251431	10.4624135
12	9.5381943	9.9724310	9.5657633	10.4342367	10.0248912	10.4620945
13	9.5385375	9.9723845	9.5661530	10.4338467	10.0246393	10.4617755
14	9.5388804	9.9723380	9.5665424	10.4334567	10.0243874	10.4614565
15	9.5392230	9.9722914	9.5669316	10.4330667	10.0241355	10.4611375
16	9.5395653	9.9722448	9.5673205	10.4326767	10.0238836	10.4608185
17	9.5399075	9.9721981	9.5677091	10.4322867	10.0236317	10.4604995
18	9.5402493	9.9721514	9.5680975	10.4318967	10.0233798	10.4601805
19	9.5405903	9.9721047	9.5684856	10.4315067	10.0231279	10.4598615
20	9.5409314	9.9720579	9.5688735	10.4311167	10.0228760	10.4595425
21	9.5412721	9.9720110	9.5692611	10.4307267	10.0226241	10.4592235
22	9.5416126	9.9719642	9.5696484	10.4303367	10.0223722	10.4589045
23	9.5419527	9.9719172	9.5700355	10.4299467	10.0221203	10.4585855
24	9.5422926	9.9718703	9.5704223	10.4295567	10.0218684	10.4582665
25	9.5426321	9.9718233	9.5708088	10.4291667	10.0216165	10.4579475
26	9.5429713	9.9717762	9.5711951	10.4287767	10.0213646	10.4576285
27	9.5433103	9.9717291	9.5715811	10.4283867	10.0211127	10.4573095
28	9.5436487	9.9716820	9.5719669	10.4279967	10.0208608	10.4569905
29	9.5439872	9.9716348	9.5723524	10.4276067	10.0206089	10.4566715
30	9.5443253	9.9715876	9.5727377	10.4272167	10.0203570	10.4563525
	L. Co-Sine.	L. Sine.	L. Co-Tang.	L. Tangent.	L. Co-Secant.	L. Secant.

69 DEGREES.

Latitude 40 Deg. 00 Min. South Declination.

	0	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20	21	22	23
8 S	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0
1	0.29	1.00	1.00	1.00	1.00	1.00	1.00	1.00	1.00	1.00	1.00	1.00	1.00	1.00	1.00	1.00	1.00	1.00	1.00	1.00	1.00	1.00	1.00	1.00
2	1.00	2.00	2.00	2.00	2.00	2.00	2.00	2.00	2.00	2.00	2.00	2.00	2.00	2.00	2.00	2.00	2.00	2.00	2.00	2.00	2.00	2.00	2.00	2.00
3	1.33	3.13	3.13	3.13	3.13	3.13	3.13	3.13	3.13	3.13	3.13	3.13	3.13	3.13	3.13	3.13	3.13	3.13	3.13	3.13	3.13	3.13	3.13	3.13
4	2.11	5.26	5.26	5.26	5.26	5.26	5.26	5.26	5.26	5.26	5.26	5.26	5.26	5.26	5.26	5.26	5.26	5.26	5.26	5.26	5.26	5.26	5.26	5.26
5	2.56	6.25	6.25	6.25	6.25	6.25	6.25	6.25	6.25	6.25	6.25	6.25	6.25	6.25	6.25	6.25	6.25	6.25	6.25	6.25	6.25	6.25	6.25	6.25
6	3.49	8.41	8.41	8.41	8.41	8.41	8.41	8.41	8.41	8.41	8.41	8.41	8.41	8.41	8.41	8.41	8.41	8.41	8.41	8.41	8.41	8.41	8.41	8.41
7	4.51	9.44	9.44	9.44	9.44	9.44	9.44	9.44	9.44	9.44	9.44	9.44	9.44	9.44	9.44	9.44	9.44	9.44	9.44	9.44	9.44	9.44	9.44	9.44
WE	6.00	9.51	10.44	10.44	10.44	10.44	10.44	10.44	10.44	10.44	10.44	10.44	10.44	10.44	10.44	10.44	10.44	10.44	10.44	10.44	10.44	10.44	10.44	10.44
1																								
2																								
3																								



## A TABLE of Natural and

20 DEGREES.

M	N. Sine.	N. Co-Sine.	N. Tangent.	N. Co-Tang.	N. Secant.	N. Co-Secant.	
30	3502074	9366722	3738847	26746215	10676694	28554509	30
31	3504799	9365703	3742163	26722516	10677255	28532312	29
32	3507523	9364683	3745479	26698343	10678418	28510152	28
33	3510247	9363662	3748797	26674227	10679582	28488028	27
34	3512970	9362640	3752115	26650385	10680747	28465941	26
35	3515693	9361618	3755434	26626505	10681914	28443891	25
36	3518416	9360595	3758753	26602659	10683081	28421877	24
37	3521139	9359571	3762073	26578810	10684250	28399899	23
38	3523862	9358548	3765394	26555045	10685420	28377959	22
39	3526586	9357521	3768716	26531248	10686591	28356054	21
40	3529306	9356495	3772038	26507408	10687763	28334185	20
41	3532027	9355468	3775361	26483531	10688936	28312353	19
42	3534748	9354442	3778685	26459662	10690110	28290556	18
43	3537469	9353411	3782010	26435809	10691286	28268796	17
44	3540190	9352383	3785335	26411941	10692463	28247071	16
45	3542910	9351352	3788661	26388089	10693641	28225382	15
46	3545630	9350321	3791988	26364243	10694820	28203729	14
47	3548350	9349290	3795316	26340392	10696000	28182111	13
48	3551070	9348256	3798644	26316546	10697182	28160529	12
49	3553789	9347223	3801973	26292706	10698364	28138982	11
50	3556508	9346189	3805303	26268869	10699548	28117471	10
51	3559226	9345154	3808633	26245034	10700733	28095995	9
52	3561944	9344118	3811964	26221206	10701919	28074554	8
53	3564662	9343082	3815296	26197386	10703106	28053143	7
54	3567380	9342045	3818629	26173571	10704295	28031777	6
55	3570097	9341007	3821962	26149761	10705484	28010441	5
56	3572814	9339967	3825296	26125956	10706675	27989140	4
57	3575531	9338928	3828631	26102156	10707867	27967873	3
58	3578248	9337887	3831967	26078369	10709060	27946641	2
59	3580965	9336846	3835303	26054588	10710254	27925444	1
60	3583682	9335804	3838640	26030811	10711450	27904281	0
	N. Co-Sine.	N. Sine.	N. Co-Tang.	N. Tangent.	N. Co-Secant.	N. Secant.	M

69 DEGREES.

Latitude 41 Deg. 00 Min. North Declination.

4th Deg. Column										Even Decimation.																						
	0	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20	21	22	23	24	25	26	27	28	29	30	
	b. m.	b. m.	b. m.	b. m.	b. m.	b. m.	b. m.	b. m.	b. m.	b. m.	b. m.	b. m.	b. m.	b. m.	b. m.	b. m.	b. m.	b. m.	b. m.	b. m.	b. m.	b. m.	b. m.	b. m.	b. m.	b. m.	b. m.	b. m.	b. m.	b. m.	b. m.	
S.N.	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	
1	0.30	1.02	1.32	1.58	2.22	2.45	2.67	2.88	3.09	3.29	3.49	3.69	3.89	4.09	4.29	4.49	4.69	4.89	5.09	5.29	5.49	5.69	5.89	6.09	6.29	6.49	6.69	6.89	7.09	7.29	7.49	
2	1.01	2.05	2.57	3.45	4.30	5.12	5.92	6.70	7.47	8.23	8.98	9.72	10.45	11.17	11.89	12.60	13.31	14.01	14.71	15.41	16.11	16.81	17.51	18.21	18.91	19.61	20.31	21.01	21.71	22.41	23.11	
3	1.35	3.02	4.02	4.98	5.92	6.84	7.74	8.62	9.49	10.35	11.20	12.04	12.87	13.69	14.51	15.33	16.14	16.95	17.75	18.55	19.35	20.15	20.95	21.75	22.55	23.35	24.15	24.95	25.75	26.55	27.35	
4	2.13	5.20	6.20	7.16	8.10	9.02	9.93	10.83	11.72	12.60	13.48	14.35	15.22	16.09	16.95	17.81	18.67	19.52	20.37	21.22	22.07	22.92	23.77	24.62	25.47	26.32	27.17	28.02	28.87	29.72	30.57	
5	2.58	6.25	7.25	8.21	9.15	10.07	10.99	11.90	12.80	13.69	14.57	15.45	16.32	17.19	18.06	18.93	19.79	20.65	21.51	22.37	23.22	24.07	24.92	25.77	26.62	27.47	28.32	29.17	30.02	30.87	31.72	
6	3.51	8.43	9.43	10.38	11.32	12.24	13.15	14.05	14.94	15.82	16.70	17.57	18.44	19.31	20.18	21.04	21.91	22.77	23.63	24.49	25.35	26.21	27.07	27.92	28.78	29.63	30.49	31.34	32.19	33.05	33.90	
7	4.53	9.44	10.44	11.39	12.33	13.25	14.16	15.06	15.95	16.83	17.70	18.57	19.44	20.31	21.18	22.04	22.91	23.77	24.63	25.49	26.35	27.21	28.07	28.93	29.79	30.65	31.51	32.37	33.23	34.09	34.95	
WE	6.00	9.51	10.51	11.46	12.40	13.32	14.23	15.13	16.02	16.90	17.77	18.64	19.51	20.38	21.24	22.11	22.97	23.83	24.69	25.55	26.41	27.27	28.13	28.99	29.85	30.71	31.57	32.43	33.29	34.15	35.01	
1																																
2																																
3																																

## Artificial Sines, Tangents, and Secants.

20 DEGREES.

M	L. Sine.	L. Co-Sine.	L. Tangent.	L. Co-Tang.	L. Secant.	L. Co-Secant.	
30	9.5443253	9.9715876	9.572377	10.4272623	10.0284124	10.4559747	30
31	9.5446630	9.9715404	9.5731227	10.4268773	10.0284596	10.4559370	29
32	9.5450005	9.9714931	9.5738704	10.4264926	10.0285069	10.4558993	28
33	9.5453377	9.9714457	9.5746199	10.4261081	10.0285543	10.4558616	27
34	9.5456745	9.9713984	9.5753701	10.4257239	10.0286016	10.4558239	26
35	9.5460110	9.9713509	9.5761201	10.4253399	10.0286491	10.4557862	25
36	9.5463472	9.9713035	9.5768703	10.4249562	10.0286965	10.4557485	24
37	9.5466832	9.9712560	9.5776207	10.4245728	10.0287440	10.4557108	23
38	9.5470189	9.9712084	9.5783714	10.4241896	10.0287916	10.4556731	22
39	9.5473542	9.9711608	9.5791222	10.4238066	10.0288392	10.4556354	21
40	9.5476893	9.9711132	9.5798731	10.4234239	10.0288868	10.4555977	20
41	9.5480240	9.9710655	9.5806240	10.4230415	10.0289345	10.4555600	19
42	9.5483585	9.9710178	9.5813749	10.4226593	10.0289822	10.4555223	18
43	9.5486927	9.9709701	9.5821258	10.4222774	10.0290299	10.4554846	17
44	9.5490266	9.9709223	9.5828767	10.4218957	10.0290777	10.4554469	16
45	9.5493602	9.9708744	9.5836276	10.4215142	10.0291256	10.4554092	15
46	9.5496935	9.9708265	9.5843785	10.4211331	10.0291735	10.4553715	14
47	9.5500265	9.9707786	9.5851294	10.4207521	10.0292214	10.4553338	13
48	9.5503592	9.9707306	9.5858803	10.4203714	10.0292694	10.4552961	12
49	9.5506916	9.9706826	9.5866312	10.4199910	10.0293174	10.4552584	11
50	9.5510237	9.9706346	9.5873821	10.4196108	10.0293654	10.4552207	10
51	9.5513555	9.9705865	9.5881330	10.4192309	10.0294135	10.4551830	9
52	9.5516871	9.9705383	9.5888839	10.4188512	10.0294617	10.4551453	8
53	9.5520184	9.9704902	9.5896348	10.4184718	10.0295099	10.4551076	7
54	9.5523494	9.9704419	9.5903857	10.4180926	10.0295581	10.4550699	6
55	9.5526801	9.9703937	9.5911366	10.4177136	10.0296063	10.4550322	5
56	9.5530105	9.9703454	9.5918875	10.4173349	10.0296546	10.4549945	4
57	9.5533406	9.9702970	9.5926384	10.4169565	10.0297030	10.4549568	3
58	9.5536704	9.9702486	9.5933893	10.4165781	10.0297514	10.4549191	2
59	9.5539999	9.9702002	9.5941402	10.4162000	10.0298000	10.4548814	1
60	9.5543292	9.9701517	9.5948911	10.4158226	10.0298483	10.4548437	0
	L. Co-Sine.	L. Sine.	L. Co-Tang.	L. Tangent.	L. Co-Secant.	L. Secant.	M

69 DEGREES.

Latitude 41 Deg. 00 Min. South Declination.

Table 1. $\log_{10} \sin \theta$ (mm. $\sin \theta$ )																													
	0	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20	21	22	23	24	25	26	27	28
S.N.	b.m.	m	b.m.	m	b.m.	m	b.m.	m	b.m.	m	b.m.	m	b.m.	m	b.m.	m	b.m.	m	b.m.	m	b.m.	m	b.m.	m	b.m.	m	b.m.	m	b.m.
1	0.30	1.03	1.03	1.03	1.03	1.03	1.03	1.03	1.03	1.03	1.03	1.03	1.03	1.03	1.03	1.03	1.03	1.03	1.03	1.03	1.03	1.03	1.03	1.03	1.03	1.03	1.03	1.03	1.03
2	1.01	2.10	2.10	2.10	2.10	2.10	2.10	2.10	2.10	2.10	2.10	2.10	2.10	2.10	2.10	2.10	2.10	2.10	2.10	2.10	2.10	2.10	2.10	2.10	2.10	2.10	2.10	2.10	2.10
3	1.35	3.13	3.13	3.13	3.13	3.13	3.13	3.13	3.13	3.13	3.13	3.13	3.13	3.13	3.13	3.13	3.13	3.13	3.13	3.13	3.13	3.13	3.13	3.13	3.13	3.13	3.13	3.13	3.13
4	2.13	5.21	5.21	5.21	5.21	5.21	5.21	5.21	5.21	5.21	5.21	5.21	5.21	5.21	5.21	5.21	5.21	5.21	5.21	5.21	5.21	5.21	5.21	5.21	5.21	5.21	5.21	5.21	5.21
5	2.58	6.24	6.24	6.24	6.24	6.24	6.24	6.24	6.24	6.24	6.24	6.24	6.24	6.24	6.24	6.24	6.24	6.24	6.24	6.24	6.24	6.24	6.24	6.24	6.24	6.24	6.24	6.24	6.24
6	3.51	7.35	7.35	7.35	7.35	7.35	7.35	7.35	7.35	7.35	7.35	7.35	7.35	7.35	7.35	7.35	7.35	7.35	7.35	7.35	7.35	7.35	7.35	7.35	7.35	7.35	7.35	7.35	7.35
7	4.53	8.42	8.42	8.42	8.42	8.42	8.42	8.42	8.42	8.42	8.42	8.42	8.42	8.42	8.42	8.42	8.42	8.42	8.42	8.42	8.42	8.42	8.42	8.42	8.42	8.42	8.42	8.42	8.42
WE																													



## A TABLE of Natural and

21 DEGREES.

68 DEGREES.								
M	N. Sine.	N. Co-Sine.	N. Tangent.	N. Co-Tang.	N. Secant.	N. Co-Secant.		
0	3583679	9335804	3838640	26050891	10711450	27904281	60	
1	3586395	9334761	3841978	26025258	10712647	27881553	59	
2	3589110	9333717	3845317	26000659	10713844	27858629	58	
3	3591825	9332673	3848656	25978095	10715043	27835699	57	
4	3594540	9331628	3851996	25956533	10716244	27812773	56	
5	3597254	9330582	3855337	25935068	10717445	27789848	55	
6	3599968	9329535	3858679	25913606	10718647	27766924	54	
7	3602682	9328487	3862021	25892137	10719851	27743999	53	
8	3605395	9327439	3865364	25870752	10721056	27721075	52	
9	3608105	9326390	3868708	25849361	10722262	27698151	51	
10	3610821	9325340	3872053	25827969	10723469	27675226	50	
11	3613533	9324289	3875398	25806573	10724678	27652302	49	
12	3616246	9323238	3878744	25785173	10725887	27629378	48	
13	3618958	9322186	3882091	25763771	10727098	27606454	47	
14	3621669	9321133	3885439	25742368	10728310	27583530	46	
15	3624380	9320079	3888787	25720964	10729523	27560606	45	
16	3627091	9319024	3892136	25699560	10730737	27537682	44	
17	3629802	9317968	3895486	25678155	10731953	27514758	43	
18	3632512	9316912	3898837	25656750	10733170	27491834	42	
19	3635222	9315855	3902189	25635345	10734388	27468910	41	
20	3637932	9314797	3905541	25613940	10735607	27445986	40	
21	3640641	9313738	3908894	25592535	10736827	27423062	39	
22	3643350	9312679	3912245	25571130	10738048	27400138	38	
23	3646059	9311619	3915596	25549725	10739271	27377214	37	
24	3648768	9310558	3918947	25528320	10740495	27354290	36	
25	3651476	9309496	3922298	25506915	10741720	27331366	35	
26	3654184	9308433	3925649	25485510	10742946	27308442	34	
27	3656892	9307370	3928999	25464105	10744173	27285518	33	
28	3659599	9306306	3932350	25442700	10745400	27262594	32	
29	3662306	9305241	3935701	25421295	10746631	27239670	31	
30	3665013	9304175	3939052	25400000	10747862	27216746	30	
N. Co-Sine.		N. Sine.	N. Co-Tang.		N. Tangent.	N. Co-Secant.	N. Secant.	M

68 DEGREES.

## Artificial Sines, Tangents, and Secants.

21 DEGREES.

M	L. Sine.	L. Co-Sine.	L. Tangent.	L. Co-Tang.	L. Secant.	L. Co-Secant.	
0	9-5543292	9-9701517	9-5841774	10-4158226	10-0298483	10-4456708	60
1	9-5546851	9-9701032	9-5845549	10-4154451	10-0298968	10-4453419	59
2	9-5549868	9-9700547	9-5849321	10-4150679	10-0299453	10-4450132	58
3	9-5553152	9-9700061	9-5853091	10-4146909	10-0299939	10-4446845	57
4	9-5556433	9-9699574	9-5856859	10-4143141	10-0300426	10-4443567	56
5	9-5559711	9-9699087	9-5860624	10-4139376	10-0300913	10-4440289	55
6	9-5562987	9-9698600	9-5864386	10-4135614	10-0301400	10-4437013	54
7	9-5566259	9-9698112	9-5868147	10-4131853	10-0301888	10-4433741	53
8	9-5569529	9-9697624	9-5871904	10-4128096	10-0302376	10-4430471	52
9	9-5572796	9-9697136	9-5875660	10-4124340	10-0302864	10-4427204	51
10	9-5576060	9-9696647	9-5879413	10-4120587	10-0303353	10-4423940	50
11	9-5579321	9-9696158	9-5883163	10-4116837	10-0303842	10-4420679	49
12	9-5582579	9-9695668	9-5886912	10-4113088	10-0304332	10-4417421	48
13	9-5585835	9-9695177	9-5890657	10-4109343	10-0304823	10-4414165	47
14	9-5589088	9-9694687	9-5894401	10-4105599	10-0305313	10-4410912	46
15	9-5592338	9-9694196	9-5898142	10-4101858	10-0305804	10-4407662	45
16	9-5595585	9-9693704	9-5901881	10-4098119	10-0306296	10-4404415	44
17	9-5598829	9-9693212	9-5905617	10-4094383	10-0306788	10-4401171	43
18	9-5602071	9-9692720	9-5909351	10-4090649	10-0307280	10-4397929	42
19	9-5605310	9-9692227	9-5913082	10-4086918	10-0307773	10-4394690	41
20	9-5608546	9-9691734	9-5916812	10-4083188	10-0308266	10-4391454	40
21	9-5611779	9-9691240	9-5920539	10-4079461	10-0308759	10-4388221	39
22	9-5615010	9-9690746	9-5924263	10-4075737	10-0309254	10-4384990	38
23	9-5618237	9-9690252	9-5927985	10-4072015	10-0309748	10-4381763	37
24	9-5621462	9-9689757	9-5931705	10-4068295	10-0310243	10-4378538	36
25	9-5624685	9-9689262	9-5935422	10-4064577	10-0310738	10-4375315	35
26	9-5627904	9-9688766	9-5939138	10-4060862	10-0311234	10-4372096	34
27	9-5631121	9-9688270	9-5942851	10-4057149	10-0311730	10-4368879	33
28	9-5634335	9-9687773	9-5946561	10-4053439	10-0312227	10-4365665	32
29	9-5637546	9-9687276	9-5950269	10-4049731	10-0312724	10-4362454	31
30	9-5640754	9-9686779	9-5953975	10-4046025	10-0313221	10-4359246	30
	L. Co-Sine.	L. Sine.	L. Co-Tang.	L. Tangent.	L. Co-Secant.	L. Secant.	M

68 DEGREES.

68 DEGREES.

Latitude 42 Deg. 00 Min. North Declination.

	0	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20	21	22	23	24
S. N.	12-0	12-0	12-0	12-0	12-0	12-0	12-0	12-0	12-0	12-0	12-0	12-0	12-0	12-0	12-0	12-0	12-0	12-0	12-0	12-0	12-0	12-0	12-0	12-0	12-0
1	0-30	1-02-9	1-20-9	1-38-9	1-56-9	2-14-9	2-32-9	2-50-9	3-08-9	3-26-9	3-44-9	4-02-9	4-20-9	4-38-9	4-56-9	5-14-9	5-32-9	5-50-9	6-08-9	6-26-9	6-44-9	7-02-9	7-20-9	7-38-9	7-56-9
2	1-02	2-10-9	3-20-9	4-30-9	5-40-9	6-50-9	8-00-9	9-10-9	10-20-9	11-30-9	12-40-9	1-00-10	1-10-10	1-20-10	1-30-10	1-40-10	1-50-10	2-00-10	2-10-10	2-20-10	2-30-10	2-40-10	2-50-10	3-00-10	3-10-10
3	1-36	2-44-9	3-54-9	4-12-9	4-30-9	4-48-9	5-06-9	5-24-9	5-42-9	5-60-9	5-78-9	5-96-9	6-14-9	6-32-9	6-50-9	7-08-9	7-26-9	7-44-9	8-02-9	8-20-9	8-38-9	8-56-9	9-14-9	9-32-9	9-50-9
4	2-10	3-18-9	4-26-9	5-34-9	6-42-9	7-50-9	8-58-9	10-06-9	11-14-9	12-22-9	1-00-10	1-18-10	1-36-10	1-54-10	2-12-10	2-30-10	2-48-10	3-06-10	3-24-10	3-42-10	4-00-10	4-18-10	4-36-10	4-54-10	5-12-10
5	3-00	4-08-9	5-16-9	6-24-9	7-32-9	8-40-9	9-48-9	10-56-9	12-04-9	1-00-10	1-18-10	1-36-10	1-54-10	2-12-10	2-30-10	2-48-10	3-06-10	3-24-10	3-42-10	4-00-10	4-18-10	4-36-10	4-54-10	5-12-10	5-30-10
6	3-55	5-03-9	6-11-9	7-19-9	8-27-9	9-35-9	10-43-9	11-51-9	12-59-9	1-00-10	1-18-10	1-36-10	1-54-10	2-12-10	2-30-10	2-48-10	3-06-10	3-24-10	3-42-10	4-00-10	4-18-10	4-36-10	4-54-10	5-12-10	5-30-10
7	4-45	5-53-9	7-01-9	8-09-9	9-17-9	10-25-9	11-33-9	12-41-9	1-00-10	1-18-10	1-36-10	1-54-10	2-12-10	2-30-10	2-48-10	3-06-10	3-24-10	3-42-10	4-00-10	4-18-10	4-36-10	4-54-10	5-12-10	5-30-10	5-48-10
8	5-35	6-43-9	7-51-9	9-00-9	10-08-9	11-16-9	12-24-9	1-00-10	1-18-10	1-36-10	1-54-10	2-12-10	2-30-10	2-48-10	3-06-10	3-24-10	3-42-10	4-00-10	4-18-10	4-36-10	4-54-10	5-12-10	5-30-10	5-48-10	6-06-10
9	6-25	7-33-9	8-41-9	9-50-9	10-58-9	12-06-9	1-00-10	1-18-10	1-36-10	1-54-10	2-12-10	2-30-10	2-48-10	3-06-10	3-24-10	3-42-10	4-00-10	4-18-10	4-36-10	4-54-10	5-12-10	5-30-10	5-48-10	6-06-10	6-24-10
10	7-15	8-23-9	9-31-9	10-40-9	11-48-9	12-56-9	1-00-10	1-18-10	1-36-10	1-54-10	2-12-10	2-30-10	2-48-10	3-06-10	3-24-10	3-42-10	4-00-10	4-18-10	4-36-10	4-54-10	5-12-10	5-30-10	5-48-10	6-06-10	6-24-10
11	8-05	9-13-9	10-21-9	11-30-9	12-38-9	1-00-10	1-18-10	1-36-10	1-54-10	2-12-10	2-30-10	2-48-10	3-06-10	3-24-10	3-42-10	4-00-10	4-18-10	4-36-10	4-54-10	5-12-10	5-30-10	5-48-10	6-06-10	6-24-10	6-42-10
12	8-55	10-03-9	11-11-9	12-20-9	1-00-10	1-18-10	1-36-10	1-54-10	2-12-10	2-30-10	2-48-10	3-06-10	3-24-10	3-42-10	4-00-10	4-18-10	4-36-10	4-54-10	5-12-10	5-30-10	5-48-10	6-06-10	6-24-10	6-42-10	7-00-10
13	9-45	10-53-9	12-01-9	1-10-10	1-28-10	1-46-10	2-04-10	2-22-10	2-40-10	2-58-10	3-16-10	3-34-10	3-52-10	4-10-10	4-28-10	4-46-10	5-04-10	5-22-10	5-40-10	5-58-10	6-16-10	6-34-10	6-52-10	7-10-10	7-28-10
14	10-35	11-43-9	12-51-9	1-00-10	1-18-10	1-36-10	1-54-10	2-12-10	2-30-10	2-48-10	3-06-10	3-24-10	3-42-10	4-00-10	4-18-10	4-36-10	4-54-10	5-12-10	5-30-10	5-48-10	6-06-10	6-24-10	6-42-10	7-00-10	7-18-10
15	11-25	12-33-9	1-00-10	1-18-10	1-36-10	1-54-10	2-12-10	2-30-10	2-48-10	3-06-10	3-24-10	3-42-10	4-00-10	4-18-10	4-36-10	4-54-10	5-12-10	5-30-10	5-48-10	6-06-10	6-24-10	6-42-10	7-00-10	7-18-10	7-36-10
16	12-15	1-03-10	1-21-10	1-39-10	1-57-10	2-15-10	2-33-10	2-51-10	3-09-10	3-27-10	3-45-10	4-03-10	4-21-10	4-39-10	4-57-10	5-15-10	5-33-10	5-51-10	6-09-10	6-27-10	6-45-10	7-03-10	7-21-10	7-39-10	7-57-10
17	13-05	1-33-10	1-51-10	2-09-10	2-27-10	2-45-10	3-03-10	3-21-10	3-39-10	3-57-10	4-15-10	4-33-10	4-51												







## A TABLE of Natural and

22 DEGREES.

M	N. Sine.	N. Co-Sine.	V. Tangent.	V. Co-Tang.	N. Secant.	N. Co-Secant.
0	3716066	9271839	4240262	2475262	10795347	26694672
1	3718763	9270749	4243616	24733155	10796616	26675467
2	3721459	9269658	4247031	24713472	10797885	26656292
3	3724156	9268566	4250417	24693816	10799156	26637148
4	3726852	9267473	4253804	24674151	10800427	26618033
5	3729549	9266380	4257191	24654486	10801698	26598947
6	3732243	9265286	4260579	24634821	10802969	26579891
7	3734938	9264191	4263968	24615154	10804240	26560865
8	3737632	9263096	4267358	24595486	10805511	26541868
9	3740327	9262000	4270748	24575819	10806782	26522901
10	3743021	9260903	4274139	24556151	10808053	26503962
11	3745714	9259805	4277531	24536482	10809324	26485054
12	3748405	9258706	4280924	24516812	10810595	26466174
13	3751101	9257606	4284318	24497141	10811866	26447323
14	3753794	9256506	4287713	24477469	10813137	26428492
15	3756485	9255405	4291108	24457797	10814408	26409680
16	3759178	9254303	4294504	24438125	10815679	26390868
17	3761870	9253200	4297900	24418453	10816950	26372056
18	3764562	9252097	4301297	24398781	10818221	26353244
19	3767253	9250993	4304694	24379109	10819492	26334432
20	3769944	9249888	4308091	24359437	10820763	26315620
21	3772635	9248783	4311488	24339765	10822034	26296808
22	3775326	9247678	4314885	24320093	10823305	26277996
23	3778017	9246573	4318282	24300421	10824576	26259184
24	3780707	9245468	4321679	24280749	10825847	26240372
25	3783398	9244363	4325076	24261077	10827118	26221560
26	3786088	9243258	4328473	24241405	10828389	26202748
27	3788779	9242153	4331870	24221733	10829660	26183936
28	3791469	9241048	4335267	24202061	10830931	26165124
29	3794160	9239943	4338664	24182389	10832202	26146312
30	3796850	9238838	4342061	24162717	10833473	26127500

67 DEGREES.

		Latitude 44 Deg. 00 Min. North Declination.																	
		0	d.	2	d.	4	d.	6	d.	8	d.	10	d.	12	d.	14	d.	16	d.
		b. m.	m.	b. m.	m.	b. m.	m.	b. m.	m.	b. m.	m.	b. m.	m.	b. m.	m.	b. m.	m.	b. m.	m.
1	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0
2	1.04	1.04	1.04	1.04	1.04	1.04	1.04	1.04	1.04	1.04	1.04	1.04	1.04	1.04	1.04	1.04	1.04	1.04	1.04
3	1.40	31.37	31.34	41.30	51.26	61.22	71.15	81.08	91.00	100.92	110.83	120.74	130.65	140.56	150.46	160.36	170.26	180.16	190.06
4	2.19	42.15	42.10	52.05	61.99	71.93	81.86	91.78	101.70	111.61	121.52	131.43	141.34	151.24	161.14	171.04	180.94	190.84	200.74
5	3.04	62.16	62.12	72.06	81.99	91.92	101.84	111.75	121.66	131.56	141.46	151.36	161.26	171.16	181.06	190.96	200.86	210.76	220.66
6	3.47	73.00	72.94	82.87	92.79	102.71	112.62	122.53	132.43	142.33	152.23	162.13	172.03	181.93	191.83	201.73	211.63	221.53	231.43
7	4.46	84.48	84.40	94.32	104.24	114.16	124.07	133.97	143.88	153.78	163.68	173.58	183.48	193.38	203.28	213.18	223.08	232.98	242.88
WE	6.00	85.52	85.44	95.36	105.27	115.18	125.08	134.98	144.88	154.78	164.68	174.58	184.48	194.38	204.28	214.18	224.08	233.98	243.88
1																			
2																			
3																			

## Artificial Sines, Tangents, and Secants.

22 DEGREES.

M	L. Sine.	L. Co-Sine.	L. Tangent.	L. Co-Tang.	L. Secant.	L. Co-Secant.
0	9.573754	9.9671859	9.6064096	10.3935904	10.0328341	10.4263426
1	9.5738880	9.9671148	9.6067732	10.3932268	10.0328882	10.4261120
2	9.5740203	9.9670437	9.6071366	10.3928634	10.0329423	10.4258814
3	9.5741523	9.9669725	9.6074997	10.3925000	10.0329964	10.4256508
4	9.5742842	9.9669014	9.6078627	10.3921366	10.0330505	10.4254202
5	9.5744161	9.9668303	9.6082254	10.3917732	10.0331046	10.4251896
6	9.5745480	9.9667592	9.6085880	10.3914097	10.0331587	10.4249590
7	9.5746800	9.9666881	9.6089507	10.3910458	10.0332128	10.4247284
8	9.5748119	9.9666170	9.6093134	10.3906819	10.0332669	10.4244978
9	9.5749438	9.9665459	9.6096761	10.3903180	10.0333210	10.4242672
10	9.5750757	9.9664748	9.6100388	10.3899541	10.0333751	10.4240366
11	9.5752076	9.9664037	9.6104015	10.3895902	10.0334292	10.4238060
12	9.5753395	9.9663326	9.6107642	10.3892263	10.0334833	10.4235754
13	9.5754714	9.9662615	9.6111269	10.3888624	10.0335374	10.4233448
14	9.5756033	9.9661904	9.6114896	10.3885005	10.0335915	10.4231142
15	9.5757352	9.9661193	9.6118523	10.3881386	10.0336456	10.4228836
16	9.5758671	9.9660482	9.6122150	10.3877767	10.0336997	10.4226530
17	9.5759990	9.9659771	9.6125777	10.3874148	10.0337538	10.4224224
18	9.5761309	9.9659060	9.6129404	10.3870529	10.0338079	10.4221918
19	9.5762628	9.9658349	9.6133031	10.3866910	10.0338620	10.4219612
20	9.5763947	9.9657638	9.6136658	10.3863291	10.0339161	10.4217306
21	9.5765266	9.9656927	9.6140285	10.3859672	10.0339702	10.4215000
22	9.5766585	9.9656216	9.6143912	10.3856053	10.0340243	10.4212694
23	9.5767904	9.9655505	9.6147539	10.3852434	10.0340784	10.4210388
24	9.5769223	9.9654794	9.6151166	10.3848815	10.0341325	10.4208082
25	9.5770542	9.9654083	9.6154793	10.3845196	10.0341866	10.4205776
26	9.5771861	9.9653372	9.6158420	10.3841577	10.0342407	10.4203470
27	9.5773180	9.9652661	9.6162047	10.3837958	10.0342948	10.4201164
28	9.5774500	9.9651950	9.6165674	10.3834339	10.0343489	10.4198858
29	9.5775819	9.9651239	9.6169301	10.3830720	10.0344030	10.4196552
30	9.5777138	9.9650528	9.6172928	10.3827101	10.0344571	10.4194246

67 DEGREES.

		Latitude 44 Deg. 00 Min. South Declination.																	
		0	d.	2	d.	4	d.	6	d.	8	d.	10	d.	12	d.	14	d.	16	d.
		b. m.	m.	b. m.	m.	b. m.	m.	b. m.	m.	b. m.	m.	b. m.	m.	b. m.	m.	b. m.	m.	b. m.	m.
1	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0
2	1.04	1.04	1.04	1.04	1.04	1.04	1.04	1.04	1.04	1.04	1.04	1.04	1.04	1.04	1.04	1.04	1.04	1.04	1.04
3	1.40	31.37	31.34	41.30	51.26	61.22	71.15	81.08	91.00	100.92	110.83	120.74	130.65	140.56	150.46	160.36	170.26	180.16	190.06
4	2.19	42.15	42.10	52.05	61.99	71.93	81.86	91.78	101.70	111.61	121.52	131.43	141.34	151.24	161.14	171.04	180.94	190.84	200.74
5	3.04	62.16	62.12	72.06	81.99	91.92	101.84	111.75	121.66	131.56	141.46	151.36	161.26	171.16	181.06	190.96	200.86	210.76	220.66
6	3.47	73.00	72.94	82.87	92.79	102.71	112.62	122.53	132.43	142.33	152.23	162.13	172.03	181.93	191.83	201.73	211.63	221.53	231.43
7	4.46	84.48	84.40	94.32	104.24	114.16	124.07	133.97	143.88	153.78	163.68	173.58	183.48	193.38	203.28	213.18	223.08	232.98	242.88
WE	6.00	85.52	85.44	95.36	105.27	115.18	125.08	134.98	144.88	154.78	164.68	174.58	184.48	194.38	204.28	214.18	224.08	233.98	243.88
1																			
2																			
3																			



## A TABLE of Natural and

22 DEGREES.

M	N. Sine.	N. Co-Sine.	V. Tangent.	V. Co-Tang.	N. Secant.	N. Co-Secant.
30	3826834	9238795	4112136	21142136	10823222	26131259
31	3829522	9237631	4145544	21122286	10825227	26112922
32	3832229	9236567	4148953	21102465	10826533	26094613
33	3834955	9235452	4152363	21082672	10827449	26076332
34	3837682	9234336	4155774	21062866	10828459	26058052
35	3840268	9233219	4159186	21043163	10829455	26039852
36	3842953	9232102	4162599	21023457	10830452	26021654
37	3845639	9230985	4166012	21003774	10831451	26003484
38	3848324	9229861	4169426	20984113	10832453	25985311
39	3851005	9228745	4172841	20964490	10833459	25967235
40	3853693	9227624	4176257	20944859	10834472	25949137
41	3856377	9226503	4179674	20925316	10835482	25931077
42	3859066	9225381	4183091	20905769	10836491	25913043
43	3861744	9224254	4186505	20886250	10837500	25895037
44	3864427	9223134	4189922	20866759	10838509	25877053
45	3867110	9222009	4193343	20847293	10839518	25859127
46	3869792	9220884	4196769	20827854	10840527	25841182
47	3872474	9219755	4200191	20808444	10841536	25823254
48	3875156	9218631	4203613	20789065	10842545	25805344
49	3877837	9217503	4207036	20769733	10843554	25787570
50	3880518	9216375	4210461	20750372	10844563	25769753
51	3883199	9215245	4213886	20731053	10845572	25751963
52	3885880	9214116	4217311	20711791	10846581	25734199
53	3888560	9212985	4220736	20692540	10847590	25716452
54	3891239	9211854	4224161	20673316	10848599	25698732
55	3893919	9210722	4227586	20654113	10849608	25681069
56	3896598	9209589	4231011	20634946	10850617	25663412
57	3899277	9208455	4234436	20615801	10851626	25645781
58	3901955	9207322	4237861	20596663	10852635	25628176
59	3904633	9206185	4241286	20577530	10853644	25610599
60	3907311	9205049	4244711	20558424	10854653	25593047
N. Co-Sine.			N. Tangent.			N. Secant.

6 DEGREES.

Latitude 45 Deg. 00 Min. North Declination.

	0	d	2	d	4	d	6	d	8	d	10	d	12	d	14	d	16	d	18	d	20	d	22	d	24
	k,m	k,m	k,m	k,m	k,m	k,m	k,m	k,m	k,m	k,m	k,m	k,m	k,m	k,m	k,m	k,m	k,m	k,m	k,m	k,m	k,m	k,m	k,m	k,m	k,m
SN	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0
1	0.32	1.03	1.73	2.43	3.13	3.83	4.53	5.23	5.93	6.63	7.33	8.03	8.73	9.43	10.13	10.83	11.53	12.23	12.93	13.63	14.33	15.03	15.73	16.43	17.13
2	1.03	2.10	3.17	4.24	5.31	6.38	7.45	8.52	9.59	10.66	11.73	12.80	13.87	14.94	16.01	17.08	18.15	19.22	20.29	21.36	22.43	23.50	24.57	25.64	26.71
3	1.73	3.17	4.61	6.05	7.49	8.93	10.37	11.81	13.25	14.69	16.13	17.57	19.01	20.45	21.89	23.33	24.77	26.21	27.65	29.09	30.53	31.97	33.41	34.85	36.29
4	2.43	4.24	6.05	7.86	9.67	11.48	13.29	15.10	16.91	18.72	20.53	22.34	24.15	25.96	27.77	29.58	31.39	33.20	35.01	36.82	38.63	40.44	42.25	44.06	45.87
5	3.13	5.31	7.49	9.67	11.85	14.03	16.21	18.39	20.57	22.75	24.93	27.11	29.29	31.47	33.65	35.83	38.01	40.19	42.37	44.55	46.73	48.91	51.09	53.27	55.45
6	3.83	6.38	8.93	11.48	14.03	16.58	19.13	21.68	24.23	26.78	29.33	31.88	34.43	36.98	39.53	42.08	44.63	47.18	49.73	52.28	54.83	57.38	59.93	62.48	65.03
7	4.53	7.33	10.13	12.93	15.73	18.53	21.33	24.13	26.93	29.73	32.53	35.33	38.13	40.93	43.73	46.53	49.33	52.13	54.93	57.73	60.53	63.33	66.13	68.93	71.73
8	5.23	8.03	10.83	13.63	16.43	19.23	22.03	24.83	27.63	30.43	33.23	36.03	38.83	41.63	44.43	47.23	50.03	52.83	55.63	58.43	61.23	64.03	66.83	69.63	72.43
9	5.93	8.73	11.53	14.33	17.13	19.93	22.73	25.53	28.33	31.13	33.93	36.73	39.53	42.33	45.13	47.93	50.73	53.53	56.33	59.13	61.93	64.73	67.53	70.33	73.13
10	6.63	9.43	12.23	15.03	17.83	20.63	23.43	26.23	29.03	31.83	34.63	37.43	40.23	43.03	45.83	48.63	51.43	54.23	57.03	59.83	62.63	65.43	68.23	71.03	73.83
11	7.33	10.13	12.93	15.73	18.53	21.33	24.13	26.93	29.73	32.53	35.33	38.13	40.93	43.73	46.53	49.33	52.13	54.93	57.73	60.53	63.33	66.13	68.93	71.73	74.53
12	8.03	10.83	13.63	16.43	19.23	22.03	24.83	27.63	30.43	33.23	36.03	38.83	41.63	44.43	47.23	50.03	52.83	55.63	58.43	61.23	64.03	66.83	69.63	72.43	75.23
13	8.73	11.53	14.33	17.13	19.93	22.73	25.53	28.33	31.13	33.93	36.73	39.53	42.33	45.13	47.93	50.73	53.53	56.33	59.13	61.93	64.73	67.53	70.33	73.13	75.93
14	9.43	12.23	15.03	17.83	20.63	23.43	26.23	29.03	31.83	34.63	37.43	40.23	43.03	45.83	48.63	51.43	54.23	57.03	59.83	62.63	65.43	68.23	71.03	73.83	76.63
15	10.13	13.03	15.83	18.63	21.43	24.23	27.03	29.83	32.63	35.43	38.23	41.03	43.83	46.63	49.43	52.23	55.03	57.83	60.63	63.43	66.23	69.03	71.83	74.63	77.43
16	10.83	13.63	16.43	19.23	22.03	24.83	27.63	30.43	33.23	36.03	38.83	41.63	44.43	47.23	50.03	52.83	55.63	58.43	61.23	64.03	66.83	69.63	72.43	75.23	78.03
17	11.53	14.33	17.13	19.93	22.73	25.53	28.33	31.13	33.93	36.73	39.53	42.33	45.13	47.93	50.73	53.53	56.33	59.13	61.93	64.73	67.53	70.33	73.13	75.93	78.73
18	12.23	15.03	17.83	20.63	23.43	26.23	29.03	31.83	34.63	37.43	40.23	43.03	45.83	48.63	51.43	54.23	57.03	59.83	62.63	65.43	68.23	71.03	73.83	76.63	79.43
19	12.93	15.73	18.53	21.43	24.23	27.03	29.83	32.63	35.43	38.23	41.03	43.83	46.63	49.43	52.23	55.03	57.83	60.63	63.43	66.23	69.03	71.83	74.63	77.43	80.23
20	13.63	16.43	19.23	22.23	25.03	27.83	30.63	33.43	36.23	39.03	41.83	44.63	47.43	50.23	53.03	55.83	58.63	61.43	64.23	67.03	69.83	72.63	75.43	78.23	81.03
21	14.33	17.13	19.93	23.03	25.83	28.63	31.43	34.23	37.03	39.83	42.63	45.43	48.23	51.03	53.83	56.63	59.43	62.23	65.03	67.83	70.63	73.43	76.23	79.03	81.83
22	15.03	17.83	20.63	23.83	26.63	29.43	32.23	35.03	37.83	40.63	43.43	46.23	49.03	51.83	54.63	57.43	60.23	63.03	65.83	68.63	71.43	74.23	77.03	79.83	82.63
23	15.73	18.53	21.43	24.63	27.43	30.23	33.03	35.83	38.63	41.43	44.23	47.03	49.83	52.63	55.43	58.23	61.03	63.83	66.63	69.43	72.23	75.03	77.83	80.63	83.43
24	16.43	19.23	22.23	25.43	28.23	31.03	33.83	36.63	39.43	42.23	45.03	47.83	50.63	53.43	56.23	59.03	61.83	64.63	67.43	70.23	73.03	75.83	78.63	81.43	84.23
25	17.13	19.93	23.03	26.23	29.03	31.83	34.63	37.43	40.23	43.03	45.83	48.63	51.43	54.23	57.03	59.83	62.63	65.43	68.23	71.03	73.83	76.63	79.43	82.23	85.03
26	17.83	20.63	23.83	27.03	29.83	32.63	35.43	38.23	41.03	43.83	46.63	49.43	52.23	55.03	57.83	60.63	63.43	66.23	69.03	71.83	74.63	77.43	80.23	83.03	85.83
27	18.53	21.43	24.63	27.83	30.63	33.43	36.23	39.03	41.83	44.63	47.43	50.23	53.03	55.83	58.63	61.43	64.23	67.03	69.83	72.63	75.43	78.23	81.03	83.83	86.63
28	19.23	22.23	25.43	28.63	31.43	34.23	37.03	39.83	42.63	45.43	48.23	51.03	53.83	56.63	59.43	62.23	65.03	67.83	70.63	73.43	76.23	79.03	81.83	84.63	87.43
29	19.93	23.03	26.23	29.43	32.23	35.03	37.83	40.63	43.43	46.23	49.03	51.83	54.63	57.43	60.23	63.03	65.83	68.63	71.43	74.23	77.03	79.83	82.63	85.43	88.23
30	20.63	23.83	27.03	30.23	33.03	35.83	38.63	41.43	44.23	47.03	49.83	52.63	55.43	58.23	61.03	63.83	66.63	69.43	72.23	75.03	77.83	80.63	83.43	86.23	89.03
31	21.43	24.63	27.83	31.03	33.83	36.63	39.43	42.23	45.03	47.83	50.63	53.43	56.23	59.03	61.83	64.63	67.43	70.23	73.03	75.83	78.63	81.43	84.23	87.03	89.83
32	22.23	25.43	28.63	31.83	34.63	37.43	40.23	43.03	45.83	48.63	51.43	54.23	57.03	59.83	62.63	65.43	68.23	71.03	73.83	76.63	79.43	82.23	85.03	87.83	90.63
33	23.03	26.23	29.43	32.63	35.43	38.23	41.03	43.83	46.63	49.43	52.23	55.03	57.83	60.63	63.43	66.23	69.03	71.83	74.63	77.43	80.23	83.03	85.83	88.63	91.43
34	23.83	27.03	30.23	33.43	36.23	39.03	41.83	44.63	47.43	50.23	53.03	55.83	58.63	61.43	64.23	67.03	69.83	72.63	75.43	78.23	81.03	83.83	86.63	89.43	92.23
35	24.63																								



## A TABLE of Natural and

23 DEGREES.

M	N. Sine.	N. Co-Sine.	N. Tangent.	N. Co-Tang.	N. Secant.	N. Co-Secant.
0	3907311	9255049	4244749	23558524	10853604	2593047
1	3909989	9203912	4248182	23539484	10864946	2575521
2	3912666	9202774	4251616	23520456	10866289	2558022
3	3915343	9201635	4255051	23501481	10867634	2540548
4	3918019	9200496	4258487	23482519	10868979	2523101
5	3920695	9199356	4261924	23463582	10870326	2505680
6	3923371	9198215	4265362	23444672	10871675	2488284
7	3926047	9197073	4268800	23425787	10873024	2470915
8	3928722	9195931	4272239	23406928	10874375	2453571
9	3931397	9194788	4275679	23388095	10875727	2436253
10	3934071	9193644	4279120	23369287	10877080	2418961
11	3936745	9192499	4282562	23350505	10878435	2401694
12	3939419	9191353	4286005	23331748	10879791	2384453
13	3942093	9190207	4289449	23313017	10881148	2367238
14	3944766	9189060	4292894	23294311	10882506	2350048
15	3947439	9187912	4296339	23275630	10883866	2332883
16	3950111	9186763	4299785	23256975	10885227	2315744
17	3952783	9185614	4303232	23238345	10886589	2298630
18	3955455	9184464	4306680	23219740	10887952	2281541
19	3958127	9183313	4310129	23201160	10889317	2264478
20	3960798	9182161	4313579	23182606	10890683	2247440
21	3963469	9181008	4317030	23164076	10892050	2230426
22	3966139	9179855	4320481	23145571	10893418	2213438
23	3968809	9178701	4323933	23127093	10894788	2196467
24	3971479	9177546	4327386	23108636	10896159	2179537
25	3974148	9176390	4330840	23090206	10897531	2162624
26	3976817	9175234	4334295	23071801	10898904	2145735
27	3979486	9174077	4337751	23053420	10890279	2128871
28	3982155	9172919	4341208	23035064	10901615	2112032
29	3984823	9171760	4344666	23016732	10903032	2095218
30	3987491	9170601	4348124	22998425	10904411	2078428
N. Co-Sine.			N. Co-Tang.		N. Co-Secant.	
N. Sine.			N. Tangent.		N. Secant.	

66 DEGREES.

Latitude 46 Deg. 00 Min. North Declination.

Longitude 46 Deg. 00 Min.																North Declination.																
	0	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20	21	22	23	24	25	26	27	28	29	30	
	b. m.	a. b. m.	b. m.	b. m.	b. m.	b. m.	b. m.	b. m.	b. m.	b. m.	b. m.	b. m.	b. m.	b. m.	b. m.	b. m.	b. m.	b. m.	b. m.	b. m.	b. m.	b. m.	b. m.	b. m.	b. m.	b. m.	b. m.	b. m.	b. m.	b. m.	b. m.	
SIN	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	
1	0.32	1.03	1.03	1.03	1.03	1.03	1.03	1.03	1.03	1.03	1.03	1.03	1.03	1.03	1.03	1.03	1.03	1.03	1.03	1.03	1.03	1.03	1.03	1.03	1.03	1.03	1.03	1.03	1.03	1.03	1.03	
2	1.05	2.10	2.10	2.10	2.10	2.10	2.10	2.10	2.10	2.10	2.10	2.10	2.10	2.10	2.10	2.10	2.10	2.10	2.10	2.10	2.10	2.10	2.10	2.10	2.10	2.10	2.10	2.10	2.10	2.10	2.10	
3	1.43	3.14	3.14	3.14	3.14	3.14	3.14	3.14	3.14	3.14	3.14	3.14	3.14	3.14	3.14	3.14	3.14	3.14	3.14	3.14	3.14	3.14	3.14	3.14	3.14	3.14	3.14	3.14	3.14	3.14	3.14	
4	2.23	4.24	4.24	4.24	4.24	4.24	4.24	4.24	4.24	4.24	4.24	4.24	4.24	4.24	4.24	4.24	4.24	4.24	4.24	4.24	4.24	4.24	4.24	4.24	4.24	4.24	4.24	4.24	4.24	4.24	4.24	
5	3.03	5.03	5.03	5.03	5.03	5.03	5.03	5.03	5.03	5.03	5.03	5.03	5.03	5.03	5.03	5.03	5.03	5.03	5.03	5.03	5.03	5.03	5.03	5.03	5.03	5.03	5.03	5.03	5.03	5.03	5.03	
6	4.00	6.34	6.34	6.34	6.34	6.34	6.34	6.34	6.34	6.34	6.34	6.34	6.34	6.34	6.34	6.34	6.34	6.34	6.34	6.34	6.34	6.34	6.34	6.34	6.34	6.34	6.34	6.34	6.34	6.34	6.34	
7	4.55	7.41	7.41	7.41	7.41	7.41	7.41	7.41	7.41	7.41	7.41	7.41	7.41	7.41	7.41	7.41	7.41	7.41	7.41	7.41	7.41	7.41	7.41	7.41	7.41	7.41	7.41	7.41	7.41	7.41	7.41	
WE	6.00	8.52	8.52	8.52	8.52	8.52	8.52	8.52	8.52	8.52	8.52	8.52	8.52	8.52	8.52	8.52	8.52	8.52	8.52	8.52	8.52	8.52	8.52	8.52	8.52	8.52	8.52	8.52	8.52	8.52	8.52	
1																																
2																																
3																																

## Artificial Sines, Tangents, and Secants.

23 DEGREES.

M	L. Sine.	L. Co-Sine.	L. Tangent.	L. Co-Tang.	L. Secant.	L. Co-Secant.
0	9.9218780	9.9640261	9.6278519	10.3721481	10.0359739	10.4031220
1	9.9217555	9.9639724	9.6282031	10.3717969	10.0360276	10.4078243
2	9.9216330	9.9639187	9.6285543	10.3714460	10.0360813	10.4075272
3	9.9215105	9.9638650	9.6289055	10.3710952	10.0361350	10.4072302
4	9.9213880	9.9638112	9.6292567	10.3707447	10.0361888	10.4069334
5	9.9212655	9.9637574	9.6296079	10.3703943	10.0362426	10.4066366
6	9.9211430	9.9637036	9.6299591	10.3700442	10.0362964	10.4063398
7	9.9210205	9.9636498	9.6303103	10.3696942	10.0363504	10.4060445
8	9.9208980	9.9635959	9.6306615	10.3693444	10.0364043	10.4057487
9	9.9207755	9.9635421	9.6310127	10.3689948	10.0364583	10.4054531
10	9.9206530	9.9634882	9.6313639	10.3686455	10.0365123	10.4051578
11	9.9205305	9.9634343	9.6317151	10.3682963	10.0365664	10.4048627
12	9.9204080	9.9633805	9.6320663	10.3679473	10.0366205	10.4045678
13	9.9202855	9.9633266	9.6324175	10.3675985	10.0366747	10.4042732
14	9.9201630	9.9632727	9.6327687	10.3672499	10.0367289	10.4039787
15	9.9200405	9.9632188	9.6331200	10.3669015	10.0367832	10.4036845
16	9.9199180	9.9631649	9.6334712	10.3665532	10.0368375	10.4033907
17	9.9197955	9.9631110	9.6338225	10.3662052	10.0368918	10.4030970
18	9.9196730	9.9630571	9.6341737	10.3658574	10.0369462	10.4028035
19	9.9195505	9.9630032	9.6345250	10.3655097	10.0370006	10.4025103
20	9.9194280	9.9629493	9.6348762	10.3651622	10.0370551	10.4022177
21	9.9193055	9.9628954	9.6352275	10.3648150	10.0371096	10.4019246
22	9.9191830	9.9628415	9.6355787	10.3644679	10.0371642	10.4016318
23	9.9190605	9.9627876	9.6359300	10.3641210	10.0372188	10.4013393
24	9.9189380	9.9627337	9.6362812	10.3637743	10.0372734	10.4010477
25	9.9188155	9.9626798	9.6366325	10.3634298	10.0373281	10.4007559
26	9.9186930	9.9626259	9.6369837	10.3630851	10.0373828	10.4004643
27	9.9185705	9.9625720	9.6373350	10.3627406	10.0374376	10.4001730
28	9.9184480	9.9625181	9.6376862	10.3623964	10.0374924	10.3998819
29	9.9183255	9.9624642	9.6380375	10.3620527	10.0375473	10.3995910
30	9.9182030	9.9624103	9.6383887	10.3617091	10.0376022	10.3993003
L. Co-Sine.			L. Tangent.		L. Secant.	
L. Sine.			L. Co-Tang.		L. Co-Secant.	

66 DEGREES.

Latitude 46 Deg. 00 Min. South Declination.

		48 Deg. 00 Min. South Declination.																							
0		d. 2	d. 4	d. 6	d. 8	d. 10	d. 12	d. 14	d. 16	d. 18	d. 20	d. 22	d. 24												
b. m.		m. b. m.	m. b. m.	m. b. m.	m. b. m.	m. b. m.	m. b. m.	m. b. m.	m. b. m.	m. b. m.	m. b. m.	m. b. m.	m. b. m.												
SIN	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0												
1	0.33	1.04	1.04	1.04	1.04	1.04	1.04	1.04	1.04	1.04	1.04	1.04	1.04												
2	1.06	2.10	2.10	2.10	2.10	2.10	2.10	2.10	2.10	2.10	2.10	2.10	2.10												
3	1.43	3.14	3.14	3.14	3.14	3.14	3.14	3.14	3.14	3.14	3.14	3.14	3.14												
4	2.23	4.27	4.27	4.27	4.27	4.27	4.27	4.27	4.27	4.27	4.27	4.27	4.27												
5	3.08	5.13	5.13	5.13	5.13	5.13	5.13	5.13	5.13	5.13	5.13	5.13	5.13												
6	4.00	6.46	6.46	6.46	6.46	6.46	6.46	6.46	6.46	6.46	6.46	6.46	6.46												
7	4.58	7.50	7.50	7.50	7.50	7.50	7.50	7.50	7.50	7.50	7.50	7.50	7.50												
WE																									



23 DEGREES.

N	N. Sine.	N. Co-Sine.	N. Tangent.	V. Co-Tang.	N. Secant.	N. Co-Secant.	
30	3987491	9170601	4348124	22998425	10924411	25078463	30
31	3990158	9169441	4351583	22998143	10925791	25076166	29
32	3992825	9168280	4355043	22997858	10927172	25073893	28
33	3995492	9167118	4358504	22997573	10928554	25071625	27
34	3998158	9165955	4361966	22997287	10929938	25069361	26
35	4000824	9164791	4365429	22997002	10931323	24994477	25
36	4003490	9163627	4368893	22996716	10932709	24979584	24
37	4006156	9162462	4372357	22996430	10934097	24964696	23
38	4008821	9161296	4375821	22996145	10935486	24949801	22
39	4011486	9160130	4379285	22995859	10936876	24934909	21
40	4014150	9158963	4382750	22995573	10938267	24919974	20
41	4016814	9157795	4386214	22995288	10939659	24905035	19
42	4019478	9156626	4389679	22995002	10941053	24890094	18
43	4022141	9155456	4393143	22994717	10922448	24875256	17
44	4024804	9154286	4396608	22994431	10923845	24860429	16
45	4027467	9153115	4400072	22994145	10925233	24845603	15
46	4030129	9151944	4403537	22993859	10926622	24830778	14
47	4032791	9150773	4407001	22993573	10928012	24815954	13
48	4035453	9149602	4410465	22993287	10929404	24801131	12
49	4038114	9148431	4413929	22993002	10930797	24786309	11
50	4040775	9147260	4417393	22992716	10932191	24771486	10
51	4043436	9146089	4420857	22992430	10933585	24756663	9
52	4046096	9144918	4424321	22992145	10934980	24741840	8
53	4048756	9143746	4427785	22991859	10936374	24727017	7
54	4051415	9142575	4431250	22991573	10937769	24712194	6
55	4054075	9141404	4434714	22991287	10939164	24697371	5
56	4056734	9140233	4438179	22991002	10940560	24682548	4
57	4059393	9139062	4441643	22990716	10941956	24667725	3
58	4062051	9137891	4445107	22990430	10943353	24652902	2
59	4064709	9136720	4448571	22990145	10944749	24638079	1
60	4067366	9135549	4452035	22989859	10946146	24623256	0
N. Co-Sine.	N. Sine.	N. Co-Sine.	N. Co-Secant.	N. Tangent.	N. Co-Secant.	N. Secant.	

## 66 DEGREES.

Latitude 47 Deg. 00 Min. North Declination.

	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20	21	22	23	24
	<i>k, m</i>	<i>k, m</i>	<i>k, m</i>	<i>k, m</i>	<i>k, m</i>	<i>k, m</i>	<i>k, m</i>	<i>k, m</i>	<i>k, m</i>	<i>k, m</i>	<i>k, m</i>	<i>k, m</i>	<i>k, m</i>	<i>k, m</i>	<i>k, m</i>	<i>k, m</i>	<i>k, m</i>	<i>k, m</i>	<i>k, m</i>	<i>k, m</i>	<i>k, m</i>	<i>k, m</i>	<i>k, m</i>	<i>k, m</i>
1	12	12	12	12	12	12	12	12	12	12	12	12	12	12	12	12	12	12	12	12	12	12	12	12
2	10	10	10	10	10	10	10	10	10	10	10	10	10	10	10	10	10	10	10	10	10	10	10	10
3	14	14	14	14	14	14	14	14	14	14	14	14	14	14	14	14	14	14	14	14	14	14	14	14
4	16	16	16	16	16	16	16	16	16	16	16	16	16	16	16	16	16	16	16	16	16	16	16	16
5	18	18	18	18	18	18	18	18	18	18	18	18	18	18	18	18	18	18	18	18	18	18	18	18
6	20	20	20	20	20	20	20	20	20	20	20	20	20	20	20	20	20	20	20	20	20	20	20	20
7	22	22	22	22	22	22	22	22	22	22	22	22	22	22	22	22	22	22	22	22	22	22	22	22
8	24	24	24	24	24	24	24	24	24	24	24	24	24	24	24	24	24	24	24	24	24	24	24	24
9	26	26	26	26	26	26	26	26	26	26	26	26	26	26	26	26	26	26	26	26	26	26	26	26
10	28	28	28	28	28	28	28	28	28	28	28	28	28	28	28	28	28	28	28	28	28	28	28	28
11	30	30	30	30	30	30	30	30	30	30	30	30	30	30	30	30	30	30	30	30	30	30	30	30
12	32	32	32	32	32	32	32	32	32	32	32	32	32	32	32	32	32	32	32	32	32	32	32	32
13	34	34	34	34	34	34	34	34	34	34	34	34	34	34	34	34	34	34	34	34	34	34	34	34
14	36	36	36	36	36	36	36	36	36	36	36	36	36	36	36	36	36	36	36	36	36	36	36	36
15	38	38	38	38	38	38	38	38	38	38	38	38	38	38	38	38	38	38	38	38	38	38	38	38
16	40	40	40	40	40	40	40	40	40	40	40	40	40	40	40	40	40	40	40	40	40	40	40	40
17	42	42	42	42	42	42	42	42	42	42	42	42	42	42	42	42	42	42	42	42	42	42	42	42
18	44	44	44	44	44	44	44	44	44	44	44	44	44	44	44	44	44	44	44	44	44	44	44	44
19	46	46	46	46	46	46	46	46	46	46	46	46	46	46	46	46	46	46	46	46	46	46	46	46
20	48	48	48	48	48	48	48	48	48	48	48	48	48	48	48	48	48	48	48	48	48	48	48	48
21	50	50	50	50	50	50	50	50	50	50	50	50	50	50	50	50	50	50	50	50	50	50	50	50
22	52	52	52	52	52	52	52	52	52	52	52	52	52	52	52	52	52	52	52	52	52	52	52	52
23	54	54	54	54	54	54	54	54	54	54	54	54	54	54	54	54	54	54	54	54	54	54	54	54
24	56	56	56	56	56	56	56	56	56	56	56	56	56	56	56	56	56	56	56	56	56	56	56	56

## 23 DEGREES.

[illegible]

## 66 DEGREES.

## Latitude 47 Deg. 00 Min. South Declination.

[illegible]



## 24 DEGREES.

M	N. Sine.	N. Co-Sine.	N. Tangent.	N. Co-Tangent.	N. Secant.	N. Co-Secant.
0	4067366	9135454	4452237	2246368	10946363	24585933
1	4070023	9134271	4455773	22442796	10947781	24569882
2	4072680	9133087	4459260	22421427	10949201	24553853
3	4075337	9131902	4462748	224007721	10950622	24537848
4	4077993	9130716	4466237	22380218	10952044	24521865
5	4080649	9129529	4469727	22359738	10953467	24505905
6	4083305	9128342	4473217	22339260	10954892	24489968
7	4085960	9127154	4476708	22318785	10956318	24474054
8	4088616	9125965	4480200	22298313	10957746	24458163
9	4091269	9124775	4483693	22277844	10959174	24442294
10	4093923	9123584	4487187	22257376	10960604	24426448
11	4096577	9122393	4490682	22236911	10962036	24410624
12	4099230	9121201	4494175	22216443	10963468	24394823
13	4101883	9120008	4497675	22195979	10964902	24379045
14	4104536	9118814	4501173	22175512	10966337	24363289
15	4107189	9117620	4504672	22155047	10967774	24347555
16	4109841	9116425	4508172	22134584	10969212	24331844
17	4112493	9115229	4511673	22114122	10970651	24316155
18	4115144	9114032	4515174	22093661	10972091	24300490
19	4117795	9112835	4518675	22073202	10973533	24284844
20	4120446	9111637	4522176	22052744	10974976	24269200
21	4123096	9110438	4525678	22032287	10976420	24253562
22	4125746	9109238	4529180	22011831	10977866	24237928
23	4128395	9108038	4532682	22001374	10979313	24222288
24	4131044	9106837	4536184	21980918	10980761	24206654
25	4133693	9105635	4539687	21960463	10982211	24191022
26	4136342	9104432	4543189	21940008	10983662	24175392
27	4138990	9103228	4546692	21919554	10985114	24160048
28	4141638	9102024	4550195	21899101	10986568	24144693
29	4144285	9100819	4553697	21878648	10988023	24129331
30	4146932	9099613	4557200	21858195	10989479	24113970

65 DEGREES.

## Latitude 48 Deg. 00 Min. North Declination.

	0	d.	2	d.	4	d.	6	d.	8	d.	10	d.	12	d.	14	d.	16	d.	18	d.	20	d.	22	d.	24
	b. m.	n.	b. m.	n.	b. m.	n.	b. m.	n.	b. m.	n.	b. m.	n.	b. m.	n.	b. m.	n.	b. m.	n.	b. m.	n.	b. m.	n.	b. m.	n.	b. m.
1	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0
2	1.34	2.32	1.35	1.33	1.36	1.34	1.37	1.35	1.38	1.36	1.39	1.37	1.40	1.38	1.41	1.39	1.42	1.40	1.43	1.41	1.44	1.42	1.45	1.43	1.46
3	1.46	2.44	1.47	1.45	1.48	1.46	1.49	1.47	1.50	1.48	1.51	1.49	1.52	1.50	1.53	1.51	1.54	1.52	1.55	1.53	1.56	1.54	1.57	1.55	1.58
4	2.26	2.21	2.27	2.23	2.33	2.29	2.39	2.35	2.49	2.45	2.59	2.55	3.13	3.09	3.27	3.23	3.45	3.41	3.67	3.63	3.91	3.87	4.17	4.13	4.43
5	3.12	3.05	3.19	3.13	3.33	3.27	3.51	3.45	3.75	3.69	4.05	3.99	4.39	4.33	4.73	4.67	5.17	5.11	5.71	5.65	6.27	6.21	6.93	6.87	7.61
6	4.03	3.95	4.19	4.13	4.43	4.37	4.73	4.67	5.17	5.11	5.61	5.55	6.11	6.05	6.67	6.61	7.33	7.27	8.07	8.01	8.93	8.87	9.91	9.85	10.99
7	5.00	4.91	5.15	5.09	5.45	5.39	5.85	5.79	6.35	6.29	6.87	6.81	7.51	7.45	8.23	8.17	9.07	9.01	10.07	10.01	11.23	11.17	12.59	12.53	14.11
8	6.00	5.91	6.15	6.09	6.55	6.49	7.05	6.99	7.65	7.59	8.27	8.21	9.03	8.97	9.87	9.81	10.91	10.85	12.13	12.07	13.47	13.41	15.03	14.97	16.79
9	7.00	6.91	7.15	7.09	7.65	7.59	8.27	8.21	9.03	8.97	9.87	9.81	10.91	10.85	12.13	12.07	13.47	13.41	15.03	14.97	16.79	16.73	18.57	18.51	20.59
10	8.00	7.91	8.15	8.09	8.75	8.69	9.47	9.41	10.33	10.27	11.33	11.27	12.47	12.41	13.83	13.77	15.43	15.37	17.33	17.27	19.43	19.37	22.19	22.13	25.19
11	9.00	8.91	9.15	9.09	9.95	9.89	10.87	10.81	12.03	11.97	13.33	13.27	14.83	14.77	16.57	16.51	18.63	18.57	21.03	20.97	23.83	23.77	27.19	27.13	30.99
12	10.00	9.91	10.15	10.09	11.15	11.09	12.33	12.27	13.73	13.67	15.33	15.27	17.13	17.07	19.23	19.17	21.73	21.67	24.73	24.67	28.23	28.17	32.39	32.33	37.19
13	11.00	10.91	11.15	11.09	12.33	12.27	13.73	13.67	15.33	15.27	17.13	17.07	19.23	19.17	21.73	21.67	24.73	24.67	28.23	28.17	32.39	32.33	37.19	37.13	42.19
14	12.00	11.91	12.15	12.09	13.55	13.49	15.13	15.07	16.93	16.87	18.93	18.87	21.13	21.07	23.53	23.47	26.33	26.27	29.63	29.57	33.93	33.87	39.19	39.13	45.19
15	13.00	12.91	13.15	13.09	15.15	15.09	16.93	16.87	18.93	18.87	21.13	21.07	23.53	23.47	26.33	26.27	29.63	29.57	33.93	33.87	39.19	39.13	45.19	45.13	51.19
16	14.00	13.91	14.15	14.09	16.55	16.49	18.43	18.37	20.53	20.47	22.93	22.87	25.53	25.47	28.63	28.57	32.23	32.17	36.33	36.27	41.39	41.33	47.19	47.13	53.19
17	15.00	14.91	15.15	15.09	18.15	18.09	20.33	20.27	22.73	22.67	25.33	25.27	28.13	28.07	31.33	31.27	35.13	35.07	39.33	39.27	44.59	44.53	50.19	50.13	56.19
18	16.00	15.91	16.15	16.09	19.95	19.89	22.33	22.27	24.93	24.87	27.73	27.67	30.73	30.67	34.13	34.07	38.13	38.07	42.53	42.47	47.99	47.93	53.59	53.53	59.59
19	17.00	16.91	17.15	17.09	21.95	21.89	24.73	24.67	27.53	27.47	30.53	30.47	33.73	33.67	37.33	37.27	41.53	41.47	46.13	46.07	51.19	51.13	56.99	56.93	62.99
20	18.00	17.91	18.15	18.09	24.15	24.09	26.93	26.87	29.93	29.87	32.93	32.87	36.13	36.07	40.13	40.07	44.33	44.27	48.93	48.87	54.19	54.13	60.19	60.13	66.19
21	19.00	18.91	19.15	19.09	26.55	26.49	29.33	29.27	32.13	32.07	35.13	35.07	38.33	38.27	42.13	42.07	46.53	46.47	51.33	51.27	56.59	56.53	62.59	62.53	68.59
22	20.00	19.91	20.15	20.09	29.15	29.09	31.93	31.87	34.73	34.67	37.73	37.67	40.93	40.87	45.13	45.07	49.53	49.47	54.13	54.07	59.39	59.33	65.39	65.33	71.39
23	21.00	20.91	21.15	21.09	31.95	31.89	34.73	34.67	37.73	37.67	40.93	40.87	44.13	44.07	48.33	48.27	52.93	52.87	57.33	57.27	62.59	62.53	68.59	68.53	74.59
24	22.00	21.91	22.15	22.09	34.95	34.89	37.73	37.67	40.93	40.87	44.13	44.07	47.33	47.27	51.53	51.47	55.93	55.87	60.33	60.27	65.59	65.53	71.59	71.53	77.59

## 24 DEGREES.

24 DEGREES.						
M	L. Sine.	L. Co-Sine.	L. Tangent.	L. Co-Tang.	L. Secant.	L. Co-Secant.
0	9.6093133	9.9607302	9.6485831	10.3514169	10.0392698	10.3906657
1	9.6093969	9.9606739	9.6486230	10.3510770	10.0393261	10.3904031
2	9.6094803	9.9606176	9.6486628	10.3507372	10.0393824	10.3901197
3	9.6101635	9.9605612	9.6487023	10.3503977	10.0394388	10.3898365
4	9.6104465	9.9605048	9.6487417	10.3500583	10.0394951	10.3895535
5	9.6107293	9.9604484	9.6487810	10.3497191	10.0395516	10.3892707
6	9.6110118	9.9603919	9.6488200	10.3493801	10.0396081	10.3889882
7	9.6112941	9.9603354	9.6488587	10.3490413	10.0396646	10.3887055
8	9.6115762	9.9602789	9.6488973	10.3487026	10.0397212	10.3884228
9	9.6118580	9.9602222	9.6489359	10.3483641	10.0397778	10.3881402
10	9.6121397	9.9601655	9.6489744	10.3480258	10.0398345	10.3878576
11	9.6124211	9.9601088	9.6490128	10.3476877	10.0398912	10.3875750
12	9.6127023	9.9600520	9.6490511	10.3473497	10.0399480	10.3872927
13	9.6129833	9.9599952	9.6490894	10.3470119	10.0400048	10.3870107
14	9.6132641	9.9599384	9.6491275	10.3466743	10.0400616	10.3867289
15	9.6135446	9.9598815	9.6491656	10.3463369	10.0401185	10.3864465
16	9.6138250	9.9598246	9.6492036	10.3459996	10.0401754	10.3861640
17	9.6141051	9.9597676	9.6492415	10.3456625	10.0402324	10.3858816
18	9.6143850	9.9597106	9.6492794	10.3453256	10.0402894	10.3855994
19	9.6146647	9.9596535	9.6493172	10.3449888	10.0403465	10.3853172
20	9.6149441	9.9595964	9.6493549	10.3446523	10.0404036	10.3850350
21	9.6152234	9.9595392	9.6493926	10.3443159	10.0404607	10.3847528
22	9.6155024	9.9594821	9.6494302	10.3439795	10.0405178	10.3844706
23	9.6157812	9.9594248	9.6494678	10.3436435	10.0405749	10.3841884
24	9.6160599	9.9593675	9.6495053	10.3433077	10.0406320	10.3839062
25	9.6163385	9.9593102	9.6495428	10.3429720	10.0406891	10.3836240
26	9.6166169	9.9592529	9.6495802	10.3426364	10.0407462	10.3833418
27	9.6168954	9.9591954	9.6496176	10.3423011	10.0408033	10.3830596
28	9.6171721	9.9591380	9.6496549	10.3419659	10.0408604	10.3827773
29	9.6174496	9.9590805	9.6496923	10.3416310	10.0409175	10.3824950
30	9.6177272	9.9590229	9.6497297	10.3412956	10.0409746	10.3822127
	L. Co-Tang.	L. Sine.	L. Tangent.	L. Secant.	L. Co-Secant.	M



## 24 DEGREES.

M	N. Sine.	N. Co-Sine.	N. Tangent.	N. Co-Tang.	N. Secant.	N. Co-Secant.
30	4146932	9099613	4557264	21942997	10989479	24114210
31	4149579	9098406	4560777	21926393	10990936	24098829
32	4152262	9097198	4564291	21909216	10992395	24083469
33	4154872	9095990	4567806	21892349	10993855	24068132
34	4157518	9094781	4571322	2187510	10995317	24052815
35	4160163	9093571	4574839	21858691	10996779	24037520
36	4162808	9092361	4578357	21841894	10998243	24022247
37	4165453	9091150	4581876	21825119	10999709	24006995
38	4168097	9089938	4585396	21808363	11001176	23991764
39	4170741	9088725	4588917	21791631	11002644	23976555
40	4173385	9087511	4592439	21774920	11004113	23961367
41	4176028	9086297	4595962	21758229	11005584	23946201
42	4178671	9085082	4599486	21741559	11007056	23931055
43	4181313	9083866	4603011	21724911	11008529	23915931
44	4183955	9082649	4606537	21708283	11010004	23900828
45	4186597	9081432	4610064	21691677	11011480	23885746
46	4189239	9080214	4613591	21675091	11012957	23870683
47	4191880	9078995	4617119	21658527	11014436	23855645
48	4194521	9077775	4620648	21641983	11015916	23840622
49	4197161	9076554	4624178	21625460	11017397	23825627
50	4199801	9075333	4627709	21608958	11018879	23810650
51	4202441	9074111	4631242	21592476	11020363	23795693
52	4205080	9072888	4634776	21576015	11021849	23780758
53	4207719	9071664	4638311	21559575	11023335	23765843
54	4210358	9070440	4641846	21543156	11024823	23750949
55	4212996	9069215	4645382	21526757	11026313	23736075
56	4215634	9067990	4648919	21510378	11027803	23721222
57	4218272	9066762	4652457	21494020	11029295	23706390
58	4220909	9065533	4655996	21477683	11030789	23691578
59	4223546	9064307	4659536	21461366	11032283	23676787
60	4226183	9063078	4663077	21445069	11033779	23662016
N. Co-Sine. N. Sine. N. Co-Tang. N. Tangent. N. Co-Secant. N. Secant. M						

## 65 DEGREES.

## Latitude 49 Deg. 00 Min. North Declination.

	0	d. 2	d. 4	d. 6	d. 8	d. 10	d. 12	d. 14	d. 16	d. 18	d. 20	d. 22	d. 24
S N	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0
1	0.34	1.033	1.032	1.031	1.030	1.029	1.028	1.027	1.026	1.025	1.024	1.023	1.022
2	1.09	2.107	2.105	2.103	2.101	2.099	2.097	2.095	2.093	2.091	2.089	2.087	2.085
3	1.47	3.144	3.141	3.138	3.135	3.131	3.128	3.125	3.122	3.119	3.116	3.113	3.110
4	2.28	4.224	4.220	4.216	4.212	4.207	4.203	4.199	4.195	4.191	4.187	4.183	4.179
5	3.14	5.309	5.304	5.299	5.294	5.289	5.284	5.279	5.274	5.269	5.264	5.259	5.254
6	4.05	6.459	6.453	6.447	6.441	6.434	6.428	6.421	6.414	6.407	6.400	6.393	6.386
7	5.01	8.458	8.451	8.444	8.437	8.429	8.421	8.413	8.405	8.397	8.389	8.381	8.373
WE	6.00	10.53	10.52	10.51	10.50	10.49	10.48	10.47	10.46	10.45	10.44	10.43	10.42
1					6.32	7.525	7.618	7.611	7.604	8.596	8.548	8.540	8.534
2									7.07	8.659	8.651	8.643	8.638
3												7.45	8.740

## Artificial Sines, Tangents, and Secants.

## 24 DEGREES.

M	N. Sine.	L. Co-Sine.	L. Tangent.	L. Co-Tang.	L. Secant.	L. Co-Secant.
30	9.6177270	9.9590229	9.6587041	10.3412950	10.0409771	10.3822730
31	9.6180041	9.9589633	9.6590387	10.3409613	10.0410347	10.3819959
32	9.6182809	9.9589077	9.6593733	10.3406267	10.0410923	10.3817191
33	9.6185576	9.9588500	9.6597076	10.3402924	10.0411500	10.3814424
34	9.6188341	9.9587923	9.6600418	10.3399582	10.0412077	10.3811659
35	9.6191103	9.9587345	9.6603765	10.3396242	10.0412655	10.3808897
36	9.6193864	9.9586777	9.6607109	10.3392902	10.0413233	10.3806136
37	9.6196622	9.9586218	9.6610454	10.3389566	10.0413812	10.3803378
38	9.6199378	9.9585659	9.6613799	10.3386231	10.0414391	10.3800622
39	9.6202132	9.9585093	9.6617103	10.3382897	10.0414970	10.3797868
40	9.6204884	9.9584525	9.6620434	10.3379566	10.0415550	10.3795116
41	9.6207634	9.9583958	9.6623765	10.3376235	10.0416131	10.3792366
42	9.6210382	9.9583388	9.6627093	10.3372907	10.0416712	10.3789619
43	9.6213127	9.9582817	9.6630420	10.3369580	10.0417293	10.3786873
44	9.6215871	9.9582245	9.6633745	10.3366255	10.0417875	10.3784129
45	9.6218612	9.9581673	9.6637069	10.3362931	10.0418457	10.3781388
46	9.6221351	9.9581100	9.6640391	10.3359609	10.0419039	10.3778649
47	9.6224088	9.9580527	9.6643711	10.3356289	10.0419622	10.3775913
48	9.6226824	9.9579954	9.6647030	10.3352970	10.0420206	10.3773176
49	9.6229557	9.9579381	9.6650346	10.3349654	10.0420790	10.3770443
50	9.6232287	9.9578808	9.6653662	10.3346338	10.0421374	10.3767713
51	9.6235016	9.9578234	9.6656975	10.3343025	10.0421959	10.3764984
52	9.6237743	9.9577659	9.6660288	10.3339712	10.0422544	10.3762257
53	9.6240469	9.9577084	9.6663600	10.3336402	10.0423130	10.3759532
54	9.6243190	9.9576508	9.6666907	10.3333093	10.0423716	10.3756810
55	9.6245911	9.9575932	9.6670214	10.3329786	10.0424303	10.3754089
56	9.6248629	9.9575355	9.6673519	10.3326481	10.0424890	10.3751371
57	9.6251346	9.9574778	9.6676823	10.3323177	10.0425478	10.3748654
58	9.6254060	9.9574199	9.6680126	10.3319874	10.0426066	10.3745940
59	9.6256772	9.9573620	9.6683426	10.3316574	10.0426654	10.3743228
60	9.6259483	9.9573039	9.6686725	10.3313275	10.0427243	10.3740517
L. Co-Sine. L. Sine. L. Co-Tang. L. Tangent. L. Co-Secant. L. Secant. M						

## 65 DEGREES.

## Latitude 49 Deg. 00 Min. South Declination.

	0	d. 2	d. 4	d. 6	d. 8	d. 10	d. 12	d. 14	d. 16	d. 18	d. 20	d. 22	d. 24
S N	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0
1	0.34	1.033	1.032	1.031	1.030	1.029	1.028	1.027	1.026	1.025	1.024	1.023	1.022
2	1.09	2.111	2.109	2.107	2.105	2.103	2.101	2.099	2.097	2.095	2.093	2.091	2.089
3	1.47	3.150	3.147	3.144	3.141	3.137	3.134	3.131	3.128	3.125	3.122	3.119	3.116
4	2.28	4.230	4.226	4.222	4.218	4.214	4.210	4.206	4.202	4.198	4.194	4.190	4.186
5	3.14	5.319	5.314	5.309	5.304	5.299	5.294	5.289	5.284	5.279	5.274	5.269	5.264
6	4.05	6.411	6.404	6.397	6.390	6.383	6.376	6.369	6.362	6.355	6.348	6.341	6.334
7	5.01	8.410	8.402	8.394	8.386	8.378	8.370	8.362	8.354	8.346	8.338	8.330	8.322
WE													



## 25 DEGREES.

M	N. Sine.	N. Co-Sine.	N. Tangent.	N. Co-Tang.	N. Secant.	N. Co-Secant.	
0	4226183	9563078	4653077	2144509	1193779	23662016	60
1	4228819	9561848	4666619	2142873	11935277	23647265	59
2	4231455	9560617	4679162	2141257	11932775	23632535	58
3	4234090	9559386	4691705	2139630	11930275	23617826	57
4	4236725	9558154	4704248	2138003	11927777	23603136	56
5	4239360	9556921	4716791	2136376	11925279	23588446	55
6	4241994	9555688	4729334	2134749	11922783	23573756	54
7	4244628	9554455	4741877	2133122	11920289	23559066	53
8	4247262	9553221	4754420	2131495	11917793	23544376	52
9	4249895	9551988	4766963	2129868	11915297	23529686	51
10	4252528	9550755	4779506	2128241	11912801	23514996	50
11	4255161	9549521	4792049	2126614	11910305	23500306	49
12	4257794	9548288	4804592	2124987	11907809	23485616	48
13	4260428	9547055	4817135	2123360	11905313	23470926	47
14	4263061	9545821	4829678	2121733	11902817	23456236	46
15	4265694	9544588	4842221	2120106	11900321	23441546	45
16	4268328	9543355	4854764	2118479	11897825	23426856	44
17	4270961	9542121	4867307	2116852	11895329	23412166	43
18	4273594	9540888	4879850	2115225	11892833	23397476	42
19	4276228	9539655	4892393	2113598	11890337	23382786	41
20	4278861	9538421	4904936	2111971	11887841	23368096	40
21	4281494	9537188	4917479	2110344	11885345	23353406	39
22	4284128	9535955	4930022	2108717	11882849	23338716	38
23	4286761	9534721	4942565	2107090	11880353	23324026	37
24	4289394	9533488	4955108	2105463	11877857	23309336	36
25	4292028	9532255	4967651	2103836	11875361	23294646	35
26	4294661	9531021	4980194	2102209	11872865	23279956	34
27	4297293	9529788	4992737	2100582	11870369	23265266	33
28	4300929	9528555	5005280	2098956	11867873	23250576	32
29	4304565	9527321	5017823	2097329	11865377	23235886	31
30	4308201	9526088	5029875	2095646	11862881	23221196	30
	V. Co-Sine	N. Sine.	N. Co-Tang	N. Tangent.	N. Co-Secant.	N. Secant.	M

64 DEGREES.

Latitude 50 Deg. 00 Min. North Declination.

	0	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20	21	22	23	24	25
SIN	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0
1	0.35	1.0.34	1.0.33	1.0.32	1.0.31	1.0.30	1.0.29	1.0.28	1.0.27	1.0.26	1.0.25	1.0.24	1.0.23	1.0.22	1.0.21	1.0.20	1.0.19	1.0.18	1.0.17	1.0.16	1.0.15	1.0.14	1.0.13	1.0.12	1.0.11	1.0.10
2	1.16	2.1.08	2.1.06	2.1.04	2.1.02	2.1.00	2.0.58	2.0.56	2.0.54	2.0.52	2.0.50	2.0.48	2.0.46	2.0.44	2.0.42	2.0.40	2.0.38	2.0.36	2.0.34	2.0.32	2.0.30	2.0.28	2.0.26	2.0.24	2.0.22	2.0.20
3	1.48	3.1.45	3.1.42	3.1.39	3.1.36	3.1.33	3.1.30	3.1.27	3.1.24	3.1.21	3.1.18	3.1.15	3.1.12	3.1.09	3.1.06	3.1.03	3.1.00	3.0.57	3.0.54	3.0.51	3.0.48	3.0.45	3.0.42	3.0.39	3.0.36	3.0.33
4	2.30	4.2.26	4.2.22	4.2.18	4.2.14	4.2.10	4.2.05	4.2.01	4.1.57	4.1.52	4.1.47	4.1.42	4.1.37	4.1.32	4.1.27	4.1.22	4.1.17	4.1.12	4.1.07	4.1.02	4.0.57	4.0.52	4.0.47	4.0.42	4.0.37	4.0.32
5	3.16	5.3.11	5.3.06	5.3.01	5.2.56	5.2.50	5.2.45	5.2.40	5.2.35	5.2.30	5.2.25	5.2.20	5.2.15	5.2.10	5.2.05	5.2.00	5.1.55	5.1.50	5.1.45	5.1.40	5.1.35	5.1.30	5.1.25	5.1.20	5.1.15	5.1.10
6	4.06	6.4.00	6.3.54	6.3.48	6.3.42	6.3.36	6.3.30	6.3.24	6.3.18	6.3.12	6.3.06	6.3.00	6.2.54	6.2.48	6.2.42	6.2.36	6.2.30	6.2.24	6.2.18	6.2.12	6.2.06	6.2.00	6.1.54	6.1.48	6.1.42	6.1.36
7	5.02	7.5.02	7.4.55	7.4.48	7.4.41	7.4.34	7.4.27	7.4.20	7.4.13	7.4.06	7.3.59	7.3.52	7.3.45	7.3.38	7.3.31	7.3.24	7.3.17	7.3.10	7.3.03	7.2.56	7.2.49	7.2.42	7.2.35	7.2.28	7.2.21	7.2.14
8	6.00	8.6.00	8.5.54	8.5.47	8.5.40	8.5.33	8.5.26	8.5.19	8.5.12	8.5.05	8.4.58	8.4.51	8.4.44	8.4.37	8.4.30	8.4.23	8.4.16	8.4.09	8.4.02	8.3.55	8.3.48	8.3.41	8.3.34	8.3.27	8.3.20	8.3.13
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25																										

## 25 DEGREES.

M	L. Sine.	L. Co-Sine.	L. Tangent.	L. Co-Tang.	L. Secant.	L. Co-Secant.	M
0	9.6259483	9.9572757	9.5686725	10.5313275	10.427243	10.3740517	60
1	9.6262191	9.9572168	9.5690023	10.5309977	10.427582	10.3737809	59
2	9.6264897	9.9571578	9.5693319	10.5306681	10.427922	10.3735103	58
3	9.6267601	9.9570988	9.5696613	10.5303385	10.4282612	10.3732395	57
4	9.6270303	9.9570397	9.5699906	10.5300090	10.4286003	10.3729687	56
5	9.6273003	9.9569805	9.5703197	10.5296793	10.4289394	10.3726979	55
6	9.6275701	9.9569215	9.5706486	10.5293491	10.4292785	10.3724271	54
7	9.6278397	9.9568623	9.5709774	10.5290188	10.4296176	10.3721563	53
8	9.6281090	9.9568030	9.5713060	10.5286884	10.4299567	10.3718855	52
9	9.6283782	9.9567437	9.5716345	10.5283590	10.4302958	10.3716147	51
10	9.6286474	9.9566844	9.5719628	10.5280292	10.4306349	10.3713439	50
11	9.6289160	9.9566250	9.5722910	10.5277000	10.4309740	10.3710731	49
12	9.6291845	9.9565656	9.5726190	10.5273708	10.4313131	10.3708023	48
13	9.6294529	9.9565061	9.5729468	10.5270416	10.4316522	10.3705315	47
14	9.6297211	9.9564466	9.5732745	10.5267124	10.4319913	10.3702607	46
15	9.6299890	9.9563870	9.5736020	10.5263832	10.4323304	10.3700000	45
16	9.6302568	9.9563275	9.5739294	10.5260540	10.4326695	10.3697392	44
17	9.6305243	9.9562679	9.5742566	10.5257248	10.4330086	10.3694784	43
18	9.6307917	9.9562081	9.5745836	10.5253956	10.4333477	10.3692176	42
19	9.6310589	9.9561483	9.5749105	10.5250664	10.4336868	10.3689568	41
20	9.6313258	9.9560885	9.5752372	10.5247372	10.4340259	10.3686960	40
21	9.6315926	9.9560287	9.5755638	10.5244080	10.4343650	10.3684352	39
22	9.6318591	9.9559689	9.5758902	10.5240788	10.4347041	10.3681744	38
23	9.6321255	9.9559090	9.5762165	10.5237496	10.4350432	10.3679136	37
24	9.6323916	9.9558490	9.5765426	10.5234204	10.4353823	10.3676528	36
25	9.6326576	9.9557890	9.5768686	10.5230912	10.4357214	10.3673920	35
26	9.6329233	9.9557289	9.5771944	10.5227620	10.4360605	10.3671312	34
27	9.6331889	9.9556688	9.5775201	10.5224328	10.4363996	10.3668704	33
28	9.6334544	9.9556087	9.5778456	10.5221036	10.4367387	10.3666096	32
29	9.6337194	9.9555485	9.5781709	10.5217744	10.4370778	10.3663488	31
30	9.6339844	9.9554882	9.5784961	10.5214452	10.4374169	10.3660880	30
L. Co-Sine.	L. Sine.	L. Tangent.	L. Co-Tang.	L. Secant.	L. Co-Secant.	L. Secant.	M

64 DEGREES.

Latitude 50 Deg. 00 Min. South Declination.

		Latitude 50 Deg. 00 Min.												South Declination.												
	0	d. 2	d. 4	d. 6	d. 8	d. 10	d. 12	d. 14	d. 16	d. 18	d. 20	d. 22	d. 23													
	b. m.	m. b. m.	m. b. m.	m. b. m.	m. b. m.	m. b. m.	m. b. m.	m. b. m.	m. b. m.	m. b. m.	m. b. m.	m. b. m.	m. b. m.													
SIN	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0													
1	0.35	1.0.36	1.0.37	1.0.38	1.0.39	1.0.40	1.0.41	1.0.42	1.0.43	1.0.44	1.0.45	1.0.46	1.0.47													
2	1.10	2.1.12	2.1.14	2.1.16	2.1.18	3.1.21	2.1.23	2.1.25	2.1.27	2.1.29	3.1.32	2.1.34	2.1.36													
3	1.45	3.1.51	3.1.54	3.1.57	3.2.00	4.2.04	3.2.07	3.2.10	3.2.13	3.2.16	4.2.20	4.2.24	5.2.27													
4	2.30	4.2.34	4.2.38	4.2.42	4.2.46	4.2.50	4.2.54	4.3.58	5.3.03	5.3.08	6.3.13	6.3.19	7.3.24													
5	3.16	5.3.21	5.3.26	5.3.31	5.3.36	5.3.41	5.3.46	5.3.51	6.3.57	6.4.03	6.4.09	7.4.15	8.4.21													
6	4.06	6.4.12	6.4.18	6.4.24	6.4.30	6.4.36	6.4.42																			
7	5.02	7.5.09	7.5.16																							
WE																										



## A TABLE of Natural and

25 DEGREES.

M	N. Sine.	N. Co-Sine.	N. Tangent.	N. Co-Tang.	N. Secant.	N. Co-Secant.
30	4305111	9025853	4769755	2995436	11079285	23228205
31	4307736	9026000	4773326	29949751	11080823	23214049
32	4310351	9026147	4776899	29945137	11082363	23199911
33	4312966	9026293	4780474	29940523	11083903	23185794
34	4315581	9026440	4784049	29935909	11085445	23171695
35	4318196	9026587	4787624	29931295	11086989	23157615
36	4320811	9026734	4791199	29926681	11088533	23143554
37	4323426	9026881	4794774	29922067	11090077	23129513
38	4326041	9027028	4798349	29917453	11091621	23115490
39	4328656	9027175	4801924	29912839	11093165	23101486
40	4331271	9027322	4805499	29908225	11094709	23087501
41	4333886	9027469	4809074	29903611	11096253	23073535
42	4336501	9027616	4812649	29898997	11097797	23059589
43	4339116	9027763	4816224	29894383	11099341	23045660
44	4341731	9027910	4819799	29889769	11100885	23031751
45	4344346	9028057	4823374	29885155	11102429	23017860
46	4346961	9028204	4826949	29880541	11103973	23003988
47	4349576	9028351	4830524	29875927	11105517	22990134
48	4352191	9028498	4834099	29871313	11107061	22976299
49	4354806	9028645	4837674	29866699	11108605	22962483
50	4357421	9028792	4841249	29862085	11110149	22948685
51	4360036	9028939	4844824	29857471	11111693	22934906
52	4362651	9029086	4848399	29852857	11113237	22921145
53	4365266	9029233	4851974	29848243	11114781	22907403
54	4367881	9029380	4855549	29843629	11116325	22893679
55	4370496	9029527	4859124	29839015	11117869	22879974
56	4373111	9029674	4862699	29834401	11119413	22866286
57	4375726	9029821	4866274	29829787	11120957	22852618
58	4378341	9029968	4869849	29825173	11122501	22838967
59	4380956	9030115	4873424	29820559	11124045	22825334
60	4383571	9030262	4876999	29815945	11125589	22811720
	N. Co-Sine.	N. Sine.	N. Tangent.	N. Co-Tang.	N. Co-Secant.	N. Secant.

64 DEGREES.

Latitude 51 Deg. 00 Min. North Declination.																									
	0	d.	2	d.	+	d.	6	d.	8	d.	10	d.	12	d.	14	d.	16	d.	18	d.	20	d.	22	d.	23
	b. m.	n.	b. m.	n.	b. m.	n.	b. m.	n.	b. m.	n.	b. m.	n.	b. m.	n.	b. m.	n.	b. m.	n.	b. m.	n.	b. m.	n.	b. m.	n.	b. m.
SN	12.0		12.0		12.0		12.0		12.0		12.0		12.0		12.0		12.0		12.0		12.0		12.0		12.0
1	0-35		1-0-34		1-0-33		1-0-32		1-0-31		1-0-30		1-0-29		1-0-28		1-0-27		1-0-26		1-0-25		1-0-24		1-0-23
2	1-11		2-1-09		2-1-07		2-1-05		2-1-03		2-1-01		2-0-59		2-0-57		2-0-55		2-0-53		2-0-51		2-0-49		2-0-47
3	1-50		3-1-47		3-1-44		3-1-41		3-1-39		3-1-37		3-1-35		3-1-32		3-1-29		3-1-26		3-1-23		3-1-20		3-1-17
4	2-31		4-2-27		4-2-23		4-2-19		4-2-15		4-2-11		4-2-07		4-2-03		4-1-59		4-1-55		4-1-51		4-1-45		4-1-41
5	3-17		5-12-12		5-12-07		5-12-02		5-11-57		5-11-52		5-11-47		5-11-42		5-11-37		5-11-32		5-11-26		5-11-20		5-11-15
6	4-06		6-14-03		6-13-57		6-13-51		6-13-45		6-13-39		6-13-33		6-13-27		6-13-21		6-13-14		7-03-07		7-03-01		6-59-55
7	5-03		7-23-57		7-23-51		7-23-45		7-23-39		7-23-33		7-23-27		7-23-21		7-23-14		7-23-07		7-13-00		7-12-54		7-12-48
WE	6-00		8-11-54		8-11-48		8-11-41		8-11-34		8-11-27		8-11-20		8-11-13		8-11-06		8-10-59		8-10-52		8-10-45		8-10-38
1									6-33		7-06-26		7-16-19		7-16-12		7-06-05		7-05-58		7-05-51		7-05-44		6-58-38
2																	7-07		8-05-59		7-06-52		7-06-45		6-56-40
3																							7-45		1-49-59

## Artificial Sines, Tangents, and Secants.

25 DEGREES.

M	L. Sine.	L. Co-Sine.	L. Tangent.	L. Co-Tang.	L. Secant.	L. Co-Secant.
30	9.6339844	9.9554882	9.6784961	10.3215039	10.0445118	10.3660156
31	9.6344280	9.9554280	9.6788821	10.3211789	10.0445720	10.3657509
32	9.6348517	9.9553676	9.6792460	10.3208540	10.0446324	10.3654863
33	9.6352700	9.9553073	9.6795908	10.3205292	10.0446927	10.3652220
34	9.6356842	9.9552469	9.6799253	10.3202047	10.0447531	10.3649578
35	9.6360962	9.9551864	9.6802598	10.3198803	10.0448136	10.3646938
36	9.6365099	9.9551259	9.6805944	10.3195560	10.0448741	10.3644301
37	9.6369235	9.9550653	9.6809290	10.3192318	10.0449347	10.3641665
38	9.6373371	9.9550051	9.6812636	10.3189079	10.0449953	10.3639031
39	9.6377507	9.9549449	9.6815982	10.3185840	10.0450559	10.3636399
40	9.6381643	9.9548847	9.6819328	10.3182603	10.0451166	10.3633760
41	9.6385779	9.9548245	9.6822674	10.3179368	10.0451773	10.3631141
42	9.6389915	9.9547643	9.6826020	10.3176135	10.0452381	10.3628516
43	9.6394051	9.9547041	9.6829366	10.3172902	10.0452989	10.3625892
44	9.6398187	9.9546439	9.6832712	10.3169672	10.0453597	10.3623269
45	9.6402323	9.9545837	9.6836058	10.3166443	10.0454205	10.3620646
46	9.6406459	9.9545235	9.6839404	10.3163215	10.0454813	10.3618031
47	9.6410595	9.9544633	9.6842750	10.3159989	10.0455421	10.3615415
48	9.6414731	9.9544031	9.6846096	10.3156764	10.0456029	10.3612801
49	9.6418867	9.9543429	9.6849442	10.3153541	10.0456637	10.3610188
50	9.6423003	9.9542827	9.6852788	10.3150319	10.0457245	10.3607578
51	9.6427139	9.9542225	9.6856134	10.3147099	10.0457853	10.3604970
52	9.6431275	9.9541623	9.6859480	10.3143880	10.0458461	10.3602363
53	9.6435411	9.9541021	9.6862826	10.3140662	10.0459069	10.3599759
54	9.6439547	9.9540419	9.6866172	10.3137447	10.0459677	10.3597156
55	9.6443683	9.9539817	9.6869518	10.3134232	10.0460285	10.3594555
56	9.6447819	9.9539215	9.6872864	10.3131019	10.0460893	10.3591956
57	9.6451955	9.9538613	9.6876210	10.3127808	10.0461501	10.3589360
58	9.6456091	9.9538011	9.6879556	10.3124598	10.0462109	10.3586765
59	9.6460227	9.9537409	9.6882902	10.3121389	10.0462717	10.3584172
60	9.6464363	9.9536807	9.6886248	10.3118182	10.0463325	10.3581580
	L. Co-Sine.	L. Sine.	L. Co-Tang.	L. Tangent.	L. Co-Secant.	L. Secant.

64 DEGREES.

Latitude 51 Deg. 00 Min. South Declination.																									
	0	d. 2	d. 4	d. 6	d. 8	d. 10	d. 12	d. 14	d. 16	d. 18	d. 20	d. 22	d. 23												
	b. m.	b. m.	b. m.	b. m.	b. m.	b. m.	b. m.	b. m.	b. m.	b. m.	b. m.	b. m.	b. m.												
S N	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0												
1	0-35	1-0-36	1-0-37	1-0-38	1-0-39	1-0-40	1-0-41	1-0-42	1-0-43	1-0-44	1-0-46	1-0-47	1-0-48												
2	1-11	2-1-13	2-1-15	2-1-17	2-1-19	2-1-21	3-1-24	2-1-25	2-1-28	2-1-30	2-1-32	2-1-34	2-1-36												
3	1-50	3-1-53	3-1-56	3-1-59	3-2-02	3-2-05	4-2-09	3-2-12	3-2-15	3-2-18	3-2-21	3-2-24	3-2-27												
4	2-31	4-2-35	4-2-39	4-2-43	4-2-47	5-2-52	5-2-57	4-3-01	4-3-05	4-3-09	4-3-13	5-3-18	3-2-21												
5	3-17	5-3-22	5-3-27	5-3-32	5-3-37	5-3-42	7-3-49	5-3-54	5-3-59	5-4-04	5-4-09	5-4-14	5-4-19												
6	4-08	6-4-13	6-4-19	6-4-25	6-4-31	6-4-37	7-4-44																		
7	5-03	6-5-09	7-5-16																						
WE																									



## 26 DEGREES.

M	N. Sine.	N. Co-Sine.	V. Tangent.	N. Co-Tang.	N. Secant.	N. Co-Secant.
0	4383712	8987940	4577326	23503038	11126019	22811720
1	4386526	8986665	4580927	23487910	11127598	22798124
2	4389540	8985389	4584530	23472300	11129179	22784546
3	4392553	8984112	4588133	23457708	11130761	22770986
4	4395566	8982834	4591737	23442634	11132345	22757445
5	4398579	8981555	4595343	23427570	11133930	22743921
6	4399932	8980276	4598949	23412540	11135516	22730415
7	4402004	8978996	4602557	23397519	11137103	22716927
8	4404616	8977715	4606166	23382417	11138692	22703457
9	4407227	8976433	4609775	23367312	11140282	22690005
10	4409838	8975151	4613386	23352205	11141874	22676571
11	4412448	8973868	4616997	23337097	11143467	22663155
12	4415058	8972584	4620610	23322003	11145062	22649756
13	4417668	8971299	4624224	23307769	11146658	22636372
14	4420278	8970015	4627838	23292873	11148255	22623012
15	4422887	8968732	4631454	23277994	11149854	22609657
16	4425496	8967448	4635071	23263133	11151454	22596339
17	4428104	8966165	4638689	23248289	11153056	22583029
18	4430712	8964880	4642308	23233462	11154659	22569736
19	4433320	8963595	4645928	23218651	11156263	22556451
20	4435927	8962309	4649549	23203852	11157869	22543184
21	4438534	8961024	4653171	23189068	11159475	22529936
22	4441140	8959739	4656794	23174291	11161081	22516701
23	4443746	8958451	4660418	23159522	11162689	22503486
24	4446352	8957163	4664043	23144769	11164306	22490288
25	4448957	8955874	4667669	23130016	11165919	22477078
26	4451562	8954582	4671297	23115277	11167533	22463884
27	4454167	8953289	4674925	23100546	11169149	22450699
28	4456771	8951995	4678554	23085813	11170766	22437529
29	4459375	8950701	4682185	23071081	11172384	22424369
30	4461978	8949405	4685816	23056357	11174004	22411218
N. Co-Sine. N. Sine. N. Co-Tang. N. Tangent. N. Co-Secant. N. Secant. M						

63 DEGREES.

## Latitude 52 Deg. 00 Min. North Declination.

	0	d	2	d	4	6	d	8	d	10	d	12	d	14	d	16	d	18	d	20	d	22	d	24
S N	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0
1	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0
2	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0
3	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0
4	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0
5	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0
6	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0
7	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0
8	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0
9	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0
10	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0
11	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0
12	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0
13	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0
14	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0
15	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0
16	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0
17	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0
18	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0
19	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0
20	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0
21	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0
22	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0
23	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0
24	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0
25	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0
26	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0
27	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0
28	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0
29	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0
30	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0

## Artificial Sines, Tangents, and Secants.

## 26 DEGREES.

M	L. Sine.	L. Co-Sine.	L. Tangent.	L. Co-Tang.	L. Secant.	L. Co-Secant.	
0	9.6418420	9.9536602	9.68831518	10.3118182	10.0463398	10.3581580	60
1	9.6421009	9.9535985	9.6885023	10.3114977	10.0464015	10.3578991	59
2	9.6423596	9.9535369	9.6886882	10.3111773	10.0464631	10.3576404	58
3	9.6426182	9.9534751	9.6888740	10.3108570	10.0465249	10.3573818	57
4	9.6428765	9.9534134	9.6890598	10.3105369	10.0465866	10.3571235	56
5	9.6431347	9.9533515	9.6892456	10.3102169	10.0466483	10.3568653	55
6	9.6433926	9.9532897	9.6894313	10.3098970	10.0467103	10.3566074	54
7	9.6436504	9.9532278	9.6896170	10.3095774	10.0467722	10.3563496	53
8	9.6439080	9.9531658	9.6898027	10.3092578	10.0468342	10.3560920	52
9	9.6441654	9.9531038	9.6899884	10.3089384	10.0468962	10.3558346	51
10	9.6444228	9.9530418	9.6901741	10.3086191	10.0469582	10.3555774	50
11	9.6446799	9.9529797	9.6903598	10.3083000	10.0470203	10.3553204	49
12	9.6449365	9.9529175	9.6905455	10.3079811	10.0470825	10.3550635	48
13	9.6451931	9.9528553	9.6907312	10.3076622	10.0471447	10.3548069	47
14	9.6454496	9.9527931	9.6909169	10.3073435	10.0472069	10.3545504	46
15	9.6457058	9.9527308	9.6911026	10.3070250	10.0472692	10.3542942	45
16	9.6459619	9.9526685	9.6912883	10.3067066	10.0473315	10.3540381	44
17	9.6462178	9.9526061	9.6914740	10.3063883	10.0473939	10.3537822	43
18	9.6464735	9.9525437	9.6916598	10.3060722	10.0474563	10.3535265	42
19	9.6467290	9.9524813	9.6918457	10.3057522	10.0475187	10.3532710	41
20	9.6469844	9.9524155	9.6920315	10.3054344	10.0475812	10.3530166	40
21	9.6472395	9.9523562	9.6922173	10.3051197	10.0476438	10.3527640	39
22	9.6474945	9.9522956	9.6924030	10.3048131	10.0477064	10.3525095	38
23	9.6477492	9.9522310	9.6925887	10.3045117	10.0477690	10.3522508	37
24	9.6480038	9.9521653	9.6927743	10.3042165	10.0478317	10.3519962	36
25	9.6482582	9.9521005	9.6929600	10.3039247	10.0478945	10.3517418	35
26	9.6485124	9.9520328	9.6931457	10.3036393	10.0479572	10.3514876	34
27	9.6487665	9.9519799	9.6933313	10.3033215	10.0480201	10.3512333	33
28	9.6490203	9.9519171	9.6935170	10.3029968	10.0480829	10.3509797	32
29	9.6492740	9.9518541	9.6937026	10.3026802	10.0481459	10.3507260	31
30	9.6495274	9.9517912	9.6938733	10.3023263	10.0482088	10.3504726	30
	L. Co-Sine.	L. Sine.	L. Co-Tang.	L. Tangent.	L. Co-Secant.	L. Secant.	M



## 26 DEGREES.

M	N. Sine.	N. Co-Sine.	N. Tangent.	N. Co-Tang.	N. Secant.	N. Co-Secant.	M
30	4461978	8949343	4985816	20056597	11174004	22411584	30
31	4464581	8948045	4989449	20042295	11175625	22398517	29
32	4467184	8946745	4993082	20027710	11177248	22385457	28
33	4469786	8945445	4996717	20013142	11178872	22372435	27
34	4472388	8944145	5000352	19998590	11180498	22359419	26
35	4474990	8942845	5003989	19984036	11182125	22346420	25
36	4477592	8941542	5007627	19969539	11183753	22333438	24
37	4480192	8940239	5011266	19955035	11185383	22320474	23
38	4482792	8938936	5014906	19940534	11187014	22307526	22
39	4485392	8937632	5018547	19926037	11188647	22294595	21
40	4487992	8936327	5022189	19911537	11190281	22281681	20
41	4490592	8935021	5025832	19897043	11191916	22268783	19
42	4493192	8933714	5029476	19882547	11193553	22255903	18
43	4495789	8932406	5033121	19868057	11195191	22243039	17
44	4498387	8931098	5036767	19853563	11196831	22230192	16
45	4500985	8929789	5040415	19839066	11198472	22217362	15
46	4503582	8928479	5044061	19824566	11200115	22204548	14
47	4506179	8927169	5047713	19810065	11201759	22191751	13
48	4508776	8925858	5051365	19795565	11203405	22178971	12
49	4511372	8924545	5055015	19781063	11205052	22166207	11
50	4513968	8923233	5058668	19766560	11206702	22153460	10
51	4516563	8921920	5062322	19752057	11208353	22140731	9
52	4519158	8920606	5065977	19737552	11210005	22128018	8
53	4521753	8919291	5069633	19723047	11211658	22115328	7
54	4524347	8917975	5073290	19708542	11213312	22102657	6
55	4526941	8916659	5076948	19694037	11214967	22089972	5
56	4529535	8915342	5080607	19679532	11216622	22077323	4
57	4532128	8914024	5084267	19665027	11218278	22064691	3
58	4534721	8912705	5087928	19650522	11219933	22052075	2
59	4537313	8911385	5091591	19636017	11221589	22039476	1
60	4539905	8910065	5095254	19621512	11223242	22026893	0
	N. Co-Sine.	N. Sine.	N. Co-Tang.	N. Tangent.	N. Co-Secant.	N. Secant.	M

## 63 DEGREES.

## Latitude 53 Deg. 00 Min. North Declination.

		Longitude												Declination												
		0	d.	2	d.	4	d.	6	d.	8	d.	10	d.	12	d.	14	d.	16	d.	18	d.	20	d.	22	d.	24
		b. m.	m.	b. m.	m.	b. m.	m.	b. m.	m.	b. m.	m.	b. m.	m.	b. m.	m.	b. m.	m.	b. m.	m.	b. m.	m.	b. m.	m.	b. m.	m.	b. m.
S	N	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	
1	0.3	1.03	1.03	1.03	1.03	1.03	1.03	1.03	1.03	1.03	1.03	1.03	1.03	1.03	1.03	1.03	1.03	1.03	1.03	1.03	1.03	1.03	1.03	1.03	1.03	
2	1.3	2.11	2.11	2.11	2.11	2.11	2.11	2.11	2.11	2.11	2.11	2.11	2.11	2.11	2.11	2.11	2.11	2.11	2.11	2.11	2.11	2.11	2.11	2.11	2.11	
3	1.52	3.14	3.14	3.14	3.14	3.14	3.14	3.14	3.14	3.14	3.14	3.14	3.14	3.14	3.14	3.14	3.14	3.14	3.14	3.14	3.14	3.14	3.14	3.14	3.14	
4	2.34	4.23	4.23	4.23	4.23	4.23	4.23	4.23	4.23	4.23	4.23	4.23	4.23	4.23	4.23	4.23	4.23	4.23	4.23	4.23	4.23	4.23	4.23	4.23	4.23	
5	3.20	5.16	5.16	5.16	5.16	5.16	5.16	5.16	5.16	5.16	5.16	5.16	5.16	5.16	5.16	5.16	5.16	5.16	5.16	5.16	5.16	5.16	5.16	5.16	5.16	
6	4.10	6.05	6.05	6.05	6.05	6.05	6.05	6.05	6.05	6.05	6.05	6.05	6.05	6.05	6.05	6.05	6.05	6.05	6.05	6.05	6.05	6.05	6.05	6.05	6.05	
7	5.04	6.58	6.58	6.58	6.58	6.58	6.58	6.58	6.58	6.58	6.58	6.58	6.58	6.58	6.58	6.58	6.58	6.58	6.58	6.58	6.58	6.58	6.58	6.58	6.58	
8	6.00	6.54	6.54	6.54	6.54	6.54	6.54	6.54	6.54	6.54	6.54	6.54	6.54	6.54	6.54	6.54	6.54	6.54	6.54	6.54	6.54	6.54	6.54	6.54	6.54	
9																										
10																										
11																										
12																										
13																										
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## Artificial Sines, Tangents, and Secants.

## 26 DEGREES.

M	L. Sine.	L. Co-Sine.	L. Tangent.	L. Co-Tang.	L. Secant.	L. Co-Secant.	
30	9.6495274	9.9517912	9.6977353	10.3022637	10.0482583	10.3504725	30
31	9.6497807	9.9517282	9.6983526	10.3019474	10.0482718	10.3502193	28
32	9.6500338	9.9516661	9.6988357	10.3016313	10.0483349	10.3499662	29
33	9.6502868	9.9516020	9.6992026	10.3013153	10.0483980	10.3497132	27
34	9.6505395	9.9515389	9.6995936	10.3009994	10.0484611	10.3494605	26
35	9.6507920	9.9514757	9.6999316	10.3006836	10.0485243	10.3492080	25
36	9.6510441	9.9514124	9.6999630	10.3003650	10.0485876	10.3489556	24
37	9.6512966	9.9513492	9.6999974	10.3000526	10.0486505	10.3487034	23
38	9.6515486	9.9512858	9.7000263	10.2997372	10.0487142	10.3484514	22
39	9.6518004	9.9512224	9.7000578	10.2994220	10.0487775	10.3481996	21
40	9.6520521	9.9511593	9.7003830	10.2991070	10.0488410	10.3479479	20
41	9.6523035	9.9510963	9.7012035	10.2987923	10.0489044	10.3476965	19
42	9.6525548	9.9510320	9.7015227	10.2984773	10.0489680	10.3474452	18
43	9.6528059	9.9509685	9.7018374	10.2981626	10.0490315	10.3471941	17
44	9.6530568	9.9509049	9.7021519	10.2978481	10.0490949	10.3469432	16
45	9.6533075	9.9508412	9.7024665	10.2975337	10.0491588	10.3466925	15
46	9.6535581	9.9507775	9.7027805	10.2972195	10.0492225	10.3464418	14
47	9.6538084	9.9507138	9.7030946	10.2969054	10.0492862	10.3461916	13
48	9.6540586	9.9506500	9.7034086	10.2965914	10.0493500	10.3459414	12
49	9.6543086	9.9505861	9.7037225	10.2962775	10.0494139	10.3456914	11
50	9.6545586	9.9505223	9.7040363	10.2959638	10.0494777	10.3454416	10
51	9.6548081	9.9504583	9.7043497	10.2956503	10.0495417	10.3451919	9
52	9.6550575	9.9503944	9.7046632	10.2953368	10.0496056	10.3449425	8
53	9.6553068	9.9503305	9.7049765	10.2950235	10.0496697	10.3446932	7
54	9.6555559	9.9502665	9.7052897	10.2947103	10.0497337	10.3444441	6
55	9.6558048	9.9502022	9.7056027	10.2943973	10.0497975	10.3441952	5
56	9.6560536	9.9501381	9.7059166	10.2940844	10.0498620	10.3439464	4
57	9.6563021	9.9500738	9.7062304	10.2937716	10.0499262	10.3436979	3
58	9.6565505	9.9500095	9.7065440	10.2934590	10.0499905	10.3434495	2
59	9.6567987	9.9499452	9.7068575	10.2931465	10.0500545	10.3432013	1
60	9.6570465	9.9498809	9.7071659	10.2928341	10.0501191	10.3429532	0
	L. Co-Sine.	L. Sine.	L. Co-Tang.	L. Tangent.	L. Co-Secant.	L. Secant.	



## A TABLE of Natural and

27 DEGREES.

M	N. Sine.	N. Co-Sine.	N. Tangent.	N. Co-Tang.	N. Secant.	N. Co-Secant.
0	4539905	8910065	5095254	19526105	11223262	22026893
1	4542497	8907441	5095919	19512000	11224926	22014326
2	4545088	8904722	5102385	19497910	11226592	22001775
3	4547679	8902000	5105052	19483737	11228259	21989240
4	4550259	8899277	5109919	19469570	11229923	21976721
5	4552859	8896455	5113588	19455403	11231598	21964203
6	4555449	8893632	5117459	19441235	11233269	21951733
7	4558038	8890802	5120930	19427067	11234942	21939262
8	4560627	8887974	5124602	19412900	11236616	21926803
9	4563216	8885149	5128275	19398733	11238292	21914370
10	4565804	8882321	5131950	19384571	11239969	21901947
11	4568392	8879493	5135625	19370418	11241648	21889541
12	4570979	8876664	5139302	19356266	11243328	21877150
13	4573566	8873834	5142980	19342113	11245010	21864775
14	4576153	8871003	5146658	19327960	11246693	21852417
15	4578739	8868171	5150338	19313807	11248377	21840074
16	4581325	8865339	5154019	19299654	11250063	21827746
17	4583910	8862506	5157702	19285501	11251750	21815435
18	4586495	8859672	5161385	19271348	11253439	21803132
19	4589080	8856837	5165069	19257195	11255129	21790839
20	4591665	8853992	5168755	19243042	11256821	21778540
21	4594249	8851155	5172441	19228889	11258514	21766245
22	4596832	8848318	5176129	19214736	11260209	21753951
23	4599415	8845481	5179818	19200583	11261905	21741895
24	4601998	8842644	5183508	19186430	11263603	21729693
25	4604580	8839807	5187199	19172277	11265302	21717506
26	4607162	8836970	5190891	19158124	11267003	21705335
27	4609744	8834133	5194584	19143971	11268705	21693180
28	4612325	8831296	5198278	19129818	11270408	21681040
29	4614905	8828459	5201974	19115665	11272113	21668915
30	4617486	8825622	5205670	19101512	11273819	21656806
	N. Co-Sine.	N. Sine.	N. Co-Tang.	N. Tangent.	N. Co-Secant.	N. Secant.

62 DEGREES.

Latitude 54 Deg. 00 Min. North Declination.

	0	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20	21	22	23
	a. b. m.	a. b. m.	a. b. m.	a. b. m.	a. b. m.	a. b. m.	a. b. m.	a. b. m.	a. b. m.	a. b. m.	a. b. m.	a. b. m.	a. b. m.	a. b. m.	a. b. m.	a. b. m.	a. b. m.	a. b. m.	a. b. m.	a. b. m.	a. b. m.	a. b. m.	a. b. m.	a. b. m.
SIN	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0
1	0.37	1.03	1.35	1.67	1.99	2.31	2.63	2.95	3.27	3.59	3.91	4.23	4.55	4.87	5.19	5.51	5.83	6.15	6.47	6.79	7.11	7.43	7.75	8.07
2	1.14	1.13	2.11	2.10	3.08	3.07	4.05	4.04	5.02	5.01	5.99	5.98	6.96	6.95	7.93	7.92	8.90	8.89	9.87	9.86	10.84	10.83	11.81	11.80
3	1.54	2.15	3.14	3.13	4.12	4.11	5.09	5.08	6.06	6.05	7.03	7.02	8.00	7.99	8.97	8.96	9.94	9.93	10.91	10.90	11.88	11.87	12.85	12.84
4	2.36	3.23	4.22	4.21	5.19	5.18	6.16	6.15	7.13	7.12	8.10	8.09	9.07	9.06	10.04	10.03	11.01	11.00	11.98	11.97	12.95	12.94	13.92	13.91
5	3.22	4.31	5.30	5.29	6.27	6.26	7.24	7.23	8.21	8.20	9.18	9.17	10.15	10.14	11.12	11.11	12.09	12.08	13.06	13.05	14.03	14.02	15.00	14.99
6	4.12	5.17	6.16	6.15	7.13	7.12	8.10	8.09	9.07	9.06	10.04	10.03	11.01	11.00	11.98	11.97	12.95	12.94	13.92	13.91	14.89	14.88	15.86	15.85
7	5.05	6.09	7.08	7.07	8.05	8.04	9.02	9.01	10.00	9.99	10.97	10.96	11.94	11.93	12.91	12.90	13.88	13.87	14.85	14.84	15.82	15.81	16.79	16.78
WE	6.00	5.55	6.54	6.53					6.57	6.51	6.55	6.51	6.51	6.51	6.51	6.51	6.51	6.51	6.51	6.51	6.51	6.51	6.51	6.51
1									6.33	6.57	6.51	6.51	6.51	6.51	6.51	6.51	6.51	6.51	6.51	6.51	6.51	6.51	6.51	6.51
2																								
3																								



## A TABLE of Natural and

27 DEGREES.

M	N. Sine.	N. Co-Sine.	N. Tangent.	N. Co-Tang.	N. Secant.	N. Co-Secant.	M
30	4617486	8870108	5205672	19209321	11273812	21656806	30
31	4620066	8869764	5209368	19196186	11275527	21644712	29
32	4622646	8869420	5213063	19182565	11277237	21632633	28
33	4625225	8869075	5216767	19168960	11278948	21620570	27
34	4627804	8868729	5220468	19155370	11280660	21608522	26
35	4630383	8868383	5224177	19141795	11282374	21596489	25
36	4632962	8868036	5227871	19128236	11284089	21584471	24
37	4635541	8867688	5231578	19114691	11285806	21572469	23
38	4638119	8867339	5235284	19101162	11287524	21560482	22
39	4640698	8866989	5238990	19087617	11289244	21548510	21
40	4643269	8866639	5242693	19074147	11290965	21536553	20
41	4645845	8866288	5246407	19060663	11292688	21524611	19
42	4648421	8865936	5250117	19047193	11294412	21512684	18
43	4650996	8865583	5253829	19033738	11296137	21500772	17
44	4653571	8865230	5257541	19020299	11297864	21488875	16
45	4656145	8864876	5261254	19006874	11299593	21476993	15
46	4658719	8864521	5264969	18993464	11301323	21465127	14
47	4661293	8864166	5268685	18980068	11303055	21453275	13
48	4663866	8863810	5272402	18966688	11304788	21441437	12
49	4666439	8863453	5276120	18953322	11306522	21429615	11
50	4669012	8863095	5279839	18939971	11308258	21417808	10
51	4671584	8862736	5283559	18926634	11309996	21406015	9
52	4674156	8862377	5287281	18913313	11311735	21394238	8
53	4676727	8862017	5291004	18900006	11313475	21382475	7
54	4679298	8861656	5294727	18886713	11315217	21370726	6
55	4681869	8861294	5298452	18873436	11316961	21358993	5
56	4684439	8860932	5302178	18860172	11318706	21347274	4
57	4687009	8860569	5305905	18846924	11320452	21335570	3
58	4689578	8860205	5309634	18833690	11322200	21323880	2
59	4692147	8859841	5313364	18820470	11323950	21312205	1
60	4694716	8859476	5317094	18807265	11325701	21300545	0
N. Co-Sine.		N. Sine.	N. Co-Tang.	N. Tangent.	N. Co-Secant.	N. Secant.	M

62 DEGREES.

Latitude 55 Deg. 00 Min. North Declination.

	0	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20	21	22	23	24
S. N.	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0
1	0.37	0.0.47	1.0.35	1.0.35	1.0.34	1.0.33	1.0.32	1.0.31	1.0.30	1.0.29	1.0.28	1.0.27	1.0.26	1.0.25	1.0.24	1.0.23	1.0.22	1.0.21	1.0.20	1.0.19	1.0.18	1.0.17	1.0.16	1.0.15	1.0.14
2	1.15	1.1.14	2.1.12	2.1.12	2.1.11	2.1.10	2.1.09	2.1.08	2.1.07	2.1.06	2.1.05	2.1.04	2.1.03	2.1.02	2.1.01	2.1.00	2.0.59	2.0.58	2.0.57	2.0.56	2.0.55	2.0.54	2.0.53	2.0.52	2.0.51
3	1.55	2.1.53	3.1.50	3.1.47	3.1.44	3.1.41	3.1.39	3.1.36	3.1.33	3.1.30	3.1.27	3.1.24	3.1.21	3.1.18	3.1.15	3.1.12	3.1.09	3.1.06	3.1.03	3.1.00	3.0.57	3.0.54	3.0.51	3.0.48	3.0.45
4	2.37	3.2.34	4.2.31	4.2.27	4.2.23	4.2.19	4.2.16	4.2.12	4.2.08	4.2.04	4.2.00	4.1.55	4.1.51	4.1.47	4.1.42	4.1.38	4.1.34	4.1.30	4.1.26	4.1.21	4.1.17	4.1.13	4.1.09	4.1.05	4.1.01
5	3.22	4.3.19	5.3.15	5.3.11	5.3.06	5.3.02	5.2.57	5.2.53	5.2.48	5.2.43	5.2.38	5.2.33	5.2.29	5.2.24	5.2.19	5.2.14	5.2.09	5.2.04	5.2.00	5.1.55	5.1.51	5.1.46	5.1.42	5.1.37	5.1.33
6	4.13	5.4.08	6.4.03	6.3.58	6.3.53	6.3.47	6.3.42	6.3.37	6.3.32	6.3.26	6.3.21	6.3.16	6.3.11	6.3.06	6.3.01	6.2.56	6.2.51	6.2.46	6.2.41	6.2.36	6.2.31	6.2.26	6.2.21	6.2.16	6.2.11
7	5.06	6.5.01	7.5.00	7.4.55	7.4.50	7.4.44	7.4.38	7.4.32	7.4.26	7.4.21	7.4.15	7.4.10	7.4.04	7.4.00	7.3.54	7.3.49	7.3.43	7.3.38	7.3.32	7.3.27	7.3.21	7.3.16	7.3.11	7.3.05	7.3.00
WE	6.00	7.5.55	8.5.50	8.5.44	8.5.38	8.5.32	8.5.26	8.5.20	8.5.14	8.5.08	8.5.02	8.4.56	8.4.50	8.4.44	8.4.38	8.4.32	8.4.26	8.4.20	8.4.14	8.4.08	8.4.02	8.3.56	8.3.50	8.3.44	8.3.38
1																									
2																									
3																									

## Artificial Sines, Tangents, and Secants.

27 DEGREES.

M	L. Sine.	L. Co-Sine.	L. Tangent.	L. Co-Tang.	L. Secant.	L. Co-Secant.	M
30	9.6644056	9.9479239	9.7161767	10.2835233	10.0520711	10.3355944	30
31	9.6646482	9.9478631	9.7167851	10.2832149	10.0521369	10.335518	29
32	9.6648906	9.9477973	9.7173933	10.2829067	10.0522027	10.3354421	28
33	9.6651329	9.9477314	9.7179914	10.2825986	10.0522686	10.3353671	27
34	9.6653749	9.9476655	9.7185904	10.2822906	10.0523345	10.3352921	26
35	9.6656168	9.9475995	9.7191893	10.2819827	10.0524005	10.3352171	25
36	9.6658586	9.9475335	9.7197883	10.2816749	10.0524665	10.3351421	24
37	9.6661001	9.9474674	9.7203872	10.2813673	10.0525326	10.3350671	23
38	9.6663415	9.9474013	9.7209862	10.2810598	10.0525987	10.3349921	22
39	9.6665828	9.9473352	9.7215852	10.2807524	10.0526648	10.3349171	21
40	9.6668238	9.9472690	9.7221842	10.2804451	10.0527311	10.3348421	20
41	9.6670647	9.9472029	9.7227832	10.2801379	10.0527973	10.3347671	19
42	9.6673054	9.9471364	9.7233822	10.2798310	10.0528636	10.3346921	18
43	9.6675459	9.9470700	9.7239812	10.2795241	10.0529300	10.3346171	17
44	9.6677863	9.9470036	9.7245802	10.2792173	10.0529964	10.3345421	16
45	9.6680266	9.9469372	9.7251792	10.2789107	10.0530628	10.3344671	15
46	9.6682669	9.9468707	9.7257782	10.2786042	10.0531293	10.3343921	14
47	9.6685071	9.9468042	9.7263772	10.2782978	10.0531958	10.3343171	13
48	9.6687471	9.9467377	9.7269762	10.2779915	10.0532624	10.3342421	12
49	9.6689875	9.9466710	9.7275752	10.2776853	10.0533290	10.3341671	11
50	9.6692280	9.9466043	9.7281742	10.2773793	10.0533957	10.3340921	10
51	9.6694682	9.9465376	9.7287732	10.2770734	10.0534624	10.3340171	9
52	9.6697083	9.9464708	9.7293722	10.2767675	10.0535292	10.3339421	8
53	9.6699482	9.9464040	9.7299712	10.2764619	10.0535960	10.3338671	7
54	9.6701879	9.9463373	9.7305702	10.2761564	10.0536629	10.3337921	6
55	9.6704279	9.9462702	9.7311692	10.2758510	10.0537298	10.3337171	5
56	9.6706676	9.9462032	9.7317682	10.2755457	10.0537968	10.3336421	4
57	9.6709075	9.9461362	9.7323672	10.2752405	10.0538638	10.3335671	3
58	9.6711473	9.9460692	9.7329662	10.2749353	10.0539308	10.3334921	2
59	9.6713871	9.9460022	9.7335652	10.2746305	10.0539979	10.3334171	1
60	9.6716269	9.9459349	9.7341642	10.2743256	10.0540651	10.3333421	0
L. Co-Sine.		L. Sine.	L. Co-Tang.	L. Tangent.	L. Co-Secant.	L. Secant.	M

62 DEGREES.

Latitude 55 Deg. 00 Min. South Declination.

	0	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20	21	22	23	24
	<i>b. m.</i>	<i>m. b.</i>	<i>m. b.</i>	<i>m. b.</i>	<i>m. b.</i>	<i>m. b.</i>	<i>m. b.</i>	<i>m. b.</i>	<i>m. b.</i>	<i>m. b.</i>	<i>m. b.</i>	<i>m. b.</i>	<i>m. b.</i>	<i>m. b.</i>	<i>m. b.</i>	<i>m. b.</i>	<i>m. b.</i>	<i>m. b.</i>	<i>m. b.</i>	<i>m. b.</i>	<i>m. b.</i>	<i>m. b.</i>	<i>m. b.</i>	<i>m. b.</i>	<i>m. b.</i>
<i>S. N.</i>	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0
1	0.37	1.0.38	1.0.39	1.0.40	1.0.41	1.0.42	1.0.43	1.0.44	1.0.45	1.0.46	1.0.47	1.0.48	1.0.49	1.0.50	1.0.51	1.0.52	1.0.53	1.0.54	1.0.55	1.0.56	1.0.57	1.0.58	1.0.59	1.1.00	1.1.01
2	1.15	1.1.16	2.1.18	2.1.20	2.1.22	2.1.24	2.1.26	2.1.28	2.1.30	2.1.32	2.1.34	2.1.36	2.1.38	2.1.40	2.1.42	2.1.44	2.1.46	2.1.48	2.1.50	2.1.52	2.1.54	2.1.56	2.1.58	2.2.00	2.2.02
3	1.55	2.1.57	3.1.59	3.2.01	3.2.03	3.2.05	3.2.07	3.2.09	3.2.11	3.2.13	3.2.15	3.2.17	3.2.19	3.2.21	3.2.23	3.2.25	3.2.27	3.2.29	3.2.31	3.2.33	3.2.35	3.2.37	3.2.39	3.2.41	3.2.43
4	2.37	3.2.40	4.2.43	4.2.45	4.2.47	4.2.49	4.2.51	4.2.53	4.2.55	4.2.57	4.2.59	4.3.01	4.3.03	4.3.05	4.3.07	4.3.09	4.3.11	4.3.13	4.3.15	4.3.17	4.3.19	4.3.21	4.3.23	4.3.25	4.3.27
5	3.22	4.3.27	5.3.30	5.3.32	5.3.34	5.3.36	5.3.38	5.3.40	5.3.42	5.3.44	5.3.46	5.3.48	5.3.50	5.3.52	5.3.54	5.3.56	5.3.58	5.4.00	5.4.02	5.4.04	5.4.06	5.4.08	5.4.10	5.4.12	5.4.14
6	4.13	5.4.18	6.4.21	6.4.23	6.4.25	6.4.27	6.4.29	6.4.31	6.4.33	6.4.35	6.4.37	6.4.39	6.4.41	6.4.43	6.4.45	6.4.47	6.4.49	6.4.51	6.4.53	6.4.55	6.4.57	6.4.59	6.5.01	6.5.03	6.5.05
7	5.06	6.5.12	7.5.15	7.5.17	7.5.19	7.5.21	7.5.23	7.5.25	7.5.27	7.5.29	7.5.31	7.5.33	7.5.35	7.5.37	7.5.39	7.5.41	7.5.43	7.5.45	7.5.47	7.5.49	7.5.51	7.5.53	7.5.55	7.5.57	7.5.59
<i>W. E.</i>																									



## A TABLE of Natural and

28 DEGREES.

M	N. Sine.	N. Co-Sine.	N. Tangent.	N. Co-Tang.	N. Secant.	N. Co-Secant.
0	459716	892476	5317294	18807265	11325701	21300545
1	4697284	8825110	5320826	18794574	11327453	21288899
2	4699852	8826743	5324559	18780893	11329207	21277267
3	4702419	8828375	5328293	18767736	11330962	21265651
4	4704986	8829995	5332029	18754588	11332719	21254048
5	4707553	8832653	5335765	18741455	11334478	21242460
6	4710119	8835268	5339503	18728336	11336238	21230887
7	4712685	8837895	5343242	18715231	11337999	21219328
8	4715252	8840527	5346982	18702141	11339762	21207783
9	4717815	8843155	5350723	18689064	11341527	21196253
10	4720380	8845782	5354465	18676003	11343293	21184737
11	4722944	8848409	5358208	18662955	11345090	21173235
12	4725508	8851035	5361953	18649921	11346829	21161748
13	4728071	8853660	5365699	18636902	11348600	21150274
14	4730634	8856284	5369446	18623896	11350372	21138815
15	4733197	8858907	5373194	18610905	11352146	21127371
16	4735759	8861530	5376943	18597928	11353921	21115940
17	4738321	8864152	5380694	18584965	11355698	21104523
18	4740882	8866773	5384445	18572015	11357476	21093121
19	4743443	8869394	5388198	18559080	11359255	21081733
20	4746004	8872014	5391952	18546159	11361036	21070359
21	4748564	8874633	5395707	18533252	11362819	21058989
22	4751124	8877251	5399464	18520359	11364603	21047652
23	4753683	8879869	5403221	18507473	11366389	21036320
24	4756242	8882486	5406980	18494591	11368176	21025002
25	4758801	8885102	5410740	18481761	11369965	21013698
26	4761359	8887717	5414501	18468929	11371755	21002408
27	4763917	8890332	5418263	18456099	11373547	20991131
28	4766474	8892946	5422027	18443289	11375340	20979869
29	4769031	8895559	5425791	18430492	11377135	20968620
30	4771588	8898171	5429557	18417709	11378932	20957385
N. Co-Sine.		N. Sine.	N. Co-Tang.	N. Tangent.	N. Co-Secant.	N. Secant.

61 DEGREES.

Latitude 56 Deg. 00 Min. North Declination.

	0	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20	21	22	23	24
S	N	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0
1	0.37	1.03	1.37	1.73	2.11	2.50	2.90	3.31	3.73	4.16	4.60	5.05	5.51	5.98	6.46	6.95	7.44	7.94	8.44	8.95	9.46	9.98	10.50	11.02	11.55
2	1.16	1.15	2.13	2.11	3.11	3.10	4.10	4.09	5.09	5.08	6.08	6.07	7.07	7.06	8.06	8.05	9.05	9.04	10.04	10.03	11.03	11.02	12.02	12.01	13.01
3	1.55	2.15	3.15	3.14	4.14	4.13	5.13	5.12	6.12	6.11	7.11	7.10	8.10	8.09	9.09	9.08	10.08	10.07	11.07	11.06	12.06	12.05	13.05	13.04	14.04
4	2.39	3.23	4.23	4.22	5.22	5.21	6.21	6.20	7.20	7.19	8.19	8.18	9.18	9.17	10.17	10.16	11.16	11.15	12.15	12.14	13.14	13.13	14.13	14.12	15.12
5	3.25	4.21	5.21	5.20	6.20	6.19	7.19	7.18	8.18	8.17	9.17	9.16	10.16	10.15	11.15	11.14	12.14	12.13	13.13	13.12	14.12	14.11	15.11	16.11	17.11
6	4.14	5.10	6.10	6.09	7.09	7.08	8.08	8.07	9.07	9.06	10.06	10.05	11.05	11.04	12.04	12.03	13.03	13.02	14.02	14.01	15.01	15.00	16.00	17.00	18.00
7	5.06	6.01	7.01	7.00	8.00	7.99	8.99	8.98	9.98	9.97	10.97	10.96	11.96	11.95	12.95	12.94	13.94	13.93	14.93	14.92	15.92	15.91	16.91	17.91	18.91
WE	6.00	7.00	8.00	8.00	9.00	9.00	10.00	10.00	11.00	11.00	12.00	12.00	13.00	13.00	14.00	14.00	15.00	15.00	16.00	16.00	17.00	17.00	18.00	19.00	20.00
1																									
2																									
3																									

## Artificial Sines, Tangents, and Secants.

28 DEGREES.

M	L. Sine.	L. Co-Sine.	L. Tangent.	L. Co-Tang.	L. Secant.	L. Co-Secant.
0	9.6716093	9.9459349	9.7250714	10.2743256	10.0544681	10.3283997
1	9.6718468	9.9458677	9.7253791	10.2740209	10.0544123	10.3281532
2	9.6720841	9.9458005	9.7256868	10.2737163	10.0543565	10.3279067
3	9.6723213	9.9457332	9.7259945	10.2734119	10.0543007	10.3276602
4	9.6725586	9.9456660	9.7263022	10.2731075	10.0542449	10.3274137
5	9.6727959	9.9455988	9.7266100	10.2728031	10.0541891	10.3271672
6	9.6730331	9.9455316	9.7269177	10.2724987	10.0541333	10.3269207
7	9.6732704	9.9454644	9.7272254	10.2721943	10.0540775	10.3266742
8	9.6735077	9.9453972	9.7275331	10.2718899	10.0540217	10.3264277
9	9.6737450	9.9453300	9.7278408	10.2715855	10.0539659	10.3261812
10	9.6739823	9.9452628	9.7281485	10.2712811	10.0539101	10.3259347
11	9.6742196	9.9451956	9.7284562	10.2709767	10.0538543	10.3256882
12	9.6744569	9.9451284	9.7287639	10.2706723	10.0537985	10.3254417
13	9.6746942	9.9450612	9.7290716	10.2703679	10.0537427	10.3251952
14	9.6749315	9.9449940	9.7293793	10.2700635	10.0536869	10.3249487
15	9.6751688	9.9449268	9.7296870	10.2697591	10.0536311	10.3247022
16	9.6754061	9.9448596	9.7299947	10.2694547	10.0535753	10.3244557
17	9.6756434	9.9447924	9.7303024	10.2691503	10.0535195	10.3242092
18	9.6758807	9.9447252	9.7306101	10.2688459	10.0534637	10.3239627
19	9.6761180	9.9446580	9.7309178	10.2685415	10.0534079	10.3237162
20	9.6763553	9.9445908	9.7312255	10.2682371	10.0533521	10.3234697
21	9.6765926	9.9445236	9.7315332	10.2679327	10.0532963	10.3232232
22	9.6768299	9.9444564	9.7318409	10.2676283	10.0532405	10.3229767
23	9.6770672	9.9443892	9.7321486	10.2673239	10.0531847	10.3227302
24	9.6773045	9.9443220	9.7324563	10.2670195	10.0531289	10.3224837
25	9.6775418	9.9442548	9.7327640	10.2667151	10.0530731	10.3222372
26	9.6777791	9.9441876	9.7330717	10.2664107	10.0530173	10.3219907
27	9.6780164	9.9441204	9.7333794	10.2661063	10.0529615	10.3217442
28	9.6782537	9.9440532	9.7336871	10.2658019	10.0529057	10.3214977
29	9.6784910	9.9439860	9.7339948	10.2654975	10.0528499	10.3212512
30	9.6787283	9.9439188	9.7343025	10.2651931	10.0527941	10.3210047
L. Co-Sine.		L. Sine.	L. Co-Tang.	L. Tangent.	L. Co-Secant.	L. Secant.

61 DEGREES.

Latitude 56 Deg. 00 Min. South Declination.

	0	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20	21	22	23	24
S	N	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0
1	0.37	1.03	1.37	1.73	2.11	2.50	2.90	3.31	3.73	4.16	4.60	5.05	5.51	5.98	6.46	6.95	7.44	7.94	8.44	8.95	9.46	9.98	10.50	11.02	11.55
2	1.16	1.15	2.13	2.11	3.11	3.10	4.10	4.09	5.09	5.08	6.08	6.07	7.07	7.06	8.06	8.05	9.05	9.04	10.04	10.03	11.03	11.02	12.02	12.01	13.01
3	1.55	2.15	3.15	3.14	4.14	4.13	5.13	5.12	6.12	6.11	7.11	7.10	8.10	8.09	9.09	9.08	10.08	10.07	11.07	11.06	12.06	12.05	13.05	13.04	14.04
4	2.39	3.23	4.23	4.22	5.22	5.21	6.21	6.20	7.20	7.19	8.19	8.18	9.18	9.17	10.17	10.16	11.16	11.15	12.15	12.14	13.14	13.13	14.13	14.12	15.12
5	3.25	4.21	5.21	5.20	6.20	6.19	7.19	7.18	8.18	8.17	9.17	9.16	10.16	10.15	11.15	11.14	12.14	12.13	13.13	13.12	14.12	14.11	15.11	16.11	17.11
6	4.14	5.10	6.10	6.09	7.09	7.08	8.08	8.07	9.07	9.06	10.06	10.05	11.05	11.04	12.04	12.03	13.03	13.02	14.02	14.01	15.01	15.00	16.00	17.00	18.00
7	5.06	6.01	7.01	7.00	8.00	7.99	8.99	8.98	9.98	9.97	10.97	10.96	11.96	11.95	12.95	12.94	13.94	13.93	14.93	14.92	15.92	15.91	16.91	17.91	18.91
WE	6.00	7.00	8.00	8.00	9.00	9.00	10.00	10.00	11.00	11.00	12.00	12.00	13.00	13.00	14.00	14.00	15.00	15.00	16.00	16.00	17.00	17.00	18.00	19.00	20.00
1																									
2																									
3																									



*A* T A B L E *of* Natural and

28 DEGREES

	N. Sine.	N. Co-Sine.	N. Tangent.	N. Co-Tang.	N. Secant.	N. Co-Secant.	
30	4771588	8788171	5429557	15417799	11378932	20957385	30
31	4774144	8786753	5433324	15404939	11380730	20946167	29
32	4776700	8785336	5437092	15392184	11382529	20934957	28
33	4779256	8783904	5440862	15379442	11384330	20923754	27
34	4781810	8782461	5444632	15366715	11386133	20912548	26
35	4784364	8781022	5448404	15353999	11387937	20901343	25
36	4786918	8779583	5452177	15341297	11389743	20890265	24
37	4789472	8778147	5455951	15328610	11391550	20879127	23
38	4792026	8776704	5459726	15315936	11393359	20868002	22
39	4794579	8775264	5463503	15303275	11395169	20856890	21
40	4797131	8773824	5467281	15290625	11396981	20845792	20
41	4799685	8772385	5471060	15277994	11398794	20834705	19
42	4802238	8771461	5474840	15265374	11400609	20823637	18
43	4804786	8770061	5478621	15252763	11402425	20812580	17
44	4807337	8768666	5482404	15240173	11404243	20801536	16
45	4809888	8767275	5486188	15227605	11406062	20790506	15
46	4812438	8765888	5489973	15215058	11407883	20779489	14
47	4814988	8764468	5493759	15202473	11409706	20768486	13
48	4817537	8763067	5497546	15189932	11411530	20757496	12
49	4820086	8761665	5501333	15177435	11413356	20746519	11
50	4822634	8760262	5505125	15164982	11415183	20735556	10
51	4825182	8758869	5508916	15152591	11417012	20724606	9
52	4827730	8757485	5512708	15140244	11418842	20713670	8
53	4830277	8756090	5516502	15127940	11420674	20702746	7
54	4832824	8754695	5520297	15115689	11422507	20691836	6
55	4835370	8753301	5524093	15103421	11424342	20680940	5
56	4837916	8751902	5527890	15091168	11426179	20670056	4
57	4840462	8750504	5531688	15078964	11428017	20659186	3
58	4843007	8749106	5535488	15066762	11429857	20648328	2
59	4845552	8747707	5539283	15054589	11431698	20637484	1
60	4848096	8746307	5543080	15042478	11433541	20626653	0
	N. Co-Sine.	N. Sine.	N. Co-Tang.	N. Tangent.	N. Co-Secant.	N. Secant.	M

61 DEGREES.

61 DEGREES.

Latitude 57 Deg. 00 Min. North Declination.

[illegible]

28 D E G R E E S

M	<i>L. Sine.</i>	<i>L. Co-Sine.</i>	<i>L. Tangent.</i>	<i>L. Co-Tang.</i>	<i>L. Secant.</i>	<i>L. Co-Secant.</i>	
30	9.6786629	9.9438995	9.7347841	10.2652356	10.0561101	10.3213371	30
31	9.6783955	9.9438299	9.7350565	10.2649344	10.0561705	10.3211045	29
32	9.6791272	9.9437612	9.7353667	10.2646333	10.0562308	10.3208372	28
33	9.6793609	9.9436925	9.7356677	10.2643323	10.0563075	10.3206398	27
34	9.6795923	9.9436238	9.7359687	10.2640315	10.0563762	10.3204477	26
35	9.6798243	9.9435549	9.7362693	10.2637307	10.0564451	10.3201757	25
36	9.6800560	9.9434861	9.7365699	10.2634301	10.0565139	10.3199440	24
37	9.6802877	9.9434172	9.7368705	10.2631295	10.0565828	10.3197123	23
38	9.6805191	9.9433484	9.7371709	10.2628291	10.0566518	10.3194839	22
39	9.6807504	9.9432792	9.7374712	10.2625285	10.0567208	10.3192466	21
40	9.6809816	9.9432102	9.7377714	10.2622286	10.0567898	10.3189874	20
41	9.6812126	9.9431411	9.7380715	10.2619295	10.0568589	10.3187487	19
42	9.6814434	9.9430720	9.7383714	10.2616286	10.0569280	10.3185165	18
43	9.6816741	9.9430028	9.7386713	10.2613287	10.0569972	10.3182829	17
44	9.6819045	9.9429335	9.7389710	10.2610290	10.0570665	10.3180954	16
45	9.6821348	9.9428643	9.7392707	10.2607293	10.0571357	10.3178651	15
46	9.6823651	9.9427949	9.7395702	10.2604295	10.0572051	10.3176349	14
47	9.6825952	9.9427255	9.7398696	10.2601304	10.0572745	10.3174043	13
48	9.6828250	9.9426561	9.7401683	10.2598311	10.0573439	10.3171750	12
49	9.6830548	9.9425866	9.7404681	10.2595319	10.0574132	10.3169455	11
50	9.6832843	9.9425171	9.7407682	10.2592328	10.0574824	10.3167157	10
51	9.6835137	9.9424476	9.7410682	10.2589333	10.0575524	10.3164856	9
52	9.6837430	9.9423779	9.7413680	10.2586350	10.0576221	10.3162570	8
53	9.6839720	9.9423083	9.7416678	10.2583362	10.0576917	10.3160280	7
54	9.6842010	9.9422385	9.7419681	10.2580376	10.0577614	10.3157990	6
55	9.6844297	9.9421688	9.7422639	10.2577391	10.0578312	10.3155703	5
56	9.6846585	9.9420990	9.7425544	10.2574406	10.0579010	10.3153417	4
57	9.6848868	9.9420291	9.7428477	10.2571423	10.0579709	10.3151132	3
58	9.6851151	9.9419592	9.7431359	10.2568441	10.0580408	10.3148849	2
59	9.6853432	9.9418893	9.7434240	10.2565460	10.0581107	10.3146568	1
60	9.6855712	9.9418195	9.7437120	10.2562480	10.0581807	10.3144288	0
	<i>L. Sine.</i>	<i>L. Sine.</i>	<i>L. Co-Tang.</i>	<i>L. Tangent.</i>	<i>L. Co-Secant.</i>	<i>L. Secant.</i>	M

61 DEGREES.

61 DEGREES

*Latitude 57 Deg. 00 Min. South Declination.*

[illegible]



A T A B L E of Natural and

29. DEGREES.									
M	N. Sine.	N.Co-Sine.	N. Tangent.	V. Co-Tang.	N. Secant.	N.Co-Secant.	V. Co- Cot.		
0	4843096	87416197	5543392	15040475	11433541	20626653	60		
1	4850640	8744786	5545894	15028105	11435385	20615836	59		
2	4858184	8743375	5548398	15015751	11437231	20605031	58		
3	4865727	8741903	5551404	15003403	11439075	20594239	57		
4	4873270	8740450	5553811	14991077	11440927	20583460	56		
5	4880812	8739016	5556219	14978755	11442779	20572635	55		
6	4888354	8737572	5558629	14966434	11444630	20561842	54		
7	4895895	8736117	5561039	14954112	11446484	20551203	53		
8	4903436	8734651	5563451	14941793	11448339	20540476	52		
9	4910977	8733191	5565864	14929476	11450196	20529762	51		
10	4918517	8731728	5568279	14917162	11452055	20519061	50		
11	4926057	8730264	5570694	14904851	11453915	20508373	49		
12	4933597	8728821	5573111	14892542	11455776	20497698	48		
13	4941136	8727367	5575526	14880275	11457639	20487036	47		
14	4948674	8725913	5577943	14867985	11459504	20476386	46		
15	4956212	8724460	5580359	14855695	11461370	20465750	45		
16	4963750	8723018	5582774	14843407	11463238	20455126	44		
17	4971287	8721565	5585191	14831143	11465108	20444515	43		
18	4978824	8720113	5587608	14818879	11466979	20433916	42		
19	4986361	8718661	5590025	14806615	11468852	20423330	41		
20	4993898	8717214	5592443	14794352	11470726	20412757	40		
21	4991433	8715761	5594861	14782090	11472602	20402197	39		
22	4998968	8714309	5597280	14771307	11474479	20391649	38		
23	5006503	8712856	5599699	14760521	11476358	20381114	37		
24	5014037	8711403	5602118	14749741	11478239	20370592	36		
25	5021571	8710010	5604534	14738955	11480121	20360082	35		
26	5029105	87086251	5606953	14728164	11482005	20349595	34		
27	5036638	8707251	5609371	14717369	11483890	20339100	33		
28	5044171	8705876	5611789	14706575	11485777	20328627	32		
29	5051704	8704499	5614205	14695783	11487665	20318168	31		
30	5059236	8703125	5616622	14684990	11489555	20307720	30		
	N. Co-Sine.	N. Sine.	N. Co-Tang.	N. Tangent.	N. Co-Secant.	N. Secant.	M		

[illegible]

29 DEGREES.							
M	<i>L. Sine.</i>	<i>L. Co-Sine.</i>	<i>L. Tangent.</i>	<i>L. Co-Tang.</i>	<i>L. Secant.</i>	<i>L. Co-Secant.</i>	
0	9.655712	9.9415193	9.7477522	10.2522478	1.00658157	1.23144288	60
1	9.6557997	9.9417152	9.7483499	10.2516501	1.00658265	1.23144229	59
2	9.6558627	9.9417679	9.7484477	10.2515524	1.00658369	1.23143775	58
3	9.6559126	9.9418106	9.7485455	10.2514547	1.00658473	1.23143715	57
4	9.6559586	9.9418538	9.7486432	10.2513572	1.00658581	1.23143184	56
5	9.6560058	9.9418965	9.7487410	10.2512597	1.00658685	1.23143212	55
6	9.6560539	9.9419392	9.7488387	10.2511624	1.00658793	1.23143641	54
7	9.6561023	9.9419819	9.7489364	10.2510651	1.00658901	1.23143572	53
8	9.6561507	9.9420247	9.7490342	10.2509678	1.00659012	1.231426105	52
9	9.6561991	9.9420674	9.7491320	10.2508705	1.00659129	1.23142539	51
10	9.6562475	9.9421101	9.7492297	10.2507731	1.00659245	1.23142570	50
11	9.6562959	9.9421528	9.7493275	10.2506758	1.00659363	1.23142502	49
12	9.6563443	9.9421955	9.7494252	10.2505785	1.00659481	1.23142501	48
13	9.6563927	9.9422382	9.7495230	10.2504812	1.00659599	1.23141791	47
14	9.6564411	9.9422809	9.7496207	10.2503839	1.00659718	1.23141233	46
15	9.6564895	9.9423236	9.7497185	10.2502866	1.00659836	1.23140727	45
16	9.6565379	9.9423663	9.7498162	10.2501893	1.00659955	1.23140682	44
17	9.6565863	9.9424090	9.7499140	10.2500920	1.00660073	1.23140568	43
18	9.6566347	9.9424517	9.7500117	10.2500000	1.00660192	1.23140461	42
19	9.6566831	9.9424944	9.7501095	10.2499077	1.00660311	1.23140355	41
20	9.6567315	9.9425371	9.7502072	10.2498154	1.00660430	1.23140250	40
21	9.6567799	9.9425798	9.7503050	10.2497231	1.00660549	1.23140145	39
22	9.6568283	9.9426225	9.7504027	10.2496308	1.00660668	1.23140040	38
23	9.6568767	9.9426652	9.7505005	10.2495385	1.00660787	1.23139935	37
24	9.6569251	9.9427079	9.7505982	10.2494462	1.00660906	1.23139830	36
25	9.6569735	9.9427506	9.7506960	10.2493539	1.00661025	1.23139725	35
26	9.6570219	9.9427933	9.7507937	10.2492616	1.00661144	1.23139620	34
27	9.6570703	9.9428360	9.7508915	10.2491693	1.00661263	1.23139515	33
28	9.6571187	9.9428787	9.7509892	10.2490770	1.00661382	1.23139410	32
29	9.6571671	9.9429214	9.7510870	10.2489847	1.00661501	1.23139305	31
30	9.6572155	9.9429641	9.7511847	10.2488924	1.00661620	1.23139200	30
	<i>L. Co-Sine.</i>	<i>L. Sine.</i>	<i>L. Co-Tang.</i>	<i>L. Tangent.</i>	<i>L. Co-Secant.</i>	<i>L. Secant.</i>	<i>M</i>



29 DEGREES.									
M	N. Sine.	N. Co-Sine.	V. Tangent.	V. Co-Tangent.	N. Secant.	N. Co-Secant.			
30	4924236	8723557	5657728	17674340	11489555	20307720	30		
31	4926767	8722124	5661568	17662950	11491447	20297286	31		
32	4929298	8720690	5665410	17650972	11493330	20286863	32		
33	4931829	8669255	5669253	17639007	11495235	20276453	28		
34	4934359	8667821	5673095	17627053	11497132	20266056	26		
35	4936889	8666385	5676944	17615112	11499030	20255670	25		
36	4939419	8664949	5680791	17603133	11500930	20245297	24		
37	4941948	8663512	5684639	17591267	11502831	20234937	23		
38	4944477	8662075	5688488	17579362	11504734	20224587	22		
39	4947005	8660635	5692332	17567470	11506638	20214251	21		
40	4949533	8659195	5696191	17555590	11508544	20203929	20		
41	4952060	8657756	5700045	17543722	11510452	20193617	19		
42	4954587	8656316	5703899	17531866	11512351	20183318	18		
43	4957113	8654873	5707755	17520023	11514272	20173031	17		
44	4959639	8653431	5711612	17508191	11516185	20162756	16		
45	4962165	8651988	5715471	17496371	11518099	20152494	15		
46	4964690	8650544	5719331	17484561	11520015	20142243	14		
47	4967215	8649100	5723192	17472768	11521932	20132005	13		
48	4969740	8647655	5727054	17460984	11523851	20121779	12		
49	4972264	8646209	5730918	17449213	11525772	20111564	11		
50	4974787	8644762	5734783	17437453	11527694	20101362	10		
51	4977310	8643314	5738649	17425705	11529618	20091172	9		
52	4979833	8641866	5742516	17413969	11531543	20080988	8		
53	4982355	8640417	5746385	17402245	11533470	20070828	7		
54	4984877	8638967	5750255	17390533	11535399	20060674	6		
55	4987399	8637517	5754126	17378833	11537329	20050532	5		
56	4989920	8636066	5757999	17367144	11539261	20040402	4		
57	4992441	8634616	5761871	17355465	11541195	20030283	3		
58	4994961	8633161	5765745	17343803	11543130	20020177	2		
59	4997481	8631708	5769625	17332149	11545067	20010083	1		
60	5000000	866-254	5773503	17320505	11547005	20000000	0		
N. Co-Sine		N. Sine.	N. Co-Tang.		N. Tangent.	N. Co-Secant.		N. Secant.	M

63 DEGREES.									
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65 DEGREES.

Latitude 59 Deg. 00 Min. North Declination.																										
	0	d.	2	d.	4	d.	6	d.	8	d.	10	d.	12	d.	14	d.	16	d.	18	d.	20	d.	22	d.	24	
	6	m.	m.	12	m.	m.	6	m.	m.	12	m.	m.	6	m.	m.	12	m.	m.	6	m.	m.	12	m.	m.	12	m.
N	12.0		12.0		12.0		12.0		12.0		12.0		12.0		12.0		12.0		12.0		12.0		12.0		12.0	
1	0.39		0.39		0.39		0.39		0.39		0.39		0.39		0.39		0.39		0.39		0.39		0.39		0.39	
2	1.18		1.17		1.16		1.14		1.12		1.10		1.08		1.06		1.04		1.02		1.00		0.98		0.96	
3	1.59		1.57		1.55		1.53		1.50		1.47		1.45		1.43		1.41		1.37		1.34		1.31		1.29	
4	2.42		2.39		2.36		2.33		2.30		2.27		2.24		2.21		2.18		2.14		2.10		2.06		2.03	
5	3.28		3.25		3.21		3.17		3.13		3.09		3.05		3.01		2.97		2.93		2.89		2.85		2.81	
6	4.17		4.13		4.09		4.05		4.01		3.96		3.92		3.87		3.83		3.78		3.74		3.69		3.65	
7	5.08		5.04		5.00		4.95		4.90		4.85		4.80		4.75		4.70		4.65		4.60		4.55		4.50	
VE	6.00		5.56		5.15		5.46		5.51		5.36		5.53		5.26		5.21		5.15		5.09		5.58		5.44	
1									6.35		6.52		5.62		5.61		5.69		5.64		5.66		5.58		5.53	
2													7.26		6.74		6.75		5.70		5.65		5.58		5.49	
3																	8.00		4.75		4.75		4.78		4.74	
4																										

29 DEGREES.											
M	L. Sine.	L. Co-Sine.	L. Tangent.	L. Co-Tang.	L. Secant.	L. Co-Secant.					
30	9.9233358	9.9396968	9.7526120	10.2473580	10.0603932	10.3076612	30				
31	9.924620	9.9396253	9.7529368	10.2470332	10.0603747	10.3074380	29				
32	9.925851	9.9395537	9.7532514	10.2467086	10.0603562	10.3072143	28				
33	9.927082	9.9394821	9.7535660	10.2463834	10.0603377	10.3069906	27				
34	9.928313	9.9394105	9.7538802	10.2460582	10.0603192	10.3067672	26				
35	9.929544	9.9393388	9.7541946	10.2457330	10.0603007	10.3065438	25				
36	9.930775	9.9392671	9.7545088	10.2454078	10.0602822	10.3063204	24				
37	9.931995	9.9391953	9.7548229	10.2450826	10.0602637	10.3060970	23				
38	9.933215	9.9391234	9.7551369	10.2447574	10.0602452	10.3058736	22				
39	9.934435	9.9390515	9.7554509	10.2444322	10.0602267	10.3056502	21				
40	9.935654	9.9389796	9.7557649	10.2441070	10.0602082	10.3054268	20				
41	9.936875	9.9389076	9.7560789	10.2437818	10.0601897	10.3052034	19				
42	9.938095	9.9388356	9.7563929	10.2434566	10.0601712	10.3049800	18				
43	9.939315	9.9387635	9.7567069	10.2431314	10.0601527	10.3047566	17				
44	9.940535	9.9386914	9.7570209	10.2428062	10.0601342	10.3045332	16				
45	9.941755	9.9386193	9.7573349	10.2424810	10.0601157	10.3043098	15				
46	9.942975	9.9385472	9.7576489	10.2421558	10.0600972	10.3040864	14				
47	9.944195	9.9384751	9.7579629	10.2418306	10.0600787	10.3038630	13				
48	9.945415	9.9384030	9.7582769	10.2415054	10.0600602	10.3036396	12				
49	9.946635	9.9383309	9.7585909	10.2411802	10.0600417	10.3034162	11				
50	9.947855	9.9382588	9.7589049	10.2408550	10.0600232	10.3031928	10				
51	9.949075	9.9381867	9.7592189	10.2405298	10.0600047	10.3029694	9				
52	9.950295	9.9381146	9.7595329	10.2402046	10.0599862	10.3027460	8				
53	9.951515	9.9380425	9.7598469	10.2398794	10.0599677	10.3025226	7				
54	9.952735	9.9379704	9.7601609	10.2395542	10.0599492	10.3022992	6				
55	9.953955	9.9378983	9.7604749	10.2392290	10.0599307	10.3020758	5				
56	9.955175	9.9378262	9.7607889	10.2389038	10.0599122	10.3018524	4				
57	9.956395	9.9377541	9.7611029	10.2385786	10.0598937	10.3016290	3				
58	9.957615	9.9376820	9.7614169	10.2382534	10.0598752	10.3014056	2				
59	9.958835	9.9376099	9.7617309	10.2379282	10.0598567	10.3011822	1				
60	9.960055	9.9375378	9.7620449	10.2376030	10.0598382	10.3009588	0				
L. Co-Sine.			L. Co-Tang.	L. Tangent.	L. Co-Secant.	L. Secant.					M

60 DEGREES.											
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A T A B L E of Natural and

30 D E G R E E S.									
M	N. Sine.	N. Co-Sine.	V. Tangent.	V. Co-Tangent.	N. Secant.	N. Co-Secant.			
0	5000000	8660254	5773503	1732559	11547305	20000000		60	
1	5002198	8658799	5777732	17335878	11548945	19998929		59	
2	5004395	8657343	5781252	17346200	11550587	19997870		58	
3	5006592	8655887	5784844	17356564	11552230	19996823		57	
4	5008789	8654430	5788407	17367067	11553875	19995788		56	
5	5010986	8652972	5791921	17377647	11555522	19994764		55	
6	5013183	8651514	5795477	17388295	11557169	19993753		54	
7	5015380	8649056	5799066	17399015	11558817	19992760		53	
8	5017577	8646598	5802637	17409797	11560457	19991764		52	
9	5019774	8644139	5806242	17420621	11562097	19990787		51	
10	5021970	8641679	5809833	17431487	11563738	19989826		50	
11	5024167	8639219	5813454	17442392	11565379	19988869		49	
12	5026363	8636758	5817097	17453337	11567020	19987927		48	
13	5028559	8634297	5820773	17464320	11568661	19986997		47	
14	5030755	8631836	5824473	17475341	11570302	19986080		46	
15	5032951	8629375	5828197	17486399	11571943	19985172		45	
16	5035147	8626913	5831947	17497492	11573584	19984267		44	
17	5037343	8624452	5835722	17508620	11575225	19983363		43	
18	5039539	8621990	5839523	17519782	11576866	19982460		42	
19	5041735	8619529	5843347	17530987	11578507	19981569		41	
20	5043931	8617067	5847194	17542225	11580148	19980680		40	
21	5046127	8614606	5851063	17553496	11581789	19979792		39	
22	5048323	8612144	5854954	17564800	11583430	19978906		38	
23	5050519	8609683	5858866	17576137	11585071	19978021		37	
24	5052715	8607221	5862800	17587507	11586712	19977137		36	
25	5054911	8604760	5866755	17598910	11588353	19976254		35	
26	5057107	8602298	5870731	17610345	11589994	19975373		34	
27	5059303	8600000	5874728	17621812	11591635	19974494		33	
28	5061499	8597699	5878746	17633311	11593276	19973616		32	
29	5063695	8595398	5882785	17644842	11594917	19972740		31	
30	5065891	8593097	5886845	17656405	11596558	19971864		30	
31	5068087	8590796	5890925	17667990	11598199	19970989		29	
32	5070283	8588495	5895025	17679607	11599840	19970114		28	
33	5072479	8586194	5899145	17691246	11601481	19969239		27	
34	5074675	8583893	5903285	17702917	11603122	19968364		26	
35	5076871	8581592	5907445	17714610	11604763	19967489		25	
36	5079067	8579291	5911625	17726325	11606404	19966614		24	
37	5081263	8576990	5915825	17738062	11608045	19965739		23	

		Latitude 60 Deg. 00 Min. North Declination.																									
		0	d.	2	d.	4	d.	6	d.	8	d.	10	d.	12	d.	14	d.	16	d.	18	d.	20	d.	22	d.	23	d.
		m.	m.	m.	m.	m.	m.	m.	m.	m.	m.	m.	m.	m.	m.	m.	m.	m.	m.	m.	m.	m.	m.	m.	m.	m.	m.
S	N	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0	12.0
1		0.59	0.39	1.18	1.38	1.37	1.0.36	1.55	0.35	1.34	1.33	1.32	1.31	1.30	1.29	1.28	1.27	1.26	1.25	1.24	1.23	1.22	1.21	1.20	1.19	1.18	1.17
2		1.19	1.18	1.17	1.16	1.15	1.14	1.13	1.12	1.11	1.10	1.09	1.08	1.07	1.06	1.05	1.04	1.03	1.02	1.01	1.00	0.99	0.98	0.97	0.96	0.95	0.94
3		2.70	2.18	2.16	2.14	2.13	2.11	2.10	2.08	2.07	2.06	2.05	2.04	2.03	2.02	2.01	2.00	1.99	1.98	1.97	1.96	1.95	1.94	1.93	1.92	1.91	1.90
4		3.24	3.24	3.23	3.22	3.21	3.20	3.19	3.18	3.17	3.16	3.15	3.14	3.13	3.12	3.11	3.10	3.09	3.08	3.07	3.06	3.05	3.04	3.03	3.02	3.01	3.00
5		4.44	3.26	3.23	3.21	3.20	3.18	3.17	3.15	3.14	3.13	3.12	3.11	3.10	3.09	3.08	3.07	3.06	3.05	3.04	3.03	3.02	3.01	3.00	2.99	2.98	2.97
6		4.18	4.14	4.10	4.08	4.07	4.05	4.04	4.03	4.02	4.01	4.00	3.99	3.98	3.97	3.96	3.95	3.94	3.93	3.92	3.91	3.90	3.89	3.88	3.87	3.86	3.85
7		5.08	4.54	4.50	4.48	4.47	4.45	4.44	4.43	4.42	4.41	4.40	4.39	4.38	4.37	4.36	4.35	4.34	4.33	4.32	4.31	4.30	4.29	4.28	4.27	4.26	4.25
WE		6.00	4.56	4.51	4.48	4.46	4.44	4.43	4.41	4.40	4.39	4.38	4.37	4.36	4.35	4.34	4.33	4.32	4.31	4.30	4.29	4.28	4.27	4.26	4.25	4.24	4.23
1							6.34	6.25	6.16	6.07	5.98	5.89	5.80	5.71	5.62	5.53	5.44	5.35	5.26	5.17	5.08	4.99	4.90	4.81	4.72	4.63	4.55
2								6.34	6.25	6.16	6.07	5.98	5.89	5.80	5.71	5.62	5.53	5.44	5.35	5.26	5.17	5.08	4.99	4.90	4.81	4.72	4.65
3									6.34	6.25	6.16	6.07	5.98	5.89	5.80	5.71	5.62	5.53	5.44	5.35	5.26	5.17	5.08	4.99	4.90	4.81	4.74
4										6.34	6.25	6.16	6.07	5.98	5.89	5.80	5.71	5.62	5.53	5.44	5.35	5.26	5.17	5.08	4.99	4.90	4.83

30 DEGREES.									
M	<i>L. Sine.</i>	<i>L. Co-Sine.</i>	<i>L. Tangent.</i>	<i>L. Co-Tang.</i>	<i>L. Secant.</i>	<i>L. Co-Secant.</i>			
0	9.6889700	9.9375366	9.7614394	10.2385666	10.0624594	10.3110300	60		
1	9.6909187	9.9374577	9.7617511	10.2382689	10.0625423	10.3068118	59		
2	9.6929073	9.9373847	9.7620227	10.2379773	10.0626153	10.3009275	58		
3	9.6949268	9.9373156	9.7623142	10.2376858	10.0626884	10.3003742	57		
4	9.6969841	9.9372519	9.7626066	10.2373944	10.0627615	10.3001559	56		
5	9.7000622	9.9371853	9.7629069	10.2371031	10.0628347	10.2999378	55		
6	9.7002802	9.9370921	9.7631881	10.2368119	10.0629079	10.2997193	54		
7	9.7019018	9.9370159	9.7634792	10.2365203	10.0629811	10.2995019	53		
8	9.7037168	9.9369466	9.7637702	10.2362294	10.0630544	10.2992842	52		
9	9.7007334	9.9368792	9.7640612	10.2359388	10.0631278	10.2990666	51		
10	9.7011508	9.9367988	9.7643520	10.2356480	10.0632012	10.2988492	50		
11	9.7013681	9.9367275	9.7646427	10.2353573	10.0632745	10.2986319	49		
12	9.7014852	9.9366519	9.7649334	10.2350666	10.0633478	10.2984148	48		
13	9.7018022	9.9365783	9.7652239	10.2347767	10.0634211	10.2981976	47		
14	9.7023190	9.9365047	9.7655143	10.2344857	10.0634943	10.2979801	46		
15	9.7028357	9.9364311	9.7658047	10.2341953	10.0635676	10.2977635	45		
16	9.7023423	9.9363574	9.7660949	10.2339051	10.0636408	10.2975477	44		
17	9.7026697	9.9362836	9.7663851	10.2336149	10.0637141	10.2973313	43		
18	9.7028842	9.9362098	9.7666751	10.2333249	10.0637872	10.2971151	42		
19	9.7031011	9.9361361	9.7669651	10.2330349	10.0638604	10.2968985	41		
20	9.7033170	9.9360621	9.7672550	10.2327450	10.0639337	10.2966830	40		
21	9.7035329	9.9359881	9.7675448	10.2324552	10.0640071	10.2964671	39		
22	9.7037486	9.9359141	9.7678344	10.2321654	10.0640805	10.2962514	38		
23	9.7039641	9.9358401	9.7681240	10.2318760	10.0641539	10.2960359	37		
24	9.7041795	9.9357663	9.7684135	10.2315865	10.0642273	10.2958205	36		
25	9.7043947	9.9356917	9.7687029	10.2312971	10.0643005	10.2956062	35		
26	9.7046099	9.9356171	9.7689922	10.2310078	10.0643738	10.2953931	34		
27	9.7048248	9.9355424	9.7692814	10.2307186	10.0644469	10.2951802	33		
28	9.7050397	9.9354679	9.7695705	10.2304293	10.0645200	10.2949673	32		
29	9.7052543	9.9353934	9.7698596	10.2301404	10.0645932	10.2947547	31		
30	9.7054689	9.9353204	9.7701485	10.2298515	10.0646665	10.2945431	30		
	<i>L. Co-Sine.</i>	<i>L. Sine.</i>	<i>L. Co-Tang.</i>	<i>L. Tangent.</i>	<i>L. Co-Secant.</i>	<i>L. Secant.</i>			M

[illegible]







*A* T A B L E *of* Natural and

## 31 DEGREES.

M	N. Sine.	N. Co-Sine.	N. Tangent.	N. Co-Tang.	N. Secant.	N. Co-Secant.
0	5150381	8571673	6008636	16542795	11666334	19416040
1	5152874	8570174	6012466	16631834	11668374	19406646
2	5155367	8568675	6016257	16720881	11670416	19397262
3	5157859	8567175	6020049	16809929	11672459	19387889
4	5160351	8565674	6024843	16899916	11674504	19378527
5	5162842	8564173	6028619	16989907	11676551	19369176
6	5165333	8562671	6032388	16977189	11678599	19359835
7	5167824	8561168	6036154	16965292	11680649	19350505
8	5170314	8559664	6039923	16953405	11682701	19341185
9	5172804	8558161	6043694	16941529	11684755	19331876
10	5175293	8556655	6047465	16933663	11686810	19322578
11	5177782	8555149	6051240	16925803	11688867	19313290
12	5180270	8553642	6055015	16917963	11690926	19304013
13	5182758	8552135	6058792	16910125	11692986	19294746
14	5185245	8550627	6062567	16902304	11695048	19285487
15	5187733	8549118	6066344	16894490	11697112	19276244
16	5190219	8547606	6070121	16886686	11699178	19267009
17	5192705	8546092	6073901	16878893	11701245	19257784
18	5195191	8544583	6077680	16871111	11703314	19248570
19	5197676	8543076	6081460	16863333	11705385	19239366
20	5200161	8541564	6085240	16855576	11707457	19230173
21	5202646	8540051	6089021	16847821	11709531	19220990
22	5205130	8538537	6092803	16840084	11711607	19211817
23	5207613	8537023	6100034	16832351	11713685	19202665
24	5210096	8535508	6104026	16824630	11715754	19193503
25	5212579	8533992	6108019	16816919	11717845	19184362
26	5215061	8532475	6112014	16809218	11719928	19175230
27	5217543	8530958	6116011	16801525	11722013	19166109
28	5220024	8529440	6120008	16793847	11724099	19156997
29	5222505	8527921	6124007	16786177	11726187	19147893
30	5224986	8526402	6128008	16778517	11728277	19138809
	V. Co-Sine.	N. Sine.	N. Co-Tang.	N. Tangent.	N. Co-Secant.	N. Secant.

## 58 DEGREES.

*The Sun's Amplitude by the Point of the Compass.*

[illegible]

### Artificial Sines, Tangents, and Secants.

## 31 D E G R E E S.

M	L. Sine.	L. Co-Sine.	L. Tangent.	L. Co-Tang.	L. Secant.	L. Co-Secant.
0	9-7115393	9-9330567	9-7787737	10-2212263	10-0666344	10-2881679
1	9-7122495	9-9329897	9-7790599	10-2209401	10-0670103	10-2879505
2	9-7122596	9-9329137	9-7793459	10-2206541	10-0673863	10-2877434
3	9-7124695	9-9328376	9-7796318	10-2203682	10-0677624	10-2875268
4	9-7126792	9-9327616	9-7799177	10-2200823	10-0681384	10-2873103
5	9-7128889	9-9326854	9-7802034	10-2197965	10-0685146	10-2871111
6	9-7130933	9-9326092	9-7804891	10-2195109	10-0688908	10-2869017
7	9-7133077	9-9325330	9-7807747	10-2192253	10-0692670	10-2866923
8	9-7135169	9-9324567	9-7810602	10-2189398	10-0696433	10-2864831
9	9-7137265	9-9323804	9-7813456	10-2186544	10-0699196	10-2862741
10	9-7139343	9-9323042	9-7816309	10-2183691	10-0702960	10-2860649
11	9-7141437	9-9322278	9-7819162	10-2180835	10-0706724	10-2858563
12	9-7143524	9-9321515	9-7822013	10-2177977	10-0710489	10-2856476
13	9-7145609	9-9320752	9-7824864	10-2175126	10-0714254	10-2854391
14	9-7147693	9-9319988	9-7827713	10-2172273	10-0718020	10-2852307
15	9-7149776	9-9319223	9-7830562	10-2169418	10-0721787	10-2850224
16	9-7151857	9-9318447	9-7833410	10-2166569	10-0725553	10-2848143
17	9-7153937	9-9317679	9-7836258	10-2163712	10-0729321	10-2846063
18	9-7156015	9-9316911	9-7839104	10-2160856	10-0733089	10-2843984
19	9-7158092	9-9316143	9-7841949	10-2158001	10-0736857	10-2841905
20	9-7160168	9-9315374	9-7844794	10-2155262	10-0740626	10-2839826
21	9-7162243	9-9314605	9-7847638	10-2152526	10-0744395	10-2837757
22	9-7164316	9-9313835	9-7850481	10-2149789	10-0748165	10-2835688
23	9-7166387	9-9313065	9-7853323	10-2147077	10-0751936	10-2833615
24	9-7168458	9-9312294	9-7856164	10-2144366	10-0755706	10-2831542
25	9-7170526	9-9311521	9-7859004	10-2141666	10-0759477	10-2829473
26	9-7172594	9-9310750	9-7861844	10-2138965	10-0763248	10-2827406
27	9-7174660	9-9309978	9-7864685	10-2136265	10-0767022	10-2825344
28	9-7176725	9-9309205	9-7867525	10-2133564	10-0770795	10-2823278
29	9-7178789	9-9308432	9-7870367	10-2130864	10-0774568	10-2821211
30	9-7180851	9-9307658	9-7873209	10-2128167	10-0778342	10-2819149
31						
32						

## 58 D E G R E E S

*The Sun's Amplitude by the Point of the Compass.*

1		27		28		29		30		31		22		23		24		25		C. R. S.	
Dec. 27		Dec. 28		Dec. 29		Dec. 30		Dec. 31		Dec. 22		Dec. 23		Dec. 24		Dec. 25					
Deg.	Min.	Deg.	Min.	Deg.	Min.	Deg.	Min.	Deg.	Min.	Deg.	Min.	Deg.	Min.	Deg.	Min.	Deg.	Min.	Deg.	Min.		
E	W	00	00	00	00	00	00	00	00	00	00	00	00	00	00	00	00	00	00	E	W
1	05	31	05	00	04	03	04	00	04	00	04	00	04	00	04	00	04	00	04	1	1
2	03	01	04	03	04	05	04	05	04	00	04	00	04	00	04	00	04	00	04	2	2
3	07	28	07	28	07	20	07	18	07	13	07	08	07	04	06	05	06	05	06	3	3
1	10	01	09	55	09	50	09	44	09	38	09	31	09	25	09	18	09	12	09	1	1
2	12	30	12	24	12	17	12	09	12	01	11	54	11	46	11	38	11	29	11	2	2
1	15	00	14	00	13	00	12	00	11	54	11	46	11	38	11	30	11	21	11	1	1
2	17	28	14	11	14	43	14	34	14	25	14	16	14	08	13	56	13	46	13	2	2
1	19	56	17	17	17	07	16	55	16	47	16	36	16	24	16	12	15	06	14	1	1
2	19	56	19	45	19	33	19	21	19	09	18	55	18	43	18	32	18	20	18	2	2
1	22	23	22	11	21	58	21	44	21	30	21	16	21	01	20	46	20	30	20	1	1
2	22	23	22	11	21	58	21	44	21	30	21	16	21	01	20	46	20	30	20	2	2



## 30 DEGREES.

M	N. Sine.	N. Co-Sine.	N. Tangent.	N. Co-Tang.	N. Secant.	N. Co-Secant.	
30	5224936	8526402	6128008	16318517	1172877	1918809	30
31	5224766	8521891	6132010	16370867	1173069	19129729	29
32	5224595	8517360	6135013	16423227	1173262	19120659	28
33	5224424	8512829	6138016	16475587	1173457	19111600	27
34	5224253	8508298	6141018	16527947	1173654	19102551	26
35	5224082	8503767	6144021	16580307	1173852	19093512	25
36	5223911	8499236	6147023	16632667	1174052	19084473	24
37	5223740	8494705	6150026	16685027	1174254	19075434	23
38	5223569	8490174	6153028	16737387	1174458	19066395	22
39	5223398	8485643	6156031	16789747	1174663	19057356	21
40	5223227	8481112	6159033	16842107	1174869	19048317	20
41	5223056	8476581	6162036	16894467	1175074	19039278	19
42	5222885	8472050	6165038	16946827	1175280	19030239	18
43	5222714	8467519	6168041	16999187	1175486	19021200	17
44	5222543	8462988	6171043	17051547	1175692	19012161	16
45	5222372	8458457	6174046	17103907	1175898	19003122	15
46	5222201	8453926	6177048	17156267	1176104	18994083	14
47	5222030	8449395	6180051	17208627	1176310	18985044	13
48	5221859	8444864	6183053	17260987	1176516	18976005	12
49	5221688	8440333	6186056	17313347	1176722	18966966	11
50	5221517	8435802	6189058	17365707	1176928	18957927	10
51	5221346	8431271	6192061	17418067	1177134	18948888	9
52	5221175	8426740	6195063	17470427	1177340	18939849	8
53	5221004	8422209	6198066	17522787	1177546	18930810	7
54	5220833	8417678	6201068	17575147	1177752	18921771	6
55	5220662	8413147	6204071	17627507	1177958	18912732	5
56	5220491	8408616	6207073	17679867	1178164	18903693	4
57	5220320	8404085	6210076	17732227	1178370	18894654	3
58	5220149	8400000	6213078	17784587	1178576	18885615	2
59	5219978	8395915	6216081	17836947	1178782	18876576	1
60	5219807	8391830	6219083	17889307	1178988	18867537	0
N. Co-Sine.	N. Sine.	N. Co-Tang.	N. Tangent.	N. Co-Secant.	N. Secant.		M

## 58 DEGREES.

Latitude	26	37	38	39	40	41	42	43	44	
to R. S.	to R. S.	to R. S.	to R. S.	to R. S.	to R. S.	to R. S.	to R. S.	to R. S.	to R. S.	to R. S.
E W	00 00	00 00	00 00	00 00	00 00	00 00	00 00	00 00	00 00	E W
1	02 16	02 15	02 13	02 11	02 09	02 07	02 06	02 04	02 03	1
2	04 34	04 30	04 26	04 22	04 19	04 16	04 14	04 07	04 05	2
3	06 49	06 43	06 38	06 32	06 27	06 22	06 16	06 10	06 04	3
1	09 05	08 58	08 50	08 43	08 36	08 28	08 20	08 12	08 05	1
2	11 21	11 12	11 03	11 03	11 03	11 03	11 03	11 03	11 03	2
3	13 36	13 26	13 14	13 03	12 51	12 40	12 28	12 16	12 03	3
1	15 49	15 36	15 23	15 10	14 57	14 44	14 30	14 16	14 01	1
2	18 02	17 48	17 33	17 18	17 03	16 47	16 31	16 15	15 59	2
3	20 15	19 58	19 41	19 25	19 07	18 50	18 32	18 14	17 54	3
1	22 28	22 07	21 49	21 30	21 10	20 51	20 31	20 19	19 50	1
2				23 32	23 11	22 50	22 27	22 05	21 42	2
3										3

The Sun's Amplitude by the Point of the Compass.

## 31 DEGREES.

M	L. Sine.	L. Co-Sine.	L. Tangent.	L. Co-Tang.	L. Secant.	L. Co-Secant.	
30	97180851	97307658	97571193	102126507	100662242	102819149	30
31	97182012	97306883	97576028	102123972	100653117	102817088	29
32	97184971	97306109	97583863	102121377	100643891	102815029	28
33	97187930	97305333	97588696	102118304	100634667	102812970	27
34	97189986	97304557	97594529	102115471	100625443	102810914	26
35	97191942	97303781	97598361	102112638	100616219	102808858	25
36	97193906	97303004	97602192	102109805	100606996	102806804	24
37	97195249	97302226	97606023	102106972	100597774	102804751	23
38	97197300	97301448	97609854	102104148	100588552	102802700	22
39	97199350	97300670	97613686	102101319	100579330	102800650	21
40	97201399	97299891	97617518	102098492	100570109	102798601	20
41	97203447	97299112	97621350	102095665	100560888	102796553	19
42	97205493	97298332	97625181	102092838	100551668	102794507	18
43	97207538	97297551	97629013	102090013	100542449	102792462	17
44	97209581	97296770	97632845	102087181	100533230	102790419	16
45	97211623	97295989	97636677	102084356	100524011	102788377	15
46	97213664	97295207	97640509	102081532	100514793	102786336	14
47	97215704	97294424	97644341	102078707	100505576	102784296	13
48	97217742	97293641	97648172	102075882	100496359	102782258	12
49	97219779	97292857	97652004	102073057	100487143	102780221	11
50	97221814	97292073	97655836	102070232	100477927	102778185	10
51	97223848	97291289	97659668	102067407	100468711	102776152	9
52	97225881	97290504	97663500	102064582	100459496	102774119	8
53	97227913	97289718	97667332	102061757	100450280	102772087	7
54	97229943	97288932	97671164	102058932	100441068	102770057	6
55	97231972	97288145	97675000	102056107	100431855	102768028	5
56	97234000	97287358	97678836	102053282	100422643	102766000	4
57	97236026	97286571	97682672	102050457	100413432	102763974	3
58	97238051	97285783	97686508	102047632	100404221	102761949	2
59	97240077	97284994	97690344	102044807	100395010	102759925	1
60	97242097	97284205	97694180	102042008	100385799	102757903	0
L. Co-Sine.	L. Sine.	L. Co-Tang.	L. Tangent.	L. Co-Secant.	L. Secant.		M

## 58 DEGREES.

Latitude	45	46	47	48	49	50	51	52	53	
to R. S.	to R. S.	to R. S.	to R. S.	to R. S.	to R. S.	to R. S.	to R. S.	to R. S.	to R. S.	to R. S.
E W	00 00	00 00	00 00	00 00	00 00	00 00	00 00	00 00	00 00	E W
1	02 00	01 58	01 55	01 53	01 51	01 48	01 46	01 44	01 42	1
2	04 19	04 15	04 12	04 09	04 06	04 03	04 01	03 58	03 55	2
3	06 38	06 33	06 29	06 25	06 22	06 19	06 16	06 13	06 10	3
1	09 56	09 47	09 39	09 30	09 22	09 14	09 06	08 58	08 50	1
2	11 51	11 38	11 25	11 12	10 59	10 46	10 33	10 20	10 07	2
3	13 45	13 31	13 17	13 01	12 46	12 30	12 14	11 58	11 41	3
1	15 42	15 24	15 05	14 45	14 28	14 11	13 56	13 37	13 19	1
2	17 36	17 16	16 57	16 36	16 17	15 57	15 36	15 16	14 55	2
3	19 30	19 07	18 46	18 24	18 01	17 40	17 16	16 52	16 29	3
1	21 24	20 55	20 31	20 07	19 42	19 18	18 52	18 27	18 01	1
2	23 08	22 42	22 16	21 49	21 22	20 55	20 28	20 00	19 31	2
3				23 29	23 01	22 31	22 01	21 31	21 01	3

The Sun's Amplitude by the Point of the Compass.



3 <sup>d</sup> DEGREES.							
M.	N. sine.	N. Co-sine.	N. Tangent.	N. Co-Tang.	N. Secant.	N. Co-Secant.	
0	5299191	81802481	6248694	16003345	11791784	13870799	60
1	5301659	8178739	6252737	15992991	11793928	138652019	59
2	5304123	8177396	6256765	15982647	11796074	138632248	58
3	5306591	8175833	6260834	15972321	11798222	138614489	57
4	5309055	8174309	6264884	15961987	11800372	138597738	56
5	5311521	8172754	6268935	15951672	11802523	138582697	55
6	5313986	8171219	6272988	15941366	11804676	138568266	54
7	5316450	8169655	6277042	15931073	11806831	138554545	53
8	5318913	8168126	6281098	15920793	11808988	138540833	52
9	5321376	8166578	6285165	15910505	11811147	138527131	51
10	5323839	8165030	6289215	15900238	11813307	138513438	50
11	5326301	8163481	6293275	15890979	11815465	138499755	49
12	5328763	8161931	6297336	15881732	11817633	138486082	48
13	5331224	8160381	6301399	15872491	11819799	138472418	47
14	5333685	8158830	6305464	15863261	11821966	138458764	46
15	5336145	8157278	6309530	15854021	11824133	138445101	45
16	5338605	8155725	6313598	15844783	11826306	138431485	44
17	5341064	8154171	6317667	15835548	11828479	138417859	43
18	5343523	8152618	6321737	15826315	11830655	138404242	42
19	5345982	8151063	6325808	15817083	11832834	138390637	41
20	5348440	8149508	6329880	15807853	11835008	138377040	40
21	5350898	8147952	6333953	15798625	11837188	138363443	39
22	5353355	8146395	6338025	15789397	11839370	138349878	38
23	5355812	8144837	6342113	15780170	11841554	138336306	37
24	5358268	8143279	6346193	15770947	11843740	138322747	36
25	5360724	8141720	6350274	15761732	11845927	138309219	35
26	5363179	8140160	6354357	15752524	11848116	138295667	34
27	5365635	8138600	6358441	15743326	11850307	138282136	33
28	5368090	8137039	6362527	15734126	11852500	138268605	32
29	5370545	8135477	6366614	15724936	11854694	138255093	31
30	5372999	8133914	6370702	15715746	11856891	138241590	30
N. Co-Sine.		N. sine.	N. Co-Tang.		N. Tangent.	N. Co-Secant.	
						N. Secant.	

## 57 DEGREES.

### The Sun's Amplitude by the Point of the Compass

Lat. true		54		55		56		57		58		59		60			
D. R. S.		Decl. true		Decl. true		Decl. true		Decl. true		Decl. true		Decl. true		Decl. true		D. R. S.	
	Dist.	Dist.	Dist.	Dist.	Dist.	Dist.	Dist.	Dist.	Dist.	Dist.	Dist.	Dist.	Dist.	Dist.	Dist.	Dist.	
E	W	00	00	00	00	00	00	00	00	00	00	00	00	00	00	00	E
1	2	01	39	01	37	01	35	01	32	01	30	01	27	01	25	01	E
3	4	03	18	03	14	03	09	03	04	03	00	02	54	02	49	02	W
5	6	04	57	04	49	04	42	04	35	04	28	04	22	04	16	04	
1	2	06	35	06	25	06	16	06	06	05	56	05	46	05	36	05	
3	4	08	13	08	01	07	49	07	36	07	24	07	11	07	06	06	1
5	6	10	50	10	35	09	21	09	09	08	51	08	36	08	21	08	2
7	8	11	25	11	05	10	41	10	26	10	11	00	09	42	09	22	3
1	2	13	03	12	41	12	25	12	06	11	45	11	22	11	02	11	4
3	4	14	33	14	12	13	50	13	28	13	08	14	42	14	21	14	5
5	6	16	05	15	42	15	18	14	53	14	28	14	42	14	13	14	6
7	8	17	35	17	09	16	42	16	16	15	48	15	21	15	04	15	7
1	2	19	05	18	36	18	06	17	37	17	07	16	37	16	08	16	8
3	4	20	51	20	14	19	56	18	56	18	24	17	52	17	20	17	9
5	6	21	35	21	11	20	47	20	33	20	18	19	44	19	30	19	10
7	8	23	15	22	39	22	05	21	27	20	08	19	44	19	38	19	11
1	2	25	18	24	18	23	39	23	00	22	00	21	22	20	42	20	12
3	4	26	08	25	08	24	08	23	08	22	26	21	55	21	45	21	13
5	6	27	27	26	27	25	27	24	27	23	27	22	27	21	42	21	14

## 32 D E G R E E S.

52 DEGREES.							
M.	<i>L. Sine.</i>	<i>L. Co-sine.</i>	<i>L. Tangent.</i>	<i>L. Co-Tang.</i>	<i>L. Secant.</i>	<i>L. Co-secant.</i>	
0	9.7244217	9.9262845	9.7978792	10.2021083	10.0775179	10.2757233	60
1	9.7244938	9.9263119	9.7983793	10.2025997	10.0776535	10.2755832	59
2	9.7245618	9.9263343	9.7988611	10.2030847	10.0777877	10.2754362	58
3	9.7246256	9.9263514	9.7993362	10.2035637	10.0779205	10.2752834	57
4	9.7246854	9.9263631	9.7998033	10.2040367	10.0780519	10.2751248	56
5	9.7247419	9.9263695	9.7997103	10.2045036	10.0781819	10.2749614	55
6	9.7247954	9.9263719	9.7997445	10.2049645	10.0783104	10.2747931	54
7	9.7248461	9.9263695	9.7997751	10.2054219	10.0784374	10.2746200	53
8	9.7248939	9.9263623	9.7998035	10.2058764	10.0785629	10.2744431	52
9	9.7249389	9.9263504	9.7998296	10.2063281	10.0786869	10.2742625	51
10	9.7249814	9.9263339	9.7998534	10.2067765	10.0788095	10.2740782	50
11	9.7250217	9.9263129	9.7998750	10.2072213	10.0789307	10.2738902	49
12	9.7250597	9.9262874	9.7998945	10.2076634	10.0790505	10.2737006	48
13	9.7250949	9.9262575	9.7999117	10.2081029	10.0791689	10.2735094	47
14	9.7251273	9.9262233	9.7999271	10.2085397	10.0792859	10.2733167	46
15	9.7251576	9.9261848	9.7999407	10.2089738	10.0794016	10.2731224	45
16	9.7251857	9.9261421	9.7999526	10.2094052	10.0795160	10.2729265	44
17	9.7252117	9.9260953	9.7999629	10.2098349	10.0796291	10.2727291	43
18	9.7252357	9.9260445	9.7999716	10.2102629	10.0797409	10.2725302	42
19	9.7252577	9.9259897	9.7999788	10.2106892	10.0798515	10.2723298	41
20	9.7252777	9.9259319	9.7999845	10.2111137	10.0799609	10.2721280	40
21	9.7252957	9.9258702	9.7999887	10.2115365	10.0800691	10.2719248	39
22	9.7253117	9.9258046	9.7999915	10.2119576	10.0801761	10.2717202	38
23	9.7253257	9.9257351	9.8000029	10.2123769	10.0802819	10.2715142	37
24	9.7253377	9.9256617	9.8000129	10.2127944	10.0803865	10.2713068	36
25	9.7253477	9.9255844	9.8000215	10.2132101	10.0804899	10.2710980	35
26	9.7253557	9.9255031	9.8000287	10.2136240	10.0805921	10.2708878	34
27	9.7253627	9.9254178	9.8000345	10.2140361	10.0806931	10.2706762	33
28	9.7253677	9.9253285	9.8000389	10.2144464	10.0807929	10.2704632	32
29	9.7253717	9.9252352	9.8000419	10.2148549	10.0808915	10.2702488	31
30	9.7253747	9.9251379	9.8000437	10.2152616	10.0809889	10.2700330	30
	<i>L. Co-Sine.</i>	<i>Sine.</i>	<i>L. Co-Tang.</i>	<i>Tangent.</i>	<i>L. Co-Secant.</i>	<i>L. Secant.</i>	

## 57 D E G R E E S.

*of the Chiefest Places of the World.*

<i>The Sea-coast of England from the Lizard to Newcastle.</i>				<i>The Places Names.</i>				<i>North</i>		<i>East</i>	
								<i>Latitud.</i>		<i>Longit.</i>	
<i>The Places Names.</i>								<i>D.</i>	<i>M.</i>	<i>D.</i>	<i>M.</i>
								<i>Latitud.</i>		<i>Longit.</i>	
The Lizard	50	10 00	00	Dartmouth	50	37 1	28				
Falmouth	50	22 00	12	Torbay	50	42 1	30				
Foy	50	35 00	34	The Bury	50	46 1	35				
Ramhead	50	34 00	49	Abloom Bar	50	47 1	37				
Plymouth	50	36 00	51	Lime	50	55 2	10				
The Edifstone	50	22 00	44	Chiddock	50	57 2	14				
The Start	50	27 1	16	Portland	50	50 2	36				
				Weymouth	51	3 2	44				
				Pool	51	43 3	34				
				Isle of Wight	50	58 4	00				



## A TABLE of Natural and

32 DEGREES.

M	N. Sine.	N. Co-Sine.	V. Tangent.	V. Co-Tang.	N. Secant.	N. Co-Secant.	M
30	5372925	8433914	6370703	15696856	11856891	18611590	30
31	5375449	8432351	6374793	15686784	11859089	18603096	29
32	5377902	8430787	6378885	15676722	11861289	18594612	28
33	5380354	8429222	6382978	15666669	11863491	18586135	27
34	5382806	8427657	6387073	15656625	11865695	18577672	26
35	5385257	8426091	6391169	15646590	11867900	18569216	25
36	5387708	8424524	6395267	15636564	11870107	18560752	24
37	5390158	8422956	6399366	15626548	11872316	18552331	23
38	5392608	8421388	6403467	15616540	11874527	18543903	22
39	5395058	8419819	6407569	15606542	11876740	18535485	21
40	5397507	8418249	6411673	15596552	11878955	18527073	20
41	5399955	8416679	6415779	15586572	11881171	18518672	19
42	5402403	8415108	6419886	15576601	11883389	18510281	18
43	5404851	8413536	6423995	15566639	11885609	18501898	17
44	5407295	8411963	6428105	15556685	11887831	18493523	16
45	5409745	8410390	6432216	15546741	11890055	18485161	15
46	5412191	8408816	6436329	15536806	11892281	18476805	14
47	5414637	8407241	6440444	15526880	11894508	18468459	13
48	5417082	8405666	6444560	15516963	11896737	18460123	12
49	5419527	8404090	6448678	15507054	11898968	18451795	11
50	5421971	8402513	6452797	15497155	11901201	18443476	10
51	5424415	8400935	6456918	15487264	11903436	18435166	9
52	5426859	8399357	6461041	15477383	11905673	18426866	8
53	5429302	8397778	6465165	15467510	11907912	18418574	7
54	5431746	8396198	6469290	15457645	11910152	18410292	6
55	5434185	8394618	6473417	15447792	11912394	18402018	5
56	5436628	8393037	6477546	15437946	11914638	18393753	4
57	5439069	8391455	6481676	15428108	11916884	18385498	3
58	5441510	8389873	6485808	15418280	11919132	18377251	2
59	5443950	8388290	6489941	15408460	11921382	18369013	1
60	5446390	8386706	6494075	15398650	11923633	18360784	0
V. Co-Sine.			N. Tangent.	N. Co-Tang.	N. Secant.	N. Co-Secant.	M

57 DEGREES.

## A Table of the Latitude and Longitude

The Places Names.	North		East		The Places Names.	North		East	
	Latitud.	Longit.	Latitud.	Longit.		Latitud.	Longit.	Latitud.	Longit.
	D.	M.	D.	M.		D.	M.	D.	M.
Portsmouth	51	8	4	24	North Foreland	51	28	6	44
Shoram	51	7	4	57	Margaret	51	29	6	34
Beache	50	58	5	15	Quinhorough	51	30	6	01
Rye	51	13	6	09	Rochester	51	28	5	54
Dongeneys	51	9	5	15	London	51	33	5	24
Dover	51	25	6	32	Graveland	51	33	5	44
Ripraps	51	13	6	49	Tilbury Hope	51	33	5	54
The South Foreland	51	22	6	44	Colchester	52	04	6	02
The Downs	51	24	6	45	Harwich	52	11	6	27
Sandwich	51	27	6	33	Ipswich	52	14	6	24

## Artificial Sines, Tangents, and Secants.

32 DEGREES.

M	L. Sine.	L. Co-Sine.	L. Tangent.	L. Co-Tang.	L. Secant.	L. Co-Secant.	
30	9.7302165	9.9262292	9.8041873	10.1255127	10.0739705	10.2627835	30
31	9.7304148	9.9259187	9.8041691	10.1255339	10.0741513	10.2625852	29
32	9.7306129	9.9256081	9.8041447	10.1255553	10.0743319	10.2623871	28
33	9.7308109	9.9252975	9.8041203	10.1255767	10.0745125	10.2621891	27
34	9.7310087	9.9249869	9.8040959	10.1255981	10.0746931	10.2619911	26
35	9.7312064	9.9246763	9.8040715	10.1256195	10.0748737	10.2617931	25
36	9.7314040	9.9243657	9.8040471	10.1256413	10.0750545	10.2615960	24
37	9.7316015	9.9240551	9.8040227	10.1256630	10.0752354	10.2613935	23
38	9.7317989	9.9237445	9.8040000	10.1256848	10.0754163	10.2612011	22
39	9.7319961	9.9234339	9.8039773	10.1257066	10.0755972	10.2610087	21
40	9.7321932	9.9231233	9.8039546	10.1257286	10.0757782	10.2608163	20
41	9.7323902	9.9228127	9.8039294	10.1257505	10.0759592	10.2606239	19
42	9.7325870	9.9225021	9.8039023	10.1257727	10.0761403	10.2604310	18
43	9.7327837	9.9221915	9.8038705	10.1257948	10.0763214	10.2602387	17
44	9.7329803	9.9218809	9.8038389	10.1258169	10.0765026	10.2600463	16
45	9.7331768	9.9215703	9.8038066	10.1258391	10.0766839	10.2598540	15
46	9.7333731	9.9212597	9.8037693	10.1258611	10.0768652	10.2596617	14
47	9.7335693	9.9209491	9.8037318	10.1258834	10.0770466	10.2594694	13
48	9.7337656	9.9206385	9.8036933	10.1259056	10.0772281	10.2592771	12
49	9.7339618	9.9203279	9.8036547	10.1259279	10.0774096	10.2590848	11
50	9.7341572	9.9200173	9.8036162	10.1259503	10.0775912	10.2588925	10
51	9.7343529	9.9197067	9.8035777	10.1259727	10.0777728	10.2586999	9
52	9.7345483	9.9193961	9.8035392	10.1259952	10.0779545	10.2585073	8
53	9.7347440	9.9190855	9.8035007	10.1260177	10.0781362	10.2583147	7
54	9.7349393	9.9187749	9.8034622	10.1260403	10.0783180	10.2581222	6
55	9.7351345	9.9184643	9.8034237	10.1260629	10.0785000	10.2579297	5
56	9.7353296	9.9181537	9.8033852	10.1260856	10.0786821	10.2577372	4
57	9.7355246	9.9178431	9.8033467	10.1261083	10.0788643	10.2575447	3
58	9.7357195	9.9175325	9.8033082	10.1261310	10.0790466	10.2573522	2
59	9.7359142	9.9172219	9.8032697	10.1261538	10.0792290	10.2571597	1
60	9.7361088	9.9169113	9.8032312	10.1261765	10.0794115	10.2569672	0
L. Co-Sine.			L. Sine.	L. Co-Tang.	L. Tangent.	L. Co-Secant.	L. Secant.
							M

57 DEGREES.

## of the Chiefest Places of the World.

The Places Names.	North		East		The Places Names.	North		East	
	Latitud.	Longit.	Latitud.	Longit.		Latitud.	Longit.	Latitud.	Longit.
	D.	M.	D.	M.		D.	M.	D.	M.
Orfordnefs	52	20	6	35	Hull	53	45	4	16
Alborow	52	24	6	39	The Sporne	53	45	5	01
Yarmouth	52	45	6	42	Burlington	51	00	4	28
Winterton	52	52	6	46	Flamborough Head	54	8	4	35
Cromar	53	20	6	41	Scarborough	54	20	4	21
Blacknefs	53	46	19		Whitby	54	35	10	
Wells	53	76	02		Hartlepool	54	37	29	
Lin	52	58	5	33	Sunderland	54	47	3	26
Boston	53	9	5	02	Shelds	53	02	3	24
Grimsbe	53	39	4	28	Newcastle.	54	58	3	14



## A TABLE of Natural and

## 33 DEGREES.

M	N. Sine.	N. Co-Sine.	V. Tangent.	V. Co-Tangent.	N. Secant.	N. Co-Secant.
0	5446392	8386726	6427076	15398650	11923633	18360784
1	5445830	8386121	6428212	15398848	11923886	18352554
2	5445262	8385515	6429350	15399055	11924141	18344353
3	5444697	8384907	6430490	15399270	11924393	18336151
4	5444135	8384298	6431631	15399484	11924652	18327958
5	5443565	8383687	6432773	15399701	11924913	18319774
6	5442997	8383075	6433917	15399920	11925178	18311599
7	5442430	8382462	6435062	15400140	11925445	18303432
8	5441862	8381848	6436208	15400362	11925712	18295272
9	5441295	8381233	6437355	15400585	11925980	18287119
10	5440728	8380617	6438502	15400809	11926249	18278973
11	5440161	8379999	6439650	15401034	11926518	18270834
12	5439594	8379381	6440798	15401260	11926788	18262702
13	5439027	8378762	6441946	15401486	11927058	18254577
14	5438460	8378143	6443094	15401713	11927329	18246459
15	5437893	8377523	6444242	15401940	11927600	18238348
16	5437326	8376902	6445390	15402167	11927871	18230234
17	5436759	8376281	6446538	15402394	11928142	18222117
18	5436192	8375660	6447686	15402621	11928413	18214007
19	5435625	8375039	6448834	15402848	11928684	18205894
20	5435058	8374418	6449982	15403075	11928955	18197778
21	5434491	8373797	6451130	15403302	11929226	18189659
22	5433924	8373176	6452278	15403529	11929497	18181538
23	5433357	8372555	6453426	15403756	11929768	18173415
24	5432790	8371934	6454574	15403983	11930039	18165290
25	5432223	8371313	6455722	15404210	11930310	18157163
26	5431656	8370692	6456870	15404437	11930581	18149034
27	5431089	8370071	6458018	15404664	11930852	18140903
28	5430522	8369450	6459166	15404891	11931123	18132770
29	5429955	8368829	6460314	15405118	11931394	18124635
30	5429388	8368208	6461462	15405345	11931665	18116500
31	5428821	8367587	6462610	15405572	11931936	18108363
32	5428254	8366966	6463758	15405799	11932207	18100225
33	5427687	8366345	6464906	15406026	11932478	18092086

## 36 DEGREES.

## Table of the Latitude and Longitude

The Coast of Scotland.				The Places Names.			
The Places Names.		North	East	Latitude		North	East
		Latitud.	Longit.			Latitud.	Longit.
		D. M. D. M.				D. M. D. M.	
Berwick		55	42	2	30	58	43
Leith		56	32	09		57	40
Dundee		56	26	2	17	57	40
Aberdeen		57	22	2	20	57	40
Bafom Nals		57	48	1	34	58	3
Cat Nals		58	3	1	38	58	3
Illes of Orkney		58	56	2	02	59	30
Fair Isle		59	30	3	10		

The Sea-coast from the Lizard to Holy-Head.

Lands End	50	20	0	34
Gulfe	50	11	1	22

## Artificial Sines, Tangents, and Secants.

## 33 DEGREES.

M	L. Sine.	L. Co-Sine.	L. Tangent.	L. Co-Tang.	L. Secant.	L. Co-Secant.
0	9.7361088	9.9225914	9.8128174	10.1874826	10.1874826	10.2335912
1	9.7363032	9.9225909	9.8127939	10.1872161	10.1872161	10.2335912
2	9.7364976	9.9225904	9.8127703	10.1869496	10.1869496	10.2335912
3	9.7366918	9.9225899	9.8127468	10.1866831	10.1866831	10.2335912
4	9.7368859	9.9225894	9.8127232	10.1864166	10.1864166	10.2335912
5	9.7370799	9.9225889	9.8126997	10.1861501	10.1861501	10.2335912
6	9.7372737	9.9225884	9.8126761	10.1858836	10.1858836	10.2335912
7	9.7374675	9.9225879	9.8126526	10.1856171	10.1856171	10.2335912
8	9.7376611	9.9225874	9.8126290	10.1853506	10.1853506	10.2335912
9	9.7378546	9.9225869	9.8126055	10.1850841	10.1850841	10.2335912
10	9.7380480	9.9225864	9.8125819	10.1848176	10.1848176	10.2335912
11	9.7382412	9.9225859	9.8125584	10.1845511	10.1845511	10.2335912
12	9.7384343	9.9225854	9.8125348	10.1842846	10.1842846	10.2335912
13	9.7386273	9.9225849	9.8125113	10.1840181	10.1840181	10.2335912
14	9.7388202	9.9225844	9.8124877	10.1837516	10.1837516	10.2335912
15	9.7390129	9.9225839	9.8124642	10.1834851	10.1834851	10.2335912
16	9.7392055	9.9225834	9.8124406	10.1832186	10.1832186	10.2335912
17	9.7393980	9.9225829	9.8124171	10.1829521	10.1829521	10.2335912
18	9.7395904	9.9225824	9.8123935	10.1826856	10.1826856	10.2335912
19	9.7397827	9.9225819	9.8123700	10.1824191	10.1824191	10.2335912
20	9.7399748	9.9225814	9.8123464	10.1821526	10.1821526	10.2335912
21	9.7401668	9.9225809	9.8123229	10.1818861	10.1818861	10.2335912
22	9.7403587	9.9225804	9.8122993	10.1816196	10.1816196	10.2335912
23	9.7405505	9.9225799	9.8122758	10.1813531	10.1813531	10.2335912
24	9.7407421	9.9225794	9.8122522	10.1810866	10.1810866	10.2335912
25	9.7409337	9.9225789	9.8122287	10.1808201	10.1808201	10.2335912
26	9.7411251	9.9225784	9.8122051	10.1805536	10.1805536	10.2335912
27	9.7413164	9.9225779	9.8121816	10.1802871	10.1802871	10.2335912
28	9.7415075	9.9225774	9.8121580	10.1799999	10.1799999	10.2335912
29	9.7416986	9.9225769	9.8121345	10.1797334	10.1797334	10.2335912
30	9.7418895	9.9225764	9.8121109	10.1794669	10.1794669	10.2335912

## 36 DEGREES.

## of the Chief Places of the World.

The Places Names.				The Places Names.			
		North	East			North	East
		Latitud.	Longit.			Latitud.	Longit.
		D. M. D. M.				D. M. D. M.	
Scilly		50	7	1	21	53	12
7 Stones		50	18	1	16	53	13
Harty Point		51	100	E. 19		53	13
London		51	200	W. 3		53	13
Holms		51	26	E. 44		53	13
Bristol		51	29	2	34	53	13
Glocester		52	3	2	39	53	13
Caldy		51	53	0	10	53	13
Milford		52	5	0	10	53	13
Ramza		52	12	0	38	53	13

The Sea-coast of Ireland.

Lambay	53	4	1	45
Dublin	53	32	1	56



## A TABLE of Natural and

33 DEGREES.

M	N. Sine.	N. Co-Sine.	N. Tangent.	N. Co-Tang.	N. Secant.	N. Co-Secant.	
30	5519370	8335553	6615356	15108352	11992049	18118010	30
31	5521795	8337252	6623042	15095507	11994359	18110052	29
32	5524220	8338945	6630725	15082271	11996671	18102102	28
33	5526645	8340638	6638413	15069024	11998985	18094161	27
34	5529069	8342330	6646102	15055774	12001301	18086228	26
35	5531492	8344021	6653792	15042519	12003619	18078304	25
36	5533915	8345712	6661484	15029261	12005938	18070388	24
37	5536338	8347402	6669178	15016001	12008259	18062481	23
38	5538760	8349091	6676873	15002739	12010582	18054582	22
39	5541182	8350780	6684569	14989475	12012907	18046691	21
40	5543603	8352468	6692265	14976210	12015234	18038809	20
41	5546024	8354155	6700000	14962944	12017563	18030935	19
42	5548444	8355841	6707784	14949677	12019894	18023070	18
43	5550864	8357527	6715568	14936409	12022227	18015213	17
44	5553283	8359212	6723350	14923140	12024562	18007365	16
45	5555702	8360896	6731131	14909870	12026899	17999515	15
46	5558121	8362579	6738911	14896600	12029237	17991663	14
47	5560539	8364261	6746690	14883329	12031577	17983809	13
48	5562956	8365943	6754468	14870058	12033919	17975954	12
49	5565373	8367624	6762246	14856787	12036264	17968101	11
50	5567790	8369305	6770024	14843515	12038610	17960248	10
51	5570206	8370985	6777802	14830244	12040958	17952395	9
52	5572621	8372665	6785580	14816972	12043308	17944542	8
53	5575036	8374344	6793358	14803701	12045660	17936689	7
54	5577451	8376023	6801136	14790429	12048014	17928837	6
55	5579865	8377702	6808914	14777158	12050370	17920985	5
56	5582279	8379381	6816692	14763887	12052728	17913133	4
57	5584693	8381060	6824470	14750615	12055088	17905281	3
58	5587107	8382739	6832248	14737344	12057450	17897429	2
59	5589521	8384418	6840026	14724072	12059814	17889577	1
60	5591935	8386097	6847804	14710801	12062180	17881725	0
N. Co-Sine.		N. Sine.	N. Co-Tang.	N. Tangent.	N. Co-Secant.	N. Secant.	M

56 DEGREES.

## A Table of the Latitude and Longitude

The Places Names.	North Latitude.	West Longitude.	The Places Names.	North Latitude.	West Longitude.
Wexford	52 33 1	44	Loopas Head	52 44 5	41
Waterford	52 30 2	24	Gally Head	53 20 5	36
Corke	52 01 2	56	Galloway	43 40 5	16
Kingfail	51 52 3	08	Illes of Arran	53 21 6	36
Old Head	51 40 3	14	Slages	54 27 6	21
Mizard Head	51 28 5	21	Illes of Arc	55 18 5	36
Cow and Calf	51 42 5	42	Fore Head	55 38 4	56
Skullakes	52 00 6	06	Fair Foreland	55 35 2	36
Blaskos	52 15 5	11			
Linnrick	53 04 4	51			

## Artificial Sines, Tangents, and Secants.

33 DEGREES.

M	L. Sine.	L. Co-Sine.	L. Tangent.	L. Co-Tang.	L. Secant.	L. Co-Secant.	
30	9.7418895	9.2921066	9.8207829	10.1792171	10.0758934	10.2581105	30
31	9.7422803	9.2910229	9.8210574	10.1789426	10.0757771	10.2579197	29
32	9.7427110	9.2899393	9.8213317	10.1786683	10.0756607	10.2577290	28
33	9.7431416	9.2888555	9.8216060	10.1783940	10.0755445	10.2575384	27
34	9.7435720	9.2877717	9.8218803	10.1781197	10.0754283	10.2573480	26
35	9.7440023	9.2866879	9.8221545	10.1778455	10.0753122	10.2571577	25
36	9.7444325	9.2856039	9.8224288	10.1775714	10.0751961	10.2569675	24
37	9.7448626	9.2845200	9.8227026	10.1772974	10.0750800	10.2567774	23
38	9.7452926	9.2834360	9.8229766	10.1770234	10.0749640	10.2565872	22
39	9.7457226	9.2823519	9.8232505	10.1767495	10.0748481	10.2563976	21
40	9.7461526	9.2812678	9.8235244	10.1764756	10.0747322	10.2562079	20
41	9.7465826	9.2801836	9.8237981	10.1762017	10.0746164	10.2560183	19
42	9.7470126	9.2790994	9.8240719	10.1759278	10.0745006	10.2558288	18
43	9.7474426	9.2780151	9.8243455	10.1756539	10.0743849	10.2556394	17
44	9.7478726	9.2769309	9.8246191	10.1753800	10.0742692	10.2554502	16
45	9.7483026	9.2758467	9.8248926	10.1751061	10.0741536	10.2552610	15
46	9.7487326	9.2747624	9.8251660	10.1748322	10.0740381	10.2550720	14
47	9.7491626	9.2736781	9.8254394	10.1745583	10.0739225	10.2548831	13
48	9.7495926	9.2725938	9.8257127	10.1742844	10.0738070	10.2546944	12
49	9.7500226	9.2715095	9.8259860	10.1740105	10.0736915	10.2545057	11
50	9.7504526	9.2704252	9.8262593	10.1737366	10.0735760	10.2543172	10
51	9.7508826	9.2693409	9.8265326	10.1734627	10.0734605	10.2541288	9
52	9.7513126	9.2682566	9.8268059	10.1731888	10.0733450	10.2539405	8
53	9.7517426	9.2671723	9.8270792	10.1729149	10.0732295	10.2537522	7
54	9.7521726	9.2660880	9.8273525	10.1726410	10.0731140	10.2535639	6
55	9.7526026	9.2650037	9.8276258	10.1723671	10.0730000	10.2533756	5
56	9.7530326	9.2639194	9.8278991	10.1720932	10.0728855	10.2531873	4
57	9.7534626	9.2628351	9.8281724	10.1718193	10.0727715	10.2530000	3
58	9.7538926	9.2617508	9.8284457	10.1715454	10.0726575	10.2528127	2
59	9.7543226	9.2606665	9.8287190	10.1712715	10.0725435	10.2526254	1
60	9.7547526	9.2595822	9.8289923	10.1710000	10.0724295	10.2524381	0
L. Co-Sine.		L. Sine.	L. Co-Tang.	L. Tangent.	L. Co-Secant.	L. Secant.	M

56 DEGREES.

## of the Chiefst Places of the World.

From Naze of Norway to Archangel.	The Places Names.	North Latitude.	East Longitude.	The Places Names.	North Latitude.	East Longitude.
The Naze of Norway	D. M. D. M.	D. M. D. M.		Gripso	D. M. D. M.	D. M. D. M.
	58 00 0	0 26			63 40 11	26
Stave Angor	58 57 9	44		Rois Illes	67 1 13	30
Out Shers	59 7 3	30		Werro	67 3 13	52
Bomal	59 31 9	04		Lawfat	68 30 14	40
Harla Island	60 24 9	02		Zanham	70 28 18	32
Katts Nafs	61 54 8	06		Assumption	71 7 20	38
Swin	62 40 9	10		North Cape	71 22 22	6
Gallee	62 52 9	46		Skitanboro	70 56 24	2
				Island Kilding	68 54 26	16
				Cape Race	65 49 29	28



## A TABLE of Natural and

34 DEGREES.

M	N. Sine.	N. Co-Sine.	N. Tangent.	N. Co-Tang.	N. Secant.	N. Co-Secant.	
0	5591929	8290376	6743005	14825610	12052180	17882516	65
1	5594349	8288748	6749315	14816311	12054548	17875208	59
2	5596971	8287121	6753553	14807921	12056918	17868568	58
3	5599515	8285493	6757790	14799731	12059289	17861917	57
4	5602171	8283864	6762028	14791546	12061662	17855233	56
5	5604838	8282234	6766265	14783372	12064037	17848447	55
6	5607506	8280603	6770502	14775203	12066414	17841752	54
7	5610172	8278972	6774739	14767038	12068793	17835051	53
8	5612838	8277340	6778975	14758871	12071175	17828359	52
9	5615504	8275707	6783212	14750704	12073559	17821655	51
10	5618169	8274074	6787449	14742537	12075944	17814951	50
11	5620834	8272440	6791686	14734374	12078331	17808247	49
12	5623499	8270805	6795923	14726211	12080720	17801543	48
13	5626164	8269170	6800160	14718048	12083112	17794839	47
14	5628829	8267534	6804397	14709885	12085505	17788135	46
15	5631494	8265897	6808634	14701722	12087899	17781431	45
16	5634159	8264260	6812871	14693559	12090293	17774727	44
17	5636824	8262622	6817108	14685396	12092687	17768023	43
18	5639489	8260985	6821345	14677233	12095082	17761319	42
19	5642154	8259348	6825582	14669070	12097476	17754615	41
20	5644819	8257711	6829819	14660907	12100000	17747911	40
21	5647484	8256074	6834056	14652744	12102524	17741207	39
22	5650149	8254437	6838293	14644581	12105048	17734503	38
23	5652814	8252800	6842530	14636418	12107572	17727799	37
24	5655479	8251163	6846767	14628255	12110096	17721095	36
25	5658144	8249526	6851004	14620092	12112620	17714391	35
26	5660809	8247889	6855241	14611929	12115144	17707687	34
27	5663474	8246252	6859478	14603766	12117668	17700983	33
28	5666139	8244615	6863715	14595603	12120192	17694279	32
29	5668804	8242978	6867952	14587440	12122716	17687575	31
30	5671469	8241341	6872189	14579277	12125240	17680871	30
	N. Co-Sine.	N. Sine.	N. Co-Tang.	N. Tangent.	N. Co-Secant.	N. Secant.	M

55 DEGREES.

## A Table of the Latitude and Longitude

The Places Names.	North Latitude.	East Longit.	The Places Names.	North Latitude.	East Longit.
Cape Gallant	67 11 28	56	Nageo Point	77 45 22	31
Cape Grace	65 17 28	54	Duckus Cove	78 25 23	26
Fox Naze	63 12 26	31	Cape Blanche	79 27 24	19
Archangel	63 22 26	46	Helis Sound	76 25 20	18
			Point Lookout	78 38 20	3
			Ball Sound	77 7 20	45
			Foe Sound	79 15 19	55
			Horn Sound	78 32 18	34
			Deer Sound		
			Black point		
The Coast of Greenland.					
Cherri Island	74 34 20	31			
Hope Island	76 13 23	16			
Hopeless Isles	77 00 22	54			

## Artificial Sines, Tangents, and Secants.

34 DEGREES.

M	L. Sine.	L. Co-Sine.	L. Tangent.	L. Co-Tang.	L. Secant.	L. Co-Secant.	
0	9.7575617	9.9185742	9.8289874	10.1710126	10.0314238	10.2524353	55
1	9.7477489	9.9184590	9.8292599	10.1707491	10.0315110	10.2522511	59
2	9.7479360	9.9184037	9.8295324	10.1704857	10.0315983	10.2520669	58
3	9.7481230	9.9183483	9.8298049	10.1702223	10.0316856	10.2518827	57
4	9.7483099	9.9182929	9.8300774	10.1699589	10.0317729	10.2516985	56
5	9.7484967	9.9182375	9.8303499	10.1696953	10.0318602	10.2515143	55
6	9.7486833	9.9181821	9.8306224	10.1694317	10.0319475	10.2513301	54
7	9.7488699	9.9181267	9.8308949	10.1691681	10.0320348	10.2511459	53
8	9.7490565	9.9180713	9.8311674	10.1689045	10.0321221	10.2509617	52
9	9.7492431	9.9180159	9.8314399	10.1686409	10.0322094	10.2507775	51
10	9.7494297	9.9179605	9.8317124	10.1683773	10.0322967	10.2505933	50
11	9.7496163	9.9179051	9.8319849	10.1681137	10.0323840	10.2504091	49
12	9.7498029	9.9178497	9.8322574	10.1678501	10.0324713	10.2502249	48
13	9.7499895	9.9177943	9.8325299	10.1675865	10.0325586	10.2500407	47
14	9.7501761	9.9177389	9.8328024	10.1673229	10.0326459	10.2498565	46
15	9.7503627	9.9176835	9.8330749	10.1670593	10.0327332	10.2496723	45
16	9.7505493	9.9176281	9.8333474	10.1667957	10.0328205	10.2494881	44
17	9.7507359	9.9175727	9.8336199	10.1665321	10.0329078	10.2493039	43
18	9.7509225	9.9175173	9.8338924	10.1662685	10.0329951	10.2491197	42
19	9.7511091	9.9174619	9.8341649	10.1660049	10.0330824	10.2489355	41
20	9.7512957	9.9174065	9.8344374	10.1657413	10.0331697	10.2487513	40
21	9.7514823	9.9173511	9.8347099	10.1654777	10.0332570	10.2485671	39
22	9.7516689	9.9172957	9.8349824	10.1652141	10.0333443	10.2483829	38
23	9.7518555	9.9172403	9.8352549	10.1649505	10.0334316	10.2481987	37
24	9.7520421	9.9171849	9.8355274	10.1646869	10.0335189	10.2480145	36
25	9.7522287	9.9171295	9.8357999	10.1644233	10.0336062	10.2478303	35
26	9.7524153	9.9170741	9.8360724	10.1641597	10.0336935	10.2476461	34
27	9.7526019	9.9170187	9.8363449	10.1638961	10.0337808	10.2474619	33
28	9.7527885	9.9169633	9.8366174	10.1636325	10.0338681	10.2472777	32
29	9.7529751	9.9169079	9.8368899	10.1633689	10.0339554	10.2470935	31
30	9.7531617	9.9168525	9.8371624	10.1631053	10.0340427	10.2469093	30
	L. Co-Sine.	L. Sine.	L. Co-Tang.	L. Tangent.	L. Co-Secant.	L. Secant.	M

55 DEGREES.

## of the Chiefest Places of the World.

The Places Names.	North Latitude.	East Longit.	The Places Names.	North Latitude.	East Longit.
Cape Cold	79 00 17	56	Witmond	55 20 16	32
Fair Foreland	79 15 19	29	Ilmond	55 20 16	41
			Burnholm	56 00 17	40
			Erthholm	56 10 17	58
			Gathe fand	56 15 22	03
			Farro Sound	58 48 21	53
			Gotland	58 20 21	22
			Heda	55 53 21	29
			Dormamel	56 55 23	44
			Dines Nat's	58 22 23	55
The Sea-coast in the Sound.					
Lizol	57 35 14	09			
Anall	57 05 14	41			
Ellen-nore	56 40 15	21			
Copenhagen	56 15 15	18			
Moan	55 41 15	20			



## A TABLE of Natural and

## 34 DEGREES.

M	N. Sine.	N. Co-Sine.	N. Tangent.	N. Co-Tangent.	N. Secant.	N. Co-Secant.
30	5664662	8241262	6872810	14550990	12134064	17655173
31	5665459	8239614	6877274	14541027	12136491	17647702
32	5666885	8237965	6881379	14531971	12138920	17640243
33	5667125	8236316	6885666	14522923	12141351	17632791
34	5667364	8234666	6889955	14513883	12143783	17625345
35	5667604	8233015	6894246	14504853	12146215	17617905
36	5667843	8231364	6898533	14495825	12148645	17610475
37	5668081	8229712	6902822	14486808	12151074	17603056
38	5668325	8228059	6907120	14477799	12153503	17595636
39	5668568	8226405	6911425	14468796	12155933	17588216
40	5668811	8224751	6915724	14459791	12158363	17580797
41	5669053	8223096	6920025	14450814	12160793	17573378
42	5669295	8221442	6924325	14441834	12163219	17565961
43	5669536	8219784	6928623	14432862	12165645	17558547
44	5669777	8218127	6932920	14423897	12168070	17551131
45	5670015	8216469	6937217	14414940	12170495	17543715
46	5670255	8214811	6941515	14405991	12172919	17536299
47	5670493	8213152	6945815	14397049	12175343	17528883
48	5670732	8211492	6950114	14388114	12177765	17521467
49	5670971	8209831	6954416	14379187	12180188	17514051
50	5671212	8208172	6958713	14370265	12182610	17506635
51	5671452	8206513	6963011	14361356	12185033	17499219
52	5671693	8204854	6967311	14352451	12187455	17491803
53	5671933	8203193	6971611	14343551	12189878	17484387
54	5672174	8201531	6975912	14334664	12192300	17476971
55	5672414	8199864	6980212	14325781	12194723	17469555
56	5672655	8198199	6984513	14316906	12197145	17462139
57	5672895	8196523	6988813	14308039	12200000	17454723
58	5673136	8194846	6993114	14299176	12202855	17447307
59	5673376	8193169	6997415	14290326	12205710	17439891
60	5673617	8191492	7001716	14281480	12208565	17432475
N. Co-Sine. N. Sine. N. Co-Tangent. N. Tangent. N. Secant. N. Co-Secant.						

## 55 DEGREES.

## A Table of the Latitude and Longitude

The Places Names.	North Latitude.	East Longitude.	The Places Names.	North Latitude.	East Longitude.
Riga	57 50 26	25	Wibro	61 16 30	00
Ruman	57 38 25	14	Wakato	61 16 20	42
Parun	58 52 26	54	Patting	61 00 28	45
Shorham	58 58 26	30	Burga	61 02 27	14
Wile	59 06 25	06	Roftbregu	61 03 25	04
Ardenbro	59 05 24	06	Abho	61 08 23	28
Dagarat	59 44 23	55	Buhoers	60 09 21	54
Ogholm	59 58 24	32	Stockholm	59 49 20	06
Norgin	60 10 25	14	Froucnboro	58 45 18	16
East Rand	50 12 28	41	Strickholm	58 23 18	24

## Artificial Sines, Tangents, and Secants.

## 34 DEGREES.

M	L. Sine.	L. Co-Sine.	L. Tangent.	L. Co-Tangent.	L. Secant.	L. Co-Secant.
30	9-7531280	9-9159937	9-7371543	10-1625617	10-2313063	10-2463720
31	9-7533118	9-9159269	9-7374249	10-1625951	10-2313951	10-2465382
32	9-7534954	9-9158600	9-7376955	10-1626285	10-2314840	10-2467045
33	9-7536790	9-9157930	9-7379660	10-1626619	10-2315729	10-2468708
34	9-7538624	9-9157260	9-7382366	10-1626953	10-2316618	10-2470371
35	9-7540457	9-9156590	9-7385071	10-1627287	10-2317507	10-2472034
36	9-7542288	9-9155920	9-7387777	10-1627621	10-2318396	10-2473697
37	9-7544119	9-9155250	9-7390482	10-1627955	10-2319285	10-2475360
38	9-7545949	9-9154580	9-7393188	10-1628289	10-2320174	10-2477023
39	9-7547777	9-9153910	9-7395893	10-1628623	10-2321063	10-2478686
40	9-7549604	9-9153240	9-7398599	10-1628957	10-2321952	10-2480349
41	9-7551431	9-9152570	9-7401304	10-1629291	10-2322841	10-2482012
42	9-7553256	9-9151900	9-7404009	10-1629625	10-2323730	10-2483675
43	9-7555080	9-9151230	9-7406714	10-1630000	10-2324619	10-2485338
44	9-7556902	9-9150560	9-7409419	10-1630375	10-2325508	10-2487001
45	9-7558724	9-9149890	9-7412124	10-1630750	10-2326397	10-2488664
46	9-7560546	9-9149220	9-7414829	10-1631125	10-2327286	10-2490327
47	9-7562368	9-9148550	9-7417534	10-1631500	10-2328175	10-2491990
48	9-7564189	9-9147880	9-7420239	10-1631875	10-2329064	10-2493653
49	9-7565999	9-9147210	9-7422944	10-1632250	10-2329953	10-2495316
50	9-7567815	9-9146540	9-7425649	10-1632625	10-2330842	10-2496979
51	9-7569630	9-9145870	9-7428354	10-1633000	10-2331731	10-2498642
52	9-7571444	9-9145200	9-7431059	10-1633375	10-2332620	10-2500305
53	9-7573256	9-9144530	9-7433764	10-1633750	10-2333509	10-2501968
54	9-7575068	9-9143860	9-7436469	10-1634125	10-2334398	10-2503631
55	9-7576879	9-9143190	9-7439174	10-1634500	10-2335287	10-2505294
56	9-7578687	9-9142520	9-7441879	10-1634875	10-2336176	10-2506957
57	9-7580495	9-9141850	9-7444584	10-1635250	10-2337065	10-2508620
58	9-7582302	9-9141180	9-7447289	10-1635625	10-2337954	10-2510283
59	9-7584108	9-9140510	9-7449994	10-1636000	10-2338843	10-2511946
60	9-7585913	9-9139840	9-7452699	10-1636375	10-2339732	10-2513609
L. Co-Sine. L. Sine. L. Co-Tangent. L. Tangent. L. Secant. L. Co-Secant.						

## 55 DEGREES.

## of the Chiefest Places of the World.

The Places Names.	North Latitude.	East Longitude.	The Places Names.	North Latitude.	East Longitude.
Yaffro	58 10 18	58	Walle Sound	58 25 11	40
Fulan	57 42 19	12	Long Sound	59 07 12	54
Chiping	56 53 18	27	Two Sea-coast of Flanders and Holland, from Callis to the Scaw.		
Fastinboro	56 02 15	49	Dunkirk	51 18 27	49
Scarlet Island	56 40 16	02	Ofend	51 30 18	29
Elfinbro	56 46 16	00	Stuice	51 58 29	11
Cape Cole	57 00 15	36	Zealand	51 48 09	05
Nading	57 53 15	04			
Holm Sound	59 08 13	44			
Mordo	58 37 12	02			



## A TABLE of Natural and

35 DEGREES.

M	N. Sine.	V. Co-Sine.	N. Tangent.	N. Co-Tang.	N. Secant.	N. Co-Secant.	
0	5735764	5191521	7022275	14281480	12207746	17434468	65
1	5735847	5189582	7026111	14272642	12210233	17427229	59
2	5735929	5188182	7030749	14263311	12212723	17419997	58
3	5736011	5186512	7035589	14253947	12215215	17412773	57
4	5736092	5184841	7040430	14244071	12217709	17405556	56
5	5736172	5183169	7045273	14234302	12220204	17398345	55
6	5736252	5181497	7050118	14224561	12222702	17391145	54
7	5736332	5179824	7054965	14214866	12225202	17383951	53
8	5736411	5178150	7059813	14205197	12227703	17376764	52
9	5736490	5176476	7064663	14195565	12230206	17369585	51
10	5736568	5174801	7069515	14185961	12232713	17362413	50
11	5736646	5173125	7074369	14176384	12235223	17355247	49
12	5736723	5171449	7079225	14166834	12237735	17348090	48
13	5736800	5169772	7084083	14157301	12240248	17340941	47
14	5736876	5168094	7088943	14147784	12242763	17333798	46
15	5736952	5166415	7093805	14138283	12245274	17326653	45
16	5737027	5164735	7098669	14128807	12247793	17319515	44
17	5737102	5163054	7103535	14119356	12250313	17312384	43
18	5737176	5161372	7108403	14109929	12252836	17305261	42
19	5737250	5159689	7113273	14100524	12255361	17298145	41
20	5737323	5158005	7118145	14091141	12257887	17291036	40
21	5737396	5156320	7123019	14081779	12260416	17283933	39
22	5737468	5154634	7127895	14072437	12262947	17276827	38
23	5737540	5152947	7132773	14063115	12265480	17269724	37
24	5737612	5151259	7137653	14053812	12268015	17262624	36
25	5737683	5149569	7142535	14044527	12270552	17255521	35
26	5737754	5147878	7147419	14035259	12273091	17248415	34
27	5737825	5146186	7152305	14026007	12275633	17241308	33
28	5737895	5144493	7157193	14016771	12278176	17234203	32
29	5737965	5142800	7162083	14007551	12280721	17227100	31
30	5738034	5141105	7166975	13998347	12283269	17220000	30
N. Co-Sine	N. Sine.	N. Co-Tang.	N. Tangent.	N. Co-Secant.	N. Secant.	M	

54 DEGREES.

## Table of the Latitude and Longitude

Part of the Latitude and Longitude							
The Places Names.		North Latitude.	East Longit.	The Places Names.		North Latitude.	East Longit.
	D.	M.	D.		D.	M.	D.
The Brill	52	08	09	Hambrough	54	04	13
Antwerp	51	37	09	Holickeland	54	30	
Rotterdam	52	05	09	Stonar	55	17	12
Amsterdam	52	40	10	The Scaw	57	52	13
The Taffel	53	20	10				
The Uly	53	30	10				
Skelling	53	35	10				
Analand	53	40	10				
Embliden	53	44	11				
Breme	53	50	12				

The Sea-coast of France, Spain, and Portugal, from Callis to Calais.

Callis	51	13	07	16
Deip	50	15	06	39

## Artificial Sines, Tangents, and Secants.

35 DEGREES.

M	L. Sine.	L. Co-Sine.	L. Tangent.	L. Co-Tang.	L. Secant.	L. Co-Secant.	
0	97589913	99132645	97589913	101547732	101547732	101547732	60
1	97589913	99132645	97589913	101547732	101547732	101547732	59
2	97589913	99132645	97589913	101547732	101547732	101547732	58
3	97589913	99132645	97589913	101547732	101547732	101547732	57
4	97589913	99132645	97589913	101547732	101547732	101547732	56
5	97589913	99132645	97589913	101547732	101547732	101547732	55
6	97589913	99132645	97589913	101547732	101547732	101547732	54
7	97589913	99132645	97589913	101547732	101547732	101547732	53
8	97589913	99132645	97589913	101547732	101547732	101547732	52
9	97589913	99132645	97589913	101547732	101547732	101547732	51
10	97589913	99132645	97589913	101547732	101547732	101547732	50
11	97589913	99132645	97589913	101547732	101547732	101547732	49
12	97589913	99132645	97589913	101547732	101547732	101547732	48
13	97589913	99132645	97589913	101547732	101547732	101547732	47
14	97589913	99132645	97589913	101547732	101547732	101547732	46
15	97589913	99132645	97589913	101547732	101547732	101547732	45
16	97589913	99132645	97589913	101547732	101547732	101547732	44
17	97589913	99132645	97589913	101547732	101547732	101547732	43
18	97589913	99132645	97589913	101547732	101547732	101547732	42
19	97589913	99132645	97589913	101547732	101547732	101547732	41
20	97589913	99132645	97589913	101547732	101547732	101547732	40
21	97589913	99132645	97589913	101547732	101547732	101547732	39
22	97589913	99132645	97589913	101547732	101547732	101547732	38
23	97589913	99132645	97589913	101547732	101547732	101547732	37
24	97589913	99132645	97589913	101547732	101547732	101547732	36
25	97589913	99132645	97589913	101547732	101547732	101547732	35
26	97589913	99132645	97589913	101547732	101547732	101547732	34
27	97589913	99132645	97589913	101547732	101547732	101547732	33
28	97589913	99132645	97589913	101547732	101547732	101547732	32
29	97589913	99132645	97589913	101547732	101547732	101547732	31
30	97589913	99132645	97589913	101547732	101547732	101547732	30
L. Co-Sine.	L. Sine.	L. Tangent.	L. Co-Tang.	L. Secant.	L. Co-Secant.	M	

54 DEGREES.

## of the Chiefest Places of the World.

of the English Ports of the North.								
<i>The Places Names.</i>	<i>North Latitud.</i>	<i>East Longit.</i>		<i>The Places Names.</i>	<i>North Latitud.</i>	<i>East Longit.</i>		
	<i>D. M. D. M.</i>				<i>D. M. D. M.</i>			
<i>Sr. Vallari</i>	50	08	05	29	<i>Jersey</i>	49	30	24
<i>Seine Head</i>	50	04	05	28	<i>Boffin</i>	49	19	03
<i>Roan</i>	49	46	05	34	<i>Colof</i>	49	05	03
<i>Cape Barlaw</i>	49	5	04	32	<i>Sr. Malloves</i>	48	45	03
<i>Cape Hogue</i>	50	04	03	52	<i>Satta Isles</i>	49	07	02
<i>Alderney</i>	50	02	03	37	<i>Morlaux</i>	48	54	01
<i>Caskats</i>	50	07	03	09	<i>Island of Basse</i>	49	01	01
<i>Ornay</i>	49	48	03	05	<i>Uthant</i>	48	48	00
<i>Garniefy</i>	49	43	02	49	<i>Conquest</i>	48	45	00
<i>Sark</i>	49	37	03	09	<i>Brest</i>	48	35	00



## A TABLE of Natural and

35 DEGREES.

M	N. Sine.	N. Co-Sine.	N. Tangent.	N. Co-Tang.	N. Secant.	N. Co-Secant.
30	5807330	9141155	7132931	14 19485	12283269	17220508
31	5809398	9133465	7137721	14 18650	12285819	17213489
32	5811765	9125775	7144713	14 18245	12289371	17206477
33	5814132	9118084	7151616	14 17935	12292925	17199472
34	5816498	9110393	7158521	13 17624	12296481	17192475
35	5818864	9102701	7165429	13 17313	12299939	17185484
36	5821230	9095009	7172341	13 17002	12303499	17178501
37	5823595	9087316	7179256	13 16691	12307061	17171525
38	5825959	9079623	7186173	13 16380	12310625	17164556
39	5828323	9071929	7193091	13 16069	12314191	17157592
40	5830687	9064236	7200011	13 15758	12317759	17150639
41	5833050	9056542	7206933	13 15447	12321329	17143691
42	5835412	9048848	7213857	13 15136	12324901	17136750
43	5837774	9041155	7220783	13 14825	12328475	17129817
44	5840135	9033462	7227711	13 14514	12332051	17122890
45	5842497	9025769	7234641	13 14203	12335629	17115970
46	5844857	9018076	7241573	13 13892	12339209	17109058
47	5847217	9010383	7248507	13 13581	12342791	17102152
48	5849577	9002689	7255443	13 13270	12346375	17095254
49	5851936	8994996	7262381	13 12959	12349961	17088364
50	5854294	8987303	7269321	13 12648	12353549	17081480
51	5856652	8979609	7276263	13 12337	12357139	17074600
52	5859009	8971916	7283207	13 12026	12360731	17067733
53	5861367	8964223	7290153	13 11715	12364325	17060869
54	5863724	8956529	7297101	13 11404	12367921	17054016
55	5866080	8948836	7304051	13 11093	12371519	17047165
56	5868435	8941143	7311003	13 10782	12375119	17040318
57	5870790	8933449	7317957	13 10471	12378721	17033475
58	5873144	8925756	7324913	13 10160	12382325	17026633
59	5875499	8918063	7331871	13 9849	12385931	17019793
60	5877853	8910369	7338831	13 9538	12389539	17012955
N. Co-Sine. N. Sine. N. Co-Tang. N. Tangent. N. Co-Secant. N. Secant. M						

54 DEGREES.

## A Table of the Latitude and Longitude

The Places Names.	North Latitude.	East Longitude.	The Places Names.	North Latitude.	East Longitude.
Camarita Bay	43	25 00 56	Piller	47	04 03 22
Seames	48	04 00 E. 23	Uls	46	04 03 20
Paiker	48	00 00 11 01	Barges	46	30 03 54
Pennes, or Pennmark	47	35 01 10	St. Martins	46	16 04 29
Glannats	47	33 01 34	Olloron	45	58 04 30
Groy	47	35 01 54	Mamofin	45	48 04 34
Belle Isle	47	19 02 14	Toppar	45	36 03 29
Cardinals	47	27 02 20	Rochel	46	17 04 54
Radon	47	55 03 33	Sherant	46	00 04 56
Nants	47	45 04 15	Rochfort	45	28 05 19

## Artificial Sines, Tangents, and Secants.

35 DEGREES.

M	L. Sine.	L. Co-Sine.	L. Tangent.	L. Co-Tang.	L. Secant.	L. Co-Secant.
30	97639540	99106360	98532630	101467320	100593140	102350460
31	976541311	99105959	98533532	101464515	100593101	102350889
32	976543080	99105057	98533023	101461977	100593143	102350929
33	976544394	99104155	985342694	101459306	100593146	102351151
34	976546616	99103251	98534365	101456535	100593149	102351384
35	976549382	99102348	985346034	101453566	100593152	102351618
36	976550147	99101444	985348704	101451295	100593155	102349853
37	976551911	99100539	985351372	101448685	100593158	102348089
38	976553674	99099634	985354041	101445959	100593161	102346326
39	976555436	99098728	985356708	101443292	100593164	102344564
40	976557197	99097821	985359376	101440624	100593167	102342803
41	976558957	99096915	985362042	101437955	100593170	102341043
42	976560715	99096007	985364710	101435292	100593173	102339285
43	976562473	99095099	985367377	101432626	100593176	102337527
44	976564230	99094190	985370043	101429961	100593179	102335771
45	976565985	99093281	985372711	101427295	100593182	102334015
46	976567739	99092371	985375378	101424632	100593185	102332261
47	976569492	99091461	985378045	101421969	100593188	102330508
48	976571244	99090550	985380711	101419306	100593191	102328756
49	976572995	99089639	985383377	101416643	100593194	102327004
50	976574746	99088727	985386043	101413981	100593197	102325254
51	976576497	99087815	985388708	101411320	100593200	102323506
52	976578247	99086903	985391374	101408659	100593203	102321758
53	976579998	99085991	985394040	101405998	100593206	102320011
54	976581735	99085079	985396705	101403339	100593209	102318265
55	976583480	99084167	985399371	101400679	100593212	102316520
56	976585223	99083254	985402036	101398020	100593215	102314777
57	976586966	99082341	985404701	101395362	100593218	102313034
58	976588707	99081428	985407366	101392704	100593221	102311293
59	976590448	99080514	985410031	101390046	100593224	102309553
60	976592187	99079599	985412696	101387390	100593227	102307813
L. Co-Sine. L. Sine. L. Co-Tang. L. Tangent. L. Co-Secant. L. Secant. M						

54 DEGREES.

## of the Chiefest Places of the World.

The Places Names.	North Latitude.	East Longitude.	The Places Names.	North Latitude.	East Longitude.
Burdeaux	45	10 35 E. 44	Hles of Boyon	42	22 02 00
St. Sebastian	43	40 04 19	Burlings	39	43 02 28
Bilboe	43	41 03 20	Rock of Lisbon	39	00 32 04
St. Andrea	43	43 02 36	Lisbone	39	08 01 06
Lyons	43	49 02 06	Cape St. Vincent	37	03 01 18
Cape Pines	44	04 00 52	Cape St. Maria	36	52 00 12 24
Cape Ortegal	44	08 00 06	Cales, or Cadiz	36	52 01 24
Sazarga	43	38 51 52			
Cape Corian	43	21 02 56			
Cape Finisterre	43	10 02 55			



## A TABLE of Natural and

36 DEGREES.

M	N. Sine.	N. Co-Sine.	N. Tangent.	N. Co-Tangent.	N. Secant.	N. Co-Secant.	
0	5877853	8290177	7254426	1375319	12360680	17013016	60
1	5880206	8288465	7263771	13755403	12363294	17006208	59
2	5882559	8286749	7273118	13757624	12365909	16999407	58
3	5884912	8285037	7282467	13759851	12368526	16992612	57
4	5887265	8283325	7291815	13762078	12371143	16985825	56
5	5889618	8281612	7301163	13764305	12373768	16979044	55
6	5891971	8279900	7310511	13766532	12376393	16972271	54
7	5894324	8278188	7319859	13768759	12379019	16965504	53
8	5896677	8276476	7329207	13770986	12381647	16958732	52
9	5899030	8274764	7338555	13773213	12384275	16951960	51
10	5901383	8273052	7347903	13775440	12386901	16945188	50
11	5903736	8271340	7357251	13777667	12389527	16938416	49
12	5906089	8269628	7366599	13779894	12392153	16931644	48
13	5908442	8267916	7375947	13782121	12394780	16924872	47
14	5910795	8266204	7385295	13784348	12397406	16918100	46
15	5913148	8264492	7394643	13786575	12400033	16911328	45
16	5915501	8262780	7403991	13788802	12402659	16904556	44
17	5917854	8261068	7413339	13791029	12405286	16897784	43
18	5920207	8259356	7422687	13793256	12407912	16891012	42
19	5922560	8257644	7432035	13795483	12410539	16884240	41
20	5924913	8255932	7441383	13797710	12413165	16877468	40
21	5927266	8254220	7450731	13799937	12415792	16870696	39
22	5929619	8252508	7460079	13802164	12418418	16863924	38
23	5931972	8250796	7469427	13804391	12421045	16857152	37
24	5934325	8249084	7478775	13806618	12423671	16850380	36
25	5936678	8247372	7488123	13808845	12426298	16843608	35
26	5939031	8245660	7497471	13811072	12428924	16836836	34
27	5941384	8243948	7506819	13813299	12431551	16830064	33
28	5943737	8242236	7516167	13815526	12434178	16823292	32
29	5946090	8240524	7525515	13817753	12436804	16816520	31
30	5948443	8238812	7534863	13819980	12439431	16809748	30

53 DEGREES.

## A Table of the Latitude and Longitude

From Giblitor to Cape Fiftiria.				The Places Names.			
The Places Names.		North Latitud.	East Longit.	North Latitud		East Longit.	
		D.	M.	D.	M.	D.	M.
Giblitor, or Gibraltar		36	40 02	06		Cape Pallomallo	49 10 08 39
Malaga		36	45 03	07		Cape de Creus	41 41 11 18
Cattle Ferry		36	49 03	33		Marfilia	43 12 12 44
Cape de Gata		36	47 05	24		Tollon	43 00 14 04
Cape de Palos		37	28 07	11		Cape Larci	42 58 14 38
Allagant		38	20 07	14		Cape Melli	43 51 15 37
Cape Martin		38	46 08	20		Legorn	43 28 19 03
						Civita vecchia	41 46 20 24
						Rome	41 56 21 09
						Neapolis	41 08 22 51

## Artificial Sines, Tangents, and Secants.

36 DEGREES.

M	L. Sine.	L. Co-Sine.	L. Tangent.	L. Co-Tangent.	L. Secant.	L. Co-Secant.	
0	97692187	99079576	98612610	10137390	1000000000	1000000000	60
1	97693235	99078568	98614307	10137393	1000000000	1000000000	59
2	97694283	99077560	98615994	10137396	1000000000	1000000000	58
3	97695331	99076552	98617681	10137399	1000000000	1000000000	57
4	97696379	99075544	98619368	10137402	1000000000	1000000000	56
5	97697427	99074536	98621055	10137405	1000000000	1000000000	55
6	97698475	99073528	98622742	10137408	1000000000	1000000000	54
7	97699523	99072520	98624429	10137411	1000000000	1000000000	53
8	97700571	99071512	98626116	10137414	1000000000	1000000000	52
9	97701619	99070504	98627803	10137417	1000000000	1000000000	51
10	97702667	99069496	98629490	10137420	1000000000	1000000000	50
11	97703715	99068488	98631177	10137423	1000000000	1000000000	49
12	97704763	99067480	98632864	10137426	1000000000	1000000000	48
13	97705811	99066472	98634551	10137429	1000000000	1000000000	47
14	97706859	99065464	98636238	10137432	1000000000	1000000000	46
15	97707907	99064456	98637925	10137435	1000000000	1000000000	45
16	97708955	99063448	98639612	10137438	1000000000	1000000000	44
17	97710003	99062440	98641299	10137441	1000000000	1000000000	43
18	97711051	99061432	98642986	10137444	1000000000	1000000000	42
19	97712099	99060424	98644673	10137447	1000000000	1000000000	41
20	97713147	99059416	98646360	10137450	1000000000	1000000000	40
21	97714195	99058408	98648047	10137453	1000000000	1000000000	39
22	97715243	99057400	98649734	10137456	1000000000	1000000000	38
23	97716291	99056392	98651421	10137459	1000000000	1000000000	37
24	97717339	99055384	98653108	10137462	1000000000	1000000000	36
25	97718387	99054376	98654795	10137465	1000000000	1000000000	35
26	97719435	99053368	98656482	10137468	1000000000	1000000000	34
27	97720483	99052360	98658169	10137471	1000000000	1000000000	33
28	97721531	99051352	98659856	10137474	1000000000	1000000000	32
29	97722579	99050344	98661543	10137477	1000000000	1000000000	31
30	97723627	99049336	98663230	10137480	1000000000	1000000000	30

53 DEGREES.

## of the Chiefst Places of the World.

<i>The Places Names.</i>				<i>The Places Names.</i>					
<i>North Latitude.</i>		<i>East Longitude.</i>		<i>North Latitude.</i>		<i>East Longitude.</i>			
Sallarne	40	51	23	32	Venetia	45	37	22	45
Pollicastro	40	05	24	02	Cape Fiftiria	44	40	24	10
Cape Sparti-vento	37	46	24	16	<i>The Sea-coasts on the Main, from Tangeir to Joppa in the Straits.</i>				
Cape Columnne	38	56	25	40					
Gallipoli	40	08	27	04					
Cape St. Maffa	39	56	26	53					
Angollo	41	31	27	02					
Ancona	43	25	24	29	Wadalio in the Straits	34	57	03	13
Giavocha	44	19	21	26	Ballis	34	57	03	48
Gorro	44	57	21	35	Oran	35	46	07	50
					Tenes	36	30	09	18



## A TABLE of Natural and

36 DEGREES.

M	N. Sine.	N. Co-Sine.	V. Tangent.	V. Co-Tang.	N. Secant.	N. Co-Secant.	M
30	5948225	8038569	7395911	13514224	12440026	16511730	30
31	5950566	8035638	7404114	13566005	12442705	16505124	29
32	5952903	8032517	7412618	13617794	12445386	16498235	28
33	5955240	8029337	7421324	13675899	12448069	16491333	27
34	5957577	8026112	7430233	13731900	12450754	16484347	26
35	5959913	8022999	7439244	13787917	12453442	16477268	25
36	5962242	8020175	7448365	13845011	12456131	16470195	24
37	5964581	8017144	7457596	13903132	12458823	16463129	23
38	5966919	8014205	7466947	13962395	12461518	16456070	22
39	5969253	8011269	7476424	14022812	12464214	16449021	21
40	5971586	8008332	7486024	14084393	12466913	16441970	20
41	5973919	8005494	7495746	14147137	12469614	16434930	19
42	5976251	8002759	7505589	14211042	12472317	16427897	18
43	5978583	8000117	7515352	14276107	12475022	16420870	17
44	5980913	8001427	7525234	14342337	12477730	16413850	16
45	5983246	8001858	7535234	14409844	12480440	16406836	15
46	5985579	8002397	7545352	14478628	12483152	16399828	14
47	5987906	8002956	7555586	14548690	12485866	16392823	13
48	5990236	8003534	7565936	14620026	12488583	16385823	12
49	5992565	8004131	7576404	14692547	12491302	16378835	11
50	5994893	8004747	7587000	14766353	12494023	16371854	10
51	5997221	8005382	7597724	14841454	12496746	16364879	9
52	5999549	8006035	7608576	14917951	12499471	16357920	8
53	6001876	8006706	7619556	15000000	12502199	16350986	7
54	6004202	8007394	7630664	15082612	12504929	16344062	6
55	6006529	8008100	7641896	15166784	12507661	16337146	5
56	6008853	8008823	7653252	15252516	12510396	16330239	4
57	6011178	8009564	7664732	15339917	12513133	16323341	3
58	6013501	8010323	7676336	15428988	12515873	16316451	2
59	6015827	8011100	7688064	15519729	12518616	16309569	1
60	6018150	8011895	7699916	15612140	12521362	16302695	0

N. Co-Sine.

N. Sine.

N. Co-Tang.

N. Tangent.

N. Co-Secant.

N. Secant.

M

53 DEGREES.

## A Table of the Latitude and Longitude

The Places Names.	North Latitude	East Longitude	The Places Names.	North Latitude	East Longitude
Serfally	D. M. D. M.		Tunis.	D. M. D. M.	
Argier	36 40 09 48		Cape Beun	37 05 17 24	
Tadallis	36 48 11 25		Suffa	37 02 18 07	
Ragin	36 50 11 44		Britto	35 23 18 41	
Gion	36 50 13 30		Cherunne	34 56 18 36	
Gigary	37 03 14 26		Cape Mizarata	32 18 24 00	
Cholla	37 08 15 14		Cape de Solona	31 01 25 49	
Stora	37 09 15 44		Cape Ruffutta	32 58 29 26	
Cape Bone	37 19 16 44		Cape Roattini	32 18 32 04	
Bozarar	37 30 17 50		Alexandria	30 40 41 28	

## Artificial Sines, Tangents, and Secants:

30 DEGREES.

M	L. Sine.	L. Co-Sine.	L. Tangent.	L. Co-Tang.	L. Secant.	L. Co-Secant.	M
30	9.774876	9.9251795	9.5692089	10.1307911	10.0942113	10.2351121	30
31	9.7745583	9.9255012	9.5694731	10.1305269	10.0942143	10.2351121	29
32	9.7742388	9.9258216	9.5697372	10.1302628	10.0942173	10.2351121	28
33	9.7739193	9.9261419	9.5700013	10.1299987	10.0942203	10.2351121	27
34	9.7735997	9.9264621	9.5702654	10.1297347	10.0942233	10.2351121	26
35	9.7732802	9.9267824	9.5705295	10.1294707	10.0942263	10.2351121	25
36	9.7729607	9.9271026	9.5707936	10.1292067	10.0942293	10.2351121	24
37	9.7726412	9.9274229	9.5710577	10.1289427	10.0942323	10.2351121	23
38	9.7723217	9.9277431	9.5713218	10.1286787	10.0942353	10.2351121	22
39	9.7720022	9.9280634	9.5715859	10.1284147	10.0942383	10.2351121	21
40	9.7716827	9.9283836	9.5718500	10.1281507	10.0942413	10.2351121	20
41	9.7713632	9.9287039	9.5721141	10.1278867	10.0942443	10.2351121	19
42	9.7710437	9.9290241	9.5723782	10.1276227	10.0942473	10.2351121	18
43	9.7707242	9.9293444	9.5726423	10.1273587	10.0942503	10.2351121	17
44	9.7704047	9.9296646	9.5729064	10.1270947	10.0942533	10.2351121	16
45	9.7700852	9.9299849	9.5731705	10.1268307	10.0942563	10.2351121	15
46	9.7697657	9.9303051	9.5734346	10.1265667	10.0942593	10.2351121	14
47	9.7694462	9.9306254	9.5736987	10.1263027	10.0942623	10.2351121	13
48	9.7691267	9.9309456	9.5739628	10.1260387	10.0942653	10.2351121	12
49	9.7688072	9.9312659	9.5742269	10.1257747	10.0942683	10.2351121	11
50	9.7684877	9.9315861	9.5744910	10.1255107	10.0942713	10.2351121	10
51	9.7681682	9.9319064	9.5747551	10.1252467	10.0942743	10.2351121	9
52	9.7678487	9.9322266	9.5750192	10.1249827	10.0942773	10.2351121	8
53	9.7675292	9.9325469	9.5752833	10.1247187	10.0942803	10.2351121	7
54	9.7672097	9.9328671	9.5755474	10.1244547	10.0942833	10.2351121	6
55	9.7668902	9.9331874	9.5758115	10.1241907	10.0942863	10.2351121	5
56	9.7665707	9.9335076	9.5760756	10.1239267	10.0942893	10.2351121	4
57	9.7662512	9.9338279	9.5763397	10.1236627	10.0942923	10.2351121	3
58	9.7659317	9.9341481	9.5766038	10.1233987	10.0942953	10.2351121	2
59	9.7656122	9.9344684	9.5768679	10.1231347	10.0942983	10.2351121	1
60	9.7652927	9.9347886	9.5771320	10.1228707	10.0943013	10.2351121	0

L. Co-Sine.

L. Sine.

L. Co-Tang.

L. Tangent.

L. Co-Secant.

L. Secant.

M

53 DEGREES.

## of the Chief Places of the World.

The Places Names.	North Latitude	East Longitude	The Places Names.	North Latitude	East Longitude
Michallat	D. M. D. M.		Cape Decexman	D. M. D. M.	
Cairo	30 30 41 55		Cape Babarnau	36 16 36 44	
Joppa	30 35 41 44		Land Miri	37 58 36 22	
	31 42 43 39		Incommodio	39 12 37 05	
The Coast from Antiochia to Sagua			Constantinople	40 26 40 39	
in the Straits.			Gallipolo	40 56 40 33	
Cape Antiochia to Sagua	34 54 46 26		Cape Degriffa	40 20 37 59	
Cape Polloppia	35 35 44 01		Cape Pimra	40 12 37 11	
Cape Seridion	35 55 41 24		Cape St. George	40 26 32 23	
			Cape Collo	39 28 32 10	
				37 40 32 35	



## A TABLE of Natural and

37 DEGREES.

M	N. Sine.	V. Co-Sine.	N. Tangent.	N. Co-Tang.	N. Secant.	N. Co-Secant.	
0	6318150	7986355	7533540	13270448	12521357	16616401	60
1	6320473	7984674	7540102	13262420	12524102	16609990	59
2	6322755	7982952	7546666	13254397	12526850	16603585	58
3	6325117	7981100	7553232	13246391	12529601	16597157	57
4	6327439	7979247	7559799	13238391	12532352	16590795	56
5	6329753	7977353	7566369	13230388	12535108	16584429	55
6	6332080	7975454	7572941	13222372	12537865	16578032	54
7	6334400	7973544	7579514	13214353	12540625	16571657	53
8	6336719	7971623	7586082	13206330	12543387	16565293	52
9	6339038	7969702	7592651	13198304	12546151	16558929	51
10	6341356	7967781	7599221	13190274	12548917	16552575	50
11	6343674	7965859	7605792	13182241	12551685	16546227	49
12	6345991	7963939	7612363	13174213	12554456	16539885	48
13	6348308	7962019	7618934	13166182	12557229	16533550	47
14	6350624	7960100	7625505	13158149	12560005	16527221	46
15	6352940	7958180	7632076	13150113	12562782	16520898	45
16	6355255	7956259	7638647	13142074	12565562	16514581	44
17	6357570	7954339	7645218	13134031	12568345	16508270	43
18	6359884	7952419	7651789	13125986	12571129	16501966	42
19	6362198	7950499	7658360	13117948	12573916	16495668	41
20	6364511	7948579	7664931	13109907	12576705	16489375	40
21	6366823	7946659	7671502	13101863	12579497	16483090	39
22	6369135	7944739	7678073	13093819	12582291	16476811	38
23	6371447	7942819	7684644	13085774	12585087	16470537	37
24	6373758	7940899	7691215	13077729	12587885	16464270	36
25	6376069	7938979	7697786	13069684	12590686	16458009	35
26	6378379	7937059	7704357	13061639	12593489	16451754	34
27	6380689	7935139	7710928	13053594	12596294	16445506	33
28	6382998	7933219	7717499	13045549	12599102	16439263	32
29	6385306	7931299	7724070	13037504	12601912	16433027	31
30	6387614	7929379	7730641	13029459	12604724	16426796	30
	V. Co-Sine	N. Sine.	N. Co-Tang.	N. Tangent.	V. Co-Secant.	N. Secant.	M

52 DEGREES.

## A Table of the Latitude and Longitude

The Places Names.	North Latitude.	East Longitude.	The Places Names.	North Latitude.	East Longitude.
Cape Sille	D. 37	M. 15	Trovor	D. 43	M. 27
Cape Matapan	36	28	Cape Gafta	43	30
Castellornis	37	45	Salonico	44	01
Drugromaftra	38	38	Zaro	44	05
Cape Linga	40	18	Sagua	44	47
Hiraffa	40	57			
Antavara	41	49	<i>Islands in the Straits, called the Archipelago.</i>		
Cattaro	42	21	Sarfanto	36	57
Ragusa	42	29	Sarfo	37	17
Stanio	42	57			

## Artificial Sines, Tangents, and Secants.

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37 DEGREES.

M	L. Sine.	L. Co-Sine.	L. Tangent.	L. Co-Tang.	L. Secant.	L. Co-Secant.	
0	9.7794630	9.9223456	9.5771144	10.4228856	10.0997614	10.2205370	60
1	9.7796306	9.9222534	9.5773772	10.4226228	10.0997746	10.2203694	59
2	9.7797981	9.9221611	9.5776400	10.4223600	10.0997878	10.2202019	58
3	9.7799655	9.9220688	9.5779027	10.4220973	10.0998010	10.2200345	57
4	9.7801328	9.9219764	9.5781654	10.4218346	10.0998142	10.2198672	56
5	9.7803000	9.9218841	9.5784281	10.4215719	10.0998274	10.2197000	55
6	9.7804671	9.9217917	9.5786907	10.4213093	10.0998406	10.2195329	54
7	9.7806341	9.9216993	9.5789534	10.4210467	10.0998538	10.2193657	53
8	9.7808010	9.9216069	9.5792161	10.4207842	10.0998670	10.2191990	52
9	9.7809677	9.9215145	9.5794788	10.4205215	10.0998802	10.2190323	51
10	9.7811344	9.9214221	9.5797415	10.4202589	10.0998934	10.2188656	50
11	9.7813010	9.9213297	9.5800041	10.4200000	10.0999066	10.2186990	49
12	9.7814675	9.9212373	9.5802667	10.4197416	10.0999198	10.2185325	48
13	9.7816339	9.9211449	9.5805292	10.4194833	10.0999330	10.2183661	47
14	9.7818002	9.9210521	9.5807917	10.4192250	10.0999462	10.2181998	46
15	9.7819664	9.9209594	9.5810542	10.4189667	10.0999594	10.2180335	45
16	9.7821324	9.9208667	9.5813167	10.4187084	10.0999726	10.2178672	44
17	9.7822984	9.9207740	9.5815792	10.4184501	10.0999858	10.2177009	43
18	9.7824644	9.9206813	9.5818417	10.4181918	10.0999990	10.2175347	42
19	9.7826301	9.9205886	9.5821042	10.4179335	10.0999999	10.2173685	41
20	9.7827958	9.9204959	9.5823667	10.4176752	10.0999999	10.2172023	40
21	9.7829614	9.9204032	9.5826292	10.4174169	10.0999999	10.2170361	39
22	9.7831268	9.9203105	9.5828917	10.4171586	10.0999999	10.2168699	38
23	9.7832922	9.9202178	9.5831542	10.4169003	10.0999999	10.2167037	37
24	9.7834575	9.9201251	9.5834167	10.4166420	10.0999999	10.2165375	36
25	9.7836227	9.9200324	9.5836792	10.4163837	10.0999999	10.2163713	35
26	9.7837879	9.9199397	9.5839417	10.4161254	10.0999999	10.2162051	34
27	9.7839532	9.9198470	9.5842042	10.4158671	10.0999999	10.2160389	33
28	9.7841177	9.9197543	9.5844667	10.4156088	10.0999999	10.2158727	32
29	9.7842824	9.9196616	9.5847292	10.4153505	10.0999999	10.2157065	31
30	9.7844471	9.9195689	9.5849917	10.4150922	10.0999999	10.2155403	30
	L. Co-Sine.	L. Sine.	L. Co-Tang.	L. Tangent.	L. Co-Secant.	L. Secant.	M

52 DEGREES.

## of the Chiefest Places of the World.

The Places Names.	North Latitude.	East Longitude.	The Places Names.	North Latitude.	East Longitude.
Famania	D. 37	M. 28	Stavifratra	D. 39	M. 28
Trava	37	49	Lamnois	39	41
Pipor	39	32	Embrosi	40	06
Laffor	39	58	Palamos	40	14
Lamo	39	44	Toffa	40	03
Stripo	39	16			
Sr. Penaga	38	52	<i>Islands in the Straits.</i>		
Andrea	38	12	Sapientia	36	47
Iplava	38	28	Stouty	37	10
Mortalin	39	54			



## A TABLE of Natural and

37 DEGREES.

M	N. Sine.	N. Co-Sine.	N. Tangent.	N. Co-Tang.	N. Secant.	N. Co-Secant.	M
30	6687614	7933533	7573270	13022254	12624724	16126796	30
31	6689922	7931752	7677893	13044407	12627539	16120572	29
32	6692250	7929970	7782517	13066560	12630356	16114354	28
33	6694583	7928210	7887144	13088712	12633175	16108142	27
34	6696841	7926445	7991773	13110865	12635997	16101936	26
35	6699147	7924671	8096404	12933081	12638820	16095736	25
36	6701452	7922895	8201037	12955265	12641646	16089542	24
37	6703756	7921121	8305672	12977454	12644475	16083355	23
38	6706060	7919345	8410309	12999649	12647306	16077173	22
39	6708365	7917569	8514943	12991850	12650140	16070997	21
40	6710668	7915792	8619579	12994057	12652975	16064828	20
41	6712970	7914014	8724213	12996263	12655813	16058664	19
42	6715270	7912235	8828848	12998469	12658653	16052507	18
43	6717572	7910456	8933483	12999712	12661496	16046355	17
44	6719873	7908676	9038117	12999931	12664341	16040210	16
45	6722173	7906896	9142752	12999917	12667188	16034070	15
46	6724473	7905115	9247387	12999741	12670038	16027937	14
47	6726772	7903333	9352022	12999462	12672890	16021809	13
48	6729071	7901550	9456657	12999029	12675745	16015683	12
49	6731369	7899767	9561292	12998485	12678601	16009562	11
50	6733666	7897983	9665927	12997841	12681469	16003456	10
51	6735963	7896198	9770562	12997197	12684322	16007359	9
52	6738260	7894413	9875197	12996553	12687186	16001269	8
53	6740556	7892628	9979832	12995909	12690052	16005181	7
54	6742852	7890841	10044468	12995265	12692921	16009093	6
55	6745147	7889054	10109603	12994621	12695792	16013003	5
56	6747442	7887266	10174738	12993977	12698665	16016920	4
57	6749737	7885477	10239873	12993333	12701541	16020836	3
58	6752032	7883688	10305008	12992689	12704419	16024759	2
59	6754327	7881898	10370143	12992045	12707299	16028684	1
60	6756621	7880107	10435278	12991401	12710182	16032609	0
N. Co-Sine.		N. Sine.	N. Co-Tang.	N. Tangent.	N. Co-Secant.	N. Secant.	M

52 DEGREES.

## A Table of the Latitude and Longitude

The Places Names.	North Latitude.	East Longit.	The Places Names.	North Latitude.	East Longit.
Zant	37 37 29	38	Corfella	42 35 27	38
Cape Sidro	38 15 29	33	Augusta	42 36 27	13
Paxa	38 49 29	30	Catfilla	42 40 27	03
Corfu	39 26 29	26	Catfio	42 44 26	58
Faimo	39 44 29	19	Lifla	43 00 26	33
Seflino	40 22 29	14	Buzo	43 02 26	18
Pianaffa	41 52 26	08	St. Andrea	43 07 25	58
Trinite	41 50 25	53	Poma	43 14 25	48
Pollagaffa	42 17 26	37	Ilford Groffo	44 00 25	36
Mallida	42 37 28	03	Sauflaga	44 20 25	02

## Artificial Sines, Tangents, and Secants.

37 DEGREES.

M	L. Sine.	L. Co-Sine.	L. Tangent.	L. Co-Tang.	L. Secant.	L. Co-Secant.	M
30	9.844471	9.8924667	9.8549305	10.1150195	10.1005333	10.2155529	30
31	9.846117	9.8933697	9.8552420	10.1147580	10.1006303	10.2153883	29
32	9.847766	9.8942727	9.8555035	10.1144965	10.1007273	10.2152238	28
33	9.849410	9.8951756	9.8557650	10.1142350	10.1008244	10.2150594	27
34	9.851049	9.8960784	9.8560265	10.1139735	10.1009216	10.2148951	26
35	9.852691	9.8969812	9.8562879	10.1137122	10.1010188	10.2147309	25
36	9.854332	9.8978840	9.8565492	10.1134508	10.1011160	10.2145668	24
37	9.855972	9.8987867	9.8568105	10.1131895	10.1012133	10.2144028	23
38	9.857611	9.8996893	9.8570718	10.1129282	10.1013107	10.2142389	22
39	9.859250	9.8995919	9.8573330	10.1126670	10.1014081	10.2140751	21
40	9.860889	9.8994944	9.8575942	10.1124058	10.1015056	10.2139114	20
41	9.862528	9.8993968	9.8578554	10.1121446	10.1016032	10.2137478	19
42	9.864167	9.8992992	9.8581166	10.1118835	10.1017008	10.2135843	18
43	9.865806	9.8992015	9.8583777	10.1116223	10.1017985	10.2134209	17
44	9.867444	9.8991038	9.8586386	10.1113611	10.1018962	10.2132576	16
45	9.869083	9.8990060	9.8588996	10.1111000	10.1019940	10.2130944	15
46	9.870721	9.8989082	9.8591605	10.1108388	10.1020918	10.2129313	14
47	9.872360	9.8988103	9.8594214	10.1105776	10.1021897	10.2127683	13
48	9.873998	9.8987123	9.8596823	10.1103164	10.1022877	10.2126054	12
49	9.875637	9.8986143	9.8599432	10.1100552	10.1023857	10.2124426	11
50	9.877275	9.8985162	9.8602040	10.1097940	10.1024838	10.2122798	10
51	9.878914	9.8984181	9.8604647	10.1095528	10.1025819	10.2121172	9
52	9.880553	9.8983199	9.8607254	10.1093116	10.1026801	10.2119547	8
53	9.882192	9.8982216	9.8609861	10.1090704	10.1027784	10.2117923	7
54	9.883831	9.8981233	9.8612468	10.1088292	10.1028767	10.2116299	6
55	9.885470	9.8980249	9.8615074	10.1085880	10.1029751	10.2114677	5
56	9.887109	9.8979265	9.8617679	10.1083468	10.1030733	10.2113056	4
57	9.888748	9.8978282	9.8620284	10.1081056	10.1031717	10.2111435	3
58	9.890387	9.8977298	9.8622889	10.1078644	10.1032701	10.2109816	2
59	9.892026	9.8976315	9.8625494	10.1076232	10.1033685	10.2108198	1
60	9.893665	9.8975331	9.8628099	10.1073820	10.1034670	10.2106580	0
L. Co-Sine.		L. Sine.	L. Co-Tang.	L. Tangent.	L. Co-Secant.	L. Secant.	M

52 DEGREES.

## of the Chiefest Places of the World.

The Places Names.	North Latitude.	East Longit.	The Places Names.	North Latitude.	East Longit.
Piper	35 52 22	15	Middle of Candia	35 08 33	56
Malta	36 00 21	54	West end of Candia	35 15 32	25
Comino	36 15 21	24	Scarpanta	45 10 36	04
East end of Cyprus	34 48 44	18	Caros	35 35 35	39
Middle of Cyprus	34 18 43	09	Langa	36 33 36	02
West end of Cyprus	34 22 41	47	Stampalia	36 11 34	59
Rhodes	35 40 37	22	Levatta	36 38 34	54
Sivia	36 05 37	17	Niza	37 02 34	31
Gozo	34 37 32	35	Cavari	36 40 32	16
East end of Candia	35 04 35	32	Palla	36 52 32	09



## A TABLE of Natural and

38 DEGREES.

M	N. Sine.	N. Co-sine.	N. Tang.	N. Co-Tang.	N. Secant.	N. Co-Secant.	
0	6156615	7880127	7812855	12792410	12550182	16242692	60
1	6158907	7873316	7817542	12791715	12633207	16235643	59
2	6161198	7865924	7822229	12791015	12725345	16228595	58
3	6163489	7858532	7826916	12790315	12817577	16221546	57
4	6165779	7851141	7831611	12789615	12909809	16214497	56
5	6168069	7843750	7836295	12788915	13002041	16207448	55
6	6170359	7836359	7841002	12788215	13094273	16200399	54
7	6172648	7828968	7845709	12787515	13186505	16193350	53
8	6174936	7821577	7850420	12786815	13278737	16186301	52
9	6177224	7814186	7855131	12786115	13370969	16179252	51
10	6179511	7806795	7859842	12785415	13463201	16172203	50
11	6181798	7799404	7864553	12784715	13555433	16165154	49
12	6184084	7792013	7869264	12784015	13647665	16158105	48
13	6186370	7784622	7873975	12783315	13739897	16151056	47
14	6188655	7777231	7878686	12782615	13832129	16144007	46
15	6190940	7769840	7883397	12781915	13924361	16136958	45
16	6193224	7762449	7888108	12781215	14016593	16129909	44
17	6195507	7755058	7892819	12780515	14108825	16122860	43
18	6197792	7747667	7897530	12779815	14201057	16115811	42
19	6200077	7740276	7902241	12779115	14293289	16108762	41
20	6202355	7732885	7906952	12778415	14385521	16101713	40
21	6204636	7725494	7911663	12777715	14477753	16094664	39
22	6206917	7718103	7916374	12777015	14569985	16087615	38
23	6209198	7710712	7921085	12776315	14662217	16080566	37
24	6211478	7703321	7925796	12775615	14754449	16073517	36
25	6213757	7695930	7930507	12774915	14846681	16066468	35
26	6216036	7688539	7935218	12774215	14938913	16059419	34
27	6218314	7681148	7939929	12773515	15031145	16052370	33
28	6220592	7673757	7944640	12772815	15123377	16045321	32
29	6222869	7666366	7949351	12772115	15215609	16038272	31
30	6225145	7658975	7954062	12771415	15307841	16031223	30

51 DEGREES.

## A Table of the Latitude and Longitude

The Places Names.	North Latitud.	East Longit.	The Places Names.	North Latitud.	East Longit.
Cardinals Hats	D. M. D. M.		Messina	D. M. D. M.	
Forleonari	37 25 32 31		East end of Sicilia	38 07 23 21	
Millo	36 50 32 37		Middle of Sicilia	37 07 23 24	
Goza	36 40 33 19		West end of Sicilia	37 42 22 09	
Samatto	35 41 20 51		Alficia	37 52 20 07	
Lampadoffa	35 46 19 39		Allieur	38 56 20 58	
Linosia	35 58 19 55		Fallieur	38 43 21 47	
Pantalaria	36 20 20 05		Lifallin	38 43 22 01	
Kambo	36 53 19 35		Lipari	38 34 22 32	
Maritimo	37 10 18 34		Volcana	38 42 22 27	
	37 52 20 02			38 42 22 30	

## Artificial Sines, Tangents, and Secants.

38 DEGREES.

M	L. Sine.	L. Co-Sine.	L. Tangent.	L. Co-Tang.	L. Secant.	L. Co-Secant.	
0	97993420	98965321	98928099	101071902	101034579	102106585	60
1	97993420	98965321	98928099	101071902	101034579	102106585	59
2	97993420	98965321	98928099	101071902	101034579	102106585	58
3	97993420	98965321	98928099	101071902	101034579	102106585	57
4	97993420	98965321	98928099	101071902	101034579	102106585	56
5	97993420	98965321	98928099	101071902	101034579	102106585	55
6	97993420	98965321	98928099	101071902	101034579	102106585	54
7	97993420	98965321	98928099	101071902	101034579	102106585	53
8	97993420	98965321	98928099	101071902	101034579	102106585	52
9	97993420	98965321	98928099	101071902	101034579	102106585	51
10	97993420	98965321	98928099	101071902	101034579	102106585	50
11	97993420	98965321	98928099	101071902	101034579	102106585	49
12	97993420	98965321	98928099	101071902	101034579	102106585	48
13	97993420	98965321	98928099	101071902	101034579	102106585	47
14	97993420	98965321	98928099	101071902	101034579	102106585	46
15	97993420	98965321	98928099	101071902	101034579	102106585	45
16	97993420	98965321	98928099	101071902	101034579	102106585	44
17	97993420	98965321	98928099	101071902	101034579	102106585	43
18	97993420	98965321	98928099	101071902	101034579	102106585	42
19	97993420	98965321	98928099	101071902	101034579	102106585	41
20	97993420	98965321	98928099	101071902	101034579	102106585	40
21	97993420	98965321	98928099	101071902	101034579	102106585	39
22	97993420	98965321	98928099	101071902	101034579	102106585	38
23	97993420	98965321	98928099	101071902	101034579	102106585	37
24	97993420	98965321	98928099	101071902	101034579	102106585	36
25	97993420	98965321	98928099	101071902	101034579	102106585	35
26	97993420	98965321	98928099	101071902	101034579	102106585	34
27	97993420	98965321	98928099	101071902	101034579	102106585	33
28	97993420	98965321	98928099	101071902	101034579	102106585	32
29	97993420	98965321	98928099	101071902	101034579	102106585	31
30	97993420	98965321	98928099	101071902	101034579	102106585	30

51 DEGREES.

## of the Chiefest Places of the World.

The Places Names.	North Latitud.	East Longit.	The Places Names.	North Latitud.	East Longit.
Stromballa	D. M. D. M.		Caprera	D. M. D. M.	
Foldemaffina	39 03 23 02		Gargona	42 48 21	
Iscia	38 20 23 29		North end of Corfica	43 20 18 28	
Ponuffa	40 46 21 30		Middle of Corfica	42 55 17 06	
Palmaroffa	40 40 20 32		South end of Corfica	42 05 17 27	
Ginnute	40 50 19 59		Taloro	41 20 17 01	
Gigio	41 59 19 48		Azanera	40 56 17 19	
Crista	41 55 18 31		North end of Sardinia	41 08 16 22	
Planoffa	42 07 18 33		Middle of Sardinia	41 14 17 25	
Lilbo	42 31 18 36		South end of Sardinia	40 06 16 54	
				38 56 16 37	



## 38 DEGREES.

M	N. Sine.	N. Co-Sine.	N. Tangent.	N. Co-Tang.	N. Secant.	N. Co-Secant.	
30	6225146	7826082	7954359	12571723	12777787	16065879	30
31	6227422	7824271	7959110	12564219	12780745	16058008	29
32	6229693	7822459	7963862	12556721	12783705	16052142	28
33	6231973	7820646	7968617	12549229	12786667	16046281	27
34	6234248	7818833	7973374	12541742	12789632	16040426	26
35	6236522	7817019	7978134	12534260	12792600	16034577	25
36	6238796	7815205	7982895	12526784	12795570	16028734	24
37	6241069	7813390	7987659	12519313	12798543	16022896	23
38	6243342	7811574	7992425	12511843	12801518	16017054	22
39	6245614	7809757	7997193	12504388	12804495	16011237	21
40	6247885	7807940	8001963	12496933	12807475	16005416	20
41	6250156	7806122	8006736	12489484	12810457	15999600	19
42	6252426	7804304	8011511	12482040	12813442	15993790	18
43	6254696	7802485	8016288	12474602	12816430	15987986	17
44	6256966	7800666	8021067	12467169	12819420	15982187	16
45	6259235	7798845	8025848	12459742	12822412	15976394	15
46	6261503	7797024	8030632	12452320	12825407	15970606	14
47	6263771	7795202	8035418	12444903	12828404	15964824	13
48	6266038	7793380	8040205	12437492	12831404	15959047	12
49	6268305	7791557	8044997	12430086	12834406	15953276	11
50	6270571	7789733	8049790	12422685	12837411	15947511	10
51	6272837	7787908	8054585	12415290	12840418	15941751	9
52	6275102	7786083	8059382	12407900	12843428	15936000	8
53	6277366	7784257	8064181	12400515	12846440	15930247	7
54	6279630	7782431	8068983	12393136	12849455	15924504	6
55	6281894	7780604	8073787	12385762	12852472	15918766	5
56	6284157	7778777	8078593	12378393	12855492	15913033	4
57	6286420	7776949	8083401	12371030	12858514	15907306	3
58	6288683	7775120	8088212	12363672	12861539	15901584	2
59	6290943	7773290	8093025	12356319	12864566	15895868	1
60	6293204	7771460	8097840	12348972	12867596	15890157	0
N. Co-Sine		N. Sine.	N. Co-Tang.	N. Tangent.	N. Co-Secant.	N. Secant.	M

## 51 DEGREES.

## A Table of the Latitude and Longitude

The Places Names.	North Latitud.	East Longit.		The Canary Islands.	North Latitud.	East Longit.
The Island of St. Pedra	39	20 16 03	D. M. D. M.			
Palmade follo	39	11 16 05				
Sarpentara	39	00 17 18				
Callatta	37	57 16 28		Forta Ventura	28	12 06 28
Minorca	39	55 12 16		Lancelotte	28	51 06 08
Majorca	39	38 11 12		Allegranfia	29	11 06 13
Cabrea	39	07 11 05		Grand Canary	27	43 03 31
Collombratta	39	50 08 44		Teneriff	28	20 09 28
Evilla	39	05 09 57		Gomero	28	09 10 15
Formentara	38	44 09 54		Ferro	28	05 10 42

## Artificial Sines, Tangents, and Secants.

## 38 DEGREES.

M	L. Sine.	L. Co-Sine.	L. Tangent.	L. Co-Tang.	L. Secant.	L. Co-Secant.	
30	9.7941496	9.8935444	9.9006352	10.0991948	10.1064556	10.2053504	30
31	9.7943083	9.8934439	9.9008645	10.0991355	10.1065561	10.2056917	29
32	9.7944670	9.8933433	9.9011237	10.0990763	10.1066567	10.2055330	28
33	9.7946256	9.8932426	9.9013830	10.0990170	10.1067574	10.2053744	27
34	9.7947841	9.8931419	9.9016422	10.0989578	10.1068581	10.2052159	26
35	9.7949425	9.8930412	9.9019013	10.0988985	10.1069588	10.2050575	25
36	9.7951008	9.8929404	9.9021604	10.0988396	10.1070596	10.2048992	24
37	9.7952590	9.8928395	9.9024195	10.0987805	10.1071605	10.2047410	23
38	9.7954171	9.8927385	9.9026786	10.0987214	10.1072615	10.2045829	22
39	9.7955751	9.8926375	9.9029376	10.0986624	10.1073625	10.2044249	21
40	9.7957330	9.8925365	9.9031965	10.0986034	10.1074635	10.2042670	20
41	9.7958909	9.8924354	9.9034555	10.0985445	10.1075646	10.2041091	19
42	9.7960486	9.8923342	9.9037144	10.0984856	10.1076656	10.2039514	18
43	9.7962062	9.8922332	9.9039733	10.0984267	10.1077667	10.2037938	17
44	9.7963638	9.8921316	9.9042321	10.0983679	10.1078678	10.2036362	16
45	9.7965212	9.8920303	9.9044910	10.0983090	10.1079689	10.2034788	15
46	9.7966786	9.8919289	9.9047497	10.0982505	10.1080701	10.2033214	14
47	9.7968359	9.8918274	9.9050085	10.0981915	10.1081712	10.2031641	13
48	9.7969932	9.8917258	9.9052672	10.0981328	10.1082724	10.2030070	12
49	9.7971501	9.8916242	9.9055259	10.0980741	10.1083735	10.2028499	11
50	9.7973071	9.8915226	9.9057845	10.0980155	10.1084747	10.2026929	10
51	9.7974640	9.8914208	9.9060431	10.0979568	10.1085759	10.2025360	9
52	9.7976208	9.8913191	9.9063017	10.0978983	10.1086772	10.2023792	8
53	9.7977775	9.8912172	9.9065603	10.0978397	10.1087784	10.2022225	7
54	9.7979341	9.8911153	9.9068188	10.0977812	10.1088797	10.2020659	6
55	9.7980906	9.8910133	9.9070773	10.0977227	10.1089809	10.2019094	5
56	9.7982470	9.8909113	9.9073357	10.0976643	10.1090822	10.2017530	4
57	9.7984034	9.8908092	9.9075941	10.0976059	10.1091835	10.2015966	3
58	9.7985596	9.8907071	9.9078525	10.0975475	10.1092848	10.2014404	2
59	9.7987158	9.8906050	9.9081109	10.0974891	10.1093861	10.2012842	1
60	9.7988718	9.8905026	9.9083692	10.0974308	10.1094874	10.2011282	0
L. Co-Sine.		L. Sine.	L. Co-Tang.	L. Tangent.	L. Co-Secant.	L. Secant.	M

## 51 DEGREES.

## of the Chiefest Places of the World.

The Places Names.	North Latitud.	East Longit.		The Places Names.	North Latitud.	East Longit.
Palma	28	58 10 42	D. M. D. M.	Corvo	40	09 24 59
Salvagias	30	05 08 57		Flauris	39	30 24 53
Dazarts	32	08 09 46		Fiall	38	49 22 15
Madera	32	27 11 19		Pico	38	30 21 37
Port-Santo	33	14 10 09		St. George	39	00 21 20
The Western Islands.				Tercera	39	31 20 22
Abrafo	37	55 29 46		Gratioffa	39	30 21 11
Vafo	40	30 27 28		Abrajo	39	52 18 53
				Vajo	38	43 18 23
				St. Michael	38	00 18 16



## 39 DEGREES.

M.	N. Sine.	N. Co-Sine.	V. Tangent.	N. Co-Tang.	N. Secant.	N. Co-Secant.
0	6293204	7771165	8297840	1234972	12867596	15890157
1	6295464	7766629	8102658	12341629	12870628	15884452
2	6297724	7762097	8107478	12334292	12873663	15878752
3	6299983	7757565	8112300	12326961	12876700	15873058
4	6302242	7753034	8117124	12319634	12879740	15867369
5	6304500	7748502	8121951	12312313	12882782	15861685
6	6306758	7743970	8126780	12304997	12885827	15856007
7	6309015	7739438	8131611	12297687	12888875	15850334
8	6311272	7734906	8136444	12290381	12891925	15844667
9	6313529	7730374	8141280	12283081	12894977	15839005
10	6315784	7725842	8146118	12275786	12898032	15833348
11	6318039	7721310	8150958	12268495	12901090	15827697
12	6320293	7716778	8155801	12261211	12904150	15822051
13	6322547	7712246	8160646	12253932	12907213	15816411
14	6324800	7707714	8165493	12246658	12910278	15810776
15	6327053	7703182	8170343	12239389	12913345	15805146
16	6329305	7698650	8175195	12232125	12916416	15799521
17	6331557	7694118	8180049	12224865	12919493	15793902
18	6333808	7689586	8184905	12217613	12922564	15788289
19	6336059	7685054	8189764	12210364	12925642	15782680
20	6338309	7680522	8194625	12203121	12928727	15777077
21	6340558	7675990	8199488	12195883	12931806	15771479
22	6342808	7671458	8204354	12188650	12934892	15765887
23	6345057	7666926	8209222	12181422	12937980	15760300
24	6347305	7662394	8214093	12174199	12941071	15754715
25	6349553	7657862	8218965	12166982	12944164	15749141
26	6351800	7653330	8223840	12159769	12947260	15743570
27	6354046	7648798	8228718	12152562	12950359	15738004
28	6356292	7644266	8233597	12145359	12953460	15732443
29	6358537	7639734	8238479	12138162	12956564	15726887
30	6360782	7635202	8243364	12130970	12959670	15721337
N. Co-Sine.		N. Sine.	N. Co-Tang.	N. Tangent.	N. Co-Secant.	N. Secant.

50 DEGREES.

## A Table of the Latitude and Longitude

The Places Names.	North Latitude.	East Longitude.	The Cape de Verd Islands.	North Latitude.	East Longitude.
Hozningo	D. M.	D. M.	Brava	D. M.	D. M.
St. Maria	37 25	17 36	Fogo	14 49	15 14
Vejp	42 22	18 56	St. Jago	14 42	14 56
Island Varda	44 48	22 46	Maya	15 00	4 02
Maiden Island	46 30	23 36	Bonavista	15 58	13 49
Old Brazil	51 03	29 56	Sid	17 00	13 26
			St. Nicholas	16 30	15 44
			St. Lucia	16 50	16 08

## 39 DEGREES.

M.	L. Sine.	L. Co-Sine.	L. Tangent.	L. Co-Tang.	L. Secant.	L. Co-Secant.
0	9.7988718	9.8905026	9.9083629	10.0916308	10.1094974	10.2011282
1	9.7990278	9.8904003	9.9086275	10.0913725	10.1095997	10.2009722
2	9.7991836	9.8902979	9.9088958	10.0911142	10.1097021	10.2008164
3	9.7993394	9.8901954	9.9091640	10.0908560	10.1098046	10.2006606
4	9.7994951	9.8900929	9.9094322	10.0905978	10.1099071	10.2005049
5	9.7996507	9.8899903	9.9096963	10.0903397	10.1100097	10.2003493
6	9.7998062	9.8898877	9.9099615	10.0900815	10.1101123	10.2001938
7	9.7999616	9.8897850	9.9102266	10.0898234	10.1102150	10.2000384
8	9.8001169	9.8896822	9.9104937	10.0895653	10.1103178	10.1998831
9	9.8002721	9.8895794	9.9107607	10.0893073	10.1104206	10.1997279
10	9.8004272	9.8894765	9.9110267	10.0890493	10.1105235	10.1995728
11	9.8005823	9.8893736	9.9112927	10.0887913	10.1106264	10.1994177
12	9.8007372	9.8892706	9.9115586	10.0885334	10.1107294	10.1992628
13	9.8008921	9.8891675	9.9118245	10.0882755	10.1108324	10.1991079
14	9.8010468	9.8890644	9.9120904	10.0880176	10.1109354	10.1989532
15	9.8012015	9.8889612	9.9123563	10.0877597	10.1110385	10.1987985
16	9.8013561	9.8888580	9.9126221	10.0875019	10.1111416	10.1986439
17	9.8015106	9.8887547	9.9128879	10.0872441	10.1112448	10.1984894
18	9.8016649	9.8886513	9.9131537	10.0869863	10.1113481	10.1983351
19	9.8018192	9.8885479	9.9134194	10.0867285	10.1114514	10.1981808
20	9.8019735	9.8884444	9.9136851	10.0864707	10.1115548	10.1980265
21	9.8021276	9.8883408	9.9139508	10.0862132	10.1116582	10.1978724
22	9.8022815	9.8882372	9.9142164	10.0859556	10.1117617	10.1977184
23	9.8024356	9.8881335	9.9144820	10.0856980	10.1118652	10.1975645
24	9.8025894	9.8880298	9.9147476	10.0854404	10.1119687	10.1974106
25	9.8027431	9.8879260	9.9150131	10.0851829	10.1120724	10.1972569
26	9.8028968	9.8878221	9.9152786	10.0849253	10.1121761	10.1971032
27	9.8030504	9.8877182	9.9155441	10.0846678	10.1122798	10.1969496
28	9.8032038	9.8876142	9.9158096	10.0844104	10.1123835	10.1967962
29	9.8033572	9.8875102	9.9160751	10.0841529	10.1124873	10.1966428
30	9.8035105	9.8874061	9.9163405	10.0838955	10.1125912	10.1964895
L. Co-Sine.		L. Sine.	L. Co-Tang.	L. Tangent.	L. Co-Secant.	L. Secant.

50 DEGREES.

## of the Chiefest Places of the World.

The Places Names.	North Latitude.	East Longitude.	The Sea-Coast of Iceland Island.	North Latitude.	East Longitude.
St. Vincent	16 55	16 32			
St. Antonio	17 07	16 56			
Cape Blanco	20 30	0 26			
Cape Boyador	26 55	02 52			
Marquepana	27 22	2 11			
Cape Denao	28 52	01 46			
Cape Gillam	29 50	01 29			
Cape de Ger	30 50	01 25			
Cape Canrin	32 27	01 06			
Tangier, East Longitude.	35 36	01 49			
			The Places Names.	North Latitude.	East Longitude.
				D. M.	D. M.
			Age Nafs	61 32	02 51
			Merchant Foreland	63 52	11 42
			Horn	63 42	10 10
			Silly	64 50	09 51
			Bargafar Point	65 27	07 01
			Long Nafs	66 26	07 36
			Grimfa	66 42	09 20



## A TABLE of Natural and

39 DEGREES.

M	N. Sine.	N. Co-Sine.	N. Tangent.	N. Co-Tang.	N. Secant.	N. Co-Secant.	
30	6360782	7716246	8243364	12130970	12959670	15721337	30
31	6363226	7714395	8248251	12123783	12962779	15715792	29
32	6365270	7712544	8253140	12116601	12965890	15710252	28
33	6367513	7710692	8258030	12109424	12969004	15704717	27
34	6369756	7708839	8262925	12102252	12972121	15699188	26
35	6371998	7706986	8267821	12095085	12975240	15693664	25
36	6374240	7705132	8272719	12087923	12978362	15688145	24
37	6376481	7703278	8277620	12080767	12981487	15682631	23
38	6378721	7701423	8282523	12073615	12984614	15677123	22
39	6380961	7699567	8287429	12066468	12987744	15671619	21
40	6383201	7697710	8292337	12059320	12990876	15666121	20
41	6385440	7695853	8297247	12052190	12994011	15660628	19
42	6387678	7693995	8302160	12045058	12997148	15655141	18
43	6389916	7692137	8307075	12037931	13000288	15649658	17
44	6392153	7690278	8311992	12030810	13003431	15644181	16
45	6394390	7688418	8316912	12023693	13006576	15638708	15
46	6396626	7686558	8321834	12016581	13009724	15633241	14
47	6398862	7684697	8326759	12009475	13012875	15627779	13
48	6401097	7682835	8331686	12002373	13016028	15622322	12
49	6403332	7680973	8336615	11995276	13019184	15616870	11
50	6405566	7679110	8341547	11988184	13022343	15611424	10
51	6407799	7677246	8346481	11981097	13025504	15605982	9
52	6410032	7675382	8351418	11974017	13028668	15600546	8
53	6412264	7673517	8356357	11966938	13031834	15595115	7
54	6414496	7671651	8361293	11959866	13035003	15589689	6
55	6416727	7669785	8366242	11952799	13038175	15584267	5
56	6418958	7667918	8371188	11945736	13041349	15578851	4
57	6421188	7666051	8376136	11938679	13044526	15573441	3
58	6423418	7664183	8381087	11931626	13047706	15568035	2
59	6425647	7662314	8386040	11924576	13050888	15562634	1
60	6427876	7660444	8390996	11917536	13054073	15557238	0
	N. Co-Sine.	N. Sine.	N. Co-Tang.	N. Tangent.	N. Co-Secant.	N. Secant.	M

50 DEGREES.

## A Table of the Latitude and Longitude

The Places Names.	North Latitud.	East Longit.		
Marza	D. M. D. M.			
Rage Point	67 08 09 42			
Fair Foreland	66 40 12 00			
Snow Hill	65 40 14 53			
Rook Point	65 11 14 50			
West main Isles	64 00 14 05			
Gammat Isles	63 17 12 53			
Grimes Hole	63 48 15 06			
	63 23 15 46			
The Places Names.	North Latitud.	East Longit.		
Cape Farewel	D. M. D. M.			
Sir Thomas Smith's Bay	59 00 41 50			
Bottom's Isles	59 10 79 50			
Bell Ifle	60 20 62 50			
	51 02 48 44			

## Artificial Sines, Tangents, and Secants.

39 DEGREES.

M	L. Sine.	L. Co-Sine.	L. Tangent.	L. Co-Tang.	L. Secant.	L. Co-Secant.	
30	9.8035105	9.8874061	9.92161045	10.08338955	10.1125939	10.1964895	30
31	9.8036637	9.8873019	9.92161045	10.08338955	10.1125939	10.1964895	29
32	9.8038168	9.8871977	9.92161045	10.08338955	10.1125939	10.1964895	28
33	9.8039699	9.8870934	9.92161045	10.08338955	10.1125939	10.1964895	27
34	9.8041228	9.8869890	9.92161045	10.08338955	10.1125939	10.1964895	26
35	9.8042757	9.8868846	9.92161045	10.08338955	10.1125939	10.1964895	25
36	9.8044284	9.8867801	9.92161045	10.08338955	10.1125939	10.1964895	24
37	9.8045811	9.8866756	9.92161045	10.08338955	10.1125939	10.1964895	23
38	9.8047338	9.8865710	9.92161045	10.08338955	10.1125939	10.1964895	22
39	9.8048861	9.8864663	9.92161045	10.08338955	10.1125939	10.1964895	21
40	9.8050385	9.8863616	9.92161045	10.08338955	10.1125939	10.1964895	20
41	9.8051908	9.8862568	9.92161045	10.08338955	10.1125939	10.1964895	19
42	9.8053430	9.8861519	9.92161045	10.08338955	10.1125939	10.1964895	18
43	9.8054951	9.8860470	9.92161045	10.08338955	10.1125939	10.1964895	17
44	9.8056472	9.8859420	9.92161045	10.08338955	10.1125939	10.1964895	16
45	9.8057991	9.8858370	9.92161045	10.08338955	10.1125939	10.1964895	15
46	9.8059510	9.8857319	9.92161045	10.08338955	10.1125939	10.1964895	14
47	9.8061027	9.8856267	9.92161045	10.08338955	10.1125939	10.1964895	13
48	9.8062544	9.8855215	9.92161045	10.08338955	10.1125939	10.1964895	12
49	9.8064060	9.8854162	9.92161045	10.08338955	10.1125939	10.1964895	11
50	9.8065575	9.8853109	9.92161045	10.08338955	10.1125939	10.1964895	10
51	9.8067089	9.8852056	9.92161045	10.08338955	10.1125939	10.1964895	9
52	9.8068602	9.8851000	9.92161045	10.08338955	10.1125939	10.1964895	8
53	9.8070114	9.8849945	9.92161045	10.08338955	10.1125939	10.1964895	7
54	9.8071626	9.8848889	9.92161045	10.08338955	10.1125939	10.1964895	6
55	9.8073136	9.8847832	9.92161045	10.08338955	10.1125939	10.1964895	5
56	9.8074646	9.8846775	9.92161045	10.08338955	10.1125939	10.1964895	4
57	9.8076154	9.8845717	9.92161045	10.08338955	10.1125939	10.1964895	3
58	9.8077662	9.8844659	9.92161045	10.08338955	10.1125939	10.1964895	2
59	9.8079169	9.8843599	9.92161045	10.08338955	10.1125939	10.1964895	1
60	9.8080675	9.8842540	9.92161045	10.08338955	10.1125939	10.1964895	0
	L. Co-Sine.	L. Sine.	L. Co-Tang.	L. Tangent.	L. Co-Secant.	L. Secant.	M

50 DEGREES.

## of the Chiefest Places of the World.

The Sea-Coast of New-found-Lanl, and New-England.				The Places Names.				North Latitud.	East Longit.			
The Places Names.				North Latitud.	East Longit.							
				D.	M.	D.	M.	D.	M.			
Cape Honblanto				52	11	30	14	Cape St. Francis	48	01	47	27
Bell-Ifle				51	02	48	44	Cape Delpair	47	36	46	03
Cape Bonavista				49	19	47	42	Cape de Raca	46	27	46	30
Trinity Bay				48	54	49	04	Bay Bulls	47	28	47	11
Bacalao				48	40	46	55	St John's Harbour	47	47	47	21
Consumption Bay				48	21	47	49	Plazentia Bay	47	32	47	41
								Cape St. Larofo.	47	10	48	59
								Island St. Paly	47	36	50	18
								Cape Raya	48	05	52	45
								Cape Degancia	54	01	53	21







## A TABLE of Natural and

40 DEGREES.

M	N. Sine.	N. Co-Sine.	N. Tangent.	N. Co-Tang.	N. Secant.	N. Co-Secant.	
30	6494450	7604060	8540807	11708496	13150870	15397590	30
31	6496692	7602170	8545539	11701601	13154139	15392449	29
32	6498903	7600280	8550873	11694712	13157410	15387212	28
33	6501114	7598389	8555910	11687827	13160684	15381980	27
34	6503324	7596498	8560950	11680947	13163961	15376752	26
35	6505533	7594606	8565992	11674071	13167241	15371530	25
36	6507742	7592713	8571037	11667200	13170523	15366312	24
37	6509950	7590820	8576084	11660334	13173805	15361100	23
38	6512158	7588926	8581133	11653472	13177086	15355892	22
39	6514366	7587031	8586185	11646615	13180365	15350689	21
40	6516572	7585136	8591240	11639763	13183677	15345491	20
41	6518778	7583240	8596297	11632916	13186975	15340297	19
42	6520984	7581343	8601357	11626073	13190274	15335109	18
43	6523189	7579446	8606419	11619234	13193575	15329925	17
44	6525394	7577548	8611484	11612400	13196881	15324746	16
45	6527598	7575650	8616551	11605571	13200188	15319572	15
46	6529801	7573751	8621621	11598747	13203498	15314403	14
47	6532004	7571851	8626693	11591927	13206811	15309238	13
48	6534206	7569950	8631768	11585111	13210126	15304078	12
49	6536408	7568049	8636846	11578301	13213444	15298933	11
50	6538609	7566147	8641926	11571495	13216765	15293773	10
51	6540810	7564245	8647009	11564693	13220089	15288627	9
52	6543010	7562342	8652094	11557896	13223416	15283487	8
53	6545209	7560439	8657181	11551104	13226747	15278351	7
54	6547408	7558535	8662271	11544316	13230077	15273219	6
55	6549606	7556630	8667364	11537532	13233412	15268093	5
56	6551804	7554724	8672460	11530754	13236750	15262971	4
57	6554001	7552818	8677558	11523979	13240091	15257854	3
58	6556198	7550911	8682659	11517210	13243435	15252741	2
59	6558394	7549004	8687762	11510445	13246781	15247634	1
60	6560590	7547096	8692868	11503684	13250130	15242531	0
V. Co-Sine.		N. Sine.	N. Co-Tang.	N. Tangent.	N. Co-Secant.	N. Secant.	M

49 DEGREES.

## A Table of the Latitude and Longitude

The Places Names.	North Latitude.	West Longit.	The Places Names.	North Latitude.	West Longit.
	D. M.	D. M.		D. M.	D. M.
Mevis	27	27 1 04	Yamacea	22	32 67 49
Sigvato	26	18 68 45	Soamia	24	20 68 50
Guatro	25	47 68 00	Javaqua	25	10 1 30
Guamina	25	15 67 53	Yamia	24	22 70 10
Tiango	24	33 66 30	Sr. John	18	30 60 42
Guanahimo	23	50 66 39	Santa Cruce	17	42 59 18
Mayagnana	23	05 66 51	Anguilla	18	48 57 00
Caycols	22	05 64 31	Sr. Martin	18	35 56 47
Amiana	21	40 64 38	Sr. Bartholomew	18	15 56 33
Inagua	21	19 67 03	Barbada	17	18 55 39

## Artificial Sines, Tangents, and Secants.

40 DEGREES.

M	L. Sine.	L. Co-Sine.	L. Tangent.	L. Co-Tang.	L. Secant.	L. Co-Secant.	
30	9.8125444	9.8810455	9.9314959	10.0535011	10.1189545	10.1874556	30
31	9.8126232	9.8809576	9.9317547	10.0532453	10.1190624	10.1873077	29
32	9.8127021	9.8808696	9.9320105	10.0529895	10.1191704	10.1871599	28
33	9.8127815	9.8807815	9.9322662	10.0527338	10.1192785	10.1870122	27
34	9.8128613	9.8806934	9.9325220	10.0524780	10.1193866	10.1868645	26
35	9.8129419	9.8806052	9.9327777	10.0522223	10.1194948	10.1867171	25
36	9.8130233	9.8805170	9.9330334	10.0519665	10.1196030	10.1865697	24
37	9.8131047	9.8804287	9.9332890	10.0517110	10.1197113	10.1864223	23
38	9.8131865	9.8803403	9.9335446	10.0514554	10.1198197	10.1862750	22
39	9.8132681	9.8802519	9.9338002	10.0512000	10.1199281	10.1861279	21
40	9.8133499	9.8801634	9.9340559	10.0509444	10.1200366	10.1859808	20
41	9.8134313	9.8800748	9.9343114	10.0506886	10.1201452	10.1858338	19
42	9.8135131	9.8799862	9.9345672	10.0504330	10.1202538	10.1856869	18
43	9.8135950	9.8798975	9.9348225	10.0501775	10.1203625	10.1855400	17
44	9.8136767	9.8798089	9.9350780	10.0499220	10.1204713	10.1853933	16
45	9.8137584	9.8797203	9.9353335	10.0496665	10.1205801	10.1852465	15
46	9.8138400	9.8796317	9.9355889	10.0494111	10.1206890	10.1851001	14
47	9.8139217	9.8795431	9.9358444	10.0491556	10.1207979	10.1849536	13
48	9.8140034	9.8794545	9.9360999	10.0489002	10.1209068	10.1848072	12
49	9.8140851	9.8793659	9.9363552	10.0486448	10.1210160	10.1846609	11
50	9.8141668	9.8792773	9.9366105	10.0483895	10.1211252	10.1845146	10
51	9.8142485	9.8791887	9.9368659	10.0481341	10.1212344	10.1843685	9
52	9.8143302	9.8791001	9.9371212	10.0478788	10.1213437	10.1842224	8
53	9.8144119	9.8790115	9.9373765	10.0476235	10.1214530	10.1840765	7
54	9.8144936	9.8789229	9.9376318	10.0473682	10.1215624	10.1839306	6
55	9.8145753	9.8788343	9.9378871	10.0471129	10.1216717	10.1837848	5
56	9.8146570	9.8787457	9.9381423	10.0468576	10.1217814	10.1836391	4
57	9.8147387	9.8786571	9.9383975	10.0466023	10.1218910	10.1834934	3
58	9.8148204	9.8785685	9.9386527	10.0463470	10.1220006	10.1833479	2
59	9.8149021	9.8784800	9.9389079	10.0460917	10.1221104	10.1832025	1
60	9.8149838	9.8783914	9.9391631	10.0458364	10.1222201	10.1830571	0
L. Co-Sine.		L. Sine.	L. Co-Tang.	L. Tangent.	L. Co-Secant.	L. Secant.	M

49 DEGREES.

## of the Chiefest Places of the World.

The Places Names.	North Latitude.	West Longit.	The Places Names.	North Latitude.	West Longit.
	D. M.	D. M.		D. M.	D. M.
Antego	16	32 54 52	Sr. Vincent	12	50 54 2
Dalhida	16	00 54 36	Guardadupa	16	00 55 3
Marigallatita	15	41 55 26	Monferrat	16	20 55 4
Dominica	15	00 55 05	Naves	17	00 56 2
Mattalina	14	20 54 44	Sr. Christophers	17	30 56 4
Sr. Lucia	13	30 54 43	Island Devas	15	57 57 2
Barbadus	13	10 52 58	Island Blanco	12	20 56 5
Tobago	11	12 53 06	Marguta	11	28 56 3
Point Degallia	10	45 53 31	Turtuga	11	30 57 4
Granada	12	10 54 32	Island Derickilla	12	19 58 0



## A TABLE of Natural and

41 DEGREES.

M	N. Sine.	N. Co-sine.	V. Tangent.	N. Co-Tang.	N. Secant.	N. Co-Secant.
0	656590	754796	8692868	1150363	13250130	15242531
1	6562785	7545157	8697975	11495928	13253482	15237433
2	6561980	7543278	8703057	11483175	13256837	15232339
3	6561474	7541363	8708220	11470329	13260194	15227250
4	6561367	7539457	8713316	11456939	13263554	15222165
5	6561560	7537546	8718435	11443949	13266918	15217087
6	6561752	7535634	8723556	11430958	13270284	15212012
7	6561944	7533721	8728680	11417966	13273653	15206942
8	6562135	7531808	8733806	11404972	13277025	15201876
9	6562326	7529894	8738935	11391979	13280399	15196815
10	6562516	7527980	8744067	11378986	13283776	15191759
11	6562706	7526065	8749201	11365993	13287156	15186708
12	6562895	7524149	8754338	11352995	13290539	15181661
13	6563083	7522233	8759478	11340000	13293925	15176619
14	6563271	7520316	8764620	11326998	13297314	15171581
15	6563458	7518398	8769765	11313995	13300706	15166548
16	6563645	7516480	8774912	11300990	13304100	15161520
17	6563831	7514561	8780062	11287985	13307497	15156496
18	6564017	7512641	8785215	11274978	13310897	15151477
19	6564202	7510721	8790370	11261970	13314300	15146462
20	6564386	7508800	8795528	11248960	13317706	15141452
21	6564569	7506879	8800689	11235947	13321115	15136447
22	6564752	7504957	8805852	11222932	13324527	15131446
23	6564935	7503034	8811018	11209915	13327942	15126450
24	6565118	7501111	8816186	11196897	13331359	15121459
25	6565300	7499187	8821357	11183878	13334779	15116472
26	6565481	7497262	8826531	11170858	13338202	15111489
27	6565662	7495337	8831707	11157837	13341628	15106511
28	6565842	7493411	8836886	11144815	13345057	15101538
29	6566022	7491484	8842068	11131792	13348489	15096569
30	6566202	7489557	8847253	11118768	13351924	15091605
N. Co-Sine.		N. Sine.	N. Co-Tang.	N. Tangent.	N. Co-Secant.	N. Secant.

48 DEGREES.

## A Table of the Latitude and Longitude

The Places Names.	North Latitude.	East Longit.	The Places Names.	North Latitude.	East Longit.
Boca	12 15 58	53	West end of Jamaica	18 38 54	57
Island Deavos.	12 29 59	22	The East end of Cuba	22 00 75	56
Bonoga	12 32 50	54	Caimanis	19 41 77	41
Quilla	12 25 50	39	Grand Caiman	19 21 78	45
Moagos	12 20 51	55	Santavilla	17 28 77	50
East end of Hispaniola	18 47 62	28	Molquito	14 50 76	04
Middle of Hispaniola	18 30 64	58	Guanabo	16 33 81	19
West end of Hispaniola	18 25 68	26	Guanabimo	16 10 83	04
East end of Jamaica	18 00 71	58	Cozumal	19 25 84	56
Jamaica Harbour	18 15 72	57	Lafallecranas	22 00 87	58

## Artificial Sines, Tangents, and Secants.

41 DEGREES.

M	L. Sine.	L. Co-Sine.	L. Tangent.	L. Co-Tang.	L. Secant.	L. Co-Secant.
0	9.8169429	9.8777799	9.9391681	10.0663856	10.1222201	10.1830571
1	9.8170882	9.8776700	9.9394182	10.0663818	10.1223300	10.1829118
2	9.8172334	9.8775601	9.9396683	10.0663780	10.1224399	10.1827666
3	9.8173785	9.8774501	9.9399184	10.0663742	10.1225499	10.1826215
4	9.8175235	9.8773401	9.9401685	10.0663704	10.1226599	10.1824765
5	9.8176685	9.8772300	9.9404186	10.0663666	10.1227699	10.1823315
6	9.8178133	9.8771198	9.9406687	10.0663628	10.1228799	10.1821867
7	9.8179581	9.8770096	9.9409188	10.0663590	10.1229899	10.1820419
8	9.8181028	9.8768993	9.9411689	10.0663552	10.1230999	10.1818972
9	9.8182474	9.8767890	9.9414190	10.0663514	10.1232099	10.1817525
10	9.8183919	9.8766785	9.9416691	10.0663476	10.1233199	10.1816078
11	9.8185364	9.8765680	9.9419192	10.0663438	10.1234299	10.1814631
12	9.8186807	9.8764574	9.9421693	10.0663400	10.1235399	10.1813184
13	9.8188250	9.8763468	9.9424194	10.0663362	10.1236499	10.1811737
14	9.8189692	9.8762361	9.9426695	10.0663324	10.1237599	10.1810290
15	9.8191133	9.8761253	9.9429196	10.0663286	10.1238699	10.1808843
16	9.8192575	9.8760145	9.9431697	10.0663248	10.1239799	10.1807396
17	9.8194016	9.8759036	9.9434198	10.0663210	10.1240899	10.1805949
18	9.8195458	9.8757927	9.9436699	10.0663172	10.1241999	10.1804502
19	9.8196898	9.8756816	9.9439199	10.0663134	10.1243099	10.1803055
20	9.8198339	9.8755706	9.9441699	10.0663096	10.1244199	10.1801608
21	9.8199779	9.8754594	9.9444199	10.0663058	10.1245299	10.1800161
22	9.8201196	9.8753482	9.9446699	10.0663020	10.1246399	10.1798714
23	9.8202630	9.8752369	9.9449199	10.0662982	10.1247499	10.1797267
24	9.8204063	9.8751256	9.9451699	10.0662944	10.1248599	10.1795820
25	9.8205496	9.8750142	9.9454199	10.0662906	10.1249699	10.1794373
26	9.8206927	9.8749027	9.9456699	10.0662868	10.1250799	10.1792926
27	9.8208358	9.8747912	9.9459199	10.0662830	10.1251899	10.1791479
28	9.8209788	9.8746795	9.9461699	10.0662792	10.1252999	10.1790032
29	9.8211217	9.8745679	9.9464199	10.0662754	10.1254099	10.1788585
30	9.8212646	9.8744561	9.9466699	10.0662716	10.1255199	10.1787138
L. Co-Sine.		L. Sine.	L. Co-Tang.	L. Tangent.	L. Co-Secant.	L. Secant.

48 DEGREES.

## of the Chiefst Places of the World.

The Places Names.	North Latitude.	East Longit.	The Sea-Coasts of Brasilia.	North Latitude.	East Longit.
The Island Delas	23 30 91	58	The River Amazons	00 00 41	30
Abraio	25 50 94	00	The Island of Sr. Paul	00 55 14	36
Labarmaia	22 55 93	16	The Island of Alcenion	07 48 20	06
Island Dearanas	22 36 93	14	Cape Blanco	02 25 22	29
Triango	21 23 53	05	Island Rocas	03 42 17	16
Zarka	20 50 93	05	Island Fernando	03 40 15	16
The Island of Prondanco	13 27 81	16	Abraho	05 00 17	56
Sr. Andrea	12 42 80	57			



## 41 DEGREES.

M	N. Sine.	V. Co-Sine.	N. Tangent.	N. Co-Tang.	N. Secant.	N. Co-Secant.	
30	6626201	7489557	3347253	11302941	13351924	15091605	30
31	6628379	7487629	3352440	1126321	13355362	15086645	29
32	6630557	7485721	3357530	11239702	13358803	15081690	28
33	6632734	7483772	3362622	11213083	13362246	15076739	27
34	6634911	7481842	3367717	11186473	13365692	15071793	26
35	6637087	7479912	3372815	11159372	13369141	15066852	25
36	6639262	7477981	3377916	11132711	13372594	15061915	24
37	6641437	7476049	3383023	11106674	13376043	15056982	23
38	6643611	7474117	3388136	11080031	13379507	15052054	22
39	6645785	7472184	3393254	11053493	13382953	15047131	21
40	6647959	7470251	3398375	11026949	13386432	15042211	20
41	6650132	7468318	3403499	11000409	13389899	15037297	19
42	6652304	7466385	3408625	11223754	13393369	15032387	18
43	6654475	7464452	3413754	11217186	13396842	15027481	17
44	6656646	7462510	3418884	11201613	13400317	15022580	16
45	6658817	7460574	3424015	11186043	13403795	15017683	15
46	6660987	7458637	3429146	11170495	13407275	15012791	14
47	6663156	7456699	3434277	11154951	13410761	15007903	13
48	6665325	7454760	3439408	11139409	13414243	15003020	12
49	6667493	7452821	3444539	11123868	13417738	14998141	11
50	6669661	7450881	3449670	11108327	13421232	14993257	10
51	6671828	7448940	3454801	11092786	13424728	14988397	9
52	6673994	7446999	3459932	11077245	13428227	14983531	8
53	6676160	7445057	3465063	11061704	13431729	14978670	7
54	6678326	7443115	3470194	11046163	13435234	14973813	6
55	6680491	7441172	3475325	11030622	13438742	14968961	5
56	6682655	7439229	3480456	11015081	13442253	14964113	4
57	6684818	7437285	3485587	11000540	13445767	14959270	3
58	6686981	7435342	3490718	10986000	13449284	14954430	2
59	6689144	7433399	3495849	10971459	13452804	14949596	1
60	6691306	7431456	3500980	10956918	13456327	14944765	0
N. Co-Sine		N. Sine.	N. Co-Tang.	N. Tangent.	N. Co-Secant.	N. Secant.	M

## 48 DEGREES.

## A Table of the Latitude and Longitude

The Places Names.	South Latitud.	West Longit.	The Places Names.	South Latitud.	West Longit.
Cape St. Raphaeli	06	10 19 36	Island de Martin	19	00 08 03
Cape St. Auguftin	08	25 18 28	Island de Pidos	21	52 05 51
River St. Mignol	09	30 19 01	Cape St. Toma	21	47 23 38
The River Roal	11	21 20 41	Cape Frio	22	52 24 43
River Gianda	14	49 22 06	Cape St. Maria	35	00 37 11
Cape de Abeotho	17	52 21 42	River de Platta	35	50 45 52
St. Harbara	18	11 21 06	Port St. Juliano	50	00 52 30
Island Afcenfon	17	19 17 01	The Streights of Ma-	53	30 56 30
Trinidad	19	50 14 24	gellane		
St. Maria Dagafia	19	38 12 14	Cape de Sancto Spirito	52	20 58 30

## 41 DEGREES.

M	L. Sine.	L. Co-Sine.	L. Tangent.	L. Co-Tang.	L. Secant.	L. Co-Secant.	
30	9.8212646	9.8744561	9.9468084	10.0531916	10.1255439	10.1878354	30
31	9.8214073	9.8743443	9.9469305	10.0529370	10.1256557	10.1878927	29
32	9.8215500	9.8742325	9.9471720	10.0526825	10.1257675	10.1879400	28
33	9.8216926	9.8741205	9.9473775	10.0524280	10.1258795	10.1879874	27
34	9.8218351	9.8740085	9.9475825	10.0521735	10.1259915	10.1880349	26
35	9.8219775	9.8738965	9.9477875	10.0519190	10.1261035	10.1880822	25
36	9.8221198	9.8737844	9.9479825	10.0516645	10.1262156	10.1881295	24
37	9.8222621	9.8736722	9.9481875	10.0514101	10.1263278	10.1881768	23
38	9.8224042	9.8735601	9.9483825	10.0511557	10.1264401	10.1882241	22
39	9.8225463	9.8734476	9.9485875	10.0509013	10.1265524	10.1882714	21
40	9.8226883	9.8733352	9.9487825	10.0506469	10.1266646	10.1883187	20
41	9.8228302	9.8732227	9.9489875	10.0503925	10.1267773	10.1883660	19
42	9.8229721	9.8731102	9.9491825	10.0501381	10.1268895	10.1884133	18
43	9.8231138	9.8729976	9.9493875	10.0498838	10.1270018	10.1884606	17
44	9.8232555	9.8728854	9.9495825	10.0496295	10.1271141	10.1885079	16
45	9.8233971	9.8727727	9.9497875	10.0493752	10.1272264	10.1885552	15
46	9.8235386	9.8726604	9.9499825	10.0491209	10.1273387	10.1886025	14
47	9.8236800	9.8725486	9.9501875	10.0488666	10.1274510	10.1886498	13
48	9.8238213	9.8724367	9.9503825	10.0486124	10.1275633	10.1886971	12
49	9.8239626	9.8723247	9.9505875	10.0483581	10.1276756	10.1887444	11
50	9.8241037	9.8722076	9.9507825	10.0481038	10.1277879	10.1887917	10
51	9.8242448	9.8720949	9.9509875	10.0478497	10.1278924	10.1888390	9
52	9.8243858	9.8719813	9.9511825	10.0475955	10.1280018	10.1888863	8
53	9.8245267	9.8718681	9.9513875	10.0473415	10.1281112	10.1889336	7
54	9.8246676	9.8717548	9.9515825	10.0470872	10.1282245	10.1889809	6
55	9.8248083	9.8716414	9.9517875	10.0468330	10.1283386	10.1890282	5
56	9.8249490	9.8715279	9.9519825	10.0465789	10.1284527	10.1890755	4
57	9.8250896	9.8714144	9.9521875	10.0463248	10.1285668	10.1891228	3
58	9.8252301	9.8713008	9.9523825	10.0460707	10.1286809	10.1891701	2
59	9.8253707	9.8711872	9.9525875	10.0458166	10.1287950	10.1892174	1
60	9.8255109	9.8710735	9.9527825	10.0455626	10.1289091	10.1892647	0
L. Co-Sine.		L. Sine.	L. Co-Tang.	L. Tangent.	L. Co-Secant.	L. Secant.	M

## 48 DEGREES.

## of the Chiefest Places of the World.

The Places Names.	South Latitud.	West Longit.	The Places Names.	South Latitud.	West Longit.
Cape Victoria, West end of the Streights	52	30 05 40	Nova Albion, or New- England, in the South Sea, the back side of it.	46	00 162 30
Lima Cape	12	00 30 30	Cape de Fortuna (Ani- ar. fra.	55	30 170 E. 0
Cape Guya, Cape Blanco	06	10 35 30	Infule Salamonis	05	50 169 30
Cape St. Francisco	01	30 80 30	Nombre de Jcius	36	N 00 153 E. 0
Cape St. Frances	North	West.	Tapan Infule	01	S 00 155 E. 0
Point de bon matre	07	30 80 00	Cape de Buena Defco		
Nombre de Dios, W. Sea.	10	00 77 30			



42 DEGREES.

M	N. Sine.	N. Co-Sine.	N. Tangent.	N. Co-Tang.	N. Secant.	N. Co-Secant.
0	6691306	7431448	9204041	11106125	13416327	14244765
1	6693467	7429501	9209329	11092530	13459583	14239940
2	6695628	7427554	9214580	11078142	13453382	14235118
3	6697788	7425606	9219834	11063531	13455914	14230301
4	6699948	7423657	9225131	11048517	13459449	14225488
5	6702107	7421708	9230411	11033693	13473987	14220680
6	6704266	7419758	9235694	11018719	13477523	14215875
7	6706424	7417808	9240972	11003750	13481072	14211076
8	6708582	7415857	9246267	11004234	13484519	14206282
9	6710739	7413905	9251558	11004751	13488169	14201489
10	6712895	7411953	9256851	11004156	13491721	14196703
11	6715051	7410000	9262147	11003491	13495277	14191920
12	6717206	7408046	9267446	11002843	13498836	14187142
13	6719361	7406092	9272743	11002201	13502398	14182365
14	6721515	7404137	9278053	11001575	13505963	14177597
15	6723668	7402181	9283363	11000911	13509531	14172834
16	6725821	7400225	9288671	11000209	13513102	14168065
17	6727973	7398268	9293984	11000521	13516676	14163317
18	6730125	7396311	9299300	11000856	13520254	14158585
19	6732276	7394353	9304619	11001201	13523834	14153817
20	6734427	7392394	9309941	11001572	13527417	14149073
21	6736577	7390435	9315265	11001968	13531003	14144334
22	6738727	7388475	9320592	11002381	13534593	14139599
23	6740876	7386515	9325922	11002812	13538186	14134868
24	6743024	7384554	9331255	11003267	13541781	14130142
25	6745172	7382592	9336591	11003740	13545379	14125420
26	6747319	7380629	9341929	11004234	13548980	14120702
27	6749466	7378666	9347270	11004751	13552585	14115988
28	6751612	7376702	9352615	11005285	13556193	14111278
29	6753757	7374738	9357962	11005836	13559803	14106573
30	6755902	7372773	9363312	11006391	13563417	14101872
N. Co-Sine N. Sine. N. Co-Tang. N. Tangent. N. Co-Secant. N. Secant. M						

47 DEGREES.

A Table of the Latitude and Longitude

The East-India Islands.			The Places Names.		North	East
The Places Names.			Latitude.	Longitude.	D. M. D. M.	D. M. D. M.
Hipon Island			06	45	125	20
Bantam, East-India			06	15	125	34
Jamba Islands			01	49	125	25
South end of Sumatra			05	52	125	48
Middle of Sumatra			01	30	120	49
North end of Sumatra			05	28	116	35
Gomaspala			05	40	116	29
Niobar			07	00	115	04
Island Desombro			08	00	114	54
Island Rusta			09	50	114	33
Quarinibar			11	10	114	44
Chitra Andomaio			12	00	114	41
Island Dandemajo			13	00	114	39
Island Decocofs			14	30	115	12
Celloan			07	50	98	39
Doda Safia			09	40	93	02
Andaio			11	30	90	51

42 DEGREES.

M	L. Sine.	L. Co-Sine.	L. Tangent.	L. Co-Tang.	L. Secant.	L. Co-Secant.
0	9.8351509	9.8719735	9.9544374	10.0455626	10.1289265	10.1744321
1	9.8356512	9.8720597	9.9546915	10.0453085	10.1290403	10.1743485
2	9.8361513	9.8721458	9.9549455	10.0450545	10.1291542	10.1742648
3	9.8366514	9.8722319	9.9551995	10.0448005	10.1292681	10.1741812
4	9.8371515	9.8723180	9.9554535	10.0445465	10.1293821	10.1740976
5	9.8376516	9.8724041	9.9557075	10.0442925	10.1294961	10.1740140
6	9.8381517	9.8724902	9.9559615	10.0440385	10.1296102	10.1739304
7	9.8386518	9.8725763	9.9562155	10.0437845	10.1297244	10.1738468
8	9.8391519	9.8726624	9.9564695	10.0435305	10.1298387	10.1737632
9	9.8396520	9.8727485	9.9567235	10.0432765	10.1299530	10.1736796
10	9.8401521	9.8728346	9.9569775	10.0430225	10.1300674	10.1735960
11	9.8406522	9.8729207	9.9572315	10.0427685	10.1301818	10.1735124
12	9.8411523	9.8730068	9.9574855	10.0425145	10.1302963	10.1734288
13	9.8416524	9.8730929	9.9577395	10.0422605	10.1304109	10.1733452
14	9.8421525	9.8731790	9.9579935	10.0420065	10.1305255	10.1732616
15	9.8426526	9.8732651	9.9582475	10.0417525	10.1306401	10.1731780
16	9.8431527	9.8733512	9.9585015	10.0414985	10.1307547	10.1730944
17	9.8436528	9.8734373	9.9587555	10.0412445	10.1308693	10.1730108
18	9.8441529	9.8735234	9.9590095	10.0409905	10.1309848	10.1729272
19	9.8446530	9.8736095	9.9592635	10.0407365	10.1310998	10.1728436
20	9.8451531	9.8736956	9.9595175	10.0404825	10.1312149	10.1727600
21	9.8456532	9.8737817	9.9597715	10.0402285	10.1313300	10.1726764
22	9.8461533	9.8738678	9.9600255	10.0400745	10.1314451	10.1725928
23	9.8466534	9.8739539	9.9602795	10.0398205	10.1315602	10.1725092
24	9.8471535	9.8740400	9.9605335	10.0395665	10.1316753	10.1724256
25	9.8476536	9.8741261	9.9607875	10.0393125	10.1317904	10.1723420
26	9.8481537	9.8742122	9.9610415	10.0390585	10.1319055	10.1722584
27	9.8486538	9.8742983	9.9612955	10.0388045	10.1320206	10.1721748
28	9.8491539	9.8743844	9.9615495	10.0385505	10.1321357	10.1720912
29	9.8496540	9.8744705	9.9618035	10.0382965	10.1322508	10.1720076
30	9.8501541	9.8745566	9.9620575	10.0380425	10.1323659	10.1719240
L. Co-Sine. L. Sine. L. Co-Tang. L. Tangent. L. Co-Secant. L. Secant. M						

47 DEGREES.

of the Chiefest Places of the World.

The Places Names.		South	East	The Places Names.		South	East
		Latitude	Longitude.			Latitude	Longitude.
Gariné		D. M. D. M.	D. M. D. M.	Adu		D. M. D. M.	D. M. D. M.
Moique		10	50	09	50	05	39
Cuballa		09	50	09	31	02	40
Island de Profol		08	53	01	07	06	10
Island de Zocha		10	23	00	55	03	30
Chorebaman		11	12	00	45	03	07
Sucatra		12	32	07	55	23	21
Abdelcari		12	18	74	01	03	40
Apouaria		12	12	71	44	03	57
		09	50	09	50	00	66



## A TABLE of Natural and

42 DEGREES.

M	N. Sine.	N. Co-Sine.	N. Tangent.	N. Co-Tang.	N. Secant.	N. Co-Secant.
30	6755902	7372773	9163312	10913085	13563417	14801872
31	6758046	7370858	9168665	10906714	13567234	14797176
32	6760190	7368812	9174020	10900347	13571051	14792483
33	6762333	7366875	9179377	10893973	13574867	14787795
34	6764476	7364937	9184740	10887521	13578683	14783111
35	6766618	7362992	9190104	10881156	13582499	14778431
36	6768760	7360971	9195471	10874791	13586316	14773755
37	6770901	7358952	9200841	10868457	13589950	14769054
38	6773041	7356932	9206214	10862122	13593583	14764344
39	6775181	7354911	9211590	10855783	13597215	14759614
40	6777320	7352890	9216968	10849454	13600846	14754874
41	6779459	7350868	9222349	10843122	13604477	14750124
42	6781597	7348846	9227731	10836786	13608107	14745374
43	6783734	7346823	9233112	10830453	13611737	14740624
44	6785871	7344800	9238494	10824120	13615367	14735874
45	6788007	7342777	9243875	10817783	13618997	14731124
46	6790143	7340754	9249257	10811446	13622627	14726374
47	6792278	7338731	9254639	10805109	13626257	14721624
48	6794413	7336708	9260020	10798772	13629887	14716874
49	6796548	7334685	9265402	10792435	13633517	14712124
50	6798684	7332662	9270783	10786098	13637147	14707374
51	6800819	7330639	9276165	10779761	13640777	14702624
52	6802954	7328616	9281547	10773424	13644407	14697874
53	6805089	7326593	9286929	10767087	13648037	14693124
54	6807224	7324570	9292310	10760750	13651667	14688374
55	6809359	7322547	9297692	10754413	13655297	14683624
56	6811494	7320524	9303073	10748076	13658927	14678874
57	6813629	7318501	9308455	10741739	13662557	14674124
58	6815764	7316478	9313837	10735402	13666187	14669374
59	6817899	7314455	9319219	10729065	13669817	14664624
60	6819934	7312432	9324600	10722728	13673447	14659874

N. Co-Sine

N. Sine.

N. Co-Tang

N. Tangent.

N. Co-Secant.

N. Secant.

M

42 DEGREES.

## A Table of the Latitude and Longitude

The Places Names.	South Latitud.	East Longit.	The Places Names.	South Latitud.	East Longit.
Aldore Has	D. M.D. M.		John Demiz	D. M.D. M.	
John de Nava	09 05 65	02	Comoro	10 48 54	24
Cofinobodo	09 06 63	26	Monhalla	11 20 55	48
Donatall	00 40 61	52	Foanna	12 11 56	25
Aignos	08 20 59	57	Mayatta	12 09 57	03
John de Comoro	09 30 58	18	St. Christopher	12 40 57	55
Pemba	09 05 57	20	John de Nova	14 30 56	03
Zanziba	05 09 53	30	Ballas de India	17 20 55	29
Manfia	06 26 53	35		22 10 55	22
	07 50 53	08			

## Artificial Sines, Tangents, and Secants.

42 DEGREES.

M	L. Sine.	L. Co-Sine.	L. Tangent.	L. Co-Tang.	L. Secant.	L. Co-Secant.
30	9.8256833	9.8676309	9.9620525	10.0379475	10.1323691	10.1703167
31	9.8258212	9.8675151	9.9621061	10.0378939	10.1324189	10.1701788
32	9.8259589	9.8673992	9.9621597	10.0378403	10.1324688	10.1700411
33	9.8260968	9.8672833	9.9622133	10.0377867	10.1325187	10.1699034
34	9.8262347	9.8671673	9.9622669	10.0377331	10.1325686	10.1697657
35	9.8263727	9.8670512	9.9623204	10.0376795	10.1326185	10.1696280
36	9.8265099	9.8669351	9.9623740	10.0376259	10.1326684	10.1694903
37	9.8266474	9.8668190	9.9624275	10.0375723	10.1327183	10.1693526
38	9.8267847	9.8667026	9.9624811	10.0375187	10.1327682	10.1692149
39	9.8269223	9.8665863	9.9625346	10.0374651	10.1328181	10.1690772
40	9.8270599	9.8664699	9.9625881	10.0374115	10.1328680	10.1689395
41	9.8271975	9.8663534	9.9626416	10.0373579	10.1329179	10.1688018
42	9.8273352	9.8662369	9.9626951	10.0373043	10.1329678	10.1686641
43	9.8274728	9.8661203	9.9627486	10.0372507	10.1330177	10.1685264
44	9.8276105	9.8660036	9.9628021	10.0371971	10.1330676	10.1683887
45	9.8277481	9.8658869	9.9628556	10.0371435	10.1331175	10.1682510
46	9.8278858	9.8657700	9.9629091	10.0370899	10.1331674	10.1681133
47	9.8280234	9.8656531	9.9629626	10.0370363	10.1332173	10.1679756
48	9.8281611	9.8655362	9.9630161	10.0369827	10.1332672	10.1678379
49	9.8282987	9.8654192	9.9630696	10.0369291	10.1333171	10.1677002
50	9.8284364	9.8653021	9.9631231	10.0368755	10.1333670	10.1675625
51	9.8285740	9.8651850	9.9631766	10.0368219	10.1334169	10.1674248
52	9.8287117	9.8650679	9.9632301	10.0367683	10.1334668	10.1672871
53	9.8288493	9.8649508	9.9632836	10.0367147	10.1335167	10.1671494
54	9.8289870	9.8648337	9.9633371	10.0366611	10.1335666	10.1670117
55	9.8291246	9.8647166	9.9633906	10.0366075	10.1336165	10.1668740
56	9.8292623	9.8645995	9.9634441	10.0365539	10.1336664	10.1667363
57	9.8293999	9.8644824	9.9634976	10.0364993	10.1337163	10.1665986
58	9.8295376	9.8643653	9.9635511	10.0364457	10.1337662	10.1664609
59	9.8296752	9.8642482	9.9636046	10.0363921	10.1338161	10.1663232
60	9.8298129	9.8641311	9.9636581	10.0363385	10.1338660	10.1661855

L. Co-Sine.

L. Sine.

L. Co-Tang.

L. Tangent.

L. Co-Secant.

L. Secant.

M

42 DEGREES.

## of the Chiefest Places of the World.

The Places Names.	South Latitud.	East Longit.	The Places Names.	South Latitud.	East Longit.
North end of St. Lawrence	D. M.D. M.		John de Lisbonc	D. M.D. M.	
St. Apohima	25 37 60	54	Romoras	25 24 68	33
Domicaicahas	20 50 55	54		28 19 31	21
Moroflas	20 50 66	54	The Sea-Coast on the Main Continent in the East-India.		
Dofgarias	20 20 68	44			
St. Branda	15 20 70	43			
England's Forest	17 13 74	44			
Diego Roize	20 50 74	14	Malacca	01 N. 41 116	14
	20 05 75	54	Queda	06 47 117	44



## 43 DEGREES.

M.	N. Sine.	N. Co-Sine.	N. Tangent.	N. Co-Tang.	N. Secant.	N. Co-Secant.
0	6819984	7313537	9325151	10723687	13673275	14662792
1	6822111	7311553	9310591	10717435	13676985	14558220
2	6824237	7309568	9306034	10711187	13680699	14453652
3	6826363	7307583	9301479	10704943	13684416	14349088
4	6828488	7305597	9296925	10698702	13688136	14244529
5	6830613	7303610	9292370	10692466	13691859	14140073
6	6832737	7301623	9287814	10686233	13695586	14035512
7	6834861	7299635	9283259	10680004	13699315	13930951
8	6836984	7297646	9278703	10673779	13703048	13826387
9	6839107	7295657	9274148	10667558	13706784	13721821
10	6841229	7293667	9269593	10661341	13710523	13617255
11	6843350	7291677	9265038	10655128	13714266	13512689
12	6845471	7289686	9260482	10648918	13718011	13408123
13	6847591	7287694	9255927	10642713	13721760	13303557
14	6849711	7285702	9251371	10636511	13725512	13198991
15	6851830	7283709	9246816	10630313	13729268	13094425
16	6853948	7281716	9242261	10624119	13733026	12989859
17	6856066	7279722	9237706	10617929	13736786	12885293
18	6858183	7277727	9233151	10611742	13740533	12780727
19	6860300	7275732	9228596	10605560	13744291	12676161
20	6862416	7273736	9224041	10599388	13748049	12571595
21	6864532	7271740	9219486	10593220	13751807	12467029
22	6866647	7269743	9214931	10587054	13755564	12362463
23	6868761	7267745	9210376	10580887	13759320	12257897
24	6870875	7265747	9205821	10574720	13763076	12153331
25	6872988	7263748	9201266	10568554	13766832	12048765
26	6875101	7261748	9196711	10562388	13770588	11944199
27	6877213	7259748	9192156	10556223	13774344	11839633
28	6879324	7257747	9187601	10550057	13778100	11735067
29	6881435	7255746	9183046	10543892	13781856	11630501
30	6883545	7253744	9178491	10537726	13785612	11525935
N. Co-Sine.	N. Sine.	N. Co-Tang.	N. Tangent.	N. Co-Secant.	N. Secant.	M

## 46 DEGREES.

A Table of the Latitude and Longitude

The Places Names.	North Latitud.	East Longit.	The Places Names.	North Latitud.	East Longit.
River de Care	D. M. D. M.		Mongalar	D. M. D. M.	
River Bengale	10 45 118 54		Dodall	12 40 97 19	
Aicopoir	22 09 121 33		Goa	17 01 98 55	
Sammabron	20 19 112 39		Chaul	14 40 57 01	
Arme Gon	18 30 108 52		Calecut in East-India	18 10 98 51	
Naga Param	14 35 100 27		Macao in the K. of Pegu	11 36 92 58	
Cape Comorin	11 21 99 56		Domon	19 30 112 43	
Cochin	07 50 97 39		Surat	11 54 99 01	
Callant	09 40 97 21		Dio	21 00 99 36	
	10 48 97 27			20 48 96 57	

## 43 DEGREES.

M.	L. Sine.	L. Co-Sine.	L. Tangent.	L. Co-Tang.	L. Secant.	L. Co-Secant.
0	9.8337833	9.8641275	9.9669559	10.0303441	10.1358725	10.1662167
1	9.8339188	9.8640096	9.9669991	10.0300909	10.1359904	10.1660812
2	9.8340541	9.8638917	9.9670162	10.0298376	10.1361083	10.1659459
3	9.8341894	9.8637737	9.9670415	10.0295843	10.1362263	10.1658106
4	9.8343246	9.8636557	9.9670668	10.0293311	10.1363443	10.1656754
5	9.8344597	9.8635376	9.9670921	10.0290779	10.1364624	10.1655403
6	9.8345948	9.8634194	9.9671175	10.0288246	10.1365805	10.1654052
7	9.8347297	9.8633011	9.9671428	10.0285714	10.1366989	10.1652703
8	9.8348646	9.8631828	9.9671681	10.0283182	10.1368172	10.1651354
9	9.8349994	9.8630644	9.9671935	10.0280650	10.1369356	10.1650006
10	9.8351341	9.8629460	9.9672188	10.0278118	10.1370540	10.1648659
11	9.8352688	9.8628274	9.9672441	10.0275587	10.1371726	10.1647312
12	9.8354033	9.8627088	9.9672694	10.0273055	10.1372912	10.1645967
13	9.8355378	9.8625902	9.9672947	10.0270523	10.1374098	10.1644622
14	9.8356722	9.8624714	9.9673200	10.0267992	10.1375286	10.1643278
15	9.8358066	9.8623526	9.9673453	10.0265461	10.1376474	10.1641934
16	9.8359408	9.8622338	9.9673707	10.0262929	10.1377662	10.1640592
17	9.8360750	9.8621148	9.9673960	10.0260398	10.1378852	10.1639250
18	9.8362091	9.8619958	9.9674213	10.0257867	10.1380042	10.1637909
19	9.8363431	9.8618767	9.9674466	10.0255336	10.1381233	10.1636569
20	9.8364771	9.8617576	9.9674719	10.0252805	10.1382424	10.1635229
21	9.8366109	9.8616383	9.9674972	10.0250274	10.1383617	10.1633891
22	9.8367447	9.8615190	9.9675225	10.0247743	10.1384810	10.1632553
23	9.8368784	9.8613997	9.9675478	10.0245213	10.1386003	10.1631216
24	9.8370121	9.8612803	9.9675731	10.0242682	10.1387197	10.1629879
25	9.8371456	9.8611608	9.9675984	10.0240151	10.1388392	10.1628544
26	9.8372791	9.8610412	9.9676237	10.0237621	10.1389588	10.1627209
27	9.8374125	9.8609215	9.9676490	10.0235091	10.1390785	10.1625875
28	9.8375458	9.8608018	9.9676744	10.0232560	10.1391982	10.1624542
29	9.8376790	9.8606821	9.9676997	10.0230030	10.1393179	10.1623210
30	9.8378122	9.8605622	9.9677250	10.0227500	10.1394378	10.1621878
L. Co-Sine.	L. Sine.	L. Tangent.	L. Co-Tang.	L. Secant.	L. Co-Secant.	M

## 46 DEGREES.

of the Chiefest Places of the World.

The Places Names.	North Latitud.	East Longit.	The Places Names.	North Latitud.	East Longit.
River Decinda	24 55 95 39		Magadox	02 30 59 24	
Gudar	24 50 89 28		Molinda	02 S. 42 52 11	
Cape Muchoaridan	25 32 82 33		Tanga	05 20 52 01	
Cape Ruffalgat	22 07 84 39		Cape Fasto	08 02 52 24	
Cape de Ponto	8 19 79 09		Dagnada	15 17 53 26	
Dofar	17 00 75 04		Cape Corintes	23 30 48 51	
Cape de Matriaia	15 33 72 39		Cape Sr. Marin	25 40 46 59	
Adon	13 03 66 50		River Sr. Luffea	28 25 46 09	
Cape Guardafuy	11 40 71 24		Bay Doliagoa	33 18 43 59	
Cape de Baflos	04 50 65 19				



M	N. Sine.	N. Co-Sine	N. Tangent.	N. Co-Tang.	N. Secant.	N. Co-Secant.	
30	6883345	7253744	9159646	12537801	13785935	14527397	30
31	6885655	7251711	9425176	10511664	13789792	14522946	29
32	6887764	7249733	9600739	10445531	13793602	14518498	28
33	6889873	7247734	9756245	10319401	13797416	14514055	27
34	6891981	7245729	9811781	10151275	13801233	14509616	26
35	6894089	7243724	9817325	10027153	13805053	14505151	25
36	6896196	7241718	9822871	10021034	13808877	14500749	24
37	6898302	7239712	9828420	10494920	13812704	14496322	23
38	6900407	7237705	9833971	10453859	13816534	14491898	22
39	6902512	7235693	9839526	10413272	13820367	14487477	21
40	6904617	7233680	9845083	10475698	13824204	14483063	20
41	6906721	7231661	9850644	10440498	13828034	14478651	19
42	6908824	7229651	9856208	10405402	13831867	14474243	18
43	6910927	7227641	9861774	10370310	13835704	14469839	17
44	6913029	7225631	9867344	10435221	13839534	14465439	16
45	6915131	7223620	9872917	10400136	13843367	14461043	15
46	6917232	7221608	9878494	10440055	13847204	14456651	14
47	6919332	7219595	9884073	10433977	13851034	14452262	13
48	6921432	7217582	9889655	10427924	13854867	14447878	12
49	6923531	7215568	9895241	10421833	13858704	14443497	11
50	6925630	7213554	9900829	10415767	13862534	14439112	10
51	6927728	7211539	9906421	10409704	13866367	14434745	9
52	6929825	7209524	9912016	10403645	13870203	14430379	8
53	6931922	7207508	9917614	10397589	13874033	14426013	7
54	6934018	7205491	9923215	10391537	13877866	14421652	6
55	6936114	7203474	9928819	10385489	13881703	14417295	5
56	6938209	7201456	9934427	10379445	13885534	14412941	4
57	6940304	7199438	9940037	10373404	13889367	14408591	3
58	6942398	7197419	9945645	10367367	13893203	14404246	2
59	6944491	7195401	9951258	10361333	13897032	14399904	1
60	6946584	7193383	9956873	10355303	13900866	14395555	0
N. Co-Sine.	N. Sine.	N. Co-Tang.	N. Tangent.	N. Secant.	N. Co-Secant.	M	

A Table of the Latitude and Longitude

		The Places Names.		South Latitude.	East Longitude.
The Sea-Coast from Cape Bone				D. M. D. M.	D. M. D. M.
Esprance to Guinney.		Cape Agullas		36 20	33 54
		Cape Bone Esprance		35 50	32 54
		Cape Sacos		29 40	30 14
		Atencion Island		07 48	05 24
		St. Hellena		16 03	10 08
		St. Nova		16 03	19 48
		Baffas		17 45	27 35
		Cape Lado		10 00	29 23
		Cape Padron		06 00	29 04
The Places Names.		South Latitude.	East Longitude.	D. M. D. M.	D. M. D. M.
Island Desfition		36 57	11 44		
Island Degiaiatia		37 56	14 04		

M	L. Sine.	L. Co-Sine.	L. Tangent.	L. Co-Tang.	L. Secant.	L. Co-Secant.	
30	9.8378122	9.8605622	9.9772500	10.0227500	10.1394378	10.1621878	30
31	9.8379453	9.8604423	9.9773750	10.0226250	10.1395577	10.1620547	29
32	9.8380783	9.8603223	9.9775000	10.0225000	10.1396777	10.1619217	28
33	9.8382112	9.8602022	9.9776250	10.0223750	10.1397977	10.1617888	27
34	9.8383441	9.8600821	9.9777500	10.0222500	10.1399179	10.1616559	26
35	9.8384769	9.8599621	9.9778750	10.0221250	10.1400381	10.1615231	25
36	9.8386096	9.8598416	9.9780000	10.0220000	10.1401584	10.1613904	24
37	9.8387422	9.8597213	9.9781250	10.0218750	10.1402787	10.1612578	23
38	9.8388747	9.8596009	9.9782500	10.0217500	10.1403991	10.1611253	22
39	9.8390072	9.8594804	9.9783750	10.0216250	10.1405196	10.1609928	21
40	9.8391396	9.8593599	9.9785000	10.0215000	10.1406401	10.1608604	20
41	9.8392719	9.8592393	9.9786250	10.0213750	10.1407607	10.1607281	19
42	9.8394041	9.8591186	9.9787500	10.0212500	10.1408814	10.1605959	18
43	9.8395363	9.8589978	9.9788750	10.0211250	10.1410022	10.1604637	17
44	9.8396684	9.8588770	9.9790000	10.0210000	10.1411230	10.1603316	16
45	9.8398004	9.8587561	9.9791250	10.0208750	10.1412439	10.1601996	15
46	9.8399323	9.8586351	9.9792500	10.0207500	10.1413649	10.1600677	14
47	9.8400642	9.8585141	9.9793750	10.0206250	10.1414859	10.1599358	13
48	9.8401959	9.8583932	9.9795000	10.0205000	10.1416071	10.1598041	12
49	9.8403276	9.8582718	9.9796250	10.0203750	10.1417284	10.1596724	11
50	9.8404593	9.8581505	9.9797500	10.0202500	10.1418495	10.1595407	10
51	9.8405908	9.8580293	9.9798750	10.0201250	10.1419708	10.1594092	9
52	9.8407223	9.8579078	9.9799999	10.0200000	10.1420922	10.1592777	8
53	9.8408537	9.8577863	9.9801250	10.0198750	10.1422137	10.1591463	7
54	9.8409850	9.8576648	9.9802500	10.0197500	10.1423352	10.1590150	6
55	9.8411162	9.8575432	9.9803750	10.0196250	10.1424568	10.1588838	5
56	9.8412474	9.8574215	9.9805000	10.0195000	10.1425785	10.1587526	4
57	9.8413785	9.8572999	9.9806250	10.0193750	10.1426999	10.1586215	3
58	9.8415095	9.8571779	9.9807500	10.0192500	10.1428215	10.1584905	2
59	9.8416404	9.8570561	9.9808750	10.0191250	10.1429431	10.1583596	1
60	9.8417713	9.8569341	9.9810000	10.0190000	10.1430648	10.1582287	0
L. Co-Sine.	L. Sine.	L. Co-Tang.	L. Tangent.	L. Secant.	L. Co-Secant.	M	

of the Chiefst Places of the World.

		The Places Names.		South Latitude.	East Longitude.
The Places Names.		South Latitude.	East Longitude.	D. M. D. M.	D. M. D. M.
Cape Lopes		01 00	25 21		
Anabona Island		01 22	22 56		
Island Sr. Mathaas		01 40	07 45		
Island Sr. Toma		00 20	23 54		
Island Chocos		00 40	23 50		
River Libano		00 10	27 16		
River de Angai		01 00	27 30		
Island Principas		01 50	25 14		
Island Defarnanda		03 10	26 06		
The Sea-Coast from Samson's River to the River of Gambo, Coast Guinney and Barbara.		Old Callabar		04 N. 50	25 E. 15



44 DEGREES.									
M	N. Sine.	N. Co-Sine.	N. Tangent.	N. Co-Tang.	N. Secant.	N. Co-Secant.			
0	6963584	7193398	9656888	10351303	13901636	14395565	60		
1	6948576	7191377	9652511	10349277	13905543	14391231	59		
2	6930767	7189355	9648137	10347254	13909453	14386900	58		
3	6912858	7187333	9643767	10345235	13913366	14382574	57		
4	6894949	7185310	9639400	10343220	13917283	14378251	56		
5	6877039	7183287	9635035	10341208	13921203	14373932	55		
6	6859128	7181263	9630674	10339199	13925127	14369616	54		
7	6841217	7179238	9626316	10337195	13929054	14365305	53		
8	6823305	7177213	9621962	10335194	13932985	14360997	52		
9	6805392	7175187	9617610	10333196	13936918	14356693	51		
10	6787479	7173161	9613262	10331202	13940856	14352393	50		
11	6769565	7171134	9608917	10329216	13944795	14348097	49		
12	6751651	7169106	9604575	10327236	13948740	14343805	48		
13	6733736	7167078	9600236	10325243	13952688	14339516	47		
14	6715821	7165049	9595901	10323263	13956639	14335231	46		
15	6697905	7163019	9591569	10321287	13960593	14330950	45		
16	6679988	7160989	9587240	10319315	13964551	14326672	44		
17	6662071	7158958	9582914	10317346	13968512	14322399	43		
18	6644153	7156927	9578591	10315378	13972477	14318129	42		
19	6626234	7154895	9574272	10313419	13976445	14313863	41		
20	6608315	7152863	9569956	10311461	13980416	14309600	40		
21	6590396	7150830	9565643	10309506	13984391	14305342	39		
22	6572476	7148796	9561333	10307555	13988369	14301087	38		
23	6554555	7146762	9557027	10305606	13992351	14296836	37		
24	6536633	7144727	9552724	10303664	13996336	14292588	36		
25	6518711	7142691	9548424	10301723	14000325	14288344	35		
26	6500789	7140655	9544127	10299786	14004317	14284104	34		
27	7002866	7138618	9539833	10297853	14008313	14279868	33		
28	7004942	7136581	9535543	10295923	14012312	14275636	32		
29	7007018	7134543	9531256	10293997	14016315	14271407	31		
30	7009093	7132505	9526973	10292074	14020321	14267182	30		
N. Co-Sine.	N. Sine.	N. Co-Sine.	N. Tangent.	N. Co-Tang.	N. Co-Secant.	N. Secant.	M		

45 DEGREES.

A Table of the Latitude and Longitude

The Places Names.	North Latitud.	East Longit.	The Places Names.	North Latitud.	East Longit.
	D. M. D. M.			D. M. D. M.	
New Callabar	04 40	23 37	Cape Mounta	05 23	01 46
Cape Formoffus	04 03	22 52	Cape Roxo	11 38	06W 13
River Binnin	05 50	22 12	River of Gambo	12 47	02 17
River Dallagoa	07 40	19 49	Cape de Verd	14 24	06 57
River de Valta	06 05	16 52			
Cape 3 Points	04 10	13 10			
River St. Andr�s	05 23	08 06			
Cape de Palmas	04 40	06 05			
River de Cabo	05 20	03 48			

44 DEGREES.									
M	L. Sine.	L. Co-Sine.	L. Tangent.	L. Co-Tang.	L. Secant.	L. Co-Secant.			
0	9.8517713	9.8569341	9.9848372	10.0151628	10.1432659	10.1582287	60		
1	9.8419021	9.8568121	9.9850900	10.0149100	10.1431879	10.1580979	59		
2	9.8420328	9.8566900	9.9853428	10.0146572	10.1431100	10.1579672	58		
3	9.8421634	9.8565678	9.9855956	10.0144044	10.1430322	10.1578366	57		
4	9.8422939	9.8564455	9.9858484	10.0141516	10.1429545	10.1577061	56		
5	9.8424244	9.8563232	9.9861012	10.0138988	10.1428768	10.1575756	55		
6	9.8425548	9.8562008	9.9863540	10.0136460	10.1427992	10.1574452	54		
7	9.8426851	9.8560784	9.9866068	10.0133932	10.1427216	10.1573149	53		
8	9.8428154	9.8559558	9.9868596	10.0131404	10.1426442	10.1571846	52		
9	9.8429456	9.8558332	9.9871123	10.0128877	10.1425668	10.1570544	51		
10	9.8430757	9.8557106	9.9873651	10.0126349	10.1424894	10.1569243	50		
11	9.8432057	9.8555878	9.9876179	10.0123821	10.1424122	10.1567943	49		
12	9.8433356	9.8554650	9.9878706	10.0121294	10.1423350	10.1566641	48		
13	9.8434655	9.8553421	9.9881234	10.0118766	10.1422579	10.1565345	47		
14	9.8435953	9.8552192	9.9883761	10.0116239	10.1421805	10.1564047	46		
15	9.8437250	9.8550961	9.9886289	10.0113711	10.1421033	10.1562750	45		
16	9.8438547	9.8549730	9.9888816	10.0111184	10.1420260	10.1561453	44		
17	9.8439842	9.8548499	9.9891344	10.0108656	10.1419488	10.1560158	43		
18	9.8441137	9.8547265	9.9893871	10.0106129	10.1418714	10.1558863	42		
19	9.8442432	9.8546033	9.9896399	10.0103601	10.1417940	10.1557568	41		
20	9.8443725	9.8544799	9.9898926	10.0101074	10.1417166	10.1556273	40		
21	9.8445018	9.8543564	9.9901453	10.0098547	10.1416392	10.1554982	39		
22	9.8446310	9.8542329	9.9903981	10.0096019	10.1415618	10.1553690	38		
23	9.8447601	9.8541093	9.9906508	10.0093492	10.1414844	10.1552399	37		
24	9.8448891	9.8539856	9.9909035	10.0090965	10.1414070	10.1551109	36		
25	9.8450181	9.8538619	9.9911562	10.0088438	10.1413296	10.1549819	35		
26	9.8451470	9.8537381	9.9914089	10.0085911	10.1412522	10.1548530	34		
27	9.8452758	9.8536142	9.9916616	10.0083384	10.1411748	10.1547242	33		
28	9.8454045	9.8534902	9.9919143	10.0080857	10.1410974	10.1545955	32		
29	9.8455332	9.8533662	9.9921670	10.0078330	10.1410200	10.1544668	31		
30	9.8456618	9.8532421	9.9924197	10.0075803	10.1409426	10.1543382	30		
L. Co-Sine.	L. Sine.	L. Co-Sine.	L. Tangent.	L. Co-Tang.	L. Co-Secant.	L. Secant.	M		

45 DEGREES.



## 44 DEGREES.

M	N. Sine.	V. Co-Sine.	N. Tangent.	N. Co-Tang.	N. Secant.	N. Co-Secant.
30	7009993	7132505	9826973	10175074	14020321	14267182
31	7011167	7130466	9832692	10170155	14024330	14262961
32	7013241	7128426	9838415	10165239	14028343	14258743
33	7015314	7126385	9844141	10160325	14032360	14254529
34	7017387	7124344	9849871	10155417	14036380	14250319
35	7019459	7122302	9855603	10150512	14040403	14246112
36	7021530	7120260	9861339	10145610	14044430	14241909
37	7023601	7118217	9867079	10140712	14048460	14237710
38	7025671	7116174	9872821	10135817	14052494	14233514
39	7027741	7114130	9878567	10130925	14056532	14229323
40	7029810	7112086	9884316	10126037	14060573	14225134
41	7031879	7110041	9890069	10121153	14064617	14220950
42	7033947	7107995	9895825	10116272	14068665	14216769
43	7036014	7105948	9901584	10099394	14072717	14212592
44	7038081	7103901	9907346	10093320	14076772	14208418
45	7040147	7101854	9913112	10087649	14080831	14204248
46	7042213	7099806	9918881	10081982	14084893	14200082
47	7044278	7097757	9924654	10075918	14088958	14195919
48	7046342	7095707	9930429	10070058	14093028	14191761
49	7048406	7093657	9936208	10064201	14097100	14187605
50	7050469	7091607	9941991	10058347	14101177	14183454
51	7052532	7089556	9947777	10052497	14105256	14179305
52	7054594	7087504	9953566	10046651	14109340	14175161
53	7056655	7085451	9959358	10040807	14113427	14171020
54	7058716	7083398	9965154	10034968	14117517	14166883
55	7060776	7081345	9970953	10029131	14121611	14162749
56	7062835	7079291	9976756	10023298	14125709	14158619
57	7064894	7077236	9982562	10017469	14129810	14154493
58	7066953	7075180	9988371	10011642	14133915	14150370
59	7069011	7073124	9994184	10005819	14138024	14146251
60	7071068	7071068	10000000	10000000	14142136	14142136
N. Co-Sine.		N. Sine.	N. Co-Tang.	N. Tangent.	N. Co-Secant.	N. Secant.

## 45 DEGREES.

## 44 DEGREES.

M	L. Sine.	L. Co-Sine.	L. Tangent.	L. Co-Tang.	L. Secant.	L. Co-Secant.
30	9.8456618	9.8532421	9.9922197	10.0075803	10.1467579	10.1542382
31	9.8457903	9.8531179	9.9925724	10.0073276	10.1468821	10.1542097
32	9.8459188	9.8529936	9.9929251	10.0070749	10.1470064	10.1541812
33	9.8460471	9.8528693	9.9932778	10.0068222	10.1471307	10.1541527
34	9.8461754	9.8527449	9.9936305	10.0065695	10.1472551	10.1541242
35	9.8463036	9.8526204	9.9939832	10.0063168	10.1473795	10.1540957
36	9.8464318	9.8524959	9.9943359	10.0060641	10.1475041	10.1540672
37	9.8465599	9.8523713	9.9946886	10.0058114	10.1476287	10.1540387
38	9.8466879	9.8522466	9.9950413	10.0055587	10.1477534	10.1539902
39	9.8468158	9.8521213	9.9953940	10.0053060	10.1478782	10.1539617
40	9.8469436	9.8519970	9.9957466	10.0050533	10.1480030	10.1539332
41	9.8470714	9.8518721	9.9960993	10.0048006	10.1481279	10.1539047
42	9.8471991	9.8517471	9.9964520	10.0045479	10.1482529	10.1538762
43	9.8473267	9.8516220	9.9968047	10.0042953	10.1483780	10.1538477
44	9.8474543	9.8514969	9.9971573	10.0040427	10.1485031	10.1538192
45	9.8475817	9.8513717	9.9975100	10.0037900	10.1486283	10.1537907
46	9.8477091	9.8512465	9.9978627	10.0035373	10.1487535	10.1537622
47	9.8478365	9.8511211	9.9982154	10.0032846	10.1488789	10.1537337
48	9.8479637	9.8509957	9.9985681	10.0030320	10.1490043	10.1537052
49	9.8480909	9.8508702	9.9989207	10.0027793	10.1491298	10.1536767
50	9.8482180	9.8507446	9.9992734	10.0025266	10.1492554	10.1536482
51	9.8483450	9.8506190	9.9996260	10.0022740	10.1493810	10.1536197
52	9.8484720	9.8504933	9.9999787	10.0020213	10.1495067	10.1535912
53	9.8485989	9.8503675	9.998214	10.0017686	10.1496325	10.1535627
54	9.8487257	9.8502417	9.9985684	10.0015160	10.1497583	10.1535342
55	9.8488524	9.8501157	9.9989237	10.0012633	10.1498843	10.1535057
56	9.8489791	9.8500000	9.9992790	10.0010107	10.1500100	10.1534772
57	9.8491057	9.8498863	9.9996343	10.0007580	10.1501363	10.1534487
58	9.8492322	9.8497735	9.9999896	10.0005053	10.1502625	10.1534202
59	9.8493586	9.8496613	9.9999449	10.0002527	10.1503887	10.1533917
60	9.8494850	9.8495490	10.0000000	10.0000000	10.1505150	10.1533632
L. Co-Sine.		L. Sine.	L. Co-Tang.	L. Tangent.	L. Co-Secant.	L. Secant.

## 45 DEGREES.

The END of the TABLE of

Sines, Tangents, and Secants.



# TABLES of DECLINATION.

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## Suns Declination.

Anno 1681, 1685, 1689.

Days.	Jan.	Feb.	Mar.	April.	May.	June.	July.	Aug.	Sept.	Octob.	Nov.	Dec.
	South.	South.	South.	North.	North.	North.	North.	North.	North.	South.	South.	South.
	D. M.	D. M.	D. M.	D. M.	D. M.	D. M.	D. M.	D. M.	D. M.	D. M.	D. M.	D. M.
1	21 41	13 42	3 20	8 40	18 7	23 11	22 4	15 6	4 17	7 21	17 43	23 8
2	21 31	13 22	5 6	2 18	22 23	15 21	56 14	4 3	54 7	54 17	59 23	13
3	21 21	13 2	8 2	9 23	18 37	23 18	21 47	14 30	3 18	6 18	15 23	16
4	21 10	12 41	9 9	45 18	51 23	21 21	38 14	11 3	8 8	29 18	31 23	20
5	20 58	12 21	11 45	10 6	19 6	23 24	21 28	13 52	2 45	8 51	18 46	23 23
6	20 47	11 59	1 21	10 27	19 19	23 26	21 18	13 33	2 21	9 13	19 1	23 25
7	20 34	11 38	0 59	10 48	19 33	23 27	21 8	13 14	1 58	9 35	19 16	23 27
8	20 22	11 17	0 34	11 9	19 46	23 29	20 58	12 54	1 35	9 56	19 30	23 28
9	20 9	10 56	0 10	11 30	19 59	23 30	20 47	12 35	1 11	10 19	19 44	23 29
10	19 56	10 34	Nov. 13	11 50	20 11	23 30	20 35	12 15	0 48	10 40	19 57	23 30
11	19 42	10 12	0 37	12 11	20 23	23 30	20 24	11 55	0 24	11 22	10 23	30
12	19 28	9 50	1 01	12 31	20 35	23 30	20 12	11 35	0 01	11 23	20 23	30
13	19 14	9 28	1 24	12 50	20 46	23 29	19 59	11 14	Nov. 22	11 44	20 36	23 29
14	18 59	9 6	1 48	13 10	20 57	23 27	19 47	10 53	0 46	12 52	20 48	23 27
15	18 44	8 43	2 11	13 30	21 8	23 26	19 34	10 35	1 0	12 26	20 59	23 25
16	18 29	8 21	2 35	13 49	21 18	23 24	19 20	10 12	1 33	12 46	21 11	23 23
17	18 13	7 58	2 58	14 8	21 28	23 21	19 7	9 51	1 56	13 7	21 21	23 20
18	17 57	7 36	3 22	14 27	21 38	23 18	53 9	29 2	2 20	13 27	21 32	23 17
19	17 41	7 13	3 45	14 45	21 47	23 15	18 38	0 72	44 13	47 21	42 23	13
20	17 24	6 50	4 8	15 3	21 56	23 11	18 24	8 46	3 14	47 51	42 9	
21	17 7	6 27	4 31	15 21	22 4	23 7	18 9	8 24	3 30	14 26	22 1	4
22	16 50	6 4	5 4	15 39	22 12	23 3	17 54	8 23	4 54	14 45	22 9	22 59
23	16 32	5 40	5 17	15 57	22 20	22 58	17 38	7 40	5 17	15 42	22 18	22 54
24	16 14	5 17	4 40	16 14	22 27	22 53	17 22	7 18	4 40	15 23	22 26	22 48
25	15 56	4 54	6 13	16 31	22 34	22 47	17 6	6 56	3 15	41 22	33 22	41
26	15 38	4 30	6 26	16 48	22 41	22 41	16 50	6 34	2 16	40 22	40 22	34
27	15 20	4 7	6 49	17 4	22 47	22 34	16 33	6 11	5 50	16 18	22 47	22 27
28	15 03	43 7	7 11	17 21	22 53	22 27	16 16	5 48	6 12	16 35	22 53	22 19
29	14 41		7 33	17 37	22 58	22 20	15 59	5 26	6 16	16 53	22 58	22 14
30	14 22		7 56	17 52	23 3	22 12	15 43	5 36	6 17	10 23		22 2
31	14 2		8 18		23 7		15 24	40		17 27		21 53

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## TABLES of DECLINATION.

## Suns Declination.

Anno 1682, 1686, 1690.

Jan.	Feb.	Mar.	April.	May.	June.	July.	Aug.	Sept.	Octob.	Nov.	Dec.
South.	South.	South.	North.	North.	North.	North.	North.	North.	South.	South.	South.
D. M.	D. M.	D. M.	D. M.	D. M.	D. M.	D. M.	D. M.	D. M.	D. M.	D. M.	D. M.
1 21 45	13 47 3	26 8	34 18	4 23 11	22 6	15 11 4	23 7	15 17 39	23 7		
2 21 34	13 27 3	02 8	56 18	19 23 14	21 58	14 53 4	07 38	17 55	23 12		
3 21 23	13 7 2	38 9	18 18	34 23 18	21 49	14 34 3	3 8	1 18 12	23 15		
4 21 12	12 46 2	15 9	40 18	48 23 21	21 40	14 16 3	14 3	23 18 27	23 19		
5 21 1	12 25 1	5 11 10	01 19	22 23 23	21 31	13 57 2	50 3	46 18 42	23 22		
6 20 49	12 5 1	27 10	22 19	16 23 25	21 21	13 38 2	27 9	8 18 58	23 24		
7 20 37	14 43 1	03 10	43 19	29 23 27	21 11	13 19 2	04 9	30 19 12	23 27		
8 20 25	11 22 0	40 11	4 19	43 23 28	21 0	12 59 1	40 9	52 19 26	23 28		
9 20 12	11 0 0	16 11	25 19	55 23 28	20 49	12 39 1	17 10	13 19 40	23 29		
10 19 59	10 38	Nov. 4	11 45 20	8 23 30	3 12	12 20 0	53 10	35 19 54	23 30		
11 16 49	10 17 0	31 12	6 20 25	3 30 20	27 12	0 30	10 57	10 7 23	30		
12 19 32	9 55 0	55 12	26 20	3 13 30	20 14	11 40 0	7 11	18 20 20	23 30		
13 19 18	9 33 1	19 12	46 20	44 23 29	20 2	11 19	17 11	39 20 33	23 29		
14 19 3	9 11 1	42 13	5 20	55 23 28	19 50	10 58 0	40 12	0 20 45	23 28		
15 18 48	8 49 2	05 13	25 21	5 23 26	19 37	10 38 1	04 12	21 20 57	23 26		
16 18 33	8 26 2	29 13	44 21	16 23 24	19 23	10 17 1	27 12	41 21 8	23 24		
17 18 17	8 4 2	33 14	3 21	26 23 22	19 10	9 56 1	5 13	2 21 19	23 21		
18 18 1	7 41 3	16 14	22 21	36 23 19	18 56	9 34 2	14 13	22 21 29	23 18		
19 17 45	7 18 3	39 14	41 21	45 23 16	18 42	9 13 2	38 13	42 21 39	23 14		
20 17 28	6 55 4	03 14	59 21	54 23 12	18 27	8 51 3	01 14	2 21 49	23 10		
21 17 11	6 32 4	26 15	17 22	2 13 8	18 12	8 29 3	25 14	21 21 58	23 6		
22 16 54	6 9 4	49 15	25 21	10 23 4	17 57	8 8 3	48 14	41 22 7	23 1		
23 16 37	5 46 5	12 15	35 22	18 22 59	17 42	7 46 4	11 15	0 22 16	22 55		
24 16 19	5 23 5	35 16	10 22	26 22 54	17 26	7 24 4	34 15	18 22 24	22 49		
25 16 1	5 0 5	58 16	2 22	33 22 48	17 10	7 01 4	58 15	37 22 31	22 43		
26 15 42	4 36 6	21 16	44 22	39 22 42	16 54	6 39 5	21 15	55 22 38	22 36		
27 15 24	4 12 6	47 17	0 22	45 22 36	16 37	6 17 5	44 16	13 12 45	22 29		
28 15 5	3 48 7	8 17	17 22	51 22 29	16 21	5 56 6	7 16	31 22 51	22 21		
29 14 46	3 27 7	17 17	33 22	57 22 22	16 3	5 31 6	30 17	39 22 57	22 13		
30 14 27	3 7 7	50 17	48 23	2 22 14	15 46	5 8 6	53 17	6 23	22 4		
31 14	2 8	12 12	23 6	15 28	14 46	4 17 23	21 58				

## TABLES of DECLINATION.

## Suns Declination.

Anno 1683, 1687, 1691.

Jan.	Feb.	Mar.	April.	May.	June.	July.	Aug.	Sept.	Octob.	Nov.	Dec.
South.	South.	South.	North.	North.	North.	North.	North.	North.	South.	South.	South.
D. M.	D. M.	D. M.	D. M.	D. M.	D. M.	D. M.	D. M.	D. M.	D. M.	D. M.	D. M.
1 21 46	13 52 3	31 8	25 18	0 23 10	22 8	15 15 4	28 7	10 17 35	23 6		
2 21 36	13 32 3	8 8	51 18	15 23 13	22 0	14 57 4	5 7	33 17 52	23 11		
3 21 26	13 12 2	44 9	13 18	30 23 17	21 51	14 39 3	42 7	55 18	23 15		
4 21 15	12 51 2	20 9	34 18	44 23 20	21 43	14 20 3	19 8	18 18 23	23 18		
5 21 04	12 31 1	57 9	56 18	59 23 23	21 33	14 01 2	56 8	40 18 39	23 21		
6 20 52	12 10 1	33 10	17 19	13 23 25	21 23	13 43 1	33 9	2 18 54	23 24		
7 20 40	11 49 1	9 10	38 19	26 23 27	21 13	13 23 2	9 9	24 19 9	23 26		
8 20 28	11 28 0	45 10	59 19	40 23 28	21 3	13 4 1	46 9	47 19 23	23 28		
9 20 15	11 6 0	22 11	20 19	52 23 29	20 52	12 44 1	23 10	8 19 37	23 29		
10 20 2	10 44	No. 02	11 40	20 5	23 30	20 41	12 24 0	59 10	30 19 51	23 30	
11 19 49	10 23 0	26 12	12 20	17 23 30	20 29	12 5 0	36 10	51 20 43	30		
12 19 35	10 1 0	49 12	21 20	29 23 30	20 18	11 44 0	12 11	13 20 17	23 30		
13 19 21	9 39 1	13 12	41 20	41 23 29	20 5	11 24	11 11	34 20 30	23 29		
14 19 7	9 17 1	36 13	0 20	52 23 28	19 53	11 3 0	35 11	55 20 42	23 28		
15 18 52	8 54 2	00 13	20 21	03 23 27	19 40	10 43 0	58 12	16 20 54	23 26		
16 18 36	8 32 2	23 13	40 21	13 23 25	19 27	10 22 1	22 12	56 21 52	23 24		
17 18 21	8 9 2	47 13	50 21	24 23 22	19 13	10 45 1	45 12	57 21 16	23 22		
18 18 5	7 46 3	10 14	18 21	33 23 20	19 0	9 40 2	9 13	17 21 27	23 19		
19 17 45	7 23 3	34 14	36 21	43 23 17	18 45	9 18 2	32 13	37 21 37	23 15		
20 17 32	7 01 3	57 14	55 21	52 23 13	18 31	8 56 2	55 13	57 21 47	23 11		
21 17 15	6 38 1	20 15	15 22	02 23 9	18 16	8 35 3	19 14	17 21 56	23 7		
22 16 58	6 14 4	43 15	31 22	8 23 5	18 1	8 13 3	42 14	36 22 52	22		
23 16 41	5 52 5	06 15	48 22	16 23 0	17 46	7 51 4	6 14	55 22 14	22 57		
24 16 23	5 28 5	29 16	6 22	24 22 55	17 30	7 29 4	29 15	14 22 22	22 51		
25 16 5	5 5 5	52 16	22 22	31 22 5	17 14	7 7 4	52 15	32 22 22	22 44		
26 15 47	4 42 6	15 16	40 22	38 22 44	16 58	6 44 5	15 5	51 22 37	22 38		
27 15 28	4 18 6	37 16	56 22	44 22 37	16 42	6 22 5	38 16	52 22 43	22 31		
28 15 10	3 55 7	07 17	12 22	50 22 31	16 25	5 59 6	2 16	22 50	22 23		
29 14 50	3 28 7	22 17	20 22	55 22 24	16 8	5 37 6	24 16	44 22 56	22 15		
30 14 31	3 7 7	45 17	44 23	0 22 16	15 50	5 14 6	47 17	23 12	22 6		
31 14 12	2 8 0	07 18	12 23	15 33 4	15 33 4	5 17 10	21 58				



## Suns Declination.

Anno 1684, 1688, 1692.

Days.	Jan.	Feb.	Mar.	April.	May.	June.	July.	Aug.	Sept.	Octob.	Nov.	Dec.
	South.	South.	South.	North.	North.	North.	North.	North.	North.	South.	South.	South.
	D. M.	D. M.	D. M.	D. M.	D. M.	D. M.	D. M.	D. M.	D. M.	D. M.	D. M.	D. M.
1	21 48	13 57	13 8	46 18	0 23	12 22	21 15	14 11	7 27	17 48	23 9	
2	21 38	13 37	2 50	7 18	27 23	16 21	54 14	43 3	48 7	50 18	4 23	14
3	21 28	13 17	2 69	29 18	41 23	19 21	45 14	21 3	25 8	12 18	20 23	17
4	21 18	12 56	2 9	51 18	55 13	22 21	35 14	63 2	28 35	18 35	23 21	
5	21 7	12 36	39 10	12 19	9 23	24 21	26 13	47 2	38 57	18 50	23 23	
6	20 55	12 15	1 15	10 33	19 23	23 26	21 16	13 28	2 15	9 18	19 53	26
7	20 43	11 54	0 51	10 54	19 36	23 28	21 5	13 9	1 52	9 41	19 20	23
8	20 31	11 32	0 28	11 15	19 45	23 29	20 55	12 49	1 28	10 31	19 34	23
9	20 19	11 11	0 4	11 35	20 23	30 20	44 12	29 1	5 10	25 19	47 23	30
10	20 7	10 50	No. 20	11 56	20 14	23 30	20 32	12 10	0 41	10 46	20 01	23
11	19 52	10 28	0 43	12 16	20 27	13 30	20 21	11 49	0 18	11 8	20 14	23
12	19 38	10 6	0 7	12 36	20 38	13 29	0 08	11 29	0 6	11 29	20 27	23
13	19 24	9 44	1 30	12 56	20 49	23 28	19 56	11 8	0 29	11 50	20 39	23
14	19 10	9 22	1 54	13 15	21 03	27 19	43 10	48 0	53 12	11 20	51 23	27
15	18 55	9 00	2 18	13 35	21 11	23 25	19 35	10 27	1 16	12 32	21 23	25
16	18 40	8 37	2 41	13 54	21 21	23 23	19 17	10 6	1 40	12 52	21 13	23
17	18 24	8 15	3 05	14 13	21 31	23 10	19 03	9 45	2 3	13 12	21 24	23
18	18 9	7 52	3 26	14 32	21 40	23 17	18 45	9 23	2 27	13 32	21 35	23
19	17 53	7 29	3 51	14 50	21 49	23 14	18 34	9 22	3 5	13 52	21 44	23
20	17 36	7 7	4 15	15 8	21 58	23 10	18 20	8 45	3 13	14 12	21 54	23
21	17 20	6 44	4 38	15 26	22 7	23 6	18 05	8 18	3 37	14 31	22 3	23
22	17 2	6 21	5 01	15 44	22 14	23 1	17 50	7 56	4 0	14 50	22 12	22
23	16 45	5 57	5 24	16 2	22 22	22 56	17 34	7 34	4 23	15 9	22 20	22
24	16 27	5 34	5 47	16 19	22 29	22 51	17 18	7 12	4 15	28 22	28 22	46
25	16 10	5 11	6 1	16 36	22 36	22 45	17 02	6 50	5 16	15 47	22 35	22
26	15 51	4 47	6 32	16 52	22 43	22 39	16 46	5 27	5 33	16 5	22 42	22
27	15 33	4 24	6 55	17 9	22 49	22 32	16 29	6 5	5 56	16 23	22 48	22
28	15 14	4 1	7 17	17 25	22 54	22 25	16 12	5 42	6 19	16 40	22 54	22
29	14 55	3 37	7 38	17 41	22 59	22 18	15 55	5 20	6 42	16 58	23 02	22
30	14 36	3 14	7 59	17 56	23 04	22 10	15 37	4 57	7 05	17 15	23 52	22
31	14 16	2 51	8 20	18 11	23 09	22 1	15 20	4 34	7 17	17 31	24 01	21

A Table, whereby you may proportion the Suns Declination to any other Meridian.

The daily Diff. in Declination. 03|06|09|12|15|18|21|24

Deg.	15	0	0	0	0	0	1	1	1
	30	0	0	0	1	1	1	2	2
	45	0	0	1	1	2	2	3	3
	60	0	1	1	2	2	3	3	4
Degrees of	75	0	1	2	2	3	4	4	5
Longitude	90	0	1	2	3	4	4	5	6
either East,	105	1	2	2	3	4	5	6	7
or West.	120	1	2	3	4	5	6	7	8
	135	1	2	3	4	5	7	8	9
	150	1	2	3	5	6	8	9	10
	165	1	2	4	5	6	8	10	11
	180	1	3	4	6	7	9	11	12

The Refraction of the Stars.

Alt.	Refract.
0	30 00
1	25 12
2	18 24
3	14 00
4	11 0
5	9 30
6	7 30
7	6 30
8	5 45
9	5 0
10	4 30
11	4 0
12	4 00
13	3 30
14	3 00
15	3 0
16	3 00
17	2 30
18	2 30
19	2 00
20	2 00
21	2 0
22	2 0
23	2 0
24	1 30
25	1 30
26	1 30
27	1 30
28	1 30
29	1 00
30	1 00



A Table of the Suns RIGHT ASCENSION.

Days.	Jan.	Feb.	Mar.	April.	May.	June.	July.	Aug.	Sept.	Octob.	Nov.	Dec.
	Alcen.	Alcen.	Alcen.	Alcen.	Alcen.	Alcen.	Alcen.	Alcen.	Alcen.	Alcen.	Alcen.	Alcen.
	H. M.	H. M.	H. M.	H. M.	H. M.	H. M.	H. M.	H. M.	H. M.	H. M.	H. M.	H. M.
1	19 35	21 43	23 28	1 21 3	14 5	26 7	24 9	26 11	19 13	08 15	08 17	16
2	19 38	21 46	23 32	1 25 3	18 5	24 7	28 9	29 11	23 13	12 15	12 17	21
3	19 43	21 50	23 36	1 29 3	22 5	28 7	33 9	33 11	26 13	16 15	16 17	25
4	19 47	21 54	23 39	1 33 3	26 5	32 7	36 9	37 11	30 13	19 15	21 17	30
5	19 51	21 59	23 43	1 36 3	30 5	36 7	40 9	41 11	34 13	23 15	25 17	34
6	19 56	22 02	23 47	1 40 3	34 5	40 7	44 9	44 11	38 13	27 15	29 17	38
7	20 00	22 06	23 51	1 43 3	38 5	44 7	48 9	48 11	41 13	31 15	33 17	43
8	20 05	22 11	23 54	1 47 3	42 5	49 7	52 9	52 11	45 13	34 15	37 17	47
9	20 09	22 14	23 58	1 51 3	46 5	53 7	56 9	56 11	48 13	38 15	41 17	52
10	20 13	22 17	01 01	1 54 3	50 5	57 8	00 9	59 11	52 13	42 15	45 17	56
11	20 17	22 21	00 05	1 58 3	54 5	01 8	04 10	03 11	55 13	46 15	50 18	01
12	20 21	22 25	00 09	2 02 3	58 5	05 8	08 10	07 11	59 13	49 15	54 18	05
13	20 25	22 29	00 12	2 06 3	02 6	09 8	12 10	10 11	03 13	53 15	58 18	10
14	20 30	22 33	00 16	2 09 3	06 6	13 8	16 10	14 11	06 13	57 15	02 18	14
15	20 34	22 36	00 19	2 13 3	10 6	17 8	20 10	18 11	10 13	01 15	06 18	18
16	20 38	22 40	00 23	2 17 3	14 6	21 8	24 10	22 11	14 13	05 15	11 18	22
17	20 42	22 44	00 27	2 21 3	18 6	25 8	28 10	26 11	18 13	09 15	15 18	27
18	20 46	22 48	00 30	2 24 3	22 6	30 8	32 10	29 11	21 13	13 15	19 18	32
19	20 50	22 51	00 34	2 28 3	26 6	34 8	36 10	33 11	24 13	16 15	24 18	36
20	20 54	22 55	00 38	2 32 3	30 6	38 8	40 10	36 11	28 13	20 15	28 18	41
21	20 59	22 59	00 41	2 36 3	34 6	42 8	43 10	40 11	31 13	24 15	32 18	45
22	21 03	23 03	00 45	2 40 3	38 6	46 8	47 10	43 11	35 13	28 15	36 18	49
23	21 07	23 06	00 48	2 44 3	43 6	51 8	51 10	47 11	39 13	32 15	41 18	54
24	21 11	23 10	00 52	2 47 3	47 6	55 8	55 10	51 11	43 13	36 15	45 18	58
25	21 15	23 14	00 56	2 51 3	51 6	59 8	59 10	54 11	46 13	40 15	50 19	03
26	21 19	23 17	00 59	2 55 3	55 6	03 8	03 10	58 11	50 13	44 15	54 19	07
27	21 23	23 21	01 03	2 59 3	59 6	07 8	06 10	02 11	54 13	48 15	59 19	11
28	21 27	23 25	01 06	3 03 3	03 6	07 8	07 10	01 11	05 13	52 15	03 19	16
29	21 31		01 10	3 07 3	07 6	07 8	15 9	14 11	09 13	01 15	07 19	20
30	21 35		01 14	3 10 3	11 6	11 8	20 9	18 11	12 13	05 15	12 19	24
31	21 39		01 17		15 6		22 11	16 11		09 15		28

A Table of the Right Ascensions, and Declinations of the fixed Stars, For the Year 1700. with their Differences in 100.

Name.	The Names of the Stars.	Right Ascen.	Declinations.	Diff. Rig.	Diff. Dec.	Name.	The Names of the Stars.	Right Ascen.	Declinations.	Diff. Rig.	Diff. Dec.
		H. M.	D. M.					H. M.	D. M.	M	M
3	In Cassiopei's breast.	0 24	54 55	6	34	21	In Orions girdle.	5 17	0 32	5	7
2	The Pole Star.	0 39	87 43	16	34	3	The Bulls South horn.	5 20	20 58	6	7
	most in the Whales Tail.	0 29	19 38	5	34	22	In Orions girdle.	5 21	01 24	5	6
2	Andromeda's girdle.	0 53	34 05	5	33	23	In Orions girdle.	5 26	02 07	5	5
3	Cassiopei's knee.	1 07	58 40	6	33	2	The right shoulder Auriga.	5 38	44 54	8	4
3	The Whales belly.	1 37	11 45	5	31	2	The bright foot of $\pi$ .	6 20	16 38	6	2
2	The South foot of Andromeda.	1 46	40 53	6	30	1	The great Dog Sirius.	6 32	16 15	5	4
3	The bright Star of $\gamma$ .	1 51	22 03	6	30	2	The upper head of $\pi$ .	7 16	32 30	7	11
2	In the Whales chap.	2 47	02 54	5	25	2	The lesser Dog, Procyon.	7 24	6 0	5	12
3	Medusa's head.	2 49	39 47	6	25	2	The lower head of $\pi$ .	7 31	28 43	6	12
2	Perseus bright side.	3 02	48 43	6	21	1	Hydra's heart.	9 13	7 22	5	25
3	The brightest of the Pleiades.	3 30	23 10	6	21	1	The Lions heart, Regulus.	9 53	13 25	5	28
3	The North eye of $\gamma$ .	4 11	18 31	6	17	2	The middle most in the Lions neck.	10 00	21 21	6	29
1	Aldebaran, or the South eye of $\gamma$ .	4 19	15 53	6	15	1	The Lions Tail.	11 24	16 15	5	34
1	The Goat Capella.	4 55	45 40	7	10	2	The Root of the Great Bears Tail.	12 41	57 37	5	33
1	The bright foot of Orion, Regulus.	5 01	8 33	5	9	1	Virgins spike.	13 10	09 33	5	32
1	The North horn of $\gamma$ .	5 08	28 20	6	8	2	The last but one in the Great Bears Tail.	13 12	56 31	4	32
2	Orion's left shoulder.	5 06	16 03	5	8						



Mag.	The Names of the Stars.	Right Ascensions.		Declinations.		Diff. Rig.	Diff. Dec.	Mag.	The Names of the Stars.	Right Ascensions.		Declinations.		Diff. Rig.	Diff. Dec.
		H. M.	D. M.	H. M.	D. M.					H. M.	D. M.	H. M.	D. M.		
2	The last in the Great Bears Tail—	13 36	50 51	4 31				1	Lyra—	18 27	38 32	3 4			
1	Arcturus—	14 02	20 49	5 29½				3	The Vulturs Tail—	18 52	23 28	5 8			
2	The South Ballance—	14 34	14 45½	5 27				3	The Swans beak—	19 19	27 21	4 11			
2	The North Ballance—	15 01	8 14½	5 24				2	The bright Star of the Vulture—	19 36	8 07	5 13			
2	Bright Star of the Crown—	15 22	27 45	4 21				3	The upper horn of ♄—	20 01	13 24½	6 16			
2	The bright * in the Serpents Neck—	15 30	7 25	5 21				3	The lower horn of ♄—	20 04	15 40½	6 17			
3	The left hand of Ophiuchus—	15 59	2 55½	5 18				3	The Swans breast—	20 12	39 19	4 18			
1	Scorpions hart Antares—	16 11	25 42½	6 16				4	The left hand of Aquarius—	20 31	10 34½	5 19			
3	Hercules right shoulder—	16 17	22 12	4 15				2	The Swans tail—	20 31	44 14	3 20½			
3	The left knee of Ophiuchus—	16 21	9 54½	5 15				3	The Swans lower wing—	20 34	32 51	4 21			
3	The right knee of Ophiuchus—	16 51	15 17½	3 10				3	The left shoulder of Aquarius—	21 16	6 49½	4 26			
3	Hercules his head—	17 01	14 47	4 8				3	The Girdle of Capheus—	21 25	69 16	1 26			
3	Hercules left shoulder—	17 02	25 14	4 8				3	Pegasus mouth—	21 30	8 31	5 26			
3	The head of Ophiuchus—	17 21	12 49	5 7				3	The right shoulder of Aquary—	21 51	1 44½	5 29			
3	The right shoulder of Ophiuchus—	17 29	4 44	5 5				1	Fomalhaut—	22 41	31 08½	6 31			
3	The bright star in the Dragons head—	17 50	51 35	2 2				2	Scheat—	22 49	26 28	5 32			
								2	Marchab—	22 50	13 37	5 32			
									Andromeda's head—	23 53	27 28	5 34			

If the Right Ascension be less than 6 hours or more than 18 hours, the Declinations of those Stars that are to the North of the Equinoctial must be increased by the Difference for time to come; and the Southern Stars Declinations decreased: but in the other Hemisphere where the Right Ascension is more than 6 hours, or less than 18 hours, the contrary.



A  
TABLE  
OF  
VERSED SINES  
BOTH  
NATURAL and ARTIFICIAL.



00 DEGREES.					
M.	Natural Versed Sine.	Natural Co. Versed Sine.	Logarithm Versed Sine.	Logarithm Co. Versed Sine.	
0	0	10000000	0.0000000	10.0000000	60
1	1	9997091	2.6264222	9.9998736	59
2	2	9994182	3.2284822	9.9997473	58
3	4	9991273	3.5806647	9.9996208	57
4	7	9988364	5.8305422	9.9994944	56
5	11	9985456	4.0243620	9.9993679	55
6	16	9982547	4.1827246	9.9992414	54
7	22	9979638	4.3166182	9.9991148	53
8	28	9976729	4.4326020	9.9989882	52
9	35	9973820	4.5349070	9.9988615	51
10	43	9970912	4.6264219	9.9987348	50
11	52	9968003	4.7092072	9.9986081	49
12	62	9965094	4.7847843	9.9984814	48
13	73	9962185	4.8543084	9.9983546	47
14	84	9959276	4.9186777	9.9982278	46
15	96	9956368	4.9786040	9.9981009	45
16	109	9953459	5.0346614	9.9979740	44
17	123	9950550	5.0873192	9.9978470	43
18	138	9947641	5.1369663	9.9977201	42
19	154	9944732	5.1839282	9.9975930	41
20	170	9941823	5.2284810	9.9974660	40
21	187	9938914	5.2708594	9.9973389	39
22	205	9936005	5.3112661	9.9972118	38
23	224	9933096	5.3498762	9.9970846	37
24	244	9930187	5.3868430	9.9969574	36
25	265	9927279	5.4223002	9.9968302	35
26	287	9924370	5.4563669	9.9967029	34
27	309	9921461	5.4891474	9.9965756	33
28	332	9918552	5.5207359	9.9964483	32
29	356	9915643	5.5512156	9.9963209	31
30	381	9912735	5.5806620	9.9961935	30
	Natural Co. Versed Sine.	Natural Versed Sine.	Logarithm Co. Versed Sine.	Logarithm Versed Sine.	M.

89 DEGREES.

00 DEGREES.					
M.	Natural Versed Sine.	Natural Co. Versed Sine.	Logarithm Versed Sine.	Logarithm Co. Versed Sine.	
30	381	9912735	5.5806620	9.9961935	30
31	407	9909826	5.6091426	9.9960660	29
32	434	9906917	5.6367191	9.9959385	28
33	461	9904008	5.6634468	9.9958110	27
34	489	9901099	5.6893765	9.9956834	26
35	518	9898191	5.7145546	9.9955558	25
36	548	9895282	5.7390233	9.9954282	24
37	579	9892373	5.7628214	9.9953005	23
38	611	9889464	5.7859850	9.9951728	22
39	644	9886555	5.8085468	9.9950450	21
40	677	9883647	5.8305373	9.9949172	20
41	711	9880738	5.8519848	9.9947894	19
42	746	9877829	5.8729154	9.9946615	18
43	782	9874921	5.8933534	9.9945336	17
44	819	9872012	5.9133217	9.9944057	16
45	857	9869104	5.9328412	9.9942777	15
46	896	9866195	5.9519314	9.9941497	14
47	935	9863286	5.9706112	9.9940216	13
48	975	9860378	5.9888977	9.9938936	12
49	1016	9857469	6.0068070	9.9937654	11
50	1058	9854561	6.0243546	9.9936373	10
51	1101	9851652	6.0415546	9.9935091	9
52	1145	9848743	6.0584206	9.9933808	8
53	1189	9845835	6.0749654	9.9932526	7
54	1234	9842926	6.0912008	9.9931243	6
55	1280	9840018	6.1071384	9.9929959	5
56	1327	9837109	6.1227887	9.9928675	4
57	1375	9834201	6.1381620	9.9927391	3
58	1424	9831292	6.1532679	9.9926106	2
59	1473	9828384	6.1681156	9.9924821	1
60	1523	9825476	6.1827137	9.9923536	0
	Natural Co. Versed Sine.	Natural Versed Sine.	Logarithm Co. Versed Sine.	Logarithm Versed Sine.	M.

89 DEGREES.

L12



1 DEGREE.					
M.	Natural Versed Sine.	Natural Co-Versed Sine.	Logarithm Versed Sine.	Logarithm Co-Versed Sine.	
0	1523	9825476	6.1827137	9.9923536	60
1	1574	9822567	6.1970707	9.9922250	59
2	1626	9819659	6.2111938	9.9920964	58
3	1679	9816750	6.2250913	9.9919677	57
4	1733	9813842	6.2387696	9.9918391	56
5	1788	9810934	6.2522361	9.9917103	55
6	1843	9808025	6.2654968	9.9915816	54
7	1899	9805117	6.2785581	9.9914528	53
8	1956	9802208	6.2914259	9.9913240	52
9	2014	9799300	6.3041058	9.9911951	51
10	2073	9796392	6.3166033	9.9910662	50
11	2133	9793483	6.3289234	9.9909372	49
12	2194	9790575	6.3410714	9.9908082	48
13	2255	9787667	6.3530516	9.9906792	47
14	2317	9784759	6.3648689	9.9905501	46
15	2380	9781851	6.3765275	9.9904210	45
16	2444	9778943	6.3880317	9.9902919	44
17	2509	9776035	6.3993855	9.9901627	43
18	2575	9773127	6.4105928	9.9900335	42
19	2641	9770219	6.4216574	9.9899043	41
20	2708	9767311	6.4325826	9.9897750	40
21	2776	9764403	6.4433603	9.9896456	39
22	2845	9761495	6.4540294	9.9895163	38
23	2915	9758587	6.4645573	9.9893869	37
24	2986	9755679	6.4749592	9.9892575	36
25	3057	9752771	6.4852380	9.9891280	35
26	3129	9749863	6.4953965	9.9889985	34
27	3202	9746955	6.5054376	9.9888689	33
28	3276	9744047	6.5153639	9.9887393	32
29	3351	9741139	6.5251780	9.9886097	31
30	3427	9738231	6.5348825	9.9884801	30
Natural Co-Versed Sine. Natural Co-Versed Sine. Logarithm Co-Versed Sine. Logarithm Co-Versed Sine.					M.
88 DEGREES.					

1 DEGREE.					
M.	Natural Versed Sine.	Natural Co-Versed Sine.	Logarithm Versed Sine.	Logarithm Co-Versed Sine.	
30	3427	9738231	6.5348825	9.9884801	30
31	3504	9735323	6.5444797	9.9883503	29
32	3581	9732415	6.5539720	9.9882206	28
33	3659	9729507	6.5633617	9.9880908	27
34	3738	9726599	6.5726509	9.9879610	26
35	3818	9723692	6.5818418	9.9878311	25
36	3899	9720784	6.5909365	9.9877013	24
37	3981	9717876	6.5999368	9.9875713	23
38	4063	9714968	6.6088450	9.9874414	22
39	4146	9712060	6.6176626	9.9873114	21
40	4230	9709153	6.6263916	9.9871813	20
41	4315	9706245	6.6350337	9.9870512	19
42	4401	9703337	6.6435907	9.9869211	18
43	4488	9700430	6.6520642	9.9867910	17
44	4576	9697522	6.6604558	9.9866608	16
45	4664	9694615	6.6687671	9.9865305	15
46	4753	9691707	6.6769996	9.9864003	14
47	4843	9688800	6.6851548	9.9862700	13
48	4934	9685892	6.6932340	9.9861396	12
49	5026	9682985	6.7012388	9.9860092	11
50	5119	9680079	6.7091706	9.9858788	10
51	5213	9677170	6.7170304	9.9857484	9
52	5307	9674263	6.7248199	9.9856179	8
53	5402	9671355	6.7325400	9.9854873	7
54	5498	9668448	6.7401921	9.9853568	6
55	5595	9665541	6.7477774	9.9852261	5
56	5693	9662633	6.7552970	9.9850955	4
57	5792	9659726	6.7627520	9.9849648	3
58	5891	9656819	6.7701436	9.9848341	2
59	5991	9653912	6.7774728	9.9847033	1
60	6092	9651005	6.7847406	9.9845725	0
Natural Co-Versed Sine. Natural Co-Versed Sine. Logarithm Co-Versed Sine. Logarithm Co-Versed Sine.					M.
88 DEGREES.					



2 DEGREES.					
M.	Natural Versed Sine.	Natural Co-Versed Sine.	Logarithm Versed Sine.	Logarithm Co-Versed Sine.	
0	6092	9651005	6.7847406	9.9845725	60
1	6194	9648098	6.7919482	9.9844417	59
2	6296	9645191	6.7990963	9.9843108	58
3	6400	9642284	6.8061860	9.9841799	57
4	6505	9639337	6.8132185	9.9840490	56
5	6610	9636470	6.8201944	9.9839179	55
6	6716	9633563	6.8271147	9.9837869	54
7	6823	9630656	6.8339812	9.9836559	53
8	6931	9627749	6.8407920	9.9835248	52
9	7040	9624842	6.8475506	9.9833936	51
10	7150	9621936	6.8542572	9.9832624	50
11	7260	9619029	6.8609122	9.9831312	49
12	7371	9616122	6.8675167	9.9830000	48
13	7483	9613215	6.8740712	9.9828686	47
14	7596	9610308	6.8805768	9.9827373	46
15	7710	9607402	6.8870338	9.9826059	45
16	7825	9604495	6.8934434	9.9824745	44
17	7940	9601588	6.8998058	9.9823431	43
18	8056	9598682	6.9061221	9.9822116	42
19	8173	9595775	6.9123926	9.9820801	41
20	8291	9592869	6.9186183	9.9819485	40
21	8410	9589962	6.9248004	9.9818169	39
22	8530	9587056	6.9309372	9.9816853	38
23	8651	9584149	6.9370316	9.9815536	37
24	8772	9581243	6.9430837	9.9814219	36
25	8894	9578337	6.9490938	9.9812901	35
26	9017	9575430	6.9550627	9.9811583	34
27	9141	9572524	6.9609886	9.9810265	33
28	9266	9569618	6.9668786	9.9808946	32
29	9392	9566712	6.9727272	9.9807627	31
30	9518	9563806	6.9785359	9.9806308	30
	Natural Co-Versed Sine.	Natural Versed Sine.	Logarithm Co-Versed Sine.	Logarithm Versed Sine.	M.

87 DEGREES.

2 DEGREES.					
M.	Natural Versed Sine.	Natural Co-Versed Sine.	Logarithm Versed Sine.	Logarithm Co-Versed Sine.	
30	9518	9563806	6.9785359	9.9806308	30
31	9645	9560900	6.9843062	9.9804988	29
32	9773	9557994	6.9900387	9.9803668	28
33	9902	9555088	6.9957334	9.9802347	27
34	10032	9552182	7.0013911	9.9801026	26
35	10163	9549276	7.0069920	9.9799704	25
36	10294	9546370	7.0125969	9.9798383	24
37	10426	9543464	7.0182460	9.9797060	23
38	10559	9540558	7.0238600	9.9795738	22
39	10693	9537652	7.0294390	9.9794415	21
40	10828	9534747	7.0349588	9.9793092	20
41	10964	9531841	7.0399946	9.9791768	19
42	11101	9528935	7.0455371	9.9790444	18
43	11239	9526030	7.0507160	9.9789119	17
44	11377	9523124	7.0556027	9.9787795	16
45	11516	9520219	7.0603068	9.9786469	15
46	11656	9517313	7.0649554	9.9785144	14
47	11797	9514408	7.0695176	9.9783817	13
48	11939	9511502	7.0739544	9.9782491	12
49	12082	9508595	7.0782108	9.9781164	11
50	12225	9505692	7.0823316	9.9779837	10
51	12369	9502786	7.0863238	9.9778509	9
52	12514	9499881	7.0901788	9.9777182	8
53	12660	9496976	7.1024228	9.9775853	7
54	12807	9494071	7.1074280	9.9774525	6
55	12955	9491166	7.1124044	9.9773195	5
56	13103	9488260	7.1173527	9.9771866	4
57	13252	9485355	7.1222728	9.9770536	3
58	13402	9482450	7.1271652	9.9769206	2
59	13553	9479545	7.1320302	9.9767875	1
60	13705	9476640	7.1368680	9.9766544	0
	Natural Co-Versed Sine.	Natural Versed Sine.	Logarithm Co-Versed Sine.	Logarithm Versed Sine.	M.

87 DEGREES.



3 DEGREES.					
M.	Natural Versed Sine.	Natural Co-Versed Sine.	Logarithm Versed Sine.	Logarithm Co-Versed Sine.	
0	13705	9476640	7.1368680	9.9766544	60
1	13857	9473735	7.1416791	9.9765212	59
2	14011	9470830	7.1464636	9.9763881	58
3	14165	9467925	7.1512219	9.9762548	57
4	14320	9465020	7.1559542	9.9761216	56
5	14476	9462116	7.1606609	9.9759883	55
6	14633	9459211	7.1653422	9.9758550	54
7	14791	9456306	7.1699984	9.9757216	53
8	14950	9453402	7.1746297	9.9755882	52
9	15109	9450497	7.1792365	9.9754547	51
10	15269	9447593	7.1838189	9.9753212	50
11	15430	9444688	7.1883773	9.9751877	49
12	15592	9441784	7.1929118	9.9750541	48
13	15755	9438880	7.1974228	9.9749205	47
14	15919	9435976	7.2019104	9.9747868	46
15	16083	9433072	7.2063750	9.9746531	45
16	16248	9430168	7.2108167	9.9745194	44
17	16414	9427264	7.2152358	9.9743856	43
18	16581	9424360	7.2196326	9.9742519	42
19	16749	9421456	7.2240071	9.9741180	41
20	16918	9418552	7.2283597	9.9739841	40
21	17088	9415648	7.2326906	9.9738502	39
22	17258	9412744	7.2370000	9.9737162	38
23	17429	9409840	7.2412881	9.9735822	37
24	17601	9406936	7.2455551	9.9734482	36
25	17774	9404033	7.2498013	9.9733141	35
26	17948	9401129	7.2540267	9.9731800	34
27	18123	9398225	7.2582317	9.9730458	33
28	18299	9395322	7.2624164	9.9729117	32
29	18475	9392418	7.2665810	9.9727774	31
30	18652	9389515	7.2707258	9.9726431	30
Natural Co-Versed Sine.	Natural Versed Sine.	Logarithm Co-Versed Sine.	Logarithm Versed Sine.	M.	

86 DEGREES.

3 DEGREES.					
M.	Natural Versed Sine.	Natural Co-Versed Sine.	Logarithm Versed Sine.	Logarithm Co-Versed Sine.	
30	18652	9389515	7.2707258	9.9726431	30
31	18830	9386611	7.2748508	9.9723088	29
32	19009	9383708	7.2789563	9.9723745	28
33	19189	9380804	7.2830425	9.9722401	27
34	19369	9377901	7.2871095	9.9721056	26
35	19550	9374998	7.2911576	9.9719712	25
36	19732	9372095	7.2951869	9.9718367	24
37	19925	9369192	7.2991975	9.9717021	23
38	20099	9366289	7.3031897	9.9715675	22
39	20284	9363386	7.3071636	9.9714329	21
40	20470	9360483	7.3111194	9.9712982	20
41	20657	9357580	7.3150572	9.9711635	19
42	20844	9354677	7.3189773	9.9710288	18
43	21032	9351774	7.3228797	9.9708940	17
44	2122	9348871	7.3267646	9.9707592	16
45	21411	9345969	7.3306322	9.9706243	15
46	21602	9343066	7.3344827	9.9704894	14
47	21793	9340163	7.3383161	9.9703545	13
48	21985	9337261	7.3421327	9.9702195	12
49	22178	9334358	7.3459326	9.9700845	11
50	22372	9331456	7.3497159	9.9699494	10
51	22567	9328553	7.3534828	9.9698143	9
52	22763	9325651	7.3572334	9.9696792	8
53	22960	9322749	7.3609678	9.9695440	7
54	23157	9319847	7.3646863	9.9694088	6
55	23355	9316945	7.3683888	9.9692735	5
56	23554	9314043	7.3720757	9.9691382	4
57	23754	9311141	7.3757469	9.9690029	3
58	23955	9308239	7.3794027	9.9688675	2
59	24157	9305337	7.3830431	9.9687321	1
60	24360	9302435	7.3866683	9.9685967	0
Natural Co-Versed Sine.	Natural Versed Sine.	Logarithm Co-Versed Sine.	Logarithm Versed Sine.	M.	

86 DEGREES.

M m



## 4 DEGREES.

M.	Natural Versed Sine.	Natural Co-Versed Sine.	Logarithm Versed Sine.	Logarithm Co-Versed Sine.	
0	24360	9302435	7.3866683	9.9685967	60
1	24563	9299533	7.3902785	9.9684611	59
2	24767	9296631	7.3938716	9.9683256	58
3	24972	9293730	7.3974540	9.9681900	57
4	25178	9290828	7.4010196	9.9680544	56
5	25385	9287927	7.4045706	9.9679188	55
6	25592	9285025	7.4081071	9.9677831	54
7	25800	9282124	7.4116293	9.9676474	53
8	26009	9279223	7.4151372	9.9675116	52
9	26219	9276322	7.4186311	9.9673758	51
10	26430	9273421	7.4221109	9.9672399	50
11	26642	9270520	7.4255767	9.9671040	49
12	26855	9267619	7.4290288	9.9669681	48
13	27069	9264718	7.4324672	9.9668321	47
14	27283	9261817	7.4358921	9.9666961	46
15	27498	9258916	7.4393034	9.9665601	45
16	27714	9256015	7.4417015	9.9664240	44
17	27931	9253114	7.4460862	9.9662879	43
18	28149	9250213	7.4494578	9.9661517	42
19	28367	9247312	7.4528163	9.9660155	41
20	28586	9244412	7.4561619	9.9658793	40
21	28806	9241511	7.4594946	9.9657430	39
22	29027	9238611	7.4628146	9.9656067	38
23	29249	9235710	7.4661219	9.9654703	37
24	29472	9232810	7.4694166	9.9653339	36
25	29696	9229910	7.4726989	9.9651974	35
26	29921	9227009	7.4759688	9.9650610	34
27	30146	9224109	7.4792265	9.9649244	33
28	30372	9221209	7.4824719	9.9647879	32
29	30599	9218309	7.4857052	9.9646512	31
30	30827	9215409	7.4889265	9.9645146	30
	Natural Co-Versed Sine.	Natural Versed Sine.	Logarithm Co-Versed Sine.	Logarithm Versed Sine.	M.

85 DEGREES.

## 4 DEGREES.

M.	Natural Versed Sine.	Natural Co-Versed Sine.	Logarithm Versed Sine.	Logarithm Co-Versed Sine.	
30	30827	9215409	7.4889265	9.9645146	30
31	31056	9212509	7.4921359	9.9643779	29
32	31285	9209609	7.4953353	9.9642412	28
33	31515	9206709	7.4985193	9.9641044	27
34	31746	9203809	7.5016934	9.9639676	26
35	31978	9200910	7.5048560	9.9638308	25
36	32211	9198010	7.5080071	9.9636939	24
37	32445	9195111	7.5111468	9.9635570	23
38	32680	9192211	7.5142751	9.9634200	22
39	32915	9189312	7.5173922	9.9632830	21
40	33151	9186413	7.5204982	9.9631460	20
41	33388	9183514	7.5235930	9.9630089	19
42	33626	9180615	7.5266769	9.9628718	18
43	33865	9177716	7.5297498	9.9627346	17
44	34105	9174817	7.5328119	9.9625974	16
45	34345	9171918	7.5358632	9.9624601	15
46	34586	9169019	7.5389038	9.9623229	14
47	34828	9166120	7.5419338	9.9621855	13
48	35071	9163222	7.5449532	9.9620482	12
49	35315	9160323	7.5479021	9.9619108	11
50	35560	9157424	7.5509607	9.9617733	10
51	35806	9154526	7.5539489	9.9616358	9
52	36052	9151628	7.5569268	9.9614983	8
53	36299	9148729	7.5598946	9.9613607	7
54	36547	9145831	7.5628522	9.9612232	6
55	36796	9142933	7.5657997	9.9610855	5
56	37046	9140035	7.5687373	9.9609478	4
57	37297	9137137	7.5716650	9.9608101	3
58	37548	9134239	7.5745828	9.9606723	2
59	37800	9131341	7.5774908	9.9605345	1
60	38053	9128443	7.5803891	9.9603967	0
	Natural Co-Versed Sine.	Natural Versed Sine.	Logarithm Co-Versed Sine.	Logarithm Versed Sine.	M.

85 DEGREES.



5 DEGREES.					
M.	Natural Versed Sine.	Natural Co-Versed Sine.	Logarithm Versed Sine.	Logarithm Co-Versed Sine.	
0	38053	9128443	7.5803891	9.9603967	60
1	38307	9125545	7.5832777	9.9602588	59
2	38562	9122647	7.5861568	9.9601209	58
3	38817	9119750	7.5890263	9.9599829	57
4	39074	9116852	7.5918864	9.9598449	56
5	39331	9113955	7.5947322	9.9597068	55
6	39589	9111057	7.5975783	9.9595688	54
7	39848	9108160	7.6004103	9.9594306	53
8	40108	9105263	7.6032331	9.9592925	52
9	40369	9102366	7.6060468	9.9591542	51
10	40630	9099469	7.6088513	9.9590160	50
11	40893	9096572	7.6116468	9.9588777	49
12	41156	9093675	7.6144333	9.9587394	48
13	41420	9090778	7.6172109	9.9586010	47
14	41685	9087881	7.6199796	9.9584626	46
15	41951	9084984	7.6227395	9.9583241	45
16	42217	9082087	7.6254906	9.9581857	44
17	42485	9079191	7.6282330	9.9580471	43
18	42753	9076294	7.6309668	9.9579086	42
19	43022	9073398	7.6336920	9.9577699	41
20	43292	9070502	7.6364086	9.9576313	40
21	43563	9067605	7.6391167	9.9574926	39
22	43835	9064709	7.6418164	9.9573539	38
23	44107	9061813	7.6445078	9.9572151	37
24	44380	9058917	7.6471908	9.9570763	36
25	44655	9056021	7.6498655	9.9569374	35
26	44930	9053125	7.6525320	9.9567985	34
27	45205	9050229	7.6551903	9.9566596	33
28	45482	9047333	7.6578404	9.9565206	32
29	45760	9044437	7.6604825	9.9563816	31
30	46038	9041542	7.6631166	9.9562425	30
	Natural Co-Versed Sine.	Natural Versed Sine.	Logarithm Co-Versed Sine.	Logarithm Versed Sine.	M

84 DEGREES.

5 DEGREES.					
M.	Natural Versed Sine.	Natural Co-Versed Sine.	Logarithm Versed Sine.	Logarithm Co-Versed Sine.	
30	46038	9041542	7.6631166	9.9562425	30
31	46317	9038646	7.6657427	9.9561034	29
32	46597	9035751	7.6683608	9.9559643	28
33	46878	9032856	7.6709711	9.9558251	27
34	47160	9029961	7.6735735	9.9556859	26
35	47443	9027066	7.6761682	9.9555466	25
36	47726	9024171	7.6787550	9.9554073	24
37	48010	9021276	7.6813342	9.9552680	23
38	48295	9018381	7.6839058	9.9551286	22
39	48581	9015486	7.6864697	9.9549891	21
40	48868	9012592	7.6890260	9.9548497	20
41	49156	9009697	7.6915749	9.9547102	19
42	49444	9006802	7.6941162	9.9545706	18
43	49734	9003908	7.6966552	9.9544310	17
44	50024	9001013	7.6991767	9.9542914	16
45	50315	8998119	7.7016959	9.9541517	15
46	50607	8995225	7.7042078	9.9540120	14
47	50900	8992331	7.7067124	9.9538723	13
48	51193	8989437	7.7092098	9.9537325	12
49	51487	8986543	7.7117001	9.9535926	11
50	51783	8983649	7.7141832	9.9534528	10
51	52079	8980755	7.7166592	9.9533138	9
52	52375	8977861	7.7191281	9.9531729	8
53	52673	8974968	7.7215900	9.9530329	7
54	52972	8972074	7.7240450	9.9528929	6
55	53271	8969181	7.7264930	9.9527528	5
56	53572	8966287	7.7289341	9.9526127	4
57	53873	8963394	7.7313683	9.9524725	3
58	54175	8960501	7.7337658	9.9523323	2
59	54477	8957608	7.7362164	9.9521920	1
60	54781	8954715	7.7386303	9.9520518	0
	Natural Co-Versed Sine.	Natural Versed Sine.	Logarithm Co-Versed Sine.	Logarithm Versed Sine.	M.

84 DEGREES.



6 DEGREES.					
M.	Natural Versed Sine.	Natural Co-Versed Sine.	Logarithm Versed Sine.	Logarithm Co-Versed Sine.	
0	54781	8954715	7.7386303	9.9520518	60
1	55086	8951822	7.7410375	9.9519114	59
2	55391	8948929	7.7434380	9.9517711	58
3	55697	8946036	7.7458319	9.9516307	57
4	56004	8943143	7.7482192	9.9514902	56
5	56312	8940251	7.7505999	9.9513497	55
6	56621	8937358	7.7529742	9.9512092	54
7	56931	8934466	7.7553419	9.9510686	53
8	57241	8931574	7.7577031	9.9509280	52
9	57552	8928682	7.7600580	9.9507874	51
10	57864	8925790	7.7624064	9.9506467	50
11	58177	8922898	7.7647485	9.9505059	49
12	58491	8920006	7.7670843	9.9503652	48
13	58806	8917114	7.7694138	9.9502243	47
14	59121	8914222	7.7717371	9.9500835	46
15	59437	8911331	7.7740541	9.9499426	45
16	59754	8908439	7.7763649	9.9498016	44
17	60072	8905548	7.7786696	9.9496606	43
18	60391	8902656	7.7809682	9.9495196	42
19	60710	8899765	7.7832607	9.9493785	41
20	61030	8896874	7.7855472	9.9492375	40
21	61351	8893983	7.7878276	9.9490963	39
22	61673	8891092	7.7901020	9.9489551	38
23	61996	8888201	7.7923705	9.9488139	37
24	62320	8885310	7.7946331	9.9486716	36
25	62645	8882420	7.7968897	9.9485313	35
26	62971	8879529	7.7991405	9.9483899	34
27	63297	8876639	7.8013855	9.9482485	33
28	63624	8873748	7.8036246	9.9481071	32
29	63952	8870858	7.8058580	9.9479656	31
30	64281	8867968	7.8080856	9.9478241	30
	Natural Co-Versed Sine.	Natural Versed Sine.	Logarithm Versed Sine.	Logarithm Co-Versed Sine.	M.

83 DEGREES.

6 DEGREES.					
M.	Natural Versed Sine.	Natural Co-Versed Sine.	Logarithm Versed Sine.	Logarithm Co-Versed Sine.	
30	64281	8867968	7.8080856	9.9478241	30
31	64611	8865078	7.8103076	9.9476825	29
32	64942	8862188	7.8123237	9.9475409	28
33	65273	8859298	7.8147343	9.9473993	27
34	65605	8856408	7.8169392	9.9472576	26
35	65938	8853518	7.8191386	9.9471159	25
36	66272	8850628	7.8213323	9.9469741	24
37	66608	8847739	7.8235205	9.9468323	23
38	66943	8844849	7.8257032	9.9466904	22
39	67279	8841960	7.8278804	9.9465485	21
40	67616	8839071	7.8300522	9.9464066	20
41	67954	8836182	7.8322185	9.9462646	19
42	68293	8833293	7.8343794	9.9461226	18
43	68633	8830404	7.8365349	9.9459805	17
44	68974	8827515	7.8386851	9.9458385	16
45	69315	8824626	7.8408299	9.9456963	15
46	69657	8821737	7.8429695	9.9455541	14
47	70000	8818847	7.8451037	9.9454119	13
48	70344	8815960	7.8472327	9.9452696	12
49	70689	8813072	7.8493565	9.9451273	11
50	71035	8810184	7.8514751	9.9449850	10
51	71382	8807296	7.8535885	9.9448425	9
52	71729	8804408	7.8556968	9.9447001	8
53	72077	8801520	7.8577999	9.9445576	7
54	72426	8798632	7.8598800	9.9444151	6
55	72776	8795745	7.8619910	9.9442726	5
56	73127	8792857	7.8640789	9.9441300	4
57	73479	8789969	7.8661618	9.9439873	3
58	73831	8787082	7.8682397	9.9438446	2
59	74184	8784194	7.8703126	9.9437019	1
60	74539	8781307	7.8723806	9.9435591	0
	Natural Co-Versed Sine.	Natural Versed Sine.	Logarithm Versed Sine.	Logarithm Co-Versed Sine.	M.

83 DEGREES.



## 7 DEGREES.

M.	Natural Versed Sine.	Natural Co-Versed Sine.	Logarithm Versed Sine.	Logarithm Co-Versed Sine.	
0	74539	8781307	7.8723806	9.9435591	60
1	74894	8778420	7.8744436	9.9434163	59
2	75250	8775533	7.8765017	9.9432735	58
3	75607	8772646	7.8785550	9.9431306	57
4	75964	8779759	7.8806033	9.9429876	56
5	76322	8766872	7.8826469	9.9428446	55
6	76681	8763985	7.8846856	9.9427016	54
7	77041	8761099	7.8867196	9.9425586	53
8	76581	8758212	7.8887487	9.9424155	52
9	77764	8755326	7.8907784	9.9422723	51
10	78126	8752440	7.8927928	9.9421291	50
11	78484	8759554	7.8948078	9.9419859	49
12	78853	8746668	7.8968181	9.9418426	48
13	79218	8743782	7.8988238	9.9416993	47
14	79584	8740896	7.9008248	9.9415560	46
15	79951	8738010	7.9028212	9.9414125	45
16	80318	8735124	7.9048130	9.9412691	44
17	80686	8732239	7.9068002	9.9411256	43
18	81055	8739353	7.9087829	9.9409822	42
19	81425	8726468	7.9107610	9.9408385	41
20	81796	8723583	7.9127346	9.9406949	40
21	82168	8720698	7.9147038	9.9405513	39
22	82541	8717813	7.9166684	9.9404076	38
23	82914	8714928	7.9186286	9.9402638	37
24	83288	8712043	7.9205844	9.9401201	36
25	83663	8709159	7.9225358	9.9399762	35
26	84039	8706274	7.9244827	9.9398324	34
27	84416	8703390	7.9264253	9.9396885	33
28	84794	8699505	7.9283636	9.9395445	32
29	85172	8697622	7.9302975	9.9394005	31
30	85551		7.9322271	9.9392565	30
	Natural Co-Versed Sine.	Natural Versed Sine.	Logarithm Co-Versed Sine.	Logarithm Versed Sine.	M.

82 DEGREES.

## 7 DEGREES.

M.	Natural Versed Sine.	Natural Co-Versed Sine.	Logarithm Versed Sine.	Logarithm Co-Versed Sine.	
30	85551	8627622	7.9322271	9.9392565	30
31	85931	8694738	7.9341523	9.9391224	29
32	86312	8691854	7.9360734	9.9389083	28
33	86694	8688970	7.9379901	9.9388241	27
34	87077	8686086	7.9399027	9.9386800	26
35	87460	8683202	7.9418110	9.9385357	25
36	87844	8677436	7.9437151	9.9383914	24
37	88229	8674553	7.9456150	9.9382471	23
38	88615	8671670	7.9475107	9.9381027	22
39	89002	8668787	7.9494023	9.9379583	21
40	89391	8665904	7.9512898	9.9378139	20
41	89779	8663021	7.9531732	9.9376693	19
42	90168	8660138	7.9550525	9.9375248	18
43	90558	8657256	7.9569276	9.9373802	17
44	90949	8654373	7.9587988	9.9372356	16
45	91341	8651491	7.9606663	9.9370909	15
46	91734	8648608	7.9625290	9.9369462	14
47	92124	8645726	7.9643880	9.9368015	13
48	92521	8642844	7.9662431	9.9366567	12
49	92916	8639962	7.9680942	9.9365118	11
50	93312	8637080	7.9699414	9.9363670	10
51	93709	8634198	7.9717846	9.9362220	9
52	94107	8631317	7.9736239	9.9360771	8
53	94506	8628436	7.9754593	9.9359321	7
54	94905	8625554	7.9772908	9.9357870	6
55	95305	8622673	7.9791184	9.9356419	5
56	95706	8619792	7.9809422	9.9354968	4
57	96108	8616911	7.9827621	9.9353516	3
58	96511	8614030	7.9845782	9.9352064	2
59	96915	8611149	7.9863905	9.9350611	1
60	97319	8608269	7.9881990	9.9349158	0
	Natural Co-Versed Sine.	Natural Versed Sine.	Logarithm Co-Versed Sine.	Logarithm Versed Sine.	M.

82 DEGREES.

N A



8 DEGREES.					
M.	Natural Versed Sine.	Natural Co-Versed Sine.	Logarithm Versed Sine.	Logarithm Co-Versed Sine.	
0	97319	8608269	7.9881990	9.9349158	60
1	97724	8605388	7.9900038	9.9347705	59
2	98130	8602508	7.9918047	9.9346251	58
3	98537	8599627	7.9936020	9.9344756	57
4	98935	8596747	7.9953955	9.9343342	56
5	99354	8593867	7.9971853	9.9341886	55
6	99763	8590987	7.9989713	9.9340431	54
7	100173	8588107	8.0007537	9.9338975	53
8	100584	8585228	8.0025325	9.9337526	52
9	100995	8582348	8.0043076	9.9336061	51
10	101409	8579469	8.0060790	9.9334604	50
11	101823	8576590	8.0078468	9.9333146	49
12	102238	8573711	8.0096110	9.9331688	48
13	102653	8570832	8.0113716	9.9330229	47
14	103069	8567953	8.0131287	9.9328771	46
15	103486	8565074	8.0148822	9.9327311	45
16	103904	8562195	8.0166321	9.9325851	44
17	104323	8559316	8.0183785	9.9324391	43
18	104743	8556438	8.0201213	9.9322930	42
19	105163	8553559	8.0218607	9.9321469	41
20	105584	8550681	8.0235965	9.9320007	40
21	106006	8547803	8.0253289	9.9318545	39
22	106429	8544925	8.0270578	9.9317083	38
23	106853	8542047	8.0287833	9.9315620	37
24	107277	8539169	8.0305053	9.9314156	36
25	107702	8536292	8.0322239	9.9312692	35
26	108128	8533414	8.0339391	9.9311228	34
27	108555	8530537	8.0356508	9.9309764	33
28	108983	8527660	8.0373592	9.9308299	32
29	109412	8524783	8.0390643	9.9306833	31
30	109841	8521906	8.0407659	9.9305367	30
	Natural Co-Versed Sine.	Natural Versed Sine.	Logarithm Co-Versed Sine.	Logarithm Versed Sine.	M.

81 DEGREES.

8 DEGREES.					
M.	Natural Versed Sine.	Natural Co-Versed Sine.	Logarithm Versed Sine.	Logarithm Co-Versed Sine.	
30	109841	8521906	8.0407659	9.9305367	30
31	110271	8519029	8.0424642	9.9303901	29
32	110702	8516152	8.0441592	9.9302434	28
33	111134	8513276	8.0458509	9.9300967	27
34	111567	8510399	8.0475393	9.9299499	26
35	112001	8507523	8.0492243	9.9298031	25
36	112436	8504647	8.0509061	9.9296563	24
37	112872	8501771	8.0525847	9.9295094	23
38	113308	8498895	8.0542599	9.9293624	22
39	113745	8496019	8.0559319	9.9292154	21
40	114183	8493143	8.0576007	9.9290684	20
41	114622	8490267	8.0592663	9.9289213	19
42	115062	8487392	8.0609286	9.9287743	18
43	115502	8484516	8.0625878	9.9286271	17
44	115943	8481641	8.0642438	9.9284799	16
45	116385	8478766	8.0658966	9.9283326	15
46	116828	8475891	8.0675463	9.9281854	14
47	117272	8473016	8.0691928	9.9280380	13
48	117717	8470141	8.0708362	9.9278907	12
49	118162	8467266	8.0724764	9.9277432	11
50	118608	8464392	8.0741136	9.9275958	10
51	119055	8461518	8.0757476	9.9274483	9
52	119503	8458644	8.0773786	9.9273008	8
53	119952	8455770	8.0790065	9.9271531	7
54	120402	8452896	8.0806313	9.9270055	6
55	120852	8450022	8.0822531	9.9268578	5
56	121303	8447148	8.0838718	9.9267101	4
57	121755	8444275	8.0854976	9.9265624	3
58	122208	8441401	8.0871002	9.9264146	2
59	122662	8438528	8.0887099	9.9262667	1
60	123117	8435655	8.0903166	9.9261188	0
	Natural Co-Versed Sine.	Natural Versed Sine.	Logarithm Co-Versed Sine.	Logarithm Versed Sine.	M.

81 DEGREES.

N n 2



9 DEGREES.					
M.	Natural Versed Sine.	Natural Co-Versed Sine.	Logarithm Versed Sine.	Logarithm Co-Versed Sine.	
0	123117	8435655	8.0903166	9.9261188	60
1	123573	8432782	8.091903	9.9259709	59
2	124029	8429909	8.0935210	9.9258229	58
3	124486	8427036	8.0951188	9.9256749	57
4	124944	8424163	8.0967136	9.9255268	56
5	125403	8411291	8.0983055	9.9253787	55
6	125863	8418419	8.0998944	9.9252306	54
7	126323	8415547	8.1014804	9.9250823	53
8	126784	8412675	8.1030635	9.9249341	52
9	127246	8409803	8.1046437	9.9247858	51
10	127709	8406931	8.1062211	9.9246375	50
11	128173	8404059	8.1077955	9.9244891	49
12	128638	8491188	8.1093671	9.9243407	48
13	128103	8398316	8.1109358	9.9241922	47
14	129569	8395445	8.1125017	9.9240437	46
15	130036	8392574	8.1140647	9.9238956	45
16	130544	8389703	8.1156249	9.9237466	44
17	130973	8386832	8.1171823	9.9235979	43
18	131443	8383962	8.1187369	9.9234493	42
19	131915	8381091	8.1202887	9.9233005	41
20	132384	8378221	8.1218377	9.9231518	40
21	132856	8375351	8.1233840	9.9220030	39
22	133329	8372481	8.1249274	9.9228541	38
23	133803	8369611	8.1264681	9.9227052	37
24	134278	8366741	8.1280061	9.9225563	36
25	134754	8363871	8.1295413	9.9234073	35
26	135230	8361001	8.1310738	9.9222583	34
27	135707	8358132	8.1326036	9.9221092	33
28	136185	8355262	8.1341307	9.9219601	32
29	136664	8352393	8.1356551	9.9218109	31
30	137144	8349524	8.1371768	9.9216617	30
	Natural Co-Versed Sine.	Natural Versed Sine.	Logarithm Co-Versed Sine.	Logarithm Versed Sine.	M.

80 DEGREES.

9 DEGREES.					
M.	Natural Versed Sine.	Natural Co-Versed Sine.	Logarithm Versed Sine.	Logarithm Co-Versed Sine.	
30	137144	8349524	8.1311768	9.9216617	30
31	137624	8346655	8.1386958	9.9215124	29
32	138105	8343786	8.1402121	9.9213632	28
33	138587	8340918	8.1417258	9.9212138	27
34	139070	8338049	8.1432368	9.9210644	26
35	139554	8335181	8.1447452	9.9209150	25
36	140039	8332313	8.1462510	9.9207656	24
37	140525	8329445	8.1477541	9.9206160	23
38	141011	8326577	8.1492546	9.9204665	22
39	141498	8323709	8.1507525	9.9203169	21
40	141986	8320841	8.1522478	9.9201672	20
41	142475	8317973	8.1537405	9.9200175	19
42	142965	8315106	8.1552307	9.9198678	18
43	143456	8312239	8.1567182	9.9197180	17
44	143947	8309372	8.1582032	9.9195682	16
45	144439	8306505	8.1596857	9.9194183	15
46	144932	8303638	8.1611656	9.9192684	14
47	145426	8300771	8.1626430	9.9191184	13
48	145921	8297905	8.1641178	9.9189685	12
49	146417	8295038	8.1655902	9.9188184	11
50	146913	8292172	8.1670600	9.9186683	10
51	147410	8289306	8.1685273	9.9185182	9
52	147908	8286440	8.1699921	9.9183680	8
53	148407	8283574	8.1714545	9.9182178	7
54	148907	8280708	8.1729144	9.9180675	6
55	149407	8277843	8.1743717	9.9179172	5
56	149908	8274978	8.1758267	9.9177669	4
57	150410	8272113	8.1772792	9.9176164	3
58	150913	8269248	8.1787292	9.9174660	2
59	151417	8266383	8.1801768	9.9173155	1
60	151922	8263518	8.1816220	9.9171650	0
	Natural Co-Versed Sine.	Natural Versed Sine.	Logarithm Co-Versed Sine.	Logarithm Versed Sine.	M.

80 DEGREES.



10 DEGREES.					
M.	Natural Versed Sine.	Natural Co-Versed Sine.	Logarithm Versed Sine.	Logarithm Co-Versed Sine.	
0	151922	8263518	8.1816220	9.9171650	60
1	152428	8260653	8.1830648	9.9170144	59
2	152934	8257789	8.1845051	9.9168638	58
3	153441	8254925	8.1859431	9.9167131	57
4	153949	8252061	8.1873786	9.9165624	56
5	154450	8249197	8.1888118	9.9164116	55
6	154968	8246333	8.1902426	9.9162609	54
7	155479	8243469	8.1916710	9.9161100	53
8	155990	8240606	8.1930971	9.9159591	52
9	156502	8237742	8.1945208	9.9158082	51
10	157015	8234879	8.1959421	9.9156572	50
11	157529	8232016	8.1973611	9.9155062	49
12	158044	8229153	8.1987778	9.9153551	48
13	158560	8226290	8.2001921	9.9152040	47
14	159076	8223427	8.2016042	9.9150528	46
15	159593	8220565	8.2030139	9.9149016	45
16	160111	8217702	8.2044213	9.9147504	44
17	160630	8214840	8.2058264	9.9145991	43
18	161150	8211978	8.2072293	9.9144478	42
19	161671	8209116	8.2086298	9.9142964	41
20	162192	8206254	8.2100281	9.9141450	40
21	162714	8203392	8.2114241	9.9139935	39
22	163237	8200531	8.2128179	9.9138420	38
23	163761	8197669	8.2142094	9.9136904	37
24	164286	8194808	8.2155987	9.9135388	36
25	164811	8191946	8.2169857	9.9133871	35
26	165337	8189086	8.2183705	9.9132355	34
27	165864	8186226	8.2197531	9.9130837	33
28	166392	8183366	8.2211334	9.9129319	32
29	166921	8180505	8.2225116	9.9127801	31
30	167451	8177645	8.2238875	9.9126282	30
	Natural Co-Versed Sine.	Natural Versed Sine.	Logarithm Co-Versed Sine.	Logarithm Versed Sine.	M

79 DEGREES.

10 DEGREES.					
M.	Natural Versed Sine.	Natural Co-Versed Sine.	Logarithm Versed Sine.	Logarithm Co-Versed Sine.	
30	167451	8177645	8.2238875	9.9126282	30
31	167981	8174785	8.2252613	9.9124763	29
32	168512	8171925	8.2266329	9.9123244	28
33	169044	8169065	8.2280023	9.9121723	27
34	169577	8166205	8.2293695	9.9120203	26
35	170111	8163346	8.2307345	9.9118682	25
36	170646	8160487	8.2320974	9.9117161	24
37	171182	8157628	8.2334581	9.9115638	23
38	171718	8154769	8.2348167	9.9114116	22
39	172255	8151910	8.2361732	9.9112593	21
40	172793	8149051	8.2375275	9.9111070	20
41	173332	8146192	8.2388797	9.9109546	19
42	173872	8143334	8.2402297	9.9108022	18
43	174413	8140476	8.2415737	9.9106498	17
44	174954	8137618	8.2429235	9.9104973	16
45	175496	8134760	8.2442673	9.9103447	15
46	176039	8131902	8.2456089	9.9101921	14
47	176583	8129044	8.2469485	9.9100395	13
48	177128	8126187	8.2482860	9.9098868	12
49	177673	8123330	8.2496214	9.9097341	11
50	178219	8120473	8.2509547	9.9095813	10
51	178766	8117616	8.2522860	9.9094285	9
52	179314	8114759	8.2536152	9.9092756	8
53	179863	8111902	8.2549424	9.9091227	7
54	180413	8109046	8.2562675	9.9089697	6
55	180963	8106190	8.2575906	9.9088167	5
56	181514	8103334	8.2589117	9.9086637	4
57	182066	8100478	8.2602307	9.9085106	3
58	182619	8097622	8.2615477	9.9083575	2
59	183173	8094766	8.2628626	9.9082043	1
60	183728	8091910	8.2641757	9.9080510	0
	Natural Co-Versed Sine.	Natural Versed Sine.	Logarithm Co-Versed Sine.	Logarithm Versed Sine.	M.

79 DEGREES.



II DEGREES.					
M.	Natural Versed Sine.	Natural Co- Versed Sine.	Logarithm Versed Sine.	Logarithm Co- Versed Sine.	
0	183728	8091910	8.2641757	9.9080510	60
1	184284	8089055	8.2654867	9.9078977	59
2	184840	8086200	8.2667957	9.9077445	58
3	185397	8083345	8.2681028	9.9075911	57
4	185955	8080490	8.2694078	9.9074377	56
5	186514	8077635	8.2707169	9.9072842	55
6	187074	8074780	8.2720119	9.9071307	54
7	187634	8071926	8.2733111	9.9069771	53
8	188195	8069072	8.2746082	9.9068236	52
9	188757	8066218	8.2759035	9.9066699	51
10	189320	8063364	8.2771967	9.9065163	50
11	189884	8060510	8.2784880	9.9063625	49
12	190449	8057656	8.2797774	9.9062087	48
13	191014	8054803	8.2810649	9.9060549	47
14	191580	8051950	8.2823504	9.9059011	46
15	192147	8049097	8.2836341	9.9057471	45
16	192715	8046244	8.2849158	9.9055932	44
17	193284	8043391	8.2861956	9.9054392	43
18	193853	8040538	8.2874735	9.9052851	42
19	194423	8037686	8.2887495	9.9051310	41
20	194994	8034834	8.2900236	9.9049769	40
21	195566	8031982	8.2912958	9.9048227	39
22	196139	8029130	8.2925661	9.9046685	38
23	196713	8026278	8.2938346	9.9045142	37
24	197288	8023426	8.2951012	9.9043599	36
25	197863	8020575	8.2963660	9.9042055	35
26	198439	8017724	8.2976289	9.9040511	34
27	199016	8014873	8.2988899	9.9038966	33
28	199594	8012022	8.3001491	9.9037421	32
29	200174	8009171	8.3014064	9.9035876	31
30	200753	8006321	8.3026619	9.9034330	30
	Natural Co- Versed Sine.	Natural Versed Sine.	Logarithm Co- Versed Sine.	Logarithm Versed Sine.	M.

78 DEGREES.

II DEGREES.					
M.	Natural Versed Sine.	Natural Co- Versed Sine.	Logarithm Versed Sine.	Logarithm Co- Versed Sine.	
30	200753	8006321	8.3026619	9.9034330	30
31	201333	8003470	8.3039156	9.9032783	29
32	201914	8000620	8.3051675	9.9031236	28
33	202496	7997770	8.3064175	9.9029689	27
34	203079	7994920	8.3076657	9.9028141	26
35	203663	7992070	8.3089122	9.9026593	25
36	204247	7989220	8.3101568	9.9025044	24
37	204832	7986371	8.3113996	9.9023495	23
38	205418	7983522	8.3126406	9.9021945	22
39	206005	7980673	8.3138798	9.9020395	21
40	206593	7977824	8.3151172	9.9018845	20
41	207182	7974975	8.3163529	9.9017293	19
42	207772	7972126	8.3175868	9.9015742	18
43	208362	7969278	8.3188189	9.9014190	17
44	208953	7966430	8.3200493	9.9012638	16
45	209545	7963582	8.3212779	9.9011085	15
46	210138	7960734	8.3225047	9.9009531	14
47	210732	7957886	8.3237298	9.9007977	13
48	211326	7955038	8.3249532	9.9006423	12
49	211921	7952191	8.3261748	9.9004868	11
50	212517	7949344	8.3273947	9.9003313	10
51	213114	7946497	8.3286128	9.8901758	9
52	213712	7943650	8.3298292	9.8900202	8
53	214311	7940803	8.3310439	9.8998645	7
54	214910	7937957	8.3322569	9.8997088	6
55	215510	7935111	8.3334682	9.8995530	5
56	216111	7932265	8.3346778	9.8993973	4
57	216713	7929419	8.3358857	9.8992414	3
58	217316	7926573	8.3370918	9.8990855	2
59	217920	7923728	8.3382963	9.8989296	1
60	218524	7920883	8.3394991	9.8987736	0
	Natural Co- Versed Sine.	Natural Versed Sine.	Logarithm Co- Versed Sine.	Logarithm Versed Sine.	M.

78 DEGREES.



12 DEGREES.					
M.	Natural Versed Sine.	Natural Co-Versed Sine.	Logarithm Versed Sine.	Logarithm Co-Versed Sine.	
0	218524	7920883	8.3394991	9.8987736	60
1	219129	7918038	8.3407002	9.8986176	59
2	219735	7915193	8.3418997	9.8984615	58
3	220342	7912348	8.3430975	9.8983054	57
4	220950	7909503	8.3442936	9.8981492	56
5	221558	7906658	8.3454880	9.8979930	55
6	222167	7903814	8.3466808	9.8978367	54
7	222777	7900970	8.3478719	9.8976804	53
8	223388	7898126	8.3490614	9.8975241	52
9	224000	7895282	8.3502492	9.8973676	51
10	224613	7892438	8.3514354	9.8972112	50
11	225227	7889595	8.3526200	9.8970547	49
12	225841	7886752	8.3538029	9.8968982	48
13	226456	7883909	8.3549842	9.8967416	47
14	227072	7881066	8.3561639	9.8965850	46
15	227689	7878223	8.3573419	9.8964283	45
16	228307	7875380	8.3585184	9.8962716	44
17	228925	7872538	8.3596932	9.8961148	43
18	229544	7869696	8.3608664	9.8959580	42
19	230164	7866854	8.3620380	9.8958011	41
20	230785	7864012	8.3632081	9.8956442	40
21	231407	7861170	8.3643765	9.8954872	39
22	232030	7858329	8.3655434	9.8953302	38
23	232653	7855488	8.3667086	9.8951731	37
24	233277	7852647	8.3678723	9.8950161	36
25	233902	7849806	8.3690344	9.8948589	35
26	234528	7846965	8.3701950	9.8947017	34
27	235155	7844124	8.3713540	9.8945445	33
28	235783	7841284	8.3725114	9.8943872	32
29	236411	7838444	8.3736672	9.8942298	31
30	237040	7835604	8.3748215	9.8940725	30
	Natural Co-Versed Sine.	Natural Versed Sine.	Logarithm Co-Versed Sine.	Logarithm Versed Sine.	M.

77 DEGREES.\*

12 DEGREES.					
M.	Natural Versed Sine.	Natural Co-Versed Sine.	Logarithm Versed Sine.	Logarithm Co-Versed Sine.	
30	237040	7835604	8.3748215	9.8940725	30
31	237670	7832764	8.3759743	9.8939150	29
32	238301	7829924	8.3771255	9.8937576	28
33	238933	7827084	8.3782751	9.8936000	27
34	239565	7824245	8.3794232	9.8934425	26
35	240198	7821406	8.3805698	9.8932848	25
36	240832	7818567	8.3817149	9.8931272	24
37	241467	7815728	8.3828584	9.8929695	23
38	242103	7812889	8.3840004	9.8928117	22
39	242740	7810051	8.3851409	9.8926539	21
40	243377	7807213	8.3862799	9.8924961	20
41	244015	7804375	8.3874174	9.8923381	19
42	244654	7801537	8.3885533	9.8921802	18
43	245294	7798700	8.3896878	9.8920222	17
44	245935	7795863	8.3908207	9.8918642	16
45	246577	7793026	8.3919522	9.8917061	15
46	247219	7790189	8.3930822	9.8915480	14
47	247862	7787352	8.3942107	9.8913898	13
48	248506	7784515	8.3953377	9.8912316	12
49	249151	7781678	8.3964638	9.8910733	11
50	249797	7778842	8.3975873	9.8909150	10
51	250443	7776006	8.3987098	9.8907566	9
52	251090	7773170	8.3998310	9.8905983	8
53	251738	7770334	8.4009506	9.8904397	7
54	252387	7767498	8.4020688	9.8902812	6
55	253037	7764663	8.4031855	9.8901226	5
56	253688	7761828	8.4043008	9.8899640	4
57	254340	7758993	8.4054147	9.8898054	3
58	254992	7756158	8.4065270	9.8896467	2
59	255645	7753323	8.4076380	9.8894879	1
60	256300	7750489	8.4087475	9.8893291	0
	Natural Co-Versed Sine.	Natural Versed Sine.	Logarithm Co-Versed Sine.	Logarithm Versed Sine.	M.

77 DEGREES.



13 DEGREES.					
M.	Natural Versed Sine.	Natural Co-Versed Sine.	Logarithm Versed Sine.	Logarithm Co-Versed Sine.	
0	256300	7750489	8.4087475	9.8893291	60
1	256955	7747655	8.4098556	9.8891703	59
2	257611	7744821	8.4109622	9.8890114	58
3	258267	7741987	8.4120675	9.8888524	57
4	258924	7739153	8.4131713	9.8886935	56
5	259582	7736320	8.4142736	9.8885344	55
6	260241	7733487	8.4153746	9.8883754	54
7	260901	7730654	8.4164741	9.8882162	53
8	261561	7727821	8.4175723	9.8880571	52
9	262222	7724988	8.4186690	9.8878978	51
10	262884	7722156	8.4197644	9.8877386	50
11	263547	7719324	8.4208583	9.8875792	49
12	264211	7716492	8.4219508	9.8874199	48
13	264876	7713660	8.4230420	9.8872604	47
14	265541	7710828	8.4241318	9.8871010	46
15	266207	7707996	8.4252280	9.8869415	45
16	266874	7705165	8.4263072	9.8867819	44
17	267542	7702334	8.4273928	9.8866223	43
18	268211	7699503	8.4284770	9.8864627	42
19	268880	7696672	8.4295600	9.8863032	41
20	269550	7693841	8.4306414	9.8861432	40
21	270221	7691011	8.4317216	9.8859834	39
22	270893	7688181	8.4328004	9.8858236	38
23	271566	7685351	8.4338778	9.8856637	37
24	272240	7682521	8.4349539	9.8855038	36
25	272915	7679691	8.4360286	9.8853437	35
26	273591	7676862	8.4371020	9.8851837	34
27	274267	7674033	8.4381740	9.8850236	33
28	274944	7671204	8.4392447	9.8848635	32
29	275622	7668375	8.4403141	9.8847033	31
30	276301	7665546	8.4413821	9.8845431	30
	Natural Co-Versed Sine.	Natural Versed Sine.	Logarithm Co-Versed Sine.	Logarithm Versed Sine.	M.

76 DEGREES.

13 DEGREES.					
M.	Natural Versed Sine.	Natural Co-Versed Sine.	Logarithm Versed Sine.	Logarithm Co-Versed Sine.	
30	276301	7665546	8.4413821	9.8845431	30
31	276980	7662718	8.4424488	9.8843828	29
32	277660	7659890	8.4435142	9.8842225	28
33	278341	7657062	8.4445743	9.8840621	27
34	279023	7654234	8.4456410	9.8839017	26
35	279706	7651406	8.4467024	9.8837412	25
36	280390	7648579	8.4477625	9.8835807	24
37	281074	7645752	8.4488213	9.8834202	23
38	281759	7642925	8.4498788	9.8832596	22
39	282445	7640098	8.4509350	9.8830989	21
40	283132	7637271	8.4519898	9.8829382	20
41	283820	7634445	8.4530434	9.8827774	19
42	284509	7631619	8.4540957	9.8826167	18
43	285198	7628793	8.4551467	9.8824558	17
44	285888	7625967	8.4561964	9.8822949	16
45	286579	7623141	8.4572448	9.8821339	15
46	287271	7620316	8.4582920	9.8819730	14
47	287964	7617491	8.4593378	9.8818119	13
48	288657	7614666	8.4603824	9.8816508	12
49	289351	7611841	8.4614257	9.8814897	11
50	290046	7609017	8.4624677	9.8813285	10
51	290742	7606192	8.4635085	9.8811672	9
52	291439	7603368	8.4645480	9.8810060	8
53	292137	7600544	8.4655863	9.8808446	7
54	292835	7597720	8.4666233	9.8806833	6
55	293534	7594896	8.4676601	9.8805218	5
56	294234	7592073	8.4686935	9.8803604	4
57	294935	7589250	8.4697269	9.8801988	3
58	295637	7586427	8.4707587	9.8800372	2
59	296340	7583604	8.4717894	9.8798756	1
60	297043	7580781	8.4728189	9.8797140	0
	Natural Co-Versed Sine.	Natural Versed Sine.	Logarithm Co-Versed Sine.	Logarithm Versed Sine.	M.

76 DEGREES.



14 DEGREES.					
M.	Natural Versed Sine.	Natural Co- Versed Sine.	Logarithm Versed Sine.	Logarithm Co- Versed Sine.	
0	297043	7580781	8.4728189	9.8797140	60
1	297747	7577959	8.4738472	9.8795522	59
2	298452	7575137	8.4748742	9.8793905	58
3	299158	7572315	8.4759001	9.8792286	57
4	299865	7569493	8.4769246	9.8790668	56
5	300572	7566671	8.4779480	9.8789048	55
6	301280	7563850	8.4789701	9.8787429	54
7	301989	7561029	8.4799910	9.8785809	53
8	302699	7558208	8.4810107	9.8784188	52
9	303410	7555387	8.4820291	9.8782567	51
10	304121	7552566	8.4830464	9.8780946	50
11	304833	7549746	8.4840625	9.8779323	49
12	305546	7546926	8.4850773	9.8777701	48
13	306260	7544106	8.4860910	9.8776078	47
14	306975	7541286	8.4871034	9.8774454	46
15	307691	7538467	8.4881146	9.8772850	45
16	308407	7535648	8.4891247	9.8771206	44
17	309124	7532829	8.4901336	9.8769581	43
18	309842	7530010	8.4911412	9.8767955	42
19	310561	7527191	8.4921477	9.8766329	41
20	311281	7524372	8.4931530	9.8764703	40
21	312002	7521554	8.4941572	9.8763076	39
22	312723	7518736	8.4951601	9.8761449	38
23	313445	7515918	8.4961619	9.8759821	37
24	314168	7513100	8.4971625	9.8758192	36
25	314892	7510283	8.4981619	9.8756563	35
26	315617	7507466	8.4991602	9.8754934	34
27	316343	7504649	8.5001573	9.8753304	33
28	317069	7501832	8.5011532	9.8751674	32
29	317796	7499016	8.5021480	9.8750043	31
30	318524	7496200	8.5031416	9.8748412	30
	Natural Co- Versed Sine.	Natural Versed Sine.	Logarithm Co- Versed Sine.	Logarithm Versed Sine.	M.

75 DEGREES.

14 DEGREES.					
M.	Natural Versed Sine.	Natural Co- Versed Sine.	Logarithm Versed Sine.	Logarithm Co- Versed Sine.	
30	318524	7496200	8.5031416	9.8748412	30
31	319253	7493384	8.5041341	9.8746780	29
32	319983	7490568	8.5051254	9.8745147	28
33	320713	7487752	8.5061136	9.8743514	27
34	321444	7484936	8.5071046	9.8741881	26
35	322176	7482121	8.5080925	9.8740247	25
36	322909	7479306	8.5090792	9.8738613	24
37	323643	7476491	8.5100648	9.8736978	23
38	324377	7473676	8.5110493	9.8735343	22
39	325112	7470862	8.5120326	9.8733707	21
40	325848	7468048	8.5130148	9.8732071	20
41	326585	7465234	8.5139959	9.8730434	19
42	327323	7462420	8.5149758	9.8728797	18
43	328062	7459607	8.5159546	9.8727159	17
44	328801	7456794	8.5169324	9.8725521	16
45	329541	7453981	8.5179089	9.8723882	15
46	330282	7451168	8.5188844	9.8722243	14
47	331024	7448355	8.5198588	9.8720603	13
48	331767	7445542	8.5208320	9.8718963	12
49	332510	7442730	8.5218042	9.8717322	11
50	333254	7439918	8.5227752	9.8715682	10
51	333999	7437106	8.5237451	9.8714040	9
52	334745	7434294	8.5247140	9.8712398	8
53	335492	7431483	8.5256817	9.8710755	7
54	336239	7428672	8.5266484	9.8709112	6
55	336987	7425861	8.5276139	9.8707468	5
56	337736	7423050	8.5285784	9.8705824	4
57	338486	7420240	8.5295417	9.8704179	3
58	339237	7417430	8.5305040	9.8702534	2
59	339989	7414620	8.5314652	9.8700888	1
60	340742	7411810	8.5324253	9.8699243	0
	Natural Co- Versed Sine.	Natural Versed Sine.	Logarithm Co- Versed Sine.	Logarithm Versed Sine.	M.

75 DEGREES.



15 DEGREES.					
M.	Natural Versed Sine.	Natural Co-Versed Sine.	Logarithm Versed Sine.	Logarithm Co-Versed Sine.	
0	340742	7411810	8.5324253	9.8699243	60
1	341495	7409000	8.5333844	9.8697596	59
2	342249	7406191	8.5343423	9.8695949	58
3	343004	7403382	8.5352992	9.8694301	57
4	343760	7400573	8.5362551	9.8692653	56
5	344516	7397764	8.5372098	9.8691004	55
6	345273	7394955	8.5381635	9.8689355	54
7	346031	7392147	8.5391161	9.8687705	53
8	346790	7389339	8.5400677	9.8686056	52
9	347550	7386531	8.5410182	9.8684405	51
10	348311	7383723	8.5419676	9.8682754	50
11	349073	7380916	8.5429160	9.8681102	49
12	349835	7378109	8.5438633	9.8679450	48
13	350598	7375302	8.5448096	9.8677797	47
14	351362	7372495	8.5457548	9.8676145	46
15	352127	7369688	8.5466983	9.8674491	45
16	352892	7366882	8.5476422	9.8672837	44
17	353658	7364076	8.5485843	9.8671182	43
18	354425	7361270	8.5495253	9.8669527	42
19	355193	7358464	8.5504654	9.8667871	41
20	355962	7355658	8.5514044	9.8666216	40
21	356732	7352853	8.5523423	9.8664559	39
22	357502	7350048	8.5532793	9.8662902	38
23	358273	7347243	8.5542152	9.8661244	37
24	359045	7344438	8.5551500	9.8659586	36
25	359818	7341634	8.5560839	9.8657927	35
26	360592	7338830	8.5570167	9.8656269	34
27	361367	7336026	8.5579485	9.8654609	33
28	362142	7333223	8.5588793	9.8652949	32
29	362918	7330420	8.5598091	9.8651288	31
30	363695	7327617	8.5607379	9.8649627	30
	Natural Co-Versed Sine.	Natural Versed Sine.	Logarithm Co-Versed Sine.	Logarithm Versed Sine.	M.

74 DEGREES.

15 DEGREES.					
M.	Natural Versed Sine.	Natural Co-Versed Sine.	Logarithm Versed Sine.	Logarithm Co-Versed Sine.	
30	363695	7327617	8.5607379	9.8649627	30
31	364473	7324814	8.5616656	9.8647965	29
32	365252	7322011	8.5625924	9.8646303	28
33	366031	7319208	8.5635181	9.8644641	27
34	366811	7316405	8.5644429	9.8642978	26
35	367592	7313603	8.5653666	9.8641314	25
36	368374	7310801	8.5662894	9.8639650	24
37	369157	7307999	8.5672111	9.8637985	23
38	369941	7305198	8.5681318	9.8636320	22
39	370725	7302397	8.5690516	9.8634655	21
40	371510	7299596	8.5699704	9.8632989	20
41	372296	7296795	8.5708881	9.8631322	19
42	373083	7293995	8.5718049	9.8629655	18
43	373871	7291195	8.5727207	9.8627987	17
44	374659	7288395	8.5736355	9.8626319	16
45	375448	7285595	8.5745494	9.8624650	15
46	376238	7282796	8.5754622	9.8622981	14
47	377029	7279997	8.5763741	9.8621314	13
48	377821	7277198	8.5762850	9.8619642	12
49	378613	7274399	8.5781949	9.8617971	11
50	379406	7271600	8.5791039	9.8616300	10
51	380200	7268802	8.5800119	9.8614628	9
52	380995	7266004	8.5809189	9.8612956	8
53	381791	7263206	8.5818250	9.8611283	7
54	382587	7260408	8.5827301	9.8609610	6
55	383384	7257611	8.5836342	9.8607936	5
56	384182	7254814	8.5845374	9.8606262	4
57	384981	7252017	8.5854396	9.8604587	3
58	385781	7249220	8.5863409	9.8602912	2
59	386582	7246423	8.5872412	9.8601236	1
60	387383	7243627	8.5881406	9.8599560	0
	Natural Co-Versed Sine.	Natural Versed Sine.	Logarithm Co-Versed Sine.	Logarithm Versed Sine.	M.

74 DEGREES.

P p



16 DEGREES.					
M.	Natural Versed Sine.	Natural Co. Versed Sine.	Logarithm Versed Sine.	Logarithm Co. Versed Sine.	
0	387383	7243627	8.5881406	9.8599560	60
1	388185	7240831	8.5890390	9.8597883	59
2	388988	7238035	8.5899365	9.8596206	58
3	389792	7235239	8.5908330	9.8594529	57
4	390597	7232444	8.5917286	9.8592851	56
5	391402	7229649	8.5926232	9.8591171	55
6	392208	7226854	8.5935170	9.8589492	54
7	393015	7224059	8.5944097	9.8587812	53
8	393823	7221265	8.5953016	9.8586132	52
9	394632	7218471	8.5961925	9.8584451	51
10	395441	7215677	8.5970824	9.8582770	50
11	296251	7212883	8.5979715	9.8581088	49
12	297062	7210089	8.5988596	9.8579406	48
13	297874	7207296	8.5997468	9.8577723	47
14	298687	7204503	8.6006330	9.8576040	46
15	299501	7201710	8.6015184	9.8574356	45
16	400315	7198918	8.6024028	9.8572672	44
17	401130	7196126	8.6032863	9.8570987	43
18	401946	7193334	8.6041689	9.8569302	42
19	402763	7190542	8.6050505	9.8567615	41
20	403581	7187750	8.6059313	9.8565929	40
21	404400	7184959	8.6068112	9.8564242	39
22	405219	7182168	8.6076901	9.8562555	38
23	406039	7179377	8.6085681	9.8560867	37
24	406860	7176586	8.6094453	9.8559179	36
25	407682	7173796	8.6103215	9.8557489	35
26	408505	7171006	8.6111968	9.8555800	34
27	409328	7168216	8.6120712	9.8554110	33
28	410152	7165426	8.6129448	9.8552420	32
29	410977	7162636	8.6138174	9.8550728	31
30	411803	7159847	8.6146891	9.8549037	30
	Natural Co. Versed Sine.	Natural Versed Sine.	Logarithm Co. Versed Sine.	Logarithm Versed Sine.	M.

73 DEGREES.

16 DEGREES.					
M.	Natural Versed Sine.	Natural Co. Versed Sine.	Logarithm Versed Sine.	Logarithm Co. Versed Sine.	
30	411803	7159847	8.6146891	9.8549037	30
31	412629	7157058	8.6155600	9.8547345	29
32	413456	7154269	8.6164299	9.8545653	28
33	414284	7151480	8.6172990	9.8543959	27
34	415113	7148692	8.6181672	9.8542266	26
35	415947	7145904	8.6190345	9.8540572	25
36	416774	7143116	8.6199009	9.8538877	24
37	417605	7140328	8.6207664	9.8537182	23
38	418437	7137541	8.6216331	9.8535486	22
39	419270	7134754	8.6224948	9.8533790	21
40	420104	7131967	8.6233577	9.8532094	20
41	420939	7129181	8.6242197	9.8530396	19
42	421775	7126395	8.6250809	9.8528699	18
43	422611	7123609	8.6259412	9.8527000	17
44	423448	7120823	8.6268006	9.8525302	16
45	424286	7118037	8.6276591	9.8523602	15
46	425125	7115252	8.6285168	9.8521903	14
47	425964	7112467	8.6293736	9.8520202	13
48	426804	7109682	8.6302295	9.8518502	12
49	427645	7106897	8.6310846	9.8516800	11
50	428487	7104112	8.6319388	9.8515099	10
51	429330	7101328	8.6327922	9.8513396	9
52	430174	7098544	8.6336447	9.8511693	8
53	431018	7095760	8.6344964	9.8509990	7
54	431863	7092977	8.6353472	9.8508286	6
55	432709	7090194	8.6361971	9.8506581	5
56	433556	7087411	8.6370462	9.8504877	4
57	434404	7084629	8.6378945	9.8503171	3
58	435253	7081847	8.6387419	9.8501465	2
59	436102	7079065	8.6395884	9.8499759	1
60	436952	7076283	8.6404342	9.8498052	0
	Natural Co. Versed Sine.	Natural Versed Sine.	Logarithm Co. Versed Sine.	Logarithm Versed Sine.	M.

73 DEGREES.



17 DEGREES.					
M.	Natural Versed Sine.	Natural Co-Versed Sine.	Logarithm Versed Sine.	Logarithm Co-Versed Sine.	
0	436952	7076283	8.6404342	9.8498052	60
1	437803	7073501	8.6412790	9.8496344	59
2	438655	7070720	8.6421231	9.8494636	58
3	439508	7067939	8.6429663	9.8492928	57
4	440361	7065158	8.6438087	9.8491219	56
5	441215	7062377	8.6446502	9.8489509	55
6	442070	7059597	8.6454909	9.8487799	54
7	442926	7056817	8.6463308	9.8486088	53
8	443782	7054037	8.6471698	9.8484377	52
9	444639	7051257	8.6479880	9.8482665	51
10	445498	7048477	8.6488454	9.8480953	50
11	446357	7045698	8.6496820	9.8479240	49
12	447216	7042919	8.6505177	9.8477527	48
13	448077	7040140	8.6513526	9.8475813	47
14	448938	7037362	8.6521867	9.8474099	46
15	449801	7034584	8.6530200	9.8472384	45
16	450664	7031806	8.6538524	9.8470669	44
17	451527	7029028	8.6546841	9.8468953	43
18	452392	7026250	8.6555149	9.8467237	42
19	453257	7023473	8.6563449	9.8465520	41
20	454124	7020696	8.6571741	9.8463802	40
21	454991	7017919	8.6580025	9.8462084	39
22	455859	7015143	8.6588301	9.8460366	38
23	456727	7012367	8.6596569	9.8458647	37
24	457597	7009591	8.6604829	9.8456927	36
25	458467	7006815	8.6613081	9.8455207	35
26	459338	7004040	8.6621324	9.8453487	34
27	460210	7001265	8.6629560	9.8451765	33
28	461083	6998490	8.6637788	9.8450044	32
29	461956	6995716	8.6646008	9.8448322	31
30	462830	6992942	8.6654220	9.8446599	30
	Natural Co-Versed Sine.	Natural Versed Sine.	Logarithm Co-Versed Sine.	Logarithm Versed Sine.	M.

72 DEGREES.

17 DEGREES.					
M.	Natural Versed Sine.	Natural Co-Versed Sine.	Logarithm Versed Sine.	Logarithm Co-Versed Sine.	
30	462830	6992942	8.6654210	9.8446599	30
31	463706	6990168	8.6662424	9.8444876	29
32	464582	6987394	8.6670620	9.8443152	28
33	465458	6984620	8.6678808	9.8441428	27
34	466336	6981847	8.6686988	9.8439703	26
35	467214	6979074	8.6695160	9.8437978	25
36	468093	6976301	8.6703324	9.8436252	24
37	468973	6973528	8.6711481	9.8434526	23
38	469854	6970756	8.6719630	9.8432799	22
39	470736	6967984	8.6727771	9.8431071	21
40	471618	6965212	8.6735904	9.8429344	20
41	472501	6962441	8.6744029	9.8427615	19
42	473385	6959670	8.6752147	9.8425886	18
43	474270	6956899	8.6760256	9.8424156	17
44	475156	6954128	8.6768358	9.8422427	16
45	476042	6951357	8.6776453	9.8420696	15
46	476929	6948587	8.6784539	9.8418965	14
47	477817	6945817	8.6792618	9.8417233	13
48	478706	6943047	8.6800689	9.8415501	12
49	479596	6940277	8.6808753	9.8413768	11
50	480486	6937508	8.6816809	9.8412035	10
51	481377	6934739	8.6824857	9.8410301	9
52	482269	6931970	8.6832897	9.8408567	8
53	483162	6929202	8.6840930	9.8406832	7
54	484056	6926434	8.6848956	9.8405097	6
55	484950	6923666	8.6856973	9.8403361	5
56	485846	6920898	8.6864984	9.8401625	4
57	486742	6918131	8.6872986	9.8399887	3
58	487639	6915364	8.6880981	9.8398150	2
59	488536	6912597	8.6888969	9.8396412	1
60	489435	6909830	8.6896949	9.8394674	0
	Natural Co-Versed Sine.	Natural Versed Sine.	Logarithm Co-Versed Sine.	Logarithm Versed Sine.	M.

72 DEGREES.



18 DEGREES.					
M.	Natural Versed Sine.	Natural Co-Versed Sine.	Logarithm Versed Sine.	Logarithm Co-Versed Sine.	
0	489435	6909830	8.6896949	9.8394674	60
1	490334	6907064	8.6904921	9.8392934	59
2	491234	6904298	8.6912886	9.8391195	58
3	492135	6901532	8.6920844	9.8389455	57
4	493037	6898766	8.6928794	9.8387714	56
5	493939	6896001	8.6936736	9.8385973	55
6	494843	6893236	8.6944672	9.8384233	54
7	495747	6890471	8.6952599	9.8382489	53
8	496652	6887706	8.6960520	9.8380746	52
9	497557	6884942	8.6968432	9.8379003	51
10	498464	6882178	8.6976338	9.8377259	50
11	499371	6879414	8.6984236	9.8375514	49
12	500279	6876651	8.6992127	9.8373770	48
13	501188	6873888	8.7000010	9.8372024	47
14	502098	6871125	8.7007886	9.8370278	46
15	503009	6868362	8.7015755	9.8368531	45
16	503920	6865600	8.7023617	9.8366785	44
17	504832	6862838	8.7031471	9.8365037	43
18	505745	6860076	8.7039318	9.8363289	42
19	506659	6857314	8.7047158	9.8361540	41
20	507574	6854552	8.7054990	9.8359791	40
21	508489	6851791	8.7062815	9.8358041	39
22	509405	6849030	8.7070633	9.8356291	38
23	510322	6846269	8.7078444	9.8354540	37
24	511240	6843509	8.7086247	9.8352789	36
25	512158	6840749	8.7094044	9.8351037	35
26	513078	6837989	8.7101833	9.8349285	34
27	513998	6835230	8.7109615	9.8347531	33
28	514919	6832471	8.7117390	9.8345778	32
29	515841	6829712	8.7125157	9.8344024	31
30	516763	6826953	8.7132918	9.8342269	30
	Natural Co-Versed Sine.	Natural Versed Sine.	Logarithm Co-Versed Sine.	Logarithm Versed Sine.	M.

71 DEGREES.

18 DEGREES.					
M.	Natural Versed Sine.	Natural Co-Versed Sine.	Logarithm Versed Sine.	Logarithm Co-Versed Sine.	
30	516763	6826953	8.7132918	9.8342269	30
31	517687	6824195	8.7140671	9.8340514	29
32	518611	6821437	8.7148418	9.8338759	28
33	519536	6818679	8.7156157	9.8337002	27
34	520462	6815921	8.7163889	9.8335246	26
35	521388	6813103	8.7171614	9.8333488	25
36	522316	6810406	8.7179332	9.8331731	24
37	523244	6807649	8.7187044	9.8329972	23
38	524173	6804892	8.7194748	9.8328213	22
39	525103	6802136	8.7202445	9.8326454	21
40	526034	6799380	8.7210135	9.8324694	20
41	526965	6796625	8.7217818	9.8322933	19
42	527897	6793870	8.7225494	9.8321172	18
43	528830	6791115	8.7233163	9.8319411	17
44	529764	6788360	8.7240825	9.8317649	16
45	530699	6785605	8.7248480	9.8315886	15
46	531634	6782850	8.7256129	9.8314123	14
47	532570	6780096	8.7263770	9.8312359	13
48	533507	6777342	8.7271404	9.8310595	12
49	534445	6774588	8.7279032	9.8308830	11
50	535384	6771835	8.7286653	9.8307064	10
51	536323	6769082	8.7294267	9.8305298	9
52	537264	6766329	8.7301874	9.8303532	8
53	538205	6763577	8.7309474	9.8301765	7
54	539146	6760825	8.7317067	9.8299997	6
55	540089	6758073	8.7324654	9.8298229	5
56	541032	6755321	8.7332233	9.8296461	4
57	541977	6752570	8.7339806	9.8294691	3
58	542922	6749819	8.7347373	9.8292922	2
59	543868	6747068	8.7354932	9.8291151	1
60	544814	6744318	8.7362485	9.8289381	0
	Natural Co-Versed Sine.	Natural Versed Sine.	Logarithm Co-Versed Sine.	Logarithm Versed Sine.	M.

71 DEGREES.



19 DEGREES.					
M.	Natural Versed Sine.	Natural Co-Versed Sine.	Logarithm Versed Sine.	Logarithm Co-Versed Sine.	
0	544810	6744318	8.7362485	9.8289381	60
1	545762	6741568	8.7370030	9.8287609	59
2	546710	6738818	8.7377570	9.8285837	58
3	547659	6736069	8.7385102	9.8284065	57
4	548609	6733319	8.7392628	9.8282292	56
5	549559	6730570	8.7400147	9.8280518	55
6	550511	6727821	8.7407659	9.8278744	54
7	551463	6725073	8.7415165	9.8276969	53
8	552416	6722325	8.7422664	9.8275194	52
9	553370	6719577	8.7430156	9.8273418	51
10	554325	6716829	8.7437642	9.8271642	50
11	555280	6714082	8.7445121	9.8269865	49
12	556236	6711335	8.7452593	9.8268088	48
13	557193	6708588	8.7460059	9.8266310	47
14	558151	6705841	8.7467518	9.8264532	46
15	559110	6703094	8.7474971	9.8262753	45
16	560069	6700348	8.7482417	9.8260973	44
17	561029	6697602	8.7489857	9.8259193	43
18	561990	6694856	8.7497290	9.8257412	42
19	562952	6692111	8.7504716	9.8255631	41
20	563915	6689366	8.7512136	9.8253849	40
21	564878	6686621	8.7519549	9.8252067	39
22	565843	6683877	8.7526956	9.8250284	38
23	566808	6681133	8.7534357	9.8248501	37
24	567773	6678389	8.7541751	9.8246717	36
25	568740	6675645	8.7549138	9.8244932	35
26	569707	6672902	8.7556519	9.8243147	34
27	570676	6670159	8.7563894	9.8241361	33
28	571645	6667415	8.7571262	9.8239576	32
29	572614	6664673	8.7578623	9.8237785	31
30	573585	6661931	8.7585979	9.8236002	30
	Natural Co-Versed Sine.	Natural Versed Sine.	Logarithm Co-Versed Sine.	Logarithm Versed Sine.	M.

70 DEGREES.

19 DEGREES.					
M.	Natural Versed Sine.	Natural Co-Versed Sine.	Logarithm Versed Sine.	Logarithm Co-Versed Sine.	
30	573585	6661931	8.7585979	9.8236002	30
31	574556	6659189	8.7593327	9.8234213	29
32	575529	6656447	8.7600670	9.8232425	28
33	576502	6653706	8.7608006	9.8230636	27
34	577475	6650965	8.7615336	9.8228847	26
35	578450	6648224	8.7622659	9.8227057	25
36	579425	6645484	8.7629976	9.8225266	24
37	580402	6642744	8.7637286	9.8223475	23
38	581379	6640004	8.7644591	9.8221684	22
39	582356	6637264	8.7651889	9.8219891	21
40	583335	6634525	8.7659180	9.8218099	20
41	584314	6631786	8.7666466	9.8216305	19
42	585295	6629047	8.7673745	9.8214511	18
43	586276	6626309	8.7681018	9.8212717	17
44	587257	6623571	8.7688284	9.8210922	16
45	588240	6620833	8.7695544	9.8209126	15
46	589223	6618095	8.7702798	9.8207330	14
47	590207	6615358	8.7710046	9.8205533	13
48	591192	6612621	8.7717288	9.8203736	12
49	592178	6609884	8.7724523	9.8201938	11
50	593164	6607148	8.7731752	9.8200140	10
51	594152	6604412	8.7738975	9.8198341	9
52	595140	6601676	8.7746192	9.8196542	8
53	596129	6598940	8.7753402	9.8194741	7
54	597119	6596205	8.7760607	9.8192941	6
55	598109	6593470	8.7767805	9.8191140	5
56	599101	6590735	8.7774997	9.8189338	4
57	600093	6588001	8.7782183	9.8187536	3
58	601086	6585267	8.7789363	9.8185733	2
59	602079	6582533	8.7796537	9.8183930	1
60	603074	6579799	8.7803705	9.8182126	0
	Natural Co-Versed Sine.	Natural Versed Sine.	Logarithm Co-Versed Sine.	Logarithm Versed Sine.	M.

70 DEGREES.



## VERSED SINES.

## 20 DEGREES.

M.	Natural Versed Sine.	Natural Co- Versed Sine.	Logarithm Versed Sine.	Logarithm Co- Versed Sine.	
0	603074	6579799	8.7803705	9.8182126	60
1	604069	6577066	8.7810863	9.8180321	59
2	605065	6574333	8.7818022	9.8178516	58
3	606062	6571600	8.7825168	9.8176711	57
4	607060	6568867	8.7832314	9.8174905	56
5	608058	6566135	8.7839499	9.8173098	55
6	609057	6563403	8.7846583	9.8171291	54
7	610057	6560671	8.7853705	9.8169483	53
8	611059	6557940	8.7860827	9.8167675	52
9	612060	6555209	8.7867937	9.8165865	51
10	613062	6552478	8.7875047	9.8164056	50
11	614066	6549747	8.7882146	9.8162246	49
12	615070	6547017	8.7889244	9.8160435	48
13	616075	6544287	8.7896330	9.8158624	47
14	617080	6541558	8.7903416	9.8156812	46
15	618087	6538829	8.7910491	9.8155000	45
16	619094	6536100	8.7917565	9.8153187	44
17	620102	6533371	8.7924627	9.8151373	43
18	621111	6530643	8.7931690	9.8149560	42
19	622120	6527915	8.7938740	9.8147745	41
20	623131	6525187	8.7945791	9.8145930	40
21	624142	6522460	8.7952830	9.8144114	39
22	625154	6519733	8.7959869	9.8142298	38
23	626167	6517006	8.7966896	9.8140481	37
24	627180	6514279	8.7973923	9.8138664	36
25	628194	6511553	8.7980938	9.8136846	35
26	629210	6509027	8.7987953	9.8135027	34
27	630226	6506101	8.7994957	9.8133208	33
28	631242	6503376	8.8001961	9.8131389	32
29	632260	6500651	8.8008953	9.8129568	31
30	633278	6497925	8.8015945	9.8127748	30
	Natural Co- Versed Sine.	Natural Versed Sine.	Logarithm Co- Versed Sine.	Logarithm Versed Sine.	M.

## 69 DEGREES.

## VERSED SINES.

## 20 DEGREES.

M.	Natural Versed Sine.	Natural Co- Versed Sine.	Logarithm Versed Sine.	Logarithm Co- Versed Sine.	
30	633278	6497925	8.8015945	9.8127748	30
31	634297	6495201	8.8022925	9.8125926	29
32	635317	6492477	8.8029906	9.8124104	28
33	636338	6489753	8.8036874	9.8122282	27
34	637359	6487029	8.8043843	9.8120459	26
35	638382	6484306	8.8050801	9.8118635	25
36	639405	6481583	8.8057758	9.8116811	24
37	640429	6478860	8.8064704	9.8114986	23
38	641453	6476138	8.8071649	9.8113161	22
39	642479	6473416	8.8078584	9.8111335	21
40	643505	6470694	8.8085518	9.8109509	20
41	644532	6467973	8.8092441	9.8107682	19
42	645560	6465252	8.8099364	9.8105854	18
43	646588	6462531	8.8106276	9.8104026	17
44	647618	6459810	8.8113187	9.8102197	16
45	648648	6457090	8.8120087	9.8100368	15
46	649679	6454370	8.8126988	9.8098538	14
47	650711	6451650	8.8133876	9.8096708	13
48	651743	6448930	8.8140765	9.8094877	12
49	652777	6446211	8.8147643	9.8093045	11
50	653811	6443492	8.8154521	9.8091213	10
51	654846	6440773	8.8161387	9.8089380	9
52	655881	6438055	8.8168253	9.8087547	8
53	656918	6435337	8.8175108	9.8085713	7
54	657955	6432620	8.8181964	9.8083879	6
55	658993	6429903	8.8188808	9.8082044	5
56	660032	6427186	8.8195652	9.8080208	4
57	661072	6424469	8.8202484	9.8078372	3
58	662112	6421753	8.8209317	9.8076536	2
59	663154	6419037	8.8216139	9.8074698	1
60	664196	6416321	8.8222901	9.8072860	0
	Natural Co- Versed Sine.	Natural Versed Sine.	Logarithm Co- Versed Sine.	Logarithm Versed Sine.	M.

## 69 DEGREES.



## 21 DEGREES.

M.	Natural Versed Sine.	Natural Co. Versed Sine.	Logarithm Versed Sine.	Logarithm Co. Versed Sine.	
0	664196	6416321	8.8222961	9.8072860	60
1	665239	6413605	8.8229772	9.8071022	59
2	666282	6410890	8.8236582	9.8069183	58
3	667327	6408175	8.8243382	9.8067343	57
4	668372	6405460	8.8250182	9.8065503	56
5	669418	6402746	8.8256970	9.8063662	55
6	670465	6400032	8.8263759	9.8061821	54
7	671512	6397318	8.8270537	9.8059979	53
8	672561	6394605	8.8277314	9.8058137	52
9	673610	6391892	8.8284081	9.8056294	51
10	674660	6389179	8.8290848	9.8054451	50
11	675710	6386467	8.8297604	9.8052606	49
12	676762	6383755	8.8304360	9.8050762	48
13	677814	6381043	8.8311105	9.8048916	47
14	678867	6378331	8.8317850	9.8047070	46
15	679921	6375620	8.8324584	9.8045224	45
16	680976	6372909	8.8331318	9.8043377	44
17	682031	6370198	8.8338041	9.8041529	43
18	683088	6367488	8.8344765	9.8039681	42
19	684145	6364778	8.8351477	9.8037832	41
20	685203	6362068	8.8358190	9.8035983	40
21	686261	6359358	8.8364892	9.8034133	39
22	687321	6356649	8.8371594	9.8032283	38
23	688381	6353940	8.8378285	9.8030431	37
24	689442	6351232	8.8384976	9.8028580	36
25	690504	6348524	8.8391657	9.8026727	35
26	691566	6345816	8.8398337	9.8024875	34
27	692630	6343108	8.8405007	9.8023021	33
28	693694	6340401	8.8411677	9.8021167	32
29	694759	6337698	8.8418337	9.8019313	31
30	695824	6334988	8.8424996	9.8017458	30
	Natural Co. Versed Sine.	Natural Versed Sine.	Logarithm Co. Versed Sine.	Logarithm Versed Sine.	M.

## 68 DEGREES.

## 21 DEGREES.

M.	Natural Versed Sine.	Natural Co. Versed Sine.	Logarithm Versed Sine.	Logarithm Co. Versed Sine.	
30	695824	6334988	8.8424996	9.8017458	30
31	696891	6332282	8.8431645	9.8015602	29
32	697958	6329576	8.8438294	9.8013746	28
33	699026	6326870	8.8444932	9.8011889	27
34	700095	6324165	8.8451570	9.8010031	26
35	701165	6321459	8.845818	9.8008173	25
36	702235	6318754	8.8464826	9.8006315	24
37	703306	6316049	8.8471443	9.8004455	23
38	704378	6313345	8.8478060	9.8002596	22
39	705451	6310641	8.8484667	9.8000735	21
40	706525	6307938	8.8491274	9.7998875	20
41	707599	6305235	8.8497870	9.7997013	19
42	708674	6302532	8.8504467	9.7995151	18
43	709750	6299830	8.8511053	9.7993288	17
44	710827	6297128	8.8517639	9.7991425	16
45	711904	6294426	8.8524215	9.7989561	15
46	712983	6291724	8.8530790	9.7987697	14
47	714062	6289023	8.8537356	9.7985831	13
48	715142	6286322	8.8543921	9.7983966	12
49	716222	6283621	8.8550476	9.7982109	11
50	717304	6280920	8.8557032	9.7980253	10
51	718386	6278220	8.8563576	9.7978395	9
52	719469	6275520	8.8570121	9.7976548	8
53	720553	6272820	8.8576656	9.7974699	7
54	721637	6270122	8.8583191	9.7972850	6
55	722723	6267423	8.8589715	9.7970999	5
56	723809	6264725	8.8596240	9.7969150	4
57	724896	6262027	8.8602754	9.7967301	3
58	725984	6259329	8.8609268	9.7965452	2
59	727072	6256631	8.8615773	9.7963603	1
60	728161	6253934	8.8622277	9.7961754	0
	Natural Co. Versed Sine.	Natural Versed Sine.	Logarithm Co. Versed Sine.	Logarithm Versed Sine.	M.

## 68 DEGREES.



22 DEGREES.					
M.	Natural Versed Sine.	Natural Co-Versed Sine.	Logarithm Versed Sine.	Logarithm Co-Versed Sine.	
0	728161	6253934	8.86222 77	9.7961533	60
1	729251	6251237	8.8628771	9.7959659	59
2	730342	6248540	8.8633265	9.7957786	58
3	731434	6245844	8.8641749	9.7955911	57
4	732526	6243148	8.8648233	9.7954037	56
5	733619	6240452	8.8654707	9.7952161	55
6	734713	6237757	8.8661181	9.7950285	54
7	735808	6235062	8.8667645	9.7948408	53
8	736904	6232367	8.8674109	9.7946531	52
9	738000	6229673	8.8680553	9.7944652	51
10	739097	6226979	8.8687018	9.7942774	50
11	740195	6224285	8.8693462	9.7940895	49
12	741294	6221592	8.8699906	9.7939015	48
13	742394	6218898	8.8706340	9.7937135	47
14	743494	6216206	8.8712774	9.7935254	46
15	744595	6213514	8.8719198	9.7933372	45
16	745697	6210822	8.8725623	9.7931491	44
17	746800	6208130	8.8732037	9.7929608	43
18	747903	6205438	8.8738452	9.7927725	42
19	749007	6202747	8.8744856	9.7925841	41
20	750112	6200056	8.8751261	9.7923956	40
21	751218	6197365	8.8757656	9.7922071	39
22	752324	6194675	8.8764051	9.7920187	38
23	753431	6191985	8.8770436	9.7918299	37
24	754539	6189296	8.8776821	9.7916413	36
25	755648	6186607	8.8783196	9.7914525	35
26	756758	6183918	8.8789571	9.7912637	34
27	757869	6181229	8.8795937	9.7910748	33
28	758980	6178541	8.8802303	9.7908859	32
29	760092	6175853	8.8808659	9.7906969	31
30	761205	6173166	8.8815014	9.7905079	30
	Natural Co-Versed Sine.	Natural Versed Sine.	Logarithm Co-Versed Sine.	Logarithm Versed Sine.	M.

67 DEGREES.

22 DEGREES.					
M.	Natural Versed Sine.	Natural Co-Versed Sine.	Logarithm Versed Sine.	Logarithm Co-Versed Sine.	
30	761205	6173166	8.8815014	9.7905079	30
31	762318	6170479	8.8821361	9.7903188	29
32	763432	6167792	8.8827707	9.7901297	28
33	764547	6165105	8.8834044	9.7899404	27
34	765663	6162419	8.8840380	9.7897512	26
35	766780	6159733	8.8846707	9.7895618	25
36	767897	6157047	8.8853034	9.7893725	24
37	769015	6154362	8.8859352	9.7891830	23
38	770134	6151677	8.8865669	9.7889935	22
39	771254	6148992	8.8871977	9.7888039	21
40	772375	6146308	8.8878285	9.7886143	20
41	773496	6143624	8.8884584	9.7884245	19
42	774618	6140940	8.8890882	9.7882348	18
43	775741	6138257	8.8897171	9.7880450	17
44	776865	6135574	8.8903460	9.7878551	16
45	777990	6132891	8.8909739	9.7876652	15
46	779116	6130209	8.8916019	9.7874752	14
47	780242	6127527	8.8922289	9.7872851	13
48	781369	6124844	8.8928559	9.7870950	12
49	782496	6122162	8.8934820	9.7869048	11
50	783624	6119482	8.8941080	9.7867146	10
51	784753	6116801	8.8947331	9.7865242	9
52	785883	6114120	8.8953583	9.7863340	8
53	787014	6111440	8.8959825	9.7861435	7
54	788145	6108760	8.8966066	9.7859531	6
55	789277	6106081	8.8972299	9.7857625	5
56	790410	6103402	8.8978532	9.7855720	4
57	791544	6100723	8.8984755	9.7853813	3
58	792679	6098043	8.8990978	9.7851906	2
59	793815	6095367	8.8997192	9.7849998	1
60	794951	6092689	8.9003406	9.7848090	0
	Natural Co-Versed Sine.	Natural Versed Sine.	Logarithm Co-Versed Sine.	Logarithm Versed Sine.	M.

67 DEGREES.



23 DEGREES.					
M.	Natural Versed Sine.	Natural Co-Versed Sine.	Logarithm Versed Sine.	Logarithm Co-Versed Sine.	
0	794951	6092689	8.903436	9.7848090	60
1	796088	6090011	8.9009611	9.7846181	59
2	797226	6087334	8.9015816	9.7844271	58
3	798365	6084657	8.9022011	9.7842361	57
4	799504	6081980	8.9020207	9.7840450	56
5	800644	6079304	8.9034393	9.7838539	55
6	801785	6076628	8.9040579	9.7836627	54
7	802927	6073952	8.9046757	9.7834714	53
8	804069	6071277	8.9052934	9.7832801	52
9	805212	6068602	8.9059102	9.7830887	51
10	806356	6065928	8.9065270	9.7828973	50
11	807501	6063254	8.9071429	9.7827058	49
12	808647	6060580	8.9077588	9.7825143	48
13	809793	6057907	8.9083738	9.7823226	47
14	810940	6055234	8.9089887	9.7821309	46
15	812088	6052561	8.9096028	9.7819392	45
16	813237	6049888	8.9102169	9.7817474	44
17	814386	6047216	8.9108301	9.7815555	43
18	815536	6044544	8.9114432	9.7813636	42
19	816687	6041872	8.9120555	9.7811716	41
20	817839	6039201	8.9126678	9.7809796	40
21	818991	6036530	8.9132792	9.7807874	39
22	820145	6033860	8.9138905	9.7805953	38
23	821299	6031190	8.9145010	9.7804030	37
24	822454	6028520	8.9151115	9.7802108	36
25	823609	6025851	8.9157211	9.7800184	35
26	824766	6023182	8.9163306	9.7798260	34
27	825923	6020513	8.9169393	9.7796335	33
28	827081	6017845	8.9175480	9.7794410	32
29	828240	6015177	8.9181558	9.7792484	31
30	829399	6012509	8.9187636	9.7790558	30
Natural Co-Versed Sine.	Natural Versed Sine.	Logarithm Co-Versed Sine.	Logarithm Versed Sine.	M.	

66 DEGREES.

23 DEGREES.					
M	Natural Versed Sine.	Natural Co-Versed Sine.	Logarithm Versed Sine.	Logarithm Co-Versed Sine.	
30	829399	6012509	8.9187636	9.7790558	30
31	830560	6009841	8.9193706	9.7788630	29
32	831721	6007174	8.9199775	9.7786703	28
33	832882	6004507	8.9205835	9.7784774	27
34	834045	6001841	8.9211895	9.7782845	26
35	835209	5999175	8.9217947	9.7780915	25
36	836373	5996509	8.9223999	9.7778985	24
37	837538	5993844	8.9230041	9.7777054	23
38	838703	5991179	8.9236084	9.7775123	22
39	839870	5988514	8.9242118	9.7773191	21
40	841037	5985850	8.9248152	9.7771258	20
41	842205	5983186	8.9254177	9.7769325	19
42	843374	5980522	8.9260202	9.7767391	18
43	844544	5977859	8.9266219	9.7765456	17
44	845714	5975196	8.9272235	9.7763521	16
45	846885	5972533	8.9278243	9.7761585	15
46	848057	5969870	8.9284251	9.7759649	14
47	849230	5967208	8.9290250	9.7757712	13
48	850403	5964546	8.9296249	9.7755775	12
49	851578	5961885	8.9302240	9.7753836	11
50	852753	5959224	8.9308231	9.7751898	10
51	853928	5956563	8.9314212	9.7749958	9
52	855105	5953903	8.9320194	9.7748018	8
53	856282	5951243	8.9326168	9.7746077	7
54	857460	5948584	8.9332141	9.7744136	6
55	858639	5945925	8.9338106	9.7742194	5
56	859819	5943266	8.9344070	9.7740252	4
57	860999	5940608	8.9350027	9.7738308	3
58	862181	5937950	8.9355983	9.7736365	2
59	863363	5935292	8.9361930	9.7734420	1
60	864545	5932634	8.9367878	9.7732475	0
Natural Co-Versed Sine.	Natural Versed Sine.	Logarithm Co-Versed Sine.	Logarithm Versed Sine.	M.	

66 DEGREES.

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24 DEGREES.					
M.	Natural Versed Sine.	Natural Co-Versed Sine.	Logarithm Versed Sine.	Logarithm Co-Versed Sine.	
0	864545	5932634	8.9367878	9.7732475	60
1	865729	5929977	8.9373817	9.7730529	59
2	866913	5927320	8.9379756	9.7728583	58
3	868098	5924663	8.9385687	9.7726636	57
4	869284	5922007	8.9391618	9.7724689	56
5	870471	5919351	8.9397540	9.7722741	55
6	871658	5916695	8.9403462	9.7720792	54
7	872846	5914040	8.9409376	9.7718842	53
8	874035	5911385	8.9415290	9.7716893	52
9	875225	5908731	8.9421195	9.7714942	51
10	876416	5906077	8.9427101	9.7712991	50
11	877607	5903423	8.9432998	9.7711039	49
12	878799	5900769	8.9438895	9.7709087	48
13	879992	5898116	8.9444783	9.7707133	47
14	881185	5895463	8.9450672	9.7705180	46
15	882380	5892811	8.9456552	9.7703225	45
16	883575	5890159	8.9462433	9.7701271	44
17	884771	5887507	8.9468305	9.7699315	43
18	885967	5884856	8.9474177	9.7697359	42
19	887165	5882205	8.9480040	9.7695402	41
20	888363	5879554	8.9485904	9.7693444	40
21	889562	5876904	8.9491759	9.7691486	39
22	890762	5874254	8.9497615	9.7689528	38
23	891962	5871603	8.9503462	9.7687568	37
24	893163	5868956	8.9509309	9.7685608	36
25	894365	5866307	8.9515148	9.7683647	35
26	895568	5863656	8.9520982	9.7681687	34
27	896771	5861011	8.9526818	9.7679724	33
28	897976	5858363	8.9532648	9.7677762	32
29	899181	5855711	8.9538471	9.7675799	31
30	900387	5853064	8.9544294	9.7673835	30
	Natural Co-Versed Sine.	Natural Versed Sine.	Logarithm Co-Versed Sine.	Logarithm Versed Sine.	M.

65 DEGREES.

24 DEGREES.					
M	Natural Versed Sine.	Natural Co-Versed Sine.	Logarithm Versed Sine.	Logarithm Co-Versed Sine.	
30	900387	5853068	8.9544294	9.7673835	30
31	901594	5850421	8.9550108	9.7671871	29
32	902801	5847774	8.9555922	9.7669906	28
33	904010	5845128	8.9561729	9.7667940	27
34	905219	5842482	8.9567535	9.7665974	26
35	906428	5839837	8.9573333	9.7664007	25
36	907639	5837192	8.9579131	9.7662040	24
37	908850	5834547	8.9584921	9.7660071	23
38	910062	5831903	8.9590711	9.7658103	22
39	911275	5829259	8.9596493	9.7656133	21
40	912489	5826615	8.9602275	9.7654164	20
41	913703	5823972	8.9608049	9.7652193	19
42	914918	5821329	8.9613823	9.7650222	18
43	916134	5818687	8.9619580	9.7648249	17
44	917351	5816045	8.9625335	9.7646277	16
45	918568	5813403	8.9631112	9.7644304	15
46	919786	5810761	8.9636870	9.7642330	14
47	921005	5808120	8.9642620	9.7640355	13
48	922225	5805479	8.9648370	9.7638381	12
49	923446	5802838	8.9654122	9.7636405	11
50	924667	5800198	8.9659854	9.7634429	10
51	925889	5797558	8.9665588	9.7632451	9
52	927112	5794919	8.9671322	9.7630474	8
53	928335	5792280	8.9677048	9.7628496	7
54	929560	5789641	8.9682774	9.7626517	6
55	930785	5787003	8.9688492	9.7624537	5
56	932011	5784365	8.9694210	9.7622557	4
57	933238	5781727	8.9699900	9.7620576	3
58	934465	5779090	8.9705630	9.7618595	2
59	935693	5776453	8.9711333	9.7616613	1
60	936922	5773817	8.9717035	9.7614630	0
	Natural Co-Versed Sine.	Natural Versed Sine.	Logarithm Co-Versed Sine.	Logarithm Versed Sine.	M.

65 DEGREES.

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25 DEGREES.					
M.	Natural Versed Sine.	Natural Co-Versed Sine.	Logarithm Versed Sine.	Logarithm Co-Versed Sine.	
0	936922	5773817	8.9717035	9.7614630	60
1	938152	5771181	8.9722729	9.7612647	59
2	939382	5768545	8.9728424	9.7610663	58
3	940614	5765910	8.9734111	9.7608678	57
4	941846	5763275	8.9739797	9.7606693	56
5	943078	5760640	8.9745476	9.7604707	55
6	944312	5758006	8.9751155	9.7602721	54
7	945546	5755372	8.9756826	9.7600733	53
8	946781	5752738	8.9762497	9.7598746	52
9	948017	5750105	8.9768161	9.7596757	51
10	949254	5747472	8.9773824	9.7594769	50
11	950491	5744839	8.9779480	9.7592779	49
12	951729	5742207	8.9785135	9.7590789	48
13	952968	5739575	8.9790783	9.7588797	47
14	954208	5736944	8.9796431	9.7586806	46
15	955449	5734313	8.9802071	9.7584813	45
16	956690	5731682	8.9807711	9.7582821	44
17	957932	5729051	8.9813344	9.7580827	43
18	959175	5726421	8.9818976	9.7578833	42
19	960418	5723794	8.9824601	9.7576838	41
20	961662	5721162	8.9830226	9.7574843	40
21	962907	5718533	8.9835843	9.7572846	39
22	964153	5715904	8.9841460	9.7570850	38
23	965400	5713276	8.9847070	9.7568852	37
24	966647	5710648	8.9852679	9.7566854	36
25	967895	5708021	8.9858281	9.7564855	35
26	969144	5705394	8.9863883	9.7562856	34
27	970394	5702767	8.9869478	9.7560856	33
28	971644	5700141	8.9875072	9.7558856	32
29	972895	5697515	8.9880669	9.7556854	31
30	974147	5694889	8.9886246	9.7554853	30
	Natural Versed Sine.	Natural Co-Versed Sine.	Logarithm Versed Sine.	Logarithm Co-Versed Sine.	M.

64 DEGREES.

25 DEGREES.					
M.	Natural Versed Sine.	Natural Co-Versed Sine.	Logarithm Versed Sine.	Logarithm Co-Versed Sine.	
30	974147	5694889	8.9886246	9.7554853	30
31	975400	5692264	8.9891825	9.7552850	29
32	976653	5689639	8.9897404	9.7550847	28
33	977908	5687014	8.9902976	9.7548843	27
34	979162	5684390	8.9908548	9.7546839	26
35	980418	5681766	8.9914112	9.7544838	25
36	981675	5679142	8.9919676	9.7542828	24
37	982932	5676519	8.9925233	9.7540821	23
38	984190	5673896	8.9930790	9.7538814	22
39	985449	5671274	8.9936339	9.7536806	21
40	986708	5668652	8.9941888	9.7534798	20
41	987969	5666030	8.9947430	9.7532789	19
42	989230	5663409	8.9952972	9.7530779	18
43	990492	5660788	8.9958506	9.7528769	17
44	991754	5658167	8.9964041	9.7526758	16
45	993018	5655547	8.9969568	9.7524746	15
46	994282	5652927	8.9975095	9.7522734	14
47	995547	5650307	8.9980614	9.7520721	13
48	996812	5647688	8.9986134	9.7518708	12
49	998079	5645069	8.9991646	9.7516693	11
50	999346	5642451	8.9997158	9.7514679	10
51	1000614	5639833	9.0002663	9.7512663	9
52	1001883	5637215	9.0008168	9.7510647	8
53	1003152	5634598	9.0013666	9.7508630	7
54	1004422	5631981	9.0019163	9.7506613	6
55	1005694	5629365	9.0024653	9.7504594	5
56	1006965	5626749	9.0030144	9.7502576	4
57	1008237	5624133	9.0035626	9.7500556	3
58	1009511	5621518	9.0041109	9.7498536	2
59	1010785	5618903	9.0046585	9.7496515	1
60	1012060	5616288	9.0052061	9.7494494	0
	Natural Versed Sine.	Natural Co-Versed Sine.	Logarithm Versed Sine.	Logarithm Co-Versed Sine.	M.

64 DEGREES.



26 DEGREES.					
M.	Natural Versed Sine.	Natural Co-Versed Sine.	Logarithm Versed Sine.	Logarithm Co-Versed Sine.	
0	1012060	5616288	9.0052061	9.7494494	60
1	1013335	5613674	9.0057529	9.7492472	59
2	1014613	5611060	9.0062997	9.7490449	58
3	1015888	5608446	9.0068458	9.7488426	57
4	1017166	5605833	9.0073920	9.7486402	56
5	1018445	5603220	9.0079344	9.7484377	55
6	1019724	5600608	9.0084827	9.7482352	54
7	1021004	5597926	9.0090274	9.7480326	53
8	1022285	5595384	9.0095721	9.7478299	52
9	1023567	5592773	9.0101160	9.7476272	51
10	1024849	5590162	9.0106600	9.7474244	50
11	1026132	5587551	9.0112032	9.7472215	49
12	1027416	5584941	9.0117465	9.7470186	48
13	1028701	5582331	9.0122890	9.7468156	47
14	1029986	5579722	9.0128315	9.7466126	46
15	1031273	5577113	9.0133733	9.7464094	45
16	1032560	5574504	9.0139154	9.7462063	44
17	1033847	5571896	9.0144562	9.7460030	43
18	1035136	5569288	9.0149973	9.7457997	42
19	1036425	5566680	9.0155377	9.7455963	41
20	1037715	5564073	9.0160781	9.7453928	40
21	1039006	5561466	9.0166177	9.7451893	39
22	1040297	5558860	9.0171574	9.7449857	38
23	1041588	5556254	9.0176964	9.7447821	37
24	1042882	5553648	9.0182353	9.7445784	36
25	1044176	5551043	9.0187736	9.7443745	35
26	1045471	5548438	9.0193119	9.7441707	34
27	1046766	5545833	9.0198494	9.7439668	33
28	1048062	5543229	9.0203870	9.7437628	32
29	1049359	5540625	9.0209238	9.7435587	31
30	1050656	5538022	9.0214607	9.7433547	30
	Natural Co-Versed Sine.	Natural Versed Sine.	Logarithm Co-Versed Sine.	Logarithm Versed Sine.	M.

63 DEGREES.

26 DEGREES.					
M.	Natural Versed Sine.	Natural Co-Versed Sine.	Logarithm Versed Sine.	Logarithm Co-Versed Sine.	
30	1050656	5538022	9.0214607	9.7433547	30
31	1051955	5535419	9.0219969	9.7431505	29
32	1053254	5532816	9.0225330	9.7429462	28
33	1054554	5530214	9.0230685	9.7427419	27
34	1055854	5527612	9.0236039	9.7425375	26
35	1057156	5525010	9.0241387	9.7423331	25
36	1058458	5522409	9.0246735	9.7421286	24
37	1059760	5519808	9.0252076	9.7419240	23
38	1061064	5517208	9.0257416	9.7417193	22
39	1062368	5514608	9.0262750	9.7415146	21
40	1063674	5512008	9.0268084	9.7413099	20
41	1064979	5509409	9.0273411	9.7411050	19
42	1066286	5506810	9.0278738	9.7409001	18
43	1067594	5504212	9.0284058	9.7406951	17
44	1068902	5501614	9.0289378	9.7404901	16
45	1070211	5499016	9.0294691	9.7402849	15
46	1071520	5496418	9.0300004	9.7400798	14
47	1072831	5493821	9.0305310	9.7398745	13
48	1074142	5491224	9.0310616	9.7396692	12
49	1075451	5488628	9.0315916	9.7394638	11
50	1076766	5486032	9.0321215	9.7392584	10
51	1078080	5483437	9.0326508	9.7390528	9
52	1079394	5480842	9.0331800	9.7388473	8
53	1080709	5478242	9.0337086	9.7386416	7
54	1082025	5475653	9.0342372	9.7384359	6
55	1083341	5473059	9.0347651	9.7382301	5
56	1084658	5470465	9.0352930	9.7380243	4
57	1085976	5467872	9.0358202	9.7378183	3
58	1087295	5465279	9.0363474	9.7376124	2
59	1088615	5462687	9.0368740	9.7374063	1
60	1089935	5460095	9.0374005	9.7372002	0
	Natural Co-Versed Sine.	Natural Versed Sine.	Logarithm Co-Versed Sine.	Logarithm Versed Sine.	M.

63 DEGREES.



27 DEGREES.					
M.	Natural Versed Sine.	Natural Co-Versed Sine.	Logarithm Versed Sine.	Logarithm Co-Versed Sine.	
0	1089935	5460095	9.374005	9.7372002	60
1	1091256	5455703	9.0374264	9.7369740	59
2	1092577	5451312	9.0384522	9.7367878	58
3	1093900	5446921	9.0389774	9.7365814	57
4	1095223	5442530	9.0395026	9.7363750	56
5	1096547	5438140	9.0400272	9.7361686	55
6	1097872	5433750	9.0405517	9.7359621	54
7	1099197	5429360	9.0410755	9.7357554	53
8	1100524	5424970	9.0415994	9.7355488	52
9	1101851	5420580	9.0421232	9.7353421	51
10	1103178	5416190	9.0426470	9.7351353	50
11	1104507	5411800	9.0431708	9.7349284	49
12	1105836	5407410	9.0436946	9.7347215	48
13	1107166	5403020	9.0442184	9.7345145	47
14	1108497	5398630	9.0447422	9.7343074	46
15	1109829	5394240	9.0452660	9.7341003	45
16	1111161	5389850	9.0457898	9.7338931	44
17	1112494	5385460	9.0463136	9.7336858	43
18	1113828	5381070	9.0468374	9.7334785	42
19	1115162	5376680	9.0473612	9.7332711	41
20	1116497	5372290	9.0478850	9.7330636	40
21	1117834	5367900	9.0484088	9.7328560	39
22	1119170	5363510	9.0489326	9.7326485	38
23	1120508	5359120	9.0494564	9.7324408	37
24	1121846	5354730	9.0499802	9.7322331	36
25	1123185	5350340	9.0505040	9.7320252	35
26	1124525	5345950	9.0510278	9.7318174	34
27	1125866	5341560	9.0515516	9.7316094	33
28	1127207	5337170	9.0520754	9.7314014	32
29	1128549	5332780	9.0525992	9.7311933	31
30	1129892	5328390	9.0531230	9.7309852	30
	Natural Co-Versed Sine.	Natural Versed Sine.	Logarithm Co-Versed Sine.	Logarithm Versed Sine.	M.

62 DEGREES.

27 DEGREES.					
M	Natural Versed Sine.	Natural Co-Versed Sine.	Logarithm Versed Sine.	Logarithm Co-Versed Sine.	
30	1129892	5328390	9.0531230	9.7309852	30
31	1131235	5323999	9.0535528	9.7307769	29
32	1132580	5319608	9.0539826	9.7305686	28
33	1133925	5315217	9.0544124	9.7303603	27
34	1135270	5310826	9.0548422	9.7301519	26
35	1136617	5306435	9.0552720	9.7299433	25
36	1137964	5302044	9.0557018	9.7297348	24
37	1139312	5297653	9.0561316	9.7295261	23
38	1140661	5293262	9.0565614	9.7293175	22
39	1142011	5288871	9.0569912	9.7291087	21
40	1143361	5284480	9.0574210	9.7288999	20
41	1144712	5280089	9.0578508	9.7286909	19
42	1146064	5275698	9.0582806	9.7284820	18
43	1147416	5271307	9.0587104	9.7282729	17
44	1148770	5266916	9.0591402	9.7280638	16
45	1150124	5262525	9.0595700	9.7278546	15
46	1151478	5258134	9.0600000	9.7276454	14
47	1152834	5253743	9.0604300	9.7274360	13
48	1154191	5249352	9.0608600	9.7272267	12
49	1155547	5244961	9.0612900	9.7270172	11
50	1156905	5240570	9.0617200	9.7268077	10
51	1158264	5236179	9.0621500	9.7265981	9
52	1159623	5231788	9.0625800	9.7263885	8
53	1160983	5227397	9.0630100	9.7261787	7
54	1162344	5223006	9.0634400	9.7259689	6
55	1163705	5218615	9.0638700	9.7257590	5
56	1165068	5214224	9.0643000	9.7255491	4
57	1166431	5209833	9.0647300	9.7253391	3
58	1167794	5205442	9.0651600	9.7251290	2
59	1169159	5201051	9.0655900	9.7249188	1
60	1170524	5196660	9.0660200	9.7247087	0
	Natural Co-Versed Sine.	Natural Versed Sine.	Logarithm Co-Versed Sine.	Logarithm Versed Sine.	M.

62 DEGREES.

S s



28 DEGREES.					
M.	Natural Versed Sine.	Natural Co-Versed Sine.	Logarithm Versed Sine.	Logarithm Co-Versed Sine.	
0	1170524	5305284	9.0683803	9.7247087	60
1	1171890	5302716	9.0688867	9.7244983	59
2	1173257	5300148	9.0693931	9.7242880	58
3	1174624	5297581	9.0698988	9.7240776	57
4	1175993	5295014	9.0704046	9.7238671	56
5	1177362	5292447	9.0709097	9.7236565	55
6	1178731	5289881	9.0714148	9.7234459	54
7	1180102	5287315	9.0719193	9.7232352	53
8	1181473	5284750	9.0724238	9.7230244	52
9	1182845	5282185	9.0729227	9.7228136	51
10	1184218	5279620	9.0734316	9.7226037	50
11	1185591	5277056	9.0739348	9.7223917	49
12	1186965	5274492	9.0744381	9.7221807	48
13	1188340	5271929	9.0749407	9.7219695	47
14	1189716	5269366	9.0754434	9.7217584	46
15	1191093	5266803	9.0759454	9.7215471	45
16	1192470	5264241	9.0764474	9.7213358	44
17	1193848	5261679	9.0769488	9.7211243	43
18	1195226	5259118	9.0774502	9.7209129	42
19	1196606	5256557	9.0779510	9.7207013	41
20	1197986	5253996	9.0784518	9.7204898	40
21	1199367	5251436	9.0789519	9.7202781	39
22	1200749	5248876	9.0794521	9.7200663	38
23	1202131	5246317	9.0799517	9.7198545	37
24	1203514	5243758	9.0804512	9.7196426	36
25	1204898	5241199	9.0809502	9.7194306	35
26	1206283	5238641	9.0814491	9.7192186	34
27	1207668	5236083	9.0819475	9.7190065	33
28	1209054	5233526	9.0824458	9.7187944	32
29	1210441	5230969	9.0829436	9.7185821	31
30	1211829	5228412	9.0834413	9.7183698	30
	Natural Co-Versed Sine.	Natural Versed Sine.	Logarithm Co-Versed Sine.	Logarithm Versed Sine.	M.

61 DEGREES.

28 DEGREES.					
M	Natural Versed Sine.	Natural Co-Versed Sine.	Logarithm Versed Sine.	Logarithm Co-Versed Sine.	
30	1211829	5228412	9.0834413	9.7183698	30
31	1213217	5225856	9.0839384	9.7181574	29
32	1214606	5223300	9.0844356	9.7179450	28
33	1215996	5220745	9.0849321	9.7177325	27
34	1217387	5218190	9.0854286	9.7175199	26
35	1218778	5215635	9.0859245	9.7173072	25
36	1220170	5213081	9.0864204	9.7170945	24
37	1221563	5210527	9.0869157	9.7168817	23
38	1222957	5207974	9.0874111	9.7166688	22
39	1224351	5205421	9.0879058	9.7164559	21
40	1225746	5202868	9.0884005	9.7162429	20
41	1227142	5200316	9.0888946	9.7160298	19
42	1228538	5197764	9.0893887	9.7158166	18
43	1229936	5195213	9.0898822	9.7156034	17
44	1231334	5192662	9.0903758	9.7153901	16
45	1232732	5190112	9.0908687	9.7151767	15
46	1234132	5187562	9.0913616	9.7149633	14
47	1235532	5185012	9.0918539	9.7147498	13
48	1236933	5182463	9.0923462	9.7145362	12
49	1238335	5179914	9.0928380	9.7143225	11
50	1239737	5177365	9.0933297	9.7141089	10
51	1241141	5174817	9.0938208	9.7138950	9
52	1242545	5172269	9.0943120	9.7136812	8
53	1243949	5169722	9.0948025	9.7134672	7
54	1245355	5167175	9.0952931	9.7132533	6
55	1246761	5164629	9.0957830	9.7130392	5
56	1248168	5162083	9.0962730	9.7128250	4
57	1249575	5159538	9.0967624	9.7126108	3
58	1250984	5156993	9.0972517	9.7123965	2
59	1252393	5154448	9.0977405	9.7121821	1
60	1253803	5151904	9.0982293	9.7119677	0
	Natural Co-Versed Sine.	Natural Versed Sine.	Logarithm Co-Versed Sine.	Logarithm Versed Sine.	M.

61 DEGREES.

S s 2



29 DEGREES.					
M.	Natural Versed Sine.	Natural Co-Versed Sine.	Logarithm Versed Sine.	Logarithm Co-Versed Sine.	
0	1253803	5151914	9.0982293	9.7119677	60
1	1255214	5159360	9.0987175	9.7117532	59
2	1256625	5146816	9.0992057	9.7115387	58
3	1258037	5144273	9.0996933	9.7113240	57
4	1259450	5141730	9.1001809	9.7111093	56
5	1260863	5139188	9.1006679	9.7108945	55
6	1262278	5136646	9.1011549	9.7106797	54
7	1263693	5134105	9.1016414	9.7104647	53
8	1265109	5131564	9.1021278	9.7102497	52
9	1266525	5129023	9.1026130	9.7100346	51
10	1267942	5126483	9.1030995	9.7098195	50
11	1269360	5123943	9.1035848	9.7096042	49
12	1270779	5121404	9.1040701	9.7093890	48
13	1272199	5118865	9.1045548	9.7091736	47
14	1273619	5116326	9.1050395	9.7089582	46
15	1275040	5113788	9.1055236	9.7087426	45
16	1276462	5111250	9.1060078	9.7085271	44
17	1277884	5108713	9.1064913	9.7083114	43
18	1279307	5106176	9.1069749	9.7080957	42
19	1280731	5103639	9.1074578	9.7078799	41
20	1282156	5101103	9.1079408	9.7076641	40
21	1283581	5098567	9.1084232	9.7074481	39
22	1285007	5096032	9.1089056	9.7072321	38
23	1286434	5093497	9.1093875	9.7070160	37
24	1287862	5090963	9.1098693	9.7067999	36
25	1289290	5088429	9.1103506	9.7065836	35
26	1290719	5085895	9.1108318	9.7063674	34
27	1292149	5083362	9.1113125	9.7061510	33
28	1293580	5080829	9.1117932	9.7059346	32
29	1295011	5078297	9.1122733	9.7057180	31
30	1296443	5075765	9.1127534	9.7055015	30
	Natural Co-Versed Sine.	Natural Versed Sine.	Logarithm Co-Versed Sine.	Logarithm Versed Sine.	M.
	60	DEGREES.			

29 DEGREES.					
M.	Natural Versed Sine.	Natural Co-Versed Sine.	Logarithm Versed Sine.	Logarithm Co-Versed Sine.	
30	1296443	5075765	9.1127534	9.7055015	30
31	1297876	5073233	9.1132330	9.7052848	29
32	1299309	5070702	9.1137126	9.7050681	28
33	1300744	5068171	9.1141915	9.7048512	27
34	1302179	5065641	9.1146705	9.7046344	26
35	1303614	5063111	9.1151490	9.7044174	25
36	1305051	5060582	9.1156274	9.7042004	24
37	1306488	5058053	9.1161052	9.7039833	23
38	1307926	5055524	9.1165831	9.7037661	22
39	1309364	5052996	9.1170604	9.7035489	21
40	1310804	5050468	9.1175377	9.7033316	20
41	1312244	5047941	9.1180145	9.7031142	19
42	1313685	5045414	9.1184912	9.7028967	18
43	1315126	5042887	9.1189674	9.7026792	17
44	1316569	5040361	9.1194436	9.7024616	16
45	1318012	5037835	9.1199192	9.7022439	15
46	1319456	5035310	9.1203948	9.7020262	14
47	1320900	5032785	9.1208699	9.7018083	13
48	1322345	5030260	9.1213449	9.7015905	12
49	1323791	5027736	9.1218194	9.7013725	11
50	1325238	5025212	9.1222939	9.7011545	10
51	1326686	5022689	9.1227679	9.7009363	9
52	1328134	5020166	9.1232419	9.7007182	8
53	1329583	5017644	9.1237153	9.7004999	7
54	1331033	5015122	9.1241887	9.7002816	6
55	1332483	5012601	9.1246615	9.7000631	5
56	1333934	5010080	9.1251344	9.6998447	4
57	1335386	5007559	9.1256057	9.6996271	3
58	1336839	5005039	9.1260790	9.6994075	2
59	1338292	5002519	9.1265507	9.6991887	1
60	1339746	5000000	9.1270225	9.6989700	0
	Natural Co-Versed Sine.	Natural Versed Sine.	Logarithm Co-Versed Sine.	Logarithm Versed Sine.	M.
	60	DEGREES.			



30 DEGREES.					
M.	Natural Versed Sine.	Natural Co- Versed Sine.	Logarithm Versed Sine.	Logarithm Co- Versed Sine.	
0	1339746	5000000	9.1270225	9.6989700	60
1	1341201	4997481	9.1274937	9.6987511	59
2	1342656	4994962	9.1279649	9.6985322	58
3	1344113	4992444	9.1284355	9.6983132	57
4	1345570	4989926	9.1289062	9.6980942	56
5	1347027	4987409	9.1293763	9.6978750	55
6	1348486	4984892	9.1298464	9.6976558	54
7	1349945	4982376	9.1303159	9.6974365	53
8	1351405	4979860	9.1307855	9.6972172	52
9	1352866	4977344	9.1312545	9.6969977	51
10	1354327	4974829	9.1317235	9.6967782	50
11	1355789	4972314	9.1321920	9.6965586	49
12	1357252	4969800	9.1326605	9.6963390	48
13	1358716	4967286	9.1331284	9.6961192	47
14	1360180	4964773	9.1335964	9.6958994	46
15	1361645	4962260	9.1340637	9.6956795	45
16	1363111	4959747	9.1345311	9.6954596	44
17	1364577	4957235	9.1349980	9.6952395	43
18	1366044	4954723	9.1354648	9.6950194	42
19	1367512	4952212	9.1359312	9.6947992	41
20	1368981	4949701	9.1363975	9.6945790	40
21	1370451	4947191	9.1368633	9.6943587	39
22	1371921	4944681	9.1373290	9.6941383	38
23	1373392	4942171	9.1377943	9.6939178	37
24	1374863	4939662	9.1382595	9.6936973	36
25	1376336	4937153	9.1387242	9.6934766	35
26	1377809	4934645	9.1391889	9.6932559	34
27	1379283	4932137	9.1396531	9.6930351	33
28	1380757	4929630	9.1401173	9.6928143	32
29	1382232	4927123	9.1405809	9.6925934	31
30	1383708	4924616	9.1410446	9.6923724	30
	Natural Co- Versed Sine.	Natural Versed Sine.	Logarithm Co- Versed Sine.	Logarithm Versed Sine.	M

59 DEGREES.

30 DEGREES.					
M.	Natural Versed Sine.	Natural Co- Versed Sine.	Logarithm Versed Sine.	Logarithm Co- Versed Sine.	
30	1383708	4924616	9.1410446	9.6923724	30
31	1385185	4922110	9.1415077	9.6921513	29
32	1386663	4919604	9.1419708	9.6919302	28
33	1388141	4917099	9.1424334	9.6917089	27
34	1389620	4914594	9.1428960	9.6914877	26
35	1391099	4912089	9.1433580	9.6912663	25
36	1392580	4909585	9.1438201	9.6910449	24
37	1394061	4907081	9.1442816	9.6908233	23
38	1395543	4904578	9.1447431	9.6906017	22
39	1397025	4902075	9.1452041	9.6903800	21
40	1398509	4899573	9.1456651	9.6901583	20
41	1399993	4897071	9.1461256	9.6899365	19
42	1401477	4894570	9.1465861	9.6897146	18
43	1402963	4892069	9.1470460	9.6894926	17
44	1404449	4889569	9.1475060	9.6892706	16
45	1405936	4887069	9.1479654	9.6890484	15
46	1407424	4884569	9.1484248	9.6888263	14
47	1408912	4882070	9.1488837	9.6886040	13
48	1410401	4879571	9.1493426	9.6883817	12
49	1411891	4877073	9.1498010	9.6881592	11
50	1413381	4874575	9.1502594	9.6879368	10
51	1414873	4872078	9.1507172	9.6877141	9
52	1416365	4869581	9.1511751	9.6874915	8
53	1417857	4867084	9.1516324	9.6872688	7
54	1419351	4864588	9.1520898	9.6870460	6
55	1420845	4862092	9.1525466	9.6868231	5
56	1422340	4859597	9.1530034	9.6866002	4
57	1423836	4857102	9.1534597	9.6863771	3
58	1425332	4854607	9.1539161	9.6861541	2
59	1426829	4852113	9.1543719	9.6859309	1
60	1428327	4849619	9.1548276	9.6857076	0
	Natural Co- Versed Sine.	Natural Versed Sine.	Logarithm Co- Versed Sine.	Logarithm Versed Sine.	M.

59 DEGREES.



31 DEGREES.					
M.	Natural Versed Sine.	Natural Co-Versed Sine.	Logarithm Versed Sine.	Logarithm Co-Versed Sine.	
0	1428327	4849619	9.1548276	9.6857076	60
1	1429826	4847126	9.1552829	9.6854843	59
2	1431325	4844633	9.1557382	9.6852609	58
3	1432825	4842141	9.1561930	9.6850374	57
4	1434326	4839649	9.1566477	9.6848139	56
5	1435827	4837157	9.1561020	9.6845902	55
6	1437329	4834666	9.1575562	9.6843665	54
7	1438832	4832175	9.1580100	9.6841427	53
8	1440336	4829685	9.1584637	9.6839189	52
9	1441840	4827195	9.1589169	9.6836949	51
10	1443345	4824706	9.1593702	9.6834710	50
11	1444851	4822217	9.1598229	9.6832468	49
12	1446357	4819729	9.1602756	9.6830227	48
13	1447865	4817241	9.1607278	9.6827984	47
14	1449373	4814754	9.1611800	9.6825741	46
15	1450881	4812267	9.1616318	9.6823497	45
16	1452391	4809780	9.1620835	9.6821253	44
17	1453901	4807294	9.1625347	9.6819007	43
18	1455412	4804808	9.1629859	9.6816761	42
19	1456923	4802323	9.1634366	9.6814514	41
20	1458436	4799838	9.1638873	9.6812266	40
21	1459949	4797354	9.1643374	9.6810018	39
22	1461462	4794870	9.1647876	9.6807769	38
23	1462977	4792385	9.1652373	9.6805518	37
24	1464492	4789903	9.1656870	9.6803268	36
25	1466008	4787420	9.1661362	9.6801016	35
26	1467525	4784938	9.1665854	9.6798764	34
27	1469042	4782456	9.1670341	9.6796510	33
28	1470560	4779975	9.1674828	9.6794257	32
29	1472079	4777494	9.1679309	9.6792002	31
30	1473598	4775014	9.1683791	9.6789747	30
	Natural Co-Versed Sine.	Natural Versed Sine.	Logarithm Co-Versed Sine.	Logarithm Versed Sine.	M.

58 DEGREES.

31 DEGREES.					
M	Natural Versed Sine.	Natural Co-Versed Sine.	Logarithm Versed Sine.	Logarithm Co-Versed Sine.	
30	1473598	4775014	9.1683791	9.6789747	30
31	1475119	4772534	9.1688268	9.6787490	29
32	1476640	4770054	9.1692745	9.6785234	28
33	1478161	4767575	9.1697217	9.6782976	27
34	1479684	4765096	9.1701689	9.6780717	26
35	1481207	4762618	9.1706156	9.6778458	25
36	1482731	4760140	9.1710623	9.6776198	24
37	1484255	4757663	9.1715085	9.6773937	23
38	1485781	4755186	9.1719547	9.6771676	22
39	1487307	4752710	9.1724004	9.6769413	21
40	1488833	4750234	9.1728461	9.6767150	20
41	1490361	4747759	9.1732913	9.6764886	19
42	1491889	4745284	9.1737365	9.6762622	18
43	1493418	4742809	9.1741812	9.6760356	17
44	1494947	4740335	9.1746259	9.6758090	16
45	1496478	4737861	9.1750701	9.6755823	15
46	1498009	4735388	9.1755144	9.6753555	14
47	1499541	4732915	9.1759581	9.6751286	13
48	1501073	4730443	9.1764018	9.6749017	12
49	1502506	4727971	9.1768451	9.6746747	11
50	1504140	4725499	9.1772883	9.6744476	10
51	1505675	4723028	9.1777311	9.6742204	9
52	1507210	4720557	9.1781738	9.6739932	8
53	1508746	4718087	9.1786161	9.6737659	7
54	1510283	4715617	9.1790584	9.6735385	6
55	1511821	4713148	9.1795002	9.6733110	5
56	1513358	4710679	9.1799419	9.6730835	4
57	1514898	4708211	9.1803832	9.6728558	3
58	1516438	4705743	9.1808245	9.6726281	2
59	1517978	4703275	9.1812653	9.6724003	1
60	1519519	4700808	9.1817061	9.6721725	0
	Natural Co-Versed Sine.	Natural Versed Sine.	Logarithm Co-Versed Sine.	Logarithm Versed Sine.	M.

58 DEGREES.

T t



32 DEGREES.					
M.	Natural Versed Sine.	Natural Co-Versed Sine.	Logarithm Versed Sine.	Logarithm Co-Versed Sine.	
0	1519519	4700008	9.1817061	9.6721725	60
1	1521061	4698341	9.1821465	9.6719445	59
2	1522603	4696875	9.1825868	9.6717165	58
3	1524147	4695409	9.1830266	9.6714883	57
4	1525691	4690944	9.1834665	9.6712602	56
5	1527235	4688479	9.1839059	9.6710319	55
6	1528781	4686015	9.1843452	9.6708036	54
7	1530327	4683551	9.1847841	9.6705751	53
8	1531874	4681087	9.1852230	9.6703467	52
9	1533421	4678624	9.1856614	9.6701181	51
10	1534970	4676161	9.1860998	9.6698895	50
11	1536519	4673699	9.1865377	9.6696607	49
12	1538068	4671237	9.1869756	9.6694319	48
13	1539619	4668776	9.1874131	9.6692030	47
14	1541170	4666315	9.1878505	9.6689741	46
15	1542722	4663855	9.1872875	9.6687450	45
16	1544274	4661395	9.1887245	9.6685159	44
17	1545828	4658935	9.1891610	9.6682867	43
18	1547382	4656476	9.1895974	9.6680574	42
19	1548936	4654017	9.1900335	9.6678280	41
20	1550492	4651559	9.1904695	9.6675986	40
21	1552048	4649102	9.1909050	9.6673691	39
22	1553605	4646645	9.1913406	9.6671395	38
23	1555162	4644188	9.1917756	9.6669098	37
24	1556721	4641732	9.1922107	9.6666801	36
25	1558280	4639276	9.1926452	9.6664502	35
26	1559839	4636821	9.1930799	9.6662203	34
27	1561400	4634366	9.1935140	9.6659903	33
28	1562961	4631912	9.1939482	9.6657603	32
29	1564523	4629458	9.1943818	9.6655301	31
30	1566086	4627004	9.1948155	9.6652989	30
	Natural Co-Versed Sine.	Natural Versed Sine.	Logarithm Co-Versed Sine.	Logarithm Versed Sine.	M.

57 DEGREES.

32 DEGREES.					
M	Natural Versed Sine.	Natural Co-Versed Sine.	Logarithm Versed Sine.	Logarithm Co-Versed Sine.	
30	1566086	4627004	9.1948155	9.6652989	30
31	1567649	4624551	9.1952487	9.6650695	29
32	1569213	4622098	9.1956819	9.6648392	28
33	1570778	4619646	9.1961146	9.6646087	27
34	1572343	4617194	9.1965473	9.6643781	26
35	1573909	4614742	9.1969795	9.6741475	25
36	1575476	4612291	9.1974118	9.6639168	24
37	1577044	4609841	9.1978436	9.6636860	23
38	1578612	4607391	9.1982754	9.6634552	22
39	1580181	4604942	9.1987067	9.6632242	21
40	1581751	4602493	9.1991380	9.6629932	20
41	1583321	4600043	9.1995689	9.6627620	19
42	1584892	4597597	9.1999997	9.6625309	18
43	1586464	4595149	9.2004301	9.6622996	17
44	1588037	4592702	9.2008605	9.6620683	16
45	1589610	4590255	9.2012904	9.6618368	15
46	1591184	4587809	9.2017204	9.6616053	14
47	1592759	4585363	9.2021498	9.6613737	13
48	1594334	4582918	9.2025793	9.6611421	12
49	1595910	4580473	9.2030083	9.6609103	11
50	1597487	4578028	9.2034373	9.6606785	10
51	1599064	4575584	9.2038659	9.6604466	9
52	1600643	4573141	9.2042944	9.6602146	8
53	1602222	4570698	9.2047225	9.6599825	7
54	1603801	4568255	9.2051506	9.6597504	6
55	1605382	4565813	9.2055782	9.6595181	5
56	1606963	4563371	9.2060058	9.6592858	4
57	1608545	4560930	9.2064330	9.6590534	3
58	1610127	4558490	9.2068602	9.6588210	2
59	1611710	4556050	9.2072869	9.6585884	1
60	1613294	4553610	9.2077136	9.6583558	0
	Natural Co-Versed Sine.	Natural Versed Sine.	Logarithm Co-Versed Sine.	Logarithm Versed Sine.	M.

57 DEGREES.

T t 2



## 33 DEGREES.

M.	Natural Versed Sine.	Natural Co-Versed Sine.	Logarithm Versed Sine.	Logarithm Co-Versed Sine.	
0	1613294	4553610	9.2077136	9.6583558	60
1	1614879	4551171	9.2081399	9.6581230	59
2	1616464	4548732	9.2085661	9.6578903	58
3	1618050	4546293	9.2089919	9.6576574	57
4	1619637	4543855	9.2094177	9.6574245	56
5	1621225	4541417	9.2098431	9.6571914	55
6	1622813	4538980	9.2102684	9.6569583	54
7	1624402	4536543	9.2106933	9.6567251	53
8	1625991	4534108	9.2111182	9.6564918	52
9	1627582	4531672	9.2115427	9.6562584	51
10	1629173	4529237	9.2119671	9.6560250	50
11	1630764	4526802	9.2123911	9.6557915	49
12	1632357	4524368	9.2128151	9.6555579	48
13	1633950	4521934	9.2132387	9.6553242	47
14	1635544	4519501	9.2136622	9.6550904	46
15	1637138	4517068	9.2140853	9.6548566	45
16	1638734	4514636	9.2145084	9.6546227	44
17	1640330	4512204	9.2149310	9.6543886	43
18	1641926	4509772	9.2153537	9.6541546	42
19	1643524	4507341	9.2157759	9.6539204	41
20	1645122	4504910	9.2161981	9.6536861	40
21	1646721	4502480	9.2166198	9.6534518	39
22	1648320	4500050	9.2170416	9.6532174	38
23	1649920	4497621	9.2174629	9.6529828	37
24	1651521	4495192	9.2178842	9.6527483	36
25	1653123	4492764	9.2183051	9.6525136	35
26	1654725	4490336	9.2187259	9.6522789	34
27	1656328	4487909	9.2191463	9.6520440	33
28	1657932	4485482	9.2195668	9.6518092	32
29	1659537	4483056	9.2199867	9.6515741	31
30	1661142	4480630	9.2204067	9.6513391	30
	Natural Co-Versed Sine.	Natural Versed Sine.	Logarithm Co-Versed Sine.	Logarithm Versed Sine.	M.

56 DEGREES.

## 33 DEGREE S.

M.	Natural Versed Sine.	Natural Co-Versed Sine.	Logarithm Versed Sine.	Logarithm Co-Versed Sine.	
30	1661142	4480630	9.2204067	9.6513391	30
31	1662748	4478205	9.2208262	9.6511039	29
32	1664354	4475780	9.2212458	9.6508687	28
33	1665962	4473355	9.2216649	9.6506333	27
34	1667570	4470931	9.2220839	9.6503980	26
35	1669178	4468507	9.2225026	9.6501625	25
36	1670788	4466084	9.2229212	9.6499269	24
37	1672398	4463662	9.2233395	9.6496912	23
38	1674009	4461240	9.2237577	9.6494556	22
39	1675620	4458818	9.2241754	9.6492197	21
40	1677232	4456397	9.2245932	9.6489839	20
41	1678845	4453976	9.2250105	9.6487478	19
42	1680459	4451556	9.2254279	9.6485118	18
43	1682073	4449136	9.2258448	9.6482756	17
44	1683688	4446717	9.2262617	9.6480394	16
45	1685304	4444298	9.2266781	9.6478031	15
46	1686920	4441880	9.2270946	9.6475667	14
47	1688537	4439462	9.2275106	9.6473302	13
48	1690155	4437044	9.2279266	9.6470937	12
49	1691774	4434627	9.2283422	9.6468570	11
50	1693393	4432210	9.2287578	9.6466204	10
51	1695013	4429794	9.2291729	9.6463835	9
52	1696634	4427378	9.2295881	9.6461467	8
53	1698255	4424963	9.2300028	9.6459097	7
54	1699877	4422548	9.2304175	9.6456726	6
55	1701500	4420134	9.2308318	9.6454355	5
56	1703123	4417720	9.2312461	9.6451983	4
57	1704748	4415307	9.2316600	9.6449609	3
58	1706372	4412894	9.2320738	9.6447236	2
59	1707998	4410482	9.2324872	9.6444861	1
60	1709624	4408071	9.2329007	9.6442486	0
	Natural Co-Versed Sine.	Natural Versed Sine.	Logarithm Co-Versed Sine.	Logarithm Versed Sine.	M.

56 DEGREES.



34 DEGREES.					
M.	Natural Versed Sine.	Natural Sine.	Logarithm Versed Sine.	Logarithm Sine.	
0	1709624	4408071	9.2329007	9.6442486	60
1	1711251	4405660	9.2333137	9.6440109	59
2	1712879	4403249	9.2337267	9.6437732	58
3	1714507	4400839	9.2341392	9.6435354	57
4	1716136	4398429	9.2345518	9.6432975	56
5	1717766	4396019	9.2349649	9.6430595	55
6	1719397	4393610	9.2353761	9.6428215	54
7	1721028	4391202	9.2357878	9.6425833	53
8	1722660	4388794	9.2361925	9.6423452	52
9	1724292	4386386	9.2366010	9.6421068	51
10	1725926	4383979	9.2370221	9.6418685	50
11	1727560	4381573	9.2374329	9.6416299	49
12	1729194	4379167	9.2378438	9.6413914	48
13	1730830	4376761	9.2382542	9.6411527	47
14	1732466	4374356	9.2386647	9.6409141	46
15	1734103	4371951	9.2390747	9.6406752	45
16	1735740	4369547	9.2394847	9.6404364	44
17	1737378	4367143	9.2398943	9.6401973	43
18	1739017	4364740	9.2403038	9.6399583	42
19	1740657	4362337	9.2407130	9.6397191	41
20	1742297	4359934	9.2411222	9.6394800	40
21	1743938	4357532	9.2415309	9.6392406	39
22	1745580	4355131	9.2419396	9.6390012	38
23	1747222	4352730	9.2423480	9.6387617	37
24	1748865	4350330	9.2427563	9.6385222	36
25	1750509	4347930	9.2431642	9.6382825	35
26	1752153	4345531	9.2435721	9.6380428	34
27	1753798	4343132	9.2439796	9.6378030	33
28	1755444	4340734	9.2443871	9.6375633	32
29	1757091	4338336	9.2447941	9.6373231	31
30	1758738	4335938	9.2452012	9.6370830	30
	Natural Co-Versed Sine.	Natural Sine.	Logarithm Co-Versed Sine.	Logarithm Sine.	M

55 DEGREES.

35 DEGREES.					
M.	Natural Versed Sine.	Natural Sine.	Logarithm Versed Sine.	Logarithm Sine.	
30	1758738	4335938	9.2452012	9.6370830	30
31	1760386	4333541	9.2456078	9.6368428	29
32	1762035	4331144	9.2460145	9.6366016	28
33	1763684	4328748	9.2464207	9.6363623	27
34	1765334	4326352	9.2468269	9.6361219	26
35	1766985	4323957	9.2472327	9.6358813	25
36	1768636	4321562	9.2476385	9.6356408	24
37	1770288	4319168	9.2480439	9.6354001	23
38	1771941	4316774	9.2484493	9.6351594	22
39	1773595	4314381	9.2488543	9.6349185	21
40	1775249	4311988	9.2492593	9.6346776	20
41	1776904	4309596	9.2496619	9.6344366	19
42	1778560	4307204	9.2500684	9.6341955	18
43	1780216	4304813	9.2504726	9.6339543	17
44	1781873	4302422	9.2508767	9.6337131	16
45	1783531	4300032	9.2512805	9.6334717	15
46	1785189	4297642	9.2516832	9.6332303	14
47	1786848	4295253	9.2520875	9.6329887	13
48	1788508	4292864	9.2524909	9.6327472	12
49	1790168	4290476	9.2528938	9.6325054	11
50	1791830	4288088	9.2532967	9.6322637	10
51	1793491	4285701	9.2536992	9.6320218	9
52	1795154	4283314	9.2541017	9.6317799	8
53	1796818	4280928	9.2545038	9.6315378	7
54	1798481	4278542	9.2549059	9.6312957	6
55	1800146	4276156	9.2553076	9.6310535	5
56	1801811	4273771	9.2557093	9.6308112	4
57	1803477	4271387	9.2561106	9.6305688	3
58	1805144	4269003	9.2565119	9.6303264	2
59	1806811	4266619	9.2569127	9.6300838	1
60	1808480	4264236	9.2573136	9.6298412	0
	Natural Co-Versed Sine.	Natural Sine.	Logarithm Co-Versed Sine.	Logarithm Sine.	M.

55 DEGREES.



35 DEGREES.					
M.	Natural Versed Sine.	Natural Co-Versed Sine.	Logarithm Versed Sine.	Logarithm Co-Versed Sine.	
0	1808480	4264236	9.2573136	9.6298412	60
1	1810148	4261853	9.2577141	9.6295984	59
2	1811818	4259471	9.2581145	9.6293557	58
3	1813488	4257089	9.2585146	9.6291127	57
4	1815159	4254708	9.2589147	9.6288698	56
5	1816831	4252328	9.2593143	9.6286267	55
6	1818502	4249948	9.2597140	9.6283836	54
7	1820176	4247568	9.2601132	9.6281403	53
8	1821849	4245189	9.2605125	9.6278970	52
9	1823524	4242810	9.2609113	9.6276535	51
10	1825199	4240432	9.2613102	9.6274101	50
11	1826875	4238054	9.2617086	9.6271664	49
12	1828551	4235677	9.2621071	9.6269228	48
13	1830228	4233300	9.2625051	9.6266790	47
14	1831906	4230924	9.2629032	9.6264352	46
15	1833584	4228548	9.2633008	9.6261912	45
16	1835264	4226173	9.2636985	9.6259473	44
17	1836944	4223798	9.2640957	9.6257031	43
18	1838624	4221424	9.2644929	9.6254589	42
19	1840305	4219050	9.2648898	9.6252146	41
20	1841987	4216676	9.2652866	9.6249703	40
21	1843670	4214303	9.2656831	9.6247258	39
22	1845353	4211931	9.2660795	9.6244813	38
23	1847037	4209559	9.2664756	9.6242366	37
24	1848722	4207188	9.2668716	9.6239919	36
25	1850407	4204817	9.2672673	9.6237471	35
26	1852094	4202447	9.2676629	9.6235022	34
27	1853780	4200077	9.2680582	9.6232572	33
28	1855468	4197708	9.2684534	9.6230122	32
29	1857156	4195339	9.2688483	9.6227670	31
30	1858845	4192970	9.2692431	9.6225218	30
	Natural Co-Versed Sine.	Natural Versed Sine.	Logarithm Co-Versed Sine.	Logarithm Versed Sine.	M.

54 DEGREES.

35 DEGREES.					
M	Natural Versed Sine.	Natural Co-Versed Sine.	Logarithm Versed Sine.	Logarithm Co-Versed Sine.	
30	1858845	4192970	9.2692431	9.6225218	30
31	1860534	4190602	9.2696376	9.6222764	29
32	1862225	4188234	9.2700321	9.6220311	28
33	1863916	4185867	9.2704261	9.6217855	27
34	1865607	4183501	9.2708202	9.6215400	26
35	1867299	4181135	9.2712139	9.6212942	25
36	1868992	4178770	9.2716075	9.6210485	24
37	1870686	4176405	9.2720008	9.6208026	23
38	1872380	4174041	9.2723941	9.6205567	22
39	1874075	4171677	9.2727870	9.6203106	21
40	1875771	4169313	9.2731799	9.6200645	20
41	1877468	4166950	9.2735724	9.6198183	19
42	1879165	4164588	9.2739649	9.6195720	18
43	1880863	4162226	9.2743570	9.6193256	17
44	1882561	4159864	9.2747491	9.6190792	16
45	1884260	4157503	9.2751408	9.6188326	15
46	1885960	4155142	9.2755325	9.6185860	14
47	1887661	4152782	9.2759238	9.6183392	13
48	1889362	4150422	9.2763151	9.6180924	12
49	1891064	4148063	9.2767061	9.6178454	11
50	1892766	4145705	9.2770970	9.6175985	10
51	1894470	4143347	9.2774875	9.6173513	9
52	1896174	4140990	9.2778781	9.6171042	8
53	1897878	4138633	9.2782683	9.6168569	7
54	1899584	4136276	9.2786584	9.6166096	6
55	1901290	4133920	9.2790482	9.6163621	5
56	1902996	4131564	9.2794380	9.6161146	4
57	1904704	4129200	9.2798273	9.6158669	3
58	1906412	4126835	9.2802167	9.6156192	2
59	1908121	4124451	9.2806057	9.6153714	1
60	1909830	4122148	9.2809947	9.6151235	0
	Natural Co-Versed Sine.	Natural Versed Sine.	Logarithm Co-Versed Sine.	Logarithm Versed Sine.	M.

54 DEGREES.

V v



36 DEGREES.					
M.	Natural Versed Sine.	Natural Co-Versed Sine.	Logarithm Versed Sine.	Logarithm Co-Versed Sine.	
0	1909830	4122148	9.2809947	9.6151235	60
1	1911540	4119795	9.2813833	9.6148755	59
2	1913251	4117442	9.2817720	9.6146275	58
3	1914963	4115090	9.2821602	9.6143793	57
4	1916675	4112738	9.2825484	9.6141311	56
5	1918388	4110387	9.2829363	9.6138827	55
6	1920101	4108036	9.2833241	9.6136343	54
7	1921815	4105686	9.2837116	9.6133857	53
8	1923530	4103336	9.2840990	9.6131372	52
9	1925246	4100987	9.2844861	9.6128884	51
10	1926962	4098639	9.2848732	9.6126397	50
11	1928679	4096291	9.2852599	9.6123907	49
12	1930397	4093944	9.2856466	9.6121418	48
13	1932115	4091597	9.2860329	9.6118927	47
14	1933834	4089250	9.2864192	9.6116436	46
15	1935554	4086904	9.2868052	9.6113943	45
16	1937274	4084558	9.2871911	9.6111451	44
17	1938995	4082213	9.2875767	9.6108956	43
18	1940717	4079868	9.2879622	9.6106461	42
19	1942440	4077524	9.2883474	9.6103965	41
20	1944163	4075180	9.2887326	9.6101469	40
21	1945887	4072837	9.2891174	9.6098970	39
22	1947611	4070495	9.2895022	9.6096472	38
23	1949336	4068153	9.2898866	9.6093972	37
24	1951062	4065811	9.2902711	9.6091472	36
25	1952789	4063470	9.2906551	9.6088970	35
26	1954516	4061129	9.2910392	9.6086468	34
27	1956244	4058789	9.2914229	9.6083965	33
28	1957972	4056449	9.2918065	9.6081461	32
29	1959701	4054110	9.2921898	9.6078956	31
30	1961431	4051772	9.2925731	9.6076450	30
	Natural Co-Versed Sine.	Natural Versed Sine.	Logarithm Co-Versed Sine.	Logarithm Versed Sine.	M.

53 DEGREES.

36 DEGREES.					
M.	Natural Versed Sine.	Natural Co-Versed Sine.	Logarithm Versed Sine.	Logarithm Co-Versed Sine.	
30	1961431	4051772	9.2925731	9.6076450	30
31	1963162	4049434	9.2929560	9.6073943	29
32	1964893	4047096	9.2933390	9.6071346	28
33	1966625	4044759	9.2937215	9.6068927	27
34	1968358	4042422	9.2941041	9.6066417	26
35	1970091	4040086	9.2944862	9.6063907	25
36	1971825	4037750	9.2948684	9.6061396	24
37	1973560	4035415	9.2952502	9.6058883	23
38	1975295	4033081	9.2956320	9.6056370	22
39	1977031	4030747	9.2960135	9.6053856	21
40	1978768	4028414	9.2963949	9.6051341	20
41	1980505	4026081	9.2967760	9.6048825	19
42	1982244	4023749	9.2971570	9.6046308	18
43	1983982	4021417	9.2975377	9.6043790	17
44	1985722	4019083	9.2979184	9.6041272	16
45	1987462	4016754	9.2982987	9.6038752	15
46	1989203	4014423	9.2986790	9.6036232	14
47	1990944	4012093	9.2990590	9.6033710	13
48	1992686	4009763	9.2994389	9.6031188	12
49	1994429	4007434	9.2998185	9.6028664	11
50	1996173	4005106	9.3001981	9.6026143	10
51	1997917	4002778	9.3005773	9.6023615	9
52	1999662	4000451	9.3009565	9.6021090	8
53	2001407	3998124	9.3013354	9.6018562	7
54	2003154	3995798	9.3017142	9.6016035	6
55	2004900	3993472	9.3020927	9.6013506	5
56	2006648	3991147	9.3024712	9.6010976	4
57	2008396	3988822	9.3028493	9.6008446	3
58	2010145	3986498	9.3032274	9.6005914	2
59	2011895	3984174	9.3036051	9.6003382	1
60	2013645	3981850	9.3039829	9.6000849	0
	Natural Co-Versed Sine.	Natural Versed Sine.	Logarithm Co-Versed Sine.	Logarithm Versed Sine.	M.

53 DEGREES.

V v 2



37 DEGREES.					
M.	Natural Versed Sine.	Natural Co-Versed Sine.	Logarithm Versed Sine.	Logarithm Co-Versed Sine.	
0	2013645	3981850	9.3039822	9.6000849	60
1	2015396	3979527	9.3043603	9.5998314	59
2	2017147	3977204	9.3047376	9.5995779	58
3	2018900	3974882	9.3051147	9.5993243	57
4	2020653	3972561	9.3054917	9.5990706	56
5	2022406	3970240	9.3058683	9.5988168	55
6	2024161	3967920	9.3062450	9.5985629	54
7	2025916	3965600	9.3066213	9.5983089	53
8	2027671	3963281	9.3069976	9.5980549	52
9	2029428	3960962	9.3073735	9.5978007	51
10	2031185	3958643	9.3077494	9.5975464	50
11	2032942	3956325	9.3081250	9.5972920	49
12	2034701	3954008	9.3085006	9.5970376	48
13	2036460	3951691	9.3088758	9.5967831	47
14	2038220	3949375	9.3092510	9.5965285	46
15	2039980	3947060	9.3096258	9.5962737	45
16	2041741	3944745	9.3100007	9.5960189	44
17	2043503	3942430	9.3103752	9.5957640	43
18	2045265	3940116	9.3107496	9.5955090	42
19	2047028	3937802	9.3111238	9.5952539	41
20	2048792	3935489	9.3114979	9.5949987	40
21	2050556	3933176	9.3118716	9.5947434	39
22	2052322	3930864	9.3122454	9.5944881	38
23	2054087	3928552	9.3126188	9.5942325	37
24	2055854	3926241	9.3129922	9.5939770	36
25	2057621	3923931	9.3133653	9.5937213	35
26	2059389	3921621	9.3137383	9.5934656	34
27	2061157	3919312	9.3141110	9.5932097	33
28	2062926	3917003	9.3144837	9.5929538	32
29	2064696	3914694	9.3148561	9.5926977	31
30	2066467	3912386	9.3152284	9.5924417	30
	Natural Co-Versed Sine.	Natural Versed Sine.	Logarithm Co-Versed Sine.	Logarithm Versed Sine.	M.

52 DEGREES.

37 DEGREES.					
M	Natural Versed Sine.	Natural Co-Versed Sine.	Logarithm Versed Sine.	Logarithm Co-Versed Sine.	
30	2066467	3912386	9.3152284	9.5924417	30
31	2068238	3910078	9.3156004	9.5921854	29
32	2070010	3907771	9.3159724	9.5919291	28
33	2071782	3905464	9.3163440	9.5916727	27
34	2073555	3903158	9.3167156	9.5914162	26
35	2075329	3900853	9.3170869	9.5911599	25
36	2077104	3898548	9.3174582	9.5909029	24
37	2078879	3896244	9.3178291	9.5906461	23
38	2080655	3893940	9.3182000	9.5903893	22
39	2082431	3891636	9.3185706	9.5901322	21
40	2084208	3889333	9.3189413	9.5898752	20
41	2085986	3887030	9.3193113	9.5896180	19
42	2087765	3884728	9.3196815	9.5893608	18
43	2089544	3882427	9.3200514	9.5891034	17
44	2091324	3880127	9.3204213	9.5888460	16
45	2093104	3877827	9.3207908	9.5885884	15
46	2094885	3875527	9.3211603	9.5883308	14
47	2096667	3873228	9.3215294	9.5880730	13
48	2098450	3870929	9.3218986	9.5878153	12
49	2100233	3868631	9.3222674	9.5875573	11
50	2102017	3866333	9.3226362	9.5872993	10
51	2103802	3864035	9.3230047	9.5870412	9
52	2105587	3861739	9.3233731	9.5867830	8
53	2107373	3859443	9.3237412	9.5865247	7
54	2109159	3857147	9.3241094	9.5862663	6
55	2110946	3854852	9.3244771	9.5860078	5
56	2112734	3852558	9.3248449	9.5857492	4
57	2114523	3850264	9.3252123	9.5854905	3
58	2116312	3847970	9.3255797	9.5852318	2
59	2118102	3845677	9.3259468	9.5849728	1
60	2119892	3843385	9.3263138	9.5847139	0
	Natural Co-Versed Sine.	Natural Versed Sine.	Logarithm Co-Versed Sine.	Logarithm Versed Sine.	M

52 DEGREES.



38 DEGREES.					
M.	Natural Versed Sine.	Natural Co-Versed Sine.	Logarithm Versed Sine.	Logarithm Co-Versed Sine.	
0	2119892	3843385	9.3263138	9.5847139	60
1	2121884	3841093	9.3266805	9.5844548	59
2	2123476	3838802	9.3270473	9.5841957	58
3	2125268	3836511	9.3274136	9.5839364	57
4	2127061	3834220	9.3277800	9.5836771	56
5	2128855	3831930	9.3281460	9.5834176	55
6	2130650	3829641	9.3285121	9.5831581	54
7	2132445	3827352	9.3288778	9.5828984	53
8	2134241	3825064	9.3292434	9.5826387	52
9	2136037	3822776	9.3296088	9.5823788	51
10	2137835	3820488	9.3299741	9.5821190	50
11	2139633	3818201	9.3303391	9.5818589	49
12	2141431	3815915	9.3307042	9.5815988	48
13	2143230	3813629	9.3310688	9.5813385	47
14	2145030	3811344	9.3314334	9.5810783	46
15	2146831	3809060	9.3317977	9.5808178	45
16	2148632	3806776	9.3321620	9.5805574	44
17	2150434	3804492	9.3325260	9.5802967	43
18	2152236	3802209	9.3328900	9.5800361	42
19	2154039	3799926	9.3332536	9.5797752	41
20	2155843	3797644	9.3336172	9.5795144	40
21	2157648	3795362	9.3339805	9.5792533	39
22	2159453	3793081	9.3343438	9.5789923	38
23	2161259	3790801	9.3347067	9.5787311	37
24	2163065	3788521	9.3350697	9.5784698	36
25	2164873	3786242	9.3354323	9.5782084	35
26	2166680	3783963	9.3357949	9.5779470	34
27	2168489	3781685	9.3361571	9.5776854	33
28	2170298	3779407	9.3365194	9.5774237	32
29	2172108	3777130	9.3368813	9.5771619	31
30	2173918	3774854	9.3372432	9.5769001	30
	Natural Co-Versed Sine.	Natural Versed Sine.	Logarithm Co-Versed Sine.	Logarithm Versed Sine.	M.
51 DEGREES					

38 DEGREES.					
M	Natural Versed Sine.	Natural Co-Versed Sine.	Logarithm Versed Sine.	Logarithm Co-Versed Sine.	
30	2173918	3774854	9.3372432	9.5769001	30
31	2175370	3772578	9.3376048	9.5766381	29
32	2177451	3770302	9.3379664	9.5763761	28
33	2179534	3768027	9.3383277	9.5761139	27
34	2181167	3765752	9.3386889	9.5758517	26
35	2182981	3763478	9.3390498	9.5755893	25
36	2184795	3761204	9.3394107	9.5753269	24
37	2186610	3758931	9.3397713	9.5750643	23
38	2188426	3756658	9.3401319	9.5748017	22
39	2190243	3754386	9.3404921	9.5745389	21
40	2192060	3752115	9.3408524	9.5742761	20
41	2193877	3749844	9.3412123	9.5740131	19
42	2195696	3747574	9.3415722	9.5737502	18
43	2197515	3745304	9.3419318	9.5734870	17
44	2199335	3743034	9.3422913	9.5732218	16
45	2201155	3740765	9.3426506	9.5729604	15
46	2202976	3738497	9.3430098	9.5726970	14
47	2204798	3736229	9.3433687	9.5724335	13
48	2206620	3733962	9.3437276	9.5721699	12
49	2208443	3731695	9.3440862	9.5719061	11
50	2210267	3729428	9.3444448	9.5716423	10
51	2212096	3727162	9.3448030	9.5713784	9
52	2213916	3724897	9.3451612	9.5711144	8
53	2215742	3722632	9.3455191	9.5708502	7
54	2217569	3720368	9.3458770	9.5705861	6
55	2219396	3718105	9.3462346	9.5703217	5
56	2221223	3715842	9.3465921	9.5700573	4
57	2223051	3713580	9.3469494	9.5697928	3
58	2224880	3711318	9.3473067	9.5695282	2
59	2226710	3709057	9.3476636	9.5692635	1
60	2228540	3706796	9.3480205	9.5689987	0
	Natural Co-Versed Sine.	Natural Versed Sine.	Logarithm Co-Versed Sine.	Logarithm Versed Sine.	M
51 DEGREES.					



39 DEGREES.					
M.	Natural Versed Sine.	Natural Co-Versed Sine.	Logarithm Versed Sine.	Logarithm Co-Versed Sine.	
0	2228540	3706796	9.3480205	9.5689987	60
1	2230371	3704536	9.3483771	9.5687337	59
2	2232203	3702276	9.3487337	9.5684688	58
3	2234035	3700017	9.3490899	9.5682036	57
4	2235868	3697758	9.3494462	9.5679385	56
5	2237702	3695499	9.3498021	9.5676731	55
6	2239536	3693241	9.3501580	9.5674078	54
7	2241371	3690984	9.3505136	9.5671422	53
8	2243206	3688727	9.3508692	9.5668766	52
9	2245043	3686471	9.3512245	9.5666109	51
10	2246879	3684216	9.3515798	9.5663451	50
11	2248717	3681961	9.3519347	9.5660792	49
12	2250555	3679707	9.3522897	9.5658132	48
13	2252394	3677453	9.3526443	9.5655471	47
14	2254233	3675200	9.3529989	9.5652804	46
15	2256074	3672947	9.3533532	9.5649564	45
16	2257914	3670695	9.3537075	9.5646782	44
17	2259756	3668443	9.3540614	9.5644017	43
18	2261598	3666192	9.3544154	9.5641251	42
19	2263441	3663941	9.3547690	9.5638484	41
20	2265284	3661690	9.3551227	9.5635716	40
21	2267128	3659440	9.3554760	9.5632947	39
22	2268973	3657191	9.3558293	9.5630177	38
23	2270818	3654942	9.3561823	9.5627405	37
24	2272664	3652694	9.3565353	9.5624634	36
25	2274511	3650447	9.3568880	9.5621860	35
26	2276358	3648200	9.3572406	9.5619087	34
27	2278206	3645954	9.3575930	9.5616311	33
28	2280055	3643708	9.3579453	9.5613536	32
29	2281904	3641463	9.3582973	9.5610758	31
30	2283754	3639218	9.3586494	9.5607980	30
	Natural Co-Versed Sine.	Natural Versed Sine.	Logarithm Co-Versed Sine.	Logarithm Versed Sine.	M.

50 DEGREES.

39 DEGREES.					
M.	Natural Versed Sine.	Natural Co-Versed Sine.	Logarithm Versed Sine.	Logarithm Co-Versed Sine.	
30	2283754	3639218	9.3586493	9.5610080	30
31	2285605	3636974	9.3590011	9.5607401	29
32	2287456	3634730	9.3593528	9.5604721	28
33	2289308	3632487	9.3597041	9.5602040	27
34	2291160	3630244	9.3600555	9.5599358	26
35	2293014	3628001	9.3604066	9.5596674	25
36	2294868	3625759	9.3607576	9.5593991	24
37	2296722	3623518	9.3611084	9.5591305	23
38	2298577	3621278	9.3614591	9.5588619	22
39	2300433	3619038	9.3618095	9.5585932	21
40	2302290	3616799	9.3621599	9.5583244	20
41	2304147	3614560	9.3625100	9.5580554	19
42	2306004	3612322	9.3628601	9.5577864	18
43	2307863	3610084	9.3632099	9.5575173	17
44	2309722	3607847	9.3635597	9.5572481	16
45	2311582	3605610	9.3639092	9.5569787	15
46	2313442	3603374	9.3642586	9.5567093	14
47	2315303	3601138	9.3646078	9.5564397	13
48	2317165	3598903	9.3649569	9.5561701	12
49	2319027	3596668	9.3653057	9.5559004	11
50	2320890	3594434	9.3656546	9.5556306	10
51	2322754	3592201	9.3660031	9.5553606	9
52	2324618	3589968	9.3663516	9.5550906	8
53	2326483	3587736	9.3666998	9.5548204	7
54	2328348	3585504	9.3670480	9.5545502	6
55	2330215	3583272	9.3673959	9.5542798	5
56	2332082	3581041	9.3677437	9.5540094	4
57	2333949	3578811	9.3680913	9.5537388	3
58	2335817	3576581	9.3684389	9.5534681	2
59	2337686	3574352	9.3687861	9.5531973	1
60	2339556	3572124	9.3691334	9.5529265	0
	Natural Co-Versed Sine.	Natural Versed Sine.	Logarithm Co-Versed Sine.	Logarithm Versed Sine.	M.

50 DEGREES.

X x



40 DEGREES.					
M.	Natural Versed Sine.	Natural Co. Versed Sine.	Logarithm Versed Sine.	Logarithm Co. Versed Sine.	
0	2339556	3572124	9.3691334	9.5529265	60
1	2341426	3569896	9.3694803	9.5526555	59
2	2343296	3567669	9.3698272	9.5523845	58
3	2345168	3565442	9.3701739	9.5521132	57
4	2347040	3563215	9.3705205	9.5518420	56
5	2348913	3560989	9.3708668	9.5515706	55
6	2350786	3558764	9.3712111	9.5512992	54
7	2352660	3556539	9.3715591	9.5510275	53
8	2354535	3554315	9.3719051	9.5507559	52
9	2356410	3552091	9.3722508	9.5504840	51
10	2358286	3549868	9.3725964	9.5502122	50
11	2360162	3547645	9.3729418	9.5499401	49
12	2362040	3545423	9.3732872	9.5496681	48
13	2363918	3543201	9.3736323	9.5493958	47
14	2365796	3540980	9.3739773	9.5491236	46
15	2367675	3538760	9.3743221	9.5488511	45
16	2369555	3536540	9.3746668	9.5485786	44
17	2371436	3534321	9.3750113	9.5483059	43
18	2373317	3532102	9.3753557	9.5480333	42
19	2375198	3529884	9.3756998	9.5477604	41
20	2377081	3527667	9.3760440	9.5474875	40
21	2378964	3525450	9.3763878	9.5472144	39
22	2380848	3523234	9.3767316	9.5469413	38
23	2382732	3521018	9.3770751	9.5466680	37
24	2384617	3518802	9.3774186	9.5463947	36
25	2386503	3516587	9.3777618	9.5461212	35
26	2388389	3514372	9.3781050	9.5458477	34
27	2390276	3512158	9.3784479	9.5455740	33
28	2392163	3509945	9.3787908	9.5453002	32
29	2394051	3507732	9.3791334	9.5450263	31
30	2395940	3505520	9.3794760	9.5447524	30
	Natural Co. Versed Sine.	Natural Versed Sine.	Logarithm Co. Versed Sine.	Logarithm Versed Sine.	M.

49 DEGREES.

40 DEGREES.					
M.	Natural Versed Sine.	Natural Co. Versed Sine.	Logarithm Versed Sine.	Logarithm Co. Versed Sine.	
30	2395940	3505520	9.3794760	9.5447524	30
31	2397830	3503308	9.3798183	9.5444783	29
32	2399720	3501097	9.3801606	9.5442041	28
33	2401611	3498886	9.3805025	9.5439298	27
34	2403502	3496676	9.3808445	9.5436554	26
35	2405394	3494467	9.3811862	9.5433809	25
36	2407287	3492258	9.3815279	9.5431063	24
37	2409180	3490050	9.3818692	9.5428315	23
38	2411074	3487842	9.3822106	9.5425568	22
39	2412969	3485635	9.3825516	9.5422818	21
40	2414864	3483428	9.3828927	9.5420068	20
41	2416760	3481222	9.3832335	9.5417316	19
42	2418657	3479016	9.3835742	9.5414564	18
43	2420554	3476811	9.3839147	9.5411810	17
44	2422452	3474606	9.3842551	9.5409056	16
45	2424350	3472402	9.3845953	9.5406300	15
46	2426249	3470199	9.3849354	9.5403544	14
47	2428149	3467996	9.3852753	9.5400786	13
48	2430049	3465794	9.3856151	9.5398027	12
49	2431950	3463592	9.3859547	9.5395267	11
50	2433852	3461391	9.3862942	9.5392507	10
51	2435754	3459191	9.3866334	9.5389744	9
52	2437657	3456991	9.3869727	9.5386982	8
53	2439561	3454792	9.3873116	9.5384217	7
54	2441465	3452593	9.3876506	9.5381452	6
55	2443370	3450394	9.3879892	9.5378686	5
56	2445276	3448196	9.3883278	9.5375919	4
57	2447182	3445999	9.3886662	9.5373150	3
58	2449089	3443802	9.3890045	9.5370381	2
59	2450996	3441606	9.3893425	9.5367610	1
60	2452904	3439410	9.3896806	9.5364839	0
	Natural Co. Versed Sine.	Natural Versed Sine.	Logarithm Co. Versed Sine.	Logarithm Versed Sine.	M.

49 DEGREES.

X x 2



41 DEGREES.					
M.	Natural Versed Sine.	Natural Co- Versed Sine.	Logarithm Versed Sine.	Logarithm Co- Versed Sine.	
0	2452904	3439410	9.3896806	9.5364839	60
1	2454813	3437215	9.3900183	9.5362066	59
2	2456722	3435021	9.3903561	9.5359293	58
3	2458632	3432827	9.3906935	9.5356518	57
4	2460543	3430633	9.3910309	9.5353742	56
5	2462454	2428440	9.3913681	9.5350965	55
6	2464366	3426247	9.3917052	9.5348187	54
7	2466279	3424055	9.3920421	9.5345408	53
8	2468192	3421864	9.3923789	9.5342628	52
9	2470106	3419674	9.3927155	9.5339846	51
10	2472020	3417484	9.3930520	9.5337065	50
11	2473935	3415295	9.3933882	9.5334281	49
12	2475851	3413106	9.3937245	9.5331497	48
13	2477767	3410918	9.3940604	9.5328711	47
14	2479684	3408730	9.3943964	9.5325925	46
15	2481602	3406542	9.3947310	9.5323137	45
16	2483520	3404355	9.3950677	9.5320349	44
17	2485439	3402169	9.3954031	9.5317558	43
18	2487359	3399984	9.3957384	9.5314768	42
19	2489279	3397799	9.3960735	9.5311975	41
20	2491200	3395614	9.3964085	9.5309183	40
21	2493121	3393430	9.3967433	9.5306388	39
22	2495043	3391247	9.3970781	9.5303593	38
23	2496966	3389064	9.3974125	9.5300797	37
24	2498889	3386882	9.3977470	9.5298000	36
25	2500813	3384700	9.3980812	9.5295201	35
26	2502738	3382519	9.3984154	9.5292402	34
27	2504663	3380339	9.3987493	9.5289601	33
28	2506589	3378159	9.3990831	9.5286799	32
29	2508516	3375979	9.3994167	9.5283996	31
30	2510443	3373800	9.3997503	9.5281195	30
	Natural Co- Versed Sine.	Natural Versed Sine.	Logarithm Co- Versed Sine.	Logarithm Versed Sine.	M.

48 DEGREES.

41 DEGREES.					
M	Natural Versed Sine.	Natural Co- Versed Sine.	Logarithm Versed Sine.	Logarithm Co- Versed Sine.	
30	2510443	3373800	9.3997503	9.5281193	30
31	2512371	3371621	9.4000836	9.5278387	29
32	2514299	3369443	9.4004169	9.5275581	28
33	2516228	3367266	9.4007499	9.5272774	27
34	2518158	3365089	9.4010829	9.5269966	26
35	2520088	3362913	9.4014157	9.5267156	25
36	2522019	3360737	9.4017484	9.5264346	24
37	2523951	3358562	9.4020808	9.5261534	23
38	2525883	3356388	9.4024132	9.5258722	22
39	2527816	3354214	9.4027453	9.5255908	21
40	2529749	3352041	9.4030775	9.5253094	20
41	2531683	3349868	9.4034093	9.5250277	19
42	2533618	3347696	9.4037412	9.5247461	18
43	2535554	3345524	9.4040727	9.5244642	17
44	2537490	3343353	9.4044043	9.5241823	16
45	2539426	3341183	9.4047355	9.5239002	15
46	2541364	3339013	9.4050668	9.5236182	14
47	2543301	3336844	9.4053978	9.5233358	13
48	2545240	3334675	9.4057287	9.5230535	12
49	2547179	3332507	9.4060594	9.5227710	11
50	2549119	3330339	9.4063901	9.5224885	10
51	2551059	3328172	9.4067205	9.5222057	9
52	2553000	3326006	9.4070509	9.5219230	8
53	2554942	3323840	9.4073810	9.5216400	7
54	2556885	3321674	9.4077111	9.5213570	6
55	2558827	3319509	9.4080409	9.5210739	5
56	2560771	3317345	9.4083708	9.5207907	4
57	2562715	3315182	9.4087003	9.5205073	3
58	2564660	3313019	9.4090298	9.5202239	2
59	2566606	3310856	9.4093591	9.5199402	1
60	2568552	3308694	9.4096883	9.5196566	0
	Natural Co- Versed Sine.	Natural Versed Sine.	Logarithm Co- Versed Sine.	Logarithm Versed Sine.	M

48 DEGREES.



42 DEGREES.					
M.	Natural Versed Sine.	Natural Co. Versed Sine.	Logarithm Versed Sine.	Logarithm Co. Versed Sine.	
0	2568552	3308694	9.4096883	9.5196566	60
1	2570498	3306532	9.4100173	9.5193727	59
2	2572446	3304371	9.4103462	9.5190889	58
3	2574394	3302211	9.4106749	9.5188048	57
4	2576342	3300051	9.4110036	9.5185207	56
5	2578292	3297892	9.4113320	9.5182364	55
6	2580242	3295733	9.4116603	9.5179521	54
7	2582193	3293573	9.4119885	9.5176676	53
8	2584143	3291418	9.4123166	9.5173830	52
9	2586095	3289261	9.4126444	9.5170984	51
10	2588047	3287105	9.4129722	9.5168136	50
11	2590000	3284949	9.4132998	9.5165286	49
12	2591954	3282794	9.4136273	9.5162436	48
13	2593908	3280639	9.4139546	9.5159585	47
14	2595863	3278485	9.4142818	9.5156732	46
15	2597819	3276332	9.4146088	9.5153879	45
16	2599775	3274179	9.4149357	9.5151024	44
17	2601732	3272027	9.4152625	9.5148168	43
18	2603689	3269875	9.4155891	9.5145311	42
19	2605647	3267724	9.4159155	9.5142453	41
20	2607606	3265573	9.4162419	9.5139594	40
21	2609565	3263423	9.4165681	9.5136733	39
22	2611525	3261274	9.4168941	9.5133872	38
23	2613485	3259125	9.4172199	9.5131009	37
24	2615447	3256976	9.4175458	9.5128146	36
25	2617408	3254828	9.4178715	9.5125280	35
26	2619371	3252681	9.4181970	9.5122415	34
27	2621334	3250535	9.4185223	9.5119547	33
28	2623297	3248389	9.4188475	9.5116679	32
29	2625262	3246243	9.4191726	9.5113810	31
30	2627227	3244098	9.4194975	9.5110939	30
	Natural Co. Versed Sine.	Natural Versed Sine.	Logarithm Co. Versed Sine.	Logarithm Versed Sine.	M.

47 DEGREES.

42 DEGREES.					
M	Natural Versed Sine.	Natural Co. Versed Sine.	Logarithm Versed Sine.	Logarithm Co. Versed Sine.	
30	2627227	3244098	9.4194975	9.5110939	30
31	2629192	3241954	9.4198223	9.5108068	29
32	2631158	3239810	9.4201470	9.5105195	28
33	2633125	3237667	9.4204714	9.5102321	27
34	2635092	3235524	9.4207958	9.5099446	26
35	2637060	3233382	9.4211201	9.5096569	25
36	2639029	3231240	9.4214442	9.5093692	24
37	2640998	3229099	9.4217681	9.5090813	23
38	2642968	3226959	9.4220919	9.5087934	22
39	2644939	3224819	9.4224156	9.5085053	21
40	2646910	3222680	9.4227391	9.5082172	20
41	2648882	3220541	9.4230625	9.5079288	19
42	2650854	3218403	9.4233858	9.5076404	18
43	2652827	3216266	9.4237089	9.5073519	17
44	2654801	3214129	9.4240319	9.5070633	16
45	2656775	3211993	9.4243547	9.5067745	15
46	2658750	3209857	9.4246774	9.5064856	14
47	2660725	3207722	9.4250000	9.5061966	13
48	2662701	3205587	9.4253224	9.5059075	12
49	2664678	3203453	9.4256447	9.5056183	11
50	2666655	3201319	9.4259669	9.5053290	10
51	2668633	3199187	9.4262889	9.5050395	9
52	2670612	3197054	9.4266108	9.5047500	8
53	2672591	3194922	9.4269325	9.5044603	7
54	2674571	3192791	9.4272541	9.5041705	6
55	2676551	3190661	9.4275755	9.5038806	5
56	2678533	3288531	9.4278969	9.5035906	4
57	2680514	3286401	9.4282181	9.5033005	3
58	2682497	3284272	9.4285391	9.5030102	2
59	2684479	3282144	9.4288600	9.5027193	1
60	2686463	3280016	9.4291808	9.5024293	0
	Natural Co. Versed Sine.	Natural Versed Sine.	Logarithm Co. Versed Sine.	Logarithm Versed Sine.	M.

47 DEGREES.



## 43 DEGREES.

M.	Natural Versed Sine.	Natural Co-Versed Sine.	Logarithm Versed Sine.	Logarithm Co-Versed Sine.	
0	2686463	3180016	9.4291808	9.5024293	60
1	2688447	3177889	9.4295015	9.5021388	59
2	2690432	3175763	9.4298220	9.5018480	58
3	2692417	3173637	9.4301424	9.5015572	57
4	2694403	3171511	9.4304626	9.5012662	56
5	2696390	3169387	9.4307827	9.5009751	55
6	2698377	3167262	9.4311026	9.5006840	54
7	2700365	3165139	9.4314224	9.5003927	53
8	2702354	3163016	9.4317423	9.5001013	52
9	2704343	3160873	9.4320617	9.4998097	51
10	2706332	3158791	9.4323811	9.4995181	50
11	2708323	3156650	9.4327004	9.4992263	49
12	2710314	3154529	9.4330195	9.4989345	48
13	2712305	3152409	9.4333385	9.4986425	47
14	2714297	3150289	9.4336574	9.4983504	46
15	2716280	3148170	9.4339761	9.4980581	45
16	2718284	3146052	9.4342948	9.4977658	44
17	2720278	3143934	9.4346132	9.4974733	43
18	2722272	3141816	9.4349316	9.4971808	42
19	2724268	3139700	9.4352497	9.4968881	41
20	2726264	3137584	9.4355678	9.4965953	40
21	2728260	3135468	9.4358857	9.4963023	39
22	2730257	3133353	9.4362035	9.4960093	38
23	2732255	3131239	9.4365212	9.4957161	37
24	2734253	3129124	9.4368387	9.4954229	36
25	2736252	3127012	9.4371561	9.4951295	35
26	2738252	3124899	9.4374734	9.4948360	34
27	2740252	3122787	9.4377994	9.4945424	33
28	2742253	3120675	9.4381075	9.4942486	32
29	2744254	3118565	9.4384243	9.4939547	31
30	2746256	3116454	9.4387410	9.4936607	30
	Natural Co-Versed Sine.	Natural Versed Sine.	Logarithm Co-Versed Sine.	Logarithm Versed Sine.	M.

## 46 DEGREES.

## 43 DEGREES.

M.	Natural Versed Sine.	Natural Co-Versed Sine.	Logarithm Versed Sine.	Logarithm Co-Versed Sine.	
30	2746256	3116454	9.4387411	9.4936607	30
31	2748259	3114345	9.4390576	9.4933666	29
32	2750262	3112236	9.4393741	9.4930724	28
33	2752266	3110127	9.4396904	9.4927780	27
34	2754271	3108019	9.4400066	9.4924836	26
35	2756276	3105911	9.4403226	9.4921890	25
36	2758281	3103805	9.4406385	9.4918944	24
37	2760288	3101698	9.4409543	9.4915995	23
38	2762295	3099593	9.4412700	9.4913046	22
39	2764302	3097488	9.4415855	9.4910095	21
40	2766310	3095383	9.4419009	9.4907144	20
41	2768319	3093279	9.4422161	9.4904191	19
42	2770329	3091176	9.4425313	9.4901237	18
43	2772339	3089073	9.4428462	9.4898281	17
44	2774349	3086971	9.4431611	9.4895325	16
45	2776360	3084869	9.4434758	9.4892361	15
46	2778372	3082768	9.4437904	9.4889409	14
47	2780385	3080668	9.4441048	9.4886448	13
48	2782398	3078568	9.4444192	9.4883488	12
49	2784411	3076469	9.4447334	9.4880525	11
50	2786426	3074370	9.4450474	9.4877562	10
51	2788441	3072272	9.4453614	9.4874597	9
52	2790456	3070175	9.4456752	9.4871631	8
53	2792472	3068078	9.4459888	9.4868663	7
54	2794488	3065982	9.4463024	9.4865696	6
55	2796506	3063886	9.4466157	9.4862726	5
56	2798524	3061791	9.4469290	9.4859755	4
57	2800543	3059696	9.4472422	9.4856783	3
58	2802562	3057602	9.4475552	9.4853810	2
59	2804582	3055509	9.4478680	9.4850835	1
60	2806602	3053416	9.4481808	9.4847860	0
	Natural Co-Versed Sine.	Natural Versed Sine.	Logarithm Co-Versed Sine.	Logarithm Versed Sine.	M.

## 46 DEGREES.



44 D E G R E E S.					
M.	Natural Versed Sine.	Natural Co- Versed Sine.	Logarithm Versed Sine.	Logarithm Co- Versed Sine.	
0	2806602	3053416	9.4481808	9.4847860	60
1	2808623	3051324	9.4484934	9.4844883	59
2	2810645	3049233	9.4488059	9.4841905	58
3	2812667	3047142	9.4491182	9.4838926	57
4	2814690	3045051	9.4494305	9.4835949	56
5	2816713	3042961	9.4497426	9.4832964	55
6	2818737	3040872	9.4500546	9.4829981	54
7	2820762	3038783	9.4503664	9.4826997	53
8	2822787	3036695	9.4506781	9.4824012	52
9	2824813	3034608	9.4509896	9.4821025	51
10	2826839	3032521	9.4513011	9.4818038	50
11	2828866	3030435	9.4516123	9.4815049	49
12	2830894	3028349	9.4519236	9.4812059	48
13	2832922	3026264	9.4522346	9.4809067	47
14	2834951	3024179	9.4525456	9.4806075	46
15	2836981	3022095	9.4528563	9.4803081	45
16	2839011	3020012	9.4531670	9.4800087	44
17	2841041	3017929	9.4534775	9.4797090	43
18	2843073	3015847	9.4537879	9.4794093	42
19	2845105	3013766	9.4540982	9.4791094	41
20	2847137	3011685	9.4544084	9.4788095	40
21	2849170	3009604	9.4547184	9.4785093	39
22	2851204	3007524	9.4550283	9.4782091	38
23	2853238	3005445	9.4553380	9.4779088	37
24	2855272	3003367	9.4556476	9.4776083	36
25	2857309	3001289	9.4559571	9.4773077	35
26	2859345	2999211	9.4562665	9.4770070	34
27	2861382	2997134	9.4565758	9.4767062	33
28	2863419	2995058	9.4568849	9.4764052	32
29	2865457	2992982	9.4571938	9.4761041	31
30	2867496	2990907	9.4575027	9.4758029	30
	Natural Co- Versed Sine.	Natural Versed Sine.	Logarithm Co- Versed Sine.	Logarithm Versed Sine.	M.

45 D E G R E E S.

44 D E G R E E.					
M.	Natural Versed Sine.	Natural Co- Versed Sine.	Logarithm Versed Sine.	Logarithm Co- Versed Sine.	
30	2867496	2990907	9.4575027	9.4758029	30
31	2869535	2988833	9.4578114	9.4755016	29
32	2871574	2986759	9.4581201	9.4752002	28
33	2873615	2984686	9.4584285	9.4748985	27
34	2875656	2982613	9.4587369	9.4745969	26
35	2877697	2980541	9.4590451	9.4742951	25
36	2879740	2978469	9.4593532	9.4739931	24
37	2881782	2976399	9.4596611	9.4736910	23
38	2883826	2974328	9.4599690	9.4733889	22
39	2885870	2972259	9.4602767	9.4730865	21
40	2887914	2970189	9.4605843	9.4727841	20
41	2889959	2968121	9.4608917	9.4724815	19
42	2892005	2966053	9.4611991	9.4721789	18
43	2894052	2963986	9.4615062	9.4718760	17
44	2896099	2961919	9.4618133	9.4715732	16
45	2898146	2959853	9.4621202	9.4712700	15
46	2900194	2957787	9.4624271	9.4709669	14
47	2902243	2955722	9.4627338	9.4706636	13
48	2904293	2953658	9.4630404	9.4703602	12
49	2906343	2951594	9.4633468	9.4700566	11
50	2908393	2949531	9.4636531	9.4697530	10
51	2910444	2947468	9.4639593	9.4694491	9
52	2912496	2945406	9.4642654	9.4691452	8
53	2914549	2943345	9.4645713	9.4688411	7
54	2916602	2941284	9.4648771	9.4685370	6
55	2918655	2939224	9.4651828	9.4682326	5
56	2920709	2937165	9.4654883	9.4679283	4
57	2922764	2935106	9.4657937	9.4676237	3
58	2924820	2933047	9.4660991	9.4673190	2
59	2926876	2930989	9.4664042	9.4670142	1
60	2928932	2928932	9.4667093	9.4667093	0
	Natural Co- Versed Sine.	Natural Versed Sine.	Logarithm Co- Versed Sine.	Logarithm Versed Sine.	M.

45 D E G R E E S.

Y y 2





# THE USE OF THE FOREGOING TABLES.

**T**Hough I have all along the *Navigation* reference to these *Tables*, and sufficiently shewed the Use of the most of them, yet forasmuch as it may happen, this Part or Book to be alone, or strayed from its fellows by one chance or other, I have thought it convenient to add a sheet or two of its Use.

## *The Use of Table I.*

I. The first is a *Table of Declinations* to 9 Degrees of Latitude from the *Ecliptick*, serving chiefly, by the *Longitude* and *Latitude* of the Moon or Planets to find the *Declination*; thus, Admit the Moon in  $5^{\circ}$  of *Sagittarius*, with  $4^{\circ} 30'$  North Latitude: Looking for the Character  $\tau$ , in *page 12*, I find it over the left hand Column, and over head the Title *North Latitude*, then I look along on the top of the Table for  $4^{\circ}$  of Latitude, and follow that Column down till I come against  $5^{\circ}$  of the left Column under  $\tau$ , there I find  $17^{\circ} 17'$ ; but seeing the Moon's given Latitude is not just 4 Degrees but 30 Minute more, I take the Parts proportional for that, and thence conclude the true Declination to be  $16^{\circ} 47'$ .

If the Longitude be between  $\psi$  and  $\S$ , you must look for the Sign at the lower Edge of the Page, and the Degrees of that Sign up along the right hand Column.

## *The Use of Table II. page 14.*

II. The second is a *Table of Right Ascensions* to every Degree of the *Ecliptick*, and 9 Degrees of Latitude both North and South, and is to be:



be entered with the *Longitude* and *Latitude*, in the very same manner as the former Table for *Declination* was, only here you'll find all the Signs on the top or upper part, without any bottom or reverse Enterings.

*The Use of Table III. page 38.*

III. The third is a *Table of Amplitudes* to 40 Degrees of Declination, and for all Latitudes to 61 Degrees, serving to find the *Distance* of the Sun or Star's Rising from the East, or Setting from the West; being of great use to rectify the Compass by. Admit the Sun in  $13^{\circ}$  of  $\Delta$ , and consequently having  $17^{\circ}$  Declination North, and I would find the Sun's Amplitude, or Distance of Rising from the East Point, in Latitude  $52^{\circ} 00'$ , I look for the Latitude on the head of the Table, (which I find in Column the fourth, page 43) and for the Declination in the first Column to the left hand, under the Title *Degrees of Declination*, and in the common meeting I find  $28^{\circ} 21'$ , the Amplitude, or Distance of Rising from the East, or Setting from the West, which is about  $2\frac{1}{2}$  Points, so that the Sun doth then rise E N E  $\frac{1}{2}$  Northerly, and set W N W  $\frac{1}{2}$  Northerly, or NW by W  $\frac{1}{2}$  Westerly.

Again, Admit the *Lion's Heart* have  $13^{\circ} 30'$  Declination North, and I require its Amplitude, or Distance of Rising from the East, in Latitude  $35^{\circ} 00'$  North: Turning to  $35^{\circ}$  of Latitude, and looking downwards thereunder 'till I come right against  $13^{\circ}$  of Declination, I find  $15^{\circ} 56'$ , and for the  $30'$  of Declination more I take the Proportional Parts  $37'$ , and add them to it, which makes  $16^{\circ} 33'$ , the true Amplitude.

*Note.* That if the Sun or Star have North Declination, the Amplitude is North; and if the Declination be South, the Amplitude is South; that is, if the Sun or Star have North Declination, it will rise to the Northward of the East, and set to the Northward of the West, &c.

*The Use of Table IV. page 44.*

IV. The fourth is a *Table of Differences of Ascensions*, serving to find the *Time* of the Sun or Star's rising or setting in any Latitude; thus, first look the *Latitude* on the head of the Table, and the *Declination* down along the first Column towards the left hand under the Title *Degrees of Declination*, and in the common meeting is the Difference of Ascension in Degrees and Minutes, which being turned into Time by the following Table is (if it be for the Sun) the Time of his rising or setting before or after 6 of the Clock.

If the Declination be towards the elevated Pole, this is the Time of rising before, or his setting after 6; but if the Declination be towards the depressed Pole, it's the Time of rising after, and setting before 6 of the Clock.

Hence, if the Sun have Declination towards the elevated Pole, this Difference of Ascension in Time being subtracted from 6 Hours gives the Time of the Sun's rising, and being added gives the Time of setting; but if

if the Sun have Declination towards the depressed Pole, it's to be added to 6 Hours for the Time of rising, and subtracted from 6 for the Time of setting.

*A Table to turn Degrees and Minutes into Time.*

Deg.	H.	M.	Deg.	H.	M.	Deg.	H.	M.
$\frac{1}{4}$	0	01	8	0	32	18	1	12
$\frac{1}{2}$	0	02	9	0	36	19	1	16
$\frac{3}{4}$	0	03	10	0	40	20	1	20
1	0	04	11	0	44	30	2	00
2	0	08	12	0	48	40	2	40
3	0	12	13	0	52	50	3	20
4	0	16	14	0	56	60	4	00
5	0	20	15	1	00	70	4	40
6	0	24	16	1	04	80	5	20
7	0	28	17	1	08	90	6	00

Lastly, If you double the Time of Sun-rising, you have the Nocturnal Arch, or Length of the Night; and if you double the Time of Sun-setting, you have the Diurnal Arch, or Length of the Day.

*Example.*

July 25. the Sun having  $17^{\circ}$  of Declination North, I require the Time of Sun-rising and setting, and Length of the Day and Night, in Latitude  $51^{\circ} 00'$  North? I look along the Head of the Table till in page 57, in the second Column, I find the Latitude  $51$  Degrees, and running downwards 'till against  $17$  Degrees of Declination I find  $22^{\circ} 11'$ , the Difference of Ascension; the  $22$  Degrees I look in the precedent little Table, and it gives 1 Hour 28 Minutes of Time, and for the  $11'$  I take 1 Minute of Time, so that it is 1 Hour 29 Minutes. Now forasmuch as the Declination is towards the elevated Pole, I subtract  $1^h 29'$  from  $6^h$ , and the Remainder shews the Sun rises at 31 Minutes after 4 of the Clock; and adding it to  $6^h$ , I find

	h.	m.
20	=	1 20
2	=	0 08
		1 28
	h.	m.
6	00	
1	29	
4	31	the Sun's Rising.
6	00	
1	29	
7	29	the Sun's Setting.



the Time of setting to be 29 Minutes after 7 of the Clock. The double of 4 Hours 31 Minutes gives 9 Hours 2 Minutes, the Length of the Night, and the double of 7 Hours 29 Minutes gives 14 Hours 58 Minutes, the Length of the Day.

h.	m.	h.	m.
4	31	7	29
4	31	7	29
9 02 the Length of the Night.		14 58 the Length of the Day.	

The Use of Table V. page 59.

V. The fifth is a *Traverse-Table* to every Quarter-point of the Compass, and Hundred-part of a Mile or League Distance, and is to give the Difference of Latitude and Departure, thus; Look the Course, if under four Points from the Meridian, in the head of the Table, and the Miles sailed down along the left Column, and in the common Angle of meeting under the Letters *E W* is the Departure from the Meridian, and under *NS* the Difference of Latitude: But if the Course be above four Points from the Meridian, look it at the bottom of the Table and the Distance sailed, look upwards in the right hand Column, and in the common Angle of meeting over the Letters *E W* at the bottom will be the Departure, and over the Letters *NS* the Difference of Latitude in sailing this Course and Distance. If the Distance be above 60, it must be broken into several Numbers, and therewith the Table entered, and the Departure and Difference of Latitudes taken out proper to each part of the Distance, the Totals or Aggregates of these will be the Difference of Latitude and Departure required.

Example 1.

Admit a Ship sail 31 Leagues South South West, that is, two Points from the Meridian, and it be required to find the Difference of Latitude and Departure.

Because the Points are less than 4 look them on the head of the Table, and right against 31 in the left hand Column under *Dist. in Leagues or Miles sailed*, is under *E W* 11.86 the Leagues departed from the Meridian, and under *NS* 28.64 the Leagues Difference of Latitude sought.

Example 2.

Admit a Ship sail 25 Miles West by South one quarter Point Westerly, that is,  $7\frac{1}{4}$  Points from the South, and it be required to find the Difference of Latitude and Departure.

Look the  $7\frac{1}{4}$  Points (because above 4) at the bottom of the Table, which

which you'll find in the 59th. page, and over  $7\frac{1}{4}$  Points and right against 25 the Miles sailed, you have 24.73 the Miles Departure, and 3.66 the Miles Difference of Latitude. If the Distance had been in Leagues, the Departure had been 24.73 Leagues, and the Difference of Latitude 3.66 Leagues.

Example 3.

Suppose a Ship sail 276 Miles North East by North, that is, 3 Points from the North, and it be required to find how much she has altered her Latitude, and also how much she's Departed from the Meridian.

Over 3 Point right against 200 Miles Distance, you'll find under the Letters *N, S*, 166.28 Miles Difference of Latitude; and under *E, W*, 111.11 Miles Departure; Secondly under 3 Points and right against 70 Miles Distance you'll find under *N, S*, 58.22 Miles Difference of Latitude, and under *E, W*, 38.88 Miles Departure; and Thirdly, under 3 Points and against 6 Miles Distance you'll find under *N, S*, 4.99 Miles Difference of Latitude, and under *E, W*, 3.33 Miles Departure.

Dist.	Diff. Lat.	Dep.
200	166.28	111.11
70	58.22	38.88
6	4.99	3.33
276	229.49	153.32

So that the Difference of Latitude for the whole Distance 276 Miles, is 229.49 Miles, and the Departure 153.32 Miles.

Example 4.

Suppose a Ship sail East North East half a Point East 134 Miles, and it be required to find the Difference of Latitude and Departure.

Dist.	Diff. Lat.	Dep.
100	29.02	95.69
34	9.87	32.54
	38.89	128.23

The Difference of Latitude for the whole Distance is 38.89 Miles, and the Departure 128.23 Miles.



## The Use of Table VI. page 68.

VI. The sixth is a Table of Meridional Miles or Parts, to every Degree and Minute of Latitude, serving to make a Mercator's Chart, or work the Mercator-failing, and is to be entered with the Degrees of Latitude on the head, and the Minute down the left hand Column. Having the Latitudes of two Places, to find the Meridional Miles or Minutes between them, consider whether the Places be one under the Equinoctial and the other wide thereof, or the one on the one side of the Equinoctial and the other on the other, or whether they both lye on the same side; for according to these Positions, there's a threefold Case.

1. When one Place lyeth under the Equinoctial, then the Meridional Minutes that are found next under the Degree of Latitude the other Place lyeth in, is the Meridional Difference of Latitude, or Latitude enlarged.

2. When one Place hath North Latitude, and the other South, add the Meridional Minutes belonging to each Latitude together, and the Sum is the Meridional Minutes between them.

3. When both Places are towards one Pole, then subtract the Meridional Parts answering to the lesser Latitude out of those for the greater, and the Remainder will be the Meridional Minutes required.

Examples of these Cases will make them more plain, which shall be these:

## Example 1.

To find the Meridional parts or Minutes, between the Equinoctial and Latitude  $43^{\circ} 11'$ .

In the Column under 43, and right against 11 Minutes in the Left-hand Column stands 2878.2, the Meridional parts required.

## Example 2.

Let it be required to find the Meridional parts between  $25^{\circ} 13'$  South Latitude, and  $51^{\circ} 30'$  North.

Under $51^{\circ}$ and against $30'$ is	3616.8
Under $25^{\circ}$ and against $13'$ is	1564.3
The Meridional parts between the two are	5181.1

## Example 3.

To find the Meridional Minutes between the Latitudes  $32^{\circ} 15'$  North, and  $53^{\circ} 23'$  North.

Under $53^{\circ}$ and against $23'$ is	3802.2
Under $32^{\circ}$ and against $15'$ is	2046.1
The Meridional parts between the Latitudes proposed, are	1756.1

VII. The

## The Use of Table VII. page 94.

VII. The seventh is a Table of the Miles East or West, that Answer to the Degrees of Longitude in the fourth Rumb: and serves to turn Miles of Easting or Westing into Degrees and Minutes of Longitude, & contr. As, Admit a Ship sail from the Equator on some Point between the North and East to  $10^{\circ}$  Latitude, and then finds she has made 400<sup>m</sup> Departure East; to find the Degrees of Longitude answering to this 400 Miles, turn to the Table page 94, and look for  $10^{\circ}$  Latitude, and right against it you'll find 600 Miles, the Miles East the Ship would have been if she had sailed on the fourth Rumb: Then say by the Golden Rule, As 600 Miles is to  $10^{\circ} 3'$  so is 400 Miles, and multiplying and dividing you will produce 402, which divided by 60 gives  $6^{\circ} 42'$  the Degrees of Longitude answering to the 400 Miles Easting.

m.	600	10 3	m.	400
	60			
	603			
	400			
600	241200	(402	60	402 (6° 42'
	2400			360
	1200			42
	1200			
	0			

On the contrary, if one knowing the Difference of Longitude made, as here  $6^{\circ} 42'$ , would find the Miles East or West answering thereto, look in the said Table against the Latitude, viz.  $10^{\circ}$ , and take out the Miles against it and also the Degrees and Minutes, and say: As  $10^{\circ} 3'$  is to 600 so is  $6^{\circ} 42'$ , which worked as before produces 400 Miles, thus:

m.	600	10 3	m.	400
	60			
	603			
	402			
	600			
603	241200	(400 m.		

Z z 2

Admit



Admit a Ship sail from Latitude  $6^{\circ} N$ , to  $16^{\circ}$  North, and hath made 400 Miles Departure East, to find the Degrees of Longitude she has altered; take out of the Table the Numbers against  $6^{\circ}$ , which are 360 Miles and  $6'$ , and also those against  $16^{\circ}$  which are 960 Miles and  $16' 12''$ , and subtract them one from the other, then say: As 600, to  $10^{\circ} 12'$ ; so 400; and it will produce  $6^{\circ} 48'$ , thus:

m.				
960	16 12	600	10 12	:: 400
360	6 00		60	
600	10 12		612	
			400	
		600	244800	(408
			2400	
			4800	
			4800	
			0	
			36	
			48	

By the reverse of this you may having the Difference of Longitude given find the Miles East or West Departure.

The Use of Table VIII. page 100.

VIII. The eighth is a Table to Change Degrees and Minutes of any Parallel into Miles, thus: Look the Latitude in the Left-hand Column, and the Degrees and Minutes of Longitude on the head of the Table, and right against the Latitude and under the Degree of Longitude you will have the Miles and parts sought.

If the Longitude given consists of Degrees and Minutes, look the Miles and parts answering the Degrees first, and then those for the Minutes, and if either the Degrees or Minutes be above 10, you must enter several times. As you will see by these Examples.

Example 1.

Admit I have altered  $3^{\circ} 15'$  of Longitude, under the Parallel of  $50^{\circ}$  Latitude, and it be required to find the Miles and parts answering thereto.

I enter the Table as directed with	3 Degrees which gives	115.7 Miles.
	10 Minutes which gives	006.4
	5 Minutes which gives	003.2
		125.3 Miles.

Example 2.

Example 2.

To find the Miles answering to  $25^{\circ} 32'$ , in the Parallel of  $46^{\circ}$  of Latitude.

20 Degrees gives	. . .	833.6 Miles.
5 Degrees gives	. . .	208.4
30 Minutes gives	. . .	020.8
2 Minutes gives	. . .	001.4
		1064.2 Miles.

The Use of Table IX. page 108.

IX. The ninth is a Table to Reduce Miles East and West into Degrees of Longitude, it is to be entered with the Miles on the head and the Degrees of Latitude in the Left-hand Column.

Admit a Ship sail 157 Miles East or West in the Parallel of  $53^{\circ}$ , and its demanded how many Degrees of Longitude are altered.

100 Miles gives	. . .	02	46	15
50 Miles gives	. . .	01	23	05
7 Miles gives	. . .	00	11	38
The Sum		04	20	58

The Use of Table X. page 120.

X. The tenth is a Table of Rumbs with the Differences of Longitudes and Latitudes.

Prop. 1.

The Latitudes of two places and their Difference of Longitude being given to find the Course and Distance.

Suppose a Ship set from Latitude  $51^{\circ} 8'$  North, and sail on some Rumb between the South and East till she fall in Latitude  $28^{\circ} 30'$  North, and have altered her Longitude  $19^{\circ} 20'$ ; what Course has she kept and what Distance has she run? I seek under the fourth Rumb in this Table against Latitude  $28^{\circ} 30'$  and find the Longitude answering thereto  $29^{\circ} 46'$ , and against  $51^{\circ} 8'$ ,  $59^{\circ} 46'$ ; the Difference of these two Longitudes  $59^{\circ} 46'$  and  $29^{\circ} 46'$ , is  $30^{\circ}$  which should be but  $19^{\circ} 20'$ , therefore the fourth was not the Rumb: Again, against these Latitudes I take out the Longitude answering to the third Rumb, and find them to differ but  $19^{\circ} 58'$  which being only a few Minutes over the true Difference of Longitude  $19^{\circ} 20'$ , I conclude her to have sailed on the third Rumb.



To find the Distance, subtract the given Latitudes one from the other, and the Difference  $22^{\circ} 38'$ , look in the Left-hand Column of the Table, under Title Latitude, and under the third Rumb you'll find 1634 Miles of 60 to a Degree, the Distance required.

If the Latitudes had been the one North and the other South, you must have added them and taken the Sum for the Difference.

## Prop. 2.

*The Course and Distance being given, with the Latitude Departed from, to find the Latitude she's in and the Difference of Longitude.*

A Ship sailing from  $10^{\circ}$  North Latitude North East 1317 Miles, what is the Latitude she's in and her Difference of Longitude? Looking under the fourth Rumb for the Distance 1317, I find 1315 the nearest to it, and right against it  $15^{\circ} 30'$ , but making a proportionable allowance for the two Miles Difference, the Latitude is  $15^{\circ} 25'$  to which add the Latitude  $10^{\circ}$ , you have  $25^{\circ} 25'$  the Latitude she's arrived in; Lastly, against these Latitudes and under the Rumb look the corresponding Longitudes, which are  $10^{\circ} 3'$  and  $26^{\circ} 17'$ , and their Difference  $16^{\circ} 14'$  is the true Difference of Longitude.

## Prop. 3.

*Both the Latitudes and the Course being given, to find the Distance sailed and the Difference of Longitude.*

A Ship sails from the Grand Canarie, in Latitude  $28^{\circ}$  North East till she be in Latitude  $36^{\circ} 30'$  North, her Distance sailed and Difference of Longitude is required?

Against Latitude  $28^{\circ}$  and under the fourth Rumb, you'll find the Longitude to be  $29^{\circ} 11'$ , and against the Latitude  $36^{\circ} 30'$ , and under the same Rumb you'll find  $39^{\circ} 15'$ , then from  $39^{\circ} 15'$  subtract  $29^{\circ} 11'$ , the remainder  $10^{\circ} 4'$  is the Difference of Longitude required.

Secondly, take the Latitudes one from the other and look the remainder  $8^{\circ} 30'$  under the Title Latitude in the Left-Column, and under Rumb the fourth you'll have 72 Miles the Distance.

## Prop. 4.

*The Latitudes of two places and the Distance being given, to find the Course and Difference of Longitude.*

A Ship sails from Latitude  $20^{\circ}$  North 4200 Miles, and then arrives in Latitude  $46^{\circ} 50'$ , what Course has she steered and what is the Difference of Longitude?

Look

Look the Difference of Latitude  $26^{\circ} 50'$  under Latitude, and right against it searching under all the Rumbs for the Distance 4200 Miles at length, I find it nearly under the sixth Rumb, the Rumb failed on.

Then against Latitude  $46^{\circ} 50'$  under the sixth Rumb is  $128^{\circ} 18'$  Long.  
Against  $20^{\circ}$  Latitude under the sixth Rumb is  $49^{\circ} 18'$  Long.

Remains the Difference of Longitude  $79^{\circ} 00'$

## Prop. 5.

*The Difference of Longitude, Distance, and one Latitude being given, to find the other Latitude and the Course.*

Take the Rumb which you judge fittest, and examine what Difference of Latitude will answer to the Distance given, with which Latitude search all the Rumbs for a Difference of Longitude like that given, and where you find it, that is the Rumb sought.

Admit a Ship sail from Latitude  $14^{\circ}$  North, till she alter her Longitude  $10^{\circ} 36'$  and make her Distance sailed 849 Miles.

I choose the fourth Rumb and search under it till I find 849, it's against  $10^{\circ}$  Latitude, which added to  $14^{\circ}$  gives  $24^{\circ}$  the second Latitude; the Longitudes that answer to these Latitudes under the fourth Rumb are  $14^{\circ} 8'$  and  $24^{\circ} 44'$ , whose Difference is  $10^{\circ} 36'$ , just agreeing to my Difference of Longitude given; whence I conclude the fourth Rumb to be that failed on.

## Prop. 6.

*The Difference of Longitude, Course, and one Latitude being given, to find the other Latitude and the Distance.*

Suppose a Ship sail from Latitude  $30^{\circ}$  North, on the fifth Rumb, till she vary her Longitude  $34^{\circ}$ ; to find the other Latitude and Distance.

Look under the fifth Rumb for the Longitude answering to  $30^{\circ}$  Latitude, and you'll find  $47^{\circ} 6'$ , to which add  $34^{\circ}$  the Difference of Longitude given, and see for the Sum  $81^{\circ} 6'$  under the same Rumb under the Title Longitude, and you will find  $47^{\circ} 35'$  the other Latitude.

To find the Distance, subtract the Distance answering to Latitude  $30^{\circ}$  from the Distance answering  $47^{\circ} 35'$ , and the Difference 1896 Miles is the Distance required.

If the Latitudes at any time be the one North, and the other South, add them for the Difference.

The



## The Use of Table XI. page 1.

XI. The eleventh is a Table of *Logarithms*, whose use is explained in the *Cosmography*.

## The Use of Table XII. page 47.

XII. The twelfth is a Table of *Proportional parts*, which makes the Table of *Logarithms* serve to 1000000, thus,

When you have found the *Logarithm* for five places by the direction in the *Cosmography*, then enter this Table of proportional parts, again, with the Difference of the Differences, and you will find a small number to be added to that *Logarithm* to make it serve the sixth place.

Let it be required to take out the *Logarithm* of 382574, first I look in the Left Column of the *Logarithm* Tables for 382, and right against it under 5 I take out 5826314, and the Difference 1135, which Difference I look in the Left Column of the Table of proportional parts, and under 7 I find 680 to be added to 5826314, which makes 5826994 the *Logarithm* of 382573, Lastly subtract 680 from the next Difference right against it viz. 793 and seek the Difference 113 in the Left Column of the Table of proportional parts, and against it under 4 I find 46 which I add to 5826994 and it makes 5827040, to which I annex 5 for the Index, and the whole number 5,5827040 is the true *Logarithm* of the natural number 382574. Let the *Logarithm* of the Natural number 130846 be required; First I look the three first Figures 130 in the Left Column of the *Logarithm* Tables, and against it under 8 I find 1166077 the *Logarithm* of 1308, and 3329 the Difference, with which entering the Table of proportional parts, under 4 I find 1332 which added to 1166077, makes 1167409; then I subtract 1332 from the next Difference 1665, and see for the remainder 333 in the said Table of proportional parts, and against it and under 6 I find 199, which added to 1167409 makes 1167608, to which last of all I prefix the Index 5, and have the Compleat *Logarithm* 5, 1167608 for the given number 130846.

## The Use of Table XIII. page 71.

XIII. The thirteenth is a Table of *Natural and Artificial Sines, Tangents and Secants*, to every Minute of the Quadrant.

To take out the *Sine*, *Tangent*, or *Secant*, either *Natural* or *Logarithmical*, of any Degrees and Minutes.

If it be the *Natural Sine*, *Tangent*, or *Secant*, that's required, look on the Left-hand pages, but if the *Logarithmical* on the Right.

If

If the Degrees be less than 45 look it on the Head of the Table, and the Minutes down the left Column under M: but if the Degrees be above 45 look it at the bottom or foot of the Table, and look the Minutes upward in the Right-hand Column, and in the Column distinguished by the Title, *Sine*, *Tangent*, or *Secant*, or *Co-sine*, *Co-tangent*, or *Co-secant* at the bottom or top, according as the Degree is, right against the Minute you have the *Sine*, *Tangent*, *Secant*, or *Co-sine* required.

As suppose you were to find the *Natural sine*, *tangent* and *secant* of 23° 13'. Look on the left-hand pages, page after page for 23° on the head of the Table, and down the left hand Column under M for 13': then right against 13' under the words *Natural sine* in the head of the Table you shall have 3942093, which is the *Natural sine* of 23° 13', against 13' under *Natural tangent*, you have 4289449 the *Natural tangent* of 23° 13', and against 13', and under the Title (*Natural secant*) you have 10881148 the *Natural secant* of 23° 13'.

If you would have also the artificial or *Logarithmical sine*, *tangent* and *secant* thereof, look on the Right-hand page having 23 Degree at the head, and run down along its left Column to 13', then right against 13', and under (*L. sine*) you have 9,5957268 the *Logar. sine* of 23° 13', against 13', and under (*L. Tang.*) you have 9,6324015, the artificial or *Logarithmical Tangent* of 23° 13', and against 13', and under (*L. secant*) you have 10,0366747 the *Log. secant* of 23° 13'.

Suppose you were to find the *Natural Sine*, *Tangent* and *Secant* of 32° 48'. Look 32 Degree at the Head of the Table on the left page, and so far as there's two leaves marked 32 turn to the latter, (because the minutes exceed 30,) and run down the left Column under M to 48', then right against 48', and under (*Nat. Sine*) you will find 5417082 the *Natural Sine* of 32° 48', against 48' and under (*Nat. Tangent*) you will have 6444560 the *Natural Tangent*, and right against 48', and under (*Nat. Secant*) you may take out 11896737 the *Natural Secant* of 32° 48'. If you would have the Artificial or *Logarithmical sine*, *Tangent* and *Secant* thereof also, look on the Right-hand page having 32 Degrees at the head, and run down along its left Column to 48', then right against 48', and under (*L. sine*) you will have 9,7337654 the *Logarith. sine* of 32° 48', against 48' and under (*L. Tangent*) you will find 9,8091933 the *Logarithmical Tangent* of 32° 48', and right against 48', and under (*L. Secant*) you will see 10,0754279 the *Logarithmical Secant* of 32° 48'.

Admit you were to find both the *Natural and Artificial Sine*, *Tangent* and *Secant* of 61° 25'. Now because the Degrees are above 45, turn to 61 Degree at the bottom, and look upwards in the Right Column of the Right-hand page to 25', and right against 25', and over (*L. Sine*) you have 9,9435549 the *Logar. Sine* of 61° 25', right against 25', and over (*L. Tangent*) is 10,2637307 the *Logar. Tangent* of 61° 25', and right against 25', and over (*L. Secant*) is 10,3201757 the *Logar. Secant* of 61° 25'. Also on the Left-hand page right against 25', in the Right-hand Column and over (*Nat. Sine*) is 8731222 the *Natural Sine* of 61° 25',

A a a

right



right against  $25'$ , and over (*Nat. Tangent*) is 18353999 the Natural Tangent of  $61^{\circ} 25'$ , and right against  $25'$ , and over (*Nat. Secant*) is 20901418 the Natural Secant of  $61^{\circ} 25'$ , and against  $25'$  and over (*Nat. Co-secant*) is 11387937 the Natural Co-secant, or Secant Complement of  $61^{\circ} 25'$ , &c.

To find the Sine, Tangent, or Secant, either Natural or Artificial, of any Degrees and Minutes exceeding 90 Degrees but under 180: subtract them from 180, and look the Sine, Tangent, or Secant of the Remainder as before directed. So the Natural Sine of  $123^{\circ} 11'$  is 8369235, the Natural Tangent 15291308 the Natural Secant 18270854, the Logar. sine 9,9226858 the Logar. Tangent 10,1844446, the Logar. Secant 10,2617588, and the Logar. Co-secant 10,0773142.

To take out the Sine, Tangent, or Secant, either Natural or Artificial of any Degrees and Minutes above 180 Degrees but under 270, subtract 180 there from, and look the Sine, Tangent, and Secant of the rest as above directed, and that shall be the Sine, Tangent, or Secant of the Arch proposed, so the Natural Sine of  $231^{\circ} 54'$  is 7869350, the Natural Co-sine 6170359, the Natural Tangent 12753473, the Natural Co-tangent 7841002, the Natural Secant 16206513, the Natural Co-secant 12707529, the Logar. Sine 9,8959389, the Logar. Co-sine 9,7903104, the Logar. Tangent 10,1056285, the Logar. Co-tangent 9,8943715, the Logar. Secant 10,2096896, the Logar. Co-secant 10,1040611.

To find the Sine, Co-sine, Tangent, Co-tangent, Secant or Co-secant, either Natural or Artificial of any Arch above 270 Degrees, and under a Circle or 360, subtract it from 360, and look the Sine, Co-sine, Tangent, or Secant, &c. Of the rest according to the foregoing Directions; and that shall be the Sine, Tangent, or Secant, &c. of the Arch proposed.

*Having the Sine, Tangent, or Secant, either Natural or Artificial, to find the Degrees and Minutes answering thereto.*

If it be a Natural Sine less than	7071068
A Natural Tangent less than	10000000
Or a Natural Secant less than	14142136

Look for it on the Left-hand pages under the Titles *Natural Sine*, *Natural Tangent*, *Natural Secant*, on the head of the Table, else look for it over those Titles which are at the bottom.

If it be a Logar. Sine less than	9,8494850
A Logar. Tangent less than	10,0000000
Or a Logar. Secant less than	10,1505150

Look.

Look for it on the Right-hand page under the Title *L. Sine*, *L. Tangent*, *L. Secant*, but if it be greater than these, then the Degree is above 45, and you must look for it on the Right-hand page over the Title *L. Sine*, *L. Tangent*, &c. which are at the bottom.

Suppose you were to find the Degrees and Minutes answering to this Natural Sine 7027782, this being less than 7071068, I run over the Columns of Sines on the Left-hand pages, looking under the Title (*Nat. Sine*) at the top, page after page, for 7027782, and under 44 Degrees, and against 39' in the Column under M, I find 7027741, which is the nearest to the Sine sought, and the Arch answering thereto is  $44^{\circ} 39'$ .

Let it be required to find the Degrees and Minutes corresponding to this Natural Sine 8672501, this being greater than 7071068, I run over the Columns of Sines on the Left pages looking over the Title (*Nat. Sine*) at the bottom, and over 60 Degrees and against 8', which is over M in the Right-hand Column, is the nearest thereto, so that the Arch is  $60^{\circ} 8'$ .

After this manner will the Arch answering to the Natural Tangent 17250936 be  $59^{\circ} 54'$ , the Arch to the Natural Secant 10002194 be  $88^{\circ} 48'$ , the Arch to the Logar. Sine 8,8647376 be  $4^{\circ} 12'$ , the Arch to the Logar. Tangent 10,3473490 be  $65^{\circ} 48'$ , and the Arch to the Logar. Secant 10,0503124 be  $2^{\circ} 03'$ .

#### *The Use of Table XIV. page 72.*

XIV. The fourteenth being a small Table inserted under the Sines, Tangents, and Secants, is a Table to find the hour of the day, in all Latitudes under  $60^{\circ}$ , by the bearing of the Sun; thus,

Turn to the Latitude, and under it in the upper Column or head Rank seek the Declination, and the point of the Compass that the Sun is upon in the left Column, and in the common place of meeting will be the time of day required. *Example.*

June 10th 1678, Being in Latitude  $46^{\circ} 00' N$ , and the Sun SSW, I require the time of day?

Looking against two Points under  $23^{\circ} \frac{1}{2}$  Declination N, (the Sines Declination at that time) I find the time to be 39' after twelve.

Admit the Sun NE by N in the Latitude  $51^{\circ} 00' N$ , and the Declination  $14^{\circ}$  South: to find the time of day?

I turn to  $51^{\circ}$  Latitude, and against three Points under  $14^{\circ}$  Declination S, I find  $2^h 12'$ , which I subtract from 12 the Remainder  $9^h 48'$ ; shews it was 48' after 9 in the Morning.

In the Latitude  $30^{\circ} N$ , the Sun having  $15^{\circ} 00' N$  Declination, its desired to know at what a Clock the Sun will come upon the SW point of the Compass?

I look in the Declination Column for  $15^{\circ}$  but not finding it, I look down along under the next nearest, *viz.* Under  $14^{\circ}$  till I come against four

A a a 2



four Points in the left Column and there I find  $1^h 2'$ : and against it under  $d$  for Difference is  $7'$ , the half whereof is  $3'$ , which being taken from  $1^h 2'$ , leaves  $59$  afternoon the true time.

If the Latitude be South, you must take North declination for South, and South for North.

Admit the Declination be  $12^\circ$  North, I desire to know at what a Clock the Sun will come upon the WSW point of the Compass, in Latitude  $30^\circ$  South?

When I have found the Latitude, I look in that Part under Title South Declination, and under  $12^\circ$  against 6 Points, I find  $27'$  after 4 in the afternoon, the true time of day.

By this Table also may be found the true hour of the Night, by the bearing of any known Star; whose Declination doth not exceed the Suns greatest Declination; Thus,

First, Find the time of the Stars coming to the Meridian on the day proposed, then if the Star be on the East side of the Meridian, you must subtract those hours and minutes which the Table shews the Star to be distant from the Meridian, from the time of the Stars coming to the Meridian: and the remainder is the true hour of the night, but if the Star be on the west side of the Meridian, then you must add those hours and minutes above said, to the time of the Stars coming to the Meridian as above said, and the Sum is the true hour of the Night.

September 12th being in Latitude  $43^\circ$  North, I observe the Bulls eye to be upon the SE point of the Compass: I require the hour of the Night?

The time of this Stars being on the Meridian . . . . .	$16^h$	$20'$
It's distance from the Meridian either at SE or SW . . . . .	1	38
<hr/>		
The time of the Stars being SE . . . . .	14	42
<hr/>		
The time of the Stars being SW . . . . .	17	58

January 7th 1684, Being in Latitude  $48^\circ$  N, I see the *Scorpions* heart upon the ESE point: what is the time of the Night? The Stars Declination is  $16^\circ$ .

The time of this Stars being on the Meridian . . . . .	$20^h$	$11'$
It's distance from the Meridian . . . . .	3	11
<hr/>		
The time of the Night . . . . .	23	22

If the Compass hath Variation, you must allow for the Variation.

Lastly,

Lastly, By this Table having the Suns Declination, Latitude of the place, and hour of the Day, you may find the point of the Compass the Sun's upon; Thus,

Look the Latitude, and in the Declination Column the Declination, and down along under the Declination, seek for the hour given; then right against that in the left Column you'll have the point the Sun's upon.

Example 1.

In Latitude  $52^\circ 00'$  North, the Sun having  $10^\circ$  South Declination, it's required to know on what point of the Compass it will be at three of the Clock in the afternoon?

At Latitude  $52^\circ$ , under  $10^\circ$  South Declination: I look for  $3^h$ , but not finding that, I take the next I can find to it, which is  $2^h 53'$ , and in the left hand Column right against it, is 4 points, which is S W.

Example 2.

In Latitude  $58^\circ$  North, the Sun having  $16^\circ$  North Declination, it's required to know on what point of the Compass he will be at 8 hours before noon, or 4 of the Clock in the Morning?

At Latitude  $58^\circ$  North, under  $16^\circ$  North Declination: I look for 8 hours: but not finding that, I take the next to it, viz.  $8^h 2'$ , and in the left Column right against it is three points, from the East Northward, that is NE by E.

The Use of Table XV. page 194.

XV. The fifteenth Table beginning under  $30^\circ$  of the Sines, Tangents, and Secants, is a Table of the points of the Compass, the Sun Rises or Sets on, in all Latitudes to  $60^\circ$ .

Look the Latitude on the head of the Table, and down along under it for the Declination, against which in the left Column you'll have the point of the Compass the Sun Rises and Sets with, and consequently the Variation of the Compass.

Example 1.

Suppose I being in Latitude  $32^\circ$  North, and the Sun having  $9^\circ 30'$  Declination North, observe the Sun to rise by the Compass ENE, I demand the true point the Sun should rise on, and consequently whether my Compass have any Variation, and if any how much.

I look



I look in this Table on the head for the Latitude, and under that for  $9^{\circ} 30'$  Declination: and against it I find one point, which is to the Northward of the East, because the Declination is North, so that the true point of rising is E by N, and of setting W by N: but by the Compaſs it's ENE, between theſe two are one point difference, which is the Variation. If I were to obſerve the Sun ſetting by the Compaſs, I ſhould find him ſet due Weſt by it, forasmuch as one point added to the Weſt by North gives Weſt.

## Example 2.

Being in Latitude  $44^{\circ}$  North, and the Sun's Declination  $10^{\circ}$  North, I obſerve the Sun to riſe upon the E by N point of the Compaſs: I demand the Variation?

Looking in the Table as directed, I find  $1\frac{1}{4}$  points from the Eaſt Northward to be the point of riſing, which is E by N  $\frac{1}{4}$  Nly, but by the Compaſs it's juſt E by N, therefore I conclude  $\frac{1}{4}$  point Variation.

## Example 3.

Being in Latitude  $53^{\circ}$ , and the Sun's Declination being  $15^{\circ}$  South, I find the Sun Riſe upon the E by N point of the Compaſs. I demand the Variation? By the Tables the Sun ſhould riſe ESE  $\frac{1}{4}$  Sly, therefore there's  $1\frac{1}{4}$  Variation. Where you cannot find the Declination exact take the next neareſt.

## The Use of Table XVI. page 201.

XVI. The ſixteenth beginning under the  $32^{\circ}$  of the Sines, Tangents, and Secants, is a Table of the Latitudes and Longitudes of places, the Longitude beginning at the Meridian of the Lizard, and increaſing both ways, that is both Eaſt and Weſt, and terminating at  $180^{\circ}$ , whence all places that lye on the Eaſt ſide of the Meridian of the Lizard lye in Eaſt Longitude: and on the contrary, all thoſe places that lye on the Weſt ſide of the Meridian of the Lizard, lye in Weſt Longitude.

If a Ship be in Eaſt Longitude, and Sail Eaſtward, ſhe increaſeth her Longitude, but Sailing to the Weſtward, ſhe decreaſeth her Longitude. On the contrary, if a Ship be in Weſt Longitude then Sailing to the Weſtward the Longitude increaſeth, and Sailing to the Eaſtward it decreaſeth.

Note alſo that to all thoſe places that lye in Eaſt Longitude, the Sun comes to their Meridian before he comes to our Lizard Meridian. And to all the places that have Weſt Longitude, the Sun or Star comes to their Meridian, after he is paſt the Lizard Meridian.

To

To find the Difference of Longitude between any two places, if they have both Eaſt or both Weſt Longitude, ſubſtract the leſſer Longitude from the greater, and the Remainder is it: but if one place be in Eaſt, and the other in Weſt Longitude, add, and the ſum is the difference of Longitude.

This Table though very well deſigned in making the Longitude begin from the Meridian of the Lizard, which being nearly the ſame with that of Uſher is the moſt convenient for all Engliſh, French, Dutch, Danes, &c. that Sail out at and come into our Channel that can be, yet to prevent others verdiſt I muſt acknowledg the Longitudes and Latitudes of the places therein not to be ſo true as they ought to be. But 'tis hoped the truth and goodneſs of the other Tables in this Volume will pretty well compenſate the badneſs of this.

## The Use of Table XVII. page 253.

XVII. The ſeventeenth is a Table of the Sun's Declination. To find the Declination thereby, look the year and month in the head of the Table, and the day of the month in the Left-hand Column of the Table, and in the Angle of meeting you'll have the Declination you ſeek for: as,

Suppoſe the Sun's Declination be required on the twenty fifth of July, 1681.

In the head of the Table I find the year and month, and in the left-hand Column of the Table, the Day, and in the common Angle of meeting is  $17^{\circ} 8'$ , the Declination required.

But if you be far Eaſt or Weſt from the Meridian of London, for which theſe Tables were computed, you muſt allow for it, making the Declination ſomewhat greater or leſs than what it is in the Tables; for if you be to the Weſtward, the Sun coming to your Meridian after it has paſſed the Meridian of London, for which the Tables are made, the Declination will be ſomewhat increaſed, and if you be to the Eaſtward, it will be diminished, thus by the ſmall Table for this purpoſe.

Admit April 20th, 1679. I be in  $118^{\circ}$  Eaſt Longitude, what will be the Sun's true Declination on that day in that Latitude?

The Declination for the 20th of April in the Meridian of London is  $14^{\circ} 52'$ , and the dayly difference at that time is  $19'$ , therefore in this Table, I look in the head thereof for the neareſt number to  $19'$ , which is 18, then I look on the left-hand of the Table for 118, but not finding that I take the next, viz. 120, and look againſt it 'till under 18, and there I find  $6'$ , which I ſubſtract from the Declination: in the Meridian of London  $14^{\circ} 52'$ , and the remainder  $14^{\circ} 46'$ , is the true Declination for that Meridian or Longitude I am in. But if the Declination had decreaſed, which is eaſily diſcerned, by obſerving whether the Declination for the Day following be greater or leſſer than that given, then you muſt have added.

The:



The Declination in the Meridian of London . . . . .	14° 52' N,
The proportional Minutes Subtracted . . . . .	0 06
The Declination for the Longitude 118° East . . . . .	14 46
The Declination for the Longitude 118° West . . . . .	14 58

To take away all doubt in this business remember these Rules.

1. If the Longitude be Easterly, and the Declination increase, the proportional parts abovementioned, must be subtracted, but the Declination decreasing it must be added.
2. If the Longitude be Westerly, and the Declination increasing, the proportional Minutes must be added to the Declination found, but if the Declination be decreasing, you must subtract.

July 25th, 1679. Being 75° Longitude West, I require the Suns true Declination at noon that day in the said Meridian from London.

The Declination at London . . . . .	17° 16' N,
The proportional Minutes . . . . .	03
The Declination in Longitude 75° East . . . . .	17 19
The Declination in Longitude 75 West . . . . .	17 13

### The Use of Table XVIII. page 258.

XVIII. The eighteenth is a Table of the Suns Right ascension, to be entred just as that of the Suns Declination was, by looking the month on the head of the Table, and the day of the month in the left-hand Column, and in the Angle of meeting you have the Suns Right-ascension for the Month and day proposed.

### The Use of Table XIX, page 259.

XIX. The nineteenth is a Table of the Right-ascension and Declination of the most notable fixt Stars, computed for the year 1700, but by the Differences that are adjoynd to them, it may serve for any other time, either past or to come.

It

It consists of five Columns, in the first are the names of the Stars, in the second their Rightascensions in time, in the third their Declinations, in the fourth the Difference of Rightascensions in 100 years, in the fifth the Difference of Declination in 100 years, and in the fifth their Magnitudes.

To take out the Rightascension and Declination, requires only your looking the Stars name in the first Column, and right against it under the respective Titles, you have the Declination and Rightascension.

The Declinations of the Stars are used in the very same manner, to find the Latitude by, as the Suns, the Rules for which you'll find in the latter Part of the Navigation.

If the time be above 10 years, before or after the year 1700, you must find the proportional Parts or Minutes to be added or subtracted; thus,

Say if 100 give the Minutes Difference: what shall 5, 10, or 20, years, &c. give?

Let it be required to find the Declination of *Caput Medusa* for the year 1750. In the Table I find its Declination for 1700, to be 39° 47', and the Difference in 100 years to be 25'. As 100 : 25' :: 50 to 12', which added to 39° 47', makes 39° 59' the Declination.

Thus are the Differences of Rightascensions to be used for time to come: But will not need taking notice of till after the year 1720.

To find the time of a Stars coming to the Meridian.

Subtract the Suns Rightascension, from the Stars Rightascension if it may be, and the Remainder is the time of the Stars coming to the Meridian: but if the Stars Rightascension be less than the Suns, add thereto twenty four hours, and then subtract, and the Remainder is the time afternoon of the Stars coming to the Meridian: but if the Remainder exceed twelve hours, subtract twelve therefrom, and then the rest is the time from Midnight.

### Example 2.

Suppose the time of *Aldebarans* coming to the Meridian, be required on December 18th.

I find in the Table the Stars Rightascension to be 4<sup>h</sup> 17', and the Suns to be 18<sup>h</sup> 33'.

Now because the Suns Rightascension is more than the Stars, I add 24<sup>h</sup> to the Stars which makes 28<sup>h</sup> 17', from which subtracting the Suns Rightascension there remains 9<sup>h</sup> 44', for the time afternoon of the Stars coming to the Meridian.

Bbb

Example



## Example 2.

Let the time of the bright Star in *Lyra* coming to the Meridian, July 25th be required.

The Stars Rightascension is . . . . .	18 <sup>h</sup> 26'
The Suns Rightascension is . . . . .	8 58
	<hr/>
	9 28

To find what Star will be on the Meridian at any time proposed.

To the Suns Rightascension add the time from Noon given, the Sum is the Rightascension of a Star that will be on the Meridian at the time proposed: which looked amongst the Stars Rightascensions will shew you what Star it is that then culminates.

Let it be required to find what Star will be on the Meridian July 25th, at eight of the Clock at Night.

The Suns Rightascension for the time is . . . . .	8 <sup>h</sup> 58'
The time from Noon is . . . . .	8 00
	<hr/>
The Sum is the Rightascension of a Star . . . . .	16 58

Which looked in the Table of the Stars Rightascension shews it will be *Caput Herculis*, and the left shoulder of *Hercules* comes within a few Minutes after.

## The Use of the Table of Versed Sines.

XX. The twentieth is a Table of *Versed Sines* both Natural and Artificial, whose uses are very many, too numerous to be here all treated of: I shall now only shew how by them more easily to solve some of the most useful cases of Spherical Triangles, which alone is enough to merit their publication. It has been a long time the votes and desires of many able Men in the Mathematicks, that such a table might be Collected and published, but especially of that ingenious and ancient Student Mr. *John Collins*, who has expressed his desire thereof more than once in his elaborate Pieces, and from whom I had the Loan of some Forin Tables, which did assist much towards the composing of these.

Prop.

## Prop. I.

Two sides of an Oblique Spherical Triangle, with the Angle Comprehended, being given, to find the third side.

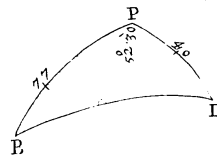
As the Cube of the Radius,  
Is to the Rectangle of the sines of the Comprehended sides,  
So is the Square of the sine of half the contained Angle,  
To half the Difference of the Versed Sines of the third side,  
And of the Ark of Difference between the two including sides.

Which is thus, Double the Logar. Sine of half the Angle given, and thereto add the Logar. Sines of the containing sides, and from the left hand of the Sum, dath out 3 for the Cube of the Radius, foreests the Logar. of half the Difference of those two Versed Sines.

Which half Difference doubled, and added to the Versed Sine of the Difference of the Legs or containing sides, gives the Versed Sine of the side sought.

## Example 1.

In the Triangle BPL, let there be given the side BP 77° 00', the side PL 40° 00', and the contained Angle BPL 52° 30', to find the side BL.



The Logar. Sine 40° 00' . . . . .	9,8080673
The Logar. Sine of 77° 00' . . . . .	9,9887239
The Logar. Sine of 26° 15' doubled . . . . .	19,2914116
	<hr/>
The Natural Sine against . . . . .	39,0882030

Is 1227355; whose double is . . . . . 2454710  
The Natural Versed Sine of 37° 00', the Diff. of the two sides is . . . . . 2013645

The Versed Sine of 57° 53' the side sought. . . . . 4468355

If you make the third term, the Square of the Sine of half the Complement of the contained Angle to 180 Degrees, you will find the half Difference of the Versed Sines of the third side, and of the Sum of the two including sides to be doubled, and subtracted from the Versed Sine of the said sum.

But



But if instead of the second Term be taken into the Proportion, the double of the Rectangle of the Sines of the containing sides; that is, if the Logar. of the Number 2 be added to the Logar. of the other middle Terms, you will have the Logar. of the whole Difference in the last place: having found it, take the Natural sine that stands against it and add it to the *Natural Versed Sine* of the Difference of the Legs, and the sum is the *Natural Versed sine* of the side sought.

*Example 2.*

Let the two containing sides be  $38^{\circ} 30'$ , and  $66^{\circ} 30'$ , and the contained Angle be  $20^{\circ} 00'$ .

The Logar. Sine of $38^{\circ} 30'$	9,7941456
The Logar. Sine of $66^{\circ} 30'$	9,9623978
The Logar. of the Numbers 2	0,3010300
The Logar. sine of $15^{\circ} 00'$ doubled is	18,8259924
The nearest Natural sine against	38,8835698

$66^{\circ} 30'$ Is	770091
$38 30$ Which taken from the Nat. Versed sine of $28^{\circ} 00'$	1170524
$28 00$ There remains	300433 the
	Natural Versed sine of $53^{\circ} 10'$ .

This Proposition is of great Use to Calculate the Distances of Places on Earth, according to the Arch of a Great Circle, by their Longitudes and Latitudes given; the Distances of Stars, by having their Declinations and Rightascensions, or Longitudes and Latitudes given, by means whereof the Altitudes of two Stars, or of the Sun with the Difference of time or *Azimuth* being observed at any time off the Meridian, the Latitude may be found.

F I N I S.



# GEOGRAPHY:

Or, a Brief

## DESCRIPTION

Of the whole

# EARTH.



THE Earths Surface, whose Description is properly termed Geography, is by many and sufficient Arguments made appear to be of no other than a Spherical Figure; and the Circumference thereof hath in this our Age been more curiously than hertofore inquired into, and found by the Concordant Observations of the Gentlemen of the Royal Academy of *Paris*, and of our worthy Countryman *Mr. Normand*, to be very near 25000 *English* Statute Miles, and consequently its Diameter 7958 Miles: The greater part of this vast Globe is covered with Water, which we call the Sea. out of which the Land rises with very slow Ascents, the hight of the highest Mountains and Prominences thereof scarce amounting to the two thousandth part of its Radius, and only serving to cause the Rivers to run with slow and easie Channels. The Air on all sides encompasses it and renders it habitable, and the principle of Gravitation, whereby all Bodies descend towards its Center, is that which defends it from dissolution, by not permitting the least part thereof to be separated far from it; into the reason whereof Philosophers have hitherto inquired in vain. This Globe by its two-fold motion enjoys the grateful Vicissitudes of Day and Night, Winter and Summer; the former by turning round upon one of its Diameters in the space of 24 hours, and shewing all its sides successively to the Sun: This Diameter is called the Axis, and its extremities the Poles of the World, which by the experience of many Ages are found unalterable and fixt in the Earth, and the direction of this Axis by some unknown Magnetical Principle of Nature is always carried parallel to it self, during the time of the revolution of the other motion, whereby the Earth is carried round the Sun in the space of a year, and the Axis being inclined to the plain in which the annual motion is performed, causes the one Hemisphere to have more of the Suns

A

light



light for the one half year, and the other Hemisphere for the other. These affections though necessary to be premised here, you will find explicated and demonstrated more at large in the Astronomical part. We come now to the Explanation of the terms which have been thought proper in the illustration of Geography.

We must observe that there are greater and lesser Circles, and that the former divide the World into two equal parts, and the latter into two parts also, but unequal. All these Circles severally are divided into three hundred and threescore parts, which are called Degrees.

There are four greater Circles, to wit, the *Equinoctial*, the *Zodiac*, the *Horizon* and the *Meridian*, and as many lesser, to wit, the Tropicks of *Cancer* and *Capricorn*, and the two Polar Circles, the *Arctic* and *Antarctic*.

The *Equinoctial* Circle is so called, because when the Sun enters it, the days and nights are of an equal length; it is also called the *Equator*, because it divides the World into two equal parts. Seamen call it only the *Line*. For the right understanding of this Circle, we must know that the Heavens seem to move upon two points, called Poles, the one bearing the name of *Arctic*, and the other of *Antarctic*; in a middle distance from which Poles this Circle is imagined to be: the use of it in Geography, is to divide the Earth into two parts, the one Northern, towards the Pole *Arctic*, and the other Southern towards the other opposite Pole. The Latitude of places is reckoned from the *Equinoctial* where it begins, towards the Poles wherein it ends, and this space contains ninety Degrees. Latitude is either Northern towards the Pole *Arctic*, or Southern towards the *Antarctic*.

The *Zodiac* is the Sun's High-way, and this Circle cuts the *Equinoctial* into two equal parts, from which its greatest distance is but twenty three Degrees and an half; it only shews what places of the Earth may have the Sun perpendicular, and more properly belongs to the Heavens than the Earth.

*Horizon* is as much as to say, boundary, because that Circle limits our sight, and divides the Heavens and the Earth into two parts, which are called Hemispheres, the one whereof we see, but cannot the other. There is a right *Horizon*, a Polar or Parallel one, and an oblique one; those places that lye under the Equator, have a right *Horizon*, and are in the right Sphere; those that are under either of the Poles have the Parallel Sphere: and all other places have an oblique *Horizon*, and are in an oblique Sphere. This Circle shews the Rising and Setting of the Stars, and the four principal Quarters of the World, which are East, West, South and North; the East is on the side of the Rising Sun; the West is where the Sun Sets; the North is towards the Pole *Arctic*; and the South towards the *Antarctic*. These four Quarters are very necessary for distinguishing the limits of Regions, as will appear throughout this whole Treatise. From thence come the four principal winds, all which the *Horizon* sheweth; but it is not marked on Maps, but only on the outside of Globes and Spheres.

*Meridian* signifies Mid-day Circle, because when the Sun is come to it; it is Noon in that place whereof it is the Meridian; for over every part of the Earth there is a Meridian, so that the number of these Circles is almost

almost infinite: However out of all those there is one pitched upon which is called the great or first Meridian, or the Geographers Meridian. The Ancients chose the Meridian of the *Canaries*, which they knew by the name of the fortunate Islands; and some Moderns make use of it still in their Maps. Others have pitched upon the Meridian of the Isles *Azores*, or Western Islands, which lie to the West of *Europe*. From this first Meridian the Longitude of places is reckoned from West to East through the three hundred and sixty Degrees of the *Equinoctial*, which is the circuit of the whole Earth; whereas Latitude is only reckoned to ninety Degrees, which make but a fourth part thereof.

The Tropicks are so called from a Greek Word *Tropos*, which signifies turning, because when the Sun is come to one of these Circles, he returns again towards the *Equinoctial*.

The Tropick of *Cancer* is towards the Pole *Arctic*, and that of *Capricorn* towards the *Antarctic*, and both carry the names of the Signs of the *Zodiac* through which they pass; each of them is distant from the *Equinoctial*, three and twenty Degrees and a half, which is the greatest distance of the Sun from that Circle.

The Polar Circles go round the Poles, from which they borrow their names, and are distant each from his Pole twenty three Degrees and a half.

### Of the Zones.

THE four lesser Circles whereof we have been speaking, divide the World into five parts, called *Zones*, that is to say, Belts or Girdles, because they begird the whole Globe. One of them is Torrid, two are temperate, and two cold: The Torrid *Zone* is comprehended between the two Tropicks, and the people that inhabit it are called *Amphiscians*, that is, such as have their shadows both ways. To all places of this *Zone* the Sun comes perpendicular twice in a year, and therefore some of the Ancients believed this *Zone* inhabitable, by reason of too much heat; but we know it to be otherways now a days.

The Northern temperate *Zone* is between the Tropick of *Cancer* and the *Arctic* Polar Circle: The Southern temperate *Zone* is between the Tropick of *Capricorn*, and the *Antarctic* Polar Circle. The Inhabitants of these *Zones* are termed *Heteroscians*, that is, such as have their shadow but one way.

The Frigid *Zones* are within the Polar Circles, the Northern within the *Arctic*, and the Southern within the *Antarctic*; the people of those two *Zones* are called *Periscians*, signifying that they have shadows round them on all sides. To all places in these *Zones* the Sun in Summer never sets for some days, and in the Winter he never rises for as long time.

The Inhabitants of the World are distinguished after another manner, according to the different Situation they have to one another; as into *Antipodes*, *Antacians* and *Periacians*. The first are wholly opposite, and when it is Noon with us, with our Antipodes it is midnight, and they have Winter when we have Summer. Our *Antacians* have Noon and Mid-night when



we have them, but Winter for our Summer. And our *Perigians* have the same seasons that we have, but the hours quite contrary; for when we have Noon it is Mid-night with them.

### Of Climates.

A Climate is a space of the Earth contained between two Circles. Betwixt the beginning and end of a Climate, in the length of the longest day of Summer there is half an hours difference. For the clearer understanding of this, it is to be observed that Countries under the Equinoctial have all the year round twelve hours day and twelve hours night; but as places recede and are distant from the Equator, they become more and more unequal, and the days in Summer are longer than the nights. This inequality is marked by the Climates; so that when on either side of the Equinoctial we find a place where the longest day of Summer is of twelve hours and a half, that is the first Climate, and so successively till we come to the Polar Circle, where the longest day of Summer extends to twenty four hours: For beyond that Circle, the days encrease by whole days and months, until ye come to the Pole under which the whole year makes but one day and one night, six months long a piece. Climates take their names from the famous places through which they pass.

Now to know in what Climate one is, we must from the number of hours of the longest Day in Summer subtract twelve, and double the Remainder; that is, reduce them into half hours, and that will shew the Climate wherein we live.

## CHAP. I.

### Of some proper terms of Geography.

HAVING explained the Circles that are useful to this Science, we are now to consider some terms and words which are peculiar to it.

*Continent* is a vast space of Earth, such as that which comprehends *Europe*, *Asia*, and *Africa*; it is likewise called the main Land.

*Island* is a piece of Land furrounded with the Sea or other Water, and so divided from the Continent.

*Peninsula*, that is to say, almost Island, is a part of the Earth encompassed by the Sea on all hands, except on that part which joyns it to the Continent: the *Greeks* call it *Chersonesus*, a term sometimes made use of in Geography.

*Isthmus* is that Neck or Piece of Land that joyns a Peninsula to the Continent.

*Promontory* is a high Land running out into the Sea. The Moderns call it a Cape.

Moun-

*Mountain* is a part of the Earth higher than the rest that is about it.

*Ocean* is that vast body of Water which environs the Continents, and is likewise called the Sea.

*Gulph* is an Arm of that Ocean running in between Lands. The *Latins* call it *Sinus*, and sometimes it has the name of Sea.

*Bay* is likewise an Arm of the Ocean, but whose entrance is much wider than that of a Gulf.

*Port* is a small part of Sea so hem'd in by the Land, that Ships may there lie in safety.

*Harbour* is the same thing almost.

*Streight* or *Frith* is commonly taken for a Channel that joyns one Sea to another, or a Gulf to the Ocean; there is also a Streight or Neck of Land, which, as we have said, is called an *Isthmus*.

*Bank* is a heap of Sand in the Sea, which puts Vessels in danger.

A *Shelf* is much the same, on which, and on hidden Rocks near the Surface of the Water Ships may split and be cast away.

*Archipelago* is a part of the Sea, where many Islands are.

*River* is a running Water that loses its streams in the Sea.

## CHAP. II.

### The Division of the Earth and Sea.

THE most common Division of the Earth is into four parts, which are *Europe*, *Asia*, *Africa* and *America*: the three first are comprehended in one Continent, and is our old World; and the other makes an Island of it self, called the new World, because it hath not been discovered but since the Year one thousand four hundred and ninety two: it is likewise called the *West-Indies* in distinction from the *East-Indies* which are in *Asia*.

Some Geographers divide the Earth into six parts, adding to the four which we have named, the *Arctic* towards the Pole that gives it its name, and the *Antarctic* towards the South Pole: this is called *Terra Australis incognita*, or the Southern Land undiscovered, and is thought to make a Continent as big as *Europe*, *Asia* and *Africa*. Of these two last we shall speak at the end of this Treatise.

*Europe* has *Asia* on the East separated from it by these limits, the *Egean* Sea or *Archipelago*, the Streights of the *Dardanelli*, the Sea of *Marmara*, the Streights of *Constantinople*, the *Black* Sea, the Streights of *Cassa*, the *Sedda*, *Zibache*, the River *Tanais* and a Line drawn from its most Eastern Bank to the North Sea: it hath the same Ocean on the North, the *Atlantic* Sea on the West, and the Streights of *Gibraltar* and *Mediterranean* Sea that divides it from *Africa*, on the South. From West to East, that is, from Cape *St. Vincent*, in *Spain*, to *Constantinople*, it contains seven hundred seventy five

French



French Leagues; and from South to North, that is, from *Cape Malee* in *Marea* to the Northern Cape of the *Laplanders*, eight hundred and twenty five Leagues.

*Asia* has to the West the same bounds that divide it from *Europe*, and the *Red Sea*, with the Straights of *Suez*, that divide it from *Africa*; on the South the *Indian Ocean*, the Ocean of *China* on the East, and on the North, the Sea of *Tartary*, called *Mare Glaciale*. From East to West it contains seven hundred and fifty Leagues, from the *Archipelago* to the Ocean of *China*; and from South to North a thousand five hundred and fifty, reckoning from *Malacca* to the Sea of *Tartary*.

*Africa* has on the North the *Mediterranean Sea*, on the East the *Red Sea*, with the *Isthmus* of *Suez*, that divide it from *Asia*, and the *Indian Ocean*: On the South the *Ethiopian Sea*, which with the *Atlantic Ocean* is likewise to the West of it. From West to East, that is, from *Cape Blank*, to the Cape of *Guardafwy*, it contains a thousand six hundred and fifty Leagues: and from South to North, that is, from the Cape of *Good Hope*, to the *Mediterranean Sea*, a thousand six hundred and seventy. It is on all sides encompassed with the Sea, except that narrow track of Land between the *Red Sea* and *Mediterranean*, which is not above thirty Leagues in Length: so that it is a perfect Peninsula.

*America* hath the North Sea to the East, the South Sea to the West, to the South the Straights of *Magellan*, which divide it from the *Terra del fuego*, and to the North unknown Lands or Seas. It is divided into two great Peninsulas, by the narrow *Isthmus* of *Panama*, which is but eighteen Leagues over: From South to North, that is, from the Straights of *Magellan* to the Northern Ocean, it contains three thousand and fifty Leagues; and from West to East, towards *Mexico*, two thousand nine hundred.

The *Terra Australis*, and that of the North, are so little known to us, that their limits and extent cannot as yet be designed.

Having taken a view of the Earth, let us now cast our eyes on the Sea, which takes divers names according to the parts of the World where it is, or the Countries it watheth. That which encompasseth Continents is called the Ocean; and this likewise hath different appellations, as on the West of *Europe*, and part of *Africa*, it is called the Western or *Atlantic Ocean*; towards the Cape of *Good Hope*, the *Ethiopian Ocean*; to the East of *Africa*, the *Indian Sea*; to the East of *Asia*, the Eastern Ocean, or Sea of *China*; to the North of *Asia*, the Sea of *Tartary*, and on the same side, and towards *Europe*, *Mare Glaciale* or the Frozen Ocean; to the East of *America*, the North Sea, and to the West, the South. These are the general denominations of the Sea, but it hath also particular names from the Countreys that lie near to it.

The chief Gulfs or Bays of the Ocean are the *Mediterranean Sea*, which lies betwixt *Europe*, *Africa* and *Asia*; the *Red Sea*, betwixt *Africa* and *Asia*; the Gulf of *Persia*, and that of *Bengala*, in the East-Indies; the *Baltick Sea* encompassed by *Germany*, *Sweden* and *Denmark*; the Gulf of *Mexico*, and that of St. *Lawrence*, in *America*.

These

These Gulfs are joyned to the Ocean by Straights; the *Mediterranean Sea* by the Straights of *Gibraltar*; the *Red Sea* by that of *Babel-mandel*; the *Persian Sea* by the Straights of *Bassora*, otherwise of *Ormuz*. The Gulfs, or rather Bays of *Bengala*, *Mexico* and St. *Lawrence* have no Straights, because their mouth or entry is very large.

The *Baltick Sea* has the famous Strait of the Sound.

The *Mediterranean Sea* hath some noted Bays that well deserve to be mentioned. Betwixt *Italy* and *Dalmatia* is the Gulf of *Venice*, called in ancient times the *Adriatick Sea*. In *Greece* is the Gulf of *Lepanto*, heretofore of *Corinth*. And in *Macedonia* that of *Salonica*, formerly of *Thessalonica*.

Between the *Egean Sea*, now called the *Archipelago*, and the *Propontis* or Sea of *Marmora*, there is a Strait heretofore called the *Hellepont*, and at present the Straights of *Gallipoli*, or the *Dardanelli*, and St. *Georges Channel*; between the Sea of *Marmora* and the black Sea, formerly called the *Euxin Sea*, is the *Bosphorus* of *Tbrace*, which is now always called the Channel of the *Black Sea*, or Straights of *Constantinople*, because that famous City is seated there; betwixt the *Black Sea* and the *Palus Meotides*, at present called the *Sea delle Zabache*, is the Straights of *Cassa*, heretofore named the *Cimmerian Bosphorus*.

Betwixt the Island of *Eubæa*, at present *Negropont*, and *Greece*, there is a narrow passage of Sea, by the Ancients called *Euripus*, who have affirmed that it ebbed and flowed seven times a day. There are some other famous Straights which joyn several parts of the Ocean together; or to say better, the Ocean to the Ocean it self.

Towards the Northern Ocean is the Straights of *Waigatz*, between *Tartary* and *nova Zembla*; between *Cathay* and the Land of *Jesso*, is the Straights of *Jesso*; between *Japan* and the Land of *Jesso*, is the Straights of *Sengar*; between the same Land and *Californiæ*, is that of *Anian*; between *Estotiland* and *Greenland*, is that of *Davin*; between *Greenland* and the Island of *Elizabeth*, is that of *Forbisher*.

Towards *Canada* is that of *Hudson*, which according to the new Maps is properly a Gulf.

Towards the *Terra Australis* is the famous Straights of *Magellan*, discovered by him who gave it the name, in the year one thousand five hundred and twenty, between *America* and the *Terra del fuego*.

Betwixt this Land and that of the States, is the Straights of *Le Maire*, discovered in the year one thousand six hundred and sixteen.

And between that Land of the States and the *Terra Australis*, is the Straights of *Brouwers*, discovered in the year one thousand six hundred and forty three. These three last Straights joyn the North and South Seas together, and serve for a passage from one to the other.

Between *Californiæ* and new *Mexico*, there is a Gut of Sea, or Straights, which is called the *Vermeillan Sea*, and was taken for a Bay before that *Californiæ* was discovered to be an Island.

We



We must not omit a Sea that is separated from all others, and which indeed is but a Lake of a vast extent, and that is the *Caspian* Sea, called at present the Sea of *Bachm* or *Kilan*. The Ancients imagined it to have been a Bay or Gulf of the North Sea, but it is now known to be on all sides encompassed with Land; it hath *Persia* to the South, and *Tartary* to the North of it: In some Relations it is reckoned to be eight hundred Leagues in Circumference.

Let us now give a hint of the greatest Rivers in the World, beginning with those that fall into the Ocean, on all sides of our Continent or old World.

In *Europe* are the River *Tagus*, the *Garonne*, the *Loyré*, the *Sein*; the *Scheld*, the *Rhine* and the *Elbe*.

In *Asia* the *Oby*, the yellow and blue Rivers, *Ganges* and *Indus*.

In *Africa*, *Cuama*, the River *de Spiritu Sancto*, the *Zaire*, and the *Niger*.

In *America* the Rivers of *St. Laurence*, *Oranogue*, the *Amazons*, and *Rio de la Plats*.

Into the *Mediterranean* Sea on the side of *Europe*, fall the *Ebre*, the *Rhosne*, and the *Tiber*; into the Gulf of *Venice*, the *Po*; into the *Euxin* Sea the *Danube*, and the *Borysthenes*, now called *Nieper*, and the River *Tanaïs* runs into the *Palus Meotis*.

On the *African* Shore the *Mediterranean* receives no famous River but the *Nile*.

In *Asia*, *Euphrates* and *Tygris* having mingled their streams fall into the *Persian* Gulf, and the *Volga* into the *Caspian*.

The *Oder* and the *Weissel*, or *Vistula*, discharge themselves into the *Baltick*; and the *Duina* into the *White* Sea.

We shall not speak of the chief Lakes till we come to describe the particular Regions wherein they are:

But we will here subjoin the most noted Mountains of the World, such as in *Europe* are, the *Pyrenees*, the *Alps* and *Appenine-Hills*. In *Asia*, *Taurus*, *Caucasus* and *Imaus*; in *Africa*, *Atlas* and the Mountains of the Moon; and in *America* the *Cordilleras* or *Andes*. The Islands we shall describe as we come to the several parts of the Earth near to which they lie.

Thus, Reader, you have a general description of the whole Earth, and Seas that environs it, or fall into its bosom. We must now descend to a more particular Description; and shall begin with that of *Europe*.



## CHAP. III.

*Europe.*

**E**UROPE, whereof we have already mentioned the limits, is the smallest, but most considerable for Learning and Arts of the four parts of the World: it comprehends the following Kingdoms and Regions. *Spain, France, Italy, the Low Countries, Germany, Hungary, Transylvania, Moldavia, Walachia, Bessarabia, Dalmatia, Bosnia, Servia, Bulgaria, Romania, Greece, Norway, Denmark, Sweden, Poland, Prussia, Lithuania, Livonia, or Liefland, Muscovy, and the lesser Tartary.* Its chief Islands in the Ocean, are *Great-Britain, Ireland, the Orcades and Hebrides, Iseland, and the Azores.* In the *Mediterranean Sea, Majorca, Minorca and Ivica, the Isle of Elbe, Corsica, Sardinia, Sicily, Candia, Negropont,* and many more in the *Archipelago.* We shall speak of its Rivers, Lakes, and Mountains, when we treat of the Regions wherein they are.

## CHAP. IV.

*Spain.*

**S**PAIN is surrounded by Seas on three sides; on the East and South it is watered with the *Mediterranean*, and the Famous Streights of *Gibraltar* divide it from *Africa*; to the West it hath the *Atlantick Ocean*, and to the North partly the *Cantabrick Ocean*, or Bay of *Biscay*, and partly the *Pyrenean Mountains* that reach from the *Mediterranean* to the Ocean, and divide it from *France*: most part of its Provinces are honoured with the Title of Kingdoms. On the *Mediterranean* are *Catalonia*, of which the Metropolis is *Parcelonna*, a large City, with a Sea-Port: the other Towns are *Terragonna*, an Archbishoprick, *Torose, Gironne, Lerde* or *Lerida*.

The Kingdom of *Valencia* with a Metropolis of the same name, and *Ali-cant*; the Country about which produces the best Wines in *Spain*.

The Kingdom of *Murcia*, the chief City whereof carries the same name. In this Province stands *Carthagena*, a very good Sea-Port.

The Kingdom of *Granada* that hath its name from its Metropolis lies to the West of that, and hath the Cities of *Malaga* and *Almeria*.

*Andalusia* is partly on the *Mediterranean* and Streights of *Gibraltar*, and partly on the Ocean. Its chief City is *Seville*, (one of the loveliest Towns in the World) seated on the *Guadalquivir*. Its other Towns are *Cordova*, the Native place of *Seneca* and *Lucan*, *Xeres* from whence our Sherries come,



Saint *Lucar* and the Famous Port of *Cadex* or *Cales*, which stands in a small Island of that name, very near to the Main on its East side.

The Provinces washed by the Ocean, are

The Kingdom of *Algarve*; its Cities are *Sylis* and *El Faro*.

The Kingdom of *Portugal*, anciently called *Lusitania*; which hath *Lisbon* a large fair City, and Arch-bishoprick for its Capital: the other chief Cities thereof are *Braga*, an Arch-bishops See, *Evora* and *Covimbre* a Famous University; this is now, and for many Ages hath been subject to a King of its own independent of *Spain*.

The Kingdom of *Galicia* hath *Compostella*, where the Body of St. *James* is, for its Metropolis, and *Cornuna* a good Sea-Port: this is the North-West corner of *Spain*.

*Asturia*, whereof *Oviedo* is the Metropolis, lies to the East of *Galicia*, fronting the Bay of *Biscay*: and yet more Easterly on the same Coast lies *Biscay*, whereof the chief City is *Bilboe*. And to this is adjoynd *Guipuscoa*; whereof *Tolose* or *Tolofete* is the Capital City: its other Cities are St. *Sebastian*, which hath a good Port, and *Fontarabie*. At the foot of the *Pyrenees* are the Kingdoms of *Navarre* and *Arragon*.

*Pampelonna* is the Metropolis of the Kingdom of *Navarre*; its other Cities are *Victoria* and *Ejella*.

*Sarragossa* is the Capital City of the Kingdom of *Arragon*, and a University; the others are *Huesca*, *Albarazin*, *Calatayud*, which some take for the ancient *Ibilis*, the Native Town of the Poet *Martial*: In the heart of *Spain* are *Leon*, the two *Castiles*, the old and new, and *Ejtremaadura*.

The Metropolis of the Kingdom of *Leon* bears the same name; *Astorga* and *Samora* are its other Cities.

*Bourgos*, an Archbishops seat, is the Capital City of old *Castille*; its other chief Towns are *Valladolid*, where some Kings of *Spain* have kept their Courts: *Palencia*, *Salamanca* a famous University. *Numance* that heretofore resisted the Roman Forces so long, was in this Province, but there remains no Footstep of it at present.

*Toledo* is the Metropolis of new *Castille*, and the Archbishop of it is Primate of all *Spain*, it is a stately and large City: The other chief Towns of that Province are *Madrid*, the usual Residence of the Kings of *Spain*, and five Leagues West from that, the famous Monastery of St. *Laurence*, called the *Escorial*, built by *Philip* the Second, and before it was burnt, one of the most Magnificent Fabricks in the World.

*Alcala de Henares*, famous for the University that Cardinal *Ximenes* Founded there.

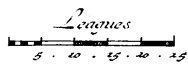
Each of the two *Castiles* is qualified with the Title of Kingdom.

*Ejtremaadura* hath two considerable Towns, *Badajos* and *Merida*.

The chief Capes in *Spain* are on the *Mediterranean*, Cape *Palafagel* in *Catalonia*, Cape *Martin* in the Kingdom of *Valencia*, Cape *Palos* in *Murcia*, and Cape de *Gates* in the Kingdom of *Granada*, Cape St. *Vincent* in *Algarve*, Cape de *Spichel* and de *Roca* in *Portugal*, and Cape *Fingsterre* and Cape *Oriogal* in *Galicia*, and Cape de *las Pennas* in *Asturia*.

The





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The G. of Cadiz



The chief Rivers that fall into the *Mediterranean* are the *Ebre* or *Iberna*, which runs through *Aragon* and *Catalonia*, and passes by *Sarragossa* and *Torose*; the *Guadalquivir* that passes by *Valencia*, and the *Xucar* in the same Kingdom; the *Guadalentia* in the Kingdom of *Marcia*: those that discharge themselves into the Ocean, are the *Guadalquivir*, otherways *Betis*, that runs through *Andalusia*, and passes by *Cordova* and *Sevil*, and empties itself into the Sea at *St. Lucar de Barrameda*: the *Guadania* in *Extremadura*, which River, a little above *Merida*, runs under ground for several Leagues, and then breaks out again.

The *Tagus* which waters new *Castile* and *Portugal*, passes by *Toledo* and *Lisbon*.

The *Duero* that runs through old *Castile* and *Portugal*, and the *Minho* that divides *Portugal* from *Galicia*.

The chief Mountains are the *Pyreneans*, *Sierra Morena*, *Sierra D' Alcaraz*, *Sierra D' Albarazin*, and the *Sierra Nevada*, commonly called the *Granadas*.

The Isles upon the Coasts of *Spain*, are the Isle of *Cadiz* in the Ocean; and near to *Andalusia*, the *Baleares*, to wit, *Majorca* and *Minorca*, the Isles of *Ivica* and *Formentera* in the *Mediterranean*.

The King of *Spain* is not at present Master of all these Provinces, for *Portugal* and *Algarbe* belong to the King of *Portugal*; and the King of *France* has made some incroachments in *Catalonia*.

There is no Religion professed in *Spain* but the Roman Catholic.

A Table of the Longitudes and Latitudes of the chief Cities and Towns of the Kingdom of *Spain*.

1. In the Kingdom of *Galicia*.

	Lat.	Long.
<i>Compostella</i> .	42 3	10 2
<i>Lugo</i> .	42 4	11 4
<i>Corunna</i> .	42 5	10 2
<i>Finisterre</i> .	43 0	9 2
<i>Cape de Ortegal</i> .	43 2	11 1
<i>Tuy</i> .	41 3	10 2

4. In *Biscay*.

	Lat.	Long.
<i>Cape Machachaca</i> .	43 4	16 4
<i>Bilbao</i> .	43 2	16 4
<i>Larido</i> .	43 1	16 0
<i>Espinosa</i> .	43 0	15 2
<i>St. Sebastian</i> .	43 2	17 4
<i>Vitoria</i> .	42 4	16 2

2. In the Kingdom of *Leon*.

	Lat.	Long.
<i>Leon</i> .	42 1	13 5
<i>Astorga</i> .	41 5	13 4
<i>Camora</i> .	41 2	13 5
<i>Salamanca</i> .	40 4	13 4
<i>Ciudad Rodrigo</i> .	40 1	12 4

5. In *Navarre*.

	Lat.	Long.
<i>Pampelona</i> .	43 0	18 1
<i>Estella</i> .	42 4	17 4

3. In the Kingdom of *Asturia*.

	Lat.	Long.
<i>Oviedo</i> .	43 0	13 1
<i>Cape de las Pennas</i> .	43 3	12 4
<i>Santilliana</i> .	43 0	14 3

6. In the Kingdom of *Aragon*.

	Lat.	Long.
<i>Saragossa</i> .	41 2	19 0
<i>Huesca</i> .	41 4	19 4
<i>Faca</i> .	41 2	19 1
<i>Catalayud</i> .	40 5	18 1
<i>Darofa</i> .	40 3	18 1
<i>Albarazin</i> .	40 0	18 2

B 2

Terrel.



	Lat.	Long.		Lat.	Long.
Tervel.	39 3	19 0	Muxarra.	36 2	17 4
Calanda.	40 2	19 2	Versa.	36 4	17 5
			Cape de Gates.	36 0	17 4

## 7. In Catalonia.

Barcelona.	40 3	22 3
Tarragona.	40 0	21 5
Tortose.	39 4	20 4
Lerida.	40 4	20 4
Solsona.	41 1	21 1
Cordone.	41 2	21 2
Blanes.	40 4	23 1
Vich.	41 0	21 5
Girona.	41 1	23 1
Montserrat.	40 3	21 5
Barraves.	42 1	21 4
Rosier.	41 3	23 5
Cape de Palafagel.	40 4	24 0
Flix.	40 1	20 3

## 8. Roussillon.

Perpignan.	42 0	23 2
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## 9. In the Kingdom of Valencia.

Valencia.	38 4	19 1
Segorbe.	39 1	19 2
Denia.	37 5	19 4
Cape St. Martin.	37 4	20 0
Bonifacia.	39 4	20 0
Xativa.	38 1	18 5
Cullera.	38 1	19 3
Seguntum.	38 4	19 4
Alicant.	37 3	19 2
Xelus.	39 2	18 2
Orignela.	37 3	18 4

## 10. In the Kingdom of Granada.

Granada.	36 5	16 0
Guadix.	36 5	16 3
Almeria.	36 1	17 2
Salobrenna.	36 2	16 3
Malaga.	36 0	14 4
Ronda.	36 1	13 5
Marbello.	35 5	14 0
Velex.	36 2	15 1
Ubeda.	37 4	15 5

## 11. The Kingdom of Murcia.

Murcia.	37 1	18 4
Cartagena.	36 5	18 5
Cape de Palos.	36 4	19 1
Lorca.	37 1	17 3

## Isle of Majorca.

Majorque.	38 2	22 5
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## Isle of Minorca.

Port Mahon.	38 4	24 2
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## In the Isle of Ivica.

Ivica.	37 4	21 1
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## Isle of Formentera.

	37 2	21 1
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## 12. Kingdom of Andalusia.

Sevil.	37 0	13 2
St. Lucar.	36 2	12 4
Xeres.	37 1	11 3
Palos.	36 5	12 0
Cadiz.	35 5	12 4
Medina Sidouia.	36 0	13 2
Echna.	36 5	14 3
Cordova.	37 2	14 5
Ayamont.	36 5	11 3
Port Real.	36 1	13 0
Gibraltar.	35 2	13 3
Tariffa.	35 2	13 1
Lucena.	36 5	15 1
Aromes.	37 4	12 4

## 13. New Castile.

Madrid.	39 5	15 5
Toledo.	39 1	15 4
Alcala de Hen.	40 0	16 2
St. Cruz.	39 0	16 2
Ciudad Real.	38 2	15 2
Malagon.	38 4	15 4
Huetti.	39 1	17 0

Cuenca.

	Lat.	Long.	15. In the Kingdom of old Castile.	Lat.	Long.
Cuenca.	38 5	17 1	Burgos.	42 0	15 4
Escorial.	39 5	15 3	Valladolid.	41 2	14 5

## 14. Estremadura.

Bajadax.	38 2	12 2	Soria.	41 2	17 0
Alcantara.	39 0	12 4	Osma.	41 0	16 5
Merida.	38 2	13 0	Avila.	40 2	14 2
Truxil.	38 3	13 4	Placentia.	39 2	13 5
			Coria.	39 4	13 0

A Table of the Longitudes and Latitudes of the most considerable Places in the Kingdom of Portugal.

## In the Province called Entre Douro &amp; Minho.

	Lat.	Long.		Lat.	Long.
Braga.	41 1	10 4	Viseu.	40 2	11 2
Porto.	40 5	10 3	Guarda.	40 0	12 1
Viana.	41 2	10 1	Trancoso.	40 3	11 3
Guimaraes.	41 1	10 5	Castel Branco.	39 3	11 5
Amarante.	41 1	11 0	Val. Verde.	40 4	11 4
Melgaom.	41 5	10 3	Sabugal.	40 0	12 2
Valensa de Minho.	41 4	10 2	Idanha.	39 3	12 2
Ponte de Lima.	41 3	10 3	Cape de Mondego.	39 5	10 0
Barcelos.	41 1	10 2			

## In the Province Trallos Montes.

Traganfa.	41 4	12 4			
Miranda.	41 1	12 5			
Castel Rodrigo.	40 3	12 3			
Villa Real.	41 0	11 3			
Chaves.	41 4	11 4			
Spadacinta.	40 5	12 4			
Pinhel.	40 2	12 2			
T. de Moncorvo.	40 5	12 2			
Mariaeva.	40 3	12 1			
Almeida.	40 1	12 4			

## In the Province of Beira.

Coimbra.	39 5	10 4			
P. Aveiro.	40 2	10 2			
Goer.	39 5	11 0			
Mira.	40 1	10 1			
Lamego.	40 5	11 3			

## In the Province of Estremadura.

Lisbon.	38 3	9 2			
Almada.	38 2	9 3			
Setuval.	38 1	10 0			
Orem.	39 3	10 2			
Alemover.	38 5	9 5			
Ega.	39 4	10 2			
Leiria.	39 3	10 1			
Tomar.	39 2	10 4			
Punbete.	39 1	10 5			
Palmela.	38 2	9 5			
Azarzedas.	39 3	11 3			
Figueras.	39 4	10 5			
Sintra.	38 4	9 1			
Cascaes.	38 3	9 1			
Atalaia.	39 1	10 3			
Santarem.	39 0	10 2			
Almerin.	39 0	10 3			
Obeder.	39 1	9 4			
Berling Island.	39 1	9 1			
Rock of Lisbon.	38 3	9 1			
Cape de Spiebel.	38 1	9 3			

In



	Lat.	Long.		Lat.	Long.
In the Province of <i>Alentejo</i> .			<i>Avis</i> .	38 4	11 1
<i>Evora</i> .	38 0	11 1	<i>Aliaftiel</i> .	37 2	10 3
<i>Elvas</i> .	38 2	11 5	<i>St. Jago de Cacem</i> .	37 3	10 0
<i>Portalegre</i> .	39 0	11 5	In the Kingdom of <i>Algarve</i> .		
<i>Villa Vicosa</i> .	38 2	11 4	<i>Silves</i> .	36 5	10 2
<i>Beja, or Bexa</i> .	37 3	10 5	<i>Lagos</i> .	36 3	10 0
<i>Olivienza</i> .	38 1	11 5	<i>Faro</i> .	36 3	10 4
<i>Montalva</i> .	39 1	11 5	<i>Tavira</i> .	36 4	11 0
<i>Estremoz</i> .	38 2	11 2	<i>Cape St. Vincent</i> .	36 3	9 4

## CHAP. V.

## France.

FRANCE is bounded on the East by *Italy*, from which it is divided by the River *Var* and the *Alpes*; by *Savoy*, *Switzerland*, the *Franche Comte*, *Germany*, and the *Low-Countries*, which are likewise to the North of it, with the Channel or Narrow Sea that divides it from *England*; on the West by the Ocean, and on the South by the *Pyrenean Hills* and the *Mediterranean*. We shall first describe its Provinces that are washed by the Ocean, proceeding from North to South.

*Picardie* hath *Amiens* for its Capital City; the other more considerable Towns are *Abbeville*, *Peronne*, *Roye*, *Corbie*, *St. Quintin*, *Calais* and *Boulogne*, which two are Sea-Ports; *Soissons*, *Laon*, *Reauvais*, *Montrucil*, *Dourlans*, *Creecy*, where *Philip de Valois* lost a Battel to the *English*, *Guise* and *Rhetel*.

*Normandy* hath *Rouen* its Capital; its other principal Towns are *Eureux*, *Bayeux*, *Caen*, *Diepe*, *Constance*, *Auranche*, and *Havre de Grace*.

*Bretagne* whereof *Rennes* is the Capital City, *Nantes*, *Vannes*, *S. Malo*, *Beauport*, *Landriguier*, *Brest* and *Blavet*, are its other Towns.

*Poitou* contains *Poitiers* its chief Towns, *Lusson*, *Maillezais*, *Niurd*, *Fontenay*, *Chastelleraud*; *Roche* is in the *Aunis*.

*Xaintonge* hath for its Capital *Xaintes*, where some *Roman Antiquities* are still to be seen; its other Towns are *Blay* and *St. John d' Angeli*.

*Guienne* hath *Bordeaux* upon the *Garonne* for its principal City; at the mouth of that River stands the Tower of *Cordonan*, a stately building, and serves for a Sea Mark to Ships. Under the name of *Guienne* several Countries are comprehended, as the *Agenois*, where are *Agea*, *Marmande*, *Clairac*; the *Condomis*, where are *Condom* and *Neras*. The County *D' Armagnac*, where are *Auch* and *Lectoure*; the County of *Cominges*, where are *Beviraud*, *Ceserans* and *Lombes*; the other Towns of *Guienne* are *Bazas*, *Ayres*, *Acs* and *Bayonne*.

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The *Basse Navarre* lies at the foot of the *Pyrenees*; its chief Towns are *Palais*, and *St. John de Pied de Port*.

The Principality of *Bern* is likewise at the foot of these Mountains; its Capital is *Pau*, and the other Towns of any note, are *Oleron* and *Lescar*.

*Bigorre* hath *Tarbes* for its Capital; *Bagueres* is likewise considerable there, because of its hot Baths from whence it has its name.

The County of *Foix* lies at the foot of the same Mountains; besides its chief Town of the same name, it hath the Town of *Pamier*.

The County of *Roussillon* taken from the *Spaniard* has the same Situation, and *Perpignan* is its Capital.

*Languedoc* comes next, and stretches along the *Mediterranean* which it hath to the South, being bounded on the North by the Mountains of *An-vergne*. The *Rhosue* divides it from *Provence* and *Dauphine* on the East, and *Gruenne* borders on it to the West; its Capital City is *Tbalouze*, *Montpelier* is the next: the Bishops seat was at *Maguelonne*, which is now ruined, nothing remaining but two Churches. It stood in an Isle in the middle of a Pool or Lake, which hath Communication with the Sea. This is that Town which *Ptolomy* calls *Agatha*, and which some Geographers take for *Agde*; but that Author calls this last *Agathopolis*, near the *Eraut*, which removes all doubt: besides, that he calls *Agatha* an Isle and City. Now there never was any City in an Isle upon that Coast, except *Maguelonne* alone, which changed its name with the Fate and Wrack of the *Roman Empire*. It is somewhat strange that the greatest Geographers should have been ignorant of this which is so easy to be perceived by any that will consider *Ptolomy* and the Situation of that Country. I make this remark in favour of *Montpellier*, which is enlarged by the Ruins of *Maguelonne*; enriched with its spoils, and adorned with its Bishoprick which was transferred thither by Pope *Paul* the third, in the Reign of *Francis* the first, the Year one thousand five hundred and thirty six. The other Towns of *Languedoc*, are *Narbonne*, an ancient *Roman Colony*, as well as *Nismes*, which by its stately Antiquities still shews what was heretofore the splendor of that place: There is an Amphitheatre, the most entire of any that is to be seen of that kind in the World, a Royal Palace, and some other magnificent Reliques of the *Roman Age*. Four Leagues from this City is a stately Aqueduct, which is called the *Pont du Gard*, because it is upon a River of that name. *Carcasson*, *Besiers*, *Agde*, *Viviers* and *Beaucaire*, famous for the Fair of *Magdalene*, are the other Towns of this Province, which is one of the pleasantest in France.

*Provence* is divided from *Languedoc*, that lies to the West of it, by the *Rhosue*, and from the County of *Nice*, which it hath to the East, by the *Var*; and from *Piemont* by the *Alpes*, it hath the *Mediterranean* to the South, and *Dauphine* to the North: its chief Towns are *Aix* its Capital, *Marseilles*, *Arles*, *Frejus*, *Toulon* one of the best Sea-Ports in France, *Hieres* and some others: *St. Maximin* preserves the Body of *Mary Magdalen*.

The County of *Venaissen* that belongs to the Pope is shut in within the limits of this Province, its Towns are *Avignon*, *Carpentras*, *Cavaillon* and *Vaison*.



The Principality of *Orange* belonging to the Princes of the House of *Nassau*, who from thence have their Title, is inclosed within the County of *Venaissin*. There is no considerable Town in it, but that of *Orange*, where are the Ruins of an Amphitheater, and a Triumphant Arch of *Marius*.

*Dauphine*, which is divided from *Languedoc* by the *Rhône*, and from *Piemont* by the *Alpes*, contains these principal Towns following; *Grenoble* its Capital, and *Ambur*; this upon the *Durance*, and that upon the *Isère*: *Vienna* and *Valence* upon the *Rhône*, both very ancient.

The *Lyonnois* is to the North of *Dauphine*, and *Lions*, one of the greatest and fairest Cities of *France*, is its Capital; it's situated on a point where the *Saône* mingles its still and gentle waters with the rapid streams of the *Rhône*: it hath no other Towns of great note.

*Bresse* is to the North of the *Lyonnois*; its chief Towns are *Bourg* in *Bresse*, *Montluel*, *Pont de Vaux*, and *St. Julian*.

The Principality of *Dombes*, which belongs to *Mademoiselle* of *Montpensier*, Cousin German to the King of *France*, is inclosed within *Bresse*; the chief Town of it is *Trevoux*.

The Duchy of *Burgundy* lies Northward from the *Lyonnois*, between which and it, are the *Beaujolois*, the chief Town whereof is *Ville Franche*, and the *Maronis*, that takes its name from the Town of *Maron*: the chief Towns of *Burgundy* are *Dijon* the Capital, *Auxhain* an ancient Town, *Chalons* on the *Seine*, *Beaune*, *Semur* and *Langres*, some place *Sens* and *Auxerre* here.

*Champaign* hath *Burgundy* to the South, and *Picardy* to the North; its chief Towns are *Rheims*, *Troyes*, *Chalons* on the *Marne*, *Bar* on the *Seine*, *Bar* on the *Aube*, *Nogent*, *Chaumont* in *Basigny* and *Joinville*. Seeing *Champaign* joins *Picardy*, and that we began the Description of the Circuit of *France* by this, we will end it here, that we may view the middle of the Kingdom, and describe the Provinces that lie there, proceeding from North to South.

*Brie* lies to the West of *Champaign*; its chief Towns are *Meaux*, *Provence*, *Lagny*, *Bricomte-Robert* and *Montereau*.

*France*, properly so called, lies West from *Brie*, and hath *Picardy* to the North; it comprehends the *Prevostie* and *Vicecounty* of *Paris*, the *Isle* of *France*, the *Valois*, the *Heurepois*, and the *Gastinois*: *Paris* is the Metropolis of all this Kingdom, the Residence of the Kings, and one of the fairest Cities in the World. In the *Isle* of *France* is *St. Denis*, the burying place of the French Kings; *Poissy*, *St. Germain*, and *Montmorency* are the other more remarkable Towns thereof. In the *Valois* are *Crespi*, *Senlis*; and *Beauvois*, with the *Beauvois*, is by some also placed there. In the *Heurepois* are *Melun*, *Corbeil*, *Moret*: in the *Gastinois* are *Montargis*, *Nemours*, *Etampes*, *Milly*, *Chastillon* and *Fontainebleau*, where the French King has a stately Houle in a vast Forest.

The *Beauvais* hath for chief Towns, *Orleans*, *Chartres*, *Dreux*, *Châteaudun*, *Vandœuvre*, *Menn*, *Nogent le Roy* and *Elois*.

*Perche* hath for principal Towns, *Nogent Le Retrou*, *Molosse* and *Moragne*.

*Anjou* hath *Angiers*, *Saumur* and *La Fleche*.

*Tourain*

*Tourain* hath *Tours*, which gives it the name, *Amboise*, *Loches*, *Chinon*, where *Rablais* was born, *Loudun* and some others.

*Sologne* hath *Remorantin*, *Gergeau* and *Sully*.

*Berry*, which is almost in the middle of *France*, hath *Bourges* its chief Town, *Sancerre*, *Yssoudun*, *Vierzon*, *Dun Le Roy* and *Selles*.

The *Nivernis* hath *Nevers*.

The *Bourbonnois* hath *Moulins*, *Bourbon L' Ancy*, and *Bourbon L' Archambaud*.

The *Forrest* hath *St. Estienne de Foursin*, *Mont Brisson*, *Fours*, and *Rouenne*.

*Auvergne* is divided into the upper and lower; in this are the Towns of *Clermont*, *Ryons*, *Montferrand*, and the Castle of *Montpensier*: in the upper, *St. Flour* and *Aurillac*.

*Limoisin* hath *Limoges* its Capital Town, *Segur* and *Chalus*, which are in the upper; and *Tulles*, *Uzerche* and *Brive* in the lower, called otherways *La Marche*.

*Quercy* hath for Capital *Cahors*, the other considerable Towns are *Montauban* and *Moissac*.

*Perigord* hath *Perigueux*, *Sarlat*, *Bergerac* and *Miremont*.

*Rouergue* hath *Rhodes*, *Ville Franche*, and *Milland*.

The *Angoumois*, *Angoulême*, *Chateaufort*, *Coignac* and *Jarnac*, where the bloody Battel was fought in time of *Charles* the Ninth, which bears that name. And this is a brief Description of all the Provinces of *France*.

We must now see what Rivers water it. Those that run into the Ocean are the *Garonne*, the *Charente*, the *Loyre*, the *Seine* and the *Somme*. Into the Mediterranean Sea, the *Aude*, the *Erau*, and the *Rhône*.

The *Garonne* hath its source in the Pyrenean Hills, runs through *Guienne*, passes by *Toulouze* and *Bordeaux*, receives into it the *Ariège*, the *Lot*, the *Tarn* and the *Dordogne*, and falls into the Ocean near to *Bordeaux*.

The *Charente* passes by *Angoulême* and *Xaintes*.

The *Loyre* hath its Head in *Languedoc*, among the Mountains of *Vivarez*; from whence it enters into the Forests, and passes by *Rouenne*, where it begins to carry Boats, it runs through the *Bourbonnois*, the *Nivernis*, *Beauvais*, *Tourain* and *Anjou*, passes by *Nevers*, *Orleans*, *Elois*, *Amboise*, *Tours*, *Saumur*, and entering a little into *Bretaign*, and having washed *Nantes*, it discharges it self into the Ocean, carrying with it the *Allier*, the *Clain*, the *Creuse*, the *Cher*, the *Vienne*, the *Mayne*, and many Riviulets.

The *Seine* comes out of *Burgundy*, waters *Champaign*, the *Isle* of *France* and *Normandy*; it passes through *Paris*, and by *Rouen*, and being increased by the *Marne*, the *Yonne*, the *Oise*, and some other Rivers, it is embraced by the Ocean near *Harve* *De-grace*.

The *Somme* springs out of *Picardy*, runs through it, and forsakes not that Province till it lose it self in the Ocean, after it hath washed *Amiens*, *Abbeville*, and several other Towns of that Country, from whence the *Escaut*, or *Scheldt*, springs also.

The *Aude* comes from the Pyrenean Mountains, and runs by *Carcassonne* and *Narbonne*.

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The *Erand* comes from the *Severnes*, and pisseth by *Agde*, the *Orb* by *Beziers*, The *Rhofne* has its source in Mount *St. Gothard* among the *Alpes*, runs through the Lake of *Geneva*, passes by *Lyons*, *Vienne*, *Valence*, under the *Pont St. Esprit*, by *Avignon*, *Beaucaire*, *Arles*, and receives into it the *Saone*, the *Isere*, the *Droume*, the *Durance*, the *Ardecbe*, the *Gardon*; and by its Branches having made an Island which is called *Camargue*, (from *Cajus Marini*, corrupting *Caii Marii Ager*, into *Camargue*,) it falls into the *Mediterranean*.

There are in *France* fifteen Archbishopsricks, and comprehending *Avignon*, sixteen, which are *Rouen*, *Tours*, *Bordeaux*, *Auch*, *Toulouze*, *Narbonne*, *Arles*, *Aix*, *Ambrun*, *Vienne*, *Lyons*, *Sens*, *Rheims*, *Paris*, *Bourges* and *Avignon*, and above an hundred Bishopsricks.

There are ten ancient Parliaments which are established at *Paris*, *Rouen*, *Rennes*, *Bordeaux*, *Pau*, *Toulouze*, *Aix*, *Grenoble*, *Dijon* and *Metz*, and two new ones, the one at *Tonrway* for the *French* Conquests in the *Netberlands*, the other at *Esfancon* for the *Franch Comty*.

Its Isles in the Ocean are *Belle-Isle*, on the Coast of *Bretaign*,; *Noirmousteir* on the Coast of *Poitou*; the Isles of *Re* and *Oleron* on the Coasts of *Annis* and *Xaintonge*: In the *Mediterranean* are the Isles of *Hieres*, of *St. Margaret*, and *St. Honorat* on the Coast of *Provence*.

Its Mountains besides the *Alpes* and *Pyrenees*, are those of *Auvergne* and *Severnes*, which the Ancients called *Montes Cebennae*, the name not much as yet altered.

There are besides, *Mount Jura*, or *St. Claude*, which is towards *Switzerland*, and *Mount Vogese*, or *Faucilles*, towards the Diocess of *Langres*.

The Catholick Religion is the publick established Religion in *France*, yet the Protestant is permitted there: And thus, Reader, you have a short draught of a large and flourishing Kingdom, under the Dominion of a great and powerful Prince.

Before we proceed to *Italy*, we must pass over into *Savoy*, which is inclosed within *France*: This Dutchy belonging to a Prince who carries the Title of it, hath to the North the Lake of *Geneva* and *Switzerland*, to the East *Piemont*, and *Dauphine* to the South and West; the chief Towns of it are *Chambrey* its Capital City, *Montmelian* and *Fonffigny*. The County of *Morienne*, where *St. John* stands, and the *Tarantaise*, where *Monstier* is, which are in the *Alpes*, belong to the Duke of *Savoy*, as well as *Piemont*, and the *Marquisat of Saluces*, of which we shall speak in the Description of *Italy*. *Geneva* lying at the end of a great Lake that carries its name, heretofore belonged to the Duke of *Savoy*, but at present it owns no Superior, and is erected into a Commonwealth.



A Table of the Longitudes and Latitudes of the principal places in the Kingdom of France.

In Picardy.		Bray.		Lat.	Long.
	Lat.	Long.	Ay.	48 3	24 2
Calais.	51 1	23 1		49 0	25 2
Bologne.	50 5	23 1			
Abbeville.	50 1	23 1	St. Malo.	In Bretagne.	
Amiens.	49 5	23 4	Dol.	48 5	18 0
St. Quintin.	50 0	25 1	Remes.	48 4	18 3
Perone.	50 0	24 4	Treguier.	48 0	18 3
Oyle.	49 4	24 3	Morlaix.	48 4	16 4
In Normandy.			St. Pol de Lior.	48 2	16 0
Rouen.	49 3	22 1	Brest.	48 4	15 4
Diepe.	50 0	22 1	Pol David.	48 0	15 2
Havre de Grace.	49 4	21 1	Blauet.	47 4	15 2
Lizieux.	48 5	21 4	Vennes.	47 3	16 4
Caen.	49 2	20 1	Nantes.	47 2	17 1
Isigny.	49 4	19 1	Macbecour.	47 1	18 5
Auranchet.	48 5	19 0	Dieu.	46 5	18 3
Seez.	48 5	20 5	Isle de Normantier.	46 4	18 1
Isle of Jersey.	49 3	18 1	Felle Isle.	47 0	18 0
Isle of Gernsey.	49 4	17 4	Isle de Uissant.	47 0	16 4
In Poitou.				48 1	14 2
Poitiers.	46 4	21 0	Mans.	In Main.	
Vivonne.	46 3	21 0	Suze.	48 0	21 0
Roche.	46 1	19 1		47 5	21 0
Isle of Re.	46 1	18 4			
Amboise.	47 2	22 0	Angers.	In Anjou.	
Gueret.	46 0	23 0	Saumur.	47 3	19 5
In the Isle de France.			Bange.	47 1	20 2
Paris.	48 5	23 3	Craon.	47 4	20 5
Soffens.	49 3	24 3	Tours.	47 5	19 2
Fountainbleau.	48 3	23 3		47 2	21 4
In Champaign.					
Sedan.	49 5	26 1		In Perche.	
Rheims.	49 2	25 2	Nevers.	48 2	21 5
Espernay.	49 0	25 0			
Chalons.	48 4	25 5		In the Orleanois.	
Troyes.	48 2	25 2	Orleans.	47 4	23 9
			Blois.	47 4	23 2
			C 2		In



In Bourgogne.			In Gascogny.		
	Lat.	Long.		Lat.	Long.
Dijon.	47 1	26 2			
Auxerre.	47 2	24 4	Fourdeaux.	44 5	19 2
Autun.	46 4	25 2	Bourg.	45 2	19 4
Chalon.	46 3	26 1	Tour de Cordovan.	45 3	18 5
Verdun.	46 4	26 1	Chusac.	45 2	20 0
Mafcon.	46 0	26 0	Albret.	44 2	20 2
			Aux.	43 4	21 0
In Berry.			Lombes.	43 2	21 2
Bourges.	47 0	23 1	Dax.	44 0	19 2
			Bayonne.	43 4	18 2
In the Bourbonnois.					
Moulins.	46 1	24 2	In Low Navar.		
			Pau.	43 2	19 4
In the Angumois.			Tarbe.	43 1	20 3
Angoulême.	45 5	20 5	St. Bertrant.	42 5	21 1
In Saintonge.			In Languedoc.		
Saintes.	45 5	19 4	Touloufe.	43 3	21 5
BroUAGE.	45 4	19 1	Alby.	43 3	22 3
Île de Oleron.	45 5	18 4	Castres.	43 2	22 5
			Carcaffon.	43 0	22 3
In the Lionnois.			Narbonne.	42 5	23 4
Lyon.	45 4	26 2	Fezieres.	43 0	24 0
Rouanne.	45 5	25 1	Montpellier.	43 1	25 1
			Nismet.	43 2	25 3
In Périgort.			Ufer.	43 3	25 3
Périgoux.	45 2	21 3	Viviers.	44 0	26 0
In Limofin.			In Rouffillon.		
Limoges.	45 4	22 1	Perpignan.	42 1	23 3
In Quercy.			In Province.		
Cabors.	44 2	22 3	Fréuli.	43 0	28 2
			Tbolon.	42 4	27 4
In Auvergne.			Marsaille.	42 5	26 5
St. Flour.	44 4	24 2	Aix.	43 0	26 5
Mercœur.	45 0	24 1	Arles.	43 0	26 0
Usson.	45 1	24 4	Avignon.	43 3	26 1
Clermont.	45 3	24 1	Orange.	43 4	26 1
			Sijfteron.	43 5	27 5
In Rouergue.					
Rodez.	44 1	23 3	In Dauphine.		
Esti.	41 4	23 2	Vienne.	45 1	26 4
Vabres.	43 4	23 5	Grenoble.	44 5	27 2
					St.



	Lat.	Long.		Lat.	Long.
St. Antoine.	44 5	26 4	St. Paul.	44 0	26 2
Valence.	44 3	26 3	Embrun.	44 3	28 1

A Table of the Longitudes and Latitudes of the principal places in the Dukedom of Savoy.

## In Savoy Proper.

	Lat.	Long.		Lat.	Long.
Chambery.	45 1	27 3	Monfiers.	45 1	28 1
Montmelian.	45 0	27 4	St. Jacquesine	45 0 $\frac{1}{2}$	28 2
Benfort.	45 1 $\frac{1}{2}$	28 1	St. Maurice.	45 1	28 3
Aix.	45 2	27 3			
Rumilly.	45 3	27 3			
Conflans.	45 1	28 0			
Milans.	45 1	27 4			
L'Escheller.	45 0	27 2			

## In the Tarantais.

## In the Genevois.

## In Bugcy.

	Lat.	Long.		Lat.	Long.
St. Genis de Hoste.	45 1	27 1	La Bonne Ville.	45 4	27 5
Tonn.	45 2	27 2	Clusé.	45 +	28 1
			Salanche.	45 3	28 2

## In Fanfigny.

## In Mauricuna.

	Lat.	Long.		Lat.	Long.
La Chambre.	44 5	28 0	Thonon.	46 0	28 0 $\frac{1}{2}$
St. Jean de Maurien.	44 4	28 0	Ripaille.	46 0	28 1
Modane.	44 4	28 2	Erism.	46 0	28 2
Lafneburg.	44 5	28 4	St. Jingo.	46 0	28 3
Mount Cenis.	44 4	29 0	Aux.	45 5	28 2

## In Chablais.

## CHAP. VI.

## Italy.

**I**TALY hath on the West the River *Var* and the *Alpes* which divide it from *France*, and the *Mediterranean Sea*; it is divided from *Germany* by the same Mountains on the North. on part of which side also is the Gulf of *Venice*: it hath to the East the *Ionian Sea*, and to the South the Sea of *Tiffany*. This Region resembles the Leg and Thigh of a man, or (if you had rather) a Boot.

The *Apennine Hills* stretch along the whole length of it; and it is divided into several states under the Dominion of divers Princes. The Pope possesses the



the Ecclesiastick State, in which are the Campania of *Rome*, the Patrimony of *St. Peter*, the Dutchies of *Spoleto*, *Urbino* and *Ferrara* the Mark of *Ancona*, *Romania* and the *Boulgnois*: and in the Kingdom of *Naples*, the Dutchy of *Benevento*. The King of *Spain* possesses the Kingdom of *Naples*, the Dutchy of *Milum*, and some places on the side of *Tuscany*, with the Marquisat of *Final*, on the Frontiers of *Genoa*. The Duke of *Florence* is Master of the greatest part of *Tuscany*. The Duke of *Savoy* holds *Piemont*, the Marquisat of *Saluces*, and the County of *Nice*. The Duke of *Parma*, the Dutchies of *Parma* and *Placentia*, and the Dutchy of *Castro*. The Duke of *Mantua*, the Dutchy of *Mantua* and *Monferrat*. The Duke of *Modena*, the Dutchies of *Modena* and *Regio*. The Prince of *Massa* the Principality that gives him the Title. The Prince of *Mirandola*, the Principality of the same name. The Bishop of *Trent* is Prince of his own Bishoprick: it contains four Republicks, two that are great, to wit, of *Venice* and *Genoa*, and two lesser, of *Lucca* and *St. Marin*. The Republick of *Venice* possesses part of *Istria*, (the rest belonging to the House of *Austria*) *Frioli*, the Mark *Trevisane*, *il Dogado*, the *Paduan*, the *Vicentin*, the *Bressian*, and the *Bergamask*. The Republick of *Genoa* possesses that which is called *Riviera di Genoa*; that of *Lucca* but little, and that of *St. Maria* less. We are now to take a view of all these States in order, Coasting along by the Sea which environs that sweet Country, and proceeding from West to East.

Having passed the *Var*, we come into the County of *Nice*, wherein is a City of the same name, and that of *Villa Franca*.

*Monaco* which belongs to its own Prince; the Marquisat of *Final* with a Town of the same name.

The *Riviera de Genoa*, wherein are the Metropolis of *Genoa*, (which is called in *Italian*, *La Superba*, the Stately, and is one of the most beautiful Towns in *Italy*.) *Savona*, *Albenga*, and some others.

*Tuscany* is separated from the *Riviera de Genoa* by *La Msera*; it reaches to the Campania of *Rome* on the East, and has that Sea which carries its name on the South, and the *Apennines* on the North. The Duke of *Florence* who takes the Title of great Duke of *Tuscany*, is Master of the greatest part of it. The chief Towns in his Territories are *Florence*, the Capital City, *Pisa*, *siena*, *Volterra*, *Pistoia*, and *Legora*, a Sea-Port Town. The small State of the Republick of *Lucca*, the Principality of *Massa*, and the *Stato delli Presidi*, in which are the Towns *Orbitello*, *Porto Hercole*, and *Piombino*, that belong to the King of *Spain*, are in *Tuscany*; as also the Dutchy of *Castro*, which belongs to the Duke of *Parma*, having a Town of the same name, and the Patrimony of *St. Peter*, wherein are *Viterbo*, *Montefiascone*, and some others: *Aquaspendente*, *Perugia* near a Lake that bears its name. *Orvieto* and *Civita Vecchia*, a fair Port where the Pope keeps his Gallies, are likewise in *Tuscany*.

The Campania of *Rome*, in ancient times called *Latinum*, hath to the East *La Terra d' Lavoro* of the Kingdom of *Naples*. to the South, the Sea, to the West *Tuscany*, from which it is separated by the *Tibre*, and to the North *Abruzzi*: its Capital City is *Rome*, so famous that none can compare with it: heretofore it gave Laws to the whole World almost, and at present extends

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its power farther than ever, seeing the Popes exercise their Authority in *America*, where the Consuls and Emperors of *Rome* were never known: There are many prints of its ancient Splendor still extant, as the *Pantheon*, which goes by the name of *Santa Maria Rotunda*, the Pillars of *Trajan* and *Antonin*, Amphitheatres, Baths, Aqueducts, and many other stately remains of Antiquity, which by their Ruins publish the *Roman* Magnificence and Grandeur: it stands upon the *Tiber*, at the mouth of which River is the Town of *Osia*. The other Towns of the Campania of *Rome*, are *Tivoli*, formerly *Tybur*, where are excellent Waters, *Avagnia*, *Palatine*, which is the ancient *Prencipe*, *Veletri*, heretofore *Velitrae*, where *Augustus* was born, *Terracine*, and some others.

The Kingdom of *Naples* is bounded on the West, by the State of the Church, and on all other sides by the Sea; to wit, the Sea of *Tuscany* on the South, that of *Ionian* on the East, and the Gulf of *Venice* on the North: it is divided into several Provinces; on the *Tuscan* Sea are, *Terra di Lavoro*, of which *Naples* is the Capital City, that hath a good Port, the others are, *Capoua*, *Puffoli*, *Cajette*, and *Baia* that is ruined: The Principality wherein *Salerno* is; *Calabria* that contains *Cosencia* and *Regio*. The *Basilicate* and Principality of *Tarento*, lie on the *Ionian* Sea; and on the Gulf of *Venice*, the Country of *Otranto*, that has a Town of the same name, and the Land of *Bari*, in which are *Bari* and *Brindisi*; *Apulia*, wherein is *Mandredonia*; *Abruzzi*, whereof the Capital Town is *Aquila*: And in that Province also is the Dutchy of *Benevento* that belongs to the Church.

The Mark of *Ancona* lies likewise on the Gulf of *Venice*, in which is a Town of the same name, and that of our Lady of *Loretto*, that is much frequented upon the account of Devotion.

Next after comes *Romania*; its Capital City is *Ravenna*, and the others are, *Faenza*, *Forli* and *Imola*.

The *Boulgnois* has *Bononia* for its Capital, which is one of the fairest Cities of *Italy*: The Dutchy of *Ferrara* with its Metropolis of the same name is situated on the *Po*.

The Dutchy of *Venice*, wherein is comprehended that delicate City built upon *Piles* in the Sea.

*Frioli*, where are *Udena*, and the Ruins of *Aquileia*.

*Istria*, which belongs partly to the *Venetians*, and partly to the Archdukes of *Austria*, bounds *Italy* on that side; the chief Towns of it are, *Cabod' Istria*, *Tergeste*, *Parentia* and *Pola*.

The Marquis, or Mark *Trevisane*, hath *Treviza*, *Verona* and *Vicensa*.

The Bishoprick of *Trent* stretches along the *Alpes*; and its chief City is famous for the last Council held there: the Bishoprick of *Bilona* is in the same Province also.

The Dutchy of *Milan* hath the *Alpes* on the North, *Piemont* on the West, *Parma* on the South, and the *Venetian* State on the East, *Milan* its Capital, is one of the greatest Towns of *Europe*, and its Castle one of the best Fortresses: in the same Province are also *Pavia*, *Cremona*, *Novarra*, *Lodi*, *Como* and *Vigevano*. The Metropolis of *Piemont*, is *Turin* on the *Po*, a lovely City where



where the Dukes of *Savoy* keep their Court : *Pignerol* a strong place belonging to *France*, is in the same Province. *Carmagnole* is the chief Town of the Marquisat of *Saluces*, as *Casal* is in *Montferrat*.

The Dutchies of *Parma*, *Placentia*, *Modena* and *Regio*, have their Capital Cities of the same name.

The Dutchy of *Mantua* hath likewise a City of the same name, built in the middle of a Lake on the River *Mincæ*.

These Dutchies that we have now named, lie in that part of *Italy* which the *Romans* called *Gallia Cisalpina*, because the *Gauls* were planted there, and that as to them it was on this side of the *Alpes* ; it was afterwards called *Lombardy*, from the *Lombards* that Conquered it, which name it still retains : it is on the South shut up by the *Apennine* Hills, the *Alpes* on the North and West, and by the Gulf of *Venice* and the River *Pisaura*, or *Foglia*, on the East. A great part of the *Venetian* State lies in that Region, as *Crema* a strong Town, *Bergamo* with its Territory, and *Fresse*, or *Brescia*, with its Dependances.

The Dutchy of *Spoleto*, and that of *St. Urbis*, which belongs to the Holy See, have each of them a Capital Town of the same name, and are Situated upon the *Apennine* Mountains in the Center of *Italy*. In the first is the Town of *Affise*, where *St. Francis* was born ; within the second is enclosed the little Republic of *St. Marin*, under the Protection of the Pope.

The chief Rivers of *Italy* that fall into the *Mediterranean*, are the *Var*, which runs through the County of *Nice*, and divides it from *Provence* ; the *Magra*, which divides *Liguria*, called *Riviera di Genova*, from *Tuscany* ; the *Arno*, that passes by *Florence* and *Pisa* ; the *Tiber*, that runs by *Rome*, and is augmented by *Tevereone* and *Cbiara* ; the *Garigliano*, heretofore *Liris*, and the *Vulturno*.

Into the Gulf of *Venice* fall, *Lofanto*, *Pescara*, and *Tronto*, which are in the Kingdom of *Naples* ; the *Foglia*, that is in the Mark of *Ancona*.

*Rubicon*, at present, *Pisanello*, that heretofore divided *Gallia Cisalpina* from the West of *Italy*.

The *Po*, which is the greatest River of *Italy*, and rises in Mount *Viso*, one of the *Alpes* ; it passes by *Turin*, and through the Dutchy of *Milan*, goes into the Lands of *Mantua*, and *Ferrara*, and from thence into the Gulf of *Venice* ; having swallowed up in its passage the *Doria*, the *Tezin*, the *Adi*, the *Oglia*, the *Mince*, the *Tixer*, and several other Rivers.

The *Adige* passes by *Trent* and *Verona*.

The *Brenta* passes by *Padua*.

*Tagliamento* and *Lisussa* with *Friuli* : *Rizano Itria* ; and *Arso* divides it from *Dalmatia*.

There are considerable Lakes in *Italy* : in *Lombardy* is the Lake *Major*, heretofore called *Verbanus*, out of which comes the *Tezin*.

The Lake of *Como*, anciently called *Larius*, out of which comes the *Adi* ; the Lake of *Iseo*, whence comes the *Oglia* ; the Lake of *Lugano*, and another called *de Garda*, which produces the *Mince*.



In *Tuscany* is the Lake *Thrasimene*, at present called the Lake of *Perugia*: the Lake *Vulfin*, now of *Bolsena*, and the Lake of *Braciano*, heretofore *Sabinus*.

In the *Campania* of *Rome*, are the Lake *Fucin*, the Lake *Fundi*, and the Lake *Albanus*, now called *Lago di Castello Gandolfo*.

The chief Islands of this Country, are *Elbe*, *Corfica*, *Sardinia*, *Iscbia*, *Caprea*, *Sicily*, and some others.

The Isle of *Elbe* is near the Shoar of *Tuscany*: it hath a Town called *Cosmopolis*, and a Mountain of Loadstone: it belongs partly to the great Duke of *Tuscany*, and partly to the King of *Spain*.

*Corfica* is over against the *Riviera* of *Genoa*, and belongs to that Republick, its chief Town is *La Bastia*, and best Port that of *St. Bonifacio*.

*Sardinia* is divided from *Corfica* by an Arm of the Sea, it lies to the South of *Corfica*, and belongs to the King of *Spain*: the chief Town of it is *Calari*, and the others are *Oristagna*, *Sassari* and *Algeri*.

Near to *Naples* is the Isle of *Iscbia*, with a Fort of the same name, and *Caprea*, famous for the Residence of *Tiberius*, is likewise near it.

*Sicily* is the greatest Island of the *Mediterranean*, it is separated from *Italy*, (to which it is thought to have been anciently united) by a narrow Branch of the Sea, called the *Fare* of *Messina*; the chief Towns of it are *Palermo*; its Capital, the Residence of the Viceroy, *Messina*, *Trepaco*, *Cigenti*, *Syracusa*, and *Catania*, near to which is the famous Mount *Ætna* that vomiteth out fire, called at present Mount *Gibello*: this Island belongs to the King of *Spain*.

The Isles of *Lipare* are not far from this, some of which cast out Fire.

In the Gulf of *Venice*, and near to Mount *Gargan*, are the Isles of *Diomedes*, at present of *Santa Maria del Trinita*.

The Mountains of *Italy* are the *Alpes* that limit it, and the *Apennine* Hills that run through it. Not far from *Naples* is Mount *Vesuvius*, which hath often cast out Fire, but not at present, it is now called *Monte di Sommo*, and produces excellent Wine. In *Apulia* is Mount *Gargan*, now of *Santo Angelo*.

There is no Religion but the Roman Catholick professed in *Italy*: and the least Towns of it are Bishopricks.

A Table of the Longitudes and Latitudes of the Principal Places in the Territories of *Italy*.

	Lat.	Long.		Lat.	Long.
I. In the Kingdom of <i>Naples</i> .					
<i>Regio</i>	37 5	40 1	<i>Matera</i>	40 4	41 0
<i>Cape Spartivento</i>	37 4	40 4	<i>Taranto</i>	40 3	41 3
<i>St. Severina</i>	39 1	41 1	<i>Orranto</i>	40 1	42 2
<i>Cesusa</i>	39 3	40 3	<i>Irindisi</i>	40 4	42 1
<i>Policastro</i>	40 0	39 2	<i>Fari</i>	41 2	40 4
<i>Salerno</i>	40 4	38 5	<i>Benevent</i>	41 1	38 5
<i>Gallipoli</i>	40 1	42 1	<i>Manfredonia</i>	41 4	39 4
<i>Ciarenza</i>	40 4	40 1	<i>Naples</i>	40 5	38 4
			<i>Aversa</i>	41 0	38 1
			D		
			<i>Capua</i>		



	Lat.	Long.		Lat.	Long.
Capua	41 1	38 2	Verona	45 1	33 1
Gaeta	41 2	37 3	Garda	45 2	32 5
Boiano	41 4	38 2	Brescia	45 1	32 2
Pescara	42 4	38 1	Istria	45 0	32 0
Chieti	42 3	38 1	Bergama	45 2	31 4

## 2. In the Estate of the Church.

Rome	41 4	36 3	Feltre	46 1	34 0
Orta	41 3	36 5	Vicenza	45 4	33 5
Mont Fiascone	42 0	35 4	Trieste	46 0	36 4
Bracciano	41 4	36 0	Citta Nova	45 1	36 3
Civita Vecchia	41 3	35 4	Pola	44 5	37 0
Orvieto	42 1	36 0	Zara	44 3	39 1
Perugia	42 4	35 2	Sebenico	44 3	39 5
Spalatto	42 4	36 1	Spalatto	44 0	40 2
Narni	42 2	36 2	Navenza	44 0	42 0

## The Isles.

Fermo	43 0	37 1	Corfu	38 4	44 4
Ancona	43 3	36 5	Cefalonia	36 5	46 3
Loreto	43 2	37 0	Zante	36 2	46 4
Urbino	43 3	35 3			
Fano	43 4	35 5			
Cagli	43 1	35 5			
Ravenna	44 0	34 5			
Rimini	43 5	35 1			
Ferrara	44 4	33 4			
Bologna	44 0	34 0			

## 3. In the Dukedom of Florence.

Florence	43 0	34 2	Turin	44 2	29 4
Pistoia	43 1	34 0	Susa	44 4	29 0
Scarpeta	43 3	34 2	Asti	44 0	30 2
Lucca	43 0	33 3	Nice	42 5	29 2
Pisa	42 4	33 1	Inurea	44 4	29 5
Leghorn	42 3	33 2	Aosta	45 2	29 1
Siena	42 4	34 3	Monaco	42 5	29 4
Pienza	42 2	35 0	Pignora	44 0	29 1
Piombino Port	41 5	33 4	Chier	44 1	30 0
Orbivello	41 3	35 0	Fossano	43 4	29 5
Port Hercule	41 2	35 0	Oneglia	43 0	30 1
Maffa	42 1	34 1			

## 4. In the Estate of Venice.

Venice	45 2	34 4	Milan	44 5	30 5
Adria	45 0	34 3	Pavia	44 3	31 0
Pudova	45 2	34 1	Como	45 1	31 0
			Novara	44 5	30 3
			Lodi	44 5	31 4
			Bobbio	43 5	31 4
			Tortona		

	Lat.	Long.		Lat.	Long.
Tortona	44 0	31 0	Trapano	36 5	36 0
Ugogna	45 3	30 0	Marsala	36 4	36 0

## 7. In the Estate of Genoa.

Cape de Melli	42 5	30 1	Palermo	37 2	37 0
Final	43 2	30 3	Milazzo	38 0	39 2
Genoa	43 3	31 0			
Lavagne	43 2	31 4			

## Isles of Lipari.

Stramboli	38 4	39 1
Felicur	38 0	37 5
Lipari	38 2	38 5
Volcano	38 1	38 4
Alicur	38 0	37 3
Ustica	38 0	36 4

## 8. In the Dutchy of Modena.

Modena	44 0	33 4
Reggio	44 0	33 0

## 9. In the Dutchy of Mantua.

Mantua	44 5	33 1
Ustiano	44 5	32 3

## In the Island of Sardinia.

Cagliari	37 5	32 2
Sarda	39 2	32 1
Sassari	39 2	31 4
Algeri	39 0	31 4
Oristagni	38 2	31 3
Villa de Iglesia	37 3	31 5

## 10. In the Dutchy of Parma.

Parma	44 0	32 4
Foronovo	43 5	32 3
Placenza	44 1	31 5

## In the Kingdom of Sicily.

Faro	38 0	39 5	Bonifacio	40 0	32 3
Messina	37 5	39 5	Aleria	41 0	32 3
Termini	37 1	37 3	Bastie	41 3	32 2
Catania	37 0	39 2	Cape Corso	41 5	32 2
Augusta	36 4	39 2	Calvi	41 1	32 0
Syracusa	36 2	39 2	Ajazzo	40 3	30 2
Nota	35 5	39 1	Genaroz	41 0	31 4
Cape Passaro	35 4	39 4			
Agrigento or Girgenti	36 1	37 4	Isle of Elba	41 4	33 3
Maxara	36 3	36 2	Isle Gorgona	42 2	32 4

## In the Island of Corsica.



## CHAP. VII.

*The Low-Countries.*

**B**EFORE we pass into *Germany*, we must view the *Low Countries*, because they lie between it and *France*. They have *Germany* to the East and North, the Ocean to the West, and *France* to the South. They are divided into seventeen Provinces, to wit, four Dutchies, seven Counties, five Signiories or Lordships, and the Marquisat of the holy Empire. The Dutchies are *Brabant*, the Capital of which is *Brussels*, the Residence of the Governours of the *Low-Countries* for the King of *Spain*; its other Towns are *Louvain*, *Antwerp*, *Beffledue*, and many others.

The Dutchy of *Limbourg*, which hath a Capital of the same name.

The Dutchy of *Luxembourg* which hath its principal Town of the same name also: its other considerable Towns are *Arton*, *Tbionville*, *Danvilliers* and *Montmedy*.

The Dutchy of *Guelldres* that hath a Town likewise of the same name, and *Nimuegen* a place of importance.

The County of *Flanders* hath *Ghent* for its Capital; the other considerable Towns are *Bruges*, *Ipre*, *Courtray*, and (upon the Sea) *Sluse*, *Newport*, *Ostend*, *Dunkirk* and *Graveline*; which twolast belong to the Crown of *France*.

The County of *Arnois* hath *Arras* for Capital, belonging likewise to *France*, the other Towns are *Beaupreme*, *Bethune*, and *St. Omer*, taken in the late Wars by the *French*.

The County of *Hainault* has *Mons* for Capital, *Valenciennes*, *Fouchain*, *Maricmburg* and *Landreecy*.

The County of *Namur* hath its Capital of the same name, *Bouvines* and *Charlemont*.

The County of *Zutphen* hath its chief Town of the same name also: it is comprehended under the Dutchy of *Guelldres*.

The County of *Holland* hath very fair Cities, as *Amsterdam* its chief, *Harlem*, *Leyden*, *Dort*, *Rotterdam*, and several others. The *Hague* is but a Town, yet there the Assembly of the States, and Court of the Prince of *Orange* are kept.

The County of *Zaaland* is composed of several Isles, made by the branches of the *Esaut*, or *Scheld*; the chief is the Isle of *Walcheren*, in which are the Towns of *Middleburg* and *Flushing*.

The Marquisat of the Holy Empire is no more but the City and Territory of *Antwerp*, comprehended under *Brabant*.

The Signiory or Province of *Salines* contains likewise only the Town of the same name, with its Territory included with *Brabant*.

The Signiory or Province of *Durbu* hath a large and beautiful Town of the same name, and besides *Rhenen*, *Amersfort*, *Udenfort* and *Wijk* at *Duerstede*.

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The Signiory or Province of *Over Iffel* is so called, because in respect of the other Provinces of the *Low-Countries*, it is on the other side of the *Iffel*, which is a branch of the *Rhine*, and is by the Latins called *Transissalana*: its Towns are *Deventer*, *Swoll*, *Campen*, *Steenwick*, *Cowerden*, and *Oldenzeel*.

The Signiory or Province of *West-Friesland* hath these remarkable Towns, *Lewarden*, *Dockum*, *Franeker*, *Staveren*, and *Harlingen*.

The Signiory or Province of *Groningen*, hath the Town which gives it its name, and another small Town called *Dam*.

The *Low-Countries* are watered with pleasant Rivers, which are the *Scheld*, the *Meuse*, and the *Rhine*; the *Scheld* hath its Source in *Fleardy*, passes by *Valenciennes*, *Tournay*, *Ghent* and *Antwerp*; and having embraced the *Isles* of *Zealand*, and received the supplies of the *Lys*, the *Licne*, the *Dender*, the *Rupel*, and some other Rivers, it falls into the Ocean.

The *Meuse* cometh from the Mount of *Vange* in the Diocess of *Langres*, passes by *Charlemont*, *Bouvincs*, *Namur*, *Masstricht*, *Grave*, and joining with the *Wahal*, one of the Branches of the *Rhine*, it receives the *Sambre* and some other Rivers.

We shall speak of the *Rhine* when we treat of *Germany*.

The nineteen Provinces, or *Low-Countries*, falling to the Crown of *Spain* by *Mary*, Heiress of the House of *Burgundy*, some of them Revolted, and erected themselves into a Commonwealth, by the name of the States of the United Provinces, commonly called the States of *Holland*: they are composed of *Holland*, *Zealand*, *Utrecht*, *Over-Iffel*, *West-Friesland*, *Groningen*, *Guedres*, and *Zutphen*. The Assembly of the States General is held at the *Hague*, and since their settlement, the Princes of *Orange* have been the Generals of their Armies. *Calvin's* Reformation is the Religion publicly established; but the *Catholic*, *Lutheran*, *Anabaptist*, *Securian*, and many other Religions are tolerated there.

The *French* in the late Wars Conquered many considerable places of the *Spanish Netherlands*, some of which have been made over to that Crown, by the *Spaniard*, in the last Treaty of Peace concluded at *Nimwegen*; so that the *Spanish* Interest in these Provinces is at present much impaired and weakened.

Before we proceed further, it is to be observed, that the *Cambresis* and Bishoprick of *Liege* are inclosed within the *Low-Countries*.

The *Cambresis* lies between *Artois* and *Hainault*, and hath *Picardy* to the South: the City of *Cambrai* that gives it the name is a spacious and fair Town, belonging now to the *French King*.

The Bishoprick of *Leige* hath to the North and West *Brabant*, *Luxemburg* on the South, and *Limbourg* on the East. The City of *Leige* is very fair and spacious, lying on the *Meuse*; the Bishop of it is Sovereign Prince of all his Diocess, which comprehends the Dutchy of *Bouillon*, the Towns of *Mosyk* and *Tongres*, with the Burrough of *Spa*, famous for its Medicinal Waters.



A Table of the Longitudes and Latitudes of the principal places  
in the Netherlands.In the French Conquests in *Artois*.

	Lat.	Long.		Lat.	Long.
<i>Arras</i>	50 1	23 5	<i>Valenciennes</i>	50 2	24 5
<i>Lens</i>	50 3	24 0	<i>Bouchain</i>	50 1	24 3
<i>Bethune</i>	50 4	23 5	<i>Baruy</i>	50 2	25 1
<i>St. Pol</i>	50 2	23 3	<i>Maubenge</i>	50 2	25 2
<i>Bapaumes</i>	50 1	24 0	<i>Chymay</i>	50 0	25 4
<i>Pas</i>	50 1	23 4	<i>Avsnes</i>	50 1	25 2
<i>Renti</i>	50 4	23 1	<i>Quesnoy</i>	50 2	25 0
<i>Hesdin</i>	50 2	23 1	<i>Landrecy</i>	50 1	25 0
<i>Teroane</i>	50 4	23 2	<i>Philippville</i>	50 2	25 5
<i>Lillers</i>	50 4	23 4	<i>Mariembourg</i>	50 1	25 5
<i>St. Omers</i>	50 5	23 2			
<i>Ayre</i>	50 4	23 4			
<i>St. Venant</i>	50 4	23 5			

## In Flanders.

<i>Graveling</i>	51 1	23 1
<i>Bourbourg</i>	51 0	23 1
<i>Mardyke</i>	51 1	23 2
<i>Dunkirk</i>	51 1	23 3
<i>Winoxberg</i>	51 0	23 3
<i>Mont-Cassel</i>	50 5	23 4
<i>Armentiers</i>	50 4	24 0
<i>Furnes</i>	51 1	23 5
<i>Ipre</i>	51 0	24 1
<i>Poperingen</i>	51 0	23 5
<i>Belle</i>	50 5	24 0
<i>Warneton</i>	50 5	24 1
<i>Conimes</i>	50 5	24 2
<i>Warwick</i>	50 5	24 2
<i>Menin</i>	50 5	24 3
<i>Lille</i>	50 4	24 2
<i>Le Raffee</i>	50 3	24 0
<i>Orchies</i>	50 3	24 3
<i>Tournay</i>	50 4	24 4
<i>Douay</i>	50 2	24 2
<i>St. Amand</i>	50 3	24 4

## In Hannault.

<i>Conde</i>	50 3	25 0
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In the County of *Namur*.

<i>Charlemont</i>	50 1	26 1
<i>Buillon</i>	50 0	26 3
<i>Cambrey</i>	50 1	26 3
<i>Chateau Cambresis</i>	50 0	24 5
<i>Crevecoeur</i>	50 0	24 3

In the Dukedom of *Luxembourg*.

<i>Tbionville</i>	49 3	27 4
<i>Montmedy</i>	49 3	26 5
<i>Marville</i>	49 3	27 0

## In the Spanish Flanders.

<i>Newport</i>	51 2	24 0
<i>Dixmude</i>	51 1	24 0
<i>Ostend</i>	51 2	24 1
<i>Bruges</i>	51 2	24 2
<i>Courtray</i>	50 5	24 3
<i>Gant</i>	51 1	25 0
<i>Damm</i>	51 2	24 2
<i>Blankenburg</i>	51 3	24 2
<i>Dendermond</i>	51 1	25 3
<i>Rupelmond</i>	51 2	25 3
<i>Alst</i>	51 0	25 3
<i>Oudenard</i>	51 0	25 0

## In Brabant.

<i>Brussels</i>	50 5	25 4
<i>Vilvorden</i>	51 0	25 5
<i>Malines, or Mechlin</i>	51 1	25 5

Antwerp

	Lat.	Long.		Lat.	Long.
<i>Antwerp</i>	51 2	25 4	<i>Tongres</i>	50 5	26 5
<i>Lovain</i>	51 0	26 0	<i>Vifcit</i>	50 5	27 1
<i>Nivelle</i>	50 4	25 4	<i>Hasselt</i>	51 0	26 4
<i>Gembours</i>	50 4	26 0	<i>Mafzyck</i>	51 1	27 1
<i>Judoign</i>	50 4	26 2			
<i>Tillemont</i>	50 5	26 2			
<i>Lewe</i>	51 0	26 3			
<i>Deift</i>	51 1	26 2			
<i>Arscott</i>	51 1	26 1			
<i>Herentals</i>	51 2	26 2			
<i>Lire</i>	51 2	26 0			

## In the Estates of the United Provinces in Flanders.

<i>Cadfant</i>	51 3	24 4
<i>Hulste</i>	51 2	25 2
<i>Sas de Gant</i>	51 2	25 0
<i>Lillo</i>	51 3	25 3
<i>Sluce</i>	51 2	24 4

## In Hannault.

<i>Hall</i>	50 5	25 4
<i>Engbien</i>	50 5	25 2
<i>Brain le Comte</i>	50 4	25 3
<i>Mons</i>	50 3	25 2
<i>St. Guislain</i>	50 3	25 1
<i>Bincb</i>	50 3	25 3
<i>Atb</i>	50 5	25 1
<i>Ligue</i>	50 4	25 0

## In Brabant.

<i>Bergen op Zoom</i>	51 3	25 3
<i>Breda</i>	51 4	26 0
<i>Bois le duc</i>	51 4	26 3
<i>Kavelstein</i>	51 5	26 5
<i>Grave</i>	51 5	27 0

## In Zealand.

<i>Middlebourg</i>	51 3½	24 5
<i>Flussing</i>	51 3	24 5
<i>Helvees sluce</i>	51 5	25 2
<i>Brewers haven</i>	51 4	25 0
<i>Brille</i>	52 0	25 1
<i>Tolcn</i>	51 4	25 2
<i>Somerdiike</i>	51 5	25 2
<i>Goree</i>	51 5	25 1

## In Namour.

<i>Namour</i>	50 3	26 2
<i>Bovines</i>	50 2	26 1
<i>Charleroy</i>	50 3	25 5

## In the Dutchy of Limburg.

<i>Limburg</i>	50 4	27 3
<i>Mastricht</i>	51 0	27 1

## In the Dutchy of Luxembourg.

<i>Luxembourg</i>	49 4	27 4
<i>Arlon</i>	49 5	27 2
<i>Newchâtel</i>	49 5	26 5
<i>Marche</i>	50 2	26 5
<i>La Roche</i>	50 2	27 1
<i>Baytoygne</i>	50 0	27 2

## In the Country of Leige.

<i>Leige</i>	50 4	27 0
<i>Huy</i>	50 4	26 4
<i>Binant</i>	50 2	26 2
<i>St. Hubers</i>	50 1	26 5
<i>St. Truyen</i>	50 5	26 3

## In the Earldom of Holland.

<i>Amsterdam</i>	52 3	26 0
<i>Harlem</i>	52 3	25 4
<i>Leyden</i>	52 1	25 4
<i>Hague</i>	52 1	25 2
<i>Delft</i>	52 0½	25 2
<i>Rotterdam</i>	52 0	25 4
<i>Dort</i>	51 5	25 5
<i>Gouda</i>	52 1	25 5
<i>Gorcum</i>	51 5	26 1
<i>Housden</i>	51 5	26 2
<i>Gertrudenburg</i>	51 4	26 0
<i>Mnyden</i>	52 2	26 1
<i>Narden</i>	52 2	26 3

In



## In North Holland.

	Lat.	Long.	Oldenzeel	Lat.	Long.
<i>Alkmaar</i>	52 5	25 5	<i>Steenwick</i>	52 3	28 2
<i>Modenblik</i>	52 5	26 2	<i>Meppel</i>	53 0	27 2
<i>Enkhsfen</i>	52 5	26 3		52 5	27 3
<i>Horn</i>	52 5	26 1			
<i>Edam</i>	52 4	26 1			
<i>Monikdam</i>	52 3½	26 1			

## In the Dutchy of Gueldres.

	Lat.	Long.	<i>Harderwick</i>	Lat.	Long.
<i>Leuwarden</i>	53 2	27 0	<i>Hatten</i>	52 3	26 5
<i>Dockum</i>	53 3	27 1	<i>Arnhem</i>	52 4	27 1
<i>Staveren</i>	53 1	26 4	<i>Secukonse</i>	52 0½	27 0
<i>Hurlingen</i>	53 2	26 4	<i>Bommel</i>	51 5½	27 2
<i>Franker</i>	53 2	26 5	<i>Tiel</i>	51 5	26 3
<i>Bolswart</i>	53 1½	26 5	<i>Nimeguen</i>	51 5½	26 4
			<i>Grave</i>	52 0	27 0
			<i>Gueldres</i>	51 5	27 0
			<i>Vento</i>	51 3	27 4
			<i>Genep</i>	51 2	27 3
				51 5	27 1

## In the Lordship of Croningen.

	Lat.	Long.		Lat.	Long.
<i>Groningen</i>	53 2	27 5			
<i>Damm</i>	53 3	28 0			
<i>Delfzeil</i>	53 3	28 1			

## In the Lordship of Utrecht.

	Lat.	Long.		Lat.	Long.
<i>Utrecht</i>	52 1	26 2			
<i>Amerfort</i>	52 2	26 4			

## In the Province of Over-Iffel.

	Lat.	Long.		Lat.	Long.
<i>Deventer</i>	52 3	27 3			
<i>Zowll</i>	52 4½	27 2			
<i>Camper</i>	52 4	27 1			
<i>Overdeu</i>	53 0	28 0			

## The Islands adjoyning.

	Lat.	Long.
<i>The Texel</i>	53 1½	26 0
<i>The Vlie</i>	53 3	26 1
<i>Schelling</i>	53 3½	26 3
<i>Ameland</i>	53 4	27 0

## CHAP. VIII.

## Germany.

Germany has on the East side *Prussia*, *Poland*, and *Hungary*; the *Baltick* Sea, *Denmark*, and Ocean on the North; on the West the *Low-Countries* and *France*, and the *Alps*, which divide it from *Italy*, on the South. On the *Baltick* Sea are *Pomerania*, whereof *Stetin* is the Capital City, and *Gripshuld* and *Colberg* two others: The Dutchy of *Mechlbouurg*, whereof the chief City is *Smerna*.



Upon the Ocean are the Dutchy of *Holface* or *Holstein*, in which are *Ham-bourg* and *Lubeck*.

The County of *Emden*, called otherways *East-Frisland*, to distinguish it from that whereof we spoke in the *Low-Countries*; its chief Town carries also the name of *Emden*: it has likewise another Town called *Aurich*.

Along the *Rhine* upwards lies *Wetphalia*, whereof the most remarkable Towns are, *Munster*, *Paderborae*, *Saxt*, *Erern*, *Oldembourg* the Capital of a County of the same name.

The Diocesses of *Cologne*, *Mayence*, and *Treves*, with their Metropolitan Cities of the same name; the *Palatinate* of the *Rhine*, whereof *Heidelberg* is the Capital City; the Dutchy of *Baden*; the Diocesses of *Worms* and *Spire*. High and Low *Alsace*; *Strasbourg* is the chief City of this, and *Frisac* and *Fribourg* are the chief Towns of the other, which is one of the last Conquests of *France*.

At the head of the *Rhine*, and in the *Alps*, are the *Swisses*, divided into thirteen Cantons, *Zurich*, *Berne*, *Lucerne*, *Basle*, *Schaffhausen*, *Fribourg*, *Zug*, *Glarin*, *Switz*, *Appenzel*, *Solcurre*, *Underwald* and *Uri*, this last both no Towns, but *Athor* is its chief Burrough: all the other Cantons have their names from their Capital Cities, and from that of *Switz* the people are called *Switzers*, and the Country *Switzerland*.

The Country of *Valais* lies along the *Rhone*, and its chief City is *Syon*, the Bishop whereof is a Temporal Lord.

The *Grisons* are united with the *Swisses*, and *Caire* is their Capital City: Along the *Danube* are *Suabia*, which comprehends the Dutchy of *Witttemberg*, the chief Towns whereof are *Tubinge* and *Stutgard*: in *Suabia*, properly so called, are *Ambourg*, *Ulme* and *Nordlingen*.

The Dutchy of *Bavaria*, whereof the Capital is *Munich*; the other Cities are *Saltsbourg*, *Ratisbonne* and *Ingolstat*: and in the *Palatinat* of *Bavaria*, *Amberg* its Capital, and *Nuremberg*, an Imperial City.

The Arch-Dutchy of *Austria* is to the East of *Bavaria*; its Metropolis is *Vienna*, the usual Residence of the Emperor. The County of *Tirol* is to the South of *Bavaria*, it hath a City of the same name, but *Innsbruck* is the Capital thereof.

*Stiria* hath *Gratz*; *Carinthia* hath *St. Veit* and *Villach*; and *Carniola*, *Laubach* for its Capital: these Provinces, as well as the County of *Tirol*, belong to the Arch-Dukes of *Austria*, and lie Southward of that Arch-Dutchy.

Then going from South to North, beyond *Austria*, lie *Moravia*, with *Ol-mutz* its Capital City.

*Silesia*, that hath *Brasslavia*, commonly called *Breslau*, for its Metropolis.

The Marquisat of *Brandenbourg*, divided into two Marches, the ancient, in which is *Brandenbourg*, and the new, wherein is *Francfort* upon the *Oder*, which are their Capitals; but the Residence of their Prince is commonly at *Berlin*.

*Saxony* is in the heart of *Germany*, divided into the Upper, where is *Wittemberg*, and the Lower, wherein is *Hall*.



The Dutchies of *Brunswick* and *Lunenbourg*, are comprehended in the lower *Saxony*, with the Cities of the same name.

The Marquisat of *Misnia*, wherein *Dresden* and *Leipsick* are; and the County of *Mansfeld*, with its Capital of the same name, are in lower *Saxony* also.

*Turinge*, a Landgraviat, hath for Capital *Erfurt*, which is the greatest City in *Germany*, and another Town called *Jena*.

The Landgraviat of *Hesse*, hath *Cassel* and *Marpurg*.

The Dutchy of *Franconia* hath for Metropolis *Wirtzburg*; its other chief Towns are *Bamberg*, and *Frankfort* on the *Main*, where the Emperor is chosen.

The Kingdom of *Bohemia* is almost in the middle of *Germany*, and its Capital City is *Prague*.

The chief Rivers of *Germany* are the *Rhine*, the *Emis*, the *Wiser*, and the *Elbe*, which discharge themselves in the Ocean; the *Oder* in the *Baltick*, and the *Danube* in the *Euxine Seas*.

The *Rhine* cometh from the *Alpes*, and hath its Source in the Mount Saint *Gotard*, from whence the *Rheine* and *Tessin* spring also; it runs through *Switzerland* and the Lake of *Constance*, passeth by *Schaffhausen* and *Raste*, continues its course through *Alsace*, by *Brissac*, *Strasbourg*, *Spire* and *Wormes*: through the palatinate, by *Mayence* and *Cologne*; and having sent out several Branches, and received the *Moselle* that passeth by *Treves*, the *Necker*, that passeth by *Heidelberg*, and the *Main* that joins it at *Mayence*: one of its Branches called the *Mahal* mingling with the *Meuse*, at length in *Holland* it loseth it self in the Sea.

The *Emis* runs through *Frisland*, and passeth by the Town of *Emden*: the *Weser* watereth *Westphalia*, and passeth near to *Breme*.

The *Elbe* hath its Fountains in *Bohemia*, and runs through both *Saxony* and the Dutchy of *Holstein*, and having washed *Hamburg*, and received the *Allda* that runs by *Prague*; the *Sal*, the *Spree*, and some other Rivers, it talleth into the Ocean.

The *Oder* passeth by *Frankfort* and *Stetin*, and empties it self into the *Baltick* Sea.

The *Danube* riseth in the Dutchy of *Witenberg*, passeth through *Saxia*, *Bavaria*, *Austria*, *Hungary*, *Serbia*, *Bulgaria*, and by several mouths it discharges it self into the *Black Sea*; after that it hath watered *Ulme*, *Ratisbonne*, *Vienna*, and received in a great many other Rivers, the chief whereof are the *Fun*, the *Drave*, the *Sava* and the *Tibisque*.

There are but six Archbishops in *Germany*, to wit, the three Electors of *Mayence*, *Cologne* and *Treves*; the Archbishops of *Magdebourg*, *Breme* and *Saltzbourg*; there are in *Germany*, free and Imperial Cities, and the *Hanz* Towns for Commerce: the States of the Empire, which are called Diets, meet usually at *Ratisbonne*. The Emperor is head of the Empire, he is choat at *Frankfort*, and has his usual Residence at *Vienna*: he is Catholic, but several Princes of the Empire are Calvinists, and others Lutherans.

There

There were in former times but seven Electors, three Ecclesiastick, who are the Archbishops of *Mayence*, *Cologne*, and *Treves*; the Duke of *Saxony*, the Marquess of *Brandebourg*, the Count Palatine, and the King of *Bohemia*: but the Juncture of times hath occasioned the addition of an eighth, who is the Duke of *Bavaria*.

A Table of the Longitudes and Latitudes of the principal Cities and Towns of *Germany*.

	Lat.	Long.		Lat.	Long.
			<i>Namslaw</i>	51 0	40 2
			<i>Glogaw</i>	51 4	38 2
In <i>Austria</i> .					
<i>Vienna</i>	48 2	39 2			
<i>Lintz</i>	48 2	36 3	In <i>Brandenbourg</i> .		
<i>Ens</i>	48 1	36 4	<i>Frankfort a. Oder</i>	52 2	37 0
<i>Loosenstein</i>	48 0	37 1	<i>Landenberg</i>	52 5	38 3
			<i>Kustrin</i>	52 3	37 3
In <i>Tyrol</i> .			<i>Berlin</i>	52 4	36 0
<i>Innsbruck</i>	47 0	33 4	<i>Stendel</i>	52 5	34 1
<i>Landeck</i>	46 3	32 4	<i>Havelburg</i>	52 5	34 4
In <i>Carinthia</i> .			In <i>Mecklenburg</i> .		
<i>St. Veis</i>	47 0	37 0	<i>Lubeck</i>	54 1	32 3
			<i>Wismar</i>	54 1	33 5
In <i>Styria</i> .			<i>Rostock</i>	54 1	34 5
<i>Gratz</i>	47 1	39 0	<i>Gustrow</i>	54 0	34 5
<i>Pettau</i>	46 4	59 2			
<i>Sekow</i>	47 3	37 5			
			In <i>Pomerania</i> .		
In <i>Carniola</i> .			<i>Bergen in J. Rugen</i>	54 2	36 3
<i>Laxbach</i>	46 2	37 2	<i>Stralsund</i>	54 1	36 0
			<i>Stetin</i>	53 2	37 2
In <i>Bohemia</i> .			<i>Dam</i>	53 3	37 2
<i>Prague</i>	50 0	36 4	<i>Stargard</i>	53 1	38 0
<i>Konigin-gratz</i>	50 0	38 1	<i>Colberg</i>	53 5	38 5
<i>Rlataw</i>	49 3	36 0			
<i>Satz</i>	50 1	35 3	In <i>Bavaria</i> .		
			<i>Munick</i>	48 0	33 4
In <i>Moravia</i> .			<i>Saltzbourg</i>	47 5	35 2
<i>Olmütz</i>	49 4	39 2	<i>Passaw</i>	48 3	35 5
<i>Brinn</i>	49 1	38 5	<i>Ratisbon</i>	48 5	34 2
			<i>Landshutt</i>	48 2	34 2
In <i>Silesia</i> .			<i>Ingolstat</i>	48 4	33 2
<i>Teschén</i>	49 4	41 0	<i>Amberg</i>	49 2	34 1
<i>Oppelen</i>	50 2	40 3	<i>Ulm</i>	48 3	32 1
<i>Brieglaw</i>	51 0	39 2	<i>Norlingen</i>	48 5	32 3
			E 2		In



	Lat.	Long.		Lat.	Long.
<i>In Suabia.</i>					
Ausburg	48 1	32 4	Paderborn	51 4	30 3
Eßlingen	48 3	30 5	Osnaburg	52 2	29 4
Friburg	47 5	29 2	Embsen	53 2	28 4
Brifac	48 0	29 1	Norden	53 4	28 3
Hall	49 1	31 4	<i>In Bremen.</i>		
Hailbrun	49 0	31 0	Breme	53 2	30 2
<i>In Alfatia.</i>					
Hagenaw	48 4	29 2	Ferden	53 1	31 2
Strasbourg	48 3	29 1	Hamburg	53 4	31 4
<i>In the Palatinate.</i>					
Heydelburg	49 2	30 3	Stade	54 0	31 0
Wormes	49 3	30 2	<i>In Lunenburg.</i>		
Spire	49 0	29 5	Lunenburg	53 2	32 2
Phillipsburg	49 5	30 0	<i>In Brunfwick.</i>		
Treves	49 4	28 0	Brunfwick	52 4	32 4
Mayence	49 4	30 2	Goffar	51 5	32 3
<i>In Franoonia.</i>					
Frankfort	49 5	31 0	Hildifheim	52 1	31 5
Henneburg	50 3	32 0	Nyenburg	52 4	31 0
Scharinfort	50 0	32 0	<i>In Turingia.</i>		
Bamburg	49 5	33 0	Erfort	50 5	33 2
Nurenburg	49 3	33 2	<i>In Saxony.</i>		
Callimbach	50 0	33 5	Dresden	51 0	35 5
<i>In Haffia.</i>					
Murpur	50 4	30 2	Leipfick	51 1	34 4
Fridburg	50 1	30 5	Wittenburg	51 5	35 2
Caffel	51 1	31 1	Minden	51 1	33 4
<i>In Cologn.</i>					
Cologn.	50 4	28 2	Bretten	51 3	35 3
Bonne	50 3	28 4	<i>In Lufatia.</i>		
<i>In Cleves.</i>					
Cleves	51 3	27 2	Bantzen	51 1	36 4
Juliers	50 4	27 5	Colbatz	51 4	36 2
Duffeldorf	51 0	28 1	Brybitz	51 3	37 5
<i>In Weftphalia.</i>					
Munfter	52 0	29 1	<i>In the Cantons of Swifferland.</i>		
<i>I. In the Canton of Zurich.</i>					
			Zurick	47 1	30 2
			Koburg	47 1	30 4
			Endelfingen	47 2	30 3
			2. In		

2. In the Canton of Bern.			8. Canton of Glaris.		
			Lat.	Long.	
Bern	46 5	29 0		46 4	30 5
Thun	46 3	29 2	9. Canton of Bafle.		
Aarburg	46 5	28 5	Bafle	47 3	29 2
3. Canton of Lucern.			10. Canton of Friburg.		
Lucern	46 4	30 0	Friburg	46 3	28 4
4. Canton of Uri.			Montenach	46 3	28 3
Altorf.	46 3	30 3	Gruieres	46 2	28 4
5. Canton of Schwitz.			11. Canton of Soleurre.		
Schwitz	46 4	30 2	Solcurre	47 1	29 0
6. Canton of Underwald.			12. Canton of Schaffbufen.		
Stantz	46 3	31 0	Schaffbufen	47 3	30 3
7. Canton of Zug.			Stein	47 3	30 4
Zug.	46 5	30 1	13. Canton of Appenzel.		
			Appenzel	46 4	31 2

## CHAP. IX.

## The Dutchie of Cleves, Juliers, Lorrain, and the County of Burgundy.

THE Dutchie of *Cleves* and *Juliers* are Situated between the *Rhine* and the *Muse*, and might be reckoned amongst the Provinces of *Germany*; that of *Cleves* has a Metropolis of the same name, and other considerable places, as *Santen*, *Calcar*, *Grefbusen* on this side the *Rhine*, and *Duisbourg* and *Embruch* on the other side.

The Dutchy of *Juliers* has its name from the chief City thereof; it hath also *Perge* and *Duerp*. *Aix la Chapelle* is in this Dutchy, and there *Charlemain* kept his usual Residence; it was the feat of his Empire, and the place of his Burial: He Beautified it with many stately Buildings, with a Church Dedicated to the Holy Virgin, that still remains, and a Palace, which in the time of *Charles* the Bald, in the Year eight hundred and eighty one, was by the Fury of the *Normans* reduced to Ashes. It hath Mineral Waters about it, proper for the Cure of several Maladies, from whence it took its Latin name, *Aquisgranum*, the *Germans* call it *Acken*, and a third of it belongs to the Duke of *Juliers*.

The



The Dutchy of *Lorrain* may be reckoned among the Provinces of *France*, being now in the possession of that King; its Capital City is *Nancy*, the other Towns thereof are *Marsal*, *Saint Nicholas*, *Pont a Mousson* and some others: *Metz*, *Toul* and *Verdun* are likewise in *Lorrain*, and belong to the *French* King.

The County of *Burgundy*, called the *Franche-County*, lies to the East of a Dutchy of the same name belonging to *France*; but the County belonged formerly to the King of *Spain*, though lately Conquered by *France*: The chief Towns of it are *Dole*, the Capital, *Bezançon*, an Imperial City, *Vesoul*, *Grez*, *Cromay*, *Salins*, *Arbois*, *Poligny*, *Nozeret* and others. The *Doux* a sweet River, waters that Country, and passes by *Dole*: it afterwards loses it self in the *Saone*, which divides the Dutchy of *Burgundy* from the County.

A Table of the Longitudes and Latitudes of the principal places in the *Franche Comty* and *Lorrain*.

In the <i>Franche County.</i>			Lat.	Long.	
	Lat.	Long.	<i>Rosiers or Salines</i>	48 4	28 2
			<i>Blamont</i>	48 4½	29 0
<i>Bezançon</i>	47 1	27 2	<i>Remerimont</i>	48 1	28 4
<i>Dole</i>	47 0	26 4	<i>Toul</i>	48 4	27 4
<i>Salins</i>	46 5	27 2	<i>Vaudemont</i>	48 3	27 5
<i>St. Claud</i>	46 1	27 3	<i>Pont a Mousson</i>	49 0	27 5
<i>Grey</i>	47 1½	26 4	<i>Metz</i>	49 2	28 0
<i>Vesoul</i>	47 4	27 3	<i>Vaudrevange</i>	49 4	28 4
<i>Mont Belliard</i>	47 4	28 2	<i>Sarbruck</i>	49 3	29 0
<i>Lure</i>	47 4	27 5	<i>Nomeny</i>	49 0	27 4
<i>Poligny</i>	46 4	27 0	<i>Phalsbourg</i>	48 5	29 2
<i>Bleterans</i>	46 2½	26 4	<i>St. Dieu</i>	48 3	29 0
<i>Granville</i>	47 2	27 1	<i>La Mothe</i>	48 1½	27 3
			<i>Newchâtel</i>	48 2	27 3
			<i>Verdun</i>	49 2	27 1
In <i>Lorrain.</i>			<i>St. Michael</i>	49 0	27 2
<i>Nancy</i>	48 5	28 0	<i>Conflans</i>	49 2	27 4
<i>St. Nicholas</i>	48 4½	28 1	<i>Barleduc</i>	48 5	26 5
<i>Chaligny</i>	48 4	27 5	<i>Espinal</i>	48 2	28 3
<i>Moyen</i>	48 3	28 3	<i>Sarbourg.</i>	48 5	29 0
<i>Marsal</i>	49 0	28 4			



## CHAP. X.

*Hungary.*

THE Kingdom of *Hungary* hath *Transylvania* on the East, *Poland* on the North, on the West *Moravia*, *Austria*, and *Stiria*, Provinces of *Germany*, and *Bosnia* and *Servia* on the South: the best part of it is under the Dominion of the *Turk*, the rest belongs to the Emperor, who is called King thereof; its chief Cities are *Euda* the Capital, which the *Germans* call *Offen*, *Strigonia*, which they call *Gran*, *Alba Regal*, five Churches, *Canise*, *Javarin* or *Rab*, *Gomorre*, *Presbourg*, and some others. This lovely Country hath been the Theatre of much Christian and Turkish blood, which hath dyed the Rivers of *Marish* and *Rab*, that falls into the *Danube*, which runs through the middle of this Kingdom.

A Table of the Longitudes and Latitudes of the principal places in *Hungary*.

*Hungares, Christian and Turkish.**Esclavonia.*

	Lat.	Long.		Lat.	Long.
<i>Presburg</i>	48 2	40 1	<i>Warisdin</i>	46 3	39 3
<i>Zerdabell</i>	48 0	40 3	<i>Zaarab</i>	46 0	40 0
<i>Raab</i>	47 5	41 0	<i>Novigrad</i>	46 1	39 2
<i>Lynback</i>	47 0	39 3	<i>Fort de Strin</i>	46 3	40 0
<i>Thara</i>	47 0	41 1			
<i>Eckeneck</i>	47 3	41 1	<i>Croatia.</i>		
<i>Wienbrun</i>	47 1	40 4	<i>Carlsbad</i>	45 5	38 5
<i>Carporazack</i>	46 5	40 0	<i>Serin</i>	45 4	39 3
<i>Sarnar</i>	47 3	40 1	<i>Kerstin</i>	45 3	39 1
<i>Tyrna</i>	48 5	40 3			
<i>Nensol</i>	48 3	42 0	<i>Morloguis.</i>		
<i>Fillek</i>	48 0	42 3	<i>Zegna</i>	45 1	38 4
<i>Porn</i>	48 3	43 1	<i>Modrustii</i>	45 2	38 5
<i>Cassia</i>	48 4	43 4	<i>Ouglin</i>	45 2	38 5
<i>Tokry</i>	48 0	43 4	<i>Terjack</i>	45 3	37 5
<i>Zarnar</i>	47 4	45 2			
<i>Zygetb</i>	48 2	45 4	<i>Hungaria Turkish.</i>		
<i>Ungivar</i>	44 4	48 3			
<i>Periga</i>	48 2	45 5	<i>Betwixt Danube and Drem.</i>		
<i>Eperies</i>	49 0	43 4	<i>Canisa</i>	46 4	40 0
<i>Musa</i>	48 4	42 4	<i>Alba Reg. or Stullwef</i>	47 0	41 1
<i>Leutch</i>	49 0	43 0	<i>Stinking.</i>		

*Petche*



	Lat.	Long.	Betwixt Marish and Danub.		Lat.	Long.
Petcbe or 5 Ecclesia	46 1	42 1				
Muhacz	46 1	43 0	Chonad		46 2	44 1
Buda, Offen, Pest	47 1	42 2	Temeswar		45 5	44 4
Gran. Strigon	47 4	41 4	Sippa		46 1	45 1
			Beckskerke		45 3	44 0
			Trena		45 4	46 2
Betwixt Danub and Tibish						
Zeged	46 3	44 0				
Zolnock	47 1	43 5	Esclavonia Turkish.			
Hat an	47 2	42 4	Potega		45 4	41 1
Agria	48 0	43 0	Zakocz		46 0	40 3
Frista	47 3	42 0	Passaw		46 0	40 2
Newbafel	48 1	41 0	Arky		45 2	41 4
Betwixt Tibish and Marish.						
Waradin	47 0	45 0	Croatia.			
Eckyn	46 5	44 0	Wibitz		45 1	39 5
Solmos	45 2	46 2	Siffeg		45 5	39 4
Gyula	46 4	44 4	Dubitz		45 4	40 3
			Velay		45 1	39 3

## CHAP. XI.

*Transylvania, Moldavia, Walachia and Bessarabia.*

THESE four Provinces which are under the Power of the Turk lye on the North side of the Danube.

*Transylvania* hath to the East *Moldavia* and *Walachia*, to the South and West *Hungary* and *Walachia*, and to the North the Territories of *Poland*; its chief Cities are *Hermenstadt*, *Cronstadt*, *Clausembourg*, and *Wasterhely*: its Rivers are *Marish*, *Aluta*, and the *Tibisque*.

*Moldavia* hath to the East *Bessarabia* and *Bulgaria*, to the South *Walachia*, to the West *Transylvania* and *Walachia*, and to the North *Podolia* and *Volinia*; its Capital City is *Jasi*: the *Pruth* watereth it, and the *Danube* divides it from *Bulgaria*.

*Walachia* hath to the East and North *Moldavia*, to the West *Transylvania*, and to the South *Bulgaria*, from which it is divided by the *Danube*: its Capital City is *Tergouisk*.

*Bessarabia* hath to the East the *Black Sea*, *Podolia* to the North, to the West *Moldavia*, and *Bulgaria* and the Mouths of the *Danube* to the South: *Filligree* at the Mouth of the *Neister* is one of its chief Towns.



A Table of the Longitudes and Latitudes of the principal places in *Transilvania*, *Moldavia*, *Walachia*, *Bessarabia*, and *Petit-Tartaria*.

<i>Transilvania.</i>		<i>Lat.</i>	<i>Long.</i>	<i>Burlach</i>	<i>Lat.</i>	<i>Long.</i>
		46 2	46 4		46 2	51 4
<i>Brensford</i>		46 2	46 4			
<i>Wessenburg, or Alba</i>	}	46 5	47 0	<i>Orano</i>	<i>Walachia.</i>	
<i>Julia</i>		46 5	46 0	<i>Zelama</i>	45 0	47 0
<i>Kerezbantia</i>		46 5	46 0	<i>Tarvis</i>	45 3	47 5
<i>Clausenburg, or Colas-</i>	}	47 1	45 3	<i>Ermistut</i>	45 5	49 4
<i>war</i>		47 1	45 3	<i>Braislun</i>	45 0	50 1
<i>Zygeth</i>		41 5	46 2		46 3	49 3
<i>Medwisch</i>		47 2	47 4			
<i>Stephanople</i>		47 1	49 1	<i>Tekyn</i>	<i>Bessarabia.</i>	
<i>Vasarl el</i>		47 3	49 2	<i>Bicelegrod</i>	47 4	54 1
<i>Czyck</i>		47 4	48 4	<i>Kilia Nova</i>	47 3	56 3
<i>Kisly</i>		47 3	48 0	<i>Kiliaftry</i>	46 0	55 2
<i>Newmark</i>		47 3	47 2		46 4	55 4
<i>Torda</i>		47 2	46 5	<i>Tartars upon the mouth of the Nieper.</i>		
<i>Dees</i>		43 3	46 2	<i>Gracom</i>		
<i>Chiche</i>		47 4	46 1	<i>Kudack</i>		
<i>Zaimurbanis</i>		48 0	46 0	<i>Stirlnicza</i>		
<i>Rodna</i>		48 0	46 2			
<i>Tikendorph</i>		47 4	46 5	<i>Crim Tartars near the Lake Maotis, or</i>		
<i>Rothmburn</i>		46 4	48 2	<i>Petit Tartary.</i>		
<i>Moldavia.</i>				<i>Tartaria Precop.</i>		
<i>Soczowa</i>		47 3	50 3	<i>Capba Turk</i>	47 1	54 4
<i>Targored</i>		46 5	50 3	<i>Basiesara</i>	47 5	63 5
<i>Jassy</i>		47 3	51 5	<i>Strayt or Precop</i>	49 0	63 3
<i>Sereb</i>		46 5	50 0	<i>Kerci</i>	47 5	66 5
<i>Pudna</i>		45 3	51 1	<i>Azow or Asack Turkish</i>	51 2	73 0



## CHAP. XII.

*Sclavonia, Bosnia, Servia, Bulgaria and Romania.*

*L*iburnia and *Dalmatia* are but a part of that which was anciently called *Illyrium*, and since *Sclavonia*, from the *Sclavonians* that seated themselves there: it comprehended besides, *Croatia*, *Stiria*, *Carinthia*, *Carniola*, and many other Provinces bordering on the *Danube* and *Adriatick* Sea.

*Dalmatia* hath to the West *Itria*, to the North *Croatia*, to the East *Albania*, and to the South the Gulf of *Venice*: the most remarkable Towns of it are *Zara*, *Sebenico*, *Spalatro*, which belong to the *Venetians*, and *Ragusa* which is taken for the ancient *Epidaurus*, and is a small Republick, Tributary to the Turk.

The Capital City of *Croatia* is *Gradisebia*: of *Bosnia*, *Belgrade*.

*Servia* hath *Semandria*, and *Bulgaria*, *Sophia*: for its Capital these two Provinces are the ancient *Mafia*.

*Romania*, heretofore called *Thrace*, hath *Constantinople* for its Metropolis: it was anciently called *Bizantium*, and was the Seat of the *Grecian* Emperors, as it is at present of the *Ottoman*: it is Situated on the *Bosphorus* of *Thrace*, called now the Channel of the *Black* Sea, and is one of the fairest and largest Cities in the World. The stately remains of the Church of *St. Sophia*, built by *Justinian*, and now converted into a Mosque, are to be seen there, with the *Seraglio*, which is the Palace of the Grand Seignior, and one of the fairest in the World. The other Cities of that Country are *Adrianople*, *Philippoli*, *Philippi*, *Trajanopoli*, *Gallipoli*, and *Sector* on the *Hellepont*, opposite to *Abidos* in *Asia*, where are two Castles called the *Dardanelli*, which defend the passage to the Sea of *Marmora* and *Constantinople*.



## CHAP. XIII.

## Greece.

UNDER the name of Greece were anciently comprehended, *Macedonia*, *Epirus*, *Thessaly*, *Phocia*, *Boeotia*, *Achaia*, *Peloponnesus*, and some other Provinces which have now lost both names and their limits: they are environed by the *Egean* Sea or *Archipelago* on the East, by the *Cretan* or Sea of *Candy* on the South, by the *Ionian* and *Adriatick* Seas on the West, and *Mesia* on the North.

The chief Towns of *Macedonia*, are *Salonichi*, heretofore *Thessalonica*, *Pella* famous for the birth of *Alexander*, and *Stagira* for that of *Aristotle*. Mount *Athos*, now called *Monte-Santo*, and the River *Strimon* are in this Province.

*Croia* is the Capital of *Albania*, heretofore called *Epirus*; its other Towns are *Durazzo*, *La Valona* and *Scutari*.

The Cities of *Thessaly* are *Larissa* and *Pharsalia*, whose Fields were dyed with the *Roman* blood in that famous Battel wherein *Cæsar* overcame *Pompey*; there is the River *Peneus*, and the Valley of *Tempe*. the Mounts *Olympus*, *Ossa* and *Pelion*, so Celebrated in the Writings of the ancient Poets.

*Phocia* had in ancient times the City of *Delphos*, with the Temple of *Apolla*, renowned for its Oracle all the World over; there you may see the Mount *Parnassus*, heretofore Sacred to the Muses, and so Celebrated by the Poets, now inhabited by nothing but ignorance and Barbarism.

*Thebes* was the Capital of *Boeotia*, where *Bacchus*, *Hercules* and *Pindar* were born.

*Attica* was the chief Province of *Achaia*, and in it was *Athens*, the Nursery of many great Men; it was the Residence of the Learned and the Heroes: there remain in it now but some pitiful ruinous places, which are called *Sestines*, *Megara*, *Eleusis*, and some others.

*Peloponnesus*, called at present *Morea*, is almost an Island joyned to *Achaia* by a Neck of Land, which was called the *Isthmus* of *Corinth*, from the adjoining City of that name: the other Towns were *Mycene*, *Argos*, *Sycione*, *Pisa*, (where the *Olympick* Games were Celebrated, and where that famous Statue of *Jupiter Olympus* stood, which was reckoned one of the seven wonders of the World,) *Sparta* or *Lacedæmon*, all Famous and Learned Cities, but now buried under their own Ruins and Barbarity, as all Greece is, which though heretofore the School of the Liberal Arts and Sciences, is now plunged into an abyss of ignorance, and groans under the Tyranny of the Turks. These follow the Religion of their Prophet *Mahomet*, and the Native *Greeks* that of the *Greek* Church.



A Table of the Longitudes and Latitudes of the principal places of *Turky* in *Europe*.

In <i>Bosnia</i> .		<i>Aspects</i>	<i>Lat.</i>	<i>Long.</i>
			41 4	50 2
<i>Sarajevo</i>	44 4		42 4	
<i>Faticza</i>	44 4		41 4	
<i>Bagivalac</i>	44 0		42 2	
<i>Turnovazza</i>	44 2		43 2	
In <i>Serbia</i> .				
<i>Pristina</i>	43 2		44 1	
<i>Novibazar</i>	43 2		46 5	
<i>Drin</i>	43 3		45 0	
<i>Semandrie</i>	44 2		47 4	
In <i>Bulgaria</i> .				
<i>Nizza</i>	43 4		47 3	
<i>Gustadile</i>	44 0		48 2	
<i>Viddin</i>	44 5		47 4	
<i>Nigeboli</i>	44 0		51 3	
<i>Uzekub</i>	43 0		48 0	
<i>Sofie</i>	43 0		50 3	
<i>Harefgrad</i>	44 0		50 2	
<i>Axiopoli</i>	45 0		51 2	
<i>Siliftra</i>	43 3		50 3	
In <i>Romania</i> .				
<i>Constantinople</i>	or 43 0		56 2	
<i>Stamboli</i>	5			
<i>Chiorick</i>	43 0		55 0	
<i>Gallipoli</i>	41 4		55 4	
<i>Adrianople</i>	43 1		53 0	
<i>Ejchibaba</i>	44 1		53 2	
<i>Trajanople</i>	42 3		53 2	
<i>Nicopoli</i>	42 2		51 2	
<i>Kirkli</i>	43 3		50 4	
<i>Caridia</i>	41 3		55 0	
<i>Meimbria</i>	44 4		54 4	
<i>Sof</i>	41 1		55 2	
<i>Varna</i>	45 0		54 4	
<i>Tomi</i>	45 4		55 0	
<i>Siliftria</i>	45 2		52 3	
<i>Zelmi</i>	44 4		52 2	
In <i>Macedonia</i> .				
<i>Philippi</i>			41 4	51 5
<i>Cavula</i>			41 5	50 4
<i>Strimon</i>			42 2	50 2
<i>Heracilia</i>			42 2	40 2
<i>Middle of Mont Sa-</i>			41 0	52 0
<i>bo, or Mont Athos</i>				
<i>Cassandria</i>			50 4	50 1
<i>Salonicchi</i>			41 2	49 0
<i>Peria</i>			41 0	48 0
<i>Contessa</i>			41 3	51 2
<i>Acomania</i>			40 4	50 1
In <i>Thessaly</i> .				
<i>Larissa</i>			39 3	48 4
<i>Amiro</i>			38 5	49 2
<i>Tricca</i>			39 1	47 5
In <i>Asia</i> .				
<i>I. Negropont</i>			38 1	51 0
<i>Corone</i>			38 0	50 0
<i>Stives, or old Thebes</i>			38 0	50 0
<i>Marathon</i>			37 4	50 5
<i>Stines, or Athens</i>			37 1	50 4
<i>Megara</i>			37 2	49 3
<i>Solona, or Delph</i>			37 5	48 2
<i>Lepanto</i>			37 3	47 5
In <i>Morea, or Peloponnesus</i> .				
<i>Patras</i>			37 0	47 4
<i>Corania</i>				
<i>Pylor</i>			36 3	47 0
<i>Sangenico</i>			36 1	47 4
<i>Areadia</i>			35 2	47 3
<i>Coron</i>			35 0	49 1
<i>Modon</i>			34 5	48 2
In <i>Lacedaemon</i> .				
<i>Argor, or Missira</i>			33 4	49 4
<i>Corinto</i>				



	Lat.	Long.		Lat.	Long.
Coriute	36 5	49 3	Risin	42 1	44 2
Napoli	36 2	50 2	Caterra	41 1	44 4
Arges	36 2	49 4			
Islands near Greece.					
In Epyre.			Isl. Stalimen	41 0	52 2
Perga	38 5	45 4	Isl. Tasse	41 4	52 0
Buirinto	38 5	45 1	Isl. Metelene	49 5	55 2
Chimera	39 2	44 1	Isl. Scio	38 5	54 3
Larta	38 3	47 2	Isl. Sciro	38 5	51 3
Bastie	38 4	45 4	Isl. Andro	38 0	51 1
Cunina	40 1	44 2	Isl. Morgo	36 3	51 0
Valdelorsa	40 1	44 0	Isl. Nilo	35 4	52 0
Preneza	38 2	46 4	Isl. Stampalia	35 4	55 1
Albania.			Isl. Cerigo	35 1	50 2
Valona	40 0	44 5	Isl. Zante	36 3	45 2
Elbuscan	41 0	45 4	Isl. Cepolania	37 1	46 1
Pirgo	41 0	44 3	Isl. St. Maura	37 4	46 1
Durazzo	41 0	45 0	Isl. Cosfu	38 5	44 5
Croia	41 1	45 2	Crim Tartars near the Lake Meotis.		
Scutari, or Iscodar	41 5	45 2	Tartaria Perceop.		
In Dalmatia.			Copha	47 1	64 4
Ragusa	42 4	43 3	Basse Sara	47 5	63 5
Dulcingo	42 0	44 0	Strayt and Perceop	49 0	63 3
Budoa	42 1	43 1	Kerci	47 5	66 5
Castel Nova	42 4	43 3	Azow, or Asuck Tur-	51 2	73 0
Narenza	43 2	43 1	kith		

## CHAP. XIV.

*The States of Denmark and Sweden.*

WE must now visit the North, and take a view of those Countries which lye under Frozen Climates.

The King of Denmark possesses there the Cymbrian *Chersonesus*, now called *Jutland*; Norway, and several Islands in the *Baltick* Sea, whereof the chief are *Frunzen* and *Zealand*.

South *Jutland* comprehends the Dutchies of *Sleswick*, with its City of the same name, and *Holsace* or *Holstein*, wherein are *Segeberg*, *Hambourg*, and *Lubick* an Imperial Town, and the *Dithmarse*, in which is *Meldorp*.

North *Jutland* has the Towns of *Seagen* and *Ripen*.

Nor-







	Lat.	Long.		Lat.	Long.
Helmsburg	56 4	34 5	Elebrug.	56 3	36 1
Landferoon	56 3	35 0	Christianstad	56 2	36 1
Lunden	56 2	35 3	A Hays	56 3	37 0
Mulmnyten	56 1	35 1	Elleholm	56 4	38 2
Udstad	55 5	35 5	Christianople		

A Table of the Longitudes and Latitudes of the principal places in *Scandinavia, Norway and Suedeland.*

Government of *Aggerbus.*

	Lat.	Long.		Lat.	Long.
Fredericstet	59 3	32 3	Soderkoping	58 4	38 3
Berga	60 2	32 3	Inf. Oeland.	57 0	39 0
Obsta	60 3	31 0	Borchholme		
Lindfues	59 0	27 3	Inf. Gotthland.		

Government of *Babus.*

Fabis	58 1	34 0	Wuby	57 4	41 3
Dalburs	58 4	34 0	Westermaine, Soudermain, and Firme-Land.		

Government of *Bergenbus.*

Eye	59 0	26 3	Nikoping	58 4	39 4
Stravanger	59 5	26 2	Koping	59 4	39 0
Bergen	61 0	26 4	Philliptad	59 5	36 2
			Carolstadt	59 3	35 4
			Kolen	60 2	34 0

Government of *Dronthenbus.*

Boe	64 0	28 0	Upland.	59 2	40 4
Dronthen	65 3	32 3	Upsal	60 0	40 2
Machstroom	68 3	32 3	Enkoping.	59 4	40 0

Government of *Wardbus.*

North Cape	71 2	48 1	Geftricie.	61 0	40 0
Wardbus	70 5	54 2	Gevalia		

*Suedeland.*

Dilsbo	62 0	39 1
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*West Gotthland.*

Gotteburg	57 3	33 3	Tana	62 0	38 0
Lidkoping	58 3	35 1	Trop	62 1	39 0
Scofde	58 3	35 4			

*East Gotthland.*

Linkoping	58 3	38 3	Bore	63 0	40 0
Norkoping	58 3	38 4	Nord Mating	63 0	42 0
			Lapland		

*Lapland, or West Bothnia.*

	Lat.	Long.	Indisalmi
Uma Lapmark	63 3	42 0	Niflot
Pitha Lapmark	65 3	43 5	Careba
Lula Lapmark	65 3	44 2	Vakclax
Torne Lapmark	65 4	46 0	Wiburg

*Savolax.*

Lat.	Long.
63 3	50 2
51 4	53 3
60 4	51 2
60 3	53 2

*East Bothnia.*

	Lat.	Long.	Kidilia
Vlaburgb	65 3	47 0	Kexholm
Cajanteburg	65 1	51 4	
Salo	64 4	47 0	
Carleby	64 0	45 3	Noneburgb
Kyro	63 3	45 0	Jamagored

*Kexholm.*

61 3	56 0
61 3	55 0

*Ingria.*

59 5	55 4
59 0	52 3

*Finland.*

	Lat.	Long.	Narus
Abo	60 4	45 4	Revel
Bierneburg	62 0	45 0	Pernaw
Gronenburgh	61 3	48 3	Doep
			Riga
Rafeburg	61 1	47 0	Kockenhaus
			Dunenburgh

*Livonia.*

59 0	52 3
59 3	48 3
58 5	47 3
58 3	51 0
57 1	47 4
57 0	49 2
56 4	50 2

## CHAP. XV.

*Great Russia, or Moscovy.*

THAT Prince whom we call the Great Duke of *Moscovy*, is by his Subjects called *Czar*, which is as much as to say, Emperor; and he may very well take that lofty Title, seeing his State is one of the greatest in *Europe*, and reaches even to *Asia*, and he is so absolute a master of the Lives and Fortunes of his people, and his Empire *Dspotick*; on the East it is bordered by *Tartary* the Great, on the South by the *Laffer*, on the West by the States of *Poland* and *Suedland*, and by the Ocean on the North: it comprehends *Great Russia*, which is divided into many Provinces.

*Mosco* is the Capital City of the State, and gives its name to the whole Empire, which it receives from a River that washes it; it is built of Wood, and contains above forty thousand Houses: The other remarkable Cities are *Sandomiry*, *Molodimer*, *Novogord*, and many more. Upon the White Sea, which is a Bay or Gulf of the Northern Ocean, are *St. Michael* Arch-Angel, and *St. Nicholas* at the mouth of the *Divina*, which is one of the greatest Rivers



versin *Russia*: the other Rivers are the *Boristhenes*, at present the *Nieper*, that falls into the *Black Sea*, the *Tanis*, now called *Don*, which discharges it self into the *Palus Maotis*, or *Delle-Zabache*. The *Volga*, heretofore *Rba*, which having its spring head in that Country, after a long Course, carries its Streams into the *Caspian Sea*.

The *Moscovites* follow the Religion of the *Greek Church*.

A Table of the Longitudes and Latitudes of the principal places in *Russia*, or *Moscovia*.

Lapland Moscovites.		Lat.	Long.
		<i>Astracan R.</i>	46 2 87 3
		<i>D. Wclodinie</i>	55 4 70 2
<i>Kielit</i>	68 3 58 0	<i>D. Susdale</i>	56 0 65 3
<i>Jorkena</i>	68 1 66 1	<i>D. Rostow</i>	57 2 65 1
<i>Cape Cadenus</i>	68 0 72 0	<i>D. Moskow</i>	55 4 64 4
<i>Kenio</i>	65 0 55 5	<i>D. Refan</i>	55 0 69 0
		<i>D. Worotin</i>	54 2 63 1
		<i>D. Smolensky</i>	54 3 57 2
		<i>D. Reukhow</i>	56 0 61 2
<i>Karagopol</i>	62 0 67 0	<i>D. Tiver</i>	56 4 62 0
<i>Dwina</i>		<i>D. Novograd Wiliiki</i>	58 0 57 1
<i>St. Michael Arch-Angel</i>	64 5 67 1	<i>Kielit</i>	66 3 57 0
<i>St. Nicholas</i>	65 0 66 3	<i>Kaudalax</i>	68 0 59 0
<i>Lampat</i>	66 0 71 0	<i>Kola</i>	70 0 57 0
<i>Inborn</i>	68 2 73 4	<i>Cape Cadenus</i>	69 2 70 0
<i>Condinsky</i>		<i>Kargapol</i>	62 1 66 0
<i>Koma</i>	62 3 77 2	<i>St. Michael Arch-Angel</i>	64 4 67 0
<i>Petgora</i>	68 2 87 1	<i>St. Nicolas</i>	64 4 66 0
		<i>Inbera</i>	68 0 76 0
		<i>Streight of Waigates</i>	71 0 85 0
		<i>Tobolska</i>	65 $\frac{1}{2}$ 95 0
		<i>Perma</i>	63 2 83 0
		<i>Oustiong</i>	61 0 72 0
		<i>Wologda</i>	59 3 67 0
		<i>Bialaozero</i>	59 0 62 0
		<i>Jeroslan</i>	57 3 65 0
		<i>Lesser Novograd</i>	59 0 71 3
		<i>Vasili gorod</i>	59 0 73 0
		<i>Cazan</i>	58 2 84 0
		<i>Fulgar</i>	56 3 36 0
		<i>Astracan</i>	49 2 83 3
		<i>Wlodimer</i>	58 0 69 0
		<i>Susdal</i>	57 1 63 0
		<i>Rostow</i>	56 4 64 0
		<i>Moskow</i>	55 0 64 3
		<i>Rezan</i>	
Upon Volga R.			
<i>Gero</i>	57 3 66 1		
<i>Nisi Novogord</i>	56 0 75 0		
<i>Vasili gorod</i>	55 3 77 1		
<i>Cazan K.</i>	55 3 84 4		
<i>Bolgar</i>	54 2 84 5		



	Lat.	Long.		Lat.	Long.
Rezan	54 4	67 0	Rzowa	56 0	59 0
Worotin	53 2	64 0	Twer	55 4	62 0
Smolensko	54 0	57 0	Greater Novogrod	58 3	57 0

## CHAP. XVI.

*The Lesser Tartary.*

THE States of the Prince of *Przecop*, or of the lesser *Tartars*, lie betwixt the mouths of the *Boristhenes* and *Tanais*; and in that Peninsula which the Ancients called the *Taurick Chersonesus*, bounded on the East by the *Palus Meotis*, and on the South and West by the *Black Seas*; on the Isthmus thereof stands the City of *Przecop*, which hath given the name of *Przecopites* to that People, and the City of *Cassa* is its Capital: the Streight that joyns the *Palus Meotis* to the *Euxin Sea*, was heretofore called the *Cimmerian Bosphorus*, and is now termed the Streight of *Cassa* or *Vospero*, and St. *Johns* Mouth.

The *Tartars* *Przecopites* are by Religion Mahometans.

## CHAP. XVII.

*The States of the King of Poland.*

THESE States have the Territories of *Moscovy* on the East, on the North those of *Sueden* and the *Baltick Sea*, on the West *Germany*, and on the South the *Carpathian Mountain* which divides them from *Hungary* and *Transylvania*: they comprehend *Poland*, *Prussia*, *Lithuania*, part of *Livonia*, *Masovia*, *Podlaffia*, *Podolia*, *Volbinia* and *Russia-Nigra*.

The Capital City of *Poland* is *Cracovia*, which is the Metropolis of the State; the others are *Guesu* an Archbishoprick, *Sandomeria*, and many more less considerable.

*Prussia Regalis* belongs to the King of *Poland*, and its chief Towns are *Moriembourg* and *Dantzick*, which has a famous Port on the *Baltick* at the Mouth of the *Weisel* or *Vistula*.

*Prussia the Ducall* belongs to the Marquess of *Brandebourg*, who does homage for it to the King of *Poland*: its Capital City is *Koningsberg*, or *Regiomontum*.



The Capital of *Lithuania* is *Vilna*.

In *Livonia*, or *Liefland*, are the Towns of *Riga*, *Reuel* and *Torpach*; it belongs almost wholly to the *Suede*, being yielded to that Crown by the Treaty of *Oliva* in the Year 1660.

The Capital of *Masovia* is *Warsaw*, of *Podlaffia*, *Bijelsko*: *Caminick* and *Bar* are in *Podolia*, and *Ulodimer* in *Volhinia*.

*Leopolis* an Archbithoprick is the Metropolis of *Russia-Nigra*.

*Samogitia* is also a Province of that State, but hath neither Town nor Castle.

The Rivers of that Country are the *Vistula* or *Wicifil*, that passes by *Cracovia*, *Sandomeria* and *Dantzick*.

The *D'una* passing by *Riga* into *Lithuania*.

The *Foristhenes* or *Nieper* bounds these States on the East, having its mouth in the *Ukraine*, the Country of the *Cossagues*, who are under the Dominion of the King of *Poland*, but none of the best Subjects.

The *Catholic* Religion is the strongest in these States, but the *Calvinist* and *Lutheran* are professed there also.

A Table of the Longitudes and Latitudes of the principal places in *Poland* and *Lytania*.

Prussia Royal to Poland.		Lat.	Long.
<i>Dantzick</i>	54 2	41 5	
<i>Elbing</i>	54 1	42 4	
<i>Marienburg</i>	53 5	42 1	
<i>Neuenburg</i>	53 3	41 5	
<i>Culm</i>	53 1	41 4	
<i>Tborn</i>	53 0	41 4	

Prussia Ducal to Brandenburg.		Lat.	Long.
<i>Brandenburg</i>	54 3	43 4	
<i>Kenningsburg</i>	54 3	44 0	
<i>Altburg</i>	54 2	44 4	
<i>Tilse</i>	54 5	45 4	
<i>Memmel</i>	55 4	45 0	

Samogitia in North Russia.		Lat.	Long.
<i>Midnick ab Nomie</i>	55 3	46 1	
<i>Rosienne</i>	55 2	46 5	
<i>Heligaw</i>	56 0	44 4	
<i>Birce</i>	56 0	48 5	
<i>Tauragen</i>	55 1	46 1	

Curland in North Russia.		Lat.	Long.
<i>Mitaw</i>	56 3	47 3	

Palatinate de Poloczck.		Lat.	Long.
<i>Poloczck</i>	55 2	53 3	
<i>Rosian</i>	55 0	55 2	
<i>Drissa</i>	55 5	52 1	

Pal. de Wittepsk.		Lat.	Long.
<i>Scasniestere</i>	55 0	54 2	
<i>Witepsk</i>	55 2	55 4	
<i>Witliff</i>	55 4	57 0	
<i>Uls</i>	55 0	54 3	
<i>Horodeck</i>	55 4	55 3	

Pal. of Vilna.		Lat.	Long.
<i>Breslaw</i>	55 4	50 4	
<i>Vilna</i>	54 3	29 1	
<i>Froki</i>	54 3	48 4	
<i>Milkeimir</i>	55 0	48 4	

*Opixy*

Lat.		Long.		Poland.	
<i>Opixy</i>	55 1	49 0			
Pal. of Troki.		Lat.		Pal. of Plotsko.	
<i>Troki</i>	54 3	48 4		<i>Plotsko</i>	52 3 42 4
<i>Pubink</i>	54 5	49 2		<i>Plousko</i>	52 5 43 0
<i>Kowne</i>	54 4	47 4		<i>Doberin</i>	52 3 42 2
<i>Grodne</i>	53 4	47 3		<i>Reppina</i>	52 5 42 3
<i>Lida</i>	53 5	49 0			
<i>Wilkeuisk</i>	53 1	48 3		Pal. of Inowloecz.	
<i>Bielicz</i>	53 4	49 1		<i>Inowloecz</i>	52 5 41 2
<i>Asuriana</i>	54 2	49 4		<i>Wladislaw</i>	52 4 40 4
				<i>Fredrelant</i>	53 2 40 4
Pal. d' Minsk.		Lat.		Pal. of Pofua.	
<i>Minsk</i>	53 5	51 4		<i>Pofua</i>	52 2 40 3
<i>Berislaw</i>	54 0	53 2		<i>Rogofua</i>	52 4 39 5
Pal. of Novigrodeck.		Lat.		<i>Welin</i>	52 5 38 5
<i>Novigrodeck</i>	53 3	49 3		<i>Krzemin</i>	52 0 40 3
<i>Skenim</i>	53 0	49 0		<i>Miedzerfec</i>	52 2 38 2
<i>Hark</i>	53 0	51 4			
<i>Mir</i>	53 2	50 2		Pal. of Kchish.	
Pal. de Mefillaw.		Lat.		<i>Ghesna</i>	52 3 40 5
<i>Mefillaw</i>	54 0	58 0		<i>Kelish</i>	51 5 40 5
<i>Orffa</i>	54 2	56 0		<i>Navle</i>	52 5 40 2
<i>Mobilow</i>	53 4	56 0		<i>Lawdic</i>	52 1 41 1
	54 3	47 3		<i>Colo</i>	52 1 41 3
<i>Robakzo</i>	52 5	55 0		Pal. of Brest.	
<i>Rzeczyea</i>	52 0	56 0		<i>Brestie</i>	52 3 42 0
				<i>Krafwick</i>	52 4 41 1
Pal. of Bressici.		Lat.		Pal. of Rava.	
<i>Bressici</i>				<i>Rava</i>	51 5 42 3
<i>Pinek</i>				<i>Gabni</i>	52 2 52 3
<i>Horodeck</i>				<i>Gytmie</i>	52 2 52 4
<i>Kolne</i>				Pal. of Seradia.	
Nassovia.		Lat.		<i>Serad</i>	51 3 41 0
<i>Warsaw</i>	52 1	44 1		<i>Telun</i>	51 1 40 5
<i>Pultansk</i>	52 4	44 3		<i>Krzepick</i>	51 0 41 0
<i>Czerika</i>	51 5	44 3		Pal. of Lencici.	
<i>Wiskow</i>	52 2	44 2			
<i>Nar</i>	52 3	46 1		<i>Lencici</i>	52 1 41 4
<i>Wifegred</i>	52 3	43 0		<i>Bresini</i>	52 3 42 5

Pal.



Pal. of Sandomira.			Pal. de Lemberg Ter.			Lat.	Long.
	Lat.	Long.	palde, or Low				
Laniewieſt	51 3	45 0	Halicz	49 4	46 5		
Sandomire	50 3	44 4	Premisław	48 5	47 5		
Wieliczka	50 1	43 3	Sanock	49 3	45 3		
Malogocz	50 4	42 5	Sniatin	49 1	45		
Zarnaw	51 1	42 5		48 3	48 4		
Radom	51 1	44 0	Pal. of Luſſuck, or Viſhinna.				
			Modzimeers	50 4	47 4		
			Conſtantino	51 1	49 5		
Cracow.	50 0	42 3	Horockle	50 5	52 5		
Zacoe	49 5	42 0	Luſſuck	50 4	49 0		
Nowopol	50 5	41 5	Pal. of Kamienieck	49 5	48 4		
Sandecz	49 4	43 1	Barr	49 1	51 2		
Preecz.	49 4	43 4	Bourack	49 0	48 3		
			Pal. de Brackław	52 4	48 5		
			Minicz	49 2	52 2		
Pal. of Lublin.			Ukraine, or Coſſack's Country.				
Lublin	51 0	45 1	Baſe Podolia.				
Czetiche	51 3	44 4	Bialeerkew	50 0	54 4		
Kazimeeres	51 0	44 4	Grudeck	50 0	53 2		
Lukow	51 4	45 4	Kiovia	50 4	55 2		
			Czyckoffſia	49 3	56 3		
			Kudack	48 5	59 3		
			Krilow	49 2	47 3		
			Hiles of y Tar-Treaſure	48 0	58 1		
Pal. of Bielsk.			Dutche de Czernihow.				
Bielsk	52 4	47 1	Moryn	51 2	56 4		
Grudeck	62 1	56 2	Kozel	50 2	57 4		
Agutſon	53 4	46 4	Czernihow	51 5	57		
Gomintz	53 2	46 1					
Drogierin	52 1	46 2					
Pal. de Cbelia	51 0	46 3					
Dubur	50 5	77 1					
Kraſnow	50 5	46 0					
Pal. of Belcz	50 1	47 4					
Krilow	50 3	17 2					

## CHAP. XVIII.

*The Isles of Europe.*

THE Isles in the Ocean which belong to *Europe*, are in the first place those that are called *British Isles*: under which name are comprehended the Island of *Great Britain*, *Ireland*, the *Orcades*, *Hebrides*, *Anglesey*, *Man*, and Isle of *Wight*; and on the West of *Normandy* are those of *Guernsey* and *Jersey*,  
all



all which are under the Dominion of the King of *Great Britain*, and compose one of the greatest States in *Europe*.

The Island of *Great Britain*, which comprehends the Kingdoms of *England* and *Scotland*, is one of the biggest Islands in the Ocean.

The Kingdom of *England* is divided from *Scotland* that lies to the North, by the River of *Tweed*, and *Cheviot Hills*, and from *France* by a narrow Sea called the Channel; the chief Cities thereof are *London* on the *Thames* the Metropolis, *York* and *Canterbury* its two Archbishopsricks: *Oxford* and *Cambridge* two famous Universities, and several other great and populous Cities. The chief Rivers of *England* are the *Thames*, the *Humber*, and the *Severne*.

This Kingdom is divided into fifty two Counties or Shires, reckoning the Dominion of *Wales* which lies to the West thereof, from which the eldest Sons of the Kings of *England* have their Titles of Princes of *Wales*.

*Scotland* a Kingdom to the North of *England* hath *Edinburgh* for its Metropolis, *St. Andrews* and *Glasgow* two Archbishopsricks and Universities, and *Aberdeen* another University, with many other Towns of less note: the Rivers of *Scotland* are not very considerable except for Fishing.

The *Orkades* to the Northward of *Scotland*, are many in number, but only thirteen of them are inhabited, and yet more Northerly are the Isles of *Shetland*, belonging likewise to *Scotland*.

The *Hebrides*, or *Hebudes*, are to the West of *Scotland*, and are above three hundred in number, the greatest of which are *Arran*, *Skie* and *Mule*.

The Isles of *Anglesey* and *Man* are to the West of *England*, and the Isle of *Wight* to the South.

*Ireland*, heretofore *Hibernia*, lies to the West of *England*: it is a great Island, and hath many good Towns, *Dublin* is its Metropolis, and its University, *Armagh*, an Archbishopsrick, *Cork*, *Limerick* and *Waterford*: its greatest River is *Shannon*.

*Island* lies under the Polar Circle, which cuts it through the middle, so that part of it lies on the *Frigid Zone*; there is a Mountain here that cast formerly out flames of fire, though at present it ceases, called *Aecla*: they have some, though but few, places of Habitation, the chief of which is *Skalhott*.

The Western Islands called the *Azores* or *Tercera's*, are betwixt *America* and *Europe*, but nearer *Europe*, and therefore they ought to be ranked among the European Islands: there are nine of them, *Tercera*, *St. Michael*, *St. Mary*, *St. George*, *Gratijsa*, *Pico*, *Fayal*, *Corvo* and *Flores*.

*Tercera* that gives the name to all the rest is the greatest, and has a Town called *Angra*; they belong to the King of *Portugal*, and produce plenty of Cedar.

We have spoken of those that are on the Coast of *France*, when we gave the Description of that Country.

There are many Isles in the *Mediterranean Sea*; and we have taken notice already of those that are on the Coasts of *Spain*, *Italy* and *France*: We must now speak of *Candia*, and of the Isles upon the Coasts of *Greece*.

*Caudy*, heretofore named *Creet*, which contained a hundred Towns, has not at present above four or five which deserve that name; *Candia* is the Capital,



tal, and hath given that name to the Island, the others are *Canea*, *Retimo* and *Siria* : it belonged to the *Venicians*, but after above twenty years War, and that famous Siege of *Candia*, it is at last fallen into the hands of the Turk : it was once the Kingdom of *Minos*, and the Labyrinth that *Dedalus* made was here, and several other things which have been the Theams to the ancient Poets.

*Corfu*, *Zant*, and *Cephalonia*, are in the *Ionick* Sea under the Dominion of the *Venicians*, as also *Cerigo*, heretofore *Cythera*, which is to the South of *Peloponessus* or *Morea*.

*Nigropent*, heretofore *Eubæa*, is upon the Coast of *Achaia* ; and on the Coast of *Romania* is *Samandracbi*, which was called *Samothracia*, and to the South of this *Isalimene*, anciently *Límnos*, where they dig *Terra Lemnia*, or *Sigillata*.

In fine, the *Egean* Sea, called the *Archipelago*, and *White Sea*, is full of scattered Islands which the ancients divided into the *Cyclades* and *Sporades*, because those lie in a round, and these are dispers'd upon and down,

The most famous have been *Delos* where *Apollo* and *Diana* were born ; at present it is called *Sdrille Paros*, now *Paro*, renowned for its White Marble : *Zea Andro*, *Nisira* *Sifano*, and many others, besides those that are near *Asia*, which we shall afterwards discourse of.

We have already mentioned the Islands in the *Baltick*, which the King of *Denmark* possesses, but there are some others also that belong to the King of *Sueden*.

That of *Oeland* lies opposite to *Calmar*, a Town of *Gothia* ; a little more to the North-Eastward is that of *Gotland*, which heretofore had a famous Sea Port called *Wibny*, which gave Laws to Commerce and Navigation. The stately Ruins whereof show it to have been very Magnificent.

The Isles of *Offel* and *Dagbo* are on the Coast of *Livonia*, and that of *Rugen* is near to *Pomerania*, all which are under the Dominion of *Sueden*, but the Isle of *Bornholm* is Subject to the *Dane*.

Before we leave *Europe*, it is to be observed, that it is almost wholly under the Northern temperate Zone ; it hath some Regions indeed under the frozen Zone, which are part of *Norway*, *Finnarchia*, and the greatest part of *Lapland*, and some Lands of *Moscovy*, towards the Straights of *Waigatz*, the Straights of *Gibraltar*, and Cape *Malapan* in *Morea*, lie in the six and thirtieth Degree of Latitude, and these are the most Southern parts of *Europe* : the North Cape lies in seventy two almost, and is the most Northern place thereof.



# A NEW GEOGRAPHY.

The SECOND BOOK.

CHAP. I.

## ASIA.



IN the First Book we have given a Description of *GEOGRAPHY* in general, and of all *EUROPE* in particular: In the following Books we shall treat of the other parts of the Earth; and in the first place of *ASIA*, as being contiguous to *EUROPE*.

*ASIA*, whereof we described the Bounds in the beginning, was variously divided by the Ancients; but at present, these famous Names are abolished, and it looks with a new countenance: I think it ought to be divided according to the Principal Empires that share it, which are under the Obedience of Five Great Monarchs; to wit, the *Grand Signior*, the *King of Persia*, the *Great Mogol*, the *King of China*, and the *Great Cham of Tartary*. To these must be added some Kings of the *East Indies*, with what the *Portuguese* possess there, and the *Hles*, that are numerous and very considerable.

A a a

CHAP.



## C H A P. I I.

## The Empire of the TURK in ASIA.

THE Emperour of the Turks, whom we call the *Grand Signior*, has his Imperial Seat at *Constantinople*, which is in *Europe*; but the greatest part of his Dominions is in *Asia*: to wit, *Anatolia*, *Syria*, *Armenia*, *Mesopotamia*, *Arabia*, *Chaldea*, *Mingrelia*, *Georgia*, and *Circassia*.

*Anatolia* of the Moderns, is the *Lesser Asia* of the Ancients; it is on three sides encompassed by Seas, on the North by the *Black Sea*, on the West by the *Propontis* and *Archipelago*, on the South by the *Mediterranean*; and hath the River *Euphrates* on the East. It was heretofore divided into Two and twenty Provinces, *Pontus*, *Bithinia*, *Asia* Proper, the greater and lesser *Phrygia*, *Troas*, the greater and lesser *Myssia*, *Eolia*, *Ionis*, *Caria*, *Doris*, *Lydia*, *Lycia*, *Paphlagonia*, *Pisidia*, *Isauria*, *Pamphilia*, *Cilicia*, *Lycaonia*, *Galatia* and *Cappadocia*; but at present their Names are lost, their Bounds confounded, their Towns ruined, and their Inhabitants heretofore so polite, are become barbarous. Nor do we certainly know how the Turks divide and name them at present; so that we must rest satisfied to remark the Chief Towns that remain. *Bursa* is one of the most considerable, and was the First Seat of the Turkish Empire; it is a large and well-peopled City: the miserable Remains of *Nice* and *Chalcedon*, famous by their General Councils, and the Ruins of *Troy* are to be seen there. On the *Archipelago* are also *Smyrna*, *Ephesus* where the Temple of *Diana* was, reckoned one of the Seven Wonders of the World, and where a General Council was also held: *Miletum*, *Halicarnassus* which is in *Caria*, where *Arthemisia* erected to her Husband *Mausolus* that Stately Monument which was also ranked among the Wonders: and hence it is that Rich Tombs are called *Mausolea*. On the *Mediterranean* is *Satalie*, which hath given its Name to a Neighbouring Bay; and *Tarsus*, where St. Paul was born. On the *Black Sea* are *Trabizonde*, the Seat of an Empire; and in the Countrey of the Amazons *Sinobi*, heretofore *Sinope*, *Angaure* and *Cenici*.

*Syria* hath the Towns of *Aleppo* and *Damascus*, which are two of the greatest Cities of the Turkish Empire. *Said*, anciently *Tyre*, and *Baruth*, heretofore *Sydon*, famous Towns; *Antioch* now ruined, *Alexandretta* or *Scanderoon*, its principal Sea Port; and *Tripoly* of *Syria*.

*Palastine*, which was comprehended in *Syria*, was called *Canaan* and the *Land of Promise*, *Judea* from a part of it; and the *Holy Land*, because of the Mysteries that there were accomplished. It is bounded on the East by Mount *Libanus* and *Arabia Petrea*, on the South by the same and *Egypt*; on the West by the Sea and *Phenicia*: it hath been divided into four parts, *Galilee* on the North side, *Samaria*, *Judea*, and *Idumea*. In *Galilee* is *Nazareth*, where our Saviour was conceived, *Cana* where he changed the Water into Wine;



Wine; *Capernaum* where he often sojourned, and raised the Daughter of *Jairus*; *Mount Tabor*, where he was transfigured; the Sea of *Galilee*, where he calmed the Tempest, and chose some of his Disciples; *Naim* where he raised the Widows Son: all these Towns are now reduced to pitiful Villages. In *Samaria* is the City of the same Name, which was the Seat of the Kings of *Israel*; there remains no more of that City nor of *Sichem*, but deplorable Ruins. In that Country also they do shew the Well, at which our Saviour spake to the Samaritan Woman: In *Judea* is *Jerusalem*, where he suffered death; its extremly fallen from the ancient splendor it had; nevertheless it is environed with good Walls, and may reach Twelve or Thirteen hundred yards in length, and as much in breadth. It is inhabited by Turks, Moors, and Arabians, who are Mahumetans; by Greeks, Armenians, Syrians, and Copties. There are no Roman Catholicks there but two Convents of Franciscans, the one of St. Saviour, and the other of St. Sepulcher; some Jews also live there. That so famous and holy City hath been often ruined, and as often repaired again. *Mount Calvary* and the *Holy Sepulcher* were once without, but now within the City. It would require a Volume to describe all the holy Places that are within and about it.

Two Leagues from *Jerusalem* is *Bethlehem*, where our Saviour was born; it is at present but a Village full of Ruins, inhabited by some poor Christians and Arabians. *Bethany* where he raised *Lazarus*, is nearer to *Jerusalem*, and is but a heap of Ruins; amongst which they still shew the Tomb where the Body of *Lazarus* lay when he was raised from the Dead, and the ruins of his house, of the houses of his Sisters, *Martba* and *Mary*, and of *Simon* the Leper. *Emaus*, where the Disciples knew their Divine Master, tis in no better condition; no more than *Jericho*: upon the Plains whereof rises a Mountain, where our Saviour fasted Forty days. On the Sea-side is *Joppa*, now called *Jaffa*, *Acre* heretofore *Ptolemais*, and in *Idumea* is *Gaza* and some other Towns. *Jordan* waters that *Holy Land*, runs through the Sea of *Galilee*, which is indeed but a Lake; and loses its clear Streams in the stinking and black Waters of the *Dead Sea*: in this River our Saviour was baptized by St. *John Baptist*.

*Arabia* is divided into three, *Deserta*, *Petrea*, and *Felix*, or the Desert, *Petrea* or the stony, and the happy, the first two are to the North, and the other to the South.

*Arabia the Desert* is the Country where the Children of *Israel* sojourned Forty years, its Chief Places are *Mesbet*, *Orem*, and *Ana*.

*Arabia Petrea* hath *Petrea* (so called from the Name of the Country, but now 'tis called *Crach*) and *Eltor*. In this Country is *Mount Sina*, upon which God delivered the Law to *Moses*.

*Arabia Felix*, or the Happy, so called because it is more fertile than the other two, and bigger also; lies between the *Red Sea* which it hath to the West, the Gulf of *Persia* to the East, and the Indian Ocean to the South. Its chief Towns are *Medina*, where the Sepulcher of *Mahomet* the Prophet of the Turks is: *Attecba* the place of his Birth, *Aden* a place of great Traffick,



*Sana, Mocha, Soar*, and many others. In this Country they gather Frankincence, and several other precious Gums.

*Chaldea* is at the Confluence of *Tygris* and *Euphrates*, its Capital was *Babylon* a famous City, and the Seat of the Babylonian Empire, the Walls whereof, built by the Famed Queen *Semiramis*, were placed amongst the Seven Wonders of the World. It stood upon *Euphrates*, and little or nothing remains of it at present, and less of the Tower of *Babylon*, that was near to it. *Bagdat* is at present what *Babylon* was anciently, being built of its ruins; but upon the *Tygris*, as the other was upon *Euphrates*.

The other Towns of *Chaldea* are *Elmara*, *Gorna*, *Balsara*, at the bottom of the Gulf of *Persia*, *Orchea* which is thought to be the *Ur* of the Chaldees, from whence God called *Abraham*; *Magdon* and some others.

*Mesopotamia*, now called *Diarbeck*, lies to the North of *Chaldea*, and to the South of *Armenia*, between *Euphrates* and *Tygris*; its Chief Towns are *Da-va*, *Merdin*, *Orpha*, *Bir*, and *Caramit*.

*Armenia* is divided into the greater and lesser, the one on this side of *Euphrates*, and the other beyond it; both the two are at present called *Turcomania*. The Chief Towns of the lesser are *Sirus* or *Sebastes*, *Kemach*, *Erzinga*, and *Suar*. Some place here *Samofata*, *Lucian's* Country; but it is in *Arminacha*, which was called *Comagene*. Those of the greater, are *Arzeron*, *Chars*, *Essechire*, which is taken for the Ancient *Artaxata*. In this *Armenia* is Mount *Ararat*, where the Ark of *Noah* rested after the Flood. Some affirm that some remains of it are still to be seen there.

*Georgia* is to the North of *Armenia*; its Towns are *Cori*, *Scander*, and *Glifca*; that Country is the *Iberia* of the Ancients.

*Zuria* or *Albania* lies to the East of it, and reaches to the *Caspian Sea*. The most remarkable places of it are *Derbent*, *Zivacha*, *Sobai* and *Chipiche*.

*Mingrelia* is now-a-days the *Colchis* of old, whither *Jason* went for the *Golden Fleece*; it hath the Sea to the West, and *Georgia* to the East. *Fazza* and *Sevastopoli* are the more considerable Towns thereof.

*Circassia* and *Comania*, Countreys of very little note, lie Northward from the afore-mentioned Territories.

The Isles that the Turk possesses about *Asia*, are famous in Antiquity.

*Tchados*, at the back of which the Grecian Fleet skulked: *Meteliv*, heretofore *Lesbos*, where the renowned *Sappho* was born.

*Chio* or *Scio*, hath a Town of the same Name; this Island produces Mastic and the best Turpentine.

*Nicaria*, anciently *Icaria*, to which *Icarus* by his fall gave the Name.

*Samos*, where *Pythagoras* was born.

*Pathmos*, at present *Palmosa*, where St. *John* the Evangelist was banished in the time of *Domitian*, and had those Divine Revelations whereof he composed the *Apocalypse*.

*Lango*, heretofore *Co* or *Cos*, illustrious by the Birth of *Hippocrates* and *Apelles*; the one gave men life by his Medicines, and the other by the Touches of his Pencil.

*Rhodes*



*Rhodes* retains its Name, but not its Ancient Splendour : Its called *Rodo*, and hath a Town of the same Name. In this place was anciently one of the Seven Wonders of the World, I mean, that famous *Colossus* of Brass, that was Erected at the Entry of the Harbour, betwixt the legs of which Vessels passed. It was thrown down by an Earthquake. This Island is Fifty Leagues in Circuit, and but Six distant from *Caria*. The Turks took it from the Knights of *Rhodes*, who afterwards retreated to *Malta*. it hath some other places as *Lindo* and *Filerno*.

*Cyprus* at present *Cipro*, is one of the greatest Islands of the *Mediterranean*, being above Six score Leagues in Circumference. It was in Ancient times Consecrated to *Venus*, and lies in the Sea of *Pamphilia*, which Country it hath to the North, *Syria* to the East, and *Egypt* to the South : It hath been a considerable Kingdom ; which from the House of *Lusignan* fell into the Dominion of the Republick of *Venice*; and is at present Subject to the Turk. The Chief Towns of it are *Nicosia* and *Famagosta*, that hath a good Port.

And thus you have a short Description of the Territories that the Grand Signior, Emperour of the Turks, possesses in *Asia* : In all which the Mahumetan Religion is publickly Established ; but the Jewish and Christian Religion are both permitted ; and this last is divided into many Sects, as *Greeks*, *Armenians*, *Jacobites*, *Georgians*, *Maronites*, *Coptites* and many others. The Roman Catholics are not so numerous there, as the others are.

There are many Governours in the Turkish Empire called *Beglerbeys*, who have under them *Sangiaes*, that are as their Deputies or Lieutenants.

### C H A P. III.

#### The Kingdome of PERSIA.

THE Empire of the *Persians*, heretofore so Vast and Famous, has been subject to many Alterations. It was founded by *Cyrus*, and overthrown by *Alexander*. The *Parthians* drove his Successors from thence, and maintained long Wars with the Romans ; it was again restored under the Name of the *Persian*, and ruined by the *Califes* the Successors of *Mahomet* : Invaded by the *Tartars* under the powerful *Tamerlan*, and at length Raised again by *Ismael Sophy*, to the State wherein now it is. It is called the Empire of the *Sophy* of *Persia* ; and is bounded on the West by the Turkish Empire, on the East by that of the great *Mogol*, on the North by the *Tartars*, from whom it is divided by the River *Oxus*, now *Abiamus* ; and on the South by the Gulf of *Persia*, and the *Indian Sea* : In a word it Reaches from *Tygris* to *Indus*, and from the *Caspian* to the *Persian Sea*, containing several



several Provinces, *Persia*, *Susiana*: *Parthia*, *Media*, *Assyria*, *Hircania*, *Paropamisada*, *Margiana*, *Carmania* and *Gedrosia*, all which have lost both their Names and Limits. The Metropolis of these States is *Hispahan* or *Isfahan*, a great and fair City containing many stately Palaces, where the *Sophy* keeps his Court and usually resides: It lies in *Parthia* now a days called *Mierak*: The other Towns of that Province are *Cassan*, *Argistan*, *Jex*, *Saba*, and *Targazin*.

In the Province of *Persia* now called *Farsy*, is the Town of *Siras*, which is taken for the Ancient *Persepolis*, burnt by *Alexander*.

*Susiana*, which is called *Cissistan*, hath for its Chief City *Sus* formerly *Susa*, the Imperial Seat of *Ahasuerus*.

*Media* now a days *Servan*, hath the City of *Tauris*, which is the *Ecbatana* of the Ancients.

*Assyria*, whereof the Turk possesses part, hath *Mosul* for its Capital, which is the Ancient *Ninive* the Metropolis of the *Assyrians*.

*Hircania* is called *Diargument*; its principal Towns are, *Mazandaron* and *Strava*.

*Paropamisada* at present *Sablestan*, hath *Candabar* for its chief Town, which gives also a name to all the Province.

*Margiana* or *Elfabar*, hath *Mexed* for its principle Town, where the Kings of *Persia* are Interred.

*Carmania* hath *Chirman*, from which it takes its modern name, *Gedrosia* or *Circan* hath the Town of *Calamate*.

The most Remarkable Isles of *Persia* are in the Gulf of that Name; that of *Ormuz* is near the *Sreights*, and hath a Town of the same name Ruined at present.

The Isle of *Baharem* is famous, by reason that about it they fish for, and take the lovliest Oriental Pearls.

The *Sophy* of *Persia* is *Mahumetan*; but follows the Doctrine of *Aly*, *Mahomet*: Son in Law, whom the *Turks* reckon a Heretick. The *Persians* are of their Prince his Sect, and civilized and polished, and much of the humour of the *French*. The Christian Religion is suffered there, and in *Hispahan* it self there are Convents of several Orders, as bare-footed *Carmelites*, *Capuchins*, *Adinims*, and many others.



## C H A P. IV.

*The Empire of the great MOGOL.*

**T**HE Ancients divided the *East-Indies*, into *India* on this side, and *India* on t'other side of *Ganges*. In the first, called now *Indostan* which lies between that and another River named *Indus*, is the Empire of the great *Mogol*. It hath to the North *Turquestan*, to the West the States of *Persia*, to the South the Territories of several Princes which we shall hereafter mention; and to the East the Kingdom of *Bengala*: It is divided into several Kingdoms, which carry generally the Names of their Capital Cities, as *Agra*, *Labor*, *Delli*, *Kabul*, *Caximir*; but the Kingdom of *Sinda* hath *Tatah* for *Metropolis*. The usual place of Residence of that Monarch is *Labor*, his Palace is Magnificent, and he is the Richest Prince in the World in precious Stones. He is Mahumetan, and most of his Subjects follow the same Religion; but there are many Christians and Idolaters amongst them, and a Sect of *Pythagoreans*, who hold it a deadly Sin to eat any thing that ever had life; who are there called *Bannians*.

## C H A P. V.

*The other States of the EAST-INDIES,  
and what the PORTUGUESE and  
other Nations Possess there.*

**B**Efore we proceed further, we must take a view of the other Kingdoms of the *East-Indies*, and of what the King of *Portugal* Possesses there, that we may not be obliged to come back to the same parts again. These *Indies* have two Peninsules, which are divided by the *Bay of Bengala*. That which is on the West side, contains the Kingdoms of *Decan*, *Onar*, *Barcelor*, *Canara* and some others, with the Coast of *Malabar*, in which are the Kingdoms of *Calicut*, *Cochin*, *Conlan* and others, all bearing the Names of their Capital Towns: They are Scituated on the Western part of this Peninsule. Towards the Eastern, is the Coast of *Coromandel*, where



where are *Negapatan*, *Maliapor* or *St. Thomas*, and the Kingdom of *Bisnagar*, *Narfingue*, *Goleconde* and *Orixa*, which bear the Names of their chief Cities. The two Coasts of this Peninsule are divided by Mount *Gate* which ends at Cape *Comorin*. The Countrey scituated on this Mountain is called *Balagate*.

At the Entry of the other Peninsule, which is to the East, we meet with the Kingdoms and Cities of *Pegu*, *Siam*, *Camboia* and *Tinquin*; and in the Peninsule is the Kingdom of *Malacca*, with its City of the same Name, which is the Southermost Extremity thereof.

In the Entry of the other Peninsule, which is to the West, is the Kingdom of *Cambaya*, with a City of the same Name, and another called *Sinrat*, which is very large, and a place of great Trade, and the Residence of our English President of *India*.

The Kingdom of *Bengala* is near the mouth of *Ganges*, between the States of the *Mogol* and *Pegu*.

The King of *Portugal* possesses the Isle of *Diu*, near the Kingdom of *Cambaya*, which has a Town of the same Name near the Kingdom of *Decan*, the City of *Goa*, one of the greatest Towns of the *Indies*, and the Residence of the Archbishop and Vice-Roy; some places on the Coast of *Malabar*, and on the other side he had heretofore *Maliapor* a considerable Town, where it is believed the Body of *St. Thomas* is. In the other Peninsule formerly he held *Malacca*, which the *Dutch* have since taken from him. Besides these, he hath several Islands, and some places in others which belong not wholly to himself.

## CHAP. VI.

### The Kingdom of CHINA.

SOME Authors make this Kingdom as big as all *Europe*, so vast is its Extent. It hath the Ocean to the East, *Cochinchina* to the South, and to the West the *Indies* and part of *Tartary*, which it hath likewise in the North, and from which it is seperated by that Famous Wall of Four hundred Leagues in Length. It is divided into Fifteen Provinces, the Names of which it is not very material to know: There are above Two thousand Cities reckoned to be in this great Kingdom, and of them *Peking* is the Chief and the Imperial Seat of their Kings. That Throne was overturned by the *Tartars*, who ruined this Empire, and possess the greatest part thereof; but the Natives have lately recovered their Liberty again and expelled the Conquerors. *Nanquin*, *Xanton* and *Amus*, are the most considerable



siderable Cities, and the least is as big if not bigger than *London*. There are in this Kingdom many Fair Navigable Rivers, the chief of which are the *Yellow* and the *Blew*, called in the *Chinese Language*, *Caramoran* and *Jansigum*, and *Chincheo* that passes by the Stately City of *Amis*. The *Chinches* are Idolaters, and Worship the Heavens and Stars, with many Idols that they place in their Temples.

The Jesuits have Converted many of them to Christianity, and are very Active in making Proselytes in those Parts.

## CHAP. VII.

## TARTARY.

THE greater *Tartary* is one of the vastest Regions of the whole Earth. It hath to the West the Straits of *Muscovy*, the Ocean to the North, to the East the Seigns of *Anian*, or *Jesso*, according to some Maps, and to the South *Persia*, *India*, and *China*. Several Princes have Dominions in the great space of Land, and among others the Prince of *Nuche* on the East-side, who Invaded and Conquered *China*: But the most considerable of all is the *Great Cham*. One of his chief Provinces is *Cathay*, which some take for *China*, and its City of *Cambalu* for that of *Pekin*, so uncertain Men are in the knowledge of those distant Countries. It is nevertheless sure that there are Vagabond *Tartars*, divided into Societies called *Hordes*: They Inhabit that place which is called *Tartary Desert*, near which is the Kingdom of *Afracan*, with a Town on the same Name on the *Volsa*. In these Countreys, as 'tis reported, grows the *Boranetz*, which is a Fant Animal, that is, half a Plant and half an Animal: It is in Shape like a Lamb, and fastned to a stalk, about which it Nibbles and Eats the Grass, which once failing, it withers and dies. The other parts of *Tartary* are, *Turquesan* and *Zagatby*, the chief City whereof is *Samar-kand*, the Imperial Seat of the Victorious *Tamerlan*. Most part of the *Tartars* are Mahumetans, there are many Idolaters, some *Jews*, and very few Christians among them.



## C H A P. VIII.

*The Isles of ASIA in the Ocean.*

**I**N treating of the Territories of the *Turk*, we spake of the Isles of *Asia* that are in the *Mediterranean*: We must now mention those in the Ocean which belong to that part of the World; but seeing they are so numerous, that a large Volume would be too little to describe them all in, we shall only touch at those which are the most considerable and of greatest Note amongst them.

The *Maldives* lie towards the Cape of *Comorin*, to the South and West thereof; there are many of them, and they reach to the Line, being divided into certain Parcels, which are called *Atollons*, and contain many small Islands, separated by very narrow Channels; they are full of *Cocotrees*; the Inhabitants are Mahumetans, and subject to a King.

*Zeilan* or *Zeilon*, is near *Cape Comorin*, being Two hundred and forty Leagues in Circumference: The *Indians* call it *Tenafirim*, that is, a Paradise of Delights; there grows the Tree whereof Cinnamon is but the Bark, and that in such plenty, that there are whole Forrests of them: Fair Emeralds and fairer Elephants are likewise to be had there. Some would have it to be the *Taprobane* of the Ancients, which others think to be *Sumatra*. One of its chief Towns is *Sitavaca*, the Residence of a Prince who takes the Title of Emperor of *Zeilan*, to whom the other Kings are Tributary. It is divided into several Kingdoms, of which *Candy*, that is in the middle of the rest, is one of the chief. The *Portuguese* had formerly some places there, of which *Columbo* was the most Important: But at present the *Hollanders* are possessed of that and much more than ever the *Portuguese* had. The Natives are either Mahumetans or Idolaters.

*Sumatra* is divided by the Straights of *Singapura*, from the Peninsula of *Malacca*. Most part of the Modern Geographers take it for *Taprobane*; the Equinoctial cuts it almost in the middle, it is very large, and some assign to it Thirty Kingdoms. Its chief Towns are, *Achein*, *Pedar*, and *Batiam*: The Inhabitants profess Mahumetanism, and many of them are still Idolaters.

Great *Java* is near to *Sumatra*, and is separated from it but by an Arm of the Sea, called the Straights of *Sonda*. This Island is about Two Hundred Leagues in Length, but not above Forty in Breadth: It is Subject to several Princes, who are Tributaries to another, by them called *Matavam*, that is to say, Emperour. It hath considerable Towns, such as *Bantam*, *Palambuan*, *Japara* and *Batavia*, called so by the *Hollanders*, being formerly



formerly called *Jacatra* : They took it in the Year One thousand six hundred and seventeen , and have strongly fortified it , and made it the Residence of their General , and Principal Seat of their great *East-India* Trade . The Inhabitants of the Island are for the most part Mahumetans.

Little *Java* is now called *Cambaya*, and but little known , some of its Inhabitants are Idolators.

*Borneo* lies to East of *Malacca* and *Sumatra* , and to the North of *Java* : This is one of the greatest Islands in the Ocean ; it is almost round , and hath above 200 Leagues in Diameter . Its Principle Town carries its Name . Most part of the Inhabitants profess Mahumetanisme , and the rest are plunged in Idoltry.

*Celebes* is to the East of *Borneo* , and is much less than it , the chief Towns thereof are one that goes by the same Name and *Durate*.

*Gilolo* isto to the East of the former , and is not so great ; it hath a Town of its own Name , and another called *Tilo*.

The *Molucca's*, so Famous for the Cloves, Nutmegs, and Mace , which they disperse through the whole World , lie under the Equinoctial , betwixt *Celebes* and *Gilolo* . The chief are *Ternate* , *Tider* , *Motir* , *Macbian* and *Bachian* . The *Portuguese* have had some places there , which have been disputed by the *English* and *Dutch*, and finally carried by the latter , who have Engrossed the Trade of those Rich Spices.

*Banda* is to the South of *Gilolo* , and furnishes also Nutmegs . The *Hollanders* have the Possession thereof.

The *Philippine Island* , called so by the *Spaniards*, in Honour of their King *Philip* the Second , are so many in number , that some Authors reckon above Ten thousand of them . They lie Northward from the *Molucca's*, and Eastward from *Cochinchina* . The greatest and most considerable of them is *Luconia* , where the Town of *Manilla* is . The other that are remarkable are those of *Mindanao*, which hath a Town of its Name , the Isles of *St. Juan* , of *Cebu* , *Matan* and *Tandayo* : Betwixt this last and the Isle of *Lucon* , is the Streights of *Manilla*, Famous amongst Navigators.

*Amacao* or *Macas* , is a small Island on the Coast of *China* , where the *Portuguese* have a Town of the same Name.

The Isle *Formosa* , the *Lucains* , and some others , are to the East of *China*.

The Empire of *Japan* , is composed of several great Islands , on the the East of *China* , the chief of which is called *Nippon* , and its Capital Town *Meaco* ; though this present Emperour hath his Court at *Jedo* in the East part of the Island . Many Jesuites have here lost their lives for Preaching Christ to that Idolatrous People . To the North of this Countrey the Land of *Jesso* hath been lately discovered , divided from it by the Streights of *Sangar*.

The chief Mountains of *Asia* , are *Taurus* , *Libanus* , *Caucasus* , and *Imanus* . Its chief Capes , are that of *Comerin* in the *Indies* , *Lampo* in *China* , *Farrach* , *Razalgate* and *Monzandam* in *Arabia* the happy , and the Promontory



tory of *Tabin* in *Tartary*. Its principal Rivers, are the *Volga*, *Araxes*, *Oxus* now *Abiamus*, and *Jaxartes* or *Chefel*, which run into the *Caspian*, Sea.

*Euphrates* and *Tigris* come from the Mountains of *Armenia*, embrace *Mesopotamia*, and uniting in *Chaldea*, fall into the Gulf of *Persia*. *Indus* comes from *Caucasus*, gives its name to *India*, which it watereth, and afterward runs into the Ocean, as *Ganges* does into the Bay of *Bengall*.

The *Cosmin* passes by *Pegu*, and the *Menan* by *Siam*, they both proceed from the Lake of *Chiamay*, and fall into the Ocean.

The Yellow and Blew Rivers are in *China*.

The *Tartar*, that is thought to have given Name to *Tartary*, runs into the Northern Ocean, and the *Oby* also.

It is to be observed, that the greatest part of *Asia* is in the Temperate Zone: It hath some Regions in the Torrid, to wit, part of *Arabia* the happy, and of the *Indies*; with many Isles. Some Countreys of *Tartary* are in the Frozen Zone. To conclude, *Asia* reaches from the Equinoctial to the Seventieth degre of North Latitude; and some of its Isles are Ten degrees beyond the Line.

## CHAP. IX.

# AFRICA.

There is no need of crolling the Sea to go from *Asia* to *Africa*, since we have a passage by Land, which is the *Isthmus* of *Suez*, betwixt the *Red Sea* and the *Mediterranean*. Having passed that, we find at first sight *Egypt*, and proceeding from East to West, we shall in order find *Berea*, *Barbary*, and the Kingdoms of *Fez* and *Morocco*, that are washed with the Ocean. Afterward from North to South, we will meet with *Biledalgerid*, *Zabara*, the Countrey of *Negres*, *Guinea*, the Kingdom of *Congo*, the Countrey of *Cassres*, as far as the Cape of good Hope. Afterward going tovvards the North, we shall find *Zanguebar*, and some other Countreys; and then having visited those Regions that are in the heart of *Africa*, as *Nubia*, *Ethiopia*, and *Monomotapa*, we shall end with its Mountains, Capes and Isles.



## C H A P. X.

## EGYPT and the Region of BARCA.

WE shall view the Countreys of *Africa*, that lie upon the Ocean, after that we have seen those that are upon the *Mediterranean*. *Egypt*, so famous both in Sacred and Prophane History; which speak so often of its *Pharaoh's* and *Ptolomies*, hath on the East the *Isthmus* of *Suez*, and the *Red Sea*; on the North the *Mediterranean*, on the West the Countrey of *Barca*, and on the South *Nubia* and *Ethiopia*. It hath not so many Towns at present, as it had heretofore. The Metropolis of it is *Caire*, a very great City on the right Bank of the River of *Nile*. On the other side of that River are to be seen those famous Pyramids, which were the Monuments of some Kings, and have been reckoned amongst the Seven Wonders of the World; and as in all probability they were the most ancientest of the Seven, so 'tis certain they are the only one remaining. *Nile* having washed *Caire*, divides it self into two Branches, which embrace the Countrey called *Delta*, from the Greek Letter  $\Delta$ , which it resembles; these two Branches produce others, which made several Mouths to that River, some of which are stopt up. The other Towns are *Asna*, anciently *Siene*, towards the South *Alexandria*, heretofore the Capital City under the *Ptolomies*, preserves still in its stately Ruins, the Name of *Alexander* the Great, who founded it: It lies upon the Sea, and near the place where the Phare stood, which was one of the Seven Wonders. *Rosetta* and *Damieta*, are also upon the Sea, at two other Mouths of the *Nile*. All this fair Countrey is made wonderfully fruitful, by the over-flowing of the *Nile*, and is subject to the Turk: the Inhabitants are Mahumetans, but there are many Jews and some Christians among them.

The Region of *Barca* was anciently called *Cyrenaica*, and hath *Egypt* on the East, the Sea on the North; on the West *Barbary*, and the Desarts that carry its name, with *Lybia* on the South; its chief Town is likewise called *Barca*; the others are *Alberton*, *Patriarcha*, *Bonandrea*, *Berniche*, and some more. The People are Mahumetans, Subjects to the Turk.



## C H A P. XL.

BARBARY, *with the Kingdoms of*  
FEZ and MOROCCO.

**B**Arbary hath to the East the Countrey of *Barca*, to the North the *Mediterranean*, to the West the Kingdoms of *Fez* and *Morocco*, and to the South Mount *Atlas*, which divides it from *Biledulgerid*.

Going from East to West we find the Kingdoms of *Tripoly*, *Tunnis*, *Algire*, and *Tremefin* or *Telenfin*, with their chief Towns of the same Name. Near to *Tunnis* are to be seen some Ruins of the famous *Carthage*. In the Kingdom of *Algire* is *Bugie* and *Gigery*; and some other places that may be seen in the Map, but very little known to us. The People of that Countrey are Mahumetans, and subject to the Turk, and have for many Ages practiced Pyracy upon the Mediterranean, to the great Annoyance of the Christians Commerce.

The Kingdom of *Fez* has to the South *Morocco*, to the East the Kingdom of *Tremefin*, to the North the Streights of *Gibraltar*, and to the West the *Atlantick* Ocean; its chief Cities carries the same Name, and is a beautiful and stately Place; the Principal Mosque of it is above a quarter of a mile in circuit, and therein burn constantly Nine hundred Lamps. The other Towns are *Mahamore*, *Larache*, *Alcazer*, and *Tetuan*; (the two former belong to the King of *Spain*) and *Tangier* belonging to the King of *Great Britain*.

The Kingdom of *Morocco* lies to the South of that of *Fez*; its chief City bears the same Name, and is beautiful and large, though it hath lost much of its ancient Splendour. On the the Top of one of its Towers, are three Golden Balls, which are believed to be Enchanted. Next to *Morocco*, the Town of *Agmet* is the most considerable: These two Kingdoms belong to one Prince, who is called Emperor of *Morocco*; he is Mahumetan, and his Subjects are of the same Religion; but there are many Jews and Christians among them.



## C H A P. XII.

## BILEDULGERID and ZAHARA.

**B**ILEDULGERID signifies a Countrey of Dates, because it abounds with Palm-trees, which bear that Fruit. The Ancients called that Region *Numidia*; it reaches from the Atlantick Ocean to *Egypt*; the space of a Thousand Leagues: Mount *Atlas* divides it from *Barbary* on the North, and *Zara* bounds it on the South. Its best Province is *Suz* on the Atlantick Ocean; the rest, which are *Tesser*, *Dara*, *Segelmesse*, *Zeb*; and some others, most of which take their Names from their Towns, are but little inhabited, by reason of the great inconveniences of want of Water, noxious Animals, and the barrenness of the Soil. *Zahara*, or the Defart, is the Ancient *Lybia*, and reaches from the Ocean to *Egypt*, and hath *Biledulgerid* to the North, and the Countrey of *Negres* to the South. There is hardly any thing there but Defarts and heaps of Sand, which being driven by the Wind, many times bury Travellers alive, and being heated by the direct Beams of the Sun, render the Air insupportably hot. However there are some places inhabited, as *Zanbaga*, *Zuerziga*, *Terga*, *Agadez*, *Berdoa*; and some others, so little known to us, that we can say nothing with any certainty of them. These People, as well as those of *Biledulgerid*, are Mahumetans, and some of them Idolaters.

## C H A P. XIII.

## The Countrey of Negres and Guinea.

**T**hat Countrey which is called the Countrey of *Negres* or *Nigritia*, hath on the West the *Atlantick Ocean*, on the North the Defarts of *Lybia*, on the East *Egypt*, *Nubia*, and the Empire of the *Abyssins*; and on the South *Guinea* and the Kingdom of *Congo*: It is about a Thousand Leagues in length, and of a very considerable breadth. The River *Niger* waters it, and overflowing like the *Nile*, renders it fruitful: It is divided into several Branches, whereof the two chief are *Senega*, *Gambao*, or *Riogrande*, which fall into the Ocean near *Cape de Verd*. That great Countrey is divided into several Kingdoms; of which the



the most remarkable are *Geneboa*, *Tombut*, *Senega*, *Gago*, *Gualata*, *Melli*, *Cano*, *Agadex*; and betwixt the Branches of the *Niger*, the Kingdom of the *Jaloffes* and *Gambia*. They have generally either given or taken their Names from their chief Towns. The People are of different Religions; a great many of them are Idolaters, and some few are Mahumetans; they are subject also to different Princes.

*Guinea* hath to the East and North the Country of *Negres*, in which some Geographers also place it, towards the West and South the *Ethiopic* Ocean. It contains the Kingdoms of *Sierra Leona*, *Sabon* and *Benin*. It hath no Towns of any note. The Coast there is called by several Names, as the *Grain Coast*, the *Quana Coast*, and the *Gold Coast*, upon which the English, Dutch, and some other Nations, have their Forts and Factories. The Natives drive a great Trade with the *Europeans*, who transport yearly into the *West-Indies*, several thousands of these wretched Animals, sold to them by their inhumane Lords, and sometimes by their own Parents, into perpetual Slavery. This Country abounds in Gold; the Nations for the most part are Idolaters, and some of them worship their Kings.

## C H A P. XIV.

### The Kingdoms of Congo, Cacongo, Angola, Malemba, and Mataman.

THESE Kingdoms are by some Geographers placed in *Ethiopia*; but we distinguish them, because under that name the Country of the *Abyssins* is chiefly understood.

The Kingdom of *Congo* hath to the East the Empire of *Prester John*, to the North the Country of *Negres*, to the West the Ocean of *Ethiopia*, and to the South the Kingdom of *Angola*. It is divided into several Provinces, and its chief Town is called *St. Salvador*. Next to that the most remarkable are *Panbo*, *Batta*, *Sanbo*, *Sunde*, *Pemba*, which take or give their Names to their Provinces. The River *Zaire*, that comes from a Lake of the same Name, runs through this Kingdom, with a Stream famous for its swiftness and breadth. That of *Coanza* makes the Isle of *Loanda* at its Mouth; there is another River likewise called *Lelinde*. In the Northern part of this Country, there are People called *Amricams*, who are reported to eat Mans Flesh, which is sold in the Shambles, as Beef and Mutton with us.

When the *Portuguese* discovered the Kingdom of *Congo*, the Inhabitants of it were Idolaters, and worshiped the Sun, believing that the Souls of good

good Men after death, were carried to Inhabit about that glorious *Luminary*. Since that time many there have Embraced the Christian Religion.

The Kingdom of *Caconga* is to the Eastward of the former; and there is no Town observed in it.

That of *Angola* is to the South of *Congo*; its chief Town is *Dongo*: Here are the Mountains of *Cambambe* (Rich in Silver Mines) and *Cape St. Mary*.

The Kingdom of *Malemba* is to the East of *Angola*, and near the Lake *Zambre*; that of *Mataman* is to the South of it. The People of these Kingdoms are Idolaters, but the Jesuites daily endeavour their Conversion.

## C H A P. XV.

### Caffreria, Sofala, Zanguebar, and some other Countreys.

THE Country of the *Caffres* or *Hottentots*, named *Caffreria*, hath to the East and North *Monomotapa*, to the West and South the Ocean, and reaches to the Cape of *Good Hope*. Along the Coasts of it are good Ports. No Towns are to be seen here; the People are altogether barbarous, having neither Laws, Kings, or Religion. Near the Cape of *Good Hope* the *Hollanders* have planted a very Noble Colony, which supplies in great abundance all Necessaries to their Ships as they go, and come from the *East-Indies*.

The Kingdom of *Sofala* is upon the Indian Ocean, its chief Town bears its Name, and is built in an Island made by the River of *Cuama*. Some Authors take this Country for the Land of *Ophir*, whither *Solomon* sent to fetch Gold for Adorning of that stately Temple which he Built.

*Zanguebar* is to the North of it, and extends it self upon the Indian Ocean, which it hath to the East, as far as the Kingdom of *Adca*, which it hath on the North side, and the Empire of the *Abyssins* to the West. It comprehends Six Kingdoms, to wit, *Mongalo*, *Mozambique*, *Angosbe*, *Quilao*, *Mombaza*, and *Melinde*; each of them having a Capital Town bearing its Name. The Inhabitants are Idolaters or Mahumetans, with some few Christians. The *Portuguese* possess *Mozambique* and *Mombaza* with some other places.

Continuing still Northward and along the Indian Sea, we find the Republick of *Brave*, consisting onely in one Maritime Town of the same Name, which was pretty Rich, before it was sacked by the *Portuguese*.

Ccc

Next



Next we find the Kingdoms of *Magadoxo* and *Adel*, with their Capitals of the same Name. the latter reaches to the Cape *Guardafuy* and the Straights of *Babel mandel* which Joyns the Ocean to the Red Sea.

The Kingdom of *Sabe* is upon that Sea and under the *Ottoman* Empire. Its chief Towns are *Avguico*, *Doncale* and *Sugum*, all three Maritime.

If there be any other little States, they are so inconsiderable, that it is not worth our while to stop and view them, just when we are about to consider larger and more Famous Territories in the middle of *Africa*, whereof we have now Surveyed the Confines.

## CHAP. XVI.

### NUBIA.

**N**UBIA hath the *Nile* on the East; which divides it from *Ethiopia*, that is likewise to the South of it. The Country of *Negro's* on the West, and *Egypt* on the North. Its Metropolis of the same Name is upon the *Nile*, and the others deserve not the Name of Towns, being but pitiful Villages. The Inhabitants have been Christians, and according to some Authors are so still; but without any Exercise of Religion: of which they retain nothing but the shadow and confused Knowledge.

## CHAP. XVII.

### Ethiopia or the Empire of the Abyssins.

**S**OME Geographers divide *Ethiopia* into the Upper and Lower, and under this comprehend the Kingdoms of *Congo*, *Angola*, and some others, whereof we have treated; and those of *Monomotapa* and *Monemgi*, of which we shall speak: And under the other they place the Empire of the *Abyssin*; but because this retains particularly the Name of *Ethiopia*; we shall use the same without perplexing our selves about that Division.

*Ethiopia* has to the North *Nubia* and *Egypt*, to the East, the Kingdom of *Abex* and *Zanguebar*, to the South *Monomotapa*; and to the West the Kingdom of *Congo*, and the Country of *Negro's*. That vast Tract of Land which makes the Empire of the *Abyssins*, is all in the Torrid Zone,

and

and reaches almost from the one Tropick to the other. Its length from North to South, is Six hundred Leagues. The *Nile* crosses it, and forms therein a Famous Island, which the Ancients Named *Meroe*, and the Moderns *Gueguerre*.

This great State is divided into a great many Kingdoms or Provinces, which bear that Name. The next to *Egypt* is the Kingdom of *Cansila*, then stretching Southward, these following are to be seen, *Barbagasso*, *Tigremahon*, *Bagamidri*, *Amara*, *Rosa*, *Nar a*, *Zir*, and several others which I mention not, as judging it useless to fill this Description with barbarous Names that are good for nothing: The Towns here are mean and inconsiderable, having neither beauty nor extent, with pitiful Houses built of mud or clay and straw, because there is but very little wood or lime in the Country. Nor hath the King of *Ethiopia* fixed upon any Town for his usual Residence, but goes from Province to Province; having all his Court lodging in Tents, of which he hath always Five or Six thousand carried about with him in his Retinue. This is an odd way of living, and yet he is one of the greatest Princes in the World; he hath vast and large Dominions, great Treasures, rich Furniture, and can send numerous and strong Armies into the Field. He is abusively called *Prester John*, his Subjects call him *Adiabogue*; which signifies Emperour, and some Moderns, *Negus*, as much as to say Monarch. That Powerful Prince and all his Subjects profess Christianity, but with some mixture of Jewish Ceremonies; for they retain both Circumcision and Baptism. Their Priests Marry, but yet they have Monks. They have a Patriarch who is the Head of their Church, whom they call the *Abuna*; and their Country is full of Monasteries.

## CHAP. XVIII.

### The Kingdoms of Monœmugi and Monomotapa.

**T**HE Kingdom of *Monœmugi* hath to the North the Empire of the *Abyssins*, to the East *Zanguebar* and *Sesala*, to the South *Monomotapa*, and to the West *Congo*. *Sesala*, whereof we have spoken, depends on it, and belongs to the same Prince: His other Countreys are inconsiderable, and the Towns that are more so, are *Bel Agag*, *Camar*. To the Northward of this State rise above the Clouds the high Mountains of the Moon. The Inhabitants are almost void of all Religion.

C c c 2

The



The Kingdom of *Monomotapa*, hath the last Kingdom we spake of to the North, and on all other sides the Countrey of the *Cassres*. The chief City of it and Seat of the Prince is of the same Name; its other Towns are *Mogar*, *Mofata* and *Gale*. Under it are comprehended the Kingdoms of *Toroa*, *Inhambane*, and *Inhamior*. Its Inhabitants are Idolaters, whom the Jesuits labour to convert to Christianity.

This Rigion is watered with the Rivers of *Cuama* and *Spiritu Sancto*.

These are the more known Regions of *Affrica*, which yet are so little, so that what we can say of them deserves not the Name of a Description. The chief Mountains are, *Atlas*, *Sierra-Liona*, *Mount Amara*, and the Mountains of the *Moon*.

The chief Capes thereof are, *Cape Verd*, the *Cape of Good Hope*, and *Guarda-fuy*.

Its Rivers are the *Nile* that runs into the *Meditarranean*, after it hath watered *Ethiopia* and *Egypt*. The *Niger* that runs through the Countrey of *Negres*, and falls into the *Atlantick* Ocean near the *Cape Verd*, where it makes many Branches. The *Zambre*, that proceeds from a Lake of the same Name, runs through the Lake of *Zachaf*, and dividing it self into two Branches, one whereof is called *Cuama*, and the other *de Spiritu Sancto*, both whereof are discharged into the Indian Sea; and the River *Zaire*, which falls with great Impetuosity into the Ethiopian Sea.

## C A H P. XIX.

### The Isles of AFRICA.

**I**N the *Mediterranean* are first the Isle of *Maha*, the *Melita* of the Ancients, Famous for the Shipwrack of the Apostle *St. Paul*, and the Residence of the great Master of the Order of *St. John* of *Jerusalem*, which bears its Name: It is Seven Leagues Long, and Four Broad. Its Towns are the *Valette*, the City, the *Bourg*, and *St. Michael*, with the Castle *St. Elme*. The Isles of *Comin* and *Comminet*, *Forfora*, *Gozze*, *Lampadosa* and *Limosfa* belong likewise to the order of *Malta*.

The Isle of *Pantalarea* belongs to the *Portuguese*, and that of *Zerbito* to the *Turks*.

In the *Atlantick* Ocean are the *Canaries* that belong to the *Spaniards*, *Porto Santo*, *Madera*, and the *Cape De Verd Islands*, which belong to the Crown of *Portugal*.

*Porto Santo* is near to *Madera*, and in respect of it inconsiderable, for *Madera* is large and fruitful, producing good Wines, and that Sugar which goes by its Name. The chief City of it is *Funchall*, and has a Bishop *Suffragant* to the Archbishop of *Lisbonne*. The People are Civil and Roman Catholics.

The



The *Canaries*, which the Ancients called the *Fortunate Islands*, because of the goodness of the Air and Soil, are to the West of the Kingdom of *Morocco*: they reckon Seven of them, that are the chief; to wit the *Grand Canaries*, the Isle of *Ferro*, the Isles of *Taneriffe*, *Lacerotte*, *Palma*, *Gomer*, and *Fortventura*. The great *Canary* which hath given its Name to all the rest, and got it from the abundance of Dogs that were found there, hath a Town of the same Name which is a Bishoprick.

The Island of *Ferro* is considerable, for that we have from thence taken our beginning of Longitude, it being the most Westerly of these Islands. There is here a Tree which so condenses the Air, that it furnishes the Inhabitants with Water, which is otherwise scarce enough with them.

*Taneriffe* is remarkable for a great Mountain, which is thought to be the highest in the World; called by the *Spaniards* *Pico*: from thence we have the best *Canary Wine*.

The rest are but inconsiderable.

The Cape *De Verd* Islands, so called, because they are opposite to that Cape, were known to the Ancients by the Name of *Hesperides*, *Gorgonia*, and *Gorgades*: The chief of them are Eight, to wit, *St. Anthony*, *St. Vincent*, *St. Luce*, *St. Nicholas*, *St. Jago, del Sal*, *Mayo* and *Fuego*. That of *St. Jago* or *St. James*, is the most considerable. It hath a City of the same Name; the Bishop whereof is Suffragant to the Arch Bishop of *Lisbon*: Its other Towns are, *Ribera* a great place and much frequented, *St. Thomas*, *St. Michael*, and *La Praya* which is its best Port. The Air of this Island is extremely bad.

In the *Ethiopick* Ocean and near *Sierra-Liona*, are the little Isles of *Farellon* and *Massacoya*.

Somewhat farther in the bottom of the Bay or Bight of *Guinea*, is that of *St. Thomas*, discovered on that Saints day whose Name it bears. It is directly under the Equinoctial: Its chief Town is *Pavosan*, Inhabited by the *Portuguese*.

The *Princes* Island is near to the former, and was so called because the Revenue thereof was appointed for the use of the Eldest Son of the King of *Portugal*.

The Isle of *Farnandopo* is to the North of that, and near the Coast of *Guinea* and the Kingdom of *Benin*.

Beyond the Line we find the Isle of *Annobon*, which last the *Portuguese* called so, because they discovered it on New-years day.

The Isle of *Ascension*, discovered on Ascension day, and therefore so called, is farther to the South in the *Ethiopick Sea*, and is neither inhabited nor habitable for want of Water, but it is abounding in Turtle or Sea Tortoise. *St. Helena*, for a like reason so named, is of all the Islands in the World the most Remote from the Continent, being about Four hundred Leagues distant from it. It hath excellent Fresh Water, and so Salubrious an Air, that the Sick who land there, recover their Health quickly. It belongs to the English, and all the Ships that come from the *East-Indies* and belong to *England*, do commonly put in and take Fresh Water there.



In the same Ocean, and towards the Cape of Good-Hope, are the small Islands of *Elizabeth*, *Cornelia* and *Fera*.

Beyond that Famous Cape, and to the East of *Africa*, in the *Indian Sea*, lies the Isle of *Madagascar*, called also of St. *Laurence*, or of *Laurence Armeide* who discovered it, in the year One thousand five hundred and six, on the day of St. *Laurence*. It is one of the greatest Islands in the World; containing about Six hundred Leagues in Circuit, Two hundred and sixty in Length, and in some places an Hundred in Breadth. Its Length reaches from North to South, from the Eleventh Degree of South Latitude, to the Five and Twentieth, so that it is almost altogether in the Torrid Zone, the Southern end of it being onely without it; over which the Tropick of *Capricorn* passes. It is very probable, that they who have taken this for the *Cerne* of *Pliny* and the *Menuthias* of *Ptolemy* are mistaken, and that the Ancients never knew it. It hath no Towns, only Villages beset with Stakes, the fairest of which is *Fauzaine*. The Inhabitants have little or no Religion, they have neither Temples nor Altars; they Fear a God, but Worship him not. The *French* have made some Voyages thither, and printed Relations of the same.

There are many little Isles about this, of the chief whereof we shall only speak. To the East of it are the Isles of St. *Mary*, of *Bombon*, *Maurice*, and *Diego Roiz*. To the North, *Gade*, *Agulha* and *Natal*. To the West, *Mobila*, *Camora*, *Mayota*, *Jobanns*, and St. *Christophers*.

Near the Coast of *Zonguebar* is an Island of the same Name, having to the South the Isle of *Monsia*, and to the North that of *Pemba*.

Near the Cape *Guardafuy* lies *Zocotora* with a Town of the same Name. This is the *Dioscorides* of the Ancients; it produces the best Aloes and Dragons Blood; between this and the said Cape lies another Island, called *Abba del Curia*.

It is to be observed that the greatest part of *Africa* is in the Torrid Zone, and that the Line cuts it so exactly in the middle, that it reaches as far to the South, as it does to the North of it, that is to the Five and thirtieth Degree of South and North Latitude; however the much greater part is to the Northwards,

*The End of the Second Book.*

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# A NEW GEOGRAPHY.

The THIRD BOOK.

## CHAP. I. AMERICA.



Eare now come to the New World; for so Men hath been pleased to call this Continent which is divided from *Europe*, *Asia* and *Africa*, because it hath not been known to us much above an Hundred and four score years. It is held, that *Christopher Columbus* a Native of *Genoa* first discovered it in the year One thousand four hundred ninety two; yet it carries not his Name, but that of *Americus Vesputius* a Florentine, who five years after *Columbus*, in the year One thousand four hundred ninety seven, discovered *Bresile*; which was the cause that all that part of the World is called *America*. It is likewise called the *West-Indies*, in distinction from the *East-Indies* in *Asia*. It hath to the East, the Sea called the *North Sea*, *Mar del Nort*, to the West the South or *Pacifick* Sea, to the South the Streights of *Magellan*; but its bounds to the North are



are unknown to us, and we cannot tell whether there be Seas or Lands. By the *Isthmus of Panama*, which makes it two Peninsules, it is divided into the North and South *America*.

In North *America*, and on the North Sea, are *Estotiland*, *Greenland*, *Terra de Labrador*, *Canada*, or new *France*, *New England*, *Maryland*, *Virginia*, *Carolina*, *Florida*, *New Spain*, *Jucatan*, *Honduras*, *Nicaragua*, *Costarica* and *Veragua*. And on the *Vermilian Sea*, *Anien*, *Quivira*, and *New Mexico*.

In South *America* are *Golden Castille*, *Guiana*, *Brasile*, *Plata*, and *Terra Magellanica*, all upon the North Sea, and on the South or *Pacific Sea*, *Chili*, and *Peru*; and *Tucuman* in the middle.

## CHAP. II.

### North AMERICA.

**E**STOTILAND, *Greenland* and *Terra de Labrador* or *Laborador*, have no Inhabitants but Savages, who live amongst Ice and Snow, with which these Countreys are covered. The Reader must not expect Towns here, for there are none at all: We are only to observe that *Greenland* is a Countrey lately discovered, and that there was another of the same Name, which cannot now be found; though the Kings of *Denmark* to whom it belonged, have in vain sent Ships in search of it. It had Towns, with Churches, and Monasteries; but no body can tell what is become of it: whether the passage to it be blockt up by the Ice, or that it hath been swallowed up in the Ocean.

*Canada* is called *New France*, because the French discovered and planted a Colony in it; the chief places thereof are *Quebec*, and *Tadoussac*, upon the great River of *St. Lawrence*.

*New England* is a Rich and Flourishing Countrey, with many Towns, the chief thereof is *Boston*, Inhabited by the English.

*Maryland* is Peopled by the King of *Great Britain*'s Subjects, and belongs to the Lord *Baltimore*, who holds it of that Crown.

*Virginia* was so called by the English, because they discovered it in the time of Queen *Elizabeth* who was never Married. In it is *James Town*, and some others; the principal product of this Countrey is Tobacco, which from hence is carried into most parts of *Europe*.

*Carolina* is a late Plantation of the English, not fully settled as yet.

*Florida* was so Named by the Spaniards, who discovered it on Palm Sunday. It stretches to the South in form of a Peninsule: In it are the  
Towns



Towns or Villages of *St. Matthew*, *St. Augustine*, and the River of the Holy Ghost.

*New Spain* is one of the loveliest Provinces in this New World. There stands the City of *Mexico*, which gave the Name to a great Empire, whereof *Montezuma* was the last King. *Fernando Cortez* Invaded it, in the year One thousand five hundred and nineteen, took that Prince, and Conquered his Country. There are many other Towns in that Countrey, the chief whereof are, *Mexicoacan*, *Los Angeles*, *Vera Cruz*, *Valladolid*, and *Guatamala*. *Mexico* the Capital stands upon a Lake, it is large and well peopled, being the Residence of a Vice-Roy, and Seat of an Archbishop. *Yucatan* is a Peninsule on the Bay of *Mexico*, the chief Town whereof is *Merida*.

*Honduras* has the Town of *Trusille*. *Nicaragua* hath *Cartagen*, and *Veragua* and *La Concepcion*. These Three last Provinces and *Costarica*, lie between the South Sea and the Bay of *Mexico*.

*Anien* is onely remarkable for the Streights that carry its Name, which are by some thought to be fabulous; and runs between *California* and the land of *Jesso*: this land is supposed to stretch far out into the West, and is seperated from *Asia*, onely by some branches of the Sea, and from *Japan* by the Streights of *Sangar*.

*Quivira* was called *New Albion* by Sir *Francis Drake* Admiral of an English Fleet, who discovered that Countrey in the year One thousand five hundred and seventy nine: it lies on the *Vermilian* Sea, that divides it from *California*; but there are no Towns observed in it.

*New Mexico* contains *New Granada*, wherein is the Town of *Staffe*.

### CHAP. III.

## South AMERICA.

UPON the Isthmus of *Panama* are two Towns, whereof the one that gives it the Name, is upon the South Sea, and the other, which is upon the North, or rather the Bay of *Mexico*, is called *Nembris di dios*. Beyond that space of Land, which lies between the two Seas, are the following Regions on the North Sea.

*Golden Castille*, so called from that precious Metal which is found there in abundance. Its chief Towns are *Caribugena*, *St. Martha*, and *St. Fe de Bogota*.

To the East of that is the Country of the *Caribbes*, in which is the North



North Cape, well known to those that Sail in these Seas. The Inhabitants go Bare Naked, and have neither Government nor Religion.

*Guiana* is to the South; it hath a Town called *Manoa*, and by the Spaniards *El Dorado* (because there is much Gold in it) with a Lake of a vast extent, almost under the Line. Some affirm that there are a kind of monstrous People in that Region, who have no Heads, and have their Eyes in their Shoulders, and their Bellies; but that is only learnt from the report of their Neighbours, who heretofore told it to Sir *Walter Raleigh*, Admiral of an English Fleet under Queen *Elizabeth*. We are not to believe all that we are told, neither are we to deny all that we cannot believe. The truth is, that report of Men without Heads is very strange, and seems contrary to the order of Nature, which is not guilty of so considerable mistakes, as to fail in the production of a whole race of People. Sometimes she produces Monsters, because she meets with bad Dispositions that hinders her Operations; but as if she repented of what she had done, and would disown such imperfect works, she puts a stop to the progress, and suffers them not to propagate and beget others like themselves.

*Brasile* stretches on the North Sea, from the River of *Amazon*es to the Region of *De la Plata*. The People go there Bare Naked, neither sow nor reap, but live on the Natural Fruits of the Earth, which are very plentiful in their Region, and by Hunting and Fishing. They eat the Prisoners they take in War, rather to satiate their Revenge than their Appetite. They have no Prince, no Laws, nor Religion; and they believed not that there was a God, until they were instructed by the Europeans, with whom they conversed.

The Portuguese, English, and Hollanders, have had Plantations there, and sometimes War for their Titles. In that Country are the Towns of *St. Salvador* or *Nave*, on the famous Bay of *Todos los Santos*, *Pernambuco*, *Rio Janeiro*; and several others. But let us not leave this fair Country without viewing the most pleasant and biggest River of the World, that watereth it: It is called the River of *Amazon*, because some Women that carrying Arms and Fighting, were observed upon the Banks thereof. It is a River called *Orghane*, from a Spanish Captain that sailed long upon it. It springs from the Mountains of *Peru*, and carries its Streams through that Country into *Brasile*; where after a course of Six hundred Leagues long, it pays the Sea the largest tribute that it any where receives. Its Mouth, in the opinion of some, is Four score Leagues over; and just under the Line it mingles with the North Sea.

The Region *De la Plata* is to the South of *Brasile*, and on the North Sea; it is refreshed by a River that gives it both its Name and Water. The Portuguese have called it *Rio de la Plata*, that is, the Silver River; because Silver is found amongst the Sands it brings with it. On the side of it is the City of *Assumption*; the others are *St. Fey* and the *Vistation*.

The Country of *Chica*, and that of *Paragons*, which borders on the Straights



Streights of *Magellan*, are to the South beyond *La Plata*, Here are no Towns, some Capes and famous Ports, is the Port *Drye*, and the Cape *De las Virgines*. It is true, that on the Streights are to be seen the Ruin of a Town called *Philippa*, built by the Spaniards, where they were almost all starved.

The most remarkable thing in this Region, is the People that inhabit it, and are called *Patagians*; they have been reported to be Ten or Twelve foot high, and to swallow down a Pistol or a Stone, with as much ease as an ordinary Man one Glass. They cover themselves with Beasts Skins, and carry Clubs, Bows and Arrows. They lay their Dead upon little Hills, and cover them with heaps of Stones, lest Beasts should devour them. It hath not been observed that they have any Laws or Religion. In a word, they are Barbarians, and for Strength and Bulk of Body, some what exceed our European. Our latest Discoveries will not permit them to be Glorious.

Having passed the Streights, we were called after *Magellan's* Name who discovered it, and have been in the Ocean thenceby; we find on the South Sea Cape *Drye*, and extending from South to North, *Chili* and *Peru*.

The Country *Chili* hath these chief Towns, *St. Jago*, *El Imperial*, *La Concepcion*, and *Valdivia*.

*Peru* is to the North of *Chili*, and reaches Five hundred Leagues from South to North; it lies to the West the South Sea, to the East the high Hills, which the Spaniards call *Las Cordilleras*, or the *Andes*, perpetually covered with Snow, in the midst of the *Torrid Zone*. When *Pizarro* and *Almagro* arrived in that Country, in the year One thousand five hundred and twenty four, it was subject to the Princes named *Incas*, who had settled a powerful Empire in those Places, extending above Fifteen hundred League in circuit; they had governed there above Six hundred years, when the Avarice and Ambition of those two Spaniards promoted them to dethrone the last that swayed that Scepter; his Name was *Atabalipa*, or *Atabalipa*, whom they took and caused to be strangled. Here they found a prodigious quantity of Gold. The Inhabitants were Polite and Civil, they worshipped the Sun, and believed there was another God Superior to him, whom they called *Pachacamac*. The City of *Cusco* was the Imperial Seat of the *Incas*. The second in Dignity was *Quito*, situated almost under the Equinoctial; both which remain still. The Spaniards have built many there, the most considerable of which is *Lima* on the Sea side, with a Port. This is the Residence of a Viceroy and Archbishop. The other chief Towns are *Arica*, *Arequipa*, *St. Augustin*, on the Sea, and in the Inland *Potosi*, near the famous Mountain of the same Name, wherein are inexhaustible Mines of Gold and Silver; *La Plata*, so called for its Silver Mines, *San Juan del Oro*, and some others.



The Original Natives of this Kingdom, have for the most part been extirpated by their Conquerors; and those that were not, were converted to the Catholick Faith: so that there are several of them Suffragant Bishops to the Archbishop of Lima.

The Countrey of Cinnamon lies betwixt Peru and Guiana; it was so called, by reason that there were Trees found there, whose Bark had a great affinity to the true Cinnamon. There are no Towns nor Villages observed there.

Tucuman is between Chili and the Region De la Plata, and hath St. Jago del Efforo for its chief Town.

We must now see what are the Mountains, Capes, Rivers, and Streights of this New World.

Its chief Mountains are the *Andes*, or *Las Cordilleras*, which lie to the East of Peru. The *Incas* caused ways to be cut out in them, which surpassed all that the Roman Grandure ever could do. They filled up deep Valleys, and cut through high Rocks; the remains of which prodigious Works are still to be seen.

In Mexico the Mount *Popocatepete* continually casts out Flames. The most famous Capes, are Cape Breton, Cape Florida, the North Cape, and that of St. Augustin.

Its greatest Rivers are that of St. Lawrence in Canada, of the Holy Ghost in Florida, *Oranoka*, *Maragnon*, the River of *Amazones*, and *Rio de la Plata*, in South America; all which run into the North Sea; no considerable Rivers fall into the South Sea.

The most noted Streights are towards the North, those of *Davies* and *Hudson*; towards the South the Streights of *Magellan*, *Le Maire* and *Brouwers*, of which we shall speak, after that we have considered the Islands that lie about this Continent.

## CHAP. IV.

### The Isles of AMERICA.

WE shall in the first place view the Isles of the North Sea, which are the most considerable; for there are but very few in the South Sea, and we shall proceed from North to South.

*New-Foundland* is an Island near the Bay of St. Lawrence and Land of Canada; upon the Banks of which there is a great Cod-fishing.

The



The Isles of *Assumption* is in the Bay of *St. Lawrence*, and the *Sandy Island*, to the South of *Newfoundland*.

The *Bermudas* are in the middle of the Ocean, and the *Bahaman* Islands to the East of *Florida*.

*Cuba* lies to the South of them, and upon the Mouth of the Bay of *Mexico*; it is above Two hundred Leagues in length, and about Three score in breadth: *St. Jago* is its chief City, and an Episcopal Seat. Next to that is the *Havana*, where the Spanish Flota Rendezvoutze, and meets on their return homeward from *America*: it lies on the West of the Island, and almost opposite to Cape *Florida*.

*Hispaniola*, called likewise *St. Domingo*, and by the Natives *Haiti*, is about Three hundred Leagues in circumference, and lies Eastward from *Cuba*. The Capital City, which gives it the Name, is *St. Domingo*; the Residence of a Viceroy, and Seat of an Archbishop. The object of Avarice is found there, I mean Gold and Silver Mines. The Spaniards have depopled these two Islands and banished the Natives, as they did from most of the others.

*Jamaica* lies South from *Cuba*, and belongs to *England*; the Two chief Towns of it are *St. Jago de la Vega*, otherway called the *Spanish Town*, by whom it was built, and *Port Royal*, or the *Point*, built by the English, and an excellent Harbour; the Governour of the Island resides in the former. It is rich and in a flourishing condition.

*St. John de Portorico* is to the East of *Hispaniola*; its chief Town, which is that of *St. John*, has an excellent Harbour. This Island was formerly called *Boriquen*.

The *Caribbe* Islands are to the East of the former, and, as it were, at the Mouth of the Gulph of *Mexico*, which they seem to shut; they lie ranked in form of a Crescent, and reach from North to South. The most remarkable of them are *Barbadoes*, *St. Christopher*, *Gradalupe*, *Dominico*, *Martinico*, *Antego*, *Grenada*, and the *Trinity*. The English, Dutch, and French, possess most part of them.

*Margareta* lies somewhat more Westward; and the Fishing of Pearls, which gave it its name, renders it famous.

The Natives of these Islands, as in many places of the main Land, were Man Eaters or Canibals, but at present the greatest part of them are destroyed, or forced to seek some other way of living.

The Isle of *Cayenne* is near the main Land, upon the Coast of *Guaiana*, an Island made by the Mouth of a River called also *Cayenne*. The French had settled there and printed Relations of it, but in the late Wars the Hollanders dispossessed them, and have planted a Colony of their own. The Isle of *Maranbaon*, is also at the Mouth of a River that likewise carries the same name.

The South Sea has very few Islands near to *America*, these are only found there:

*Mocha*



*Mocha*, on the Coast of *Chily*, is an Island of some consideration. *California* hath been long taken for a Continent, but it is at length found to be an Island supposed to be divided from the Land of *Feslo*, by the Straits of *Anien*, and from *New Granada*, by a pretty large Channel, which is called the Vermilian Sea.

The Isles of *St. Thomas*, *Nublada*, and *Recapartida*, are to the South of *California*.

The Isles of *Salomon* are in the middle of the South Sea, towards the Coasts of *New Guinea*.

And now you have, Reader, what we thought fit to speak of this New World. When it was discovered, the Inhabitants were either plunged in Idolatry or void of all Religion. Of this kind were the People of *Erasle*. Those of *Mexico* worshiped Idols, and Sacrificed Men unto them; they plucked out the Hearts of those wretched Victims, and threw them at the Feet of their Gods, made of Gold and Silver.

The People of *Peru* were more moderate in their Worship, their Sacrifices were not so cruel; they chose for their God the most Glorious of all the Lights of Heaven, but they believed him not the Almighty, for they assigned a Father and Sovereign to him, as well as to all other created Beings, and called him as we have already said, *Pachacamac*. But it is strange, that in all this vast Continent there was no trace of Christianity to be found; all of them were ignorant of that, yea, and of a matter of far less importance, though of great use, I mean of writing. They could not conceive how a piece of Paper could convey the words and thoughts of People at a great distance from one another. We may affirm that these Countreys are every way far distant from ours. The Beasts, Plants, Flowers and Fruits, are quite different from what are amongst us; and the People of *Europe* imparted theirs to them, with the Religion that they profess.

## CHAPTER V.

### The TERRA AUSTRALIS.

When *Magellan* passed the famous Streights that is called by his Name, on his left hand to the South, he observed a Land that shone with multitudes of Fires, and therefore he called it *Terra del Fuego*. He took it for a Part of the *Terra Australis*; but *Le Maire* having discovered another Streight in the year 1616, which carries his Name also, perceived that that Land of Fire was but an Island,

and



and observed another on his left hand, that he named, *Statenland*, which in his Language signifies, the Countrey of the *States Brouwers*, who found another Streight more Southward than that of *Le Maire*, in the year One thousand six hundred and forty three, hath discovered the Countrey of the States to be likewise an Island.

Betwixt the 30 and 40 degrees of South Latitude, and the 210 and 220 of Longitude, some late Maps mark a Countrey which they call *New Zealand*, discovered in the year One thousand six hundred and fifty four.

Under the same Latitude, but between the 160 and 170 degrees of Longitude, they mark another Land, discovered in the year One thousand six hundred and fourty two, called *Antony van Diemanland*: Under the same Longitude, and the Tropick of *Capricorn*, they place a Countrey called, *New-Holland*, discovered in the year One thousand six hundred and forty four.

*New Guinea* is near the *Molucca's*, but it is believed to be an Island, and it is not certain whether the Lands we have just now named, be Isles or parts of the Continent.

To the South of the Cape of *Good Hope*, it is supposed that there is Land, and some have called it the *Land of Parrets*. They talk of some Kingdoms there, but all the knowledge we have of those Countreys is very uncertain; for no progress has been made into them: some small Touches of the Coast have only been discovered. Time and Industry may possibly afford us greater Discoveries.



CHAP. VI.

The Land near the ARCTICK  
or NORTH POLE.

ABOUT this Pole are *Greenland*, *Nova Zembla*, and *Spitzberge*, with some other Countreys, of which we know very little. It is certain that some have failed within Eight degrees of the Pole; and it is affirmed that the *Hollanders* have been under the very Pole: but with what truth I shall not adventure to say. It is thought by some, That about that place, *America* is joyned to the

Con-



Continent, either on the side of *Asia*, or of that of *Europe*; but nothing of it is yet certain.

It is to be observed that *America* reaches North, to the 70 degree or farther, and South to the 52 or 53 degree of Latitude: so that it lies partly in the Torrid Zone, partly in the North and South temperate Zones, and partly in the Northern Frozen Zone.

Thus, Reader, I have given you a short and as exact Description of the Earth, as I could, and have said nothing but what I thought true.

The little knowledge that we have of the Inland parts of these quarters of the World, together with the uncertainty of the Relations of different Travellers, made me unwilling to impose upon you for truth, those things that I was not well satisfied in my self; which has rendred this Treatise possibly, more short than the Vast tract of Land it pretends to describe, may seem to require.

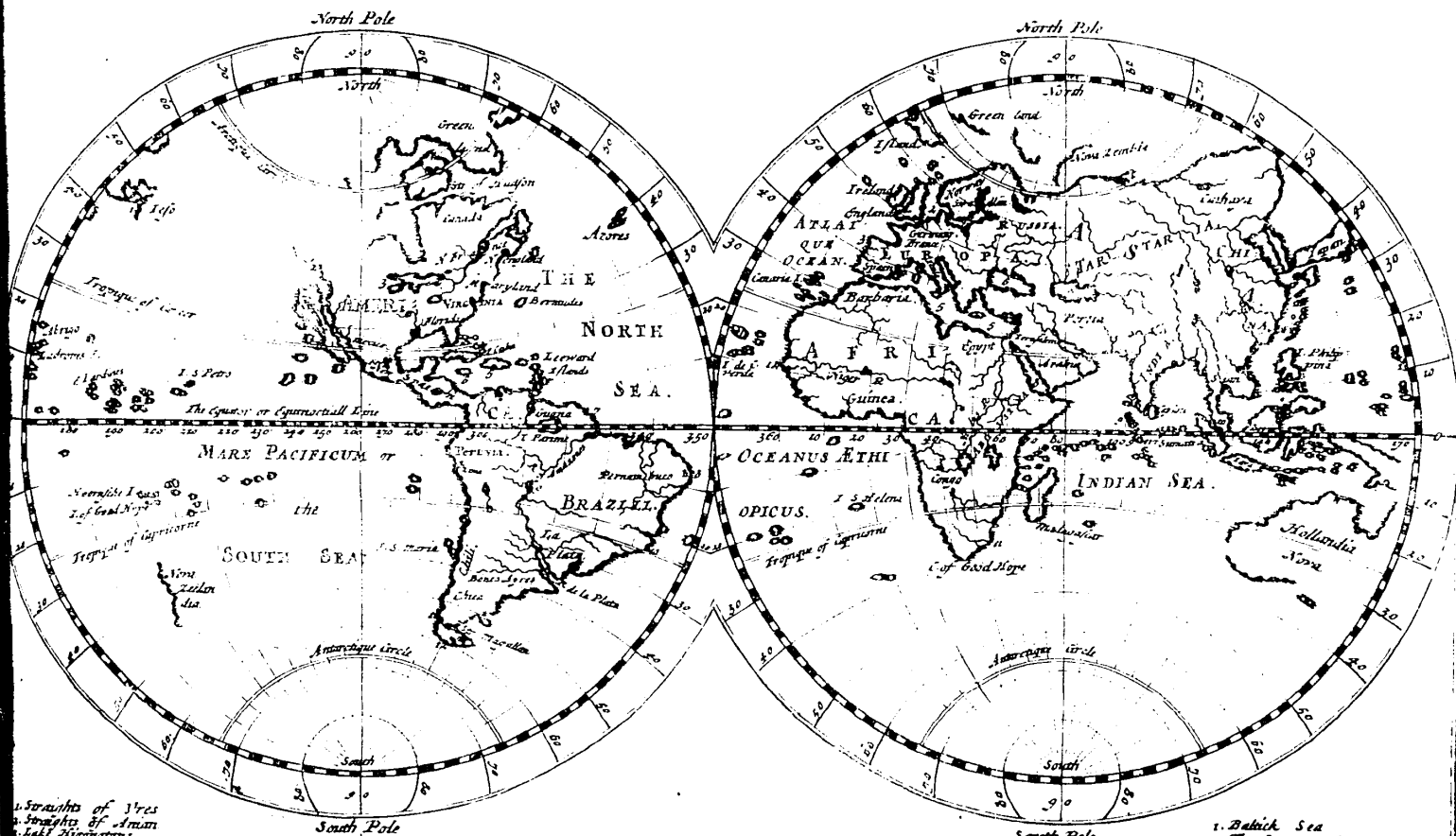
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F I N I S.

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# THE WORLD IN PLANISPHERE.



1. Straights of Vres
2. Straights of Anam
3. Lake Michigan
4. Straights of Bahama
5. Isle of Hispaniola
6. Isle of Jamaica
7. Isle of Cayana
8. Isle of St. Augustin
9. Lake of Nicaragua
10. C. Fern
11. Victoria
12. C. Horn

1. Baltic Sea
2. The German Ocean
3. Cape Finisterre
4. The Straights of Gibraltar
5. The Mediterranean Sea
6. The Black Sea or Pontus Euxinus
7. The Caspian Sea
8. The Red Sea
9. Malabar Islands
10. Malacca
11. Cape Corrientes
12. Cape Verde

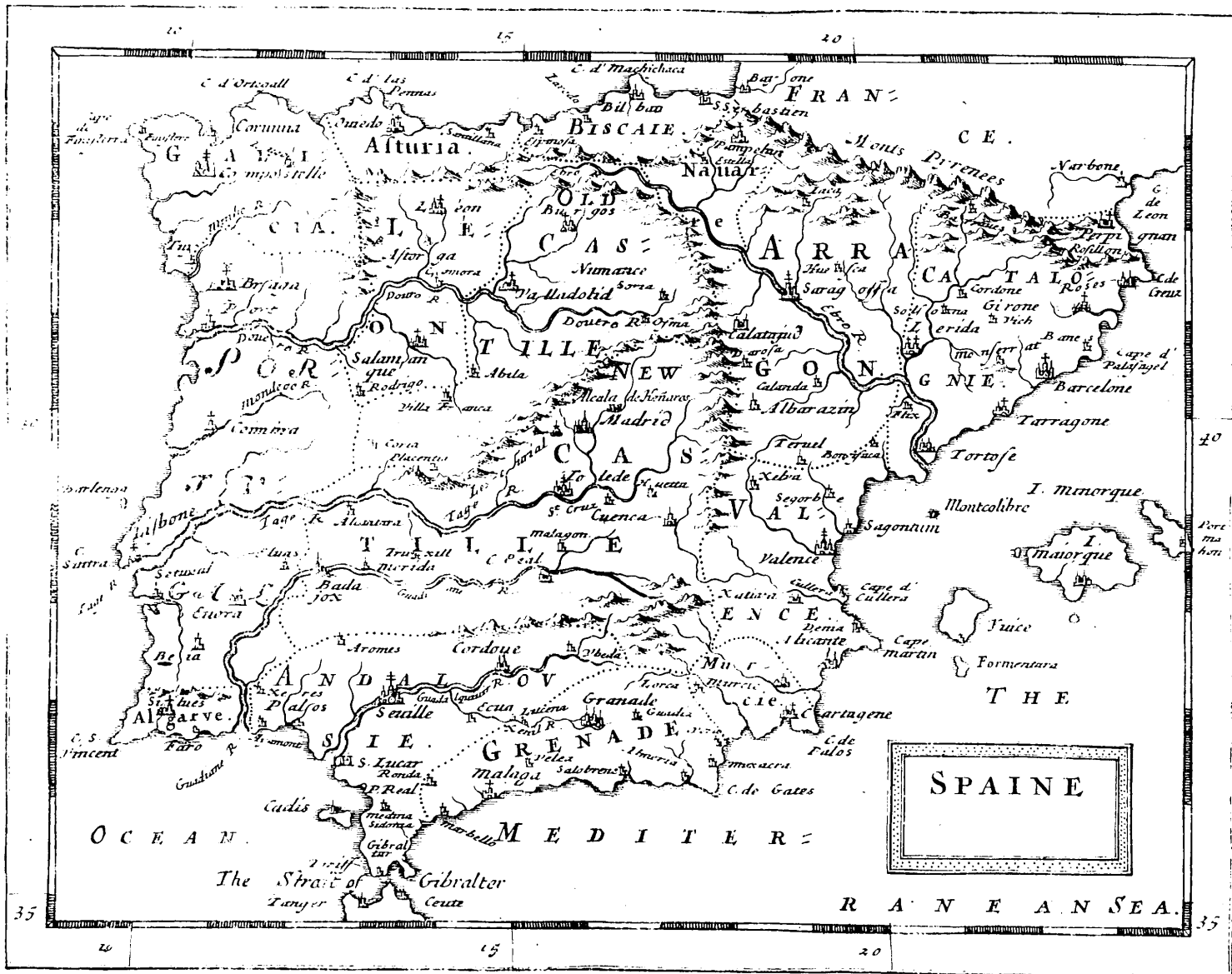
























ITALIE.

Leagues

10 20 30 40

MARE MEDITERRANEUM.

SARDINIA

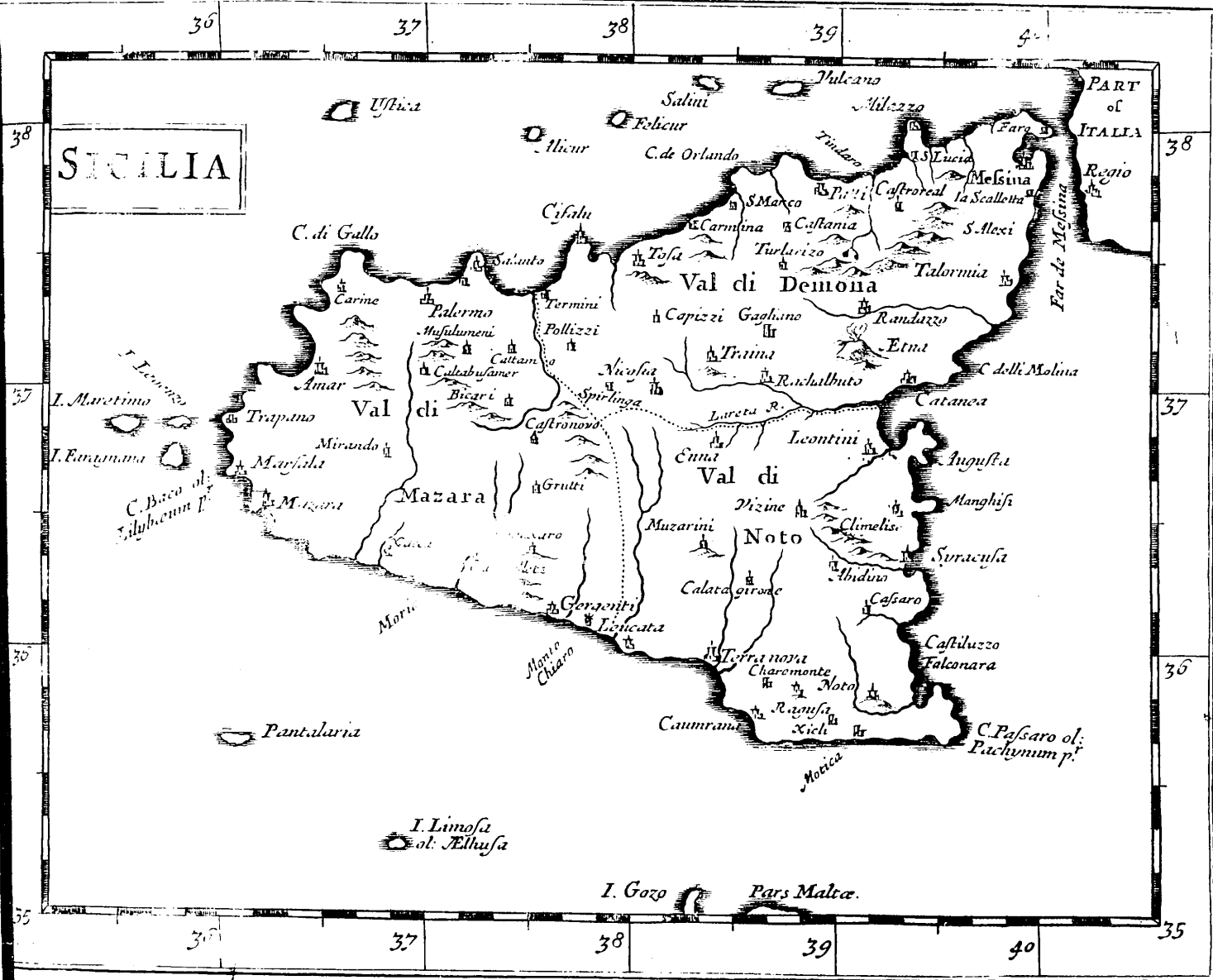
Isles de Ligaria

RA NE UM.

Sardinia

Isles de Ligaria











**HOLLAND**  
Or the United  
PROVINCES.

M A R E

GERMA

NICUM.

SOUTH  
SEA.

D. DE  
Vellow.  
GVELDRES.

G E R  
M A N Y.

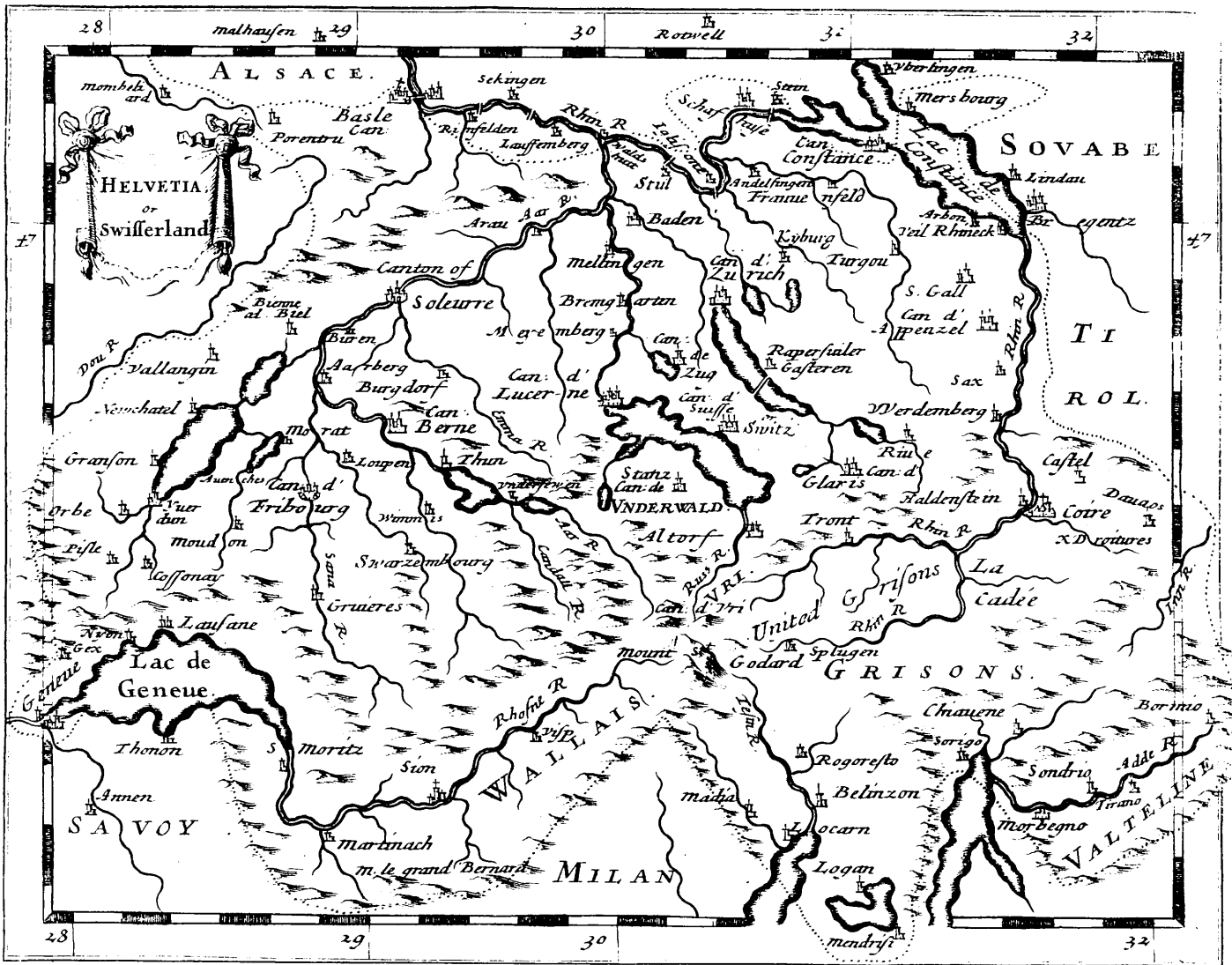
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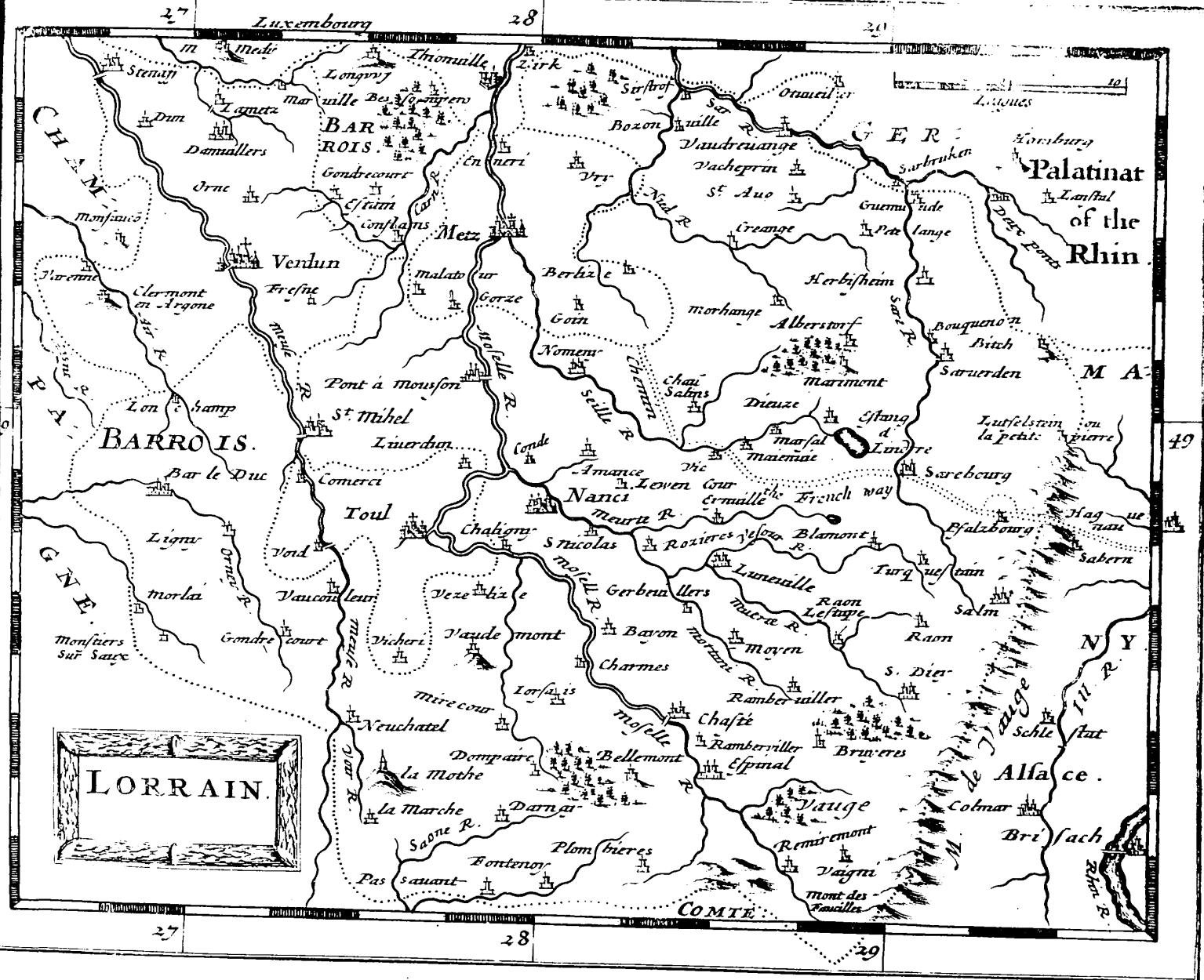












27 Luxembourg 28 29

10  
Lignes

Palatinat  
of the  
Rhin

BARROIS.

LORRAIN.

M A

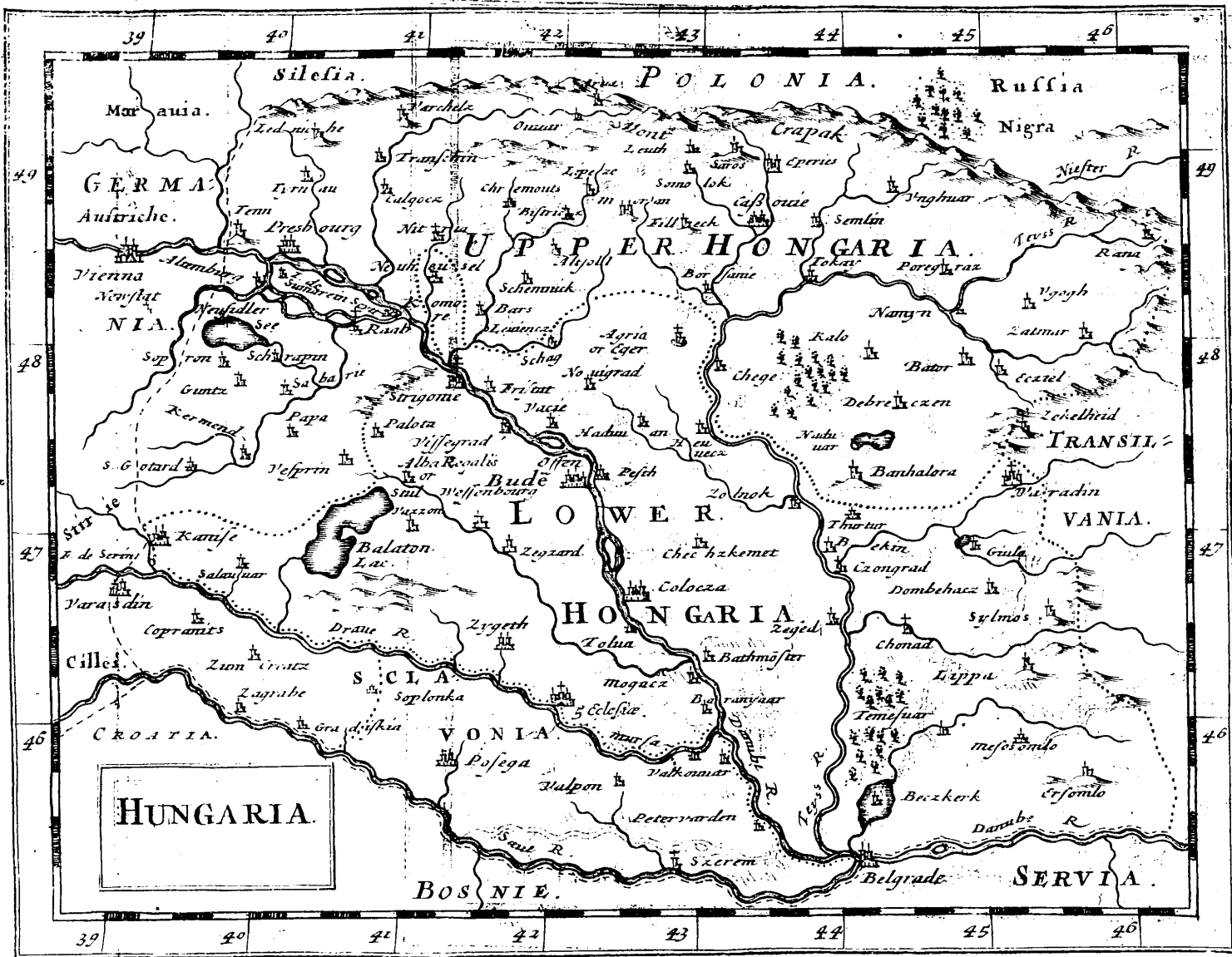
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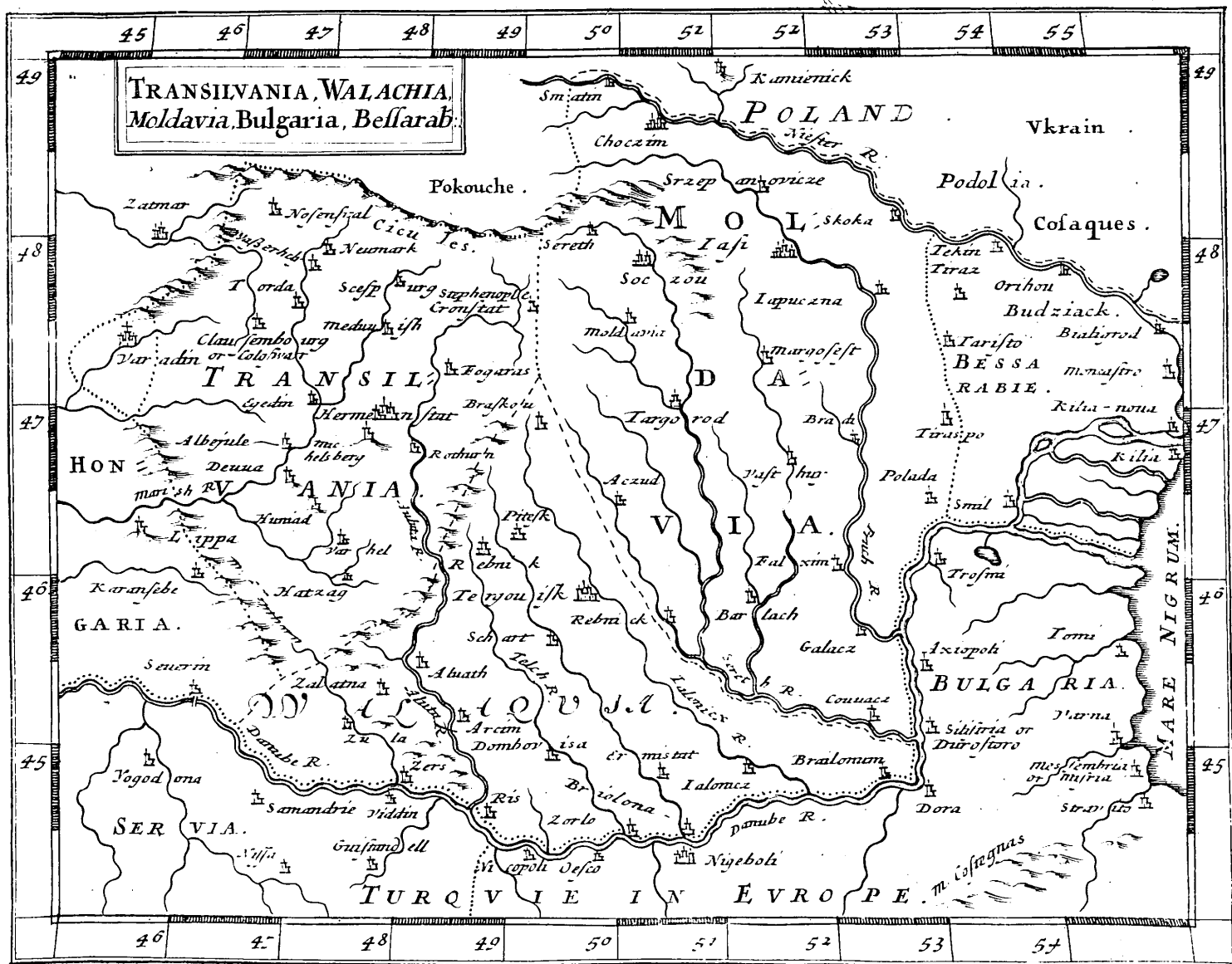
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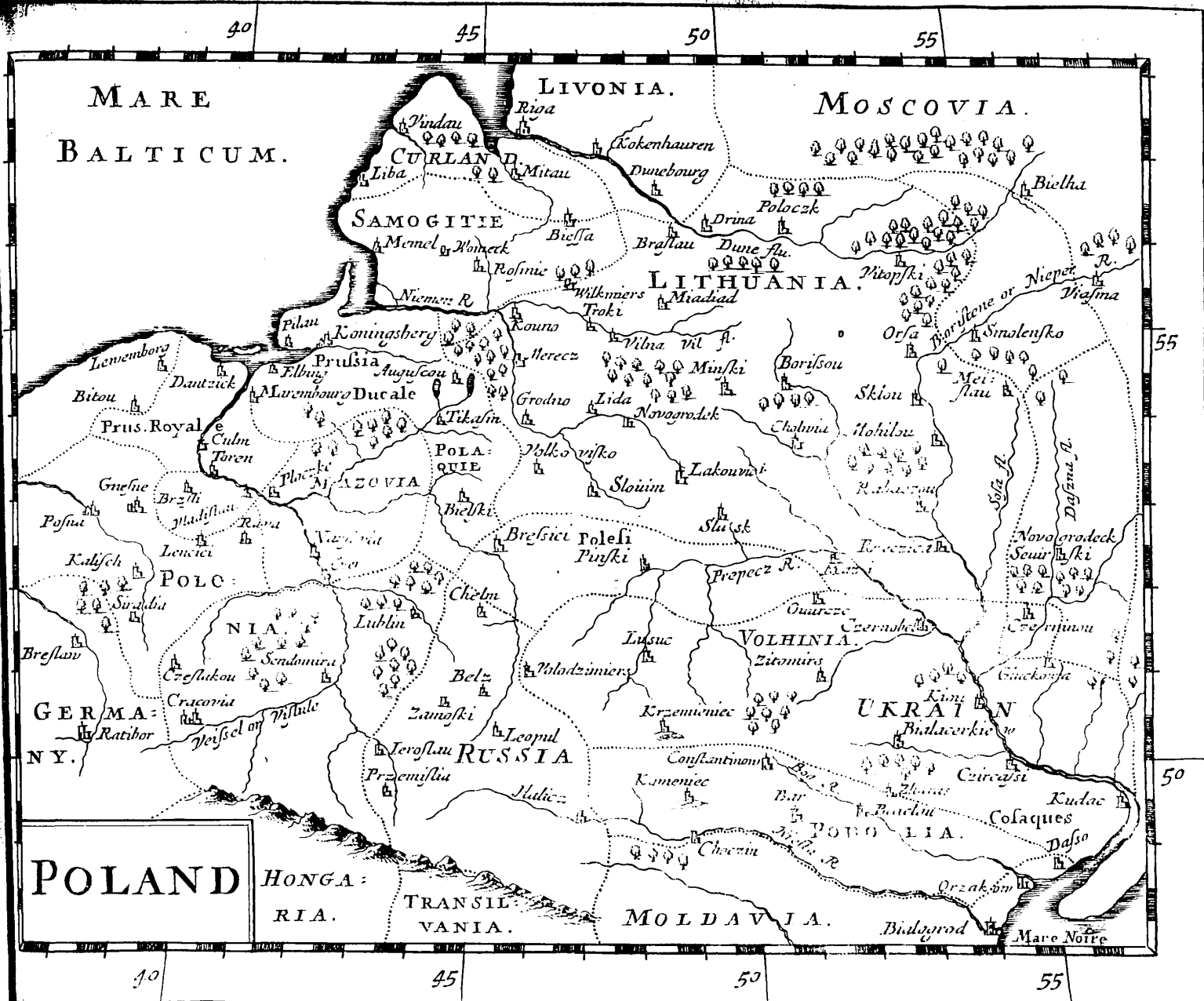












POLAND

HONGA-  
RIA.

TRANSIL-  
VANIA.

MOLDAVIA.

Budagrod

Mare Noire







ENGLAND, SCOTLAND,  
& IRELAND, with the ILES.  
Thereto Belonging.

Leaguas  
10 20 30 40 50 60







THE  
IRISH  
SEA.

THE ENGLISH CHANNEL



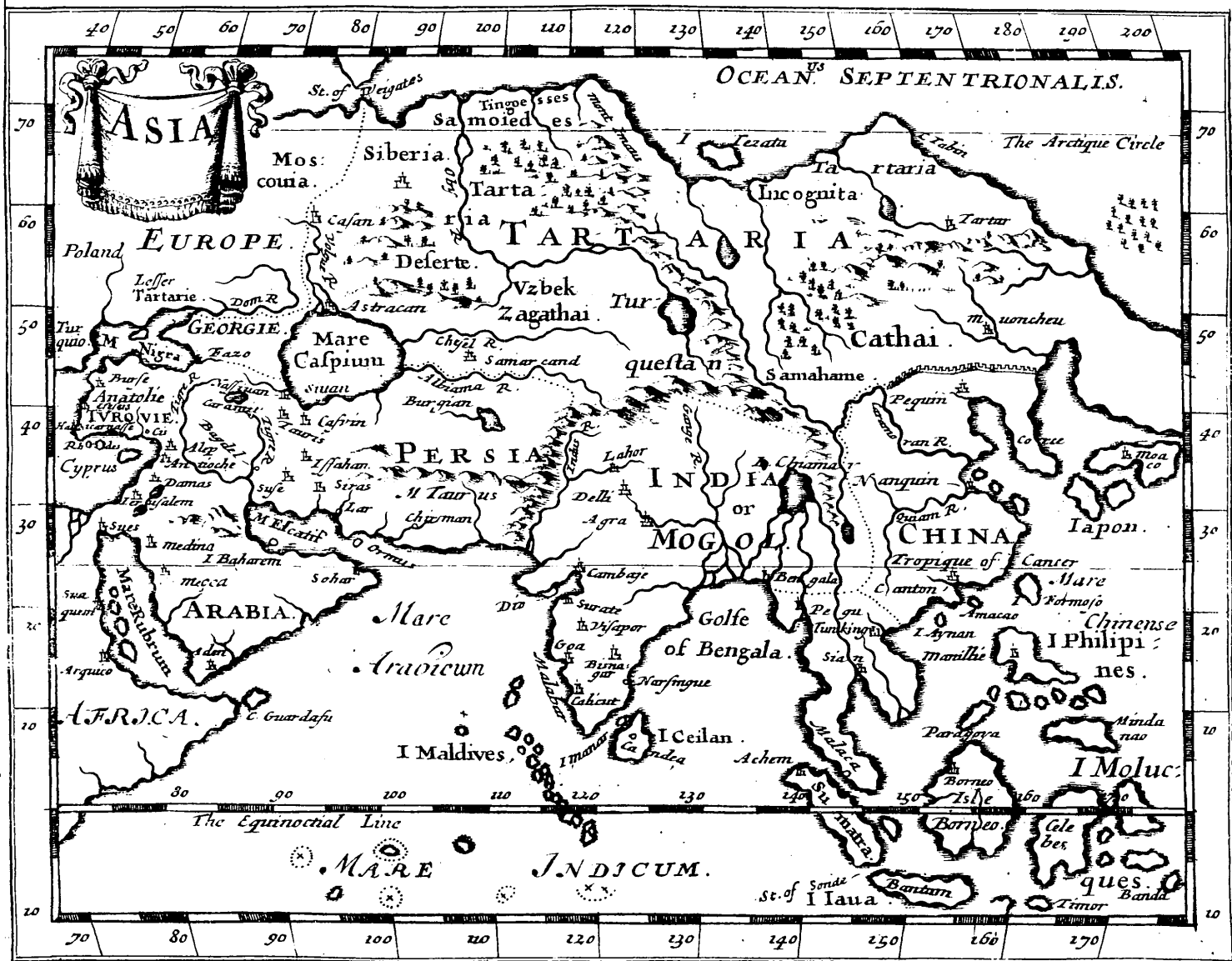




# IRELAND



















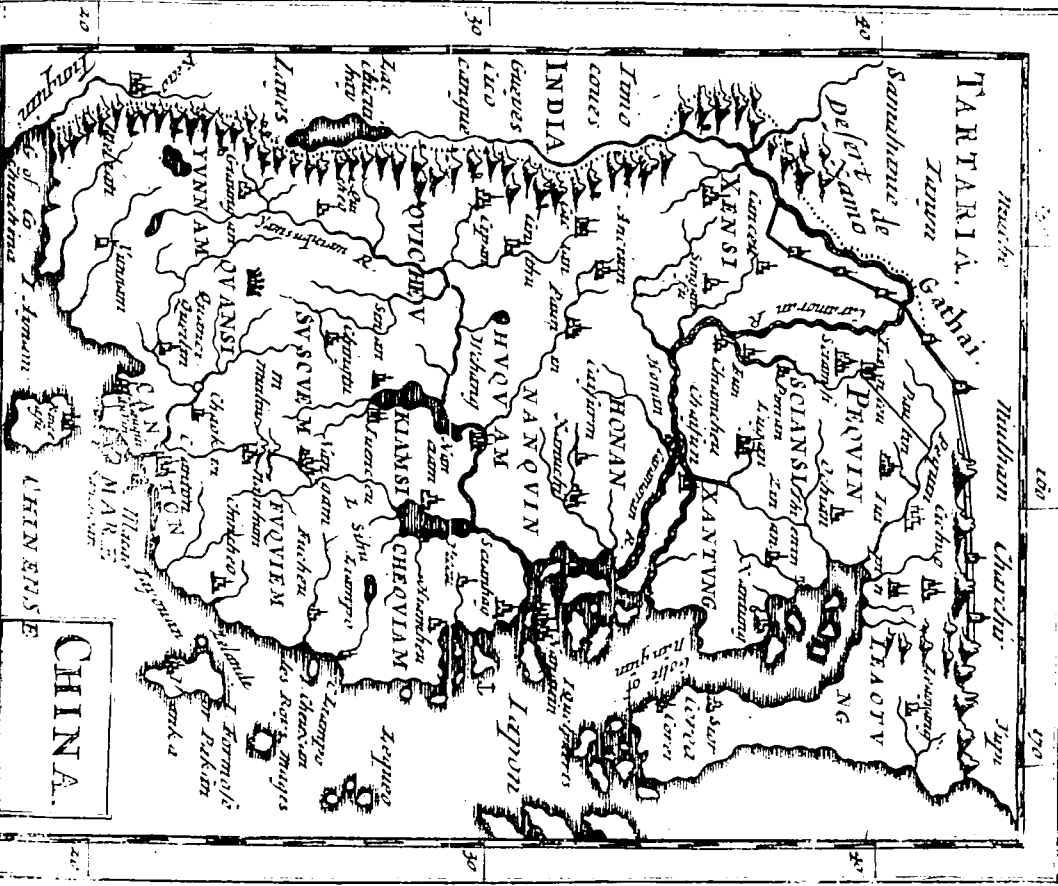










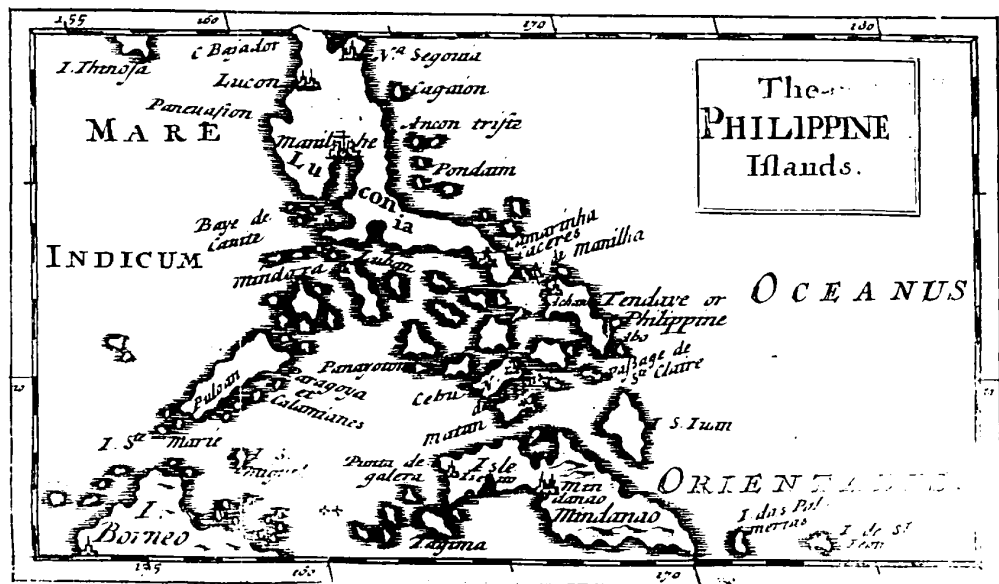


CHINA.





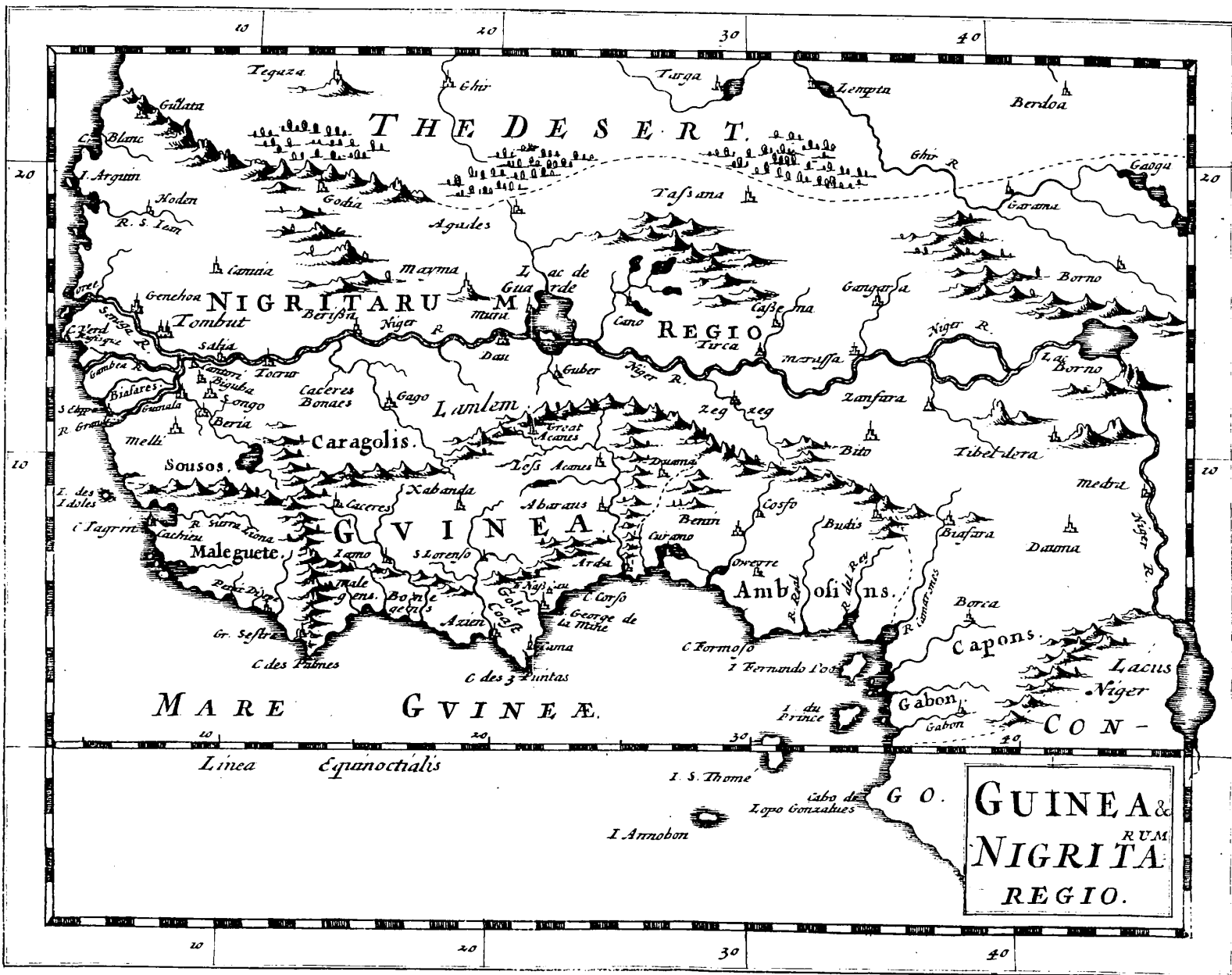








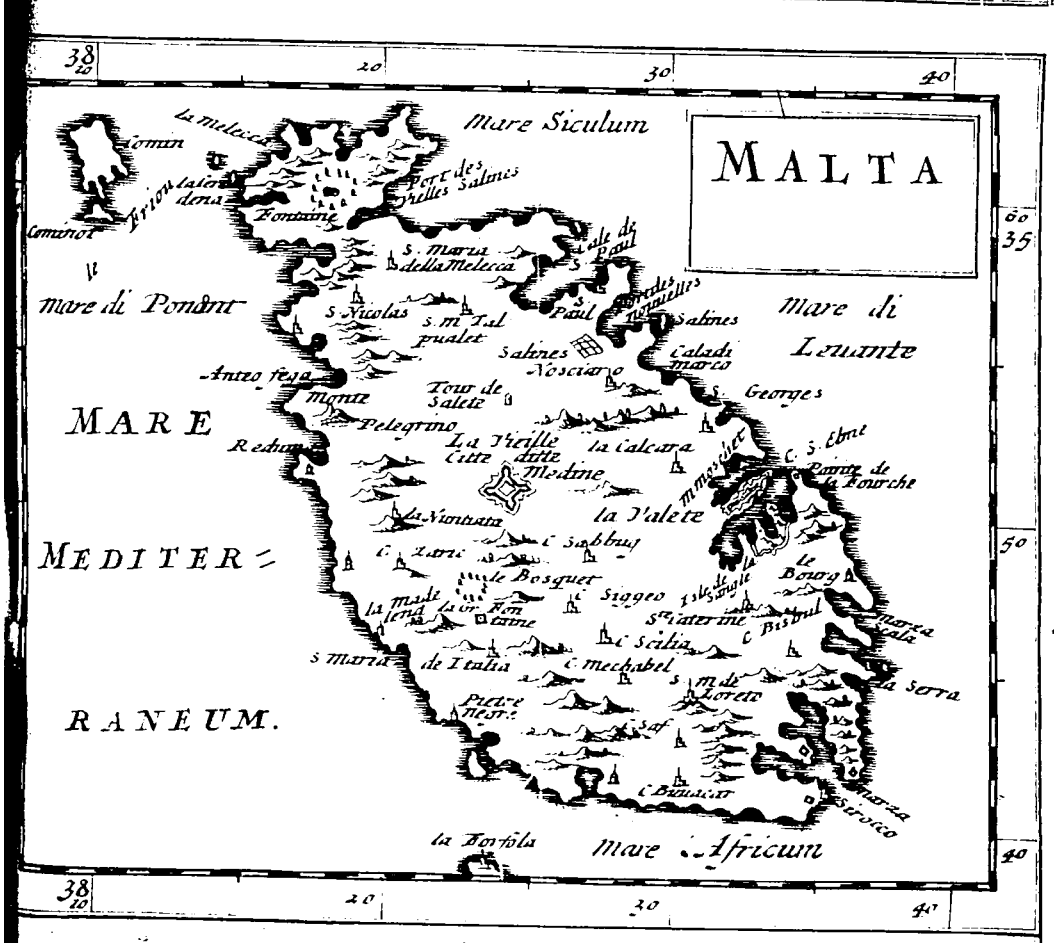
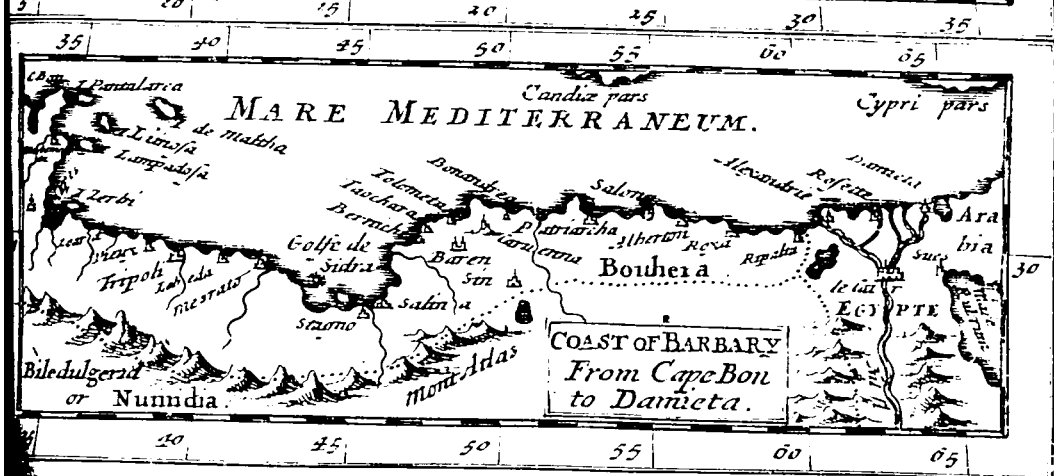
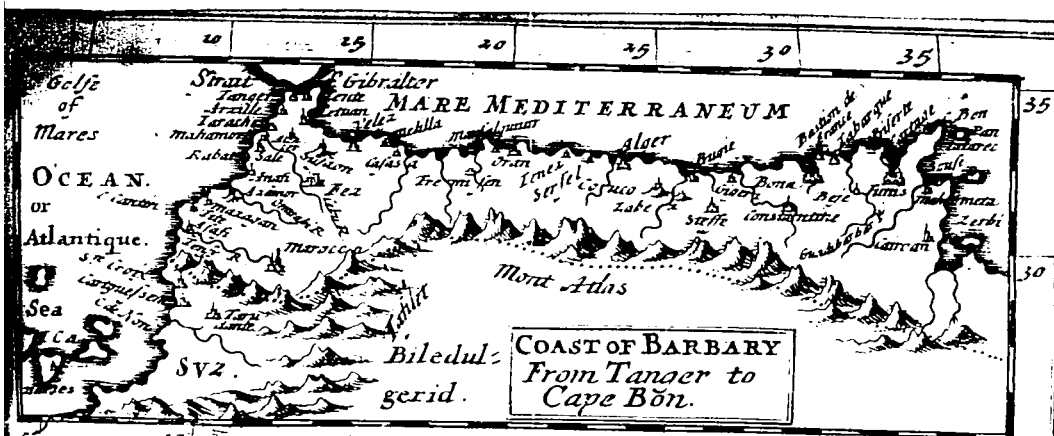






















ZANGUEBAR

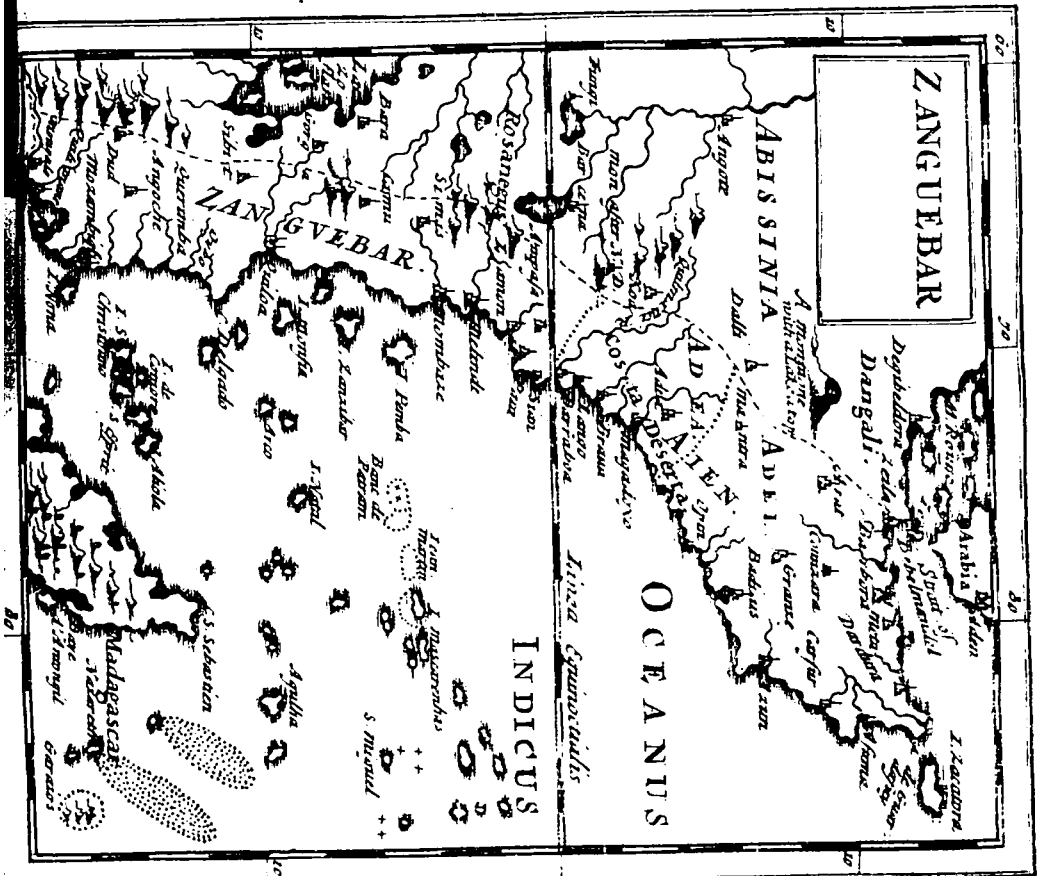
A magnificent  
with a Lak. & top  
I.A  
Dalt. A. m. d.

# OCEANUS

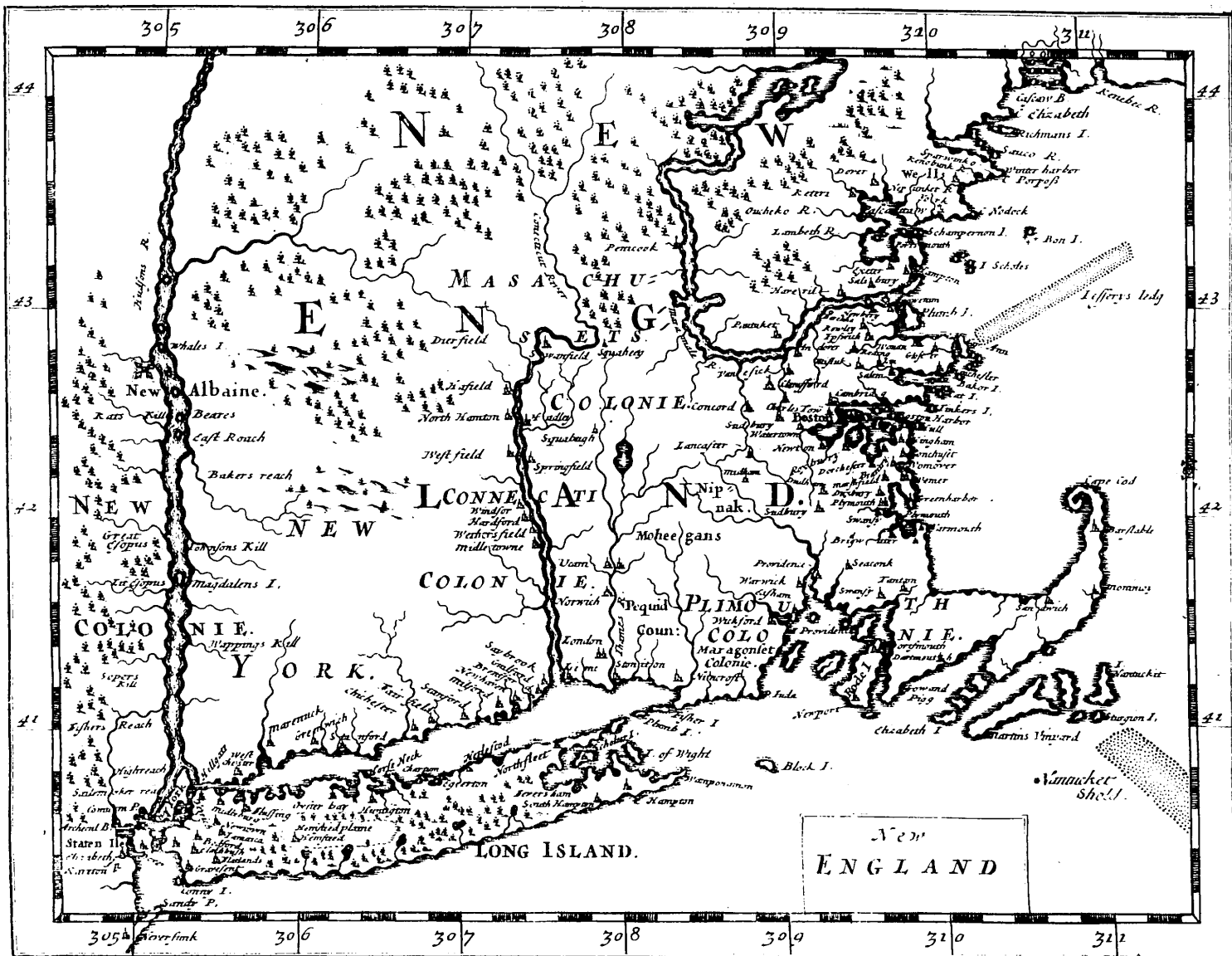
*Tringa squamulalis*

# INDICUS

Madagascar



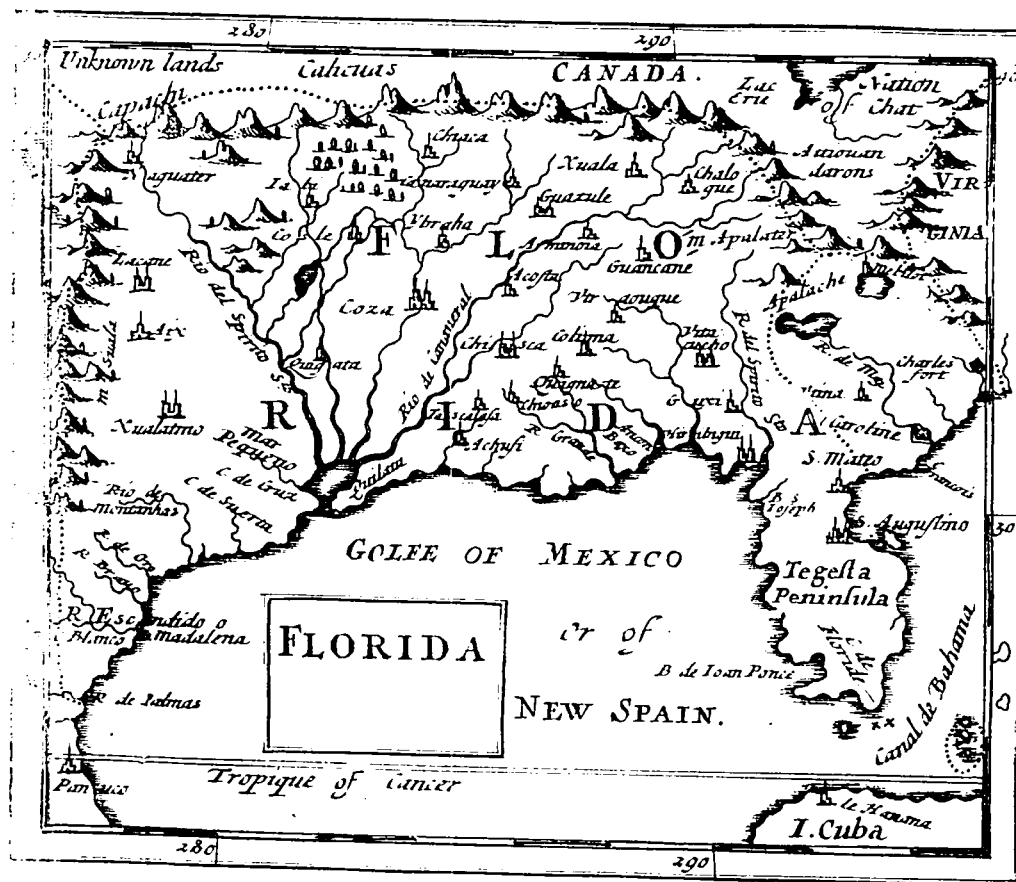
















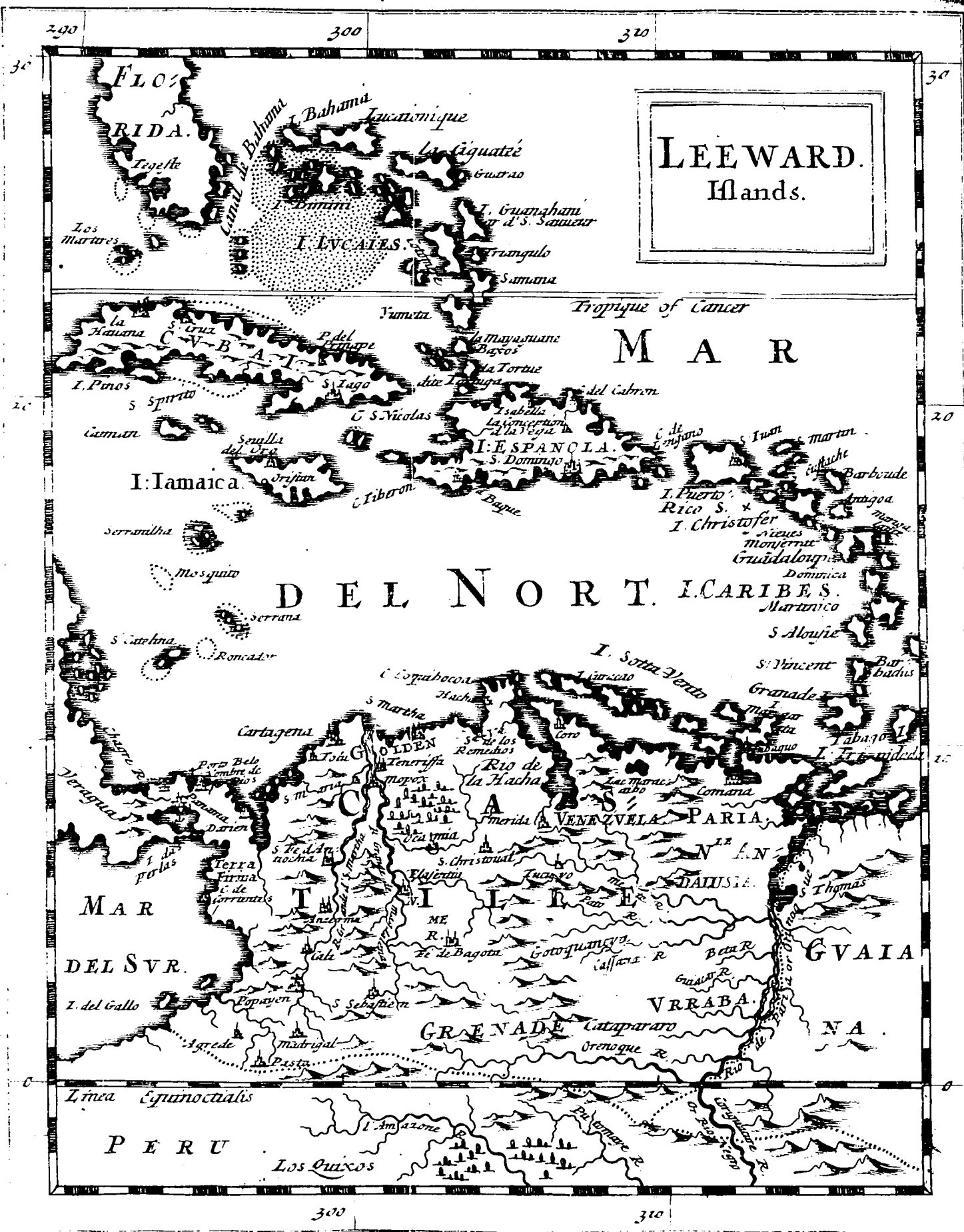














# NORTH

# POLE

